



3D Phase Field Modelling of the Austenite Decomposition

Matthias Militzer

**The Centre for Metallurgical Process Engineering
University of British Columbia
Vancouver, BC, Canada V6T 1Z4**

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**M.G. Mecozzi, J. Sietsma and S. van der Zwaag (TU Delft)
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Background

Phase Field Modelling

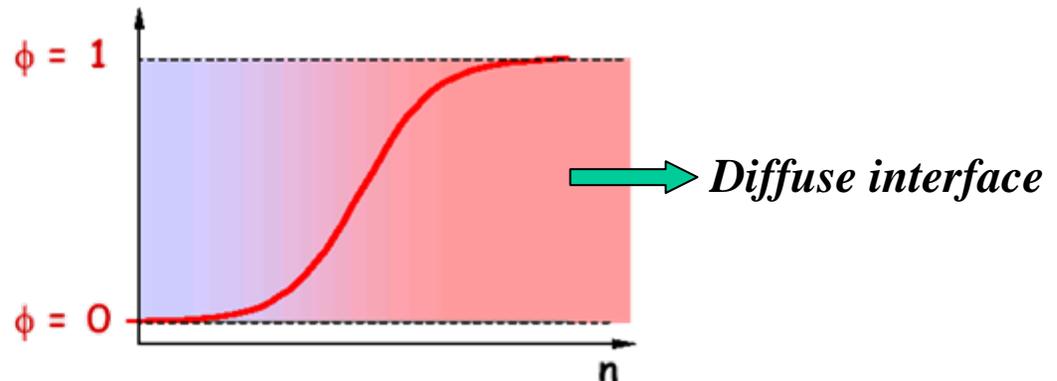
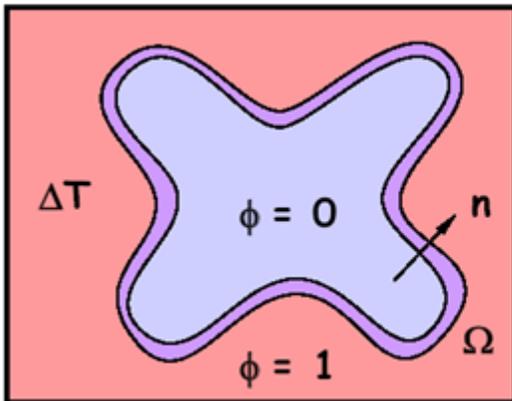
Modelling tool on the mesoscopic length scale

Phase field equation:

$$\frac{\partial \phi}{\partial t} = \mu \left\{ \sigma \left[\nabla^2 \phi - \frac{18}{\eta^2} (1 - \phi) \phi \left(\frac{1}{2} - \phi \right) \right] + \frac{6 \Delta G}{\eta} (1 - \phi) \phi \right\}$$

$\mu, \sigma, \Delta G$: Material parameters

η : Interface thickness



□ The phase field equation is coupled with the carbon diffusion equation to model the austenite/ferrite transformation



Background

PFM calculations of 3D phenomena frequently in 2D

3D PFM of austenite-ferrite transformation

⇒ Comparison with 2D results

⇒ Evaluation of 3D vs 2D calculations

Here, use of commercial code: **MICRESS with multi-phase field approach**

$$\frac{d\phi_i}{dt} = \sum_j \mu_{ij} \left[\sigma_{ij} \left(\phi_i \nabla^2 \phi_j - \phi_j \nabla^2 \phi_i + \frac{\pi^2}{2\eta_{ij}^2} (\phi_i - \phi_j) \right) + \frac{\pi}{\eta_{ij}} \sqrt{\phi_i \phi_j} \Delta G_{ij} \right]$$



Basic Assumptions

Investigated Case

- Fe-0.1wt% C-0.49wt% Mn
- Austenite grain size (EQAD) = 20 μ m
- Continuous cooling transformation (0.4 and 10K/s)

Assumptions

- Only carbon redistribution
- Carbon diffusion coefficients independent of carbon content
- Thermodynamics based on paraequilibrium
- Linearized phase diagram
- Carbon partitioning ratio in interface = equilibrium partitioning ratio



Parameters

Numerical parameters:

Interface thickness = 4 nodes, driving pressure averaging

Node size x and automatic time stepping such that convergency

Periodic boundary conditions

Maximum calculation domain size $165 \times 165 \times 165$ nodes

Physical parameters (adjustable):

Interface mobility (pre-exponential term, μ_0)

Nucleation conditions (temperature range, nuclei distribution)

⇒ Shield time, shield distance



Conversion 2D \rightarrow 3D

Grain sizes, nuclei densities

2D

$$N_0 \frac{\pi}{4} d^2 = fA$$

3D

$$N \frac{\pi}{6} (1.2d)^3 = fV$$

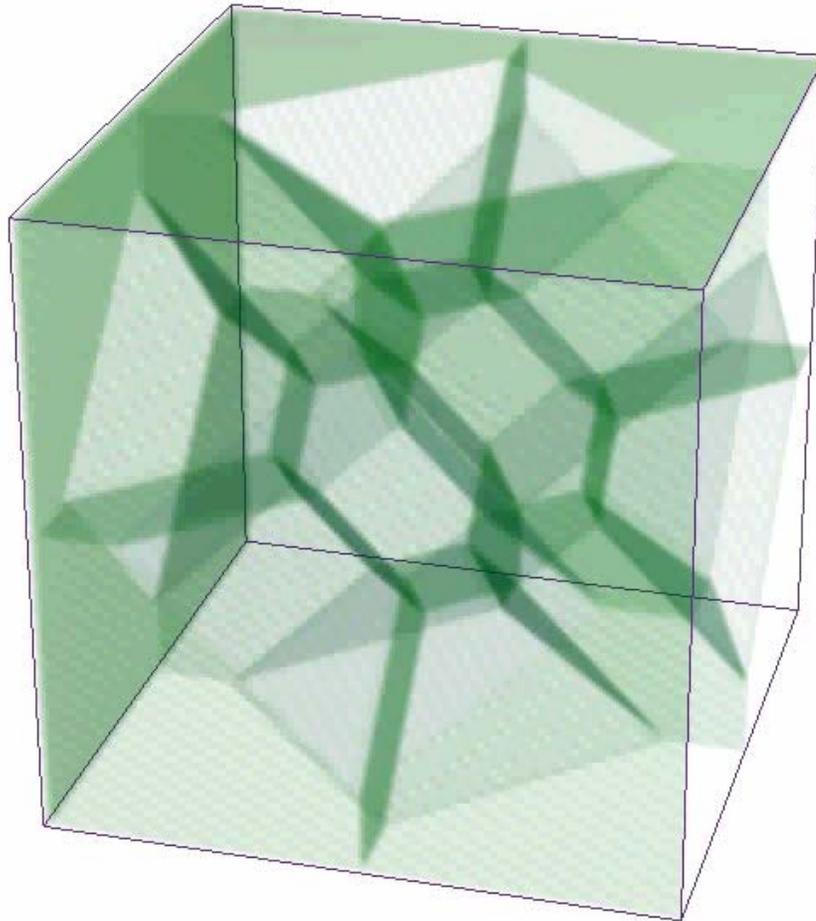
\Downarrow

$$\frac{N_0}{N} = \frac{2}{3} (1.2)^3 d \frac{A}{V}$$



Nucleation at Triple Lines

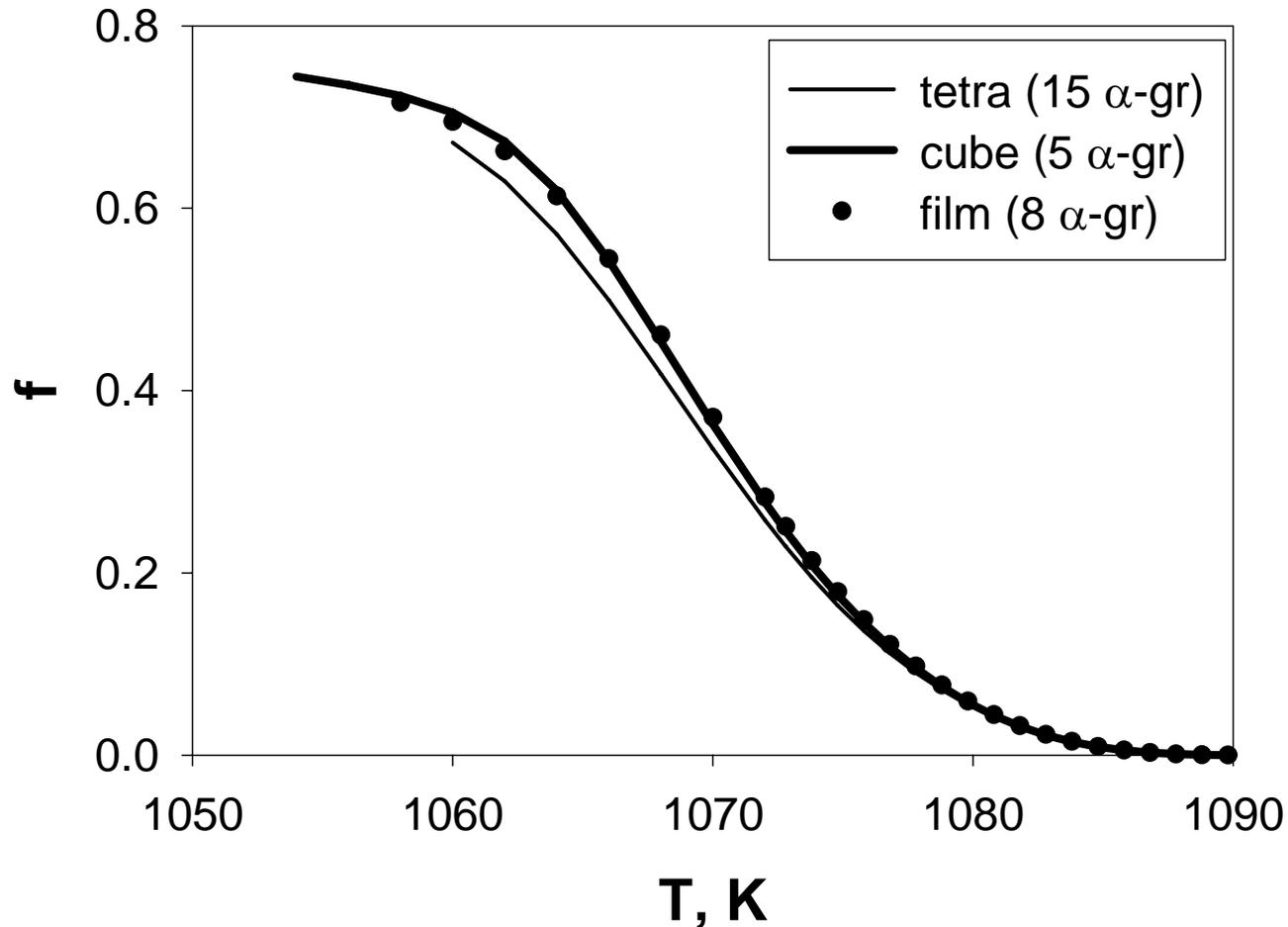
0.4 K/s: Ferrite grain size = Austenite grain size





Nucleation at Triple Lines

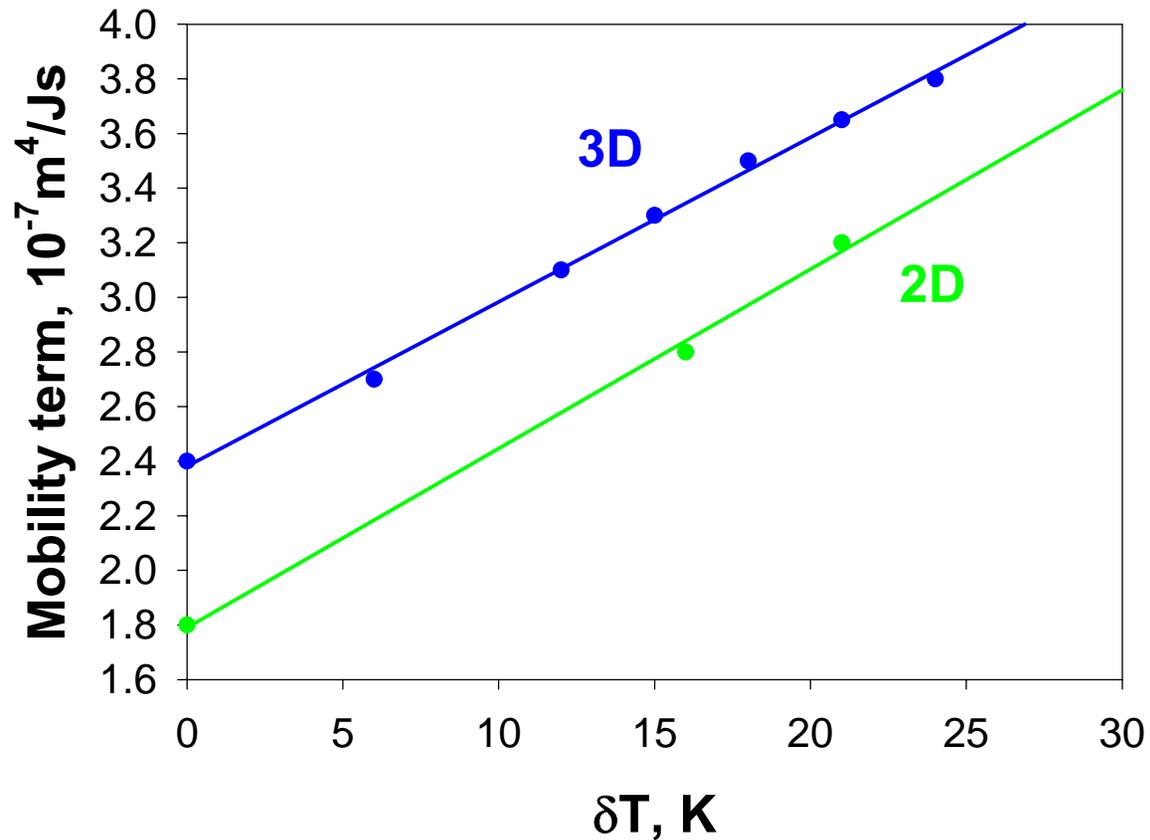
Effect of initial austenite microstructure





Nucleation at Triple Lines

3D vs 2D mobility results

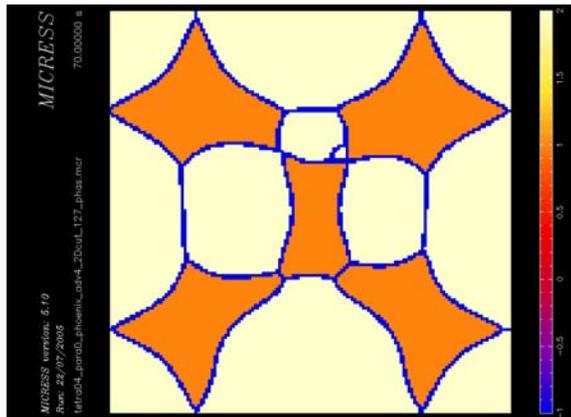
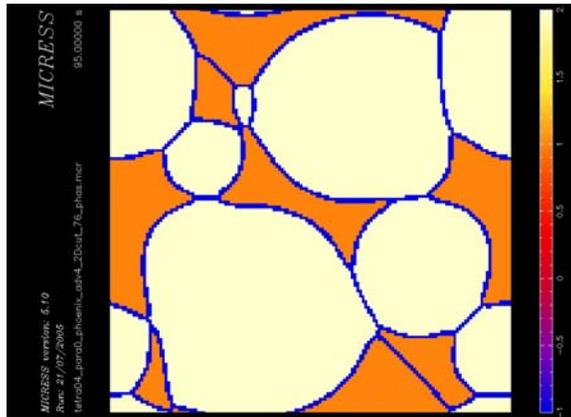




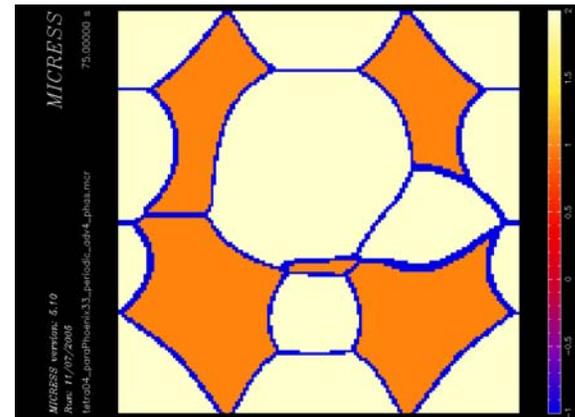
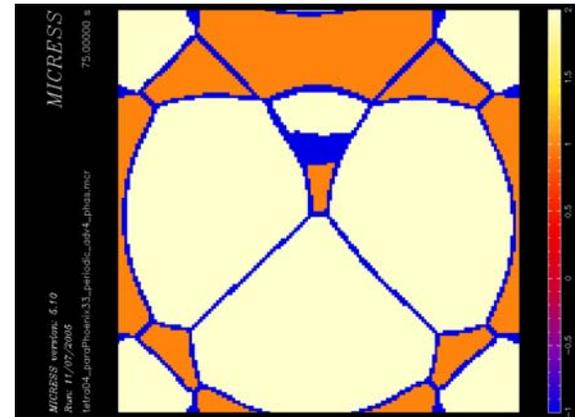
Nucleation at Triple Lines

Comparison 3D – 2D for $\delta T=18K$

2D



3D





TL + Interface Nucleation

10 K/s

Substantial ferrite grain refinement to 9 μm

⇒ Additional nucleation modes active

⇒ Nucleation at triple lines (TL) and **interfaces**

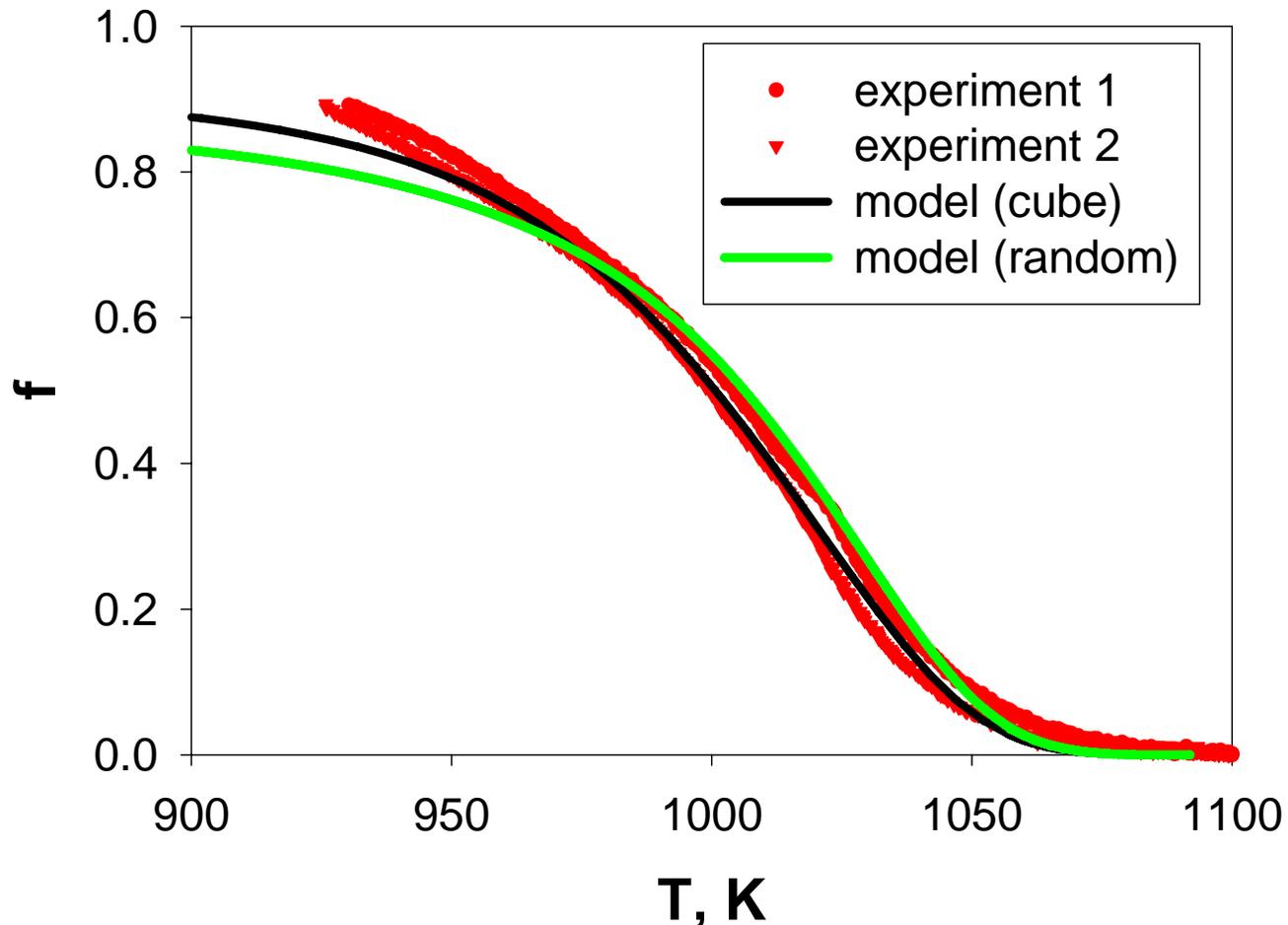
Transformation temperatures lower than for 0.4 K/s

⇒ Finer node size required (0.2 vs 0.3 μm)



TL + Interface Nucleation

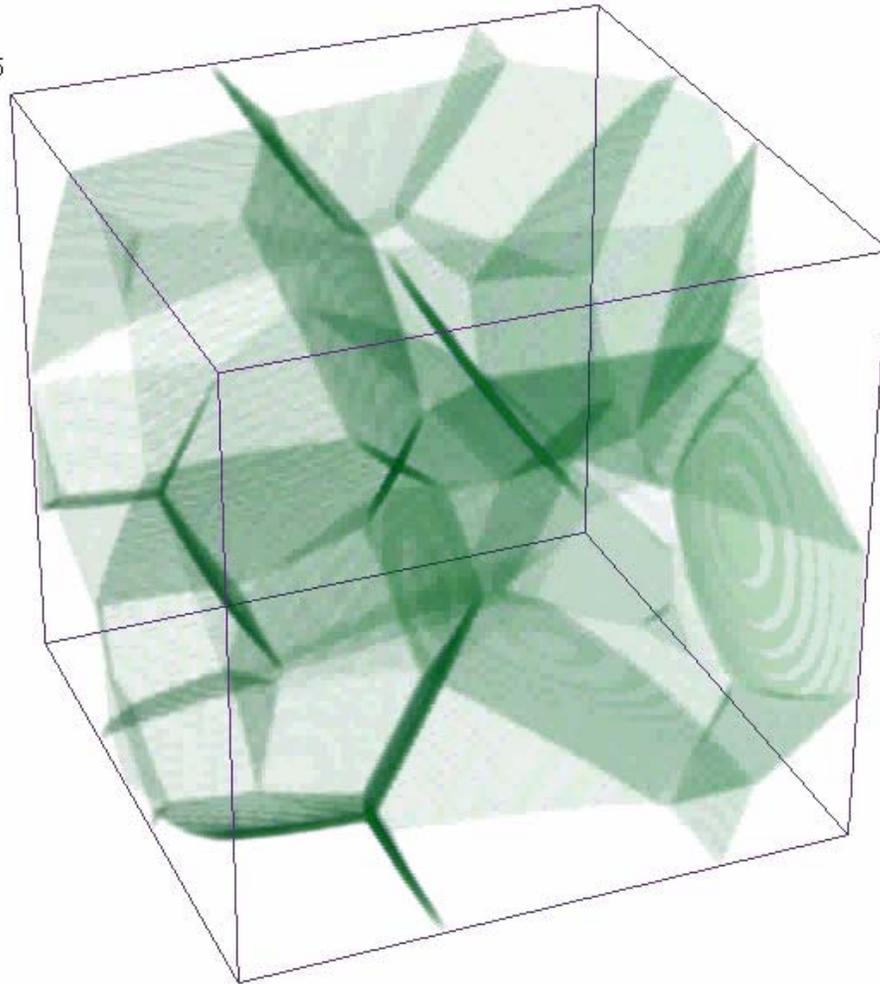
$\delta T = 16\text{K}/14\text{K}$ and $\mu_0 = 24 \times 10^{-7} \text{m}^4/\text{Js}$





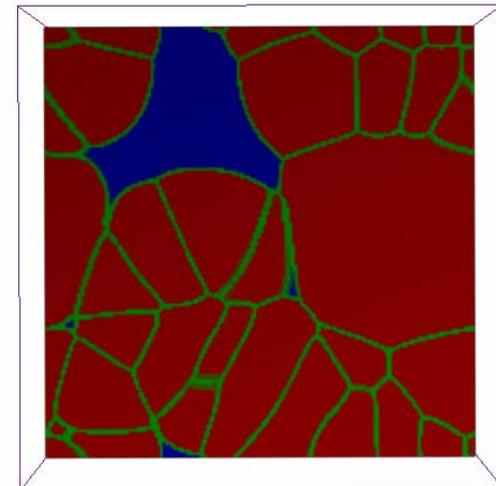
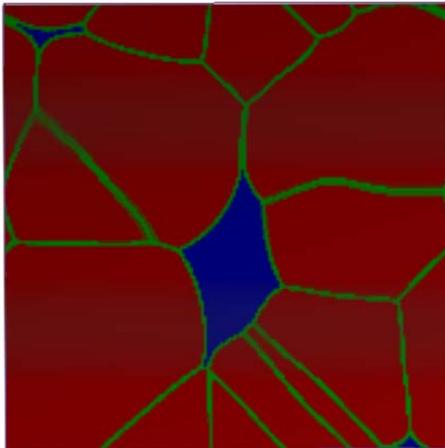
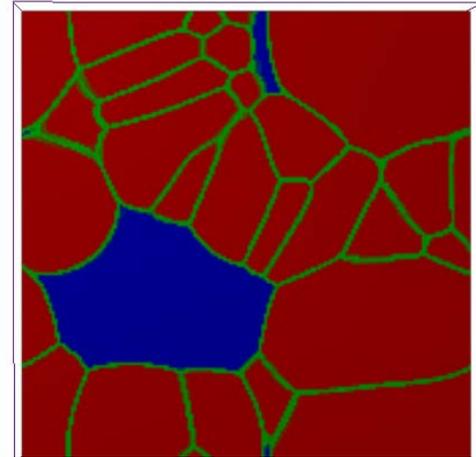
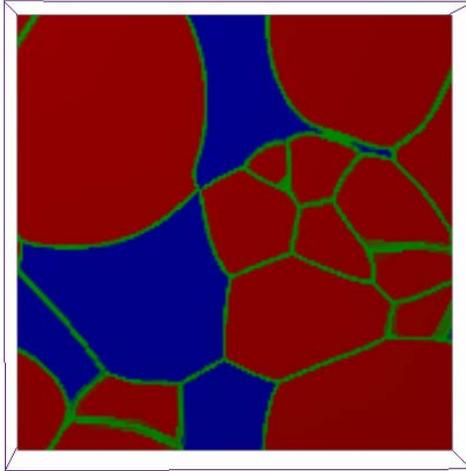
TL + Interface Nucleation

Time: 0
Frame nr: 1 of 100
Gridsize: 165 x 165 x 165





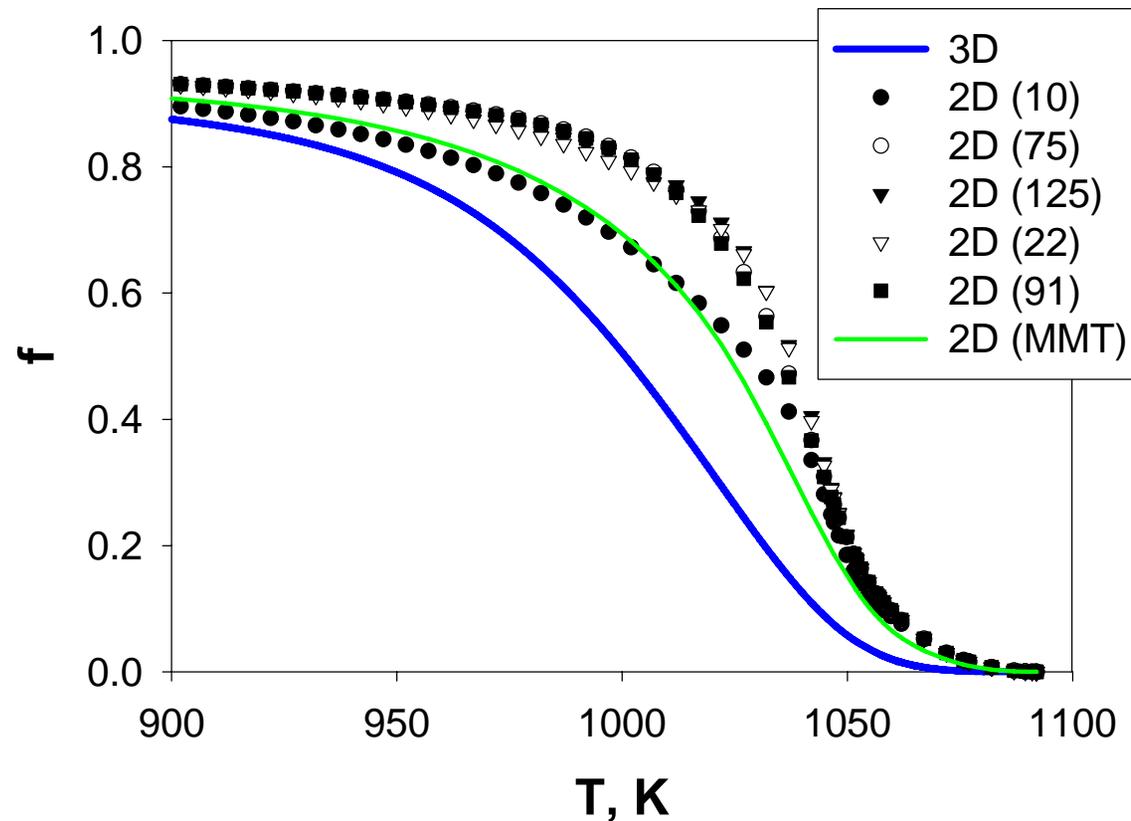
TL + Interface Nucleation





TL + Interface Nucleation

Comparison 3D – 2D for cube structure



Nucleation temperatures:

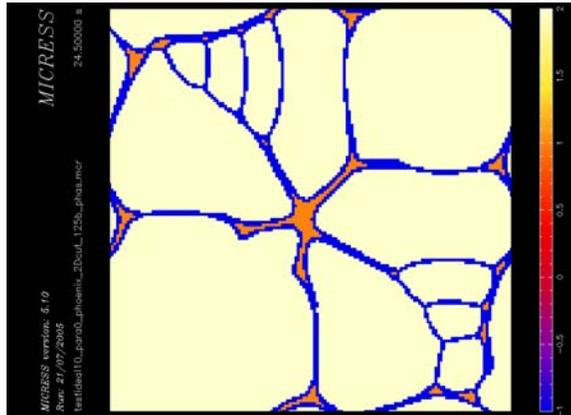
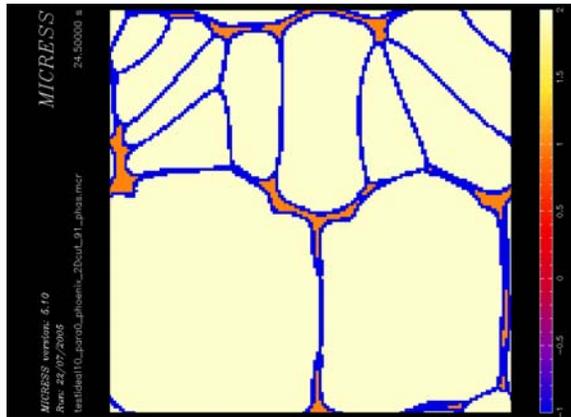
1092-1076 K (TP) + 1072-1057 K (interfaces)



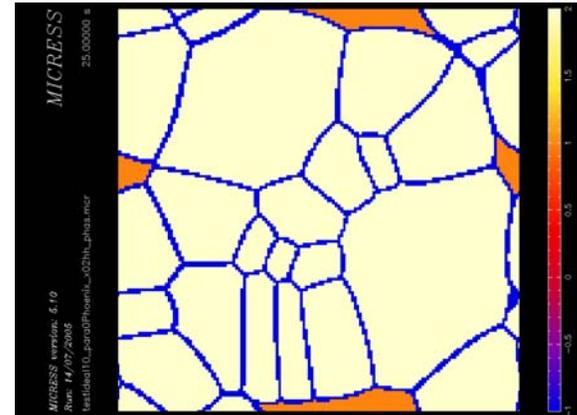
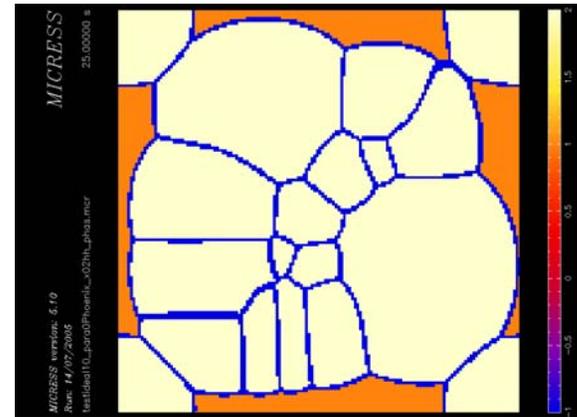
TL + Interface Nucleation

Comparison 3D – 2D

2D



3D

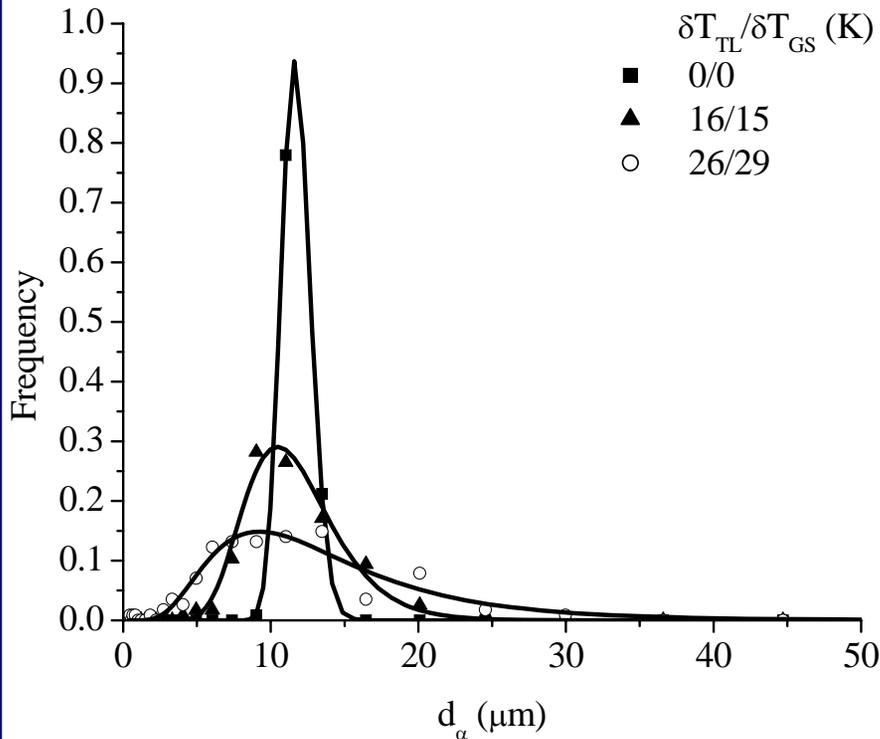




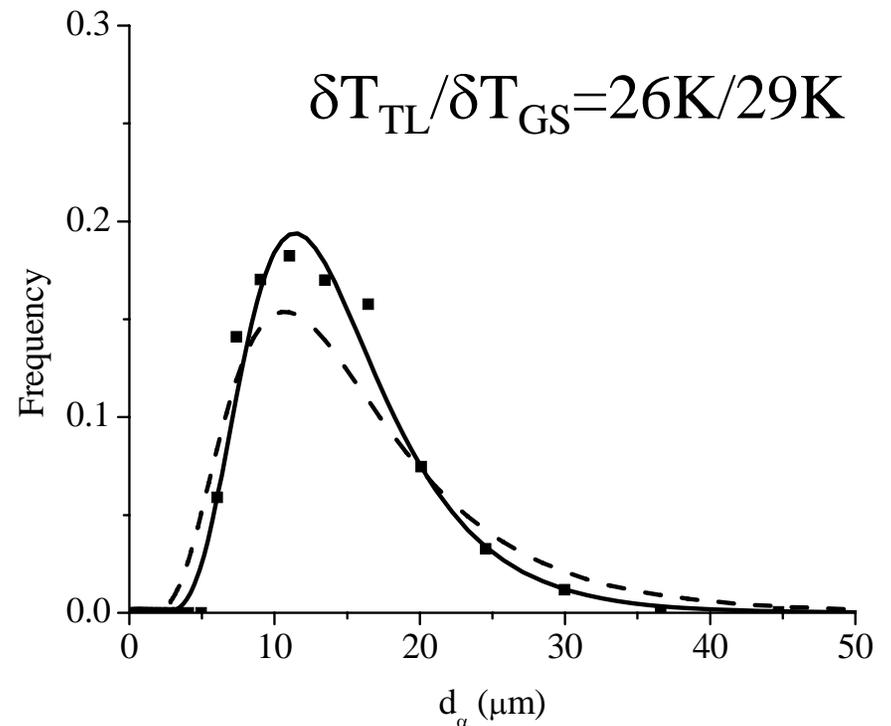
TL + Interface Nucleation

Use grain size distribution to determine μ_0 - δT combination

Simulation



Comparison with experiment





Summary

3D PFM predicts more realistic final microstructures

3D transformation “slower” than 2D due to different growth geometries

⇒ 3D mobilities approximately 30% larger

Challenges:

Control of complex nucleation modes with MICRESS

Intermediate microstructures (e.g. ferrite film)

Statistical relevance of 3D calculations



Ongoing/Future Work

Comparison of 3D PFM with single grain and spherical shell models

Analysis of mixed-mode character

Evaluation of temperature dependence of mobility

Application to deformation induced ferrite transformation

Application to austenite formation



Ongoing/Future Work

What can we learn from PFM?

- **Effective mobility as a function of nucleation conditions**
- **Evaluation of solute drag and/or diffusion of substitutional elements**
- **Transition from restrictive equilibria (e.g. paraequilibrium) to full equilibrium (orthoequilibrium)**



Ongoing/Future Work

Evaluation of Role of Alloying Elements

- $\gamma \rightarrow \alpha$ transformation: Connect PFM with solute drag model by describing effective mobility as a function of temperature and velocity
- $\alpha \rightarrow \gamma$ transformation: Considering long-range diffusion of substitutional elements in vicinity of interface (small domain size?, fast diffusion paths?)