



Solute-Interface Interactions: Experimental and Atomistic Simulation Results

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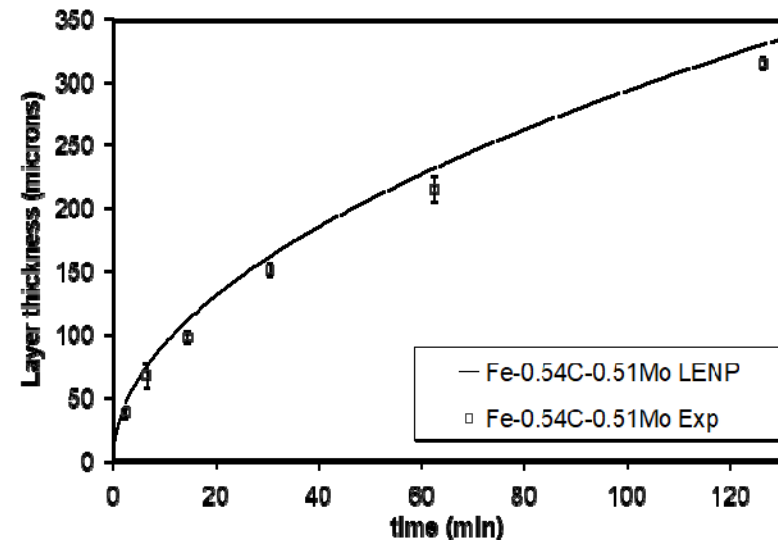
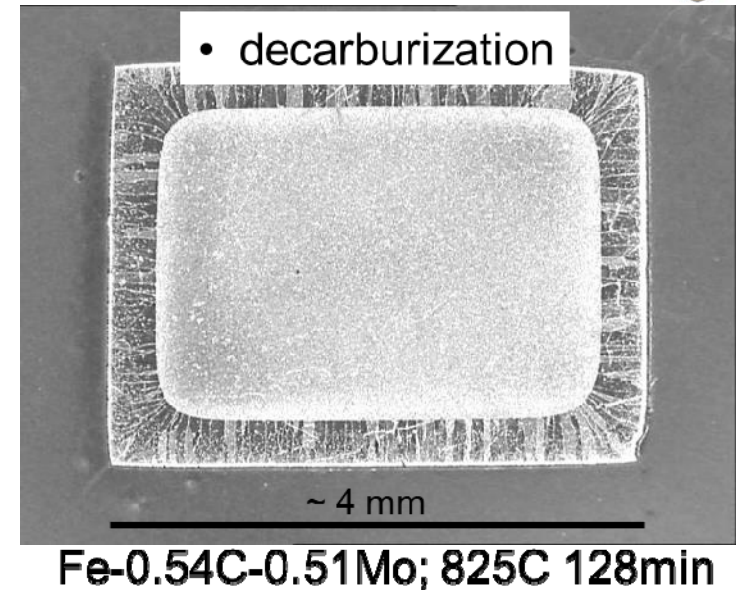
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Review of Experimental Results

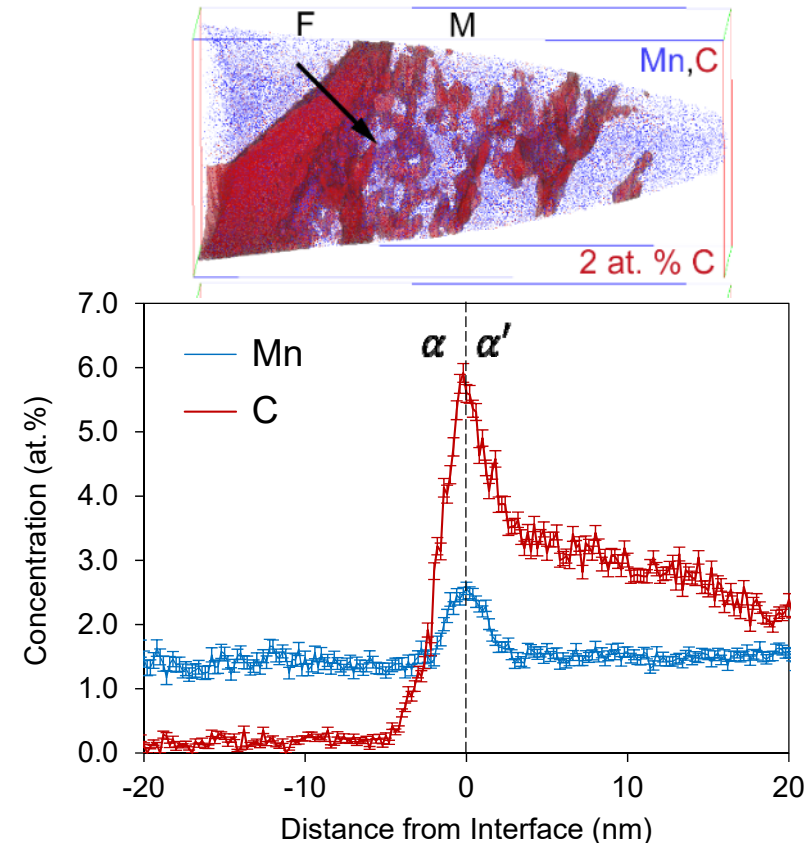
- We have examined a number of ternary and quaternary systems:
 - Fe-Mo-C
 - Fe-Cr-C
 - Fe-Mn-C
 - Fe-Si-C
 - Fe-Ni-C
 - Fe-Mn-Si-C
 - Fe-Mn-Mo-C



C. R. Hutchinson et al, Met. Trans A37, 1711.

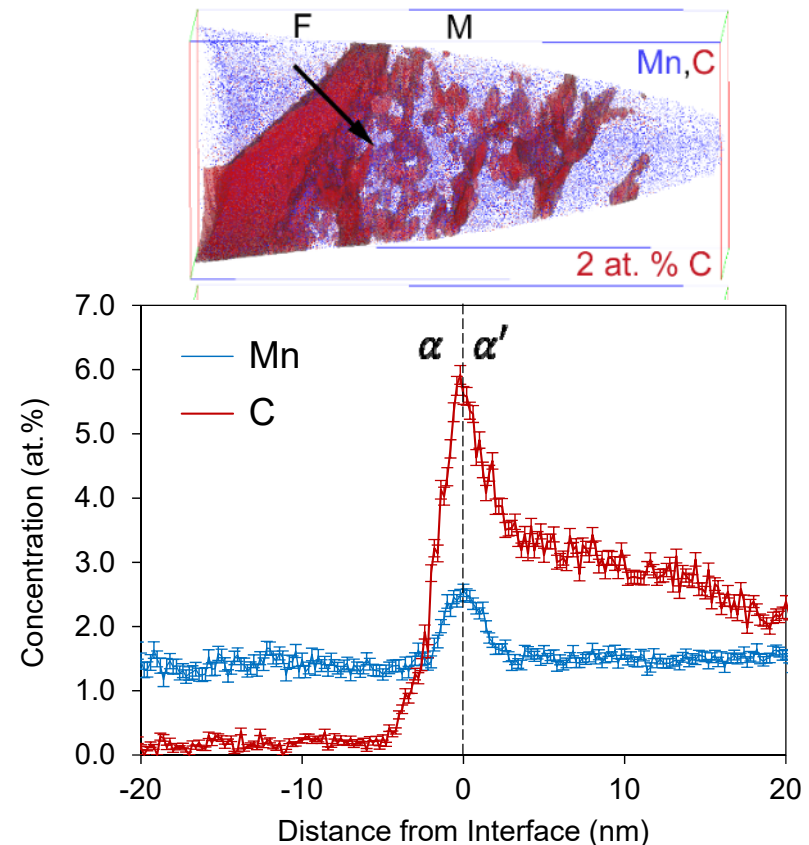
Review of Experimental Results

- Atom probe shows segregation to the interface.
- We measure the enrichment and use it to calculate a binding energy.



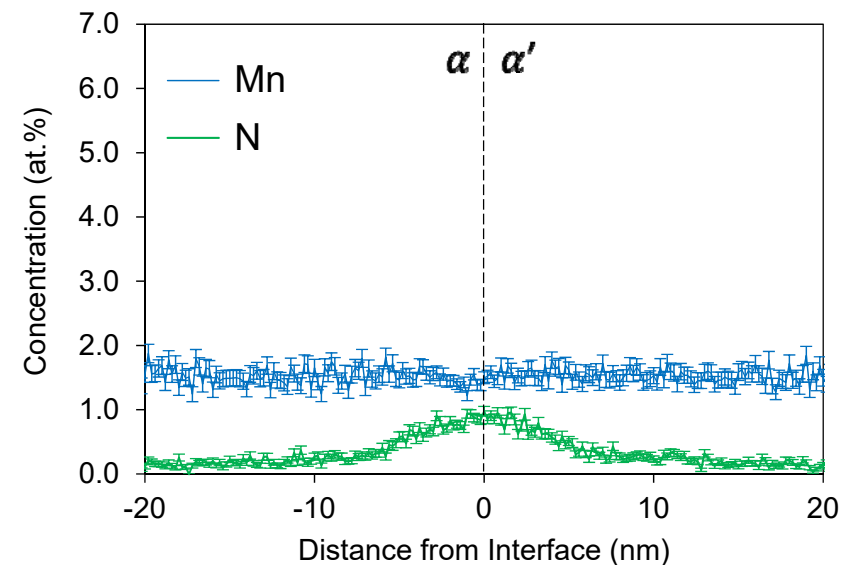
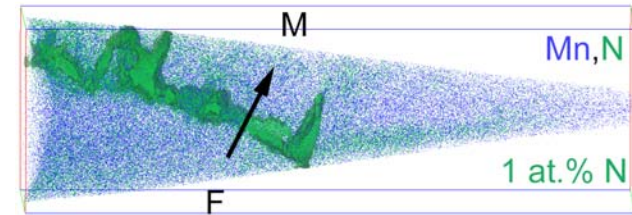
Review of Experimental Results

- There are several key points to remember about the experimental results:
 - The atom probe data shows segregation over a wide region.
 - We don't know the velocity of the interface.
 - We can only calculate an effective binding energy.



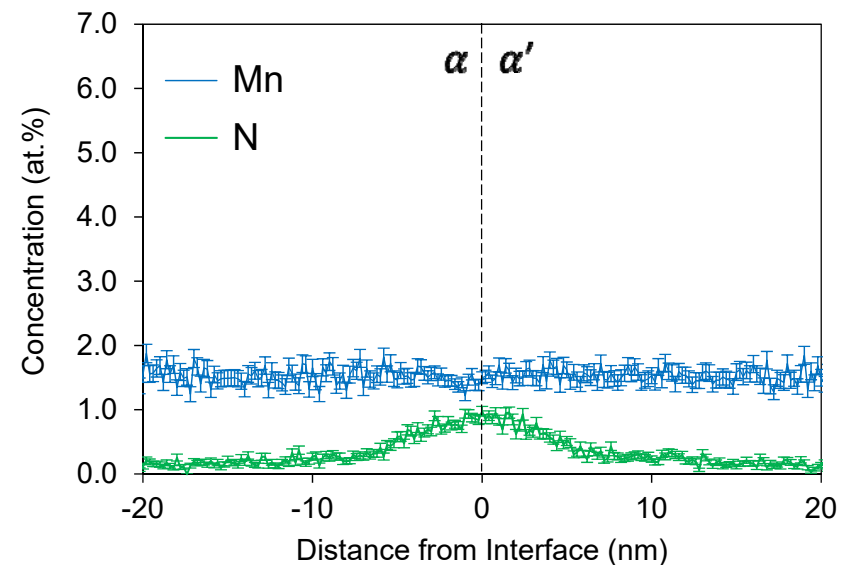
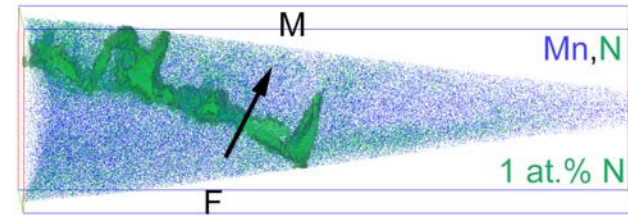
Review of Experimental Results

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Review of Experimental Results

- There are several key points to remember about the experimental results:
 - The atom probe data shows segregation over a wide region.
 - We don't know the velocity of the interface.
 - We can only calculate an effective binding energy.
 - In some systems, we see large variations in the measured enrichment.



Review of Experimental Results

<i>kJ/mole</i>	Austenite G.B.	Ferrite G.B.	Ferrite/Aust.
Mo	-15+/- 3 (Enomoto et al.)	-28 +/- 2 (Murayama & Smith)	-19 +/- 2 -25 +/- 3
Cr		-8 [Lejček & Hofmann]	-9 +/- 2 -18 +/- 3
Ni	Too small to measure (Enomoto et al.)		0 0 to -5
Mn	-8+/-3 (Enomoto et al.)	-8+/-4 (Kaufman)	-6 to -8 in Fe-Mn-C Less than 5 for Fe-Mn-N -10 to -15 for Fe-Mn-C
Si	-23+/-6 (Enomoto et al.)	-7 [Lejček]	Difficulty to determine, but appears to be repulsive in Fe-C-Si

Quaternary Systems

- Fe-Mn-Si-C:
 - Example of a system in which we expect strong interactions between substitutional elements.
 - Is also interesting because of the X-C interactions; Si-C repulsive, Mn-C attractive.

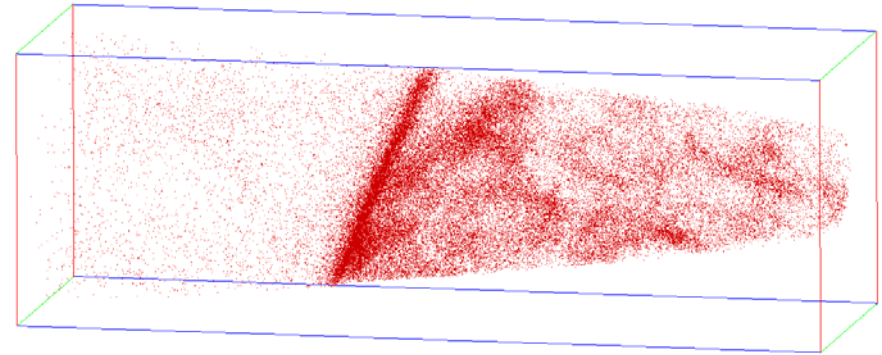
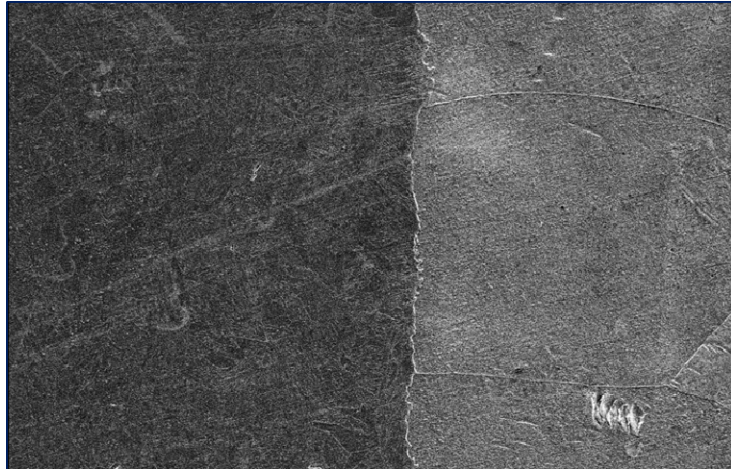
ϵ	Ferrite
C-C	6.5
Mn-Mn	-4.5
Si-Si	21.2
C-Mn	-7.5
C-Si	8.0
Mn-Si	-11.0

Interaction parameters @ 650C Guo et al.,
Met. Trans A, 37, 1721

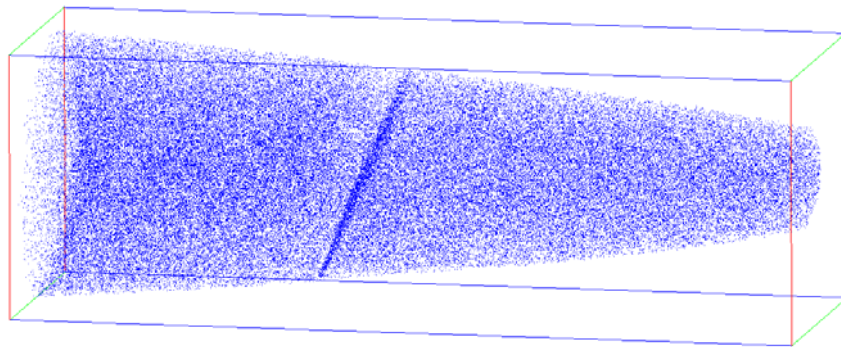
- Fe-Mn-Mo-C:
 - Example of a system in which we don't expect strong interaction between substitutional elements.

Fe-1.5wt%Mn-1.3wt%Si-0.7wt%C

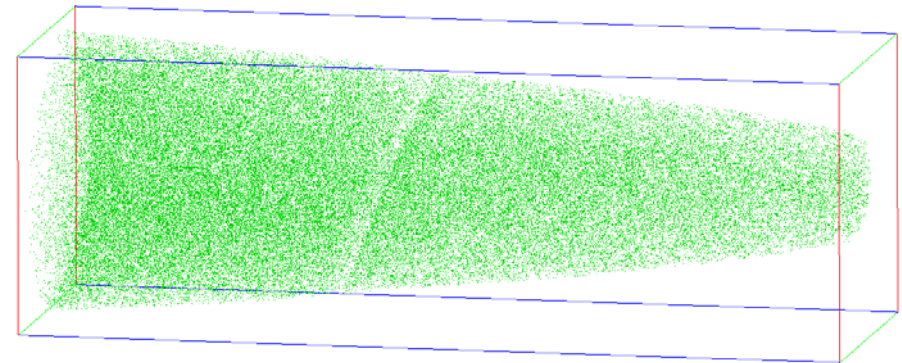
755°C for 16 minutes



C



Mn

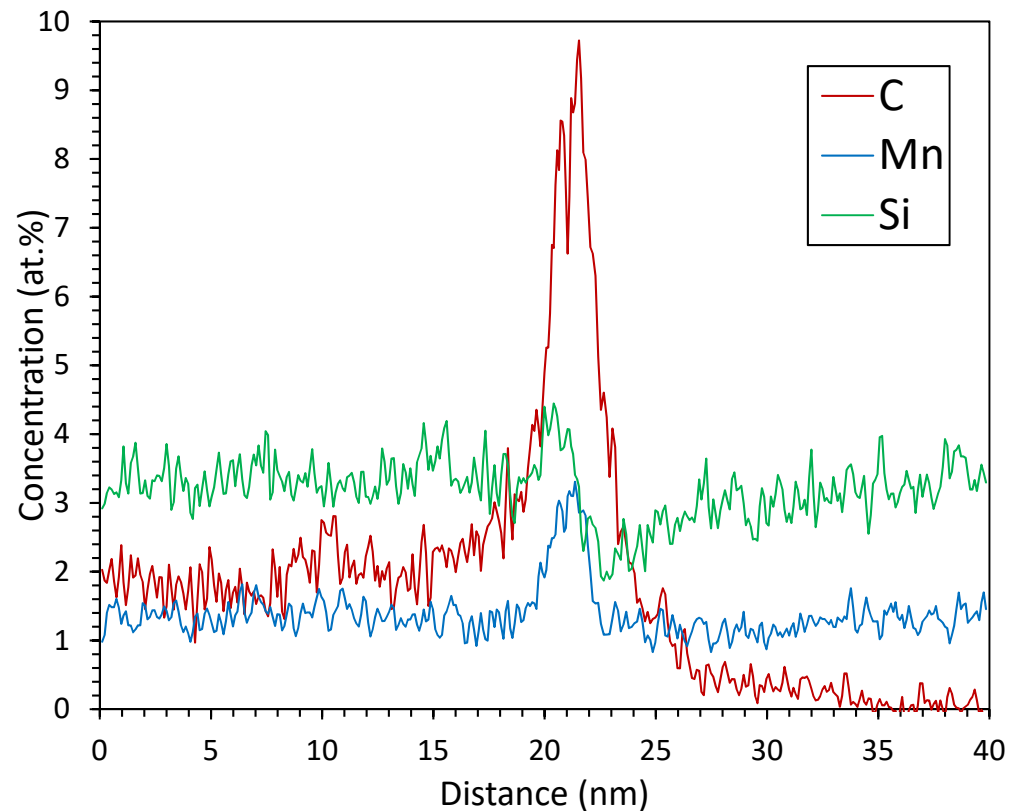


Si

Fe-1.5wt%Mn-1.3wt%Si-0.7wt%C

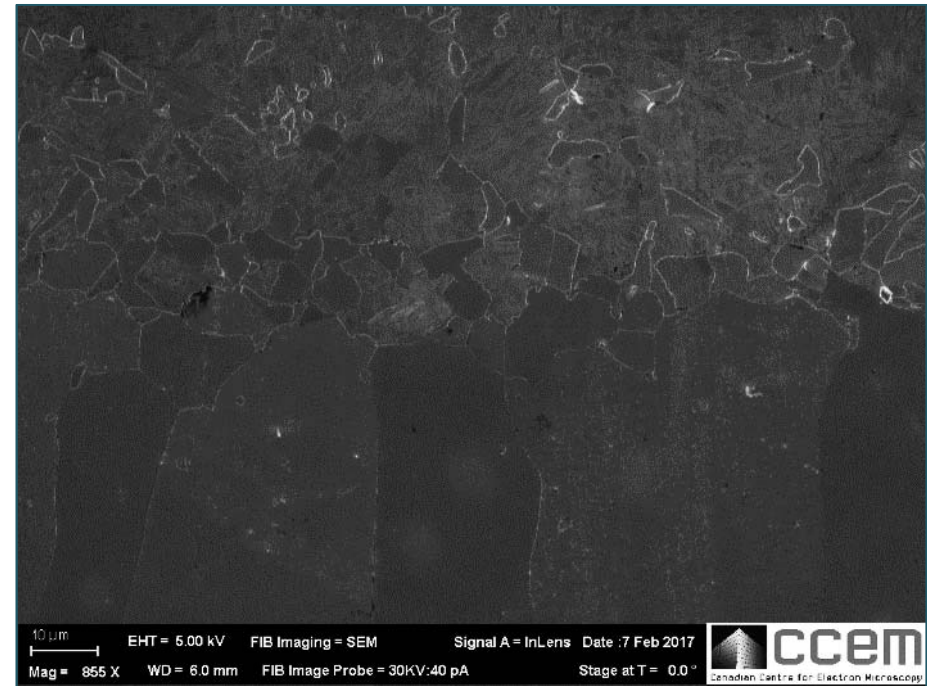
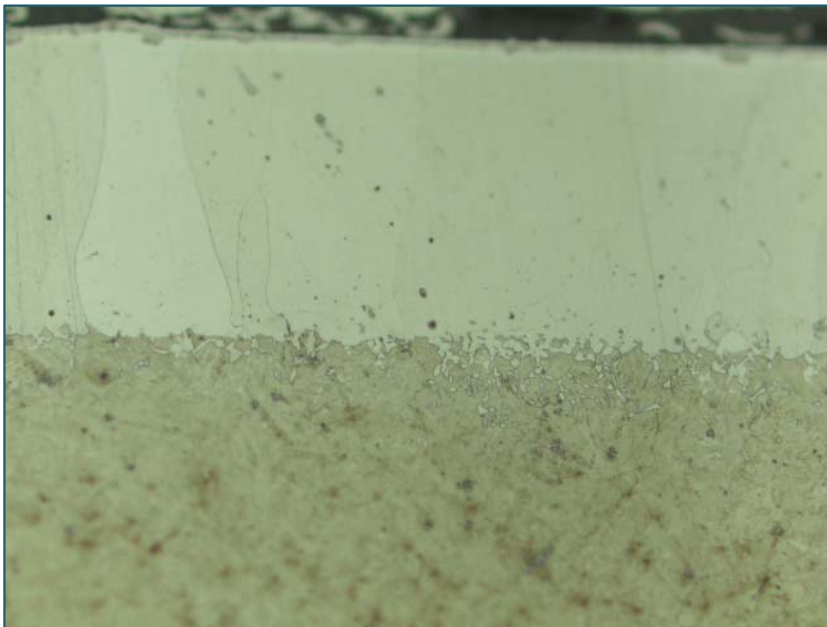
755°C for 16 min

- Si shows a complicated profile with possible desegregation on one side of the interface.
- Mn segregates to levels comparable to the ternary system.
- No evidence of Mn/Si co-segregation.



Fe-1.5wt%Mn-1.3wt%Si-0.7wt%C

755°C for 4 hours

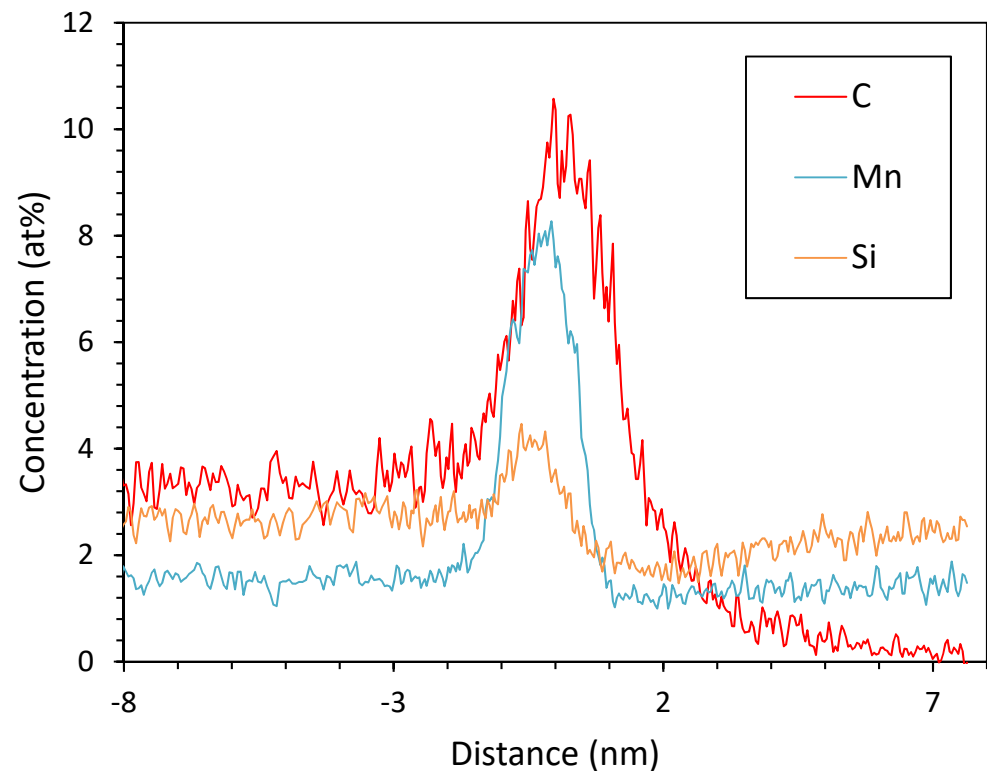


Many areas of the interface were not suitable for a liftout due to the roughness of the interface

Fe-1.5wt%Mn-1.3wt%Si-0.7wt%C

755°C for 4 hrs

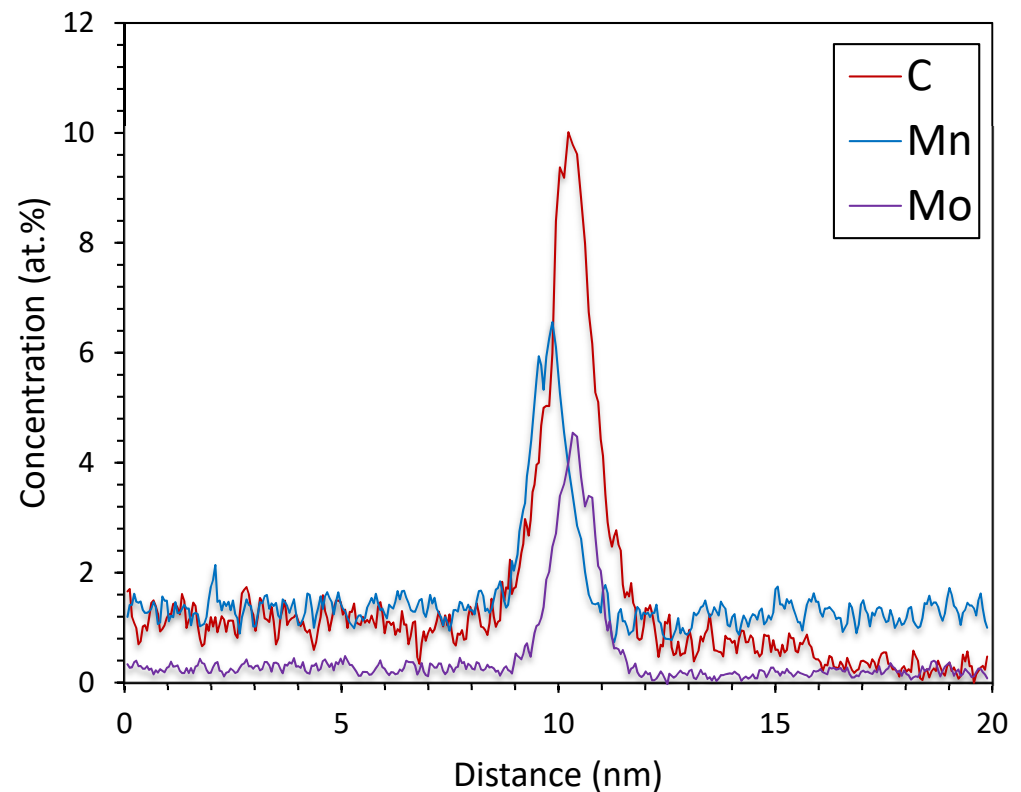
- Complex Si profile.
- Mn segregates stronger than previous sample.
- Could this unusually high value be due to Mn/Si interaction?



Fe-1.3%Mn-0.5%Mo-0.5%C

23.5 min at 755°C

- Mn segregation is similar to the ternary.
- Mo segregates more strongly than observed for the ternary.
- At longer times, both elements showed less segregation. We are repeating the measurements.





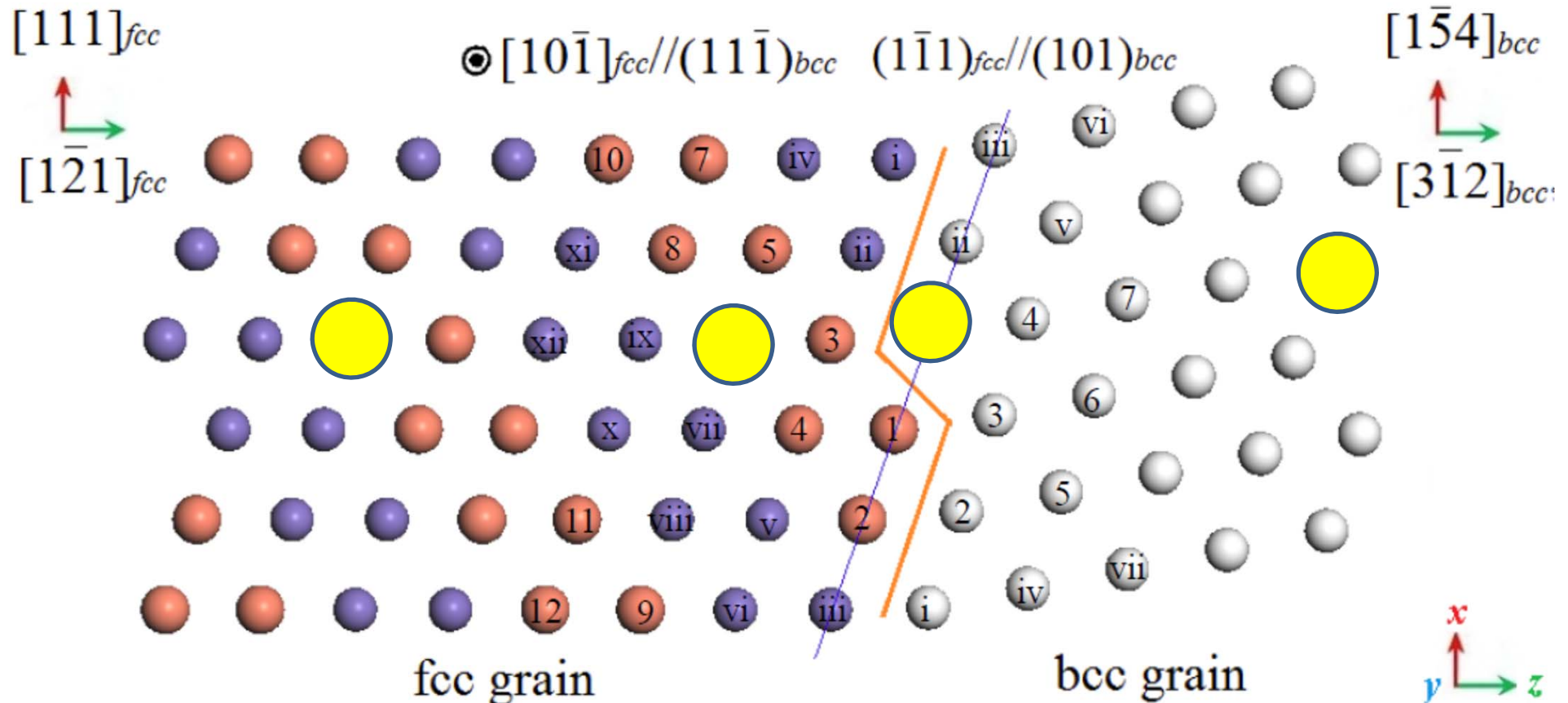
Density functional theory (DFT)

α - γ (bcc-fcc) interface in Fe

Ground state theory: $T = 0\text{K}$



K-S orientation relationship: $(111)_{fcc} \parallel (101)_{bcc}$, $[10\bar{1}]_{fcc} \parallel [1\bar{1}\bar{1}]_{bcc}$



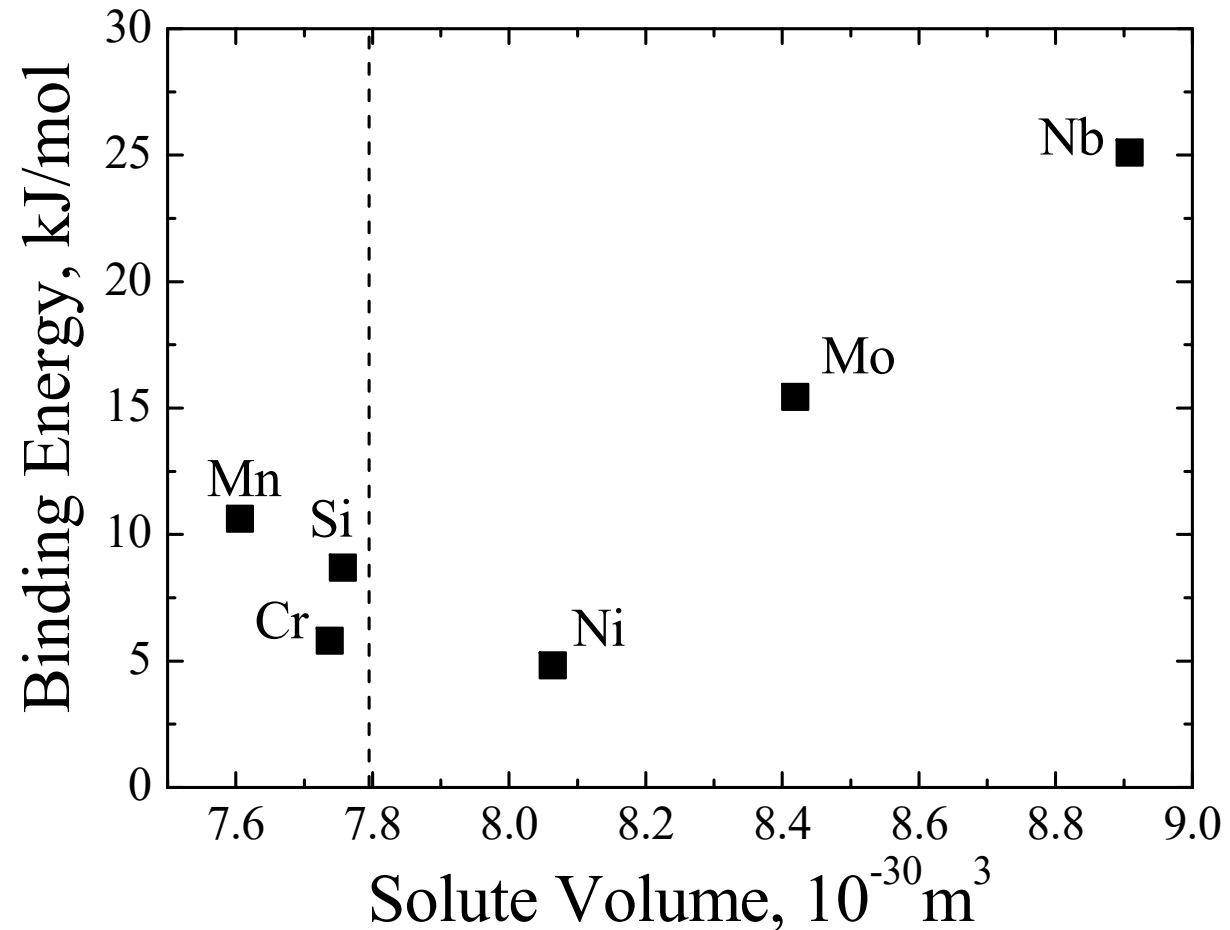
Double-layer antiferromagnetic



Binding energies with α – γ interface in Fe

Enrichment
factor for
500 – 800 °C

$$\frac{C_{\text{interface}}}{C_{\text{bulk}}} = \exp\left(-\frac{E}{kT}\right)$$



H. Jin (2018)

E...Representative binding energy that can be used for comparison with experiments where concentrations (i.e. enrichment factors) are measured



Comparison of APT and DFT results

Width of interface

DFT: approximately 1 nm

APT: approximately 2 – 5 nm

“chemical” width of interface due to co-segregation with C?

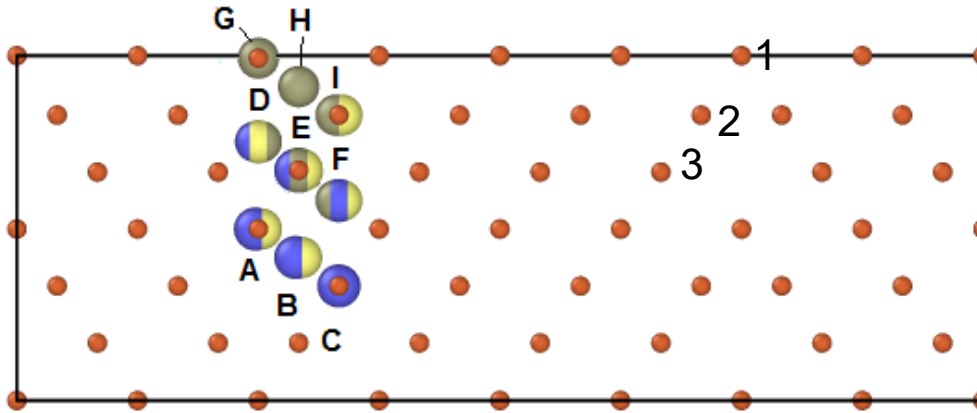
broadening of APT width due to interface structure (steps etc.)?

Binding energies (kJ/mol)

Element	DFT	APT
Mo	15	19 – 25
Mn	10 – 13	5 – 15
Cr	3	9 – 18
Ni	5	0 – 5



$\Sigma 3$ grain boundary as model case for Fe-C-Mn



Each substitutional site (1, 2, 3) is associated with 6 octahedral sites

Need to consider 18 C-Mn pairs

Mn – C co-segregation

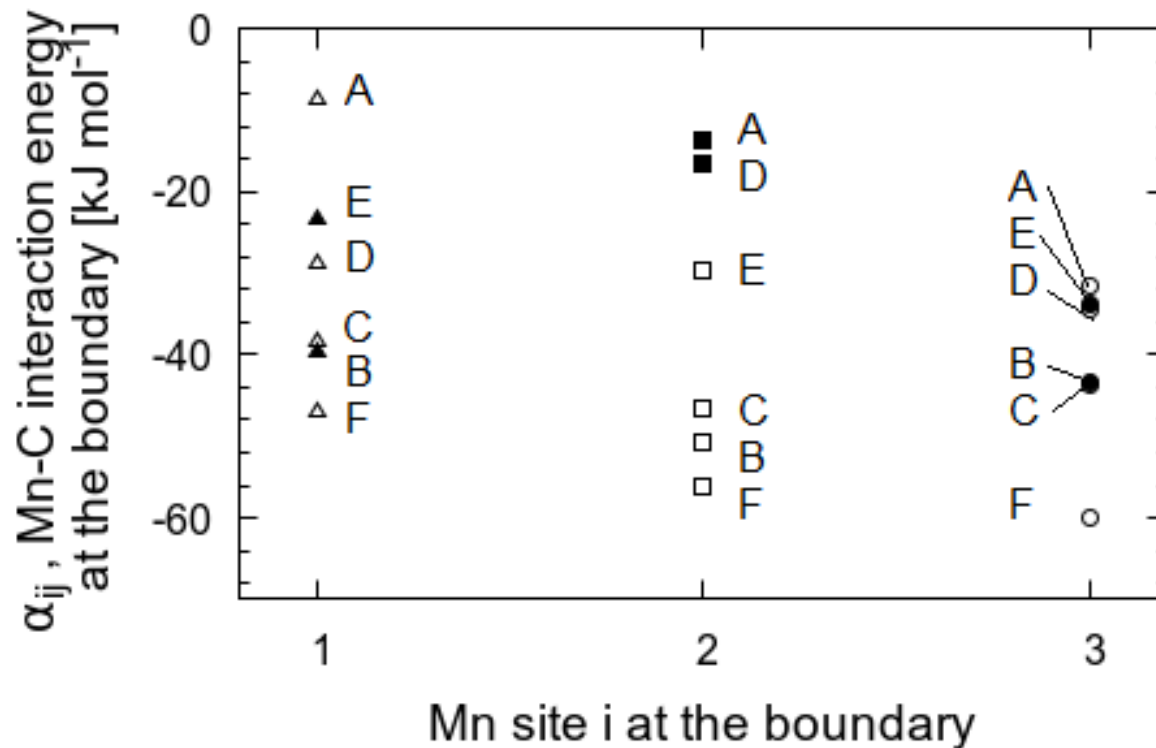
$$E_{Mn-C}^{ij} = E_{Mn}^i + E_C^j + \alpha_{ij}$$

Effective binding energy of Mn

$$E_{Mn}^{eff} = E_{Mn}^i + \alpha_{ij} X_C^j$$

$$X_C^j \sim 0.1:$$

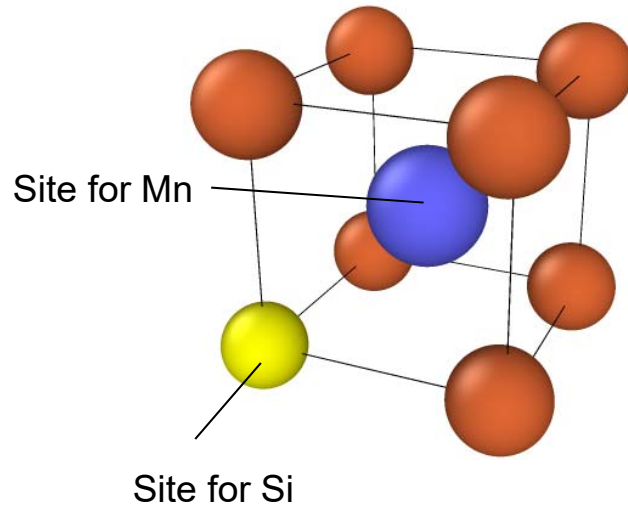
$$E_{Mn}^{eff} = E_{Mn}^i + (3 - 5) kJ/mol$$



T. Wicaksono (2017)



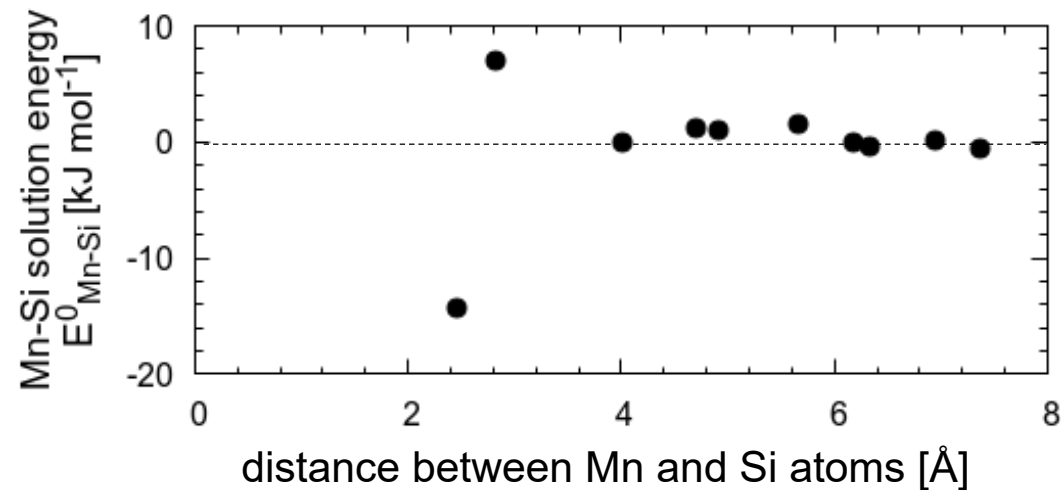
Mn-Si Interaction in bcc-Fe



$$E_{Mn-Si}^0(d_{Mn-Si}) = \left(E_{Mn-Si,total}^0 + E_{pure}^0 \right) - \left(E_{Mn,total}^0 + E_{Si,total}^0 \right)$$

$E_{X,total}^0$ = total energy of bulk cell with containing 1 X species

d_{Mn-Si} = distance between Mn and Si

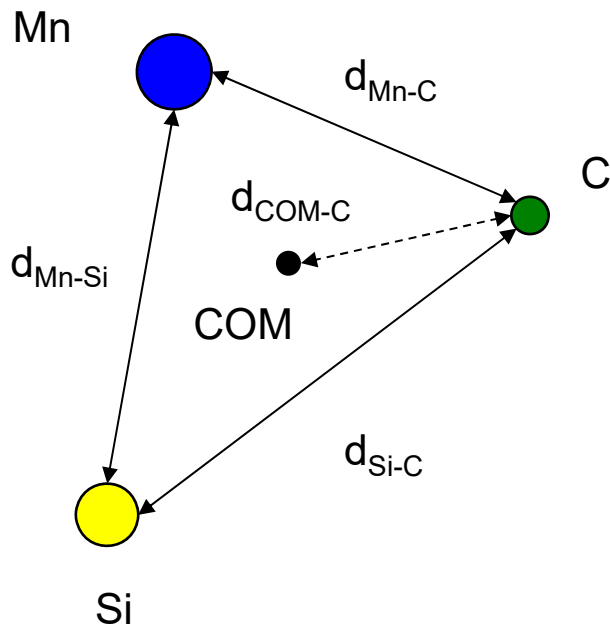




Interactions in Fe-C-Mn-Si

C-Mn attractive, C-Si repulsive in ternary system

$\Delta E_{MnSi \leftarrow \infty C}$ = Change in energy due to bringing a C atom from far away in the bulk bcc to the vicinity of Mn-Si pair



COM: center of mass

d_{Mn-Si} [Å]	d_{Mn-C} [Å]	d_{Si-C} [Å]	d_{COM-C} [Å]	$\Delta E_{(MnSi \leftarrow \infty C)}$ [kJ/mol]
2.45	1.42	2.00	0.82	+11
	1.42	3.47	1.57	-39
	2.00	1.42	0.82	+14
	2.00	3.17	1.57	-29
	2.00	4.25	2.06	-27
	3.17	2.00	1.57	+10
	3.17	3.47	2.06	-9
	3.47	1.42	1.57	+15
	3.47	3.17	2.06	+4
	4.25	2.00	2.06	+9

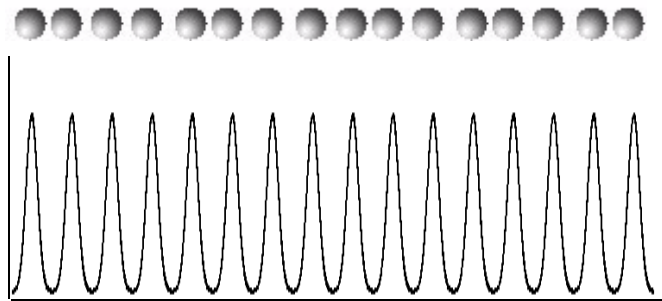
What about atomistic simulations of segregation kinetics and interface migration with appropriate diffusional timescales?



Alloy Diffusional Molecular Dynamics

Integrate over atomic vibrations

Instantaneous atom positions



Gaussian Distributions

Use EAM potentials to obtain free energy density

Application to Mg segregation in Al-Mg system

Evgeniya Dontsova

Jörg Rottler (Physics)

Chad Sinclair (Materials Eng.)

Al-10at%Mg



Al



Mg

Diffusional Molecular Dynamics

million's of atoms



Evgeniya Dontsova

Jörg Rottler (Physics)

Chad Sinclair (Materials Eng)

Formation of Crystal Defect

Diffusional Molecular Dynamics

million's of atoms



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

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Allow atoms to move

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Allow atoms to move

Diffusional Molecular Dynamics

The image shows a rectangular grid of small, semi-transparent blue circles representing atoms in a crystal lattice. The circles are arranged in a regular, repeating pattern. In the center of the grid, there is a small, irregular region where the circles are slightly more opaque and white, indicating a defect or a region of interest. The text "Allow atoms to move" is written in white in the upper right quadrant of the image.

Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics

The image shows a rectangular grid of small, semi-transparent blue circles representing atoms in a crystal lattice. The circles are arranged in a regular, repeating pattern. In the center of the grid, there is a rectangular region where the circles are slightly offset from their regular positions, creating a visible distortion or defect in the lattice structure. This region is approximately 10% of the total width and height of the image. The text "Allow atoms to move" is overlaid on the upper right portion of the lattice.

Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

Diffusional Molecular Dynamics



Allow atoms to move

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Diffusional Molecular Dynamics



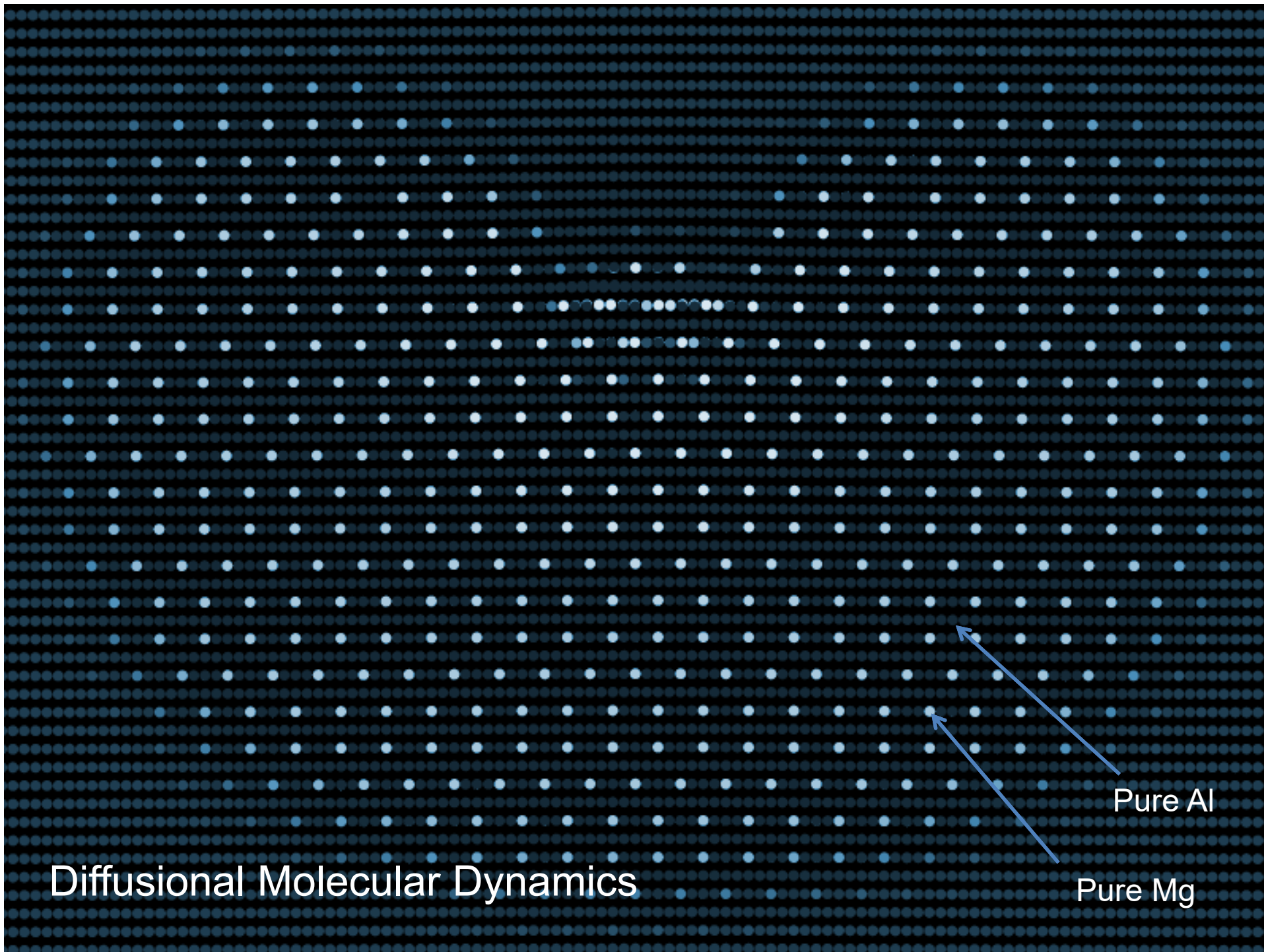
Allow atoms to move

Diffusional Molecular Dynamics

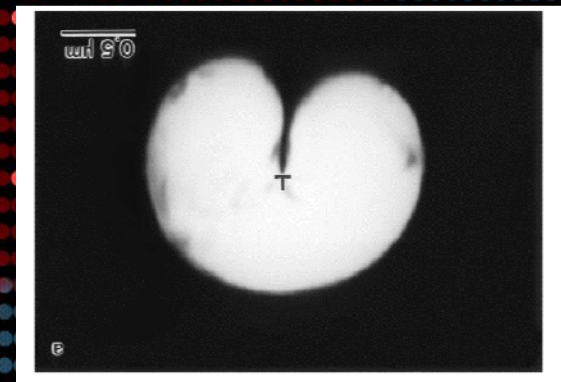


Allow atoms to move

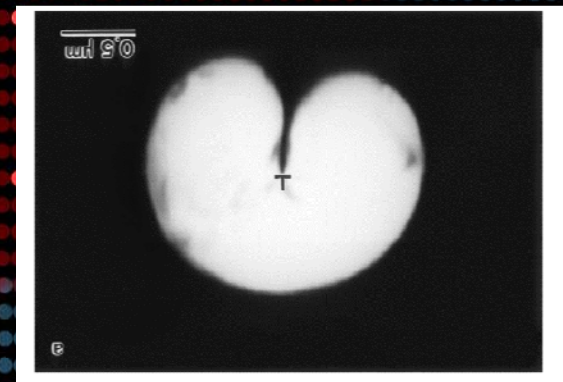
Diffusional Molecular Dynamics



Diffusional Molecular Dynamics

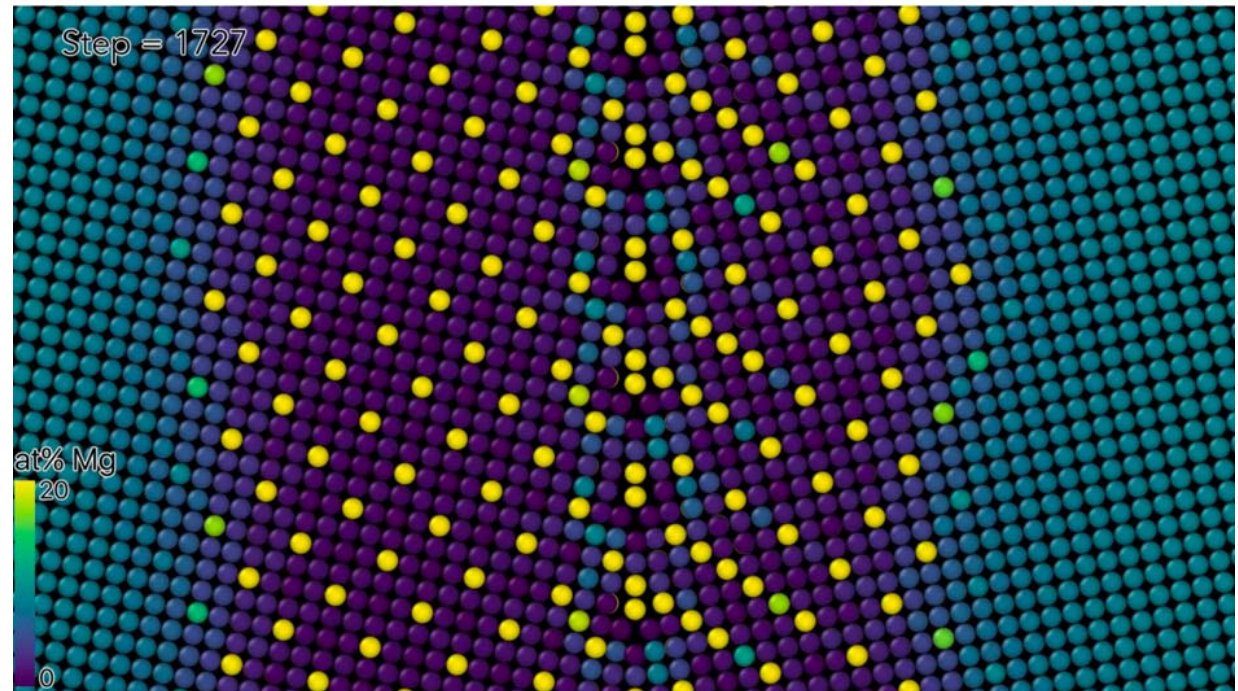
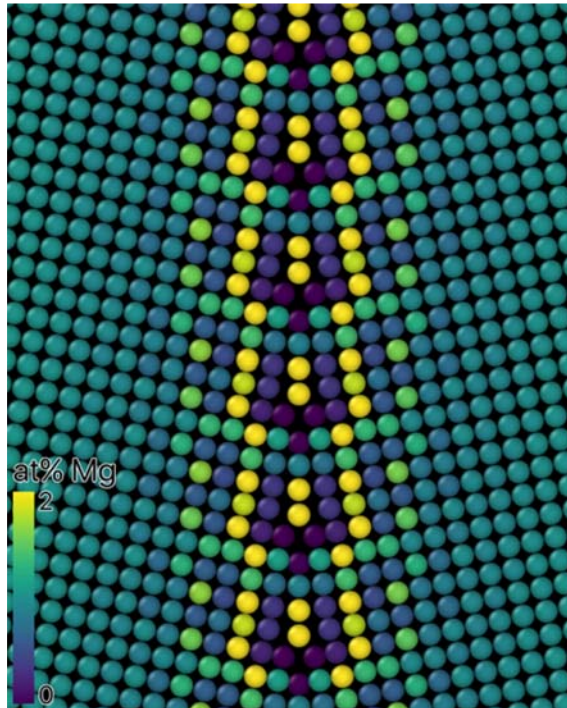


Diffusional Molecular Dynamics



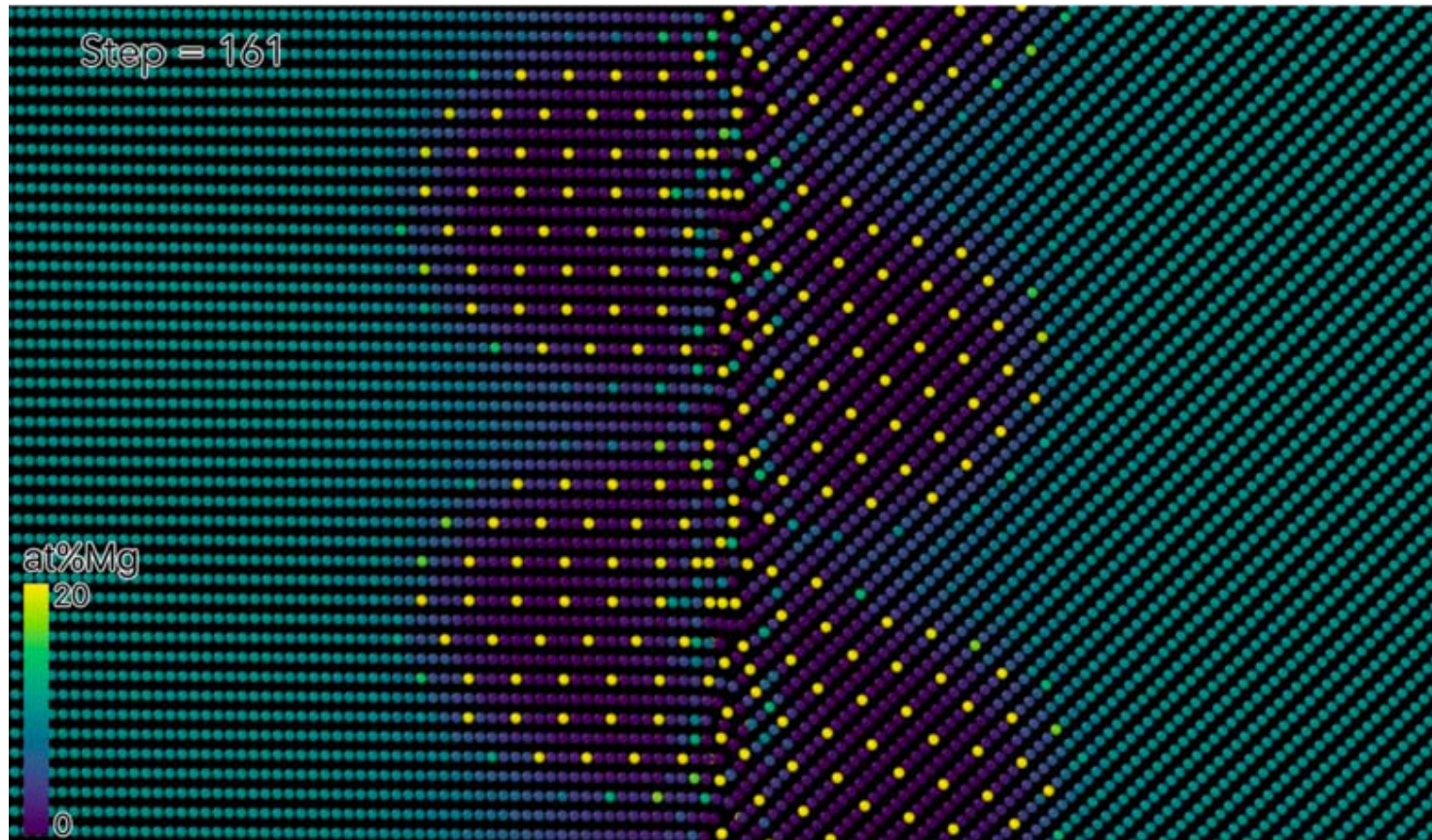


Mg segregation to symmetric tilt boundary





Mg segregation to asymmetric tilt boundary





Conclusions

- Trends of DFT simulations ($T=0\text{K!}$) consistent with experimental results (APT) for binding energies of alloying elements to the bcc-fcc interface in iron
- Extension of APT studies and DFT simulations to multi-component Fe systems in progress – initial results available for Fe-C-Mn-Mo, Fe-C-Mn-Si, Fe-C-Mn-Al
- Extension of atomistic simulations for segregation kinetics and interface migration at diffusional timescales using aDMD in addition to PFC