# Vertical Mergers with Input Substitution: Double Marginalization, Foreclosure and Welfare

# Serge Moresi\* and Marius Schwartz\*\*

Georgetown University, Department of Economics, Working Paper

March 12, 2021

# Abstract

We consider differentiated duopolists that face symmetric linear demands and produce using identical or different Cobb-Douglas technologies with a monopolized input and a competitively supplied input. A merger between the input monopolist and either firm eliminates double marginalization but—unlike with fixed-proportions technologies in the same setting—can lead to foreclosure and reduce consumer welfare and total welfare. The same can occur under a CES technology with greater input substitutability than Cobb-Douglas. When firms use identical Cobb-Douglas technologies, the merged firm raises the rival's cost by more, and the welfare effects are worse, when the input it controls constitutes a low rather than high share of downstream input costs. If that share is sufficiently low then consumer welfare and total welfare decline, while rising elsewhere despite foreclosure. With different Cobb-Douglas technologies, the input monopolist may foreclose completely either firm pre-merger. A merger's welfare effects then can be non-monotonic in the monopoly input's share of costs.

JEL Classification: L4, L41, L42

Keywords: Vertical Mergers, Foreclosure, Input Substitution, Antitrust

<sup>\*</sup> Charles River Associates, Inc., Washington DC 2004 <smoresi@crai.com>.

<sup>\*\*</sup> Department of Economics, Georgetown University, Washington DC 20057 <mariusschwartz@mac.com>. We thank Martino De Stefano, Michael Katz, David Kovo, Federico Mini, John Rust, and Steve Salop for helpful input. Any errors are ours alone.

#### 1. Introduction

Vertical mergers combine firms or assets at different stages of the supply chain, such as an upstream input supplier and a downstream output producer. Unlike horizontal mergers, the parties to a vertical merger are not competitors but instead engage in complementary economic activities. Examples of prominent vertical mergers include Comcast/NBCU (2011), AT&T/Time Warner (2018), and CVS/Aetna (2019).<sup>1</sup> Competition policy recognizes that vertical mergers can generate efficiencies, by alleviating transaction costs between the parties or reducing pricing distortions. In the familiar case of successive monopoly—e.g., a monopolist manufacturer selling to a monopolist distributor under linear pricing—vertical integration benefits the merging firms and consumers by expanding output (Spengler, 1950) due to elimination of double marginalization (EDM).<sup>2</sup> This successive monopoly scenario underlies common perceptions that vertical mergers are beneficial.

However, when one of the merging parties commands substantial market power and initially transacts with rivals of its merger partner a major competitive concern is foreclosure. The merged firm may worsen the access terms to its assets for rivals compared to the terms that rivals would enjoy absent the merger, and thereby harm competition either "upstream" (via *customer foreclosure*).<sup>3</sup>

To sharpen the contrast with the beneficial scenario, consider an alternative hypothetical where firms 1 and 2 produce differentiated substitutes goods using different technologies, and only firm 2 utilizes an input sold by a monopolist supplier, firm S. A merger of firm S with firm 1 yields no EDM.<sup>4</sup> Instead, the merger generates two anti-competitive pricing incentives for the merged firm M. One is the familiar foreclosure or *raising rivals' costs* (RRC) *incentive*: raise the input price to firm 2 in order to induce a price rise for good 2, which increases profits from firm M's sales of good 1. Another is the *Chen incentive*: raise the price of good 1 to increase sales of good 2, hence firm M's

<sup>&</sup>lt;sup>1</sup> See, e.g., Rogerson (2014); Memorandum Opinion of Judge Richard J. Leon in *United States v. AT&T and Time Warner*, June 12, 2018, at <u>https://ecf.dcd.uscourts.gov/cgi-bin/show\_public\_doc?2017cv2511-146</u>; and Memorandum Opinion of Judge Richard J. Leon in *United States v. CVS and Aetna*, September 4, 2019, at <u>https://ecf.dcd.uscourts.gov/cgi-bin/show\_public\_doc?2018cv2340-135</u>.

<sup>&</sup>lt;sup>2</sup> EDM refers to the incentive of the merged firm to reduce its output price because it obtains the input internally at cost.

<sup>&</sup>lt;sup>3</sup> See, e.g., supra note 1, and section 4 of the *Vertical Merger Guidelines* issued by the U.S. Department of Justice and Federal Trade Commission, June 30, 2020 (hereafter, "VMG").

<sup>&</sup>lt;sup>4</sup> The VMG call such a merger "diagonal" as it combines "firms or assets at different stages of competing supply chains" (VMG, p.1; see also Example 7).

profitable input sales to firm 2, a gain that was ignored by the independent firm 1.<sup>5</sup> Although the merging firms operate at different stages of the economic value chain, in this scenario the merger is more accurately characterized as purely horizontal as judged by the incentives it creates. RRC is akin to forcing firm 2 to join in downstream collusion. The Chen incentive is akin to firm 1 acquiring a partial ownership interest in its rival, because firm 1 now shares in firm 2's gross profits via input sales to firm 2 by firm 1's merger partner.<sup>6</sup> Both incentives push downstream prices higher.

Vertical mergers that draw antitrust scrutiny typically lie between the above polar cases: the merging supplier initially sells both to its downstream merger partner and to the partner's rival(s). Thus, a 'vertical' merger in oligopoly is best characterized as both vertical and horizontal, exhibiting all three incentives: RRC, EDM and Chen.<sup>7</sup> These three incentives, which can interact in complex ways, jointly determine the post-merger equilibrium values of the relevant variables. This paper addresses the welfare effects of such vertical mergers when downstream firms can substitute (imperfectly) away from the input available only from the merging supplier.

We consider an input monopolist (firm S) that may supply to two downstream producers (firms 1 and 2) of differentiated substitute goods. In our main model both producers use constant-returns Cobb-Douglas technologies with two inputs: the monopoly input X and a competitively supplied input whose price is given. The parameter  $\alpha_i$  is the elasticity of firm *i*'s output with respect to input X. Firm S merges with firm 1. The model nests the two polar cases when input X is needed (i) only by the merger partner ( $\alpha_1 > 0, \alpha_2 = 0$ ) or (ii) only by the rival ( $\alpha_1 = 0, \alpha_2 > 0$ ), with the other firm utilizing only the competitive input. It also includes the more interesting mixed cases ( $\alpha_1 > 0$  and  $\alpha_1 > 0$ ). For tractability we consider symmetric linear demands for the differentiated goods.

Pre-merger, the monopoly input is sold at linear prices (implying double marginalization) under public offers. These assumptions simplify the analysis and let us focus on the role of input

<sup>&</sup>lt;sup>5</sup> To our knowledge, this incentive was first identified in Chen (2001). It is not mentioned in the VMG but was noted in the draft issued for public comment, January 2020, p.7: "[I]f the merged firm raises its price in the downstream market, downstream rivals may increase their sales, which could increase their demand for inputs from the merged firm's upstream business."

<sup>&</sup>lt;sup>6</sup> Moresi and Salop (2020) use the analogy to partial ownership interests for the purpose of quantifying the increase in "effective concentration" from vertical mergers that raise input foreclosure concerns.

<sup>&</sup>lt;sup>7</sup> We view the EDM incentive as referring to the merged firm setting its output price so as to internalize the effect on its profit from inputs used by its downstream unit (which firm 1 ignored pre-merger), while the Chen incentive internalizes the profit from inputs sold to the rival. The EDM and Chen incentives push the merged firm's output price in opposite directions.

substitution.<sup>8</sup> We solve the model numerically in Wolfram Mathematica using a uniform grid for  $(\alpha_1, \alpha_2)$  with a step size of 0.005. The code is available upon request.

With linear demands for the differentiated products, a merger in our setting would increase consumer welfare and total welfare if inputs were not substitutable but instead were used in fixed proportions with output (see Lu et al., 2007 and Section 3.1 below). Fixed-proportions production is a limiting case in our model ( $\alpha_1 = \alpha_2 = 1$ ). One might conjecture that a merger will increase welfare also when input substitution is possible, as this could only reduce the merged firm's *ability* to foreclose rivals. However, we refute this conjecture: we show that a merger can reduce (consumer and total) welfare when firms produce with identical or different Cobb-Douglas technologies. As a robustness check, we also consider a common CES technology with greater input substitutability than Cobb-Douglas and where each input individually is not essential. The merger can reduce welfare also in that setting. Intuitively, with input substitution the rival is a less attractive input customer than under fixed-proportions, which magnifies the merged firm's *incentive* to divert output from the rival to its own good by raising the input price.

When firms use the same Cobb-Douglas technology, the welfare effects of a merger are worse if the input controlled by the merged firm is used in low rather than high intensity (accounts for a low share of downstream input costs). There are two main forces. First, when the usage intensity is lower the cost distortion eliminated for the merged firm is smaller, hence its incentive to cut its output price due to EDM is weaker. Second, the RRC incentive is stronger. The merged firm diverts more output sales from the rival to itself—via a sufficiently larger increase in the input price because it loses a smaller input margin (per unit of the rival's output) than when the input is used with high intensity.<sup>9</sup>

When firms use different Cobb-Douglas technologies, the input monopolist may foreclose completely either firm pre-merger. The welfare effects of a merger then can be non-monotonic. For example, when the rival's usage intensity is low, the merger reduces welfare if the merger partner's usage intensity lies in an intermediate range but raises welfare elsewhere.

The remainder of the paper is organized as follows. Section 2 presents the model and some comparative statics for the above polar cases, varying only  $\alpha_1$  or only  $\alpha_2$ . Section 3 analyzes the

<sup>&</sup>lt;sup>8</sup> The VMG (2020) predominantly discuss linear pricing. For an analysis that addresses nonlinear pricing, secret contracts, and upstream strategic competition, see Rey and Vergé (2019). Our framework is similar to Inderst and Valletti (2011), but they consider a different technology and focus on different issues.

<sup>&</sup>lt;sup>9</sup> With fixed proportions (Leontief technologies), the input monopolist earns the same margin per unit of output regardless of the input proportions used by a firm.

case where the merging supplier's input is used by both firms with Cobb-Douglas technologies. Section 4 considers a common CES technology, and Section 5 concludes.

# 2. A Model where 'Vertical' Mergers Can Be Vertical, Horizontal, or Both

## 2.1 The Setting

Firms 1 and 2 sell differentiated substitute goods to consumers. Firm *i* produces its good using two inputs (X and Y) and a Cobb-Douglas technology with constant returns to scale:

$$Q_i = \beta_i X_i^{\alpha_i} Y_i^{1-\alpha_i} \tag{1}$$

where  $Q_i$  is the quantity of good *i*,  $X_i$  and  $Y_i$  are the input quantities,  $\beta_i > 0$  is a scale factor, and  $0 \le \alpha_i \le 1$  is the elasticity of output with respect to input X.

Input Y is available competitively at a price equal to 1, while input X is produced by a monopolist supplier (firm S) with marginal cost also equal to  $1.^{10}$  Input X is sold to firm *i* at price  $W_i$ . Cost minimization with technology (1) implies that firm *i*'s spending on input X accounts for a fraction  $\alpha_i$  of firm *i*'s total spending on both inputs. In other words,  $\alpha_i$  is the *cost share* of the monopoly input at firm *i*.

We assume  $\beta_i = \alpha_i^{-\alpha_i}(1-\alpha_i)^{-(1-\alpha_i)}$ , so that firm *i*'s marginal cost of production is  $c_i = W_i^{\alpha_i}$ . After firm S merges with firm 1, the merged firm sources input X internally at a cost equal to 1, purchases input Y at a price equal to 1, and hence  $c_1 = 1$  post-merger. Otherwise, firm S sets prices above marginal cost ( $W_i > 1$ ) and thus  $c_i = W_i^{\alpha_i} > 1$  if  $\alpha_i > 0$ . Firm *i*'s conditional factor demand for input X is:

$$X_i = \alpha_i (1/W_i)^{1-\alpha_i} Q_i \tag{2}$$

Demand functions for the two differentiated goods are assumed to be symmetric and linear:

$$Q_i = 2 - 2P_i + P_j \tag{3}$$

where  $P_i$  is the price of good i (and  $j \neq i$ ). Thus, the two goods are imperfect substitutes with a diversion ratio of  $\frac{1}{2}$ . We further assume that demands are derived from a linear-quadratic utility function of a representative consumer, whose utility gives consumer welfare (CW). Total welfare

<sup>&</sup>lt;sup>10</sup> If input X was available competitively (as is input Y), then the model would be symmetric with respect to both the demand for the two goods and the supply of the two inputs. It follows that input X will be more expensive than input Y (since it is supplied by a monopolist) and that the marginal cost of a downstream firm is higher if it uses input X more intensively (ceteris paribus).

(TW) is the sum of CW and the profits of firms S, 1 and 2.

The pre-merger game has several stages. First, firm S sets input prices  $W_1$  and  $W_2$ . Second, firms 1 and 2 observe both input prices and simultaneously set output prices  $P_1$  and  $P_2$  to consumers. Third, firms 1 and 2 receive the order quantities  $Q_1$  and  $Q_2$  from consumers, purchase the required (cost-minimizing) quantities of inputs X and Y, produce, and deliver the goods. Each firm sets its price(s) to maximize its own profit:  $\pi_i = (P_i - W_i^{\alpha_i})Q_i$  for firm i (i=1,2), where  $Q_i$  is given in (3), and  $\pi_S = \sum_{i=1,2} (W_i - 1)X_i$  for firm S, where  $X_i$  and  $Q_i$  are given by (2) and (3).

The post-merger game is similar. The merged firm (firm M) sets the input price  $W_2$  to firm 2. Then, firms M and 2 set output prices  $P_1$  and  $P_2$  to consumers, receive order quantities  $Q_1$  and  $Q_2$ , obtain the required inputs, produce, and deliver the goods. Firm M maximizes its integrated profit:  $\pi_M = (P_1 - 1)Q_1 + (W_2 - 1)X_2$ .<sup>11</sup> As before, firm 2 maximizes  $\pi_2 = (P_2 - W_2^{\alpha_2})Q_2$ .

The above setting nests the two polar cases and the mixed case from the Introduction. We summarize here some results for the polar cases which help provide intuition for the mixed case.

#### 2.2 Merging supplier's input is used only by merger partner

Let firms 1 and 2 have the Cobb-Douglas technology in (1), with  $\alpha_1 > 0$  and  $\alpha_2 = 0$ . Here,  $c_2 = 1$  since firm 2 uses only the competitive input. Figure 1 shows how the pre-merger equilibrium input price to firm 1 ( $W_1$ ) and firm 1's marginal cost of good 1 ( $c_1$ ) vary as functions of the parameter  $\alpha_1$ . As  $\alpha_1$  falls, firm 1's demand for input X becomes less elastic: When  $\alpha_1$  is lower (input X accounts for a lower share of total input costs), the pass-through from  $W_1$  to firm 1's marginal cost  $c_1 = W_1^{\alpha_1}$  is lower, so a given increase in  $W_1$  has a smaller effect on firm 1's price  $P_1$  and output  $Q_1$ , dampening the decrease in demand for X. In response, firm S raises  $W_1$  as  $\alpha_1$  falls, but  $c_1$  still decreases. It follows that the pre-merger price  $P_1$  decreases as  $\alpha_1$  falls. Firm 2's price  $P_2$  also decreases (because with linear demands prices are strategic complements), though more slowly.

Post-merger, good 1's marginal cost is  $c_1 = 1$  for any  $\alpha_1$ , since the marginal cost of the merged firm's internally sourced input is equal to the price of the competitively supplied input, 1. The reduction in  $c_1$  due to the merger therefore is smaller at lower  $\alpha_1$ , i.e., when the merging supplier's input comprises a smaller share of the merger partner's cost. Because the merged firm in this

<sup>&</sup>lt;sup>11</sup> This view of the behavior of an integrated firm as a centralized unit is standard in the literature. See, e.g., Chen (2001) and Arya et al. (2008). Moresi and Schwartz (2017) consider that case and an alternative scenario (Delegation) where the downstream unit acts autonomously to maximize its own profits, in which case  $W_1$  is no longer an irrelevant internal transfer price.

scenario does not supply input X to firm 2, it treats  $c_1 = 1$  as its relevant marginal cost for good 1.<sup>12</sup> It sets  $P_1$  accordingly, so  $P_1$  is independent of  $\alpha_1$  post-merger. Thus, the *reduction* in  $P_1$  due to elimination of double marginalization also is smaller at lower  $\alpha_1$ : *The EDM effect is weaker when*  $\alpha_1$ *is smaller*.



Figure 1: Pre-merger  $W_1$  and  $c_1$  as functions of  $\alpha_1$ 

The welfare effects in this case are straightforward. Due to EDM, the merger always (for all  $\alpha_1$ ) benefits the merging firms, consumers and total welfare, while harming the rival. The changes are potentially large. Consumer welfare and the merging firms' profits each can rise by over 40%, total welfare by over 15%, while the rival's profit can fall by over 20%.

# 2.3 Merging supplier's input is used only by merger partner's rival

Suppose  $\alpha_1 = 0$  and  $\alpha_2 > 0$ . In this scenario there is no EDM since firm 1 does not use the input controlled by its merger partner, firm S. While the merger ostensibly is still 'vertical' because firm S and firm 1 operate at different stages of the supply chain, the incentives generated are purely horizontal in nature and the merger will raises all downstream prices.

<sup>&</sup>lt;sup>12</sup> If the merged firm also supplies input X to the rival (Section 3), its marginal cost of supplying good 1 to consumers includes the resource cost  $c_1 = 1$  and an opportunity cost—the input profits lost per additional unit sold of good 1 due to diversion of sales from good 2. Internalization of this opportunity cost when setting  $P_1$  is the "Chen incentive."

Pre-merger, firm S earns profit only from input sales to firm 2. After firms *S* and 1 merge, the merged firm M has two potential sources of profit: input sales to firm 2 and sales of its own good 1. These profit sources are substitutes for firm M because goods 1 and 2 are substitutes. Therefore, relative to the individual incentives of firm S and firm 1 pre-merger, firm M has two anti-competitive pricing incentives noted earlier: RRC and Chen.

We denote an increase in  $W_2$  as RRC or "foreclosure" and find two sub-cases: *partial foreclosure*, where firm 2 remains active but pays a higher input price; and *complete foreclosure*, where firm 2 is driven completely out of the market.<sup>13</sup> For  $\alpha_2$  above a threshold ( $\alpha_2 > 0.145$ ), firm M continues to supply its input X to firm 2, though at a higher  $W_2$  than pre-merger. As  $\alpha_2$  decreases from 1 in this range, firm 2 becomes a less attractive input customer and firm M raises  $W_2$  by a greater percent compared to the pre-merger level. For  $\alpha_2$  below the threshold ( $\alpha_2 < 0.145$ ), firm M sets  $W_2$  prohibitively high and firm 2 is foreclosed completely. In this range, input *X* would earn such a low share of firm 2's total input spending that firm M prefers to forgo all input sales and earn profits solely from selling increased quantities of its own good 1. Thus, foreclosure becomes more attractive to the merged firm when the customer/rival is a less important input customer.<sup>14</sup>

Figure 2 shows the percent increase in  $W_2$  post-merger as a function of  $\alpha_2$  in a range where firm 2 remains active (partial foreclosure). Figure 3 contrasts the resulting behavior of firm 2's marginal cost  $c_2$  pre-merger versus post-merger as functions of  $\alpha_2$ .<sup>15</sup> As  $\alpha_2$  decreases, firm S raises the input price  $W_2$  but  $c_2$  still decreases because firm 2 uses fewer units of the higher-priced input X. Post-merger, firm M raises  $W_2$  more rapidly as  $\alpha_2$  decreases (Figure 2), and by enough that  $c_2$  increases as  $\alpha_2$  decreases (Figure 3).<sup>16</sup> Perhaps surprisingly, therefore, the *RRC effect is stronger when*  $\alpha_2$  is

<sup>&</sup>lt;sup>13</sup> The VMG (2020, Section 4.a) use "foreclosure" to denote refusal to supply the input, even if the rival remains active, and "raising rivals' costs" to denote an increase in the input price (presumably to a non-prohibitive level, since a prohibitive price increase would amount to refusal to supply).

<sup>&</sup>lt;sup>14</sup> This finding is reminiscent of O'Brien and Salop's (2000) analysis of the competitive effects of partial ownership by competing firms. The greatest harm arises when the partial owner has voting control over the other firm's pricing but holds only a small ownership share, hence does not lose much by handicapping that firm. Here, the merged firm controls firm 2's pricing through the input price, and its loss from handicapping firm 2 is lower when firm 2's spends a smaller share of its input costs on the merged firm's input.

<sup>&</sup>lt;sup>15</sup> Pre-merger, the behavior of  $c_2$  as a function of  $\alpha_2$  is identical to  $c_1$  as a function of  $\alpha_1$  from Figure 1. In both scenarios, firm S initially supplies to a single firm that produces with the technology given in (1) and competes against a rival that uses only the competitive input.

<sup>&</sup>lt;sup>16</sup> Firm S being an unconstrained monopolist is important here. If the price of input X were capped, say because X is available from a higher-cost source at a fixed price not much above firm S's marginal cost, then firm S would be unable to raise  $W_2$  enough to outweigh the direct effect on  $c_2$  of a decrease in  $\alpha_2$ .

*smaller* — the increase in the rival's cost due to the merger is larger when the monopoly input controlled by the merged firm constitutes a *smaller* share of the rival's cost.<sup>17</sup>





Figure 3: Firm 2's cost  $c_2$  pre-merger and post-merger as functions of  $\alpha_2$ 

Further intuition for why RRC is stronger when  $\alpha_2$  is smaller can be gleaned by considering how the pre-merger equilibrium changes as  $\alpha_2$  falls below 1.<sup>18</sup> Table 1 shows the equilibrium values of relevant variables pre-merger and post-merger. Firm S's margin per unit of firm 2's output,  $(W_2 - 1)(X_2/Q_2)$ , declines as  $\alpha_2$  falls, due to the fall in  $X_2/Q_2$ . Therefore, starting at the premerger equilibrium values, the loss of input profits to firm M if firm 2's output is reduced by one

<sup>&</sup>lt;sup>17</sup> We will find the same pattern in Section 3 where both downstream firms use the monopoly input and in equal intensity ( $\alpha_1 = \alpha_2 \in (0, 1]$ ).

<sup>&</sup>lt;sup>18</sup> In the spirit of UPP analysis, we start at the pre-merger equilibrium outcome and consider the "first round" pricing incentives following a merger.

unit decreases as  $\alpha_2$  falls. Firm M's gain from selling an additional unit of good 1,  $(P_1 - 1)$ , also declines (because pre-merger, when  $\alpha_2$  falls  $c_2$  decreases, which reduces  $P_2$  hence also  $P_1$ ), but more slowly than the loss. Since the diversion ratio from good 2 to good 1 is constant with linear demands, the merged firm finds it increasingly attractive to divert output from the rival's good to its own as  $\alpha_2$  falls. It implements such greater diversion by inducing a larger increase in  $c_2$  when  $\alpha_2$  is smaller through successively larger increases in  $W_2$ .

		PRE-M	ERGER			POST-MERGER		CHANGE	
α2	$W_2$	<i>C</i> <sub>2</sub>	$\frac{X_2}{Q_2}$	$(W_2 - 1) \frac{x_2}{Q_2}$	<i>P</i> <sub>1</sub>	$W_2$	<i>C</i> <sub>2</sub>	$\Delta W_2$	$\Delta c_2$
1	1.357	1.357	1.00	0.357	1.381	1.492	1.492	0.135	0.135
0.8	1.458	1.352	0.74	0.339	1.380	1.651	1.493	0.193	0.141
0.6	1.636	1.343	0.49	0.312	1.379	1.955	1.495	0.319	0.152

# Table 1: Understanding RRC when only the rival uses the monopoly input

Prices of both goods rise post-merger, as shown in Figure 4.<sup>19</sup> The percentage increase in the rival's price  $P_2$  diminishes as  $\alpha_2$  rises above 0.145, tracking the RRC pattern from Figure 3. The increase in  $P_1$  also diminishes initially as  $\alpha_2$  rises above 0.145, but eventually becomes larger—despite the continued decline in  $\Delta P_2$ (%). This illustrates the *Chen incentive*: as firm 2 uses the merging supplier's input more intensively ( $\alpha_2$  increases), the merged firm stimulates sales of the rival's good not only by reducing the increase in the input price  $W_2$  but also by magnifying the increase in the price of its own good  $P_1$ .<sup>20</sup>

<sup>&</sup>lt;sup>19</sup> In Figure 4, there is a kink at  $\alpha_2 = 0.145$ , where total foreclosure turns into partial foreclosure. For  $\alpha_2 \le 0.145$ , we set  $P_2$  equal to the 'choke price' of firm 2's residual demand conditional on  $P_1$ .

<sup>&</sup>lt;sup>20</sup> The Chen and RRC incentives interact and jointly determine the behavior of  $P_1$ . For  $\alpha_2 \ge 0.15$ , firm M increases  $P_1$  for two reasons: diversion of output sales to the rival increases input sales to the rival, and partial foreclosure makes good 1's demand less elastic. For  $\alpha_2 \le 0.145$ , the first reason vanishes due to complete foreclosure, but the second reason becomes stronger.



Figure 4:  $\Delta P_1$  (%) and  $\Delta P_2$  (%) as functions of  $\alpha_2$ 

The merger reduces the rival's profit by at least 35% under partial foreclosure and by 100% with complete foreclosure, while joint profits of the merging firms rise between 10% and 55%. Total welfare declines between (approximately) 15% and 35%, while consumer welfare declines between 35% and 55%.

# 3 Both Producers Use the Merging Supplier's Input

# 3.1 Same Cobb-Douglas Technology

Suppose firms 1 and 2 have the same technology:  $\alpha_1 = \alpha_2 = \alpha \in (0,1]$ . Variations in the common  $\alpha$  do not affect the marginal cost of good 1 post-merger ( $c_1 = 1$ ), but will affect firm 2's cost as well as the pre-merger equilibrium. When  $\alpha = 1$ , both firms use only the input supplied by firm S, which then is used in *fixed proportions* with output. In that case, and for a broad class of linear demands downstream, Lu et al. (2007) showed that a vertical merger of an input monopolist and a downstream duopolist raises consumer welfare (CW) and total welfare (TW): it lowers the prices of both goods, and even lowers the input price to the rival.<sup>21</sup> The last column in Table 2 shows the merger effects in our model when  $\alpha = 1$ .<sup>22</sup> We will discuss the intuition for all the patterns in Table 2 shortly.

<sup>&</sup>lt;sup>21</sup> That result does not extend to logit demand or upstream bargaining. See Das Varma and De Stefano (2020).

<sup>&</sup>lt;sup>22</sup> A merger raises welfare also in a related setting with fixed proportions analyzed by Agkün et al. (2020). They consider a monopolist seller of one component that is used with a second component to form a system assembled by consumers. Differentiated duopolists facing linear demands sell the second component directly

Input X's cost share ( $\alpha$ )	0.05	0.1	0.25	0.5	1
Input price to firm 2 ( $W_2$ )			42.8%	4.46%	-0.51%
Marginal cost of good 2 ( $c_2$ )			9.31%	2.21%	-0.51%
Price of good 2 ( $P_2$ )			2.28%	-1.04%	-2.27%
Quantity of good 2 ( $Q_2$ )	-100%	-100%	-47.7%	-27.8%	-18.2%
Marginal cost of good 1 ( $c_1$ )	-16.9%	-22.7%	-28.9%	-31.8%	-33.3%
Price of good 1 ( $P_1$ )	2.1%	-1.88%	-7.19%	-8.11%	-8.18%
Quantity of good 1 ( $Q_1$ )	41.1%	59.1%	67.6%	70.0%	70.5%
Consumer welfare (CW)	-33.6%	-15.6%	31.9%	54.7%	65.7%
Total welfare (TW)	-10.3%	1.02%	18.7%	21.1%	18.2%

#### Table 2: Merger effects when firms 1 and 2 use the same Cobb-Douglas technology

Input substitution ( $0 < \alpha < 1$ ), whereby inputs are used in *variable proportions* with output, introduces rich possibilities not captured by the fixed-proportions case. In Table 2, consider the merger effects as  $\alpha$  declines from 1 to 0.05. When  $\alpha = 0.5$ , firm M raises the input price  $W_2$ . The rival's price  $P_2$  still falls, however, due to the expected fall in  $P_1$ , triggered by EDM. When  $\alpha = 0.25$ ,  $W_2$  increases by much more, causing  $P_2$  to rise. In both cases ( $\alpha = 0.5$  or 0.25), CW and TW increase despite partial foreclosure of firm 2 (rise in  $W_2$ ), due to the reduction in  $P_1$  and expansion in  $Q_1$ .<sup>23</sup> For  $\alpha$  below about 0.15, firm M chooses complete foreclosure of firm 2. When  $\alpha = 0.1$ , firm M still reduces  $P_1$ , but now CW falls (due to the loss of good 2), though TW still rises (due to elimination of cost distortion in production of good 1). Complete foreclosure occurs also when  $\alpha = 0.0.5$ , and this time firm M raises  $P_1$ , leading to a reduction in both CW and TW.

Consumer welfare and total welfare each can rise or fall substantially. For CW, the range is from about – 55% at  $\alpha$  near 0 to over 60% at  $\alpha = 1$ , while for TW the range is from –35% at  $\alpha$  near 0 to 20% at  $\alpha$  around 0.3. As expected, joint profits of the merging firms always rise, with the gain

to consumers, and pre-merger all three prices are set simultaneously (whereas in our setting the monopoly price is set first). A merger between the monopolist and either duopolist leads to an *increase* in the monopoly component's price (unlike our decrease in *W*<sub>2</sub>), but still lowers both systems' prices.

<sup>23</sup> With partial foreclosure, the increase in  $c_2$  is smaller than the increase in  $W_2$  because of input substitution. For all  $\alpha$  between 0 and 1,  $c_1$  decreases post-merger. The decrease is smaller at lower  $\alpha$  because post-merger  $c_1 = 1$  regardless of  $\alpha$ , whereas pre-merger  $c_1$  is lower when  $\alpha$  is lower (recall discussion of Figure 1, which applied when only firm 1 used input X, but the same logic holds when firms have the same  $\alpha$ ). ranging from about 10% to almost 90%. The rival's profit falls by at least 30% and up to 100% with complete foreclosure.<sup>24</sup> Both magnitudes, merging firms' gain and the rival's loss, are larger at low  $\alpha$  than at high  $\alpha$ , corresponding to the finding that the extent of foreclosure is greater at low  $\alpha$ .

The patterns in Table 2 can be further understood as follows. First, consider the merged firm's incentives regarding  $P_1$ , starting at the pre-merger equilibrium values of  $P_1$ ,  $P_2$ ,  $W_1$  and  $W_2$ . Express firm M's profit as  $\pi_M = \pi_1 + (W_1 - c)X_1 + (W_2 - c)X_2$ , where  $\pi_1$  is the profit of former firm 1, c is the marginal cost of input X, and  $\partial \pi_1 / \partial P_1 = 0$  at the pre-merger equilibrium. Thus,

$$\frac{\partial \pi_{M}}{\partial P_{1}} = \underbrace{(W_{1} - c)\left(\frac{\partial X_{1}}{\partial Q_{1}}\frac{\partial Q_{1}}{\partial P_{1}}\right)}_{EDM \ incentive} + \underbrace{(W_{2} - c)\left(\frac{\partial X_{2}}{\partial Q_{2}}\frac{\partial Q_{2}}{\partial P_{1}}\right)}_{Chen \ incentive}$$

Pre-merger,  $W_1 = W_2 = W^* > c$ , and  $\partial X_1 / \partial Q_1 = \partial X_2 / \partial Q_2$  since the firms have identical technologies and we are starting from a symmetric equilibrium. Thus,

$$\frac{\partial \pi_M}{\partial P_1} = (W^* - c) \frac{\partial X_i}{\partial Q_i} \Big[ \frac{\partial Q_1}{\partial P_1} + \frac{\partial Q_2}{\partial P_1} \Big] < 0.$$

The inequality holds because with linear demands the term in square brackets is constant and negative (-1 in our demand system (3))—own-price effect outweighs cross-price effect—and the other two terms are positive. Thus, the EDM incentive dominates the Chen incentive, so firm M wants to reduce  $P_1$  for all  $\alpha \in (0,1]$  (holding all other prices constant).

The net EDM incentive (EDM net of Chen) measured by  $\partial \pi_M / \partial P_1$  is strongest when  $\alpha = 1$ . As  $\alpha$  falls, there are two opposing effects on this net incentive: (i)  $W^*$  rises pre-merger, hence ( $W^* - c$ ) rises; but (ii) from (2),  $\partial X_i / \partial Q_i = \alpha (1/W^*)^{1-\alpha}$  falls, since  $W^* > 1$ . That is, when  $\alpha$  is lower, an increase in output leads to a smaller increase in demand for input X. Effect (ii) dominates, so the merged firm's incentive to reduce  $P_1$  (evaluated at the pre-merger equilibrium) diminishes when its input is used less intensively.

Now consider the interaction between the RRC and net EDM incentives. For  $\alpha$  near 1, the net EDM incentive is strong, leading to a large decrease in  $P_1$ , which reduces firm 2's output and demand for input X, making the latter more elastic. This effect is strong enough that firm M prefers to reduce the input price  $W_2$ , despite the RRC incentive. As  $\alpha$  decreases, starting at the pre-merger

<sup>&</sup>lt;sup>24</sup> The rival's large loss is relevant for policy if the rival has significant fixed costs and one is concerned about adverse long-term effects on market structure. However, claims of harm to rivals generally should be treated with healthy skepticism, to avoid condemning mergers that harm rivals but benefit consumers.

equilibrium values, the net EDM incentive weakens whereas the RRC incentive strengthens (as discussed shortly), explaining the patterns in Table 2.

In particular, as  $\alpha$  falls,  $W_2$  eventually increases above its pre-merger level and the percentage increase becomes larger, ultimately leading to complete foreclosure. The pattern is similar to that in Figure 2 (where only the rival used input X), except that for high values of the common  $\alpha$  (0.84  $\leq \alpha$  $\leq$  1) firm M now reduces  $W_2$  below the pre-merger level due to the EDM incentive. Driven by the change in  $W_2$ , post-merger  $c_2$  increases as  $\alpha$  falls, whereas pre-merger  $c_2$  decreases as  $\alpha$  falls.<sup>25</sup>

Thus, the merger-induced  $\Delta c_2$  is larger when  $\alpha$  is smaller.<sup>26</sup> The logic is the same as in Section 2.3, where only the rival used input X, and Table 3 is the counterpart to Table 1. As  $\alpha$  falls, firm M's loss of input profits if firm 2's output is reduced by one unit,  $(W_2 - 1)(X_2/Q_2)$ , declines faster than M's gain from selling another unit of good 1,  $(P_1 - 1)$ . Therefore, firm M diverts more output from the rival's good to its own as  $\alpha$  fall, by increasingly raising  $c_2$  through larger increases in  $W_2$ .

		<u>PRE-MI</u>	<u>ERGER</u>		POST-I	<u>MERGER</u>	<u>CHANGE</u>		
α	$W_2$	<i>c</i> <sub>2</sub>	$\frac{X_2}{Q_2}$	$(W_2-1)\frac{X_2}{Q_2}$	<i>P</i> <sub>1</sub>	$W_2$	<i>C</i> <sub>2</sub>	$\Delta W_2$	$\Delta c_2$
1	1.500	1.500	1.00	0.500	1.667	1.492	1.492	-0.008	-0.008
0.8	1.648	1.491	0.72	0.467	1.661	1.651	1.493	0.003	0.002
0.6	1.915	1.477	0.46	0.421	1.651	1.955	1.495	0.040	0.018

# Table 3: Understanding RRC when both firms have the same Cobb-Douglas technology

### 3.2 Different Cobb-Douglas Technologies

New possibilities emerge when firms 1 and 2 have different technologies ( $\alpha_1 \neq \alpha_2$ ) and both use input X. The pre-merger equilibrium will be asymmetric. And unlike in the polar cases, firm S premerger is able to foreclose completely either firm by refusing to supply its input. If  $\alpha_1$  and  $\alpha_2$  are strictly positive but different enough, firm S pre-merger will foreclose the low user of its input. The merger effects thus can be quite complex.

<sup>&</sup>lt;sup>25</sup> The patterns are the same as in Figure 3, where only  $\alpha_2$  varied, except that  $c_2$  there always rose postmerger, whereas now  $c_2$  falls post-merger at high  $\alpha$  due to the decrease in  $W_2$ .

<sup>&</sup>lt;sup>26</sup> Moresi and Schwartz (2020) cite this finding for identical Cobb-Douglas technologies (common  $\alpha$ ) to caution against a safe-harbor for vertical mergers based on the merging supplier's input accounting for a low share of rivals' input costs. (The same pattern was found, and its logic was explained, in Section 2.3 when only the merger partner's rival uses firm S's input.)



Figure 5: Regions where input price  $W_2$  falls or rises

Refer to Figure 5. First, there is a discontinuity at  $\alpha_2 = 0$  since firm M can foreclose completely firm 2 when  $\alpha_2 > 0$  by not supplying its input or charging a prohibitive price for it, but cannot when  $\alpha_2 = 0$ .

Second, when  $\alpha_1 > \alpha_2 > 0$  and  $\alpha_2$  is sufficiently small, firm S elects to "marginalize" firm 2 *premerger*—charge an input price that is just high enough to drive firm 2's output down to zero. Intuitively, when firm S obtains much greater input sales per unit output of firm 1 than of firm 2, it prefers to divert maximal output to firm 1 by raising  $W_2$  while maintaining potential competition from firm 2 in order to cap firm 1's price (raising  $W_2$  any higher, hence firm 2's cost, would allow firm 1 to raise  $P_1$  thereby reducing input sales to firm 1). That occurs in the red region in Figure 5. (There is a symmetric region, not shown, where firm S "marginalizes" firm 1 pre-merger.)

Third, post-merger  $c_1 = 1$  for any  $\alpha_1$ , so the post-merger equilibrium depends only on  $\alpha_2$  and complete foreclosure occurs for  $0 < \alpha_2 \le 0.145$ . The merger thus induces *additional* complete foreclosure in the green region in Figure 5. For  $\alpha_2 \ge 0.15$ , complete foreclosure never occurs, but partial foreclosure can occur as shown by the orange region in Figure 5.

For high  $\alpha_2$ , the change in  $W_2$  is non-monotonic in  $\alpha_1$  because the EDM effect is non-monotonic. Consider for example  $\alpha_2 = 0.9$  in Figure 5. When  $\alpha_1 = 0$ , we are in the polar case where the monopolized input is used only by firm 2: post-merger there is no EDM and there is partial foreclosure as firm M raises  $W_2$ . Figure 5 does not show that because of a discontinuity at  $\alpha_1 = 0$ : for  $0 < \alpha_1 < 0.075$ , firm S "marginalizes" firm 1 pre-merger (i.e., charges firm 1 an input price  $W_1$  that is sufficiently high to drive firm 1's output down to exactly zero) and charges a relatively high  $W_2$ , while post-merger firm M *enters* the output market with good 1—which is effectively a very large EDM effect. The entry of good 1 reduces firm 2's input demand and makes it sufficiently more elastic that firm M chooses to reduce  $W_2$  despite the RRC incentive. A post-merger reduction in  $W_2$  also occurs for  $\alpha_1 > 0.77$ , because, again, there is a strong EDM effect that outweighs RRC, although here the strong EDM effect is due to good 1 using input X with high intensity (not to good 1 entering the market). For intermediate  $\alpha_1$ , the RRC incentive dominates and  $W_2$  rises.

As expected, the merger always increases the joint profits of the merging firms and harms the rival, except when the rival was "marginalized" pre-merger. Figure 6 shows the regions where CW and TW rise or fall. The merger lowers CW only for relatively low values of  $\alpha_1$  and  $\alpha_2$  (orange region) and lowers TW in a smaller (green) region. Both regions are small subsets of the region where the merger raises  $W_2$  (compare with Figure 5)—providing an important reminder that harm to competitors does not imply harm to competition.



Figure 6: Regions where consumer and total welfare rise or fall

Interestingly, for low  $\alpha_1$  and  $\alpha_2$ , the welfare effects are non-monotonic as one of these parameters varies holding the other fixed. For example, consider  $\alpha_2 = 0.145$ , so firm 2 is foreclosed completely only post-merger. If  $0.05 \le \alpha_1 \le 0.16$ , CW falls post-merger: the EDM effect does not

reduce  $P_1$  enough to offset consumers' harm from losing good 2.<sup>27</sup> For  $\alpha_1 \ge 0.165$ , the EDM effect is stronger and CW rises. For  $0 < \alpha_1 \le 0.045$ , the EDM effect is stronger as well, since firm S drove firm 1's output to zero whereas the merged firm discretely increases that output, and CW rises. Intuitively, consumers purchase only one good both pre-merger and post-merger, but post-merger the price is lower due to EDM.

#### 4. CES technology

With Cobb-Douglas technology, each input is essential. To test the role of this assumption, we consider again the symmetric case with  $\alpha_1 = \alpha_2 = \alpha \in (0,1]$ , and replace Cobb-Douglas by a CES technology with greater elasticity of substitution, 2 instead of 1 in Cobb-Douglas:

$$Q_i = \beta (\alpha X_i^{1/2} + (1 - \alpha) Y_i^{1/2})^2$$
(4)

where  $0 < \alpha \le 1$  is a share parameter and  $\beta = 1/(\alpha^2 + (1 - \alpha)^2)$  is a scale factor. It follows that the cost share of input X at firm *i* (denoted  $s_i$ ) and firm *i*'s marginal cost are given by:<sup>28</sup>

$$s_i = \frac{1}{1 + W_i/\phi} \qquad \text{and} \qquad c_i = \frac{1 + \phi}{1 + \phi/W_i} \tag{5}$$

where  $\phi = (\alpha/(1-\alpha))^2$ . As  $W_i \to \infty$ ,  $c_i \to 1 + \phi$ , which is *finite* if  $\alpha < 1$  because input X is not essential if  $\alpha < 1$ . Thus, unlike for Cobb-Douglas, firm M can no longer raise  $c_2$  indefinitely by raising  $W_2$  post-merger. As before, demand is given by (3).

The merger always increases joint profits of the merging firms and reduces the rival's profit (to zero when there is complete foreclosure). Table 4 illustrates the other merger effects. The last column in Table 4 corresponds to the case where both firms use only the input supplied by firm S, and thus is identical to the last column in Table 2. The other columns show several interesting differences from the symmetric Cobb-Douglas case in Table 2, as well as commonalities.

<sup>&</sup>lt;sup>27</sup> In the symmetric case ( $\alpha_1 = \alpha_2 = \alpha$ ), CW falls only if firm 2 is completely foreclosed ( $\alpha \le 0.145$ ) and the same is true with asymmetry if  $\alpha_1 > \alpha_2$ . However, if  $\alpha_1 < \alpha_2$ , there is a (small) region where CW falls even though firm 2 remains active post-merger (e.g. ( $\alpha_1, \alpha_2$ )=(0.12, 0.16)).

<sup>&</sup>lt;sup>28</sup> For Cobb-Douglas, we have  $s_i = \alpha$ . For the CES technology in (4),  $s_i$  is decreasing in  $W_i$  and increasing in  $\alpha$ .

Firm S's cost share (s)	0.1	0.25	0.3	0.5	1
Input price to firm 2	46.2%			10.3%	-0.51%
Marginal cost of good 2	3.27%	33.7%	43.7%	4.91%	-0.51%
Price of good 2	0.60%	12.7%		0.35%	-2.27%
Quantity of good 2	-9.33%	-96.7%	-100%	-32.8%	-18.2%
Marginal cost of good 1	-9.78%	-21.2%	-23.8%	-29.3%	-33.3%
Price of good 1	-2.74%	-5.74%	-2.71%	-7.26%	-8.18%
Quantity of good 1	14.4%	75.1%	63.7%	61.2%	70.5%
Consumer welfare	5.58%	4.15%	-10.7%	37.9%	65.7%
Total welfare	2.83%	-3.89%	-7.07%	16.8%	18.2%

#### Table 4: Merger effects when firms 1 and 2 use the same CES technology

First, unlike with Cobb-Douglas, refusal to deal does not imply complete foreclosure. For example, when firm S's cost share is s = 0.25, the merged firm refuses to sell its input to firm 2, and firm 2's output falls substantially (by 96.7%) but not to zero because firm 2's marginal cost remains non-prohibitive. Complete foreclosure can still occur, however, for example when s = 0.3: firm 2's output is driven to zero by the joint impact of a higher input price and a lower downstream price for firm M due to EDM.

Second, whereas for Cobb-Douglas technology complete foreclosure occurs when firm S's cost share is low ( $0 < \alpha < 0.15$ ), for the CES technology it occurs for intermediate values (0.26 < s < 0.31). Intuitively, when the cost share is low, withholding the input would not raise firm 2's cost sufficiently to induce firm 2 to exit the market, and when the share is high the merged firm could raise firm 2's cost sufficiently but prefers to continue to supply firm 2.

Despite these differences, the key finding from the Cobb-Douglas case carries over: the merger can reduce consumer welfare and/or total welfare, unlike in the case without input substitution.<sup>29</sup>

<sup>&</sup>lt;sup>29</sup> However, a reduction in CW implies a reduction in TW, while with Cobb-Douglas a reduction in TW implies a reduction in CW.

#### 5. Concluding Remarks

We analyzed the effects of a vertical merger between a monopolist input supplier and a downstream firm engaged in duopoly competition with a rival that supplies a differentiated substitute good, when both firms can substitute imperfectly from the monopoly input. Our main model considered Cobb-Douglas technologies (identical or different), and an extension considered a common CES technology. Linear pricing was assumed throughout, hence the merged firm generally has three different pricing incentives compared to the separate merger partners: to decrease the price of the firm's final good in order to reflect the true resource cost of that input (EDM incentive), to increase that same price in order to reflect the opportunity cost from lost input sales to the rival due to sales diverted from its good (Chen incentive), and to raise the input price to the rival (RRC incentive). The EDM and Chen incentives work in opposite directions, and the actual changes in the equilibrium values of all prices will reflect the joint effect of all three incentives.

Somewhat surprisingly, with input substitution—Cobb-Douglas or CES technologies—the merger can reduce total welfare and consumer welfare, whereas in the same environment (including linear demands), prior work showed that a merger is beneficial if the production technology involves fixed proportions. Relatedly, with identical Cobb-Douglas technologies (yielding a symmetric pre-merger equilibrium) the merged firm raises the rival's cost by more, and welfare harm is greater, when the merged firm's input is used in low rather than high intensity. Both findings derive from the same force. Under fixed proportions technologies, the rival's output yields commensurate input profits to the merged firm, reducing its incentive to handicap the rival. With input substitution, the merged firm has a stronger incentive to divert output to its own good by raising the input price and rival's cost and this incentive grows as the rival uses its input less intensively. When firms use different Cobb-Douglas technologies, the merger effects can be complex and non-monotonic in the usage intensity of either firm.

We caution that our analysis involved specific examples and therefore only illustrates possibilities. Future work could explore the robustness of our findings to alternative assumptions about demand and technology. Nevertheless, the analysis does offer two implications for assessing vertical mergers. It cautions against using the ability of a rival to substitute the merged firm's input with other inputs as an indicator of reduced foreclosure concerns. And it reiterates the need to consider the merged firm's profits from sales of inputs to rivals, not only from its own output.

#### References

- Agkün, U., Caffarra, C., Etro, F., and Stillman, R., 2020. "On the Welfare Impact of Merger of Complements With Raising Rivals' Costs." *Economics Letters*, Vol. 195, Issue C.
- Arya, A., Mittendorf, B., and Sappington, D.E.M., 2008. "Outsourcing, Vertical Integration, and Price vs. Quantity Competition." *International Journal of Industrial Organization*, Vol. 26, pp. 1-16.
- Chen, Y., 2001. "On Vertical Mergers and Competitive Effects." *RAND Journal of Economics*, Vol. 32, pp. 667-685.
- Das Varma, G. and De Stefano, M., 2020. "Equilibrium Analysis of Vertical Mergers." *The Antitrust Bulletin*, Vol. 65, pp. 445-458.
- Inderst, R. and Valletti, T., 2011. "Incentives for Input Foreclosure." *European Economic Review*, Vol. 55, pp. 820-831.
- Lu, S., Moresi, S., and S. C. Salop. 2007. "A Note on Vertical Mergers with an Upstream Monopolist: Foreclosure and Consumer Welfare Effects." Mimeo. <u>https://www.crai.com/sites/default/files/publications/Merging-with-an-upstream-monopolist.pdf</u>.
- Moresi, S. and Salop, S.C., 2020. "Quantifying the Increase in 'Effective Concentration' from Vertical Mergers that Raise Input Foreclosure Concerns: Comment on the Draft Vertical Merger Guidelines." Mimeo. <u>https://ssrn.com/abstract=3543774</u>.
- Moresi, S. and Schwartz, M., 2017. "Strategic Incentives When Supplying to Rivals With an Application to Vertical Firm Structure." *International Journal of Industrial Organization*, Vol. 51, pp. 137-161.
- Moresi, S. and Schwartz, M., 2020. "Vertical Mergers and Input Foreclosure When Rivals Can Substitute Inputs: Safe Harbor for Low Share of Input Sales to Rivals?" *Competition Policy International*, December 7. Earlier version available at: <u>https://ssrn.com/abstract=3630589</u>.
- O'Brien, D.P. and Salop, S.C., 2000. "Competitive Effects of Partial Ownership: Financial Interest and Corporate Control." *Antitrust Law journal*, Vol. 67, pp. 559-614.
- Rey, P., and Vergé. T., 2019. "Secret Contracting in Multilateral Relations." Mimeo. <u>https://www.tse-fr.eu/publications/secret-contracting-multilateral-relations</u>.
- Rogerson, W.P., 2014. "A Vertical Merger in the Video Programming and Distribution Industry: The Case of Comcast-NBCU." In J. Kwoka and L. White eds., *The Antitrust Revolution*, 6<sup>th</sup> Ed., New York: Oxford U Press, pp. 534-575.
- Spengler, J.J., 1950. "Vertical Integration and Antitrust Policy." *Journal of Political Economy*, Vol. 58, pp. 347-3.
- U.S. Department of Justice & The Federal Trade Commission, 2020. *Vertical Merger Guidelines*. <u>https://www.justice.gov/opa/pr/department-justice-and-federal-trade-commission-issue-new-vertical-merger-guidelines</u>.