

AKTU



B. Tech I-Year

Gateway O

Semester -I & II

Common to All Branches

BAS101 / BAS201: ENGINEERING PHYSICS

UNIT-3 (P-1) ONE SHOT : Wave Optics



Gateway Series for Engineering

- ✓ Topic Wise Entire Syllabus
- ✓ Long - Short Questions Covered
- ✓ AKTU PYQs Covered
- ✓ DPP
- ✓ Result Oriented Content



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B. Tech I-Year

Gateway Classes



BAS101 / BAS201: ENGINEERING PHYSICS

Unit-3

Introduction to : Wave Optics

Syllabus

Coherent sources, Interference in uniform and wedge shaped thin films, Necessity of extended sources, Newton's Rings and its applications, Introduction to diffraction, Fraunhofer diffraction at single slit and double slit, Absent spectra, Diffraction grating, Spectra with grating, Dispersive power, Resolving power, Rayleigh's criterion of resolution, Resolving power of grating.



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Engg. Physics

ONE SHOT



Unit-3 : Wave Optics

Interference



By Gulshan Sir

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One Shot PDF Notes Available On

Gateway Class Application

FREE

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AKTU : B.Tech (II-Sem & IV-Sem)



S.No	COMBO PACK
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2	B.Tech IV-SEM : CS, IT & C
3	B.Tech IV-SEM : EC & Allied
4	B.Tech IV-SEM : ME Allied
5	B.Tech IV-SEM : EE & EE Allied

Validity till semester exam

Helpline No. 7819 0058 53



AKTU : B.Tech (IV-Sem)



Engg. Maths-4 All Branch (except CE/ENV)

Validity till semester exam

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AKTU : B.Tech



- Video Lectures
- Pdf Notes
- DPP
- PYQs
- Unit wise One Shot

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Validity till semester exam

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Interference

- Coherent sources
- Interference in uniform and wedge shaped thin films
- Necessity of extended sources
- Newton's Rings and its applications

Diffraction

- Introduction to diffraction
- Fraunhofer diffraction at single slit and double slit
- Absent spectra, Diffraction grating, Spectra with grating
- Dispersive power, Resolving power, Rayleigh's criterion of resolution, Resolving power of grating

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Section – A

c. What happens if the slit is smaller than wavelength in diffraction pattern?

Section – B

c. Newton's rings are observed normally in reflected light of wavelength $6000\text{\AA}$. The diameter of the 10th dark ring is 0.50cm. Find the radius of curvature of lens and thickness of the film.

Section – C

5. Attempt any one part of the following:

- (a) Discuss the phenomenon of interference of light in parallel thin films and find the condition of maxima and minima. Show that the interference patterns of reflected and transmitted source of light are complementary.
- (b) Discuss single slit Fraunhofer diffraction and show that the relative intensities of successive maximum are nearly $1: 1/22: 1/62: 1/17$

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Section – A

d. What do you understand by coherent sources ?

Section – B

c. What do you understand by the phenomenon of Fraunhofer diffraction. Find out the ratio of intensities of successive secondary maxima compared to the intensity of principle maximum.

Section – C

5. Attempt any one part of the following:

(a)(i) Describe the phenomenon of interference in thin film (uniform thickness) due to reflected light and write down the conditions for constructive and destructive interference.

(ii) A light source of wavelength $6000\text{\AA}$ is used in a Newton's ring arrangement with plano – convex lens With radius of curvature equal to 100cm in a Newton's ring arrangement. Find out the diameter of the 15th dark ring.

(b) Explain briefly the Rayleigh criterion of resolution. Discuss the resolving power of plane transmission grating and find the relation between resolving and dispersive power of the grating.

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Section – A

- (d) Why two independent light sources cannot produce interference pattern?
- e. What are the changes that are caused in the diffraction pattern if the number of slits are made large?

Section – B

- (c) Describe how Newton's ring experiment can be used to determine the refractive index of a liquid.

Section – C

5. Attempt any one part of the following:

- (a) (i) Obtain an expression for the fringe width in λ – shaped thin film and explain nature of fringe pattern.
- (ii) A light of wavelength $6000\text{\AA}$ falls normally on a slit of width 0.10 mm . Calculate the total angular width of the central maximum.
- (b) (i) What particular spectra would be present if width of the transparencies and opacities of the grating are equal.
- (ii) A plane transmission grating has 16,000 lines to an inch over a length of 5 inches. Find in wavelength region of $6000\text{\AA}$, in the second order, the smallest wavelength difference that can be resolved.

Section – A

- g.** The light rays from two independent bulbs do not show interference. Give reason.
- h.** State the Rayleigh criteria of resolution.

Section – B

- d.** White light is incident on a soap film at an angle $\sin^{-1} \frac{1}{2}$ and the reflected light is observed with a spectroscope. It is found that two consecutive dark fringes correspond to wavelengths $6.1 \times 10^{-5} \text{ cm}$ and $6.0 \times 10^{-5} \text{ cm}$. If the refractive index of the film is $4/3$, calculate the thickness.

6. Attempt any one part of the following:

- (a)** What do you mean by a wedge-shaped film? Discuss the interference due to it and obtain the expression for the fringe width.
- (b)** Discuss the formation of Newton's rings. Show that the diameters of the bright rings are proportional to the square root of odd natural numbers.

Section – A

- g.** Why the center of Newton's ring in reflected system is dark?
- h.** Explain Rayleigh's criterion of resolution.

Section – B

- d.** Newton's rings are observed in reflected light of wavelength $6500 \text{ \AA}$. The diameter of 10th dark ring is 0.50 cm . Find the radius of curvature of the lens.

6. Attempt any one part of the following:

- (a)** What is Rayleigh criterion of resolution how increase the resolving power of a diffraction grating? Using Rayleigh criterion for justification show that the resolving power of grating is equal to nN , where n is the order of the spectrum and N is total no of lines on the grating.
- (b)** Discuss the phenomena of Fraunhofer diffraction at a single slit and show that the relative intensities of the successive maximum are in the ratio $1 : 4/9\pi^2 : 4/(25\pi^2) : 4/49\pi^2 : \dots$

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Section – A

- (g) Two independent sources of light cannot produce interference, why?
- h. State Rayleigh criterion of Resolution. Also define resolving power.

Section – B

- (d) Calculate the thickness of a soap bubble thin film that will show constructive interference in reflected light. The film is illuminated with light of wavelength $5000 \text{ \AA}$ and the refractive index of the film is 1.45.

6. Attempt any one part of the following:

- (a) Describe the formation of Newton's rings using monochromatic light. Show that in reflected light, the diameters of dark rings are proportional to the square roots of natural numbers.
- (b) What is a diffraction grating? Discuss the phenomenon of diffraction due to plane diffraction grating.

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Section – A

- f.** Two independent sources could not produce interference, why?
- g.** What is dispersive power of plane transmission grating?

Section – B

- d.** A plane transmission grating has 16,000 lines to an inch of length of 5 inches. Find in the wavelength region of $6000 \text{ \AA}$, in the second order (i) the resolving power of grating and (ii) the small wavelength difference that can be resolved.

6. Attempt any one part of the following:

- (a)** Describe and explain the formation of 'Newton's rings' in reflected monochromatic light. Deduce the necessary expression for bright and dark rings.
- (b)** Discuss the phenomenon of Fraunhofer diffraction at a single slit. Show that the intensity of the first subsidiary maximum is about 4.5% of the principal maximum.

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B. Tech : Engg. Physics



Unit : Wave Optics



(Interference)

Lecture 1

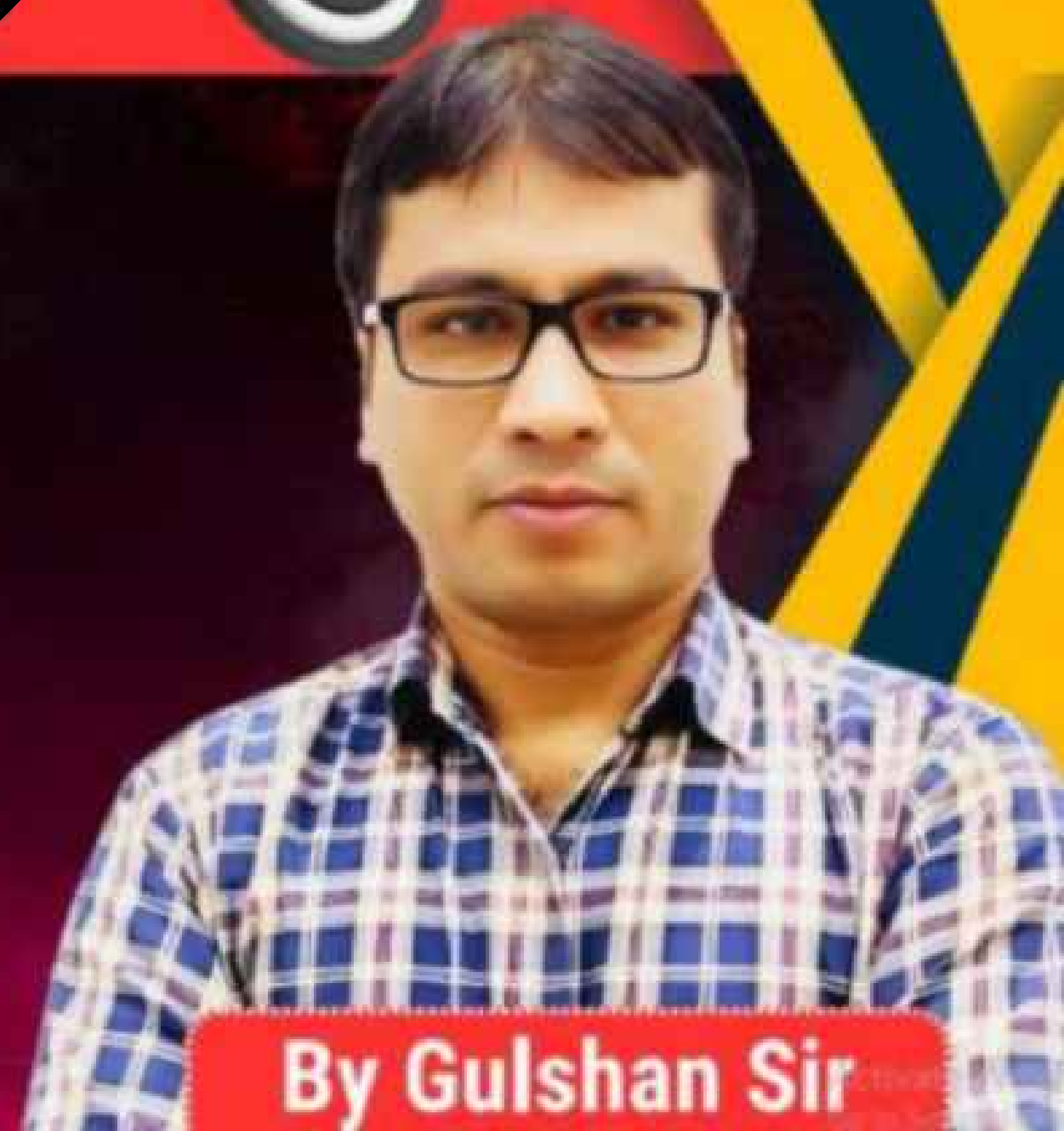
Today's Target

✓ Introduction to Wave optics

✓ DPP

✓ PYQs

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By Gulshan Sir

Interference of light

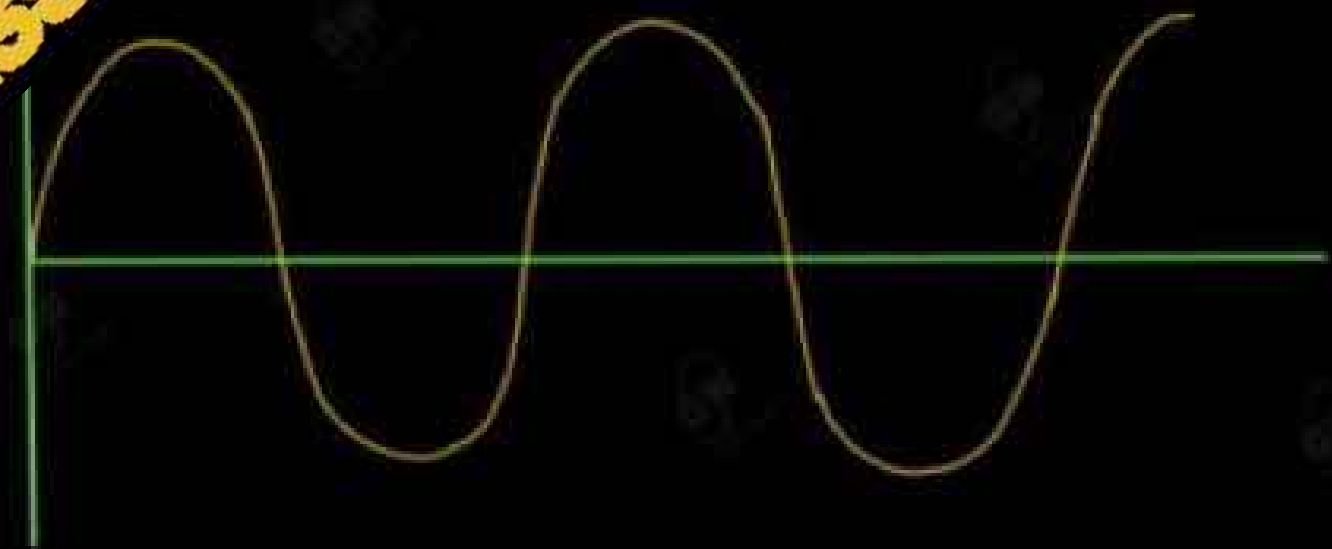
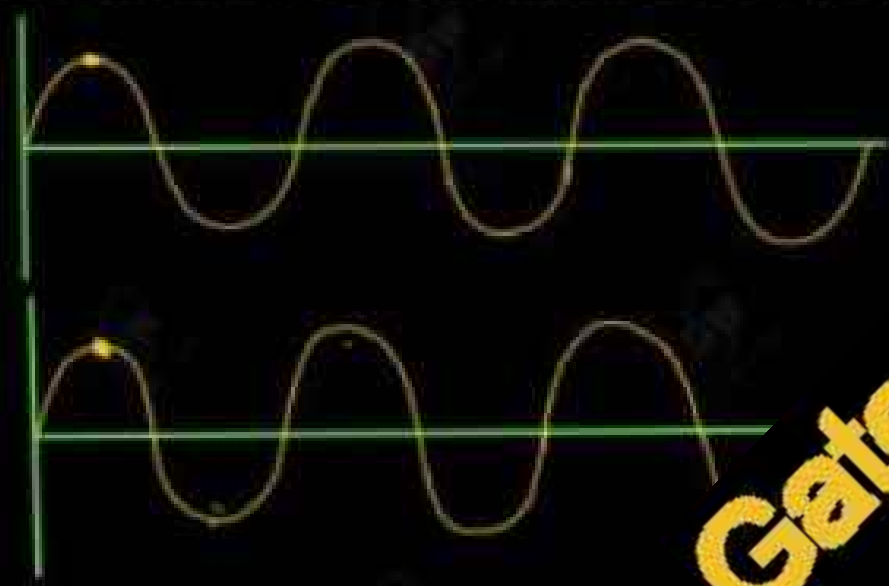
It is the phenomena of redistribution of intensity of light on account of superposition of light waves coming from the two Coherent sources of light (i.e. same frequency, constant phase difference)

Types of Interference

(i) Constructive interference (Bright or Maxima)

At those points of the medium where the two interfering waves reach in phase, the resultant displacement and hence the resultant intensity is the Maximum. These points are called Maxima and this interference is called Constructive interference.

(crest + crest) or (trough + trough] → constructive



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(ii) Destructive interference (Dark or Minima)

At those points of the medium where the two interfering waves reach in **opposite** phase, the resultant displacement and hence the resultant intensity become zero. These points are called Minima and this interference is called Destructive interference.



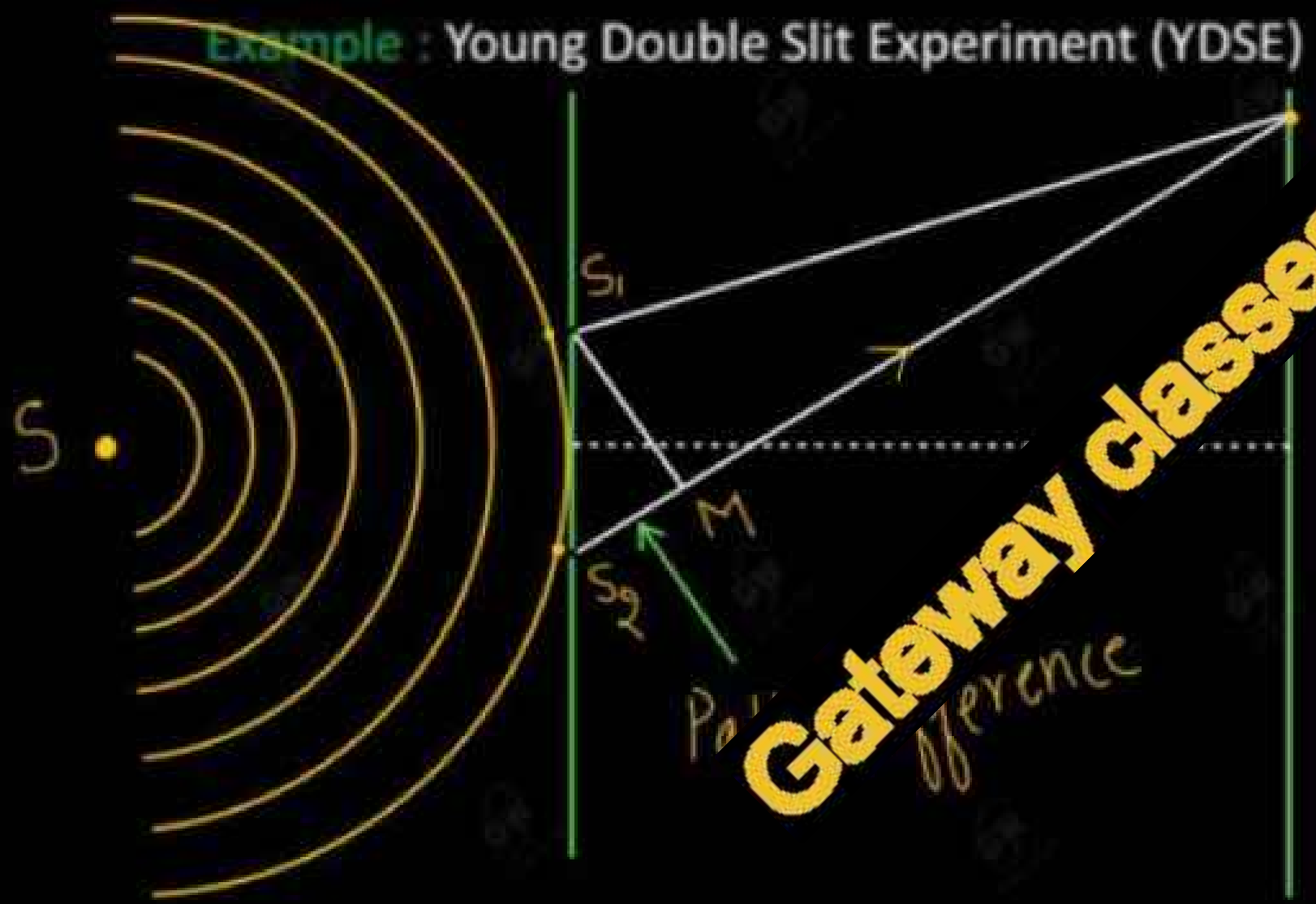
Coherent Sources

v. imp.

- The sources of light emitting waves of same frequency having zero or constant phase difference are called coherent sources.
- The sources of light emitting waves with a random phase difference are called incoherent sources.

Note : For interference Phenomenon, the sources must be coherent.

Example : Young Double Slit Experiment (YDSE)



Path Difference = $\frac{\lambda}{2\pi}$ Phase Difference

$$\Delta x = \frac{\lambda}{2\pi} \phi$$

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Two independent sources can not produce interference. Why ?

OR

Two independent sources of light can not be coherent

- Two independent sources of light can not be coherent because two independent beams of light do not have constant phase difference. Light is emitted from millions of excited atoms or molecules whose vibrations are independent of each other.
- Hence, two independent sources of light can not produce interference.

V. imp.
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Types of Interference on the basis of source formation

Based on the formation of two Coherent sources, interference are of two types

(i) Division of wave front

Coherent sources are obtained by dividing the wave front, originating from a common source

- Young's Double Slit Experiment (YDSE)
- The Fresnel's Double mirror method
- Lloyd's mirror method

(ii) Division of Amplitude

In this method, the amplitude of incident beam is divided in to two or more parts either by partial reflection or refraction.

- The interference in thin film
- The interference in Wedge shaped thin film
- Newton's ring

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Resultant intensity due to superposition of two interfering waves

Let a_1 and a_2 are amplitude of interfering waves and ϕ is the phase difference at a point under consideration, then resultant intensity at a point in the region of superposition

$$y_1 = a_1 \sin \omega t$$

$$y_2 = a_2 \sin(\omega t + \phi)$$

Apply Principle of Superposition

$$y = A \sin(\omega t + \phi)$$

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \phi$$

$$I = KA^2$$

$$I_1 = Ka_1^2$$

$$I_2 = Ka_2^2$$

$$KA^2 = Ka_1^2 + Ka_2^2 + 2Ka_1a_2 \cos \phi$$

$$I = I_1 + I_2 + 2\sqrt{I_1I_2} \cos \phi$$

Intensity $\propto$ (Amplitude)²

$$I \propto A^2$$

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OR

Condition for Maxima

$$I = I_1 + I_2 + 2I_1 I_2 \cos \phi$$

Intensity will be maximum, when

$$\cos \phi = 1$$

$$\phi = 2n\pi, \quad n = 0, 1, 2, 3, \dots$$

(i) Phase Difference

$$\phi = 2n\pi$$

(ii) Path Difference

$$\Delta x = 2n \left(\frac{\lambda}{2} \right) \quad n = 0, 1, 2, 3, \dots$$

OR

Condition for Minima

$$I = I_1 + I_2 + 2I_1 I_2 \cos \phi$$

Intensity will be minimum, when

$$\cos \phi = -1$$

$$\phi = (2n+1)\pi, \quad n = 0, 1, 2, 3, \dots$$

$$\phi = (2n-1)\pi, \quad n = 1, 2, 3, \dots$$

(i) Phase Difference

$$\phi = (2n+1)\pi \text{ OR } \phi = (2n-1)\pi$$

(ii) Path Difference

$$\Delta x = (2n+1) \frac{\lambda}{2} \quad n = 0, 1, 2, 3, \dots$$

$$\Delta x = (2n-1) \frac{\lambda}{2} \quad n = 1, 2, 3, \dots$$

Condition for sustained interference

VIMP

- Two sources of light should emit light continuously
- The light waves should be of same wavelength
- The light waves should be of same amplitude
- The light waves should be of same frequency
- The two waves must be in same phase or bear a constant phase difference.
- For constructive interference

$$I_{\max} = I_1 + I_2 + 2\sqrt{I_1 I_2}$$

- For destructive interference

$$I_{\min} = 0$$

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Q.1 Write the main condition for sustained interference.

Q.2 What do you understand by Coherent sources ?

Q.3 Why two independent light sources can not produce interference pattern ?

Q.4 The light rays from two independent bulbs do not show interference. Give reason

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B. Tech : Engg. Physics



Unit : Wave Optics

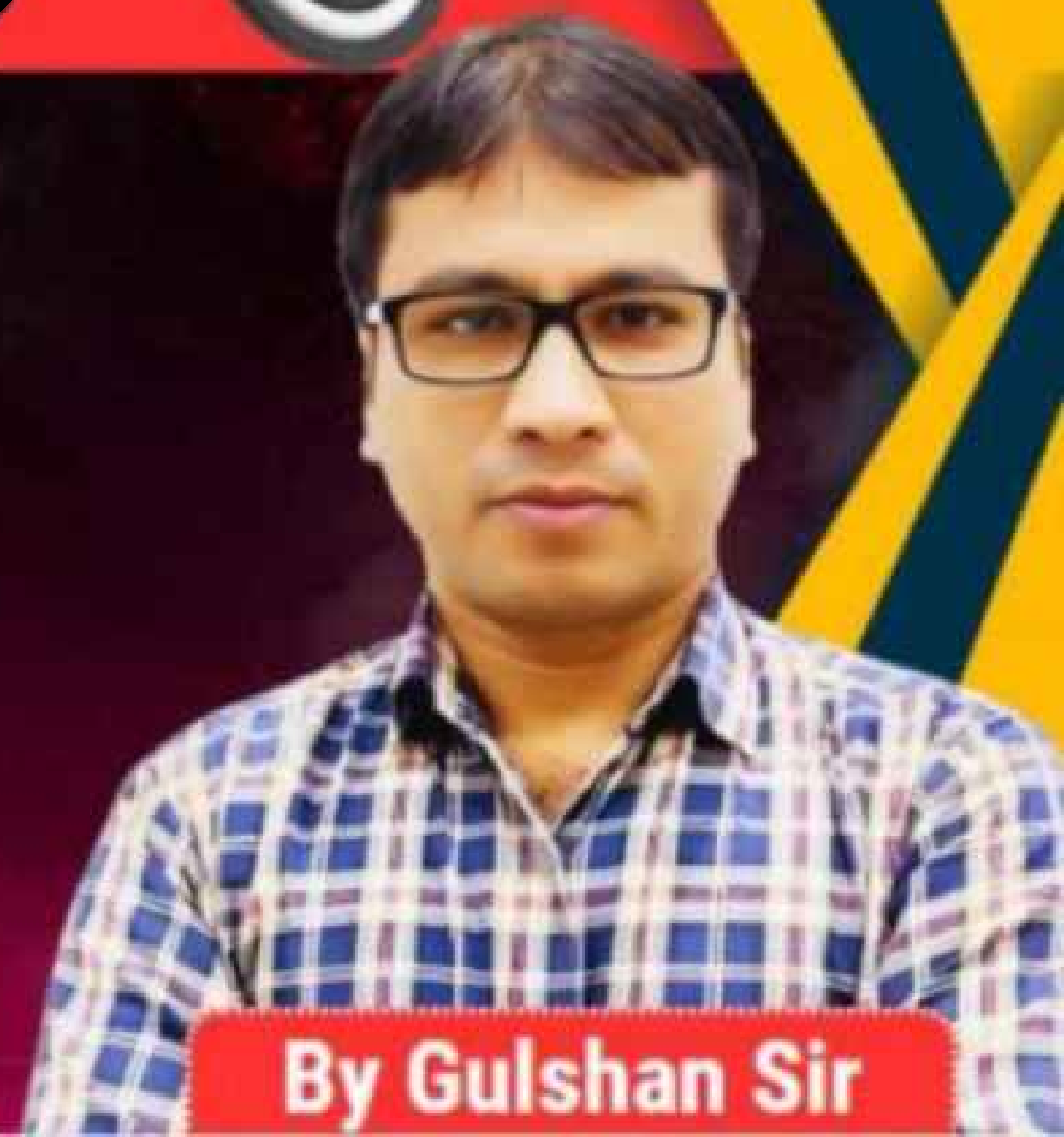


(Interference)
Lecture 1

Today's Target

- ✓ Interference in a Thin Film
- ✓ DPP
- ✓ PYQs

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By Gulshan Sir

CASE - 1 : Interference in a thin film by Reflected light

CASE - 2 : Interference in thin film by Transmitted light

Interference in a thin film by Reflected light

Consider a thin transparent film of thickness t and refractive index μ



Let a light ray SA is incident on the upper surface of the film.

(i) At point A : The light ray SA is partially reflected along AR_1 and partially refracted along AB

(ii) At point B : The light ray AB is partially reflected along BC

(iii) At point C : The light ray BC is partially refracted along CR_2

➤ Since the light rays AR_1 and CR_2 are derived from the incident ray SA, so they act as coherent light rays and produce interference pattern.

optical path Difference (Δ)

$\Delta = \text{Path ABC in thin Film} - \text{Path AN in Air}$

$$\Delta = \mu (AB + BC) - AN \quad \text{--- (1)}$$

$$\cos \gamma = \frac{BM}{AB}$$

$$AB = \frac{BM}{\cos \gamma}$$

$$AB = \frac{t}{\cos \gamma}$$

Also

$$\tan \gamma = \frac{AM}{BM}$$

$$AM = BM \tan \gamma$$

$$AM = t \tan \gamma$$

In Right Angle triangle BCM

$$\cos \gamma = \frac{BM}{BC}$$

$$BC = \frac{BM}{\cos \gamma}$$

$$BC = \frac{t}{\cos \gamma}$$

Also

$$\tan \gamma = \frac{MC}{BM}$$

$$MC = BM \tan \gamma$$

$$MC = t \tan \gamma$$

In Right Angle triangle ACN

$$\sin i = \frac{AN}{AC}$$

$$AN = AC \sin i$$

$$AN = (AM + MC) \sin i$$

$$AN = (t \tan \gamma + t \tan \gamma) \sin i$$

$$AN = 2t \tan \gamma \sin i$$

$$AN = 2t \times \frac{\sin \gamma}{\cos \gamma} \times \frac{\sin i}{\sin \gamma} \times \sin \gamma$$

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By Snell's law

$$\frac{\sin i}{\sin r} = \mu$$

$$AN = 2t \times \frac{\sin r}{\cos r} \times \mu \times \sin r$$

$$AN = \frac{2\mu t}{\cos r} \times \sin^2 r$$

Put AB, BC and AN in

eqn ①

$$\Delta = \mu(AB + BC) - AN$$

$$\Delta = \mu\left(\frac{t}{\cos r} + \frac{t}{\cos r}\right) - \frac{\mu t}{\cos r} \sin^2 r$$

$$\Delta = \frac{2\mu t}{\cos r} - \frac{\mu t}{\cos r} \sin^2 r$$

$$\Delta = \frac{2\mu t}{\cos r} (1 - \sin^2 r)$$

$$= \frac{2\mu t}{\cos r} \times \cos^2 r$$

$$\Delta = 2\mu t \cos r$$

$$\left\{ \because \sin^2 \theta + \cos^2 \theta = 1 \right\}$$

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According to Stoke's law, when light reflected from the surface of denser Medium, an additional phase change of π or path difference of $\frac{\lambda}{2}$ is produced

$$\Delta = 2\mu t \cos \gamma \pm \frac{\lambda}{2}$$

Actual path difference

Condition For constructive interference (or Maxima/Bright)

We know that

$$\Delta = 2n\left(\frac{\lambda}{2}\right)$$

$$2\mu t \cos \gamma \pm \frac{\lambda}{2} = 2n\left(\frac{\lambda}{2}\right)$$

$$2\mu t \cos \gamma = 2n\left(\frac{\lambda}{2}\right) \pm \frac{\lambda}{2}$$

$$2\mu t \cos \gamma = (2n \pm 1) \frac{\lambda}{2}$$

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$$2\mu t \cos \gamma = (2n+1) \frac{\lambda}{2} \quad n=0, 1, 2, \dots$$

$$2\mu t \cos \gamma = (2n-1) \frac{\lambda}{2} \quad n=1, 2, 3$$

Thin film will appear Bright
Condition For Destructive interference
(or Minima/Dark)

We know that

$$\Delta = (2n-1) \frac{\lambda}{2}$$

$$2\mu t \cos \gamma - \frac{\lambda}{2} = (2n-1) \frac{\lambda}{2}$$

$$2\mu t \cos \gamma = (2n-1) \frac{\lambda}{2} + \frac{\lambda}{2}$$

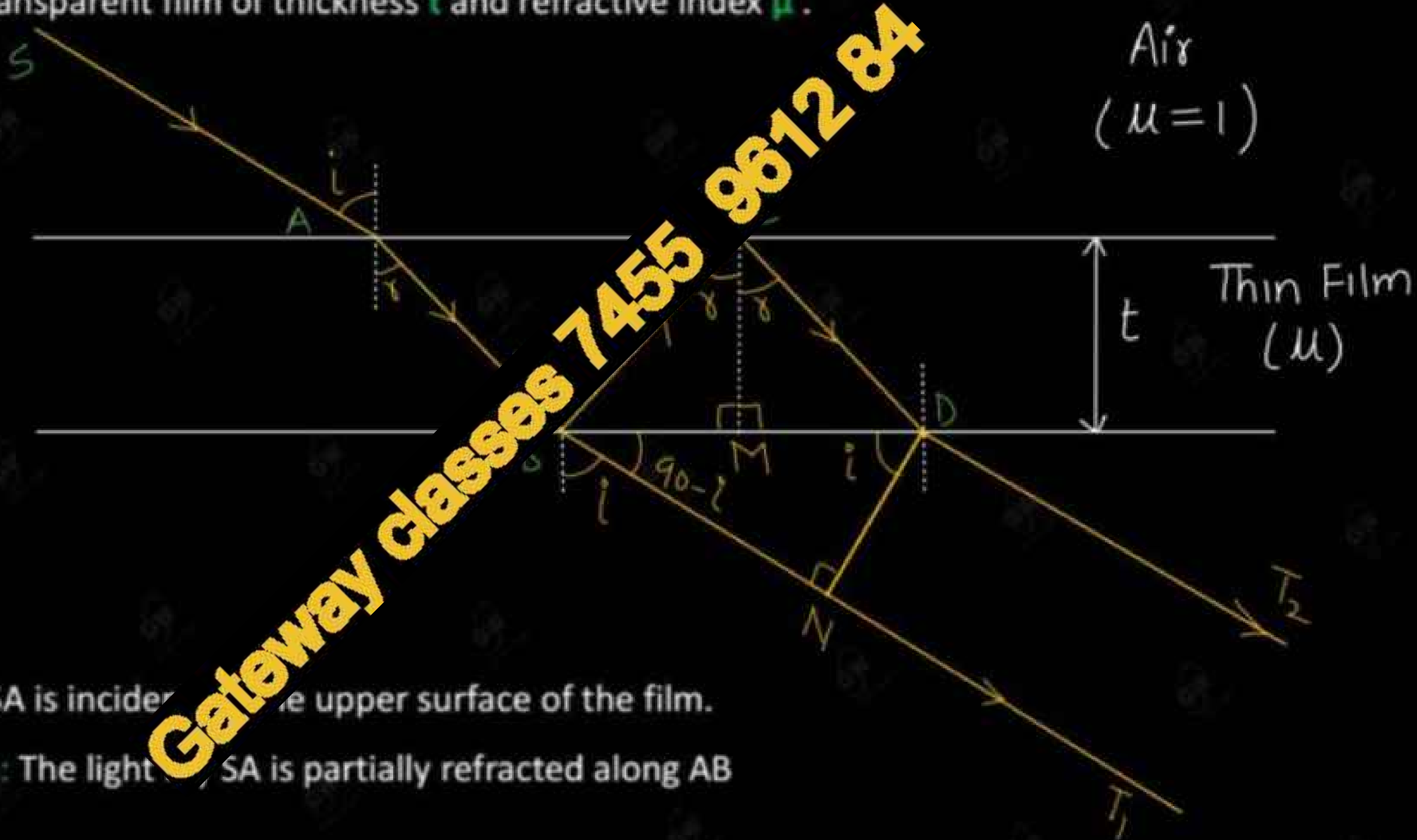
$$2\mu t \cos \gamma = 2n \frac{\lambda}{2} - \frac{\lambda}{2} + \frac{\lambda}{2}$$

$$2\mu t \cos \gamma = n\lambda$$

Thin film will appear Dark

Interference in a thin film by Transmitted light

Consider a thin transparent film of thickness t and refractive index μ .



➤ Let a light ray SA is incident on the upper surface of the film.

(i) At point A : The light ray SA is partially refracted along AB

(ii) At point B : The light ray AB is partially reflected along BC and partially refracted along BT_1

(iii) At point C : The light ray BC is partially reflected along CD

(iv) At point D : The light ray CD is partially refracted along DT_2

➤ Since, the transmitted ray BT_1 and DT_2 are derived from the same incident ray SA, so they act as coherent light rays and produced interference pattern.

Optical path difference (Δ)

$$\Delta = \text{Path BCD in film} - \text{Path BN in air}$$

$$\Delta = \mu(BC + CD) - BN \quad (1)$$

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Right angle - triangle BCM

$$\cos \gamma = \frac{CM}{BC}$$

$$BC = \frac{CM}{\cos \gamma}$$

$$BC = \frac{t}{\cos \gamma}$$

Also

$$\tan \gamma = \frac{BM}{CM}$$

$$BM = CM \tan \gamma$$

$$BM = t \tan \gamma$$

In triangle CDM

$$\cos \gamma = \frac{CM}{CD}$$

$$CD = \frac{CM}{\cos \gamma}$$

$$CD = \frac{t}{\cos \gamma}$$

Also

$$\tan \gamma = \frac{MD}{CM}$$

$$MD = CM \tan \gamma$$

$$MD = t \tan \gamma$$

In triangle BDN

$$\sin i = \frac{BN}{BD}$$

$$BN = BD \sin i$$

$$BN = (t + MD) \sin i$$

$$BN = (t \tan \gamma + t \tan \gamma) \sin i$$

$$BN = 2t \tan \gamma \sin i$$

$$BN = 2t \times \frac{\sin \gamma}{\cos \gamma} \times \sin i$$

$$BN = 2t \times \frac{\sin \gamma}{\cos \gamma} \times \left(\frac{\sin i}{\sin \gamma} \right) \times \sin \gamma$$

By Snell's law

$$\frac{\sin i}{\sin \gamma} = \mu$$

$$BN = 2t \times \frac{\sin \gamma}{\cos \gamma} \times \mu \times \sin \gamma$$

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$$BN = \frac{2\mu t}{\cos \gamma} \times \sin^2 \gamma$$

Put BC, CD and BN in ①

$$\Delta = \mu(BC + CD) - BN$$

$$\Delta = \mu \left(\frac{t}{\cos \gamma} + \frac{t}{\cos \gamma} \right) - \frac{2\mu t}{\cos \gamma} \sin^2 \gamma$$

$$\Delta = \frac{2\mu t}{\cos \gamma} - \frac{2\mu t}{\cos \gamma} \times \sin^2 \gamma$$

$$\Delta = \frac{2\mu t}{\cos \gamma} (1 - \sin^2 \gamma)$$

$$\Delta = \frac{2\mu t}{\cos \gamma} \times \cos^2 \gamma$$

$$\Delta = 2\mu t$$

Actual path
Difference

Condition For constructive interference
(or Maxima/Bright)

We know that

$$\Delta = 2n \left(\frac{\lambda}{2} \right)$$

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$$2nt \cos \gamma = n \left(\frac{\lambda}{2} \right)$$

$$2nt \cos \gamma = n\lambda$$

(2)

Thin film will appear Bright

Condition Destructive interference
(or minima / Dark)

We know that

$$\Delta = (2n-1) \frac{\lambda}{2}$$

$$2nt \cos \gamma = (2n-1) \frac{\lambda}{2} \quad n=0, 1, 2, \dots$$

(3)

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Interference in Thin Film due to Reflected light

➤ Condition for Maxima

$$2\mu t \cos r = (2n + 1)\frac{\lambda}{2} \quad \text{--- (2)}$$

➤ Condition for Minima

$$2\mu t \cos r = n\lambda \quad \text{--- (3)}$$

Interference in Thin Film due to Transmitted light

➤ Condition for Maxima

$$2\mu t \cos r = n\lambda \quad \text{--- (2)}$$

➤ Condition for Minima

$$2\mu t \cos r = (2n + 1)\frac{\lambda}{2} \quad \text{--- (3)}$$

From equation 2 and 3 in both the cases it is clear that the film, which appears dark in reflected light will appear bright in transmitted light and vice versa. Hence reflected and transmitted system are complementary in thin film.

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Q.1 Calculate the thickness of thin film (soap bubble) that will result in constructive interference in reflected light. The film is illuminated with light of wavelength $5000 \text{ \AA}$ and refractive index of film is 1.45.

Given

$$\lambda = 5000 \text{ \AA} = 5000 \times 10^{-10} \text{ m}$$

$$\mu = 1.45$$

For constructive interference
in Reflected light

$$2\mu t \cos r = (2n-1) \frac{\lambda}{2}$$

For least thickness

$$r = 0$$

$$n = 1$$

$$2\mu t \cos 0 = \frac{\lambda}{2}$$

$$t = \frac{\lambda}{4\mu}$$

$$t = \frac{5000 \times 10^{-10}}{4 \times 1.45}$$

$$t = 8.62 \times 10^{-8}$$

✓✓

$$1 \text{ \AA} = 10^{-10} \text{ m}$$

$$1 \text{ \AA} = 10^{-8} \text{ cm}$$

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Q.2 Light of wavelength $5893 \text{ \AA}$ is reflected at nearly normal incidence from a soap film of refractive index 1.42. What is the least thickness of the film that will appear (i) Bright (ii) Dark?

Given

$$\lambda = 5893 \text{ \AA} = 5893 \times 10^{-10} \text{ m}$$

$$\mu = 1.42$$

(i) Condition for Bright

$$2\mu t \cos r = (2n-1) \frac{\lambda}{2}$$

For normal incidence

$$\cos r = 1$$

For least thickness

$$n=1$$

$$2\mu t \times 1 =$$

$$\frac{\lambda}{4\mu}$$

$$= \frac{5893 \times 10^{-10}}{4 \times 1.42}$$

$$t = 1037.5 \text{ \AA}$$

Condition for Dark

$$2\mu t \cos r = n\lambda$$

$$2\mu t \times 1 = \lambda$$

$$t = \frac{\lambda}{2\mu}$$

$$t = \frac{5893 \times 10^{-10}}{2 \times 1.42}$$

$$t = 2075 \text{ \AA}$$

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Q.3 A soap film of refractive index 1.43 is illuminated by white light incident at an angle of 30° . The reflected light is examined by a spectroscope in which dark band corresponding to the wavelengths 6×10^{-7} m is observed. Calculate the thickness of the film.

Given

$$\mu = 1.43$$

$$i = 30^\circ$$

$$\lambda = 6 \times 10^{-7} \text{ m}$$

By Snell's law

$$\mu = \frac{\sin i}{\sin r}$$

$$\sin r = \frac{\sin i}{\mu}$$

$$\sin r = \frac{\sin 30^\circ}{1.43}$$

$$\sin r = 0.3496$$

$$\cos^2 r = 1 - \sin^2 r$$

$$\cos r = \sqrt{1 - \sin^2 r}$$

$$\cos r = \sqrt{1 - (0.3496)^2}$$

$$\cos r = 0.94$$

Condition for Dark band

$$2\mu t \cos r = n\lambda$$

$$t = \frac{n\lambda}{2\mu \cos r} = \frac{1 \times 6 \times 10^{-7} \text{ m}}{2 \times 1.43 \times 0.94}$$

$$t = 2.23 \times 10^{-7} \text{ m}$$

- Q.1** Describe the phenomenon of interference in thin film (uniform thickness) of reflected light and write down the conditions for constructive and destructive interference.
- Q.2** Discuss the phenomenon of interference of light due to parallel thin films and find the condition of maxima and minima. Show that the interference patterns of reflected and transmitted source of light are complementary.
- Q.3** Calculate the thickness of a soap bubble thin film that will give rise to constructive interference in reflected light. The film is illuminated with light of wavelength 500 nm and the refractive index of the film is 1.45 .
- Q.4** A parallel beam of sodium light of $5880\text{ \AA}$ is incident on a thin glass plate of refractive index 1.5 . Such that the angle of refraction in the plate is 60° . Calculate the smallest thickness of the plate, which will make it appear dark by reflection.
- Q.5** White light is incident on a soap film at an angle $\sin^{-1}\left(\frac{4}{5}\right)$ and the reflected light is observed with a spectroscope. It is found that two consecutive dark bands correspond to wavelengths $6.1 \times 10^{-5}\text{ cm}$ and $6.0 \times 10^{-5}\text{ cm}$. If the refractive index of the film is $\frac{4}{3}$, calculate the thickness.



B. Tech : Engg. Physics



Unit : Wave Optics

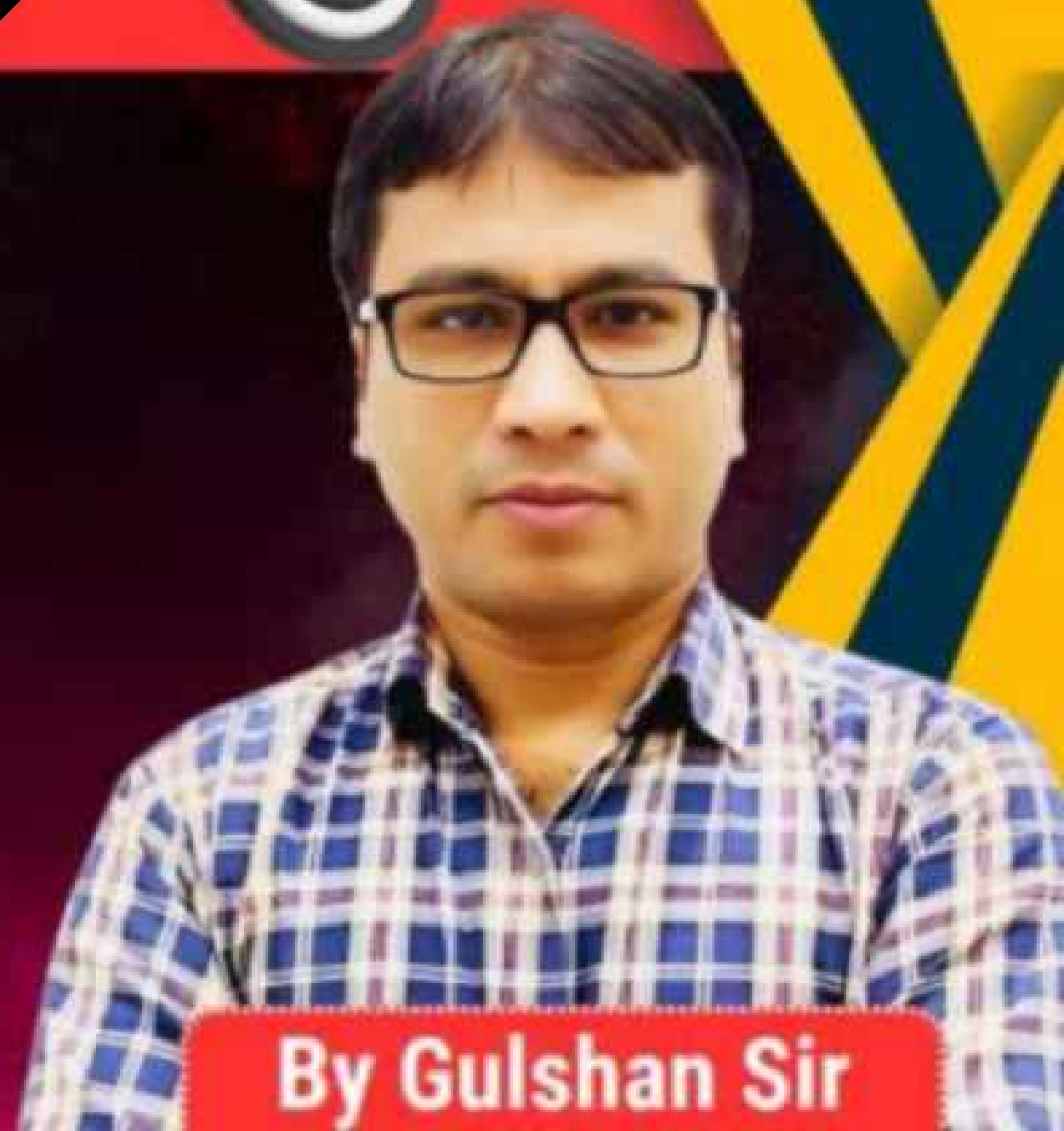


(Interference)
Lecture

Today's Target

- ✓ Interference in a Wedge and Thin Film
- ✓ DPP
- ✓ PYQs

Gateway classes 7455 9612 84



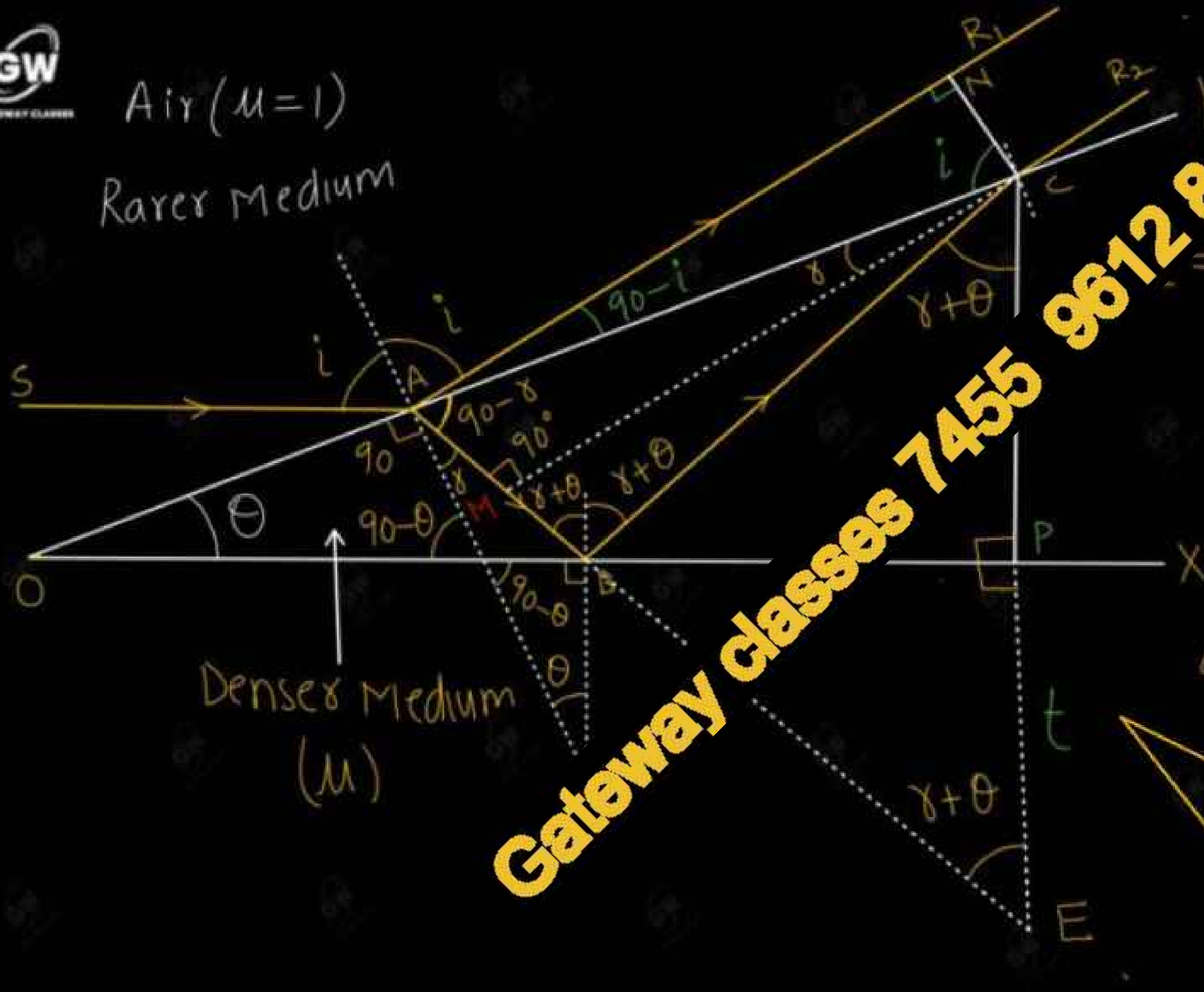
By Gulshan Sir

A wedge-shaped thin film is one whose plane surfaces (OY and OX) are slightly inclined to each other at an angle θ and encloses a film of transparent material of refractive index μ . The thickness of the film increases from one end to other end.

Interference in a Wedge-Shaped thin film by Reflection

- Consider a thin transparent Wedge-Shaped film of varying thickness and refractive index μ
- Let a light ray SA is incident on the upper surface OY
 - (i) **At point A** : The light ray SA is partially reflected along AR_1 and partially refracted along AB
 - (ii) **At point B** : The light ray AB is partially reflected along BC
 - (iii) **At point C** : The light ray BC is partially refracted along CR_2
- Since the reflected rays AR_1 and CR_2 are derived from the incident ray SA, they act as coherent light rays and produce interference pattern.

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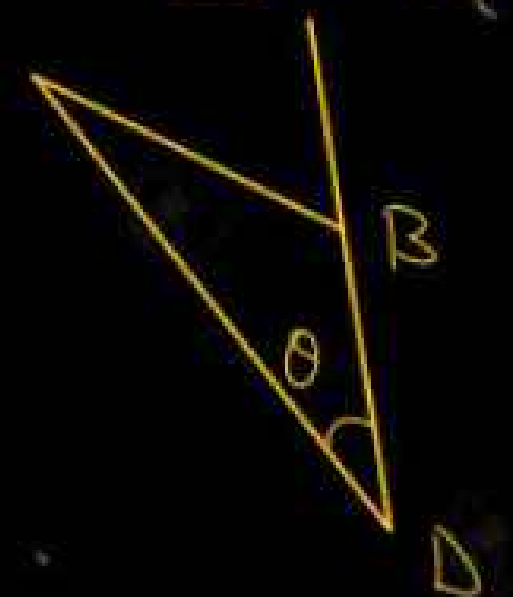
Air ($\mu=1$)
Rarer Medium

Denser Medium
(μ)

Optical path Difference
= Path ABC in thin Film -
Path AN in Air

$$\Delta = \mu(AB + BC) - AN$$

$$\Delta = \mu(AM + MB + BC) - AN$$



①

In ΔACN

$$\sin i = \frac{AN}{AC}$$

In ΔACM

$$\sin r = \frac{AM}{AC}$$

$$\frac{\sin i}{\sin r} = \frac{AN}{AC} \times \frac{AC}{AM}$$

$$\frac{\sin i}{\sin r} = \frac{AN}{AM}$$

By Snell's law

$$\mu = \frac{\sin i}{\sin r}$$

$$\mu = \frac{AN}{AM}$$

$$AN = \mu AM$$

Put $AN = \mu AM$ (1)

$$\Delta = \mu (AM + MB + BC) - \mu AM$$

$$= \mu (AM + MB + BC - AM)$$

$$\Delta = \mu (MB + BC)$$

(2)

Draw, $CP \perp OX$ and produced CP and AB to meet at E

$$\therefore \Delta BPC \cong BPE$$

$$\therefore BC = BE$$

$$\therefore CP = PE = t$$

Put BC in (2)

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$$\Delta = \mu(MB + BE)$$

$$\Delta = \mu ME \quad \text{--- (3)}$$

In ΔMCE

$$\cos(\gamma + \theta) = \frac{ME}{CE}$$

$$ME = CE \cos(\gamma + \theta)$$

$$ME = 2t \cos(\gamma + \theta)$$

Put ME in (3)

$$\Delta = 2\mu t \cos(\gamma + \theta)$$

By Stoke's law

$$\Delta = 2\mu t \cos(\gamma + \theta) \pm \frac{\lambda}{2}$$

Actual path
Difference

Condition for Maxima

We know that

$$\Delta = 2n\left(\frac{\lambda}{2}\right)$$

$$2\mu t \cos(\gamma + \theta) \pm \frac{\lambda}{2} = 2n\left(\frac{\lambda}{2}\right)$$

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$$2\mu t \cos(r+\theta) = 2n\left(\frac{\lambda}{2}\right) \pm \frac{\lambda}{2}$$

$$2\mu t \cos(r+\theta) = (2n \pm 1) \frac{\lambda}{2}$$

$$2\mu t \cos(r+\theta) = (2n+1) \frac{\lambda}{2}$$

$$2\mu t \cos(r+\theta) = (2n-1) \frac{\lambda}{2}$$

Thin film will appear

Bright

condition for Minima

We know that

$$\Delta = (2n-1)$$

$$2\mu t \cos(r+\theta) - \frac{\lambda}{2} = (2n-1) \frac{\lambda}{2}$$

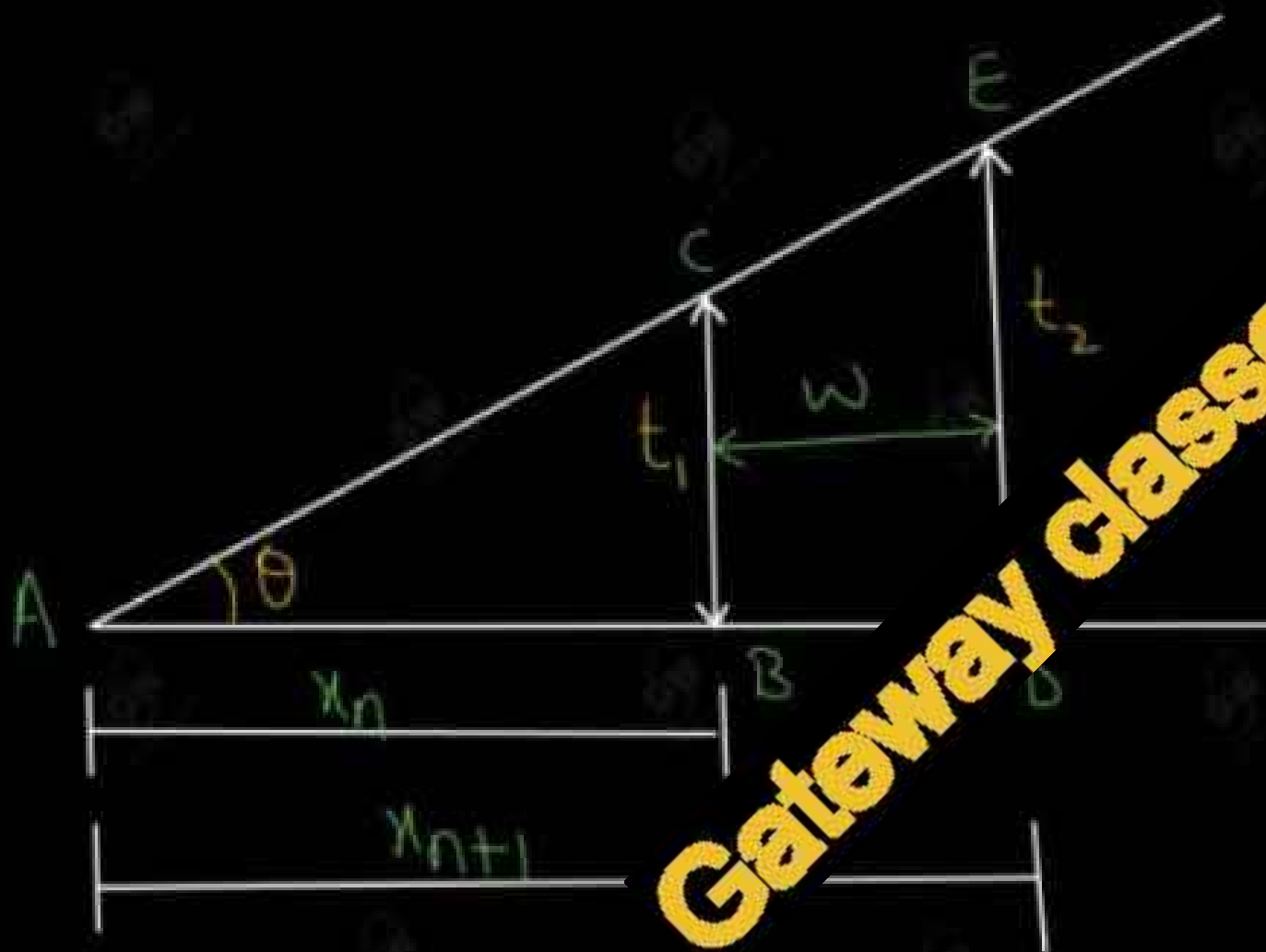
$$2\mu t \cos(r+\theta) = n\lambda$$

Thin Film will appear dark

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Fringe-width

- Consider a thin transparent Wedge-Shaped film of varying thickness and refractive index μ
- Let x_n be the distance of n^{th} bright fringe from the edge of the film
- Let x_{n+1} be the distance of $(n+1)^{\text{th}}$ bright fringe from the edge of the film



$$\tan \theta = \frac{t_1}{x_n}$$

$$t_1 = x_n \tan \theta$$

For Bright Fringe

$$2\mu t_1 \cos(\gamma + \theta) = (2n-1) \frac{\lambda}{2}$$

Put t_1 in above eqn

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$$2\mu n_n \tan \theta \cos(\gamma + \theta) = (2n-1) \frac{\lambda}{2}$$

①

In $\triangle ADE$

$$\tan \theta = \frac{t_2}{n_{n+1}}$$

$$t_2 = n_{n+1} \tan \theta$$

For Bright Fringe

$$2\mu t_2 \cos(\gamma + \theta) = (2n-1) \frac{\lambda}{2}$$

Put t_2 in above eqn

$$2\mu n_{n+1} \tan \theta \cos(\gamma + \theta) = (2n-1) \frac{\lambda}{2}$$

$$2\mu n_{n+1} \tan \theta \cos(\gamma + \theta) = (2n+2-1) \frac{\lambda}{2}$$

$$2\mu n_{n+1} \tan \theta \cos(\gamma + \theta) = (2n+1) \frac{\lambda}{2} \quad \text{--- ②}$$

Subtract ① From ②

$$2\mu n_{n+1} \tan \theta \cos(\gamma + \theta) - 2\mu n_n \tan \theta \cos(\gamma + \theta) = (2n+1) \frac{\lambda}{2} - (2n-1) \frac{\lambda}{2}$$

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$$2\mu \tan \theta \cos(\gamma + \theta) \{n_{n+1} - n_n\} = \frac{\lambda}{2} (2n+1 - \cancel{2n+1})$$

$$2\mu \tan \theta \cos(\gamma + \theta) \{n_{n+1} - n_n\} = \lambda$$

$$n_{n+1} - n_n = \frac{\lambda}{2\mu \tan \theta \cos(\gamma + \theta)}$$

$$W = \frac{\lambda}{2\mu \tan \theta \cos(\gamma + \theta)}$$

For normal incidence

$$\gamma = 0$$

$$= \frac{\lambda}{2\mu \tan \theta \cos \theta} = \frac{\lambda}{2\mu \times \frac{\sin \theta}{\cos \theta} \cos \theta}$$

$$W = \frac{\lambda}{2\mu \sin \theta}$$

$\sin \theta$ is very-very small

$$\sin \theta \approx \theta$$

$$\tan \theta \approx \theta$$

$$W = \frac{\lambda}{2\mu\theta}$$

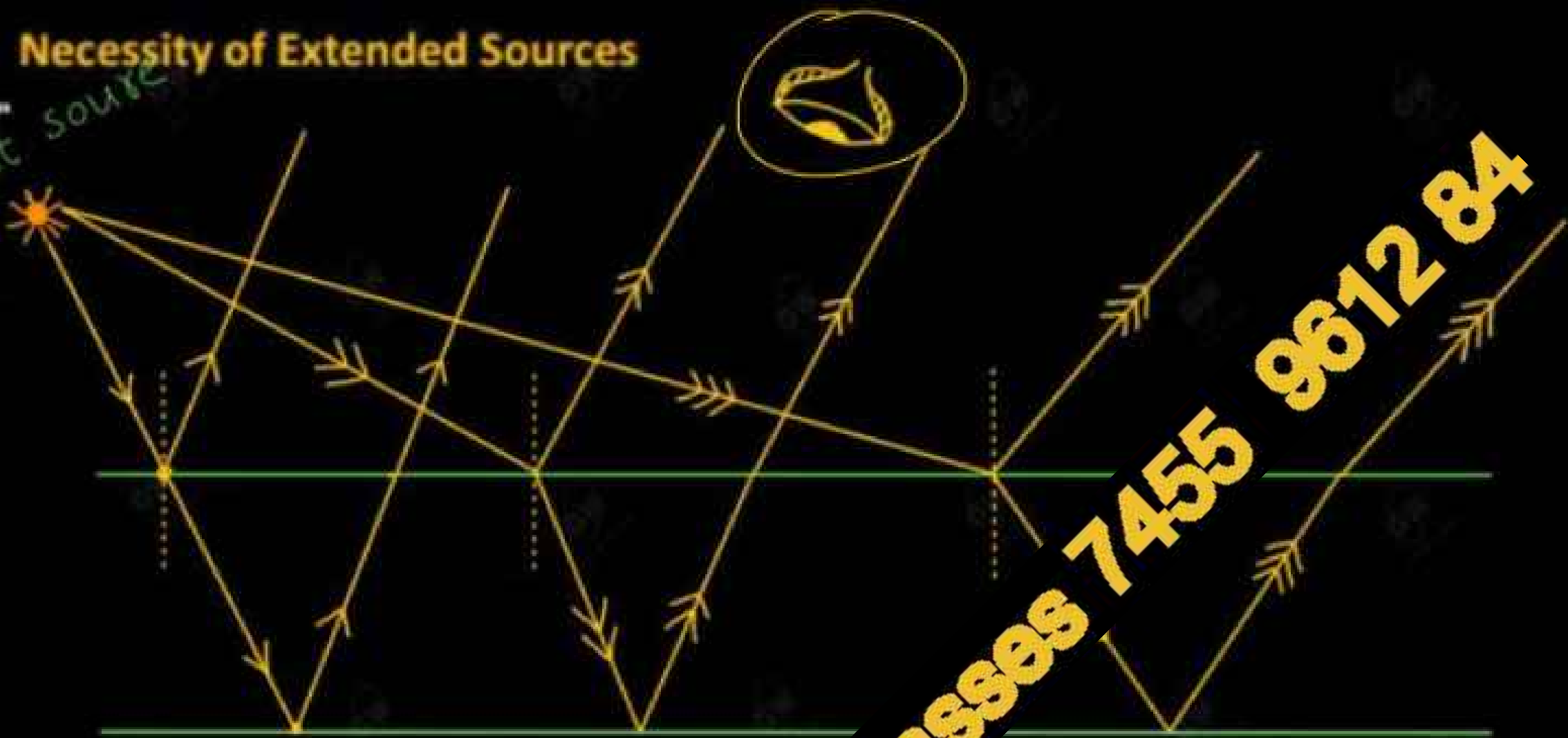
For Air Film

$$\mu = 1$$

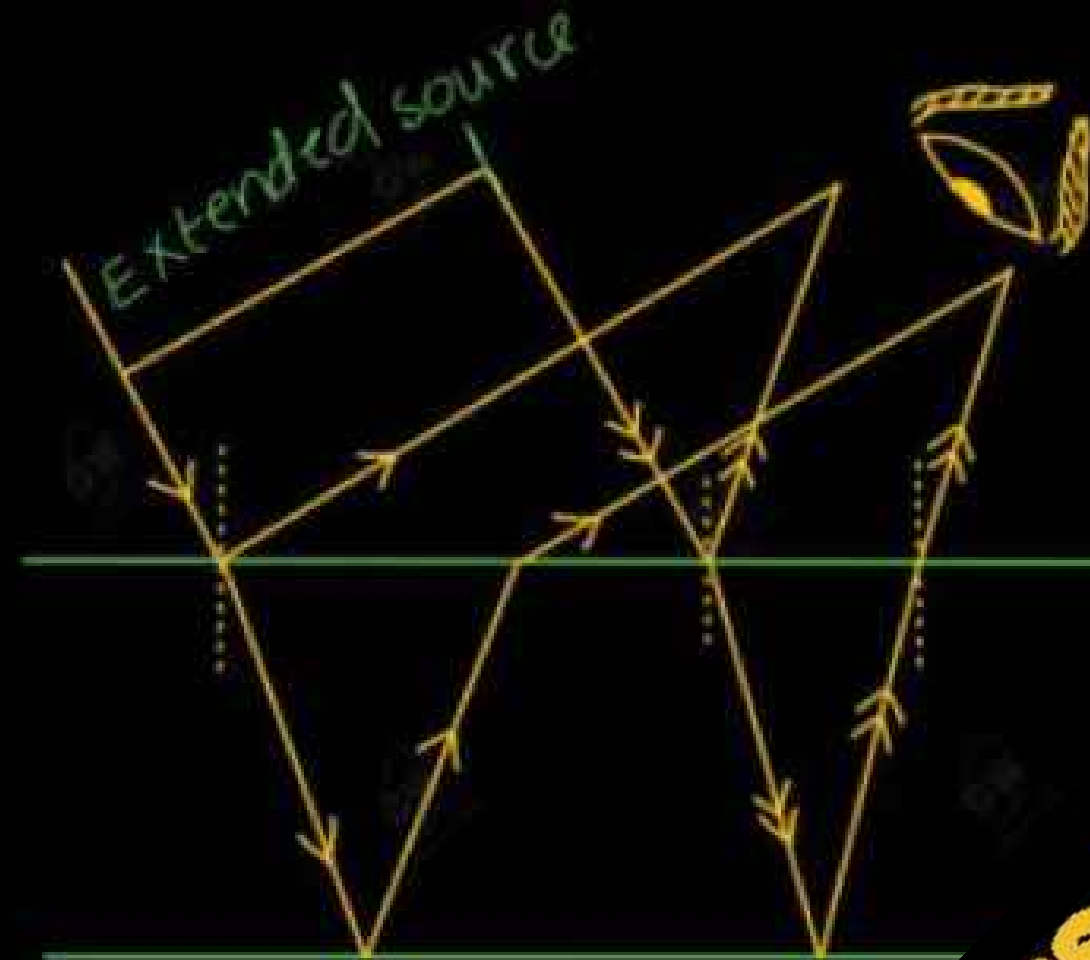
$$W = \frac{\lambda}{2\theta}$$

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Point source



- If the light is incident on thin film from point source then for different incident rays, different pairs of interfering rays are obtained along different directions. All these pairs can not be seen by the eye simultaneously. Hence, only a small portion of the film is visible



- On the other hand, if we use an extended source instead of point source then the different pairs of interfering reflected rays will reach the film from a large portion of the film (may be from the whole film)
- Hence to see the interference effect over the entire film simultaneously, an extended source of light is necessary

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Q.1 Light of wavelength 6000 Å falls normally on a thin wedge-shaped film of refractive index 1.4 forming fringes that are 2.0 mm apart. Find the angle of wedge in seconds.

Given

$$\lambda = 6000 \text{ Å} = 6000 \times 10^{-10} \text{ m}$$

$$\mu = 1.4$$

$$w = 2 \text{ mm} = 2 \times 10^{-3} \text{ m}$$

For normal incidence

$$w = \frac{\lambda}{2\mu\theta}$$

$$\theta = \frac{\lambda}{2w\mu}$$

$$\theta = \frac{6000 \times 10^{-10}}{2 \times 10^{-3} \times 1.4} \times \frac{180}{\pi}$$

$$= 0.0061^\circ = 0.0061 \times 60 \times 60$$

$$\theta = 21.96 \text{ second}$$

$$1^\circ = 60 \text{ min}$$

$$1 \text{ min} = 60 \text{ sec}$$

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Q.2 Two plane glass surfaces in contact along one edge are separated at the opposite edge by a thin wire. if 20 interference fringes are observed between these edges in sodium light of $\lambda = 5890 \text{ \AA}$ of normal Incidence, find the diameter of the wire.

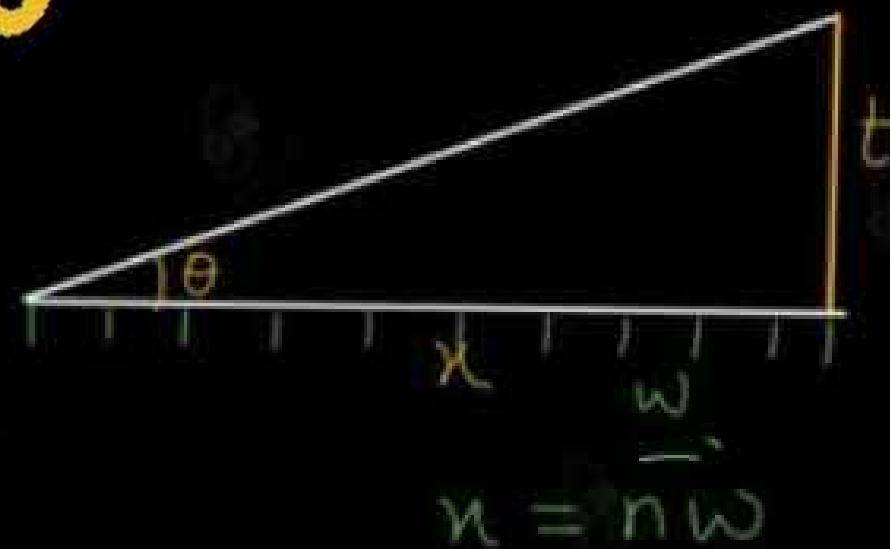
Given

$$n = 20$$

$$\lambda = 5890 \text{ \AA} = 5890 \times 10^{-10} \text{ m}$$

Let t be the thickness or diameter
of wire

$$\tan \theta = \frac{t}{x}$$



for normal incidence

$$w = \frac{\lambda}{2\theta}$$

$$w = \frac{\lambda \times n}{2 \times t}$$

But

$$n = n_w$$

$$w = \frac{\lambda \times n_w}{2t}$$

$$t = \frac{\lambda \times n_w}{2w}$$

$$t = \frac{\lambda n}{2} = \frac{5890 \times 10^{-7} \times 20}{2}$$

$$t = 5.89 \times 10^{-6} \text{ m}$$

$$t = 5.89 \times 10^{-4} \text{ cm}$$

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- Q.1** Obtain an expression for the fringe width in a wedge – shaped film and explain nature of fringe pattern.
- Q.2** What do you mean by a wedge- shaped film? Discuss the interference due to it and obtain the expression for the fringe width.
- Q.3** Two plane rectangular piece of glass in contact at one edge and separated by a hair at opposite edge so that a wedge is formed. When light of wave length $6000 \text{ \AA}$ falls normally on the wedge, 9 interference fringes are observed. What is the thickness of the hair?

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B. Tech : Engg. Physics



Unit : Wave Optics



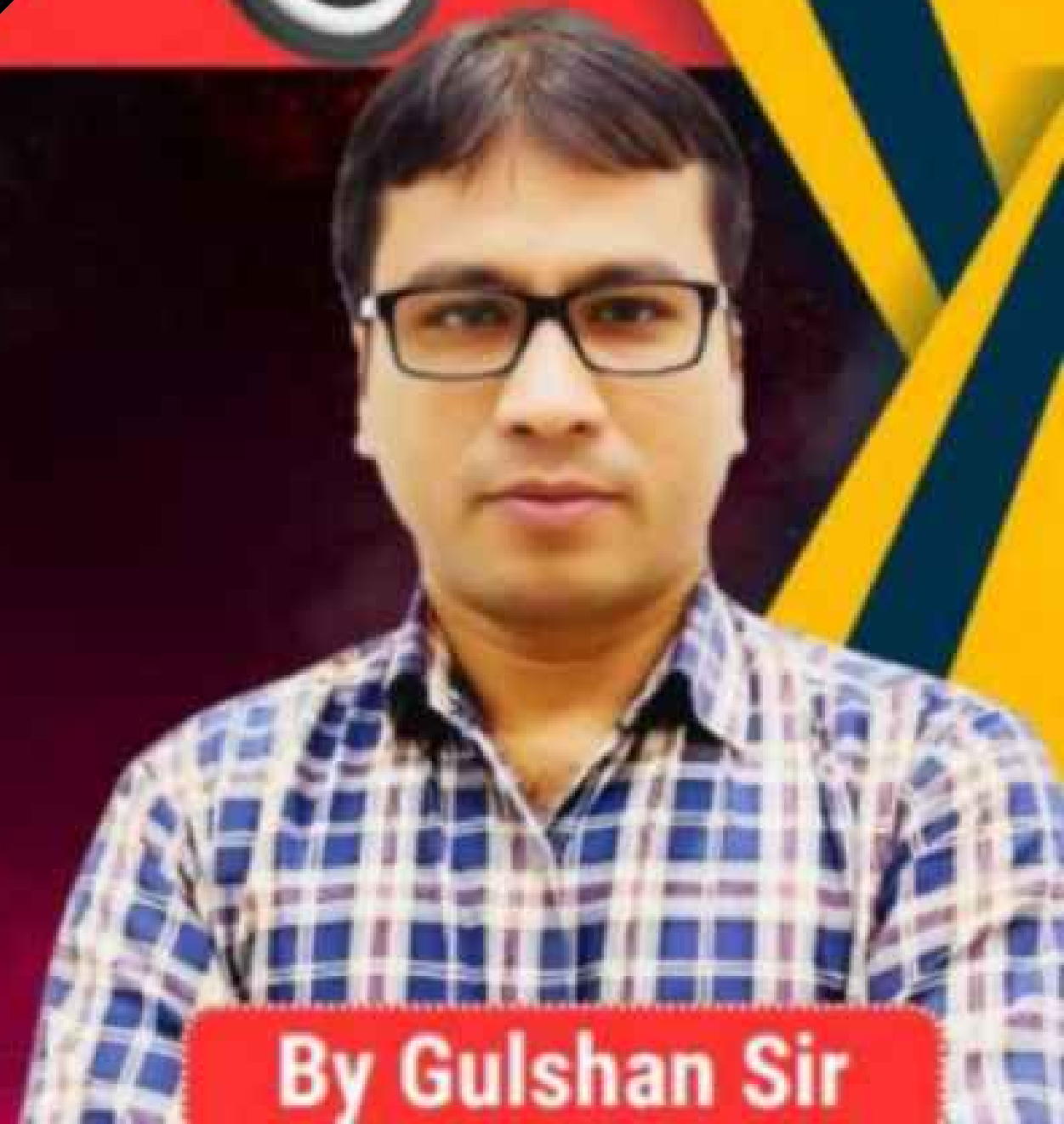
(Interference)
Lecture



Today's Target

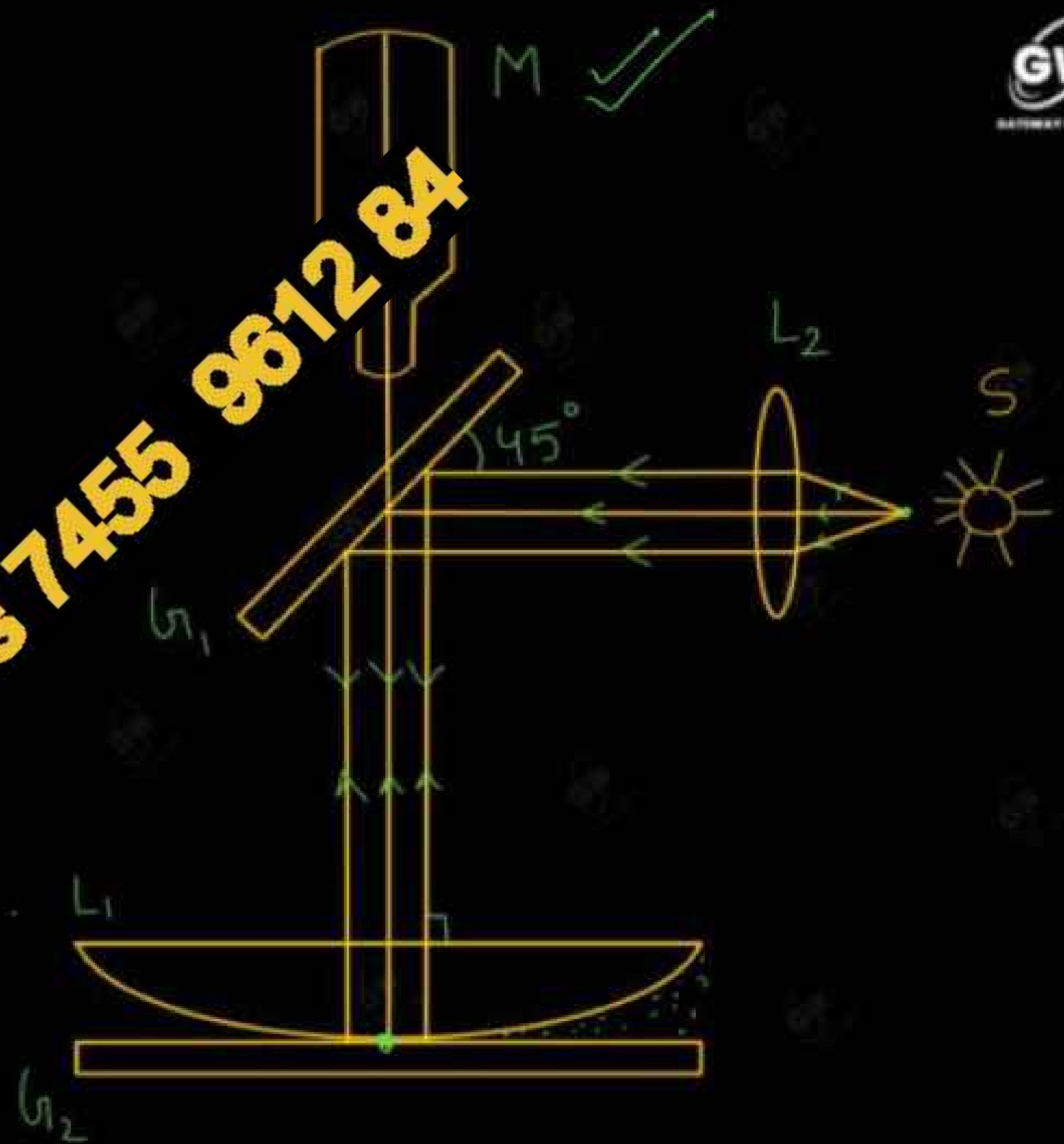
- ✓ Newton's Rings
- ✓ Applications of Newton's Rings
- ✓ DPP
- ✓ PYQs

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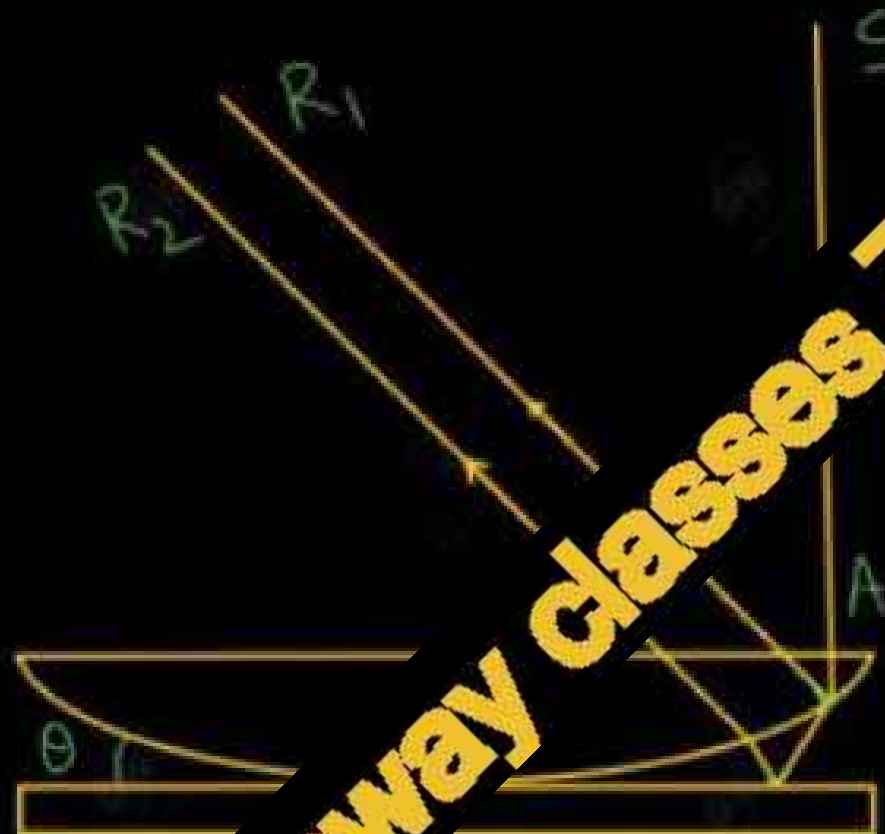


By Gulshan Sir

- The experimental arrangement to obtain Newton's Rings is shown in figure
- Light from a monochromatic source (Sodium light) **S** is converted into a parallel beam by a lens **L₂**. Which falls on a glass plate **G₁** oriented at an angle of **45°** with the vertical.
- The light reflected by a plate **G₁** turns through 90° and is incident normally on the wedge-shaped film formed between the Plano-convex lens and the glass plate **G₂**.
- A microscope **M** placed above the plano-convex lens **L₁** is used to see the concentric dark and bright Newton's rings.



- When a Plano-Convex lens of large radius of curvature is placed on a plane glass plate, a thin film of air is enclosed between the lower surface (convex surface) of the lens and the upper surface of the glass plate.
- The thickness of air film is zero at the point of contact and it gradually increases as we move away from the point of contact.



- If a Monochromatic light is allowed to fall on this air film then alternate Bright and Dark concentric Rings with their Centre Dark are formed. These rings are known as Newton's Rings.

Newton's rings are formed due to the interference between the waves reflected from the top surface (R_1) and bottom surface (R_2) of wedge – shaped air film between the Plano-Convex lens and plane glass plate.

Inference theory in Newton's Rings

Path Difference

The path difference between R_1 and R_2 is given

$$\Delta = 2 \mu t \cos (r + \theta) \pm \frac{\lambda}{2}$$

Since, θ is very – very small ($\theta \approx 0$)

$$\Delta = 2 \mu t \cos r \pm \frac{\lambda}{2}$$

For normal incidence ($r = 0$)

$$\Delta = 2 \mu t \pm \frac{\lambda}{2}$$

For air film ($\mu = 1$)

$$\Delta = 2 t \pm \frac{\lambda}{2}$$

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Condition for constructive interference

(Maxima or Bright Rings)

We know that

$$\Delta = 2n \left(\frac{\lambda}{2} \right)$$

$$2\mu t \pm \frac{\lambda}{2} = 2n \frac{\lambda}{2}$$

$$2\mu t = (2n \pm 1) \frac{\lambda}{2}$$

For air film ($\mu=1$)

$$2t = (2n \pm 1) \frac{\lambda}{2}$$

Condition for destructive interference

(Minima or Dark Rings)

We know that

$$\Delta = (2n + 1) \frac{\lambda}{2}$$

$$2\mu t + \frac{\lambda}{2} = (2n + 1) \frac{\lambda}{2} = 2n \left(\frac{\lambda}{2} \right) + \frac{\lambda}{2} - \frac{\lambda}{2}$$

$$2\mu t = n\lambda$$

For air film ($\mu=1$)

$$2t = n\lambda$$

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thickness is t

Diagram illustrating the geometry of a thick-walled cylinder. The outer radius is R and the inner radius is r . The thickness is t . The diagram shows the cylinder is divided into four quadrants by a vertical and a horizontal line. The center is labeled O . The outer boundary is a dashed circle, and the inner boundary is a solid circle. The thickness t is indicated by a vertical arrow on the right side. The diagram is labeled with $A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z$ and Greek letters α and β .

Since, $t \ll 2R$

$$t = \frac{\gamma^2}{2R}$$

OR

$$t = \frac{D^2}{8R}$$

v. imp

Where D is diameter
of Newton's Ring

Diameter of Bright Rings

Put value of t in $2\mu t = (2n-1)\frac{\lambda}{2}$

$$2\mu \frac{\gamma^2}{2R} = (2n-1)\frac{\lambda}{2} \quad \left(\frac{D_n}{2}\right)^2 = (2n-1)\frac{\lambda R}{2\mu}$$

$$\gamma^2 = (2n-1)\frac{\lambda R}{\mu}$$

For Air Film

$$= (2n-1)\frac{\lambda R}{2\mu}$$

$$D_n^2 = \frac{2(2n-1)\lambda R}{\mu} \quad \text{v. imp}$$

For Air Film ($\mu=1$)

$$D_n^2 = 2(2n-1)\lambda R$$

$$D_n = \sqrt{2(2n-1)\lambda R}$$

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$$D_n = \sqrt{2(2n-1)\lambda R}$$

$$D_n = \sqrt{2\lambda R} \times \sqrt{2n-1}$$

Put $\sqrt{2\lambda R} = K$

$$D_n = K \sqrt{2n-1}$$

$$D_n \propto \sqrt{2n-1}$$

Thus, Diameter of Bright rings is directly proportion to square root of odd natural numbers

Diameter of Dark rings ✓✓

Put the value of t in $2\mu t = n\lambda$

$$2\mu \times \frac{r^2}{2} = n\lambda$$

$$r^2 = \frac{n\lambda R}{\mu}$$

For n^{th} ring

$$r_n^2 = \frac{n\lambda R}{\mu}$$

$$\left(\frac{D_n}{2}\right)^2 = \frac{n\lambda R}{\mu}$$

$$D_n^2 = \frac{4n\lambda R}{\mu} \quad \text{v. imp}$$

For air Film

$$D_n^2 = 4n\lambda R$$

$$D_n = \sqrt{4n\lambda R}$$

$$D_n = \sqrt{4\lambda R} \sqrt{n}$$

$$\text{Let } \sqrt{4\lambda R} = K$$

$$D_n = K \sqrt{n}$$

$$D_n \propto \sqrt{n}$$

Thus, Diameter of Davy's rings is directly proportional to the square root of natural number.

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Centre of Newton's Rings is Dark. Give reason

The wedge – shaped air film is formed between the curved surface of Plano-convex lens and plane glass plate, therefore path difference between interfering rays in reflected light will be

$$\Delta = 2 \mu t \cos (\tau + \theta) + \frac{\lambda}{2}$$

At the point of contact ($t = 0$)

$$\Delta = \frac{\lambda}{2}$$

Which is the condition for minimum intensity. Hence the Centre of Newton's ring is dark

Fringes in Newton's Ring experiment are circular. Give reason

Fringes in Newton's Ring experiment are circular because the wedge-shaped air film is symmetrical about the point of contact of the lens with the plane glass plate and locus of all the points of equal thickness are concentric circles with respect to the point of contact.

Application of Newton's Rings Experiment

(i) Determination of Wavelength of Monochromatic light (or sodium light) using Newton's Ring.

Let $D_n = \text{Diameter of } n^{\text{th}} \text{ Dark Ring}$

$D_{n+p} = \text{Diameter of } (n+p)^{\text{th}} \text{ Dark Ring}$

We know that

$$D_n^2 = 4n\lambda R \quad \text{--- (1)}$$

$$D_{n+p}^2 = 4(n+p)\lambda R$$

$$D_{n+p}^2 = 4n\lambda R + 4p\lambda R$$

Subtract (1) from (2)

$$D_{n+p}^2 - D_n^2 = 4n\lambda R + 4p\lambda R - 4n\lambda R$$

$$D_{n+p}^2 - D_n^2 = 4p\lambda R$$

$$\lambda = \frac{D_{n+p}^2 - D_n^2}{4pR}$$

Same result will be obtained for bright ring

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(ii) Determination of refractive index of a liquid using Newton's Ring.

The transparent liquid whose refractive index is to be determined is introduced between lens and glass plate.

The diameter of n^{th} dark ring is given by

$$D_n^2 = \frac{4n\lambda R}{\mu} \quad \text{--- (1)}$$

Diameter of $(n+p)^{th}$ dark ring is given by

$$D_{n+p}^2 = \frac{4(n+p)\lambda R}{\mu} \quad \text{--- (2)}$$

Subtract (1) from (2)

$$D_{n+p}^2 - D_n^2 = \frac{4(n+p)\lambda R}{\mu} - \frac{4n\lambda R}{\mu}$$

$$D_{n+p}^2 - D_n^2 = \frac{4n\cancel{\lambda} R - 4n\cancel{\lambda} R + 4p\lambda R}{\mu}$$

$$D_{n+p}^2 - D_n^2 = \frac{4p\lambda R}{\mu} \quad \text{--- (3)}$$

For air ($\mu = 1$)

$$D_{n+p}^2 - D_n^2 = 4p\lambda R \quad \text{--- (4)}$$

Divide (4) by (3)

$$\mu = \frac{[D_{n+p}^2 - D_n^2]_{air}}{[D_{n+p}^2 - D_n^2]_{liquid}}$$

Thickness of film

$$t = \frac{\gamma^2}{2R}$$

OR

$$t = \frac{D^2}{8R}$$

Diameter of Bright Ring

$$D_n^2 = \frac{2(2n-1)\lambda R}{\mu}$$

For Air Film ($\mu=1$)

$$D_n^2 = 2(2n-1)\lambda R$$

Diameter of ring

$$D_n^2 = \frac{4n\lambda R}{\mu}$$

Air Film

$$D_n^2 = 4n\lambda R$$

Wavelength (λ)

$$\lambda = \frac{D_{n+p}^2 - D_n^2}{4PR}$$

Refractive index

$$\mu = \frac{[D_{n+p}^2 - D_n^2]_{\text{Air}}}{[D_{n+p}^2 - D_n^2]_{\text{liquid}}}$$

Q.1 If in a Newton's ring experiment, the air in the interspace is replaced by a liquid of refractive index

1.33. In what proportion would the diameter of the rings changed.

Given

$$\mu_{\text{air}} = 1$$

$$\mu_{\text{liquid}} = 1.33$$

Diameter of ring

$$D \propto \frac{1}{\sqrt{\mu}}$$

$$D_{\text{air}} = \frac{k}{\sqrt{\mu_{\text{air}}}} \quad \text{--- (1)}$$

$$D_{\text{liquid}} = \frac{k}{\sqrt{\mu_{\text{liquid}}}} \quad \text{--- (2)}$$

Divide (2) by (1)

$$\frac{D_{\text{liquid}}}{D_{\text{air}}} = \frac{k}{\sqrt{\mu_{\text{liquid}}}} \times \frac{\sqrt{\mu_{\text{air}}}}{k}$$

$$\frac{D_{\text{liquid}}}{D_{\text{air}}} = \sqrt{\frac{\mu_{\text{air}}}{\mu_{\text{liquid}}}}$$

$$\frac{D_{\text{liquid}}}{D_{\text{air}}} = \sqrt{\frac{1}{1.33}}$$

$$= 0.867$$

$$D_{\text{liquid}} = 0.867 D_{\text{air}}$$

Q.2 A light source of wavelength $6000 \text{ \AA}$ is used along with Plano – convex lens with radius of curvature equal to 100 cm in a Newton's ring arrangement. Find the diameter of the 15^{th} dark ring.

Given

$$\lambda = 6000 \text{ \AA}$$

$$R = 100 \text{ cm}$$

$$n = 15$$

$$\mu = 1$$

We know that

$$D_n^2 = \frac{4n\lambda R}{\mu}$$

$$D_{15}^2 = \frac{4 \times 15 \times 6000 \times 10^{-8} \times 100}{1}$$

$$D_{15}^2 = 3.6 \times 10^{-8} = 0.36$$

$$D_{15} = 0.6 \text{ cm}$$

$$1 \text{ \AA} = 10^{-10} \text{ m}$$

$$1 \text{ \AA} = 10^{-8} \text{ cm}$$

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Q. 3 Newton's rings are observed normally in reflected light of wavelength $6000 \text{ \AA}$. The diameter of 10^{th} dark ring is 0.50 cm . Find the radius of curvature of the lens and the thickness of the air film.

Given

$$\lambda = 6000 \text{ \AA}$$

$$n = 10$$

$$D_{10} = 0.50 \text{ cm}$$

$$R = ?$$

$$t = ?$$

$$D_n^2 = 4n\lambda R$$

$$D_{15}^2 = 4 \times 10 \times 6000 \times R$$

$$(0.50)^2 = 24 \times 10^4 R$$

$$R = \frac{0.50 \times 0.50}{24 \times 10^4} = \frac{2500}{24}$$

$$R = 104.16 \text{ cm}$$

$$t = \frac{D_{15}^2}{8R}$$

$$t = \frac{(0.50)^2 \times 24}{8 \times 2500}$$

$$t = 3 \times 10^{-4} \text{ cm} \quad \checkmark$$

Q. 4 In Newton's rings experiment the diameter of 4th and 12th dark ring are 0.400 cm and 0.700 cm respectively. Deduce the diameter of 20th dark ring

Given

$$D_4 = 0.4 \text{ cm}$$

$$D_{12} = 0.7 \text{ cm}$$

Let D_n = Diameter of n^{th} ring

D_{n+p} = Diameter of $(n+p)^{\text{th}}$ ring

We know that

$$D_{n+p}^2 - D_n^2 = 4p\lambda R$$

$$D_{12}^2 - D_4^2 = 4 \times 8 \times \lambda R \quad \text{--- ①}$$

Also

$$D_{20}^2 - D_4^2 = 4 \times 16 \times \lambda R \quad \text{--- ②}$$

Divide eqn ② by ①

$$\frac{D_{20}^2 - D_4^2}{D_{12}^2 - D_4^2} = \frac{4 \times 16 \times \lambda R}{4 \times 8 \times \lambda R}$$

$$\frac{D_{20}^2 - D_4^2}{D_{12}^2 - D_4^2} = 2$$

$$D_{20}^2 - D_4^2 = 2D_{12}^2 - 2D_4^2$$

$$D_{20}^2 = 2D_{12}^2 - D_4^2$$

$$D_{20}^2 = 2(0.7)^2 - (0.4)^2$$

$$D_{20}^2 = 0.98 - 0.16$$

$$D_{20} = 0.906 \text{ cm}$$

Q. 5 Newton's rings are observed by keeping a spherical surface of 100 cm radius on a plane glass plate. If the diameter of 15th bright ring is 0.590 cm and diameter of 5th ring 0.336 cm.

What is the wavelength of light used ?

Given

$$R = 100 \text{ cm}$$

$$D_{15} = 0.590 \text{ cm}$$

$$D_5 = 0.336 \text{ cm}$$

We know that

$$\lambda = \frac{D_{n+p}^2 - D_n^2}{4pR}$$

$$\lambda = \frac{D_{15}^2 - D_5^2}{4 \times 10 \times 100}$$

$$= \frac{(0.590)^2 - (0.336)^2}{4 \times 10 \times 100}$$

$$\lambda = 5880 \text{ \AA}$$

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Q. 6 Newton's rings are formed in reflected light of wavelength $6000 \text{ \AA}$ with a liquid between the plane and curved surface. If the diameter of 6th bright ring is 3.1 mm and the radius of curvature of the curved surface is 100 cm , calculate the refractive index of the liquid.

Given

$$\lambda = 6000 \text{ \AA}$$

$$D_6 = 3.1 \text{ mm}$$

$$= 0.31 \text{ cm}$$

$$R = 100 \text{ cm}$$

$$n = 6$$

Diameter of Bright ring

$$D_n^2 = \frac{2(2n-1)\lambda R}{\mu}$$

$$\mu = \frac{2(2n-1)\lambda R}{D_n^2}$$

$$= \frac{2 \times 11 \times 6000 \times 10^{-8} \times 100}{(0.31)^2}$$

$$\mu = 1.373$$

UNIT : Wave Optics

- Q.1** Why the center of Newton's ring in reflected system is dark?
- Q.2** Describe and explain the formation of Newton's rings in transmitted monochromatic light. Deduce the necessary expression for bright and dark rings.
- Q.3** Discuss the formation of Newton's rings. Show that the diameters of the bright rings are proportional to the square root of odd natural numbers.
- Q.4** Describe the formation of Newton's rings in reflected monochromatic light. Show that in reflected light, the diameters of dark rings are proportional to the square roots of natural numbers.
- Q.5** Describe how Newton's ring experiment can be used to determine the wavelength of light.
- Q.6** Describe how Newton's ring experiment can be used to determine the refractive index of a liquid.

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