

Review Quizes

I want to re-index this from 0 to 9

$$\sum_{i=1}^{10} i^2 \leftarrow \sum_{k=0}^9 (k+1)^2 = \sum_{i=0}^9 (i+1)^2$$

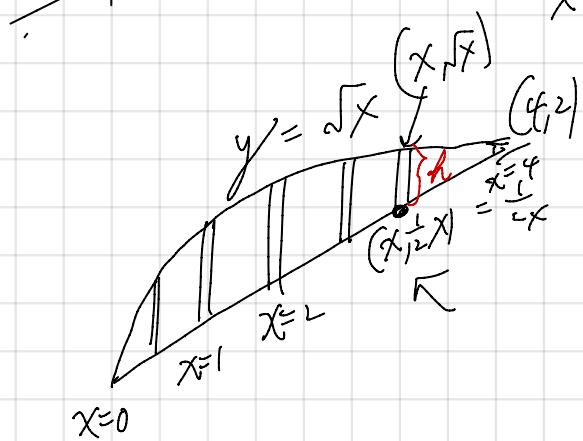
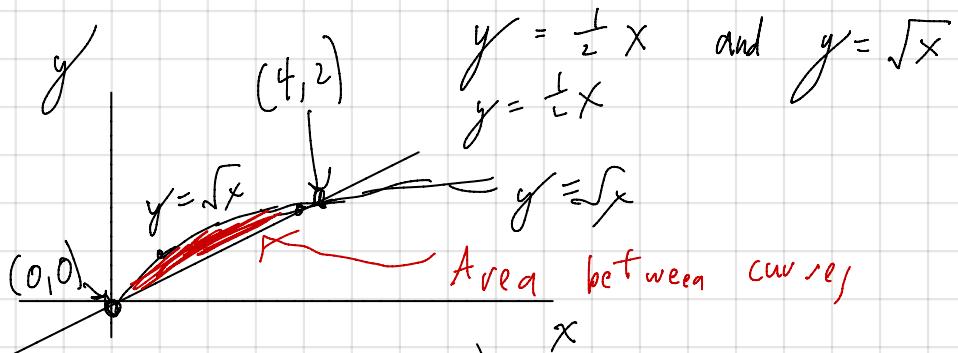
$$k = i - 1$$

$$k+1 = i$$

Section 6.1

Area between curves. (6.1 leads into 6.2, 6.3)

Example Problem What is the area between the curves



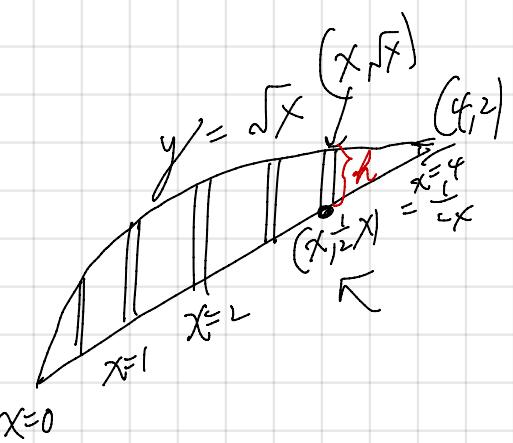
Let x be the horizontal position of each rectangle

We divide the region into a "large" (maybe infinite) number of vertical rectangles, that are very thin, and then we add up the area of the rectangles.

$$x = 4 \text{ height } + \text{thickness}$$

$$h = \sqrt{x} - \frac{1}{2}x$$

$$\int_{x=0}^{x=4} (\sqrt{x} - \frac{1}{2}x) dx$$



We divide the region into a "large" (maybe infinite?) number of vertical rectangles, that are very thin, and then we add up the area of the rectangles.

Let x be the horizontal position of each rectangle

$$\int_0^4 (\sqrt{x} - \frac{1}{2}x) dx$$

$x=0$ $x=4$ height thickness
 $b = \sqrt{x} - \frac{1}{2}x$

$$\begin{aligned} \int_0^4 \left(x^{\frac{1}{2}} - \frac{1}{2}x \right) dx &= \left[\frac{2}{3}x^{\frac{3}{2}} - \frac{1}{4}x^2 \right]_0^4 = \frac{2}{3} \cdot 8 - \frac{1}{4} \cdot 16 \\ &= \frac{16}{3} - 4 = \frac{16}{3} - \frac{12}{3} = \left(\frac{4}{3} \right) \end{aligned}$$

FTC

$$\int_a^b f(x) dx = F(b) - F(a)$$

where $F(x)$ is any particular antiderivative of $f(x)$

$$F'(x) = f(x)$$

$$\begin{aligned} \int_0^4 \left(x^{\frac{1}{2}} - \frac{1}{2}x \right) dx &= \left[\underbrace{\frac{2}{3}x^{\frac{3}{2}} - \frac{1}{4}x^2}_{+ 17} \right]_0^4 \\ &= \left(\frac{4}{3} + 17 \right) - (0 + 17) = \left(\frac{4}{3} \right) \end{aligned}$$

