

# Fission yields measurement in inverse kinematics at relativistic energies

The R3B/SOFIA experiments at the GSI/FRS facility

**FIESTA Workshop**

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# The SOFIA project

## 1. Inverse kinematic at relativistic energies

- Pros & cons
- Which setup ?
- Which observables ?
- Which physics cases ?

## 2. Some results

- Study of fission along the uranium chain: high statistics data for application
- Study of fission along the thorium chain: correlated data to study microscopic effects



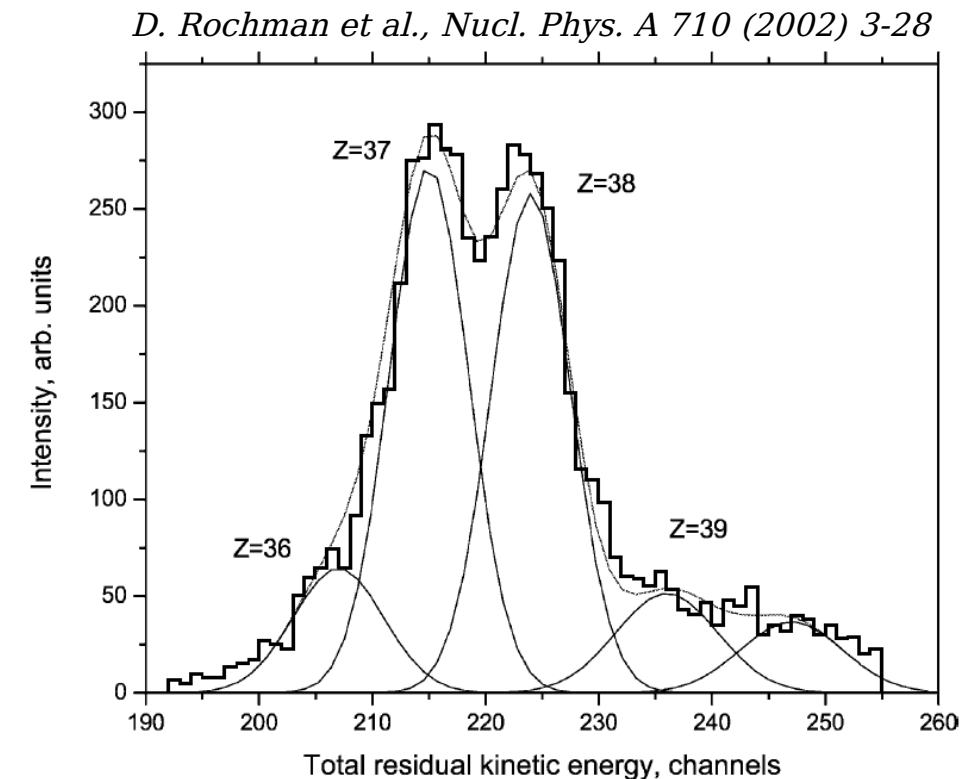
# 1 ■ Inverse kinematics at relativistic energies

An alternative method for fission studies

# Limitation of the direct kinematics for fission yields

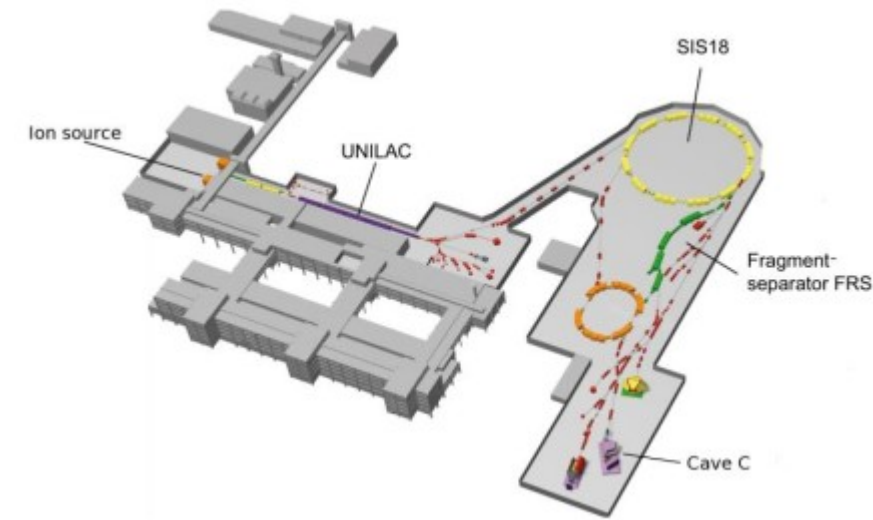
Nuclear charge measurement limited to  $Z \leq 40$  in direct kinematics

- DIRECT KINEMATICS: n-, p-, LCP-beam on an actinide target (at rest)
- FF are emitted with low energy in the lab frame: problem of ionic charge states
- FF are emitted in  $4\pi$ : low geometrical efficiency
- Long-lived actinide targets only
- Availability of actinide targets

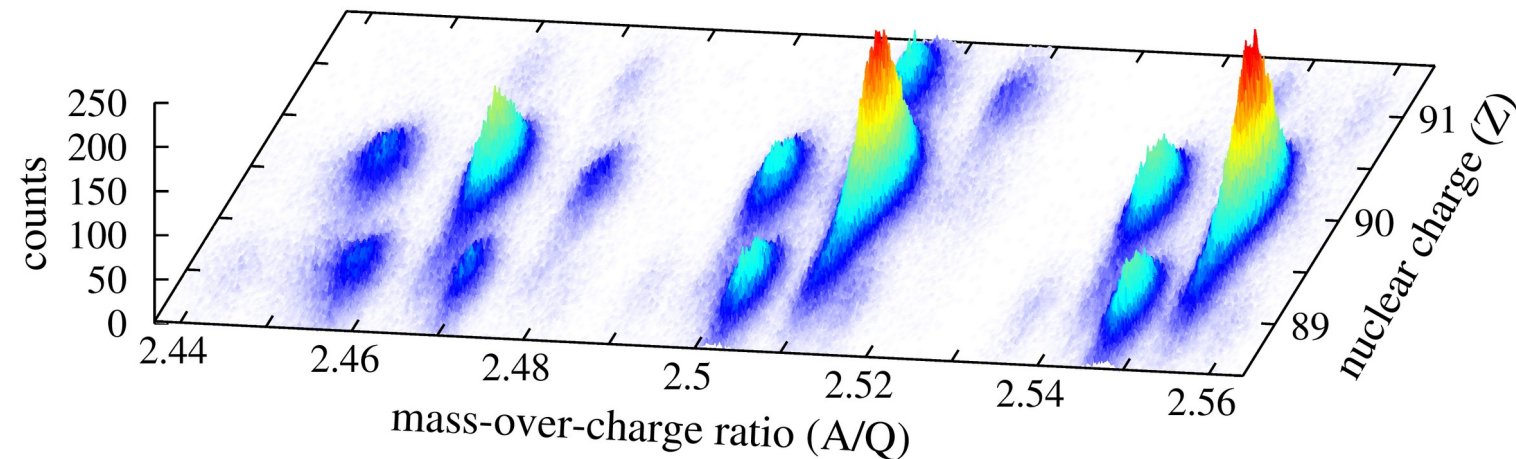
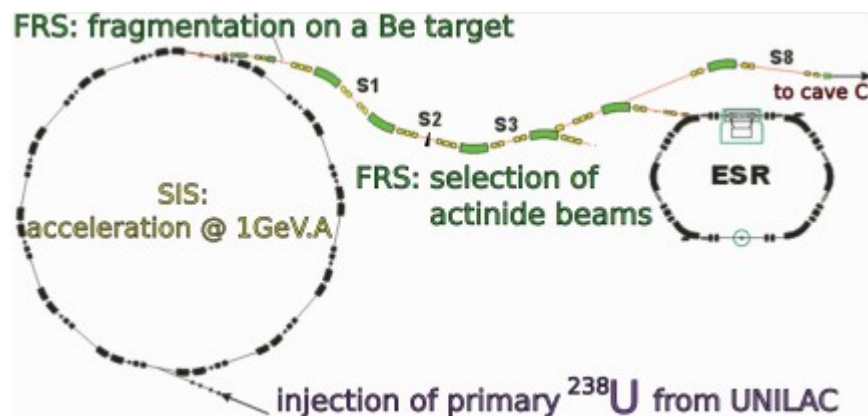


# The inverse kinematics at relativistic energies (I)

## Production of radioactive fissioning nuclei in-flight by fragmentation



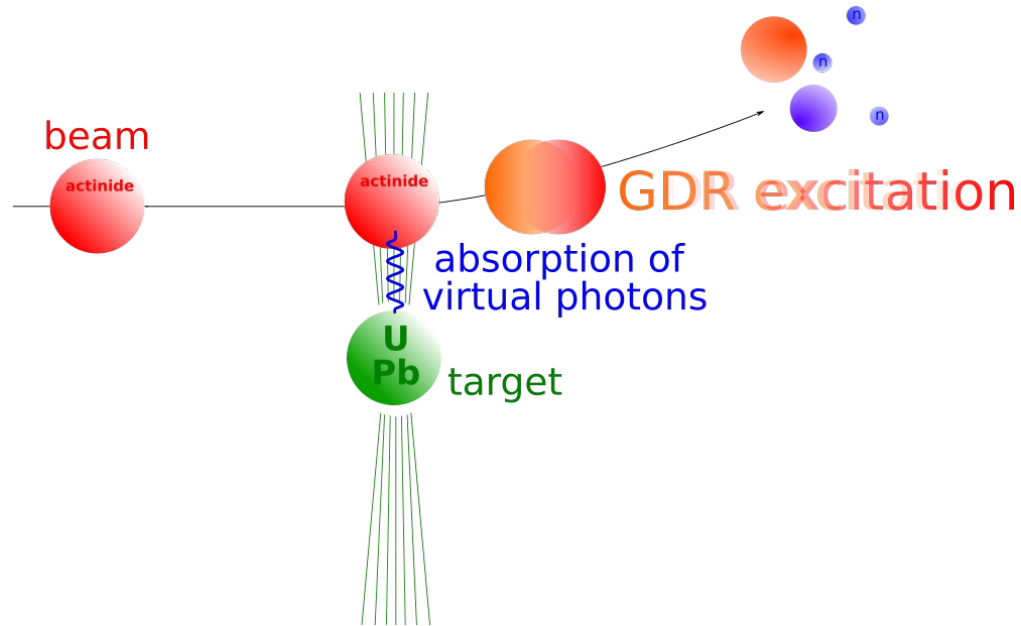
- @GSI, production of primary beam up to  $^{238}\text{U}$  at 1 A.GeV
- @FRS, fragmentation of  $^{238}\text{U}$  on a Be target and production of **cocktail beams**  $\sim 750$  A.MeV with a selection in  $(B\rho, \Delta E)$  around  $(A/Z, Z)$



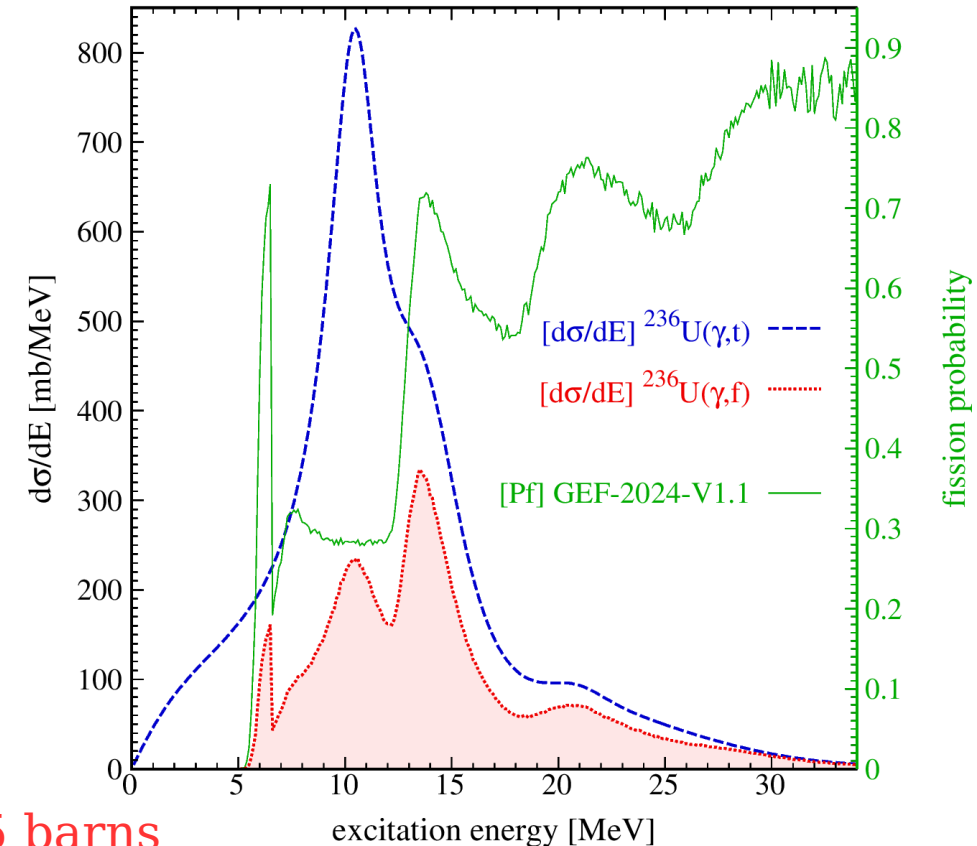
Identification plot for 3 different FRS settings around  $^{222}\text{Th}$ ,  $^{226}\text{Th}$  and  $^{230}\text{Th}$

# Electromagnetic induced fission

A surrogate reaction with large cross section to study low energy fission at relativistic energies



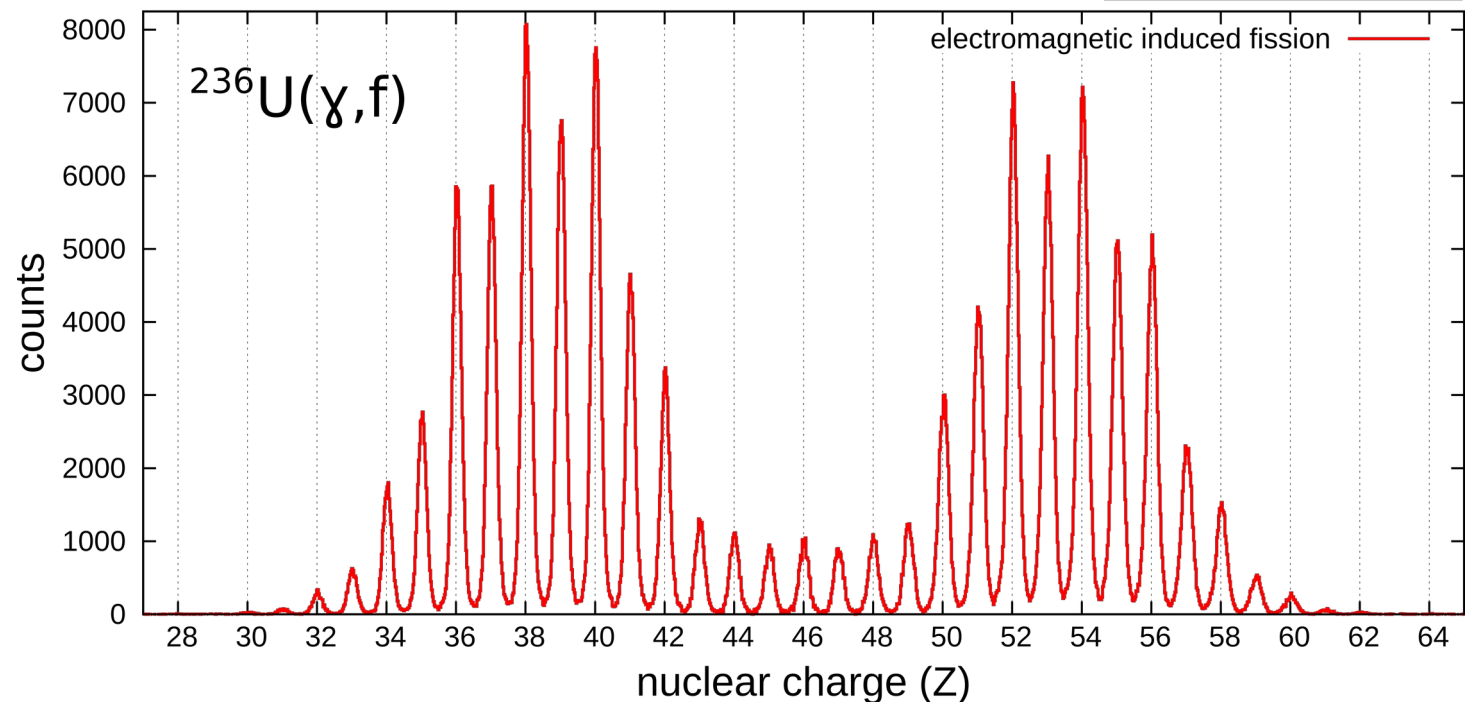
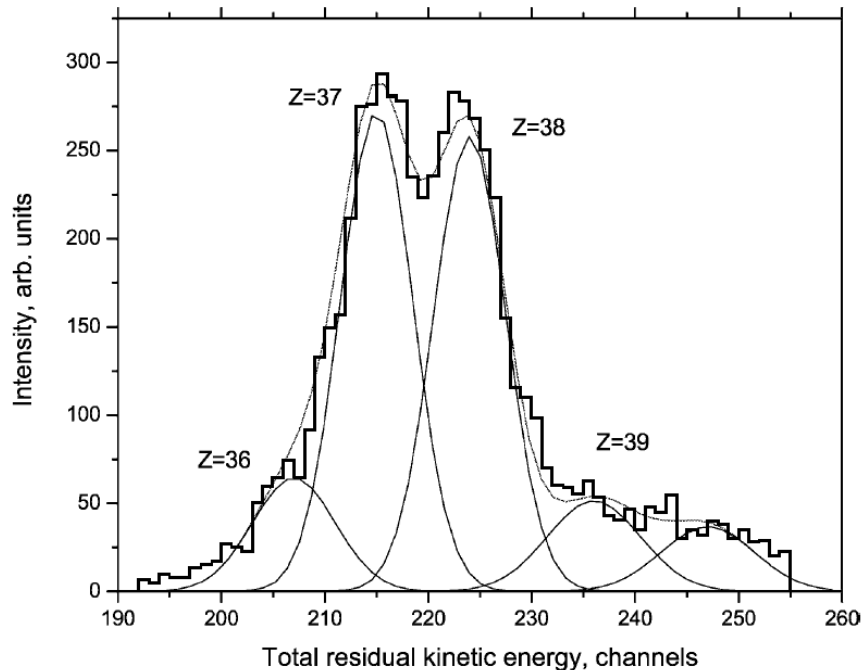
- Average excitation energy:  $\langle E^* \rangle \sim 14.6 \text{ MeV}$
- Average electromagnetic induced fission:  $\sigma_{^{236}\text{U}(\gamma, f)} \sim 2.5 \text{ barns}$
- Surrogate reaction:  $^{236}\text{U}(\gamma, f) \rightleftharpoons ^{235}\text{U}(n_{8.2\text{MeV}}, f)$



# The inverse kinematics at relativistic energies (II)

A unique tool to get an absolute resolution in charge distribution on the full FF range

- At GSI, production of radioactive relativistic beam at FRS ( $\sim 750$  A.MeV)
- Ions are fully stripped: Energy loss measurement directly gives the atomic number

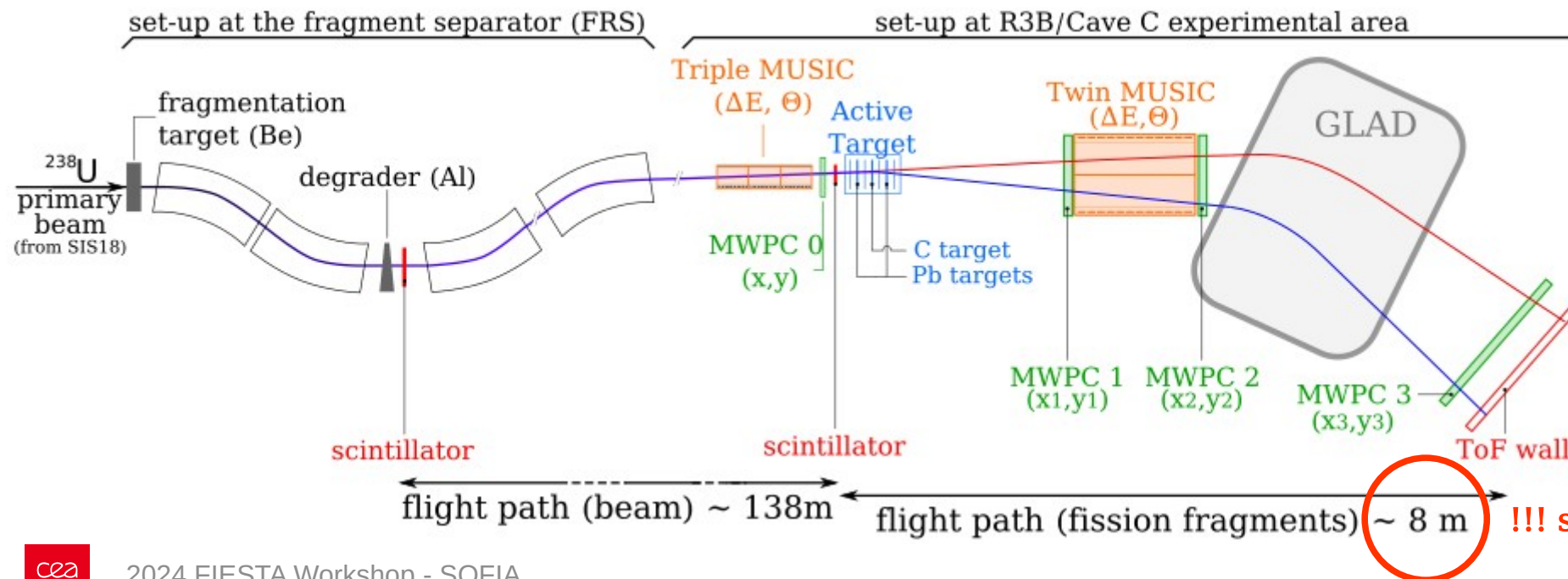




# The inverse kinematics at relativistic energies (III)

Lorentz boost: all FF are emitted at forward angles  $\Rightarrow$  very high geometrical efficiency

- Nuclear charge and mass of both FF in coincidence
- Pioneer experiment with Z only at GSI by K.-H. Schmidt *et al.*, Nucl. Phys. A 665 (2000) 221
- Mass identification based on the  $\Delta E - B\rho - \text{ToF}$  method with  $A/Z \sim B\rho / \beta\gamma$



Both FF in coincidence !

RESOLUTION [FWHM]

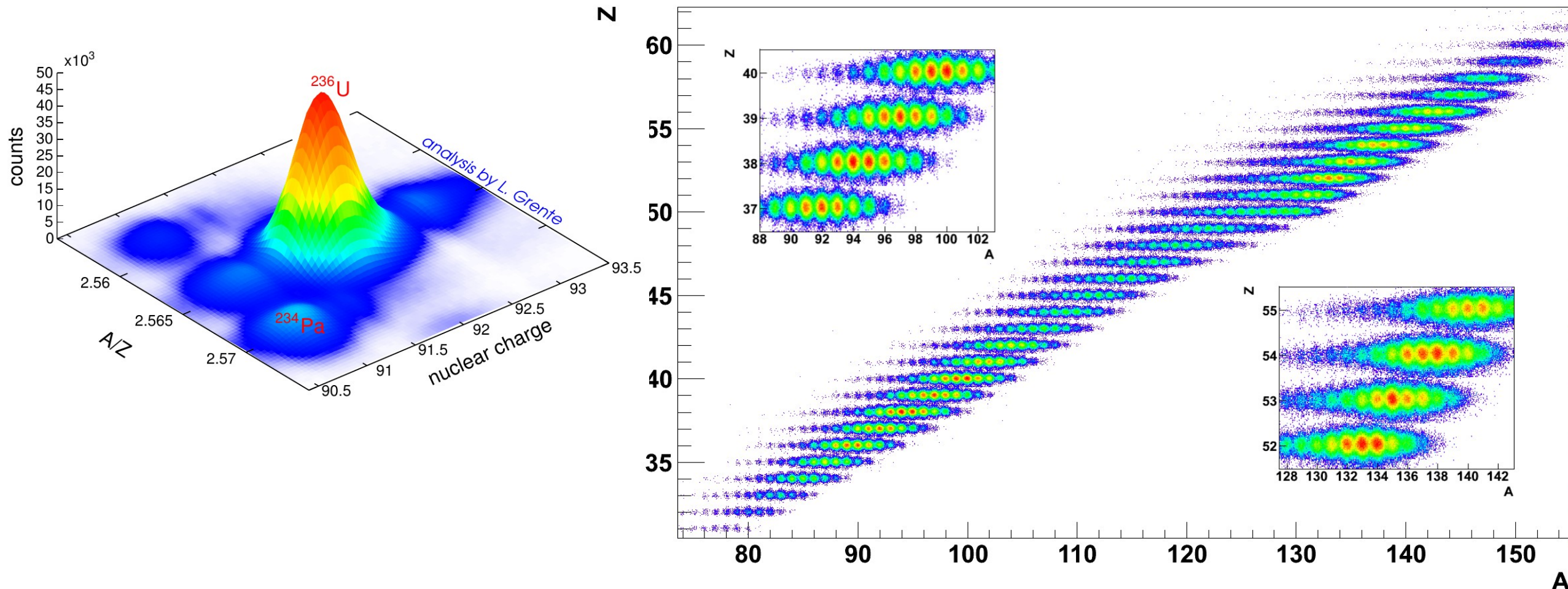
$x = 100 \text{ to } 300 \mu\text{m}$

**ToF = 35 ps**



# (Z,A) identification for the $^{236}\text{U}(\gamma, f)$ study

RESOLUTION [FWHM] :  $\Delta Z = 0.31$  to  $0.34$  charge unit &  $\Delta A = 0.55$  to  $0.80$  mass unit



# Fission observables

Identification of both FF after the prompt neutron emission and prior to any  $\beta$ -decay

- **Fission yields** from the isotopic identification fission fragments

$$Y(Z), Y(A_{\text{post}}), Y(N_{\text{post}}), Y(Z, A_{\text{post}})$$

$\Rightarrow Z$  : direct measurement of the number of proton per fragment at scission

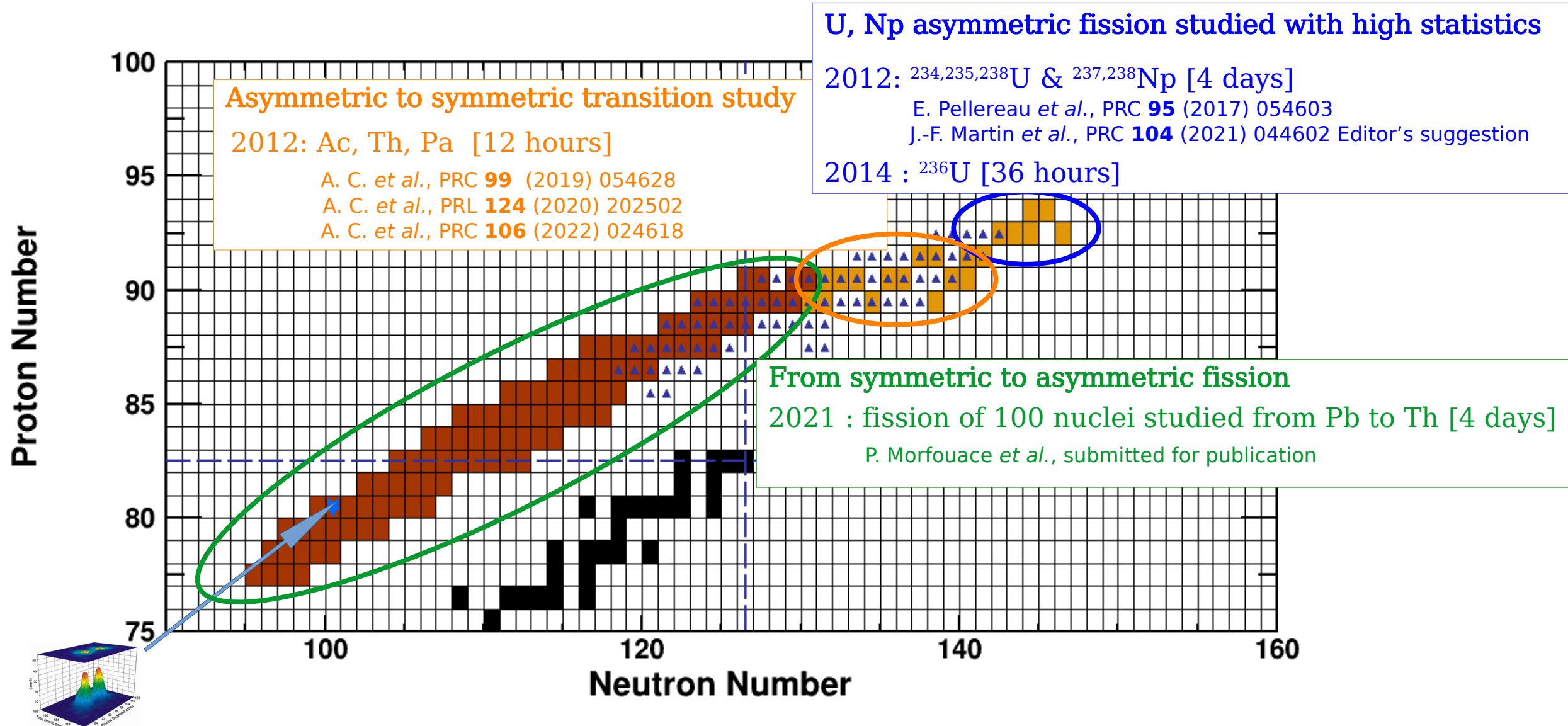
$\Rightarrow N_{\text{post}}$  : should be interpreted taking into account the evaporation phase

- **Total prompt-neutron multiplicity** from the mass measurement of beam and FF

$$\mathcal{V}_{\text{tot}} = A_{\text{beam}} - A_{\text{FF1}} - A_{\text{FF2}}$$

- **Total kinetic energy** from the velocity vectors reconstruction

# The SOFIA experiments



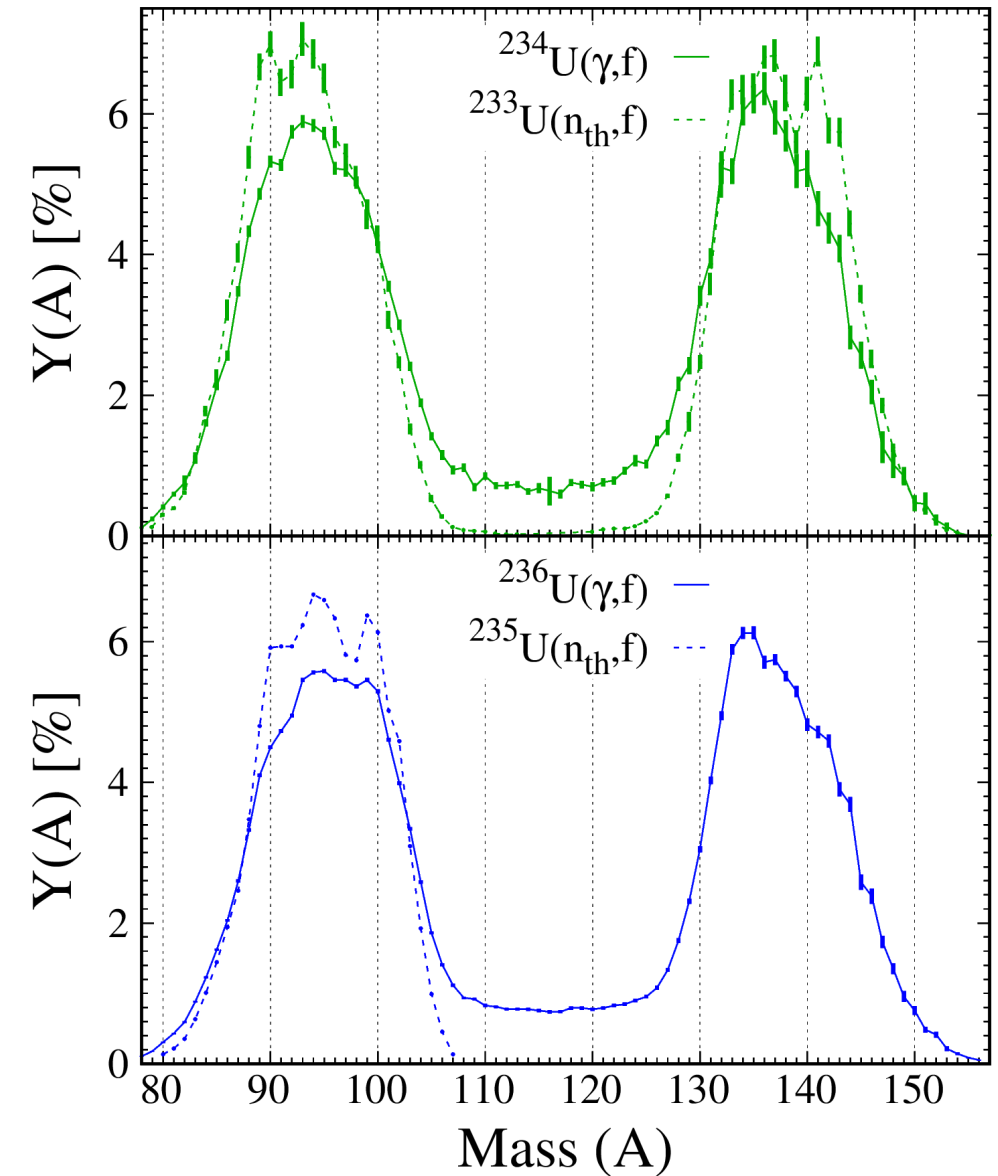
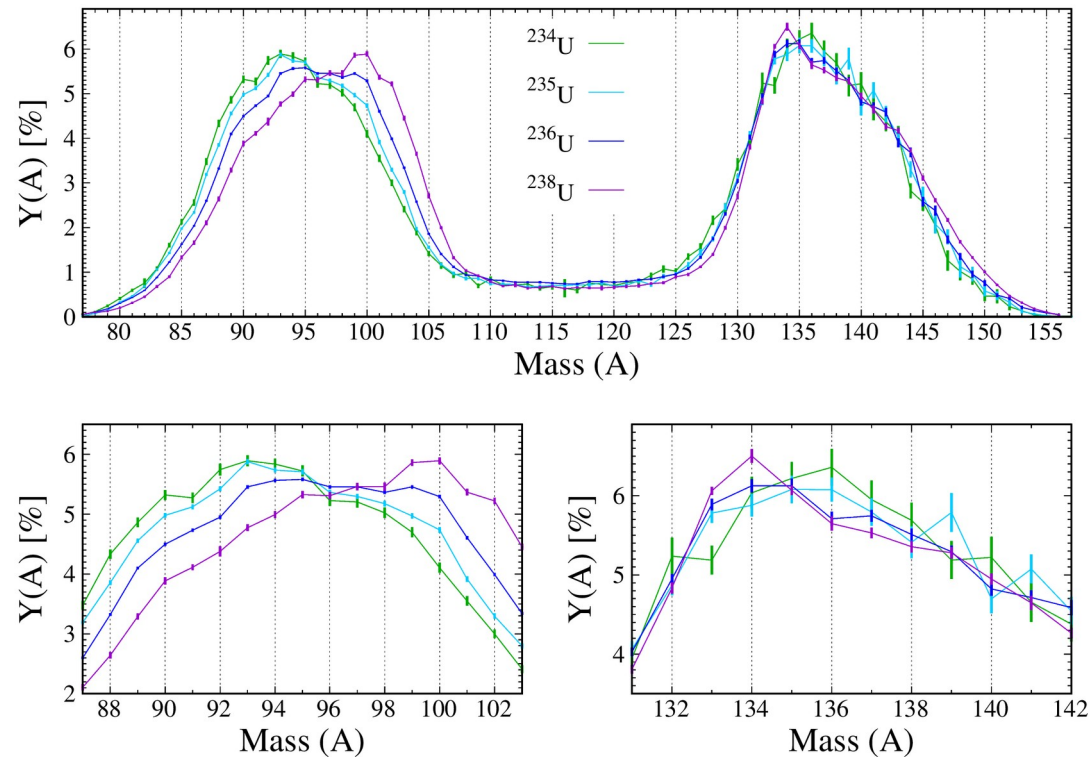


# 2.1 Along the U-chain

Accurate data for nuclear data need

# Isobaric yields

## Experimental results and comparison to $(n_{th},f)$

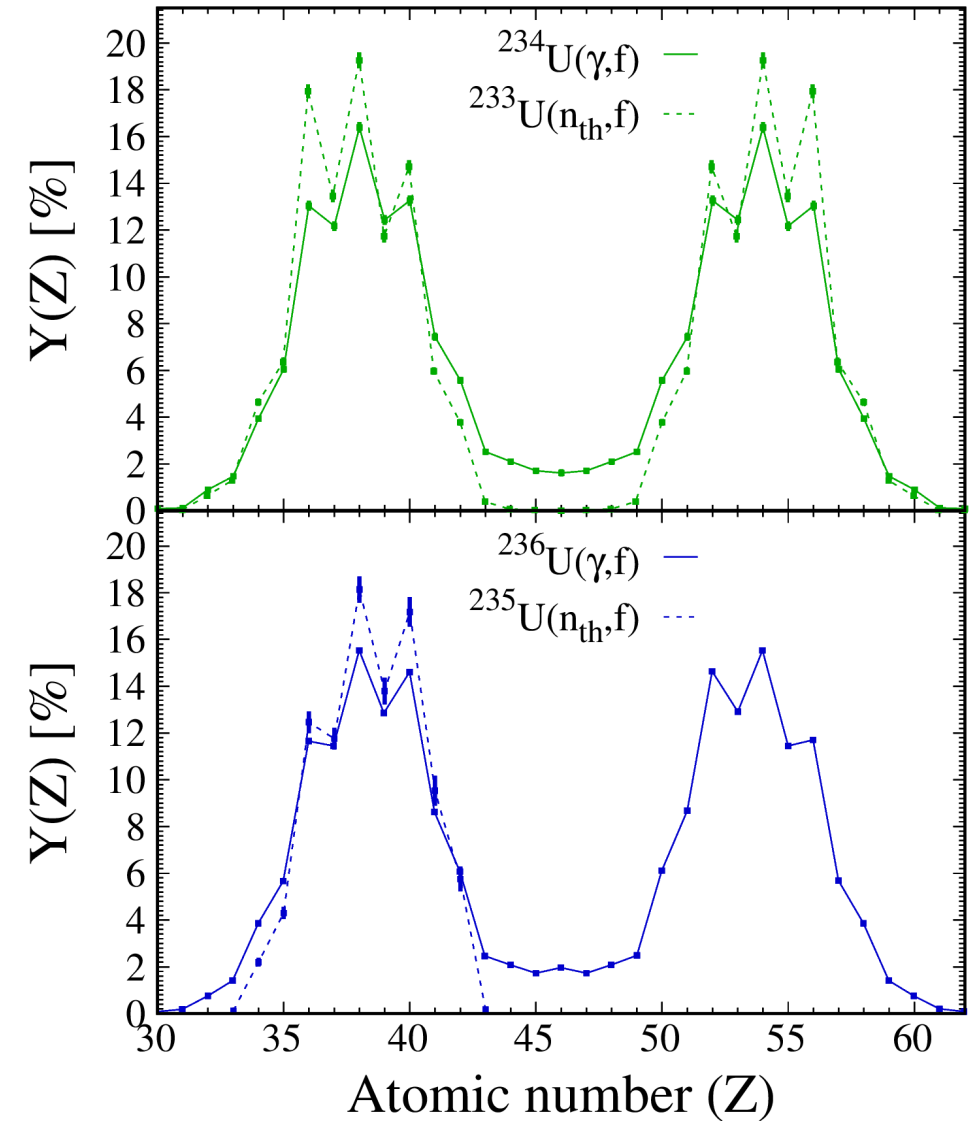
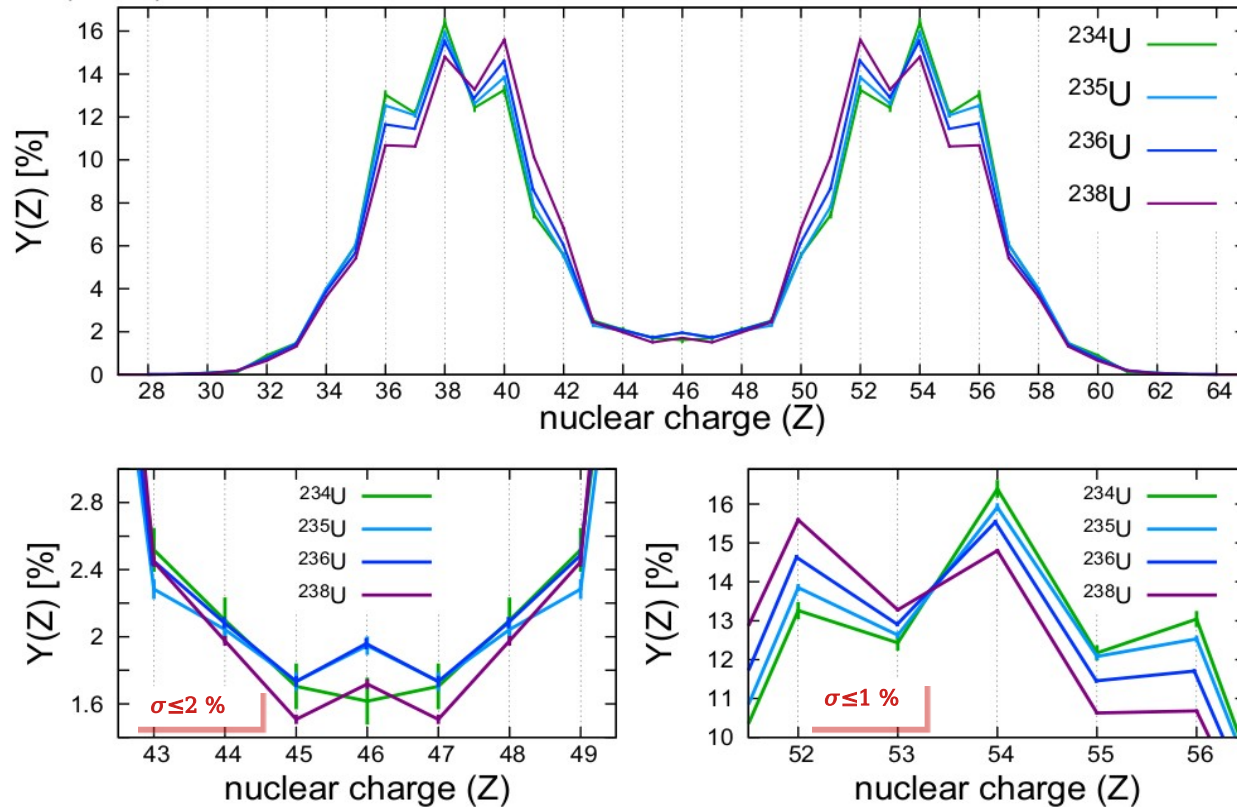


Analysis by L. Grente, J-F. Martin, E. Pellereau (CEA/DAM/DIF)



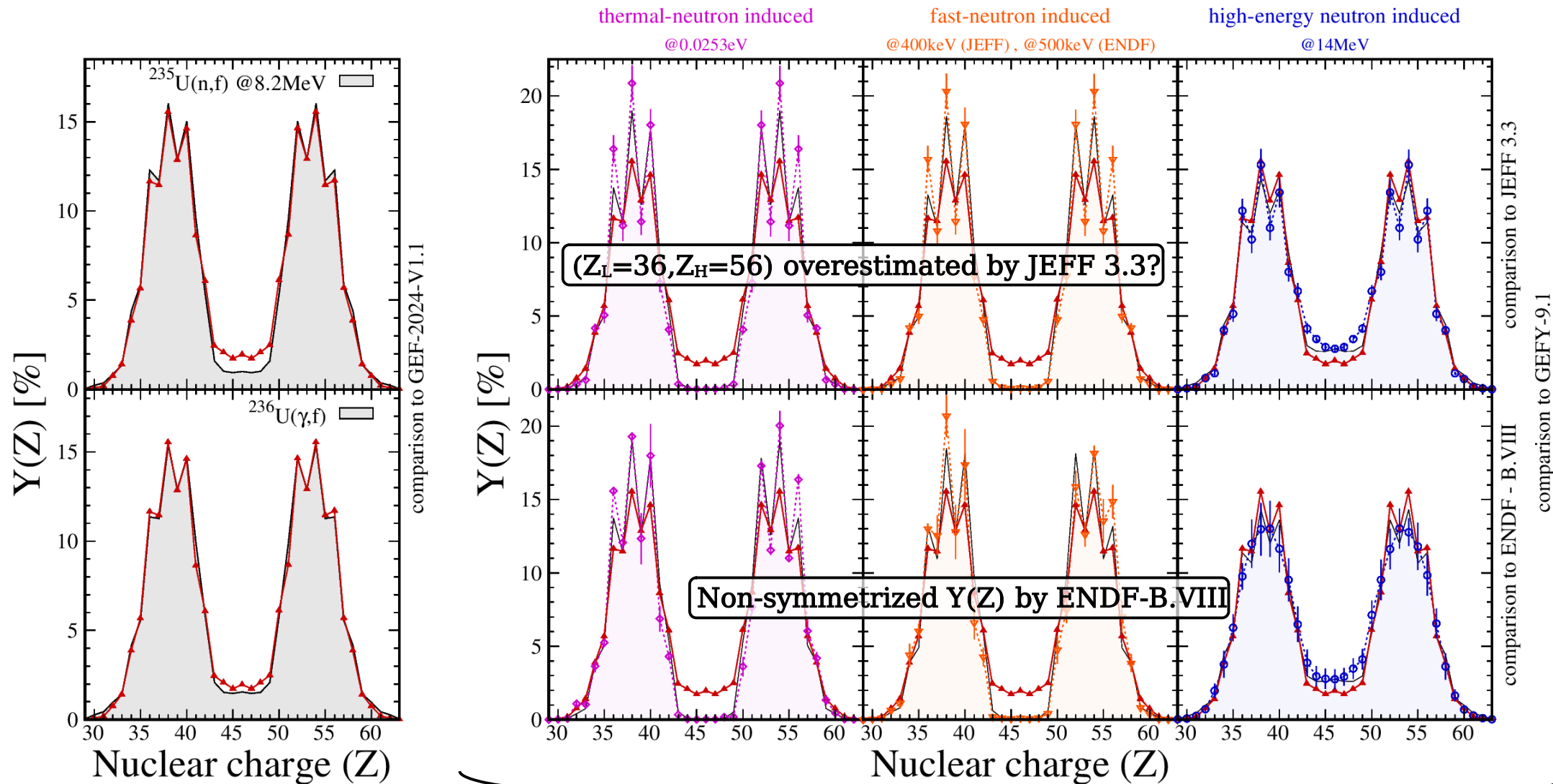
# Elemental yields (I)

Experimental results and comparison to  $(n_{th},f)$



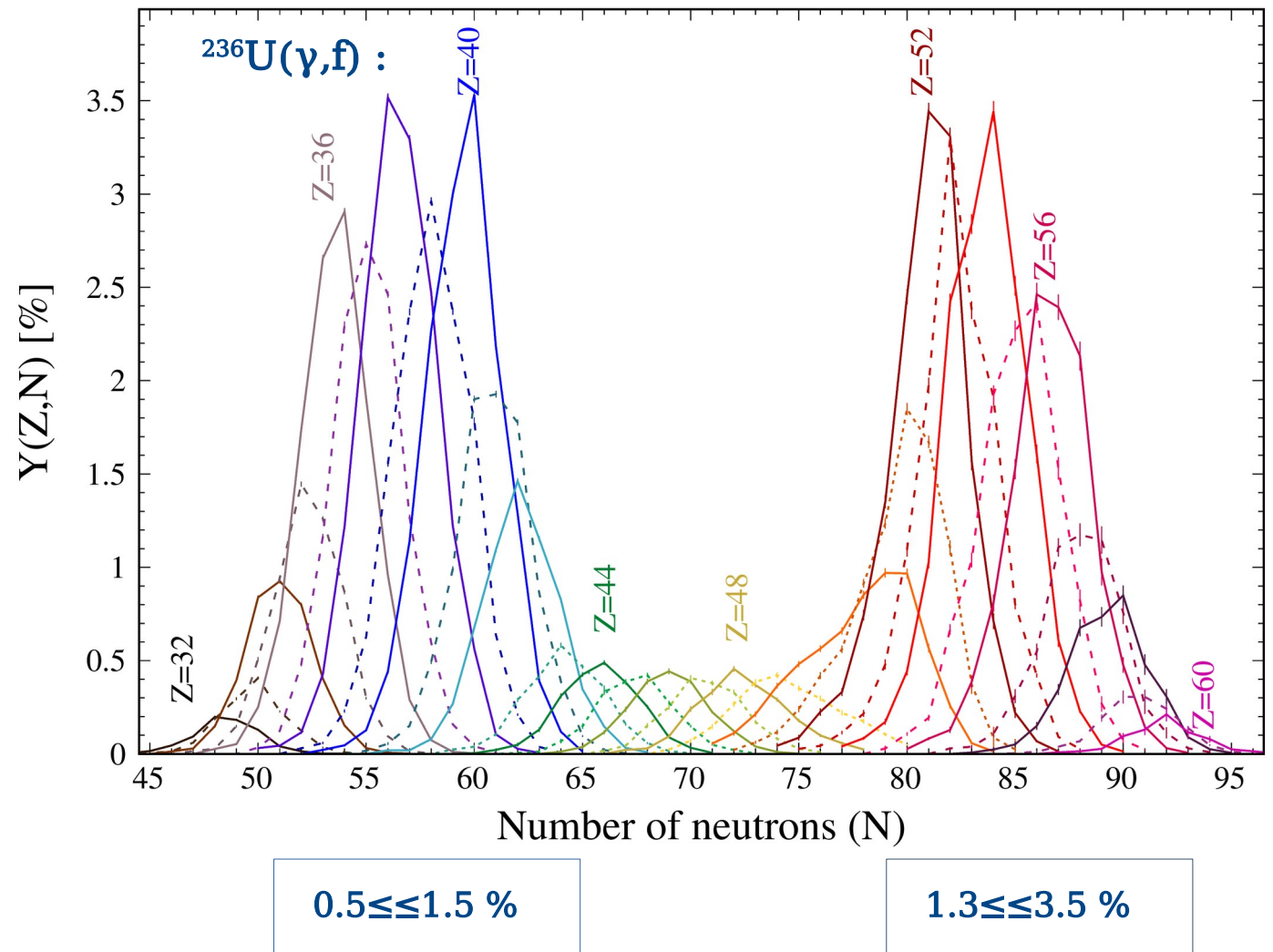
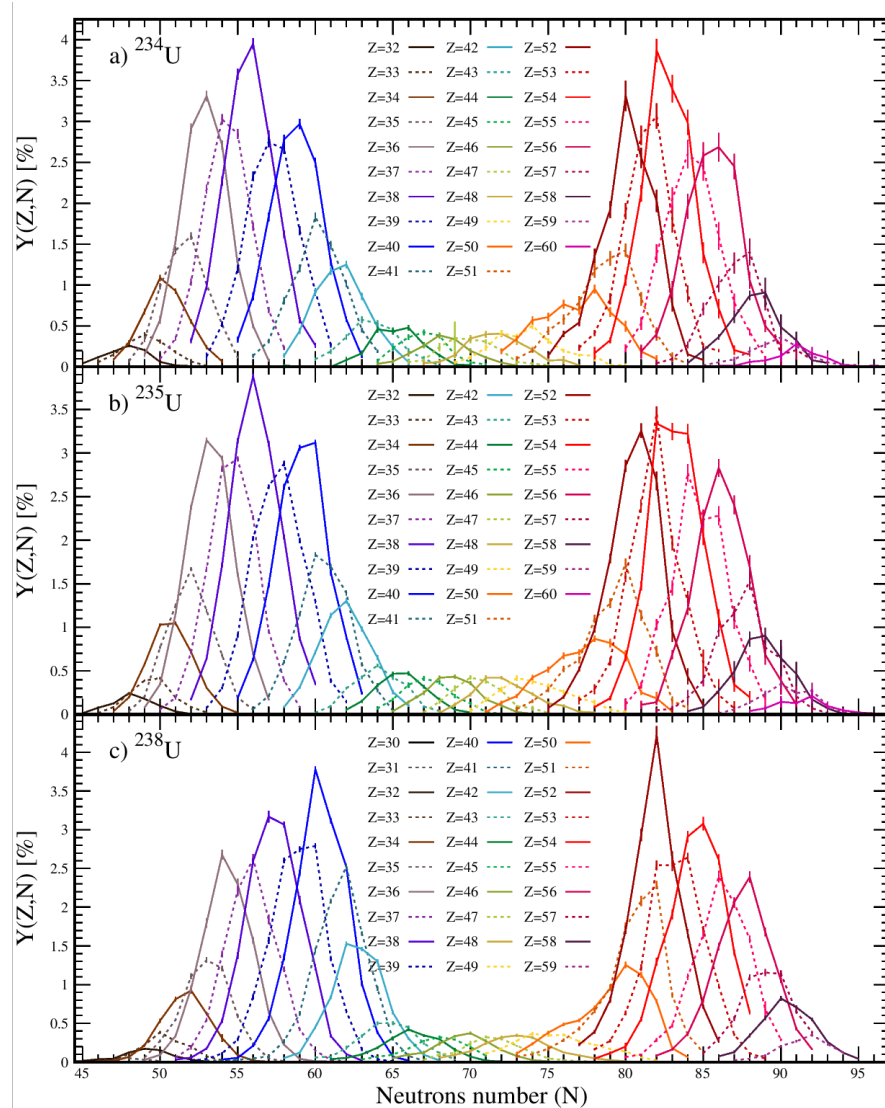
# Elemental yields (II)

## Comparison to GEF-2024-V1.1 and evaluations





# Isotopic yields





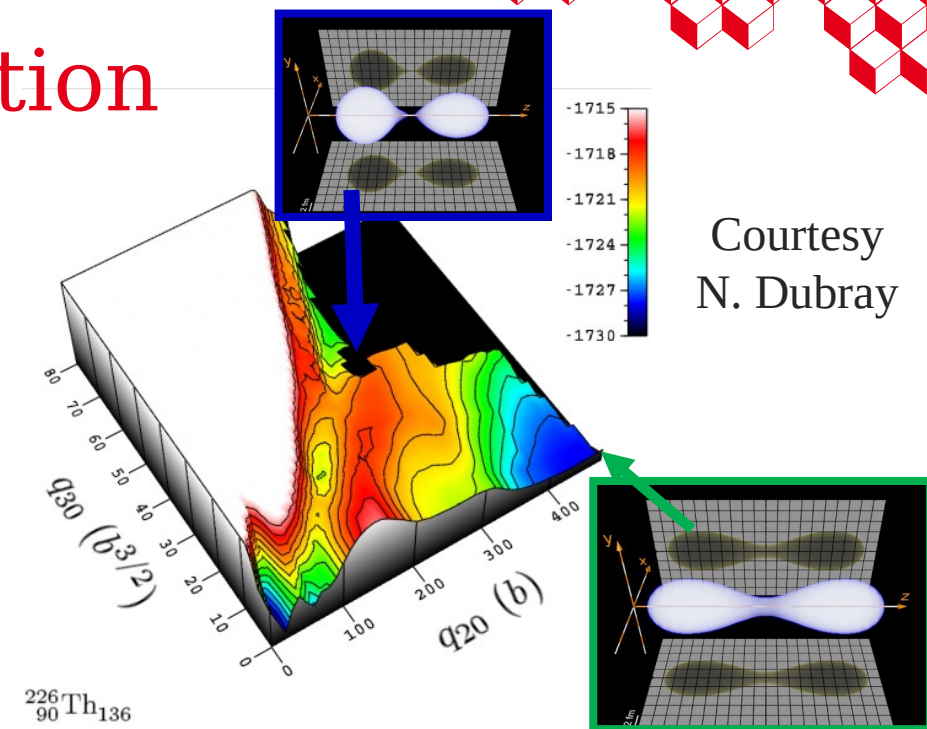
# 2.2 Along the Th-chain

Correlated data to study microscopic effects

# $\langle \nu_{\text{tot}} \rangle$ to probe scission configuration

## Three fission modes in the uranium region

- Proposed by Brosa *et al.*: 2 asymmetric, 1 symmetric
- One path on PES per mode due to different shell effects
- Each path reach the scission line at specific  $(Q_{20}, Q_{30})$



### STANDARD 1

ALMOST SPHERICAL HEAVY FF  
spherical ( $Z=50, N=82$ ) shells  
compact configuration

High TKE, low  $\nu$

### STANDARD 2

OCTUPOLE FF  
octupole p-shells in heavy FF  
main mode

### SUPER-LONG

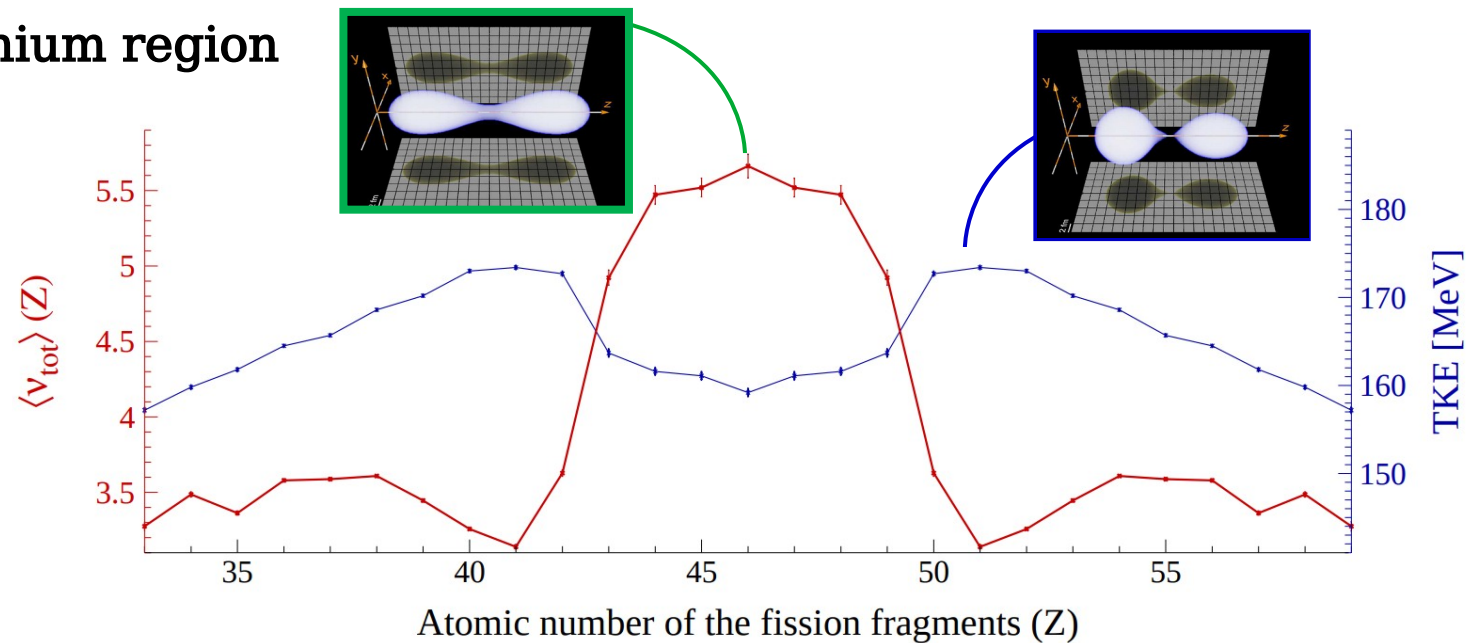
HIGHLY DEFORMED FF  
shell effects washed-out with  $E^*$   
deformed configuration

LOW TKE, HIGH  $\nu$

# $\langle \nu_{\text{tot}} \rangle$ to probe scission configuration

## Three fission modes in the uranium region

■  $^{235}\text{U}(\gamma, f)$  SOFIA results :



Analysis by J-F. Martin (CEA/DAM/DIF)

### STANDARD 1

ALMOST SPHERICAL HEAVY FF  
spherical (Z=50, N=82) shells  
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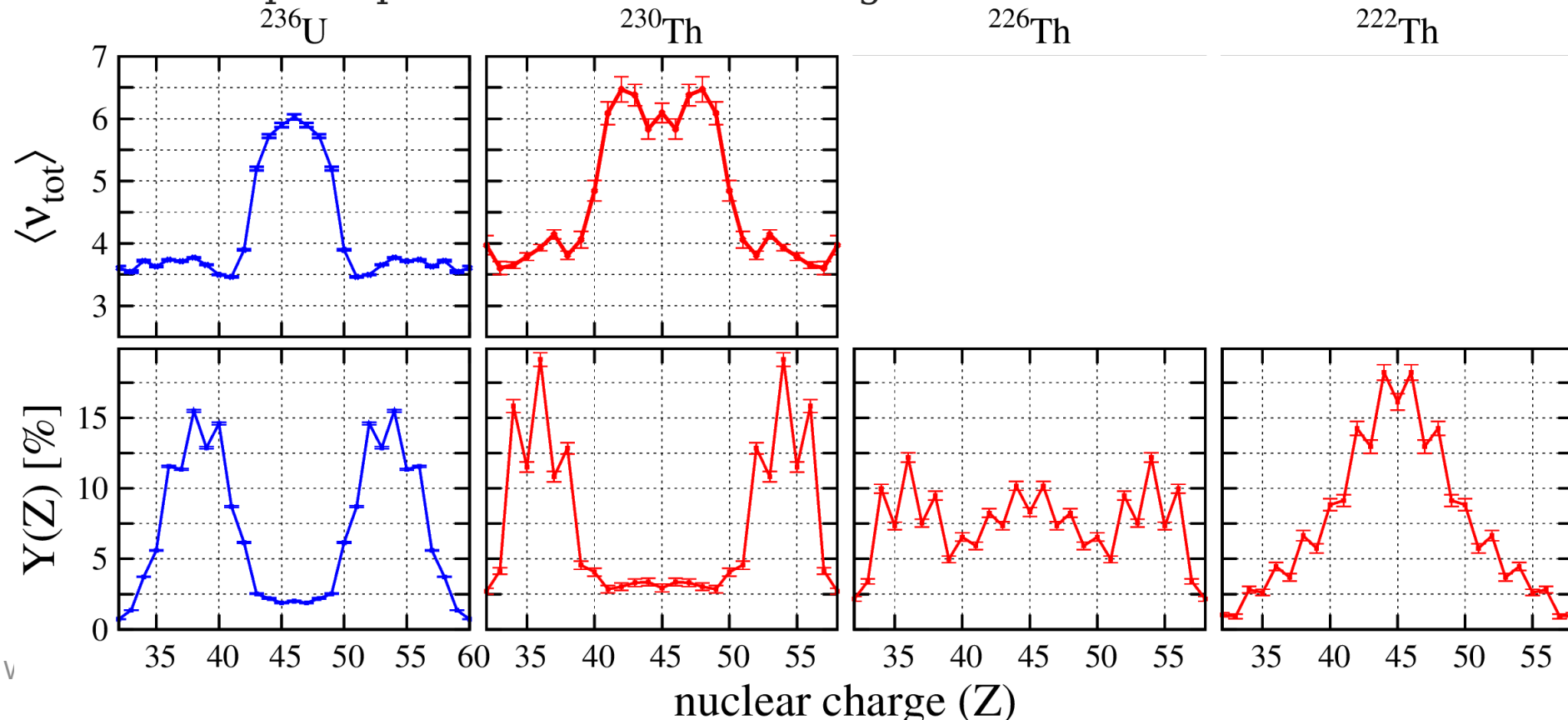
HIGHLY DEFORMED FF  
shell effects washed-out with E\*  
deformed configuration

LOW TKE, HIGH  $\nu$

# Correlation $Y(Z)$ vs $\langle \nu_{\text{tot}} \rangle$

For neutron deficient neutron isotopes ...

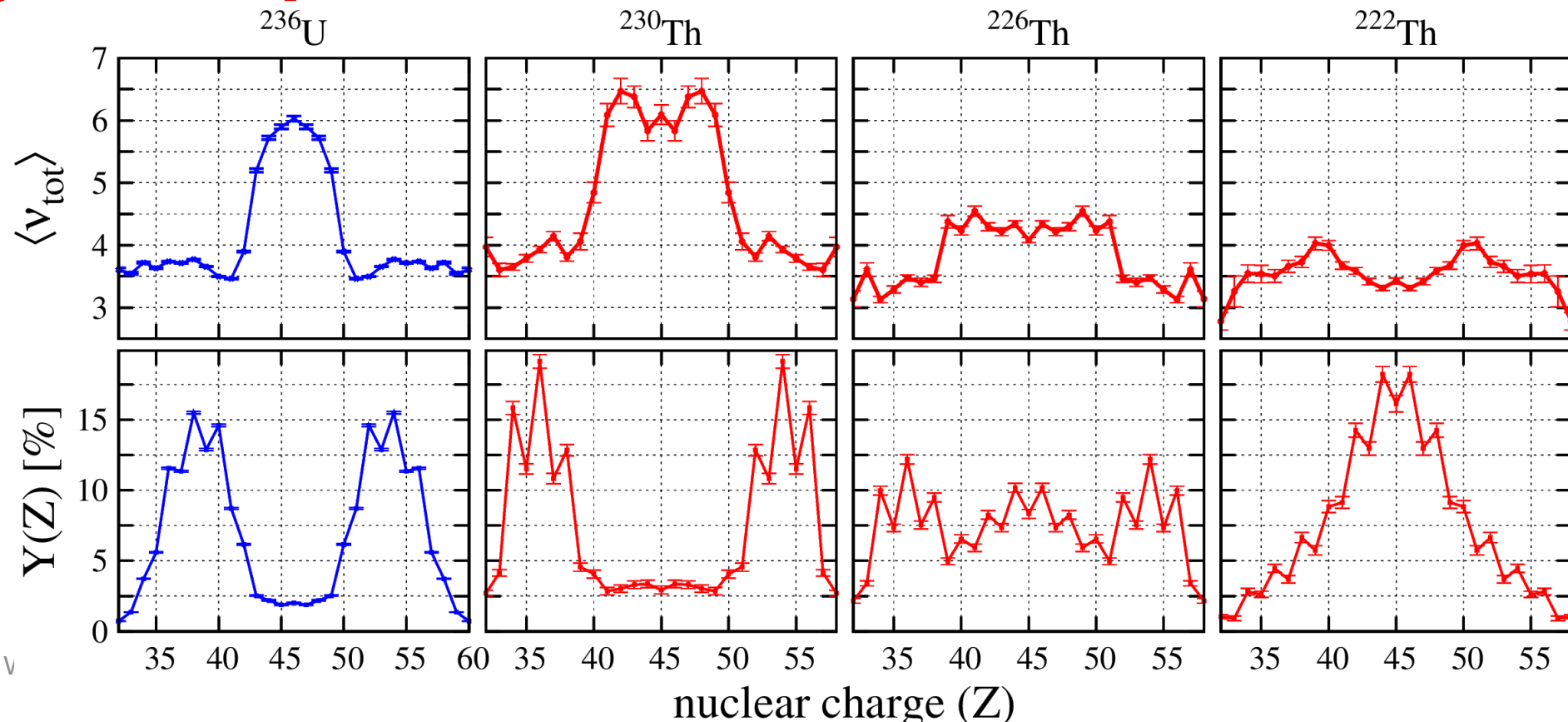
- Symmetric fission is becoming more and more important
- Odd-even staggering remains
- Correlated data helps to probe the scission configuration of the fission modes



# Correlation $Y(Z)$ vs $\langle \nu_{\text{tot}} \rangle$

For neutron deficient neutron isotopes ...

- Symmetric fission is becoming more and more important
- Odd-even staggering remains and  $\langle \nu_{\text{tot}} \rangle$  drop for symmetric fission of around 2.7 neutrons
- **New symmetric compact mode**



# Fission yields measurement with SOFIA

## Inverse kinematics at relativistic energies

Isotopic identification of both fission fragments in coincidence

High statistics data for accurate measurement

BUT : Excitation energy distribution is not measured

Mass of the compound nucleus limited to 238

## Set-up: SOFIA spectrometer combined with the FRS spectrometer

$\Delta E - B\rho - \text{ToF}$  method to identify in  $(Z,A)$  beam and **both FF**

## Observables:

$Y(Z)$ ,  $Y(A_{\text{post}})$ ,  $Y(N_{\text{post}})$ ,  $Y(Z, A_{\text{post}})$ ,  $\langle \nu_{\text{tot}} \rangle$ ,  $\langle \text{TKE} \rangle$

## Physics cases:

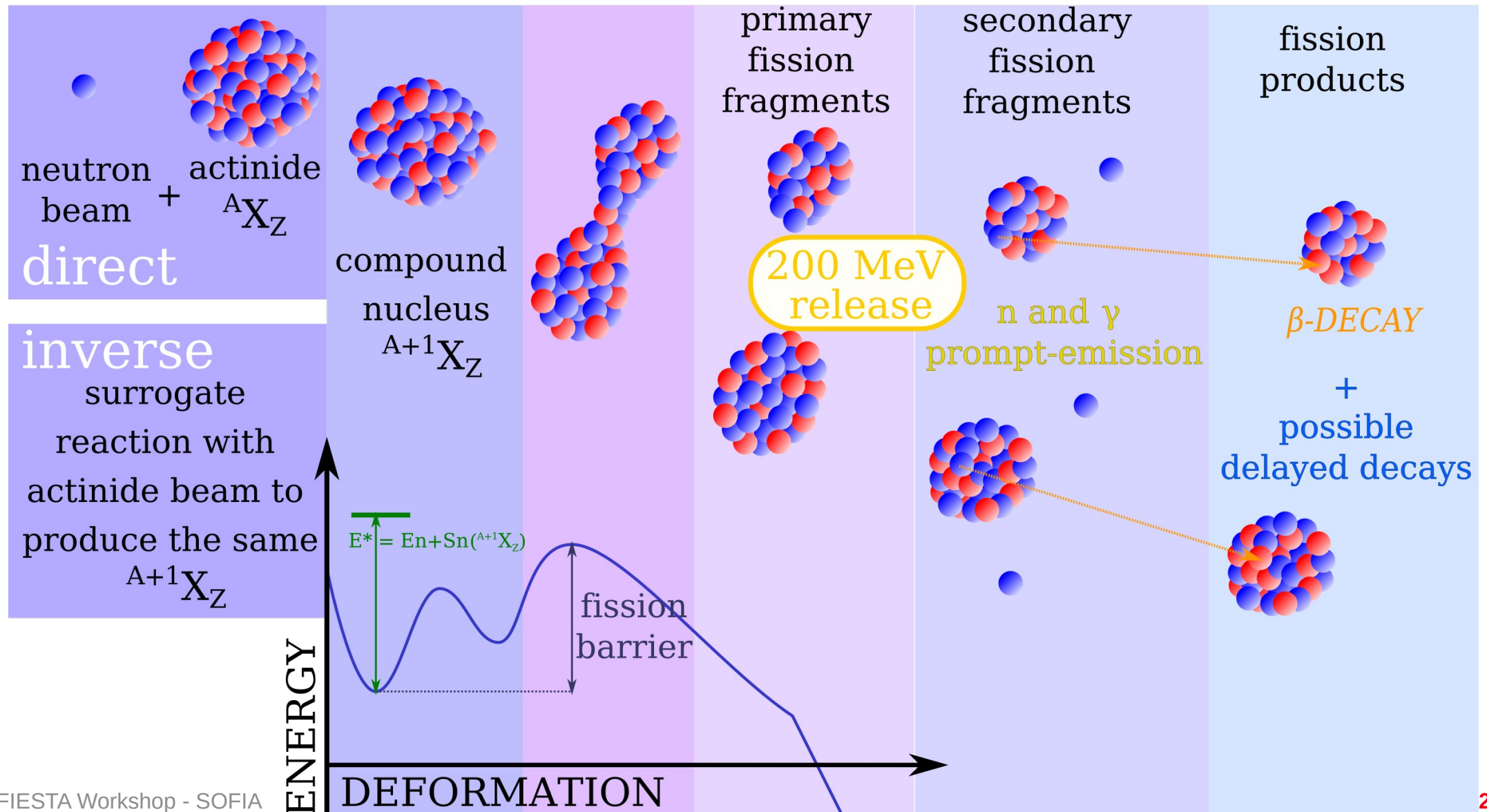
for nuclear data need & basic science



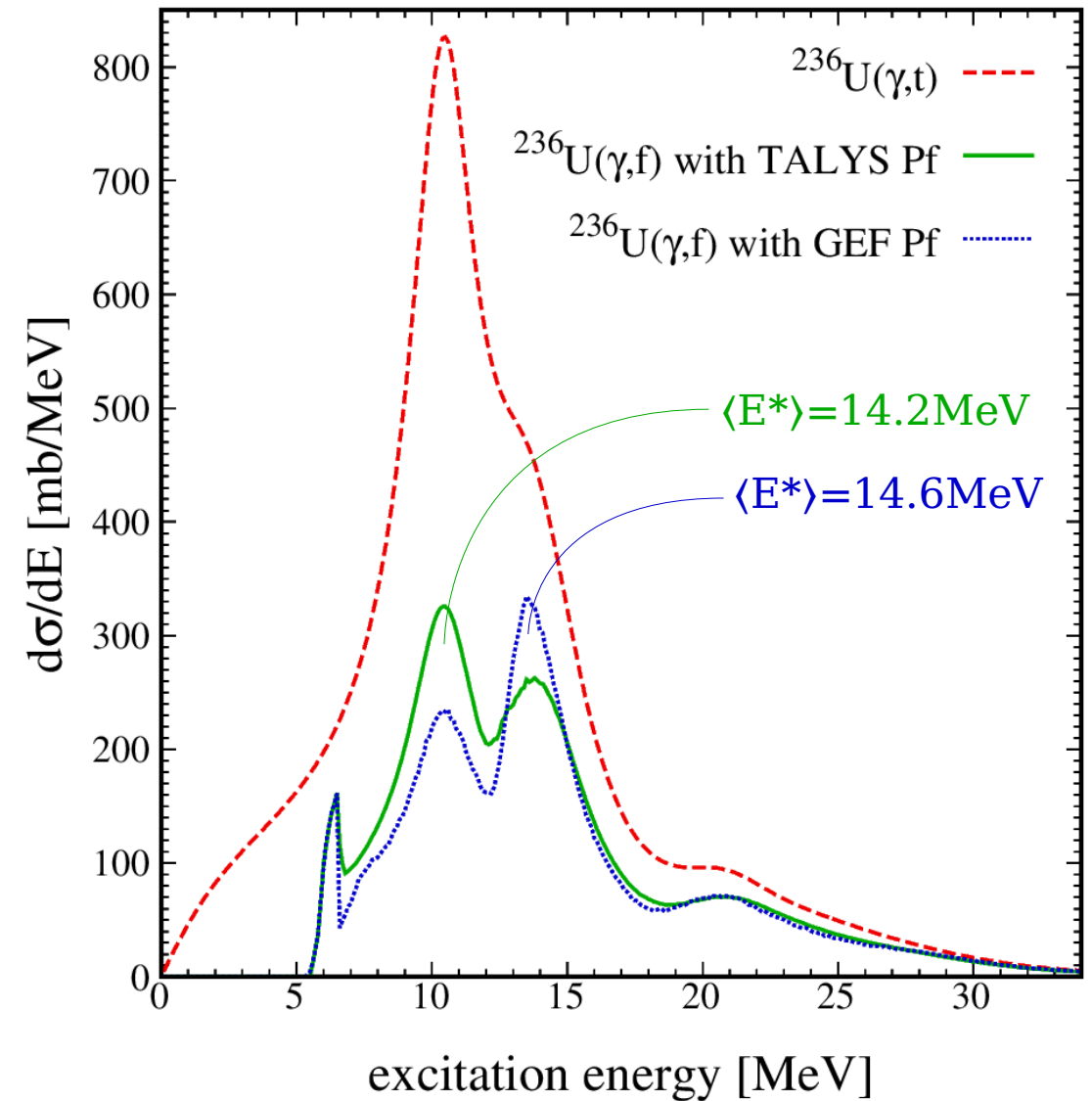
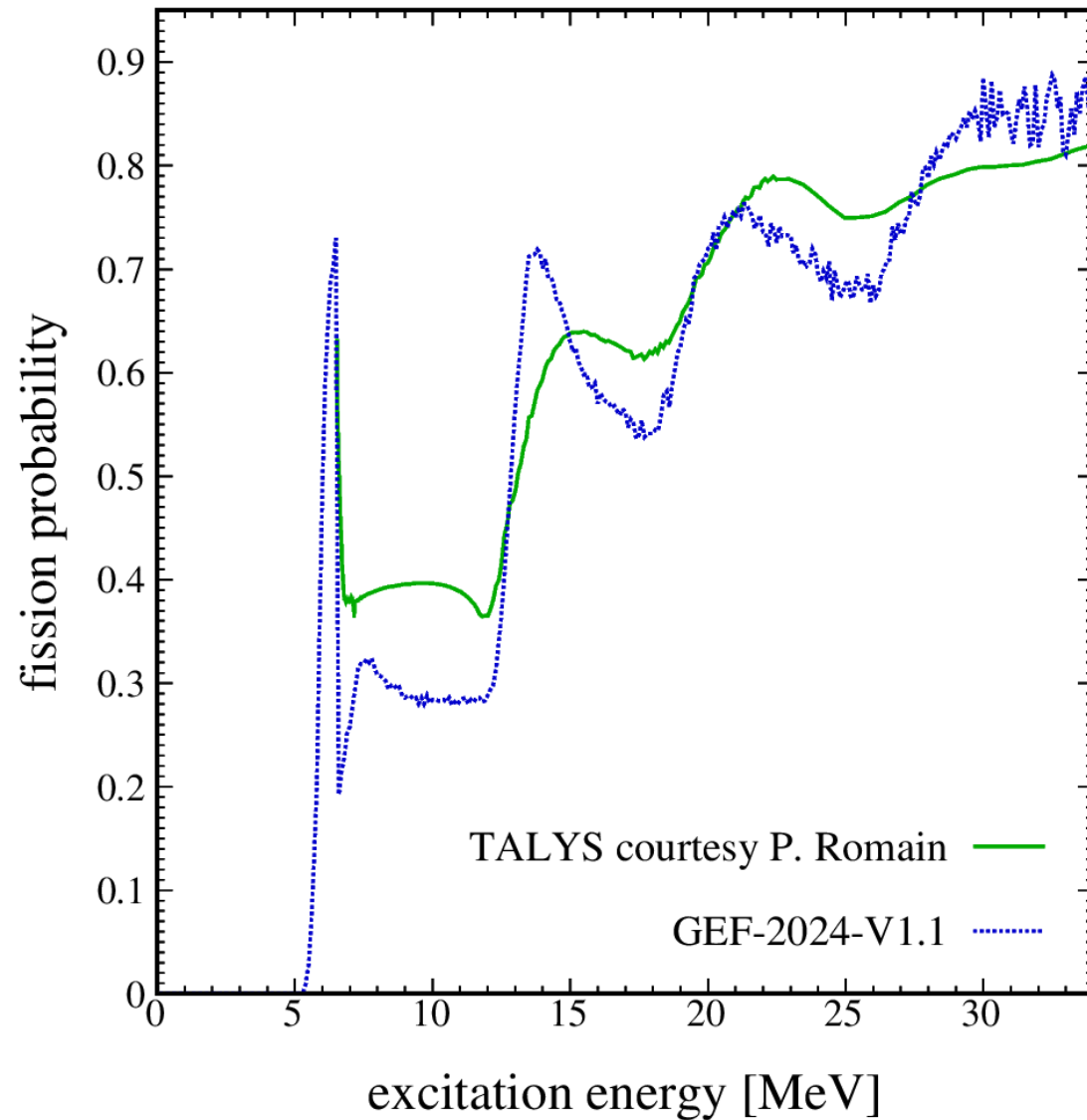


# 3 ■ Extra slides

# Fission scheme

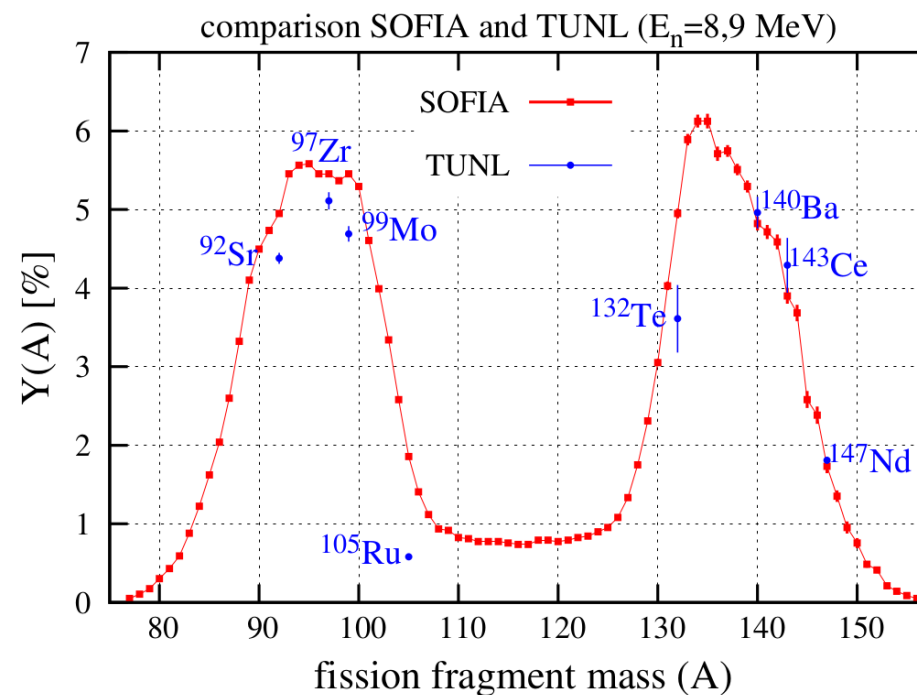
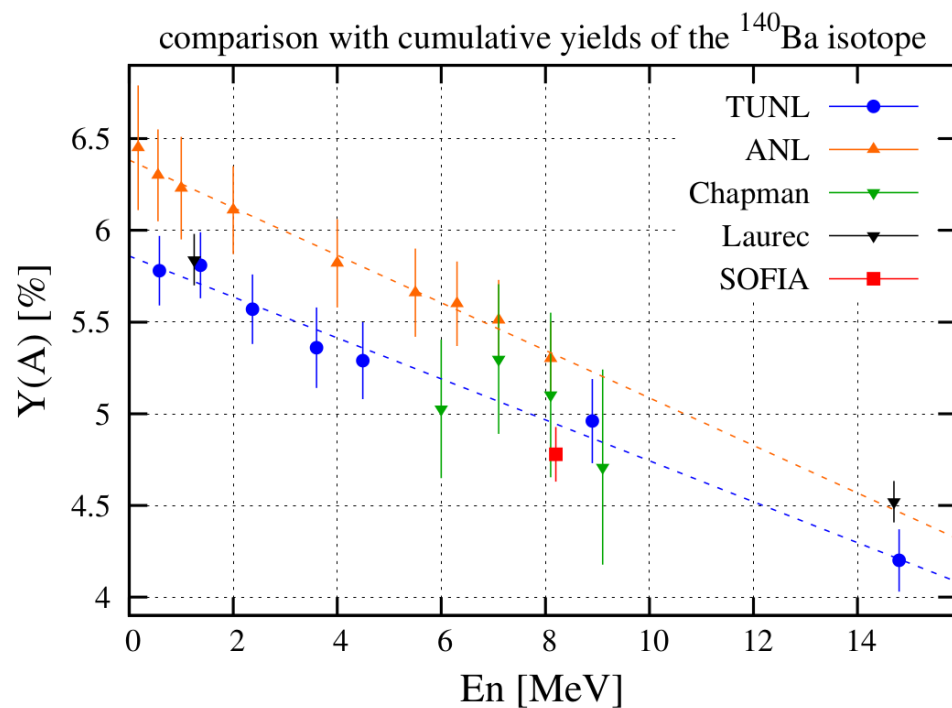


# Excitation energy distribution for $^{236}\text{U}(\gamma, f)$



# Isobaric yields (II)

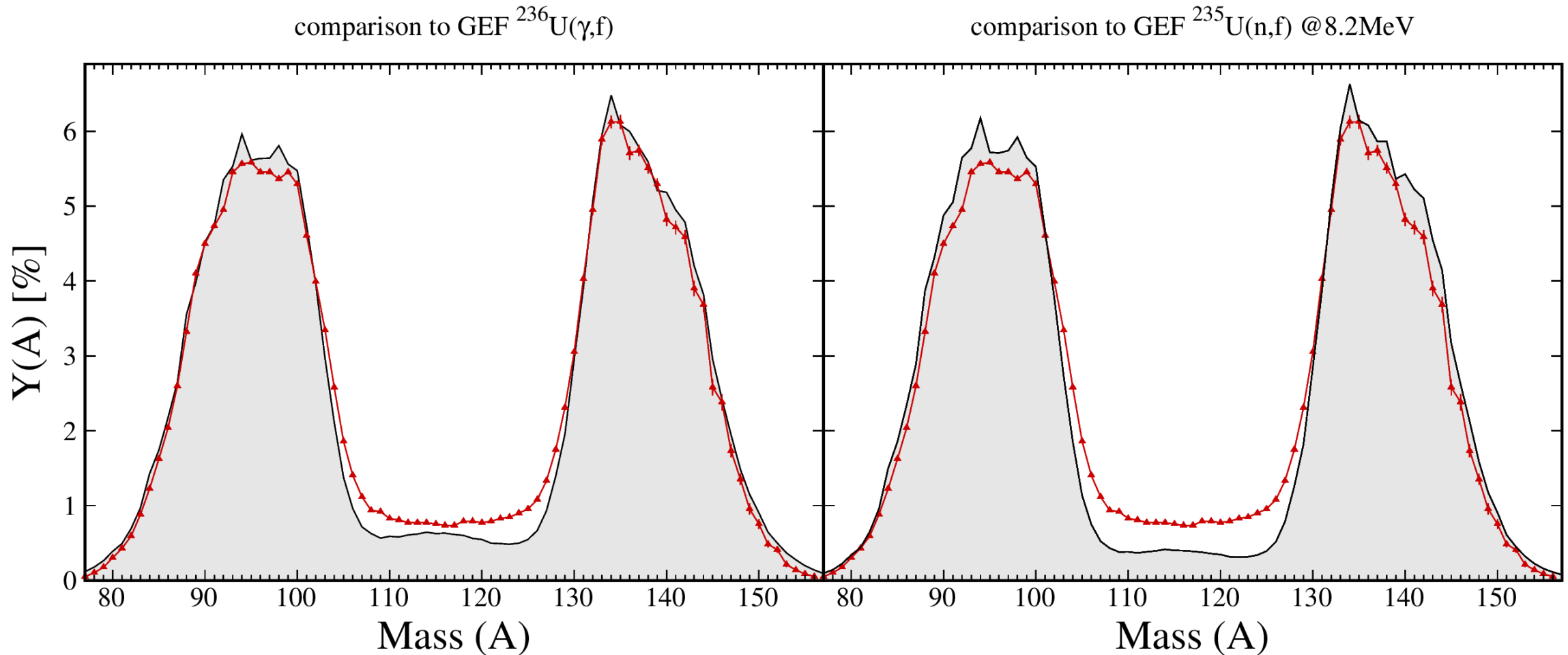
$^{236}\text{U}(\gamma, f)$  from SOFIA compared to  $^{235}\text{U}(n, f)$  cumulative yields



*Analysis by L. Grente (CEA/DAM/DIF)*

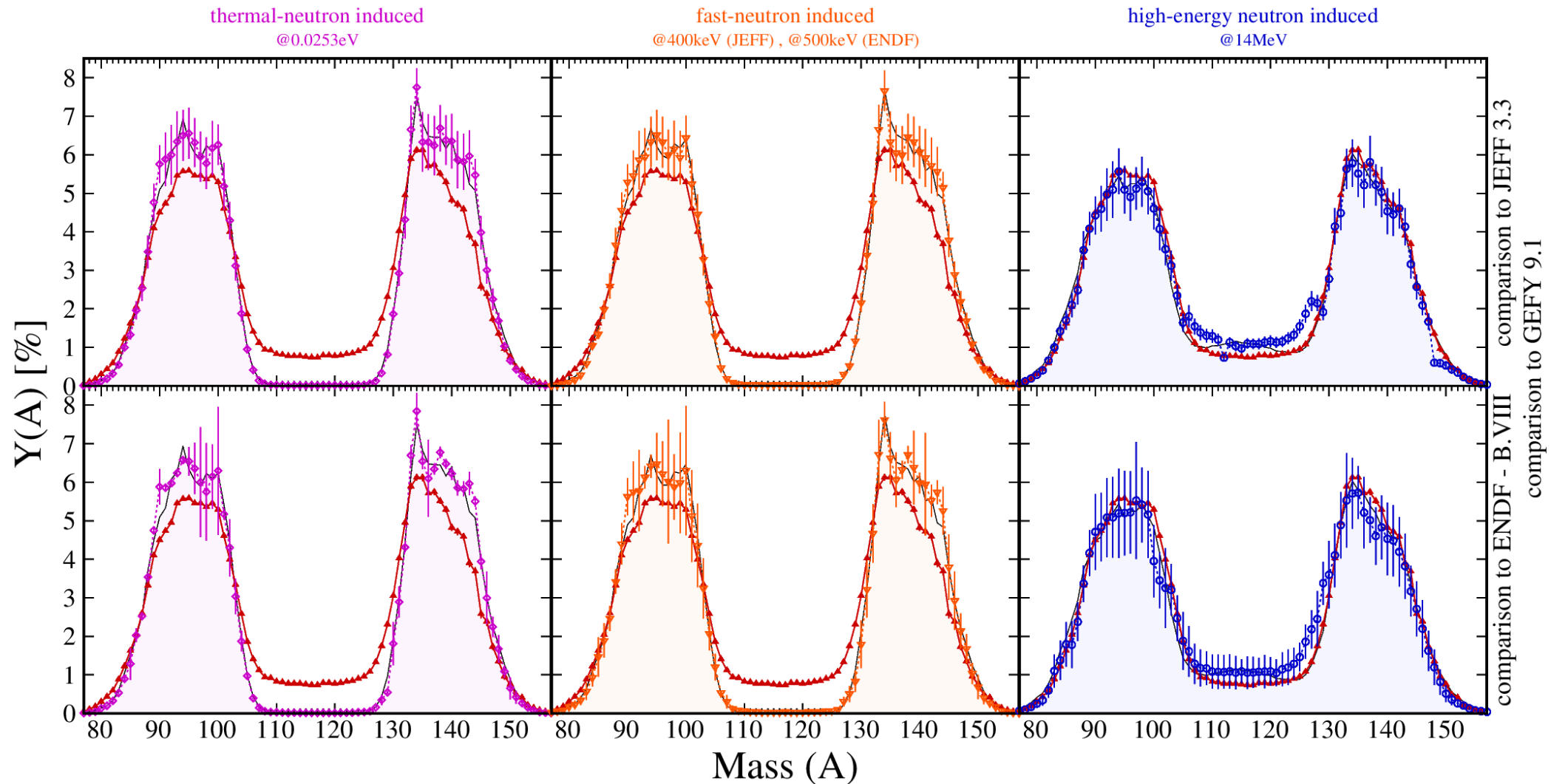
# Isobaric yields (III)

$^{236}\text{U}(\gamma, f)$  from SOFIA compared to GEF-2024-V1.1 with Pf from GEF



# Isobaric yields (IV)

$^{236}\text{U}(\gamma, f)$  from SOFIA compared to evaluations : JEFF3.3, ENDF-B.VIII, GEFY 9.1



# Th chain: $\langle \nu_{\text{tot}} \rangle$ sharing to extract $\langle N_{\text{pre}} \rangle_{\text{L,H}}$

How to share  $\langle \nu_{\text{tot}} \rangle$  between light fragment and heavy fragment ?

$$\langle N_{\text{pre}} \rangle_{\text{L,H}} = \langle N_{\text{post}} \rangle_{\text{L,H}} + \langle \nu \rangle_{\text{L,H}}$$

## ■ Method 1: Fission consider as an adiabatic process in a Fermi gas

$$\rightarrow \langle A_{\text{pre,L}} \rangle / \langle A_{\text{pre,H}} \rangle = \langle E_{\text{L}}^* \rangle / \langle E_{\text{H}}^* \rangle \sim \langle \nu_{\text{L}} \rangle / \langle \nu_{\text{H}} \rangle$$

$$\rightarrow \langle \nu_{\text{L,H}} \rangle = \langle \nu_{\text{tot}} \rangle (Z_{\text{L}}, Z_{\text{H}}) * \langle A_{\text{post,L,H}} \rangle / (\langle A_{\text{post,L}} \rangle + \langle A_{\text{post,H}} \rangle)$$

→ this method can be applied to all compound systems studied with SOFIA

## ■ Method 2: Based on combination of experimental data only

→ No model : combination of results from SOFIA and previous experiments in neutron-induced

→ Can be applied only to the specific cases with existing and precise n-induced data

→ Used for the validation of method 1

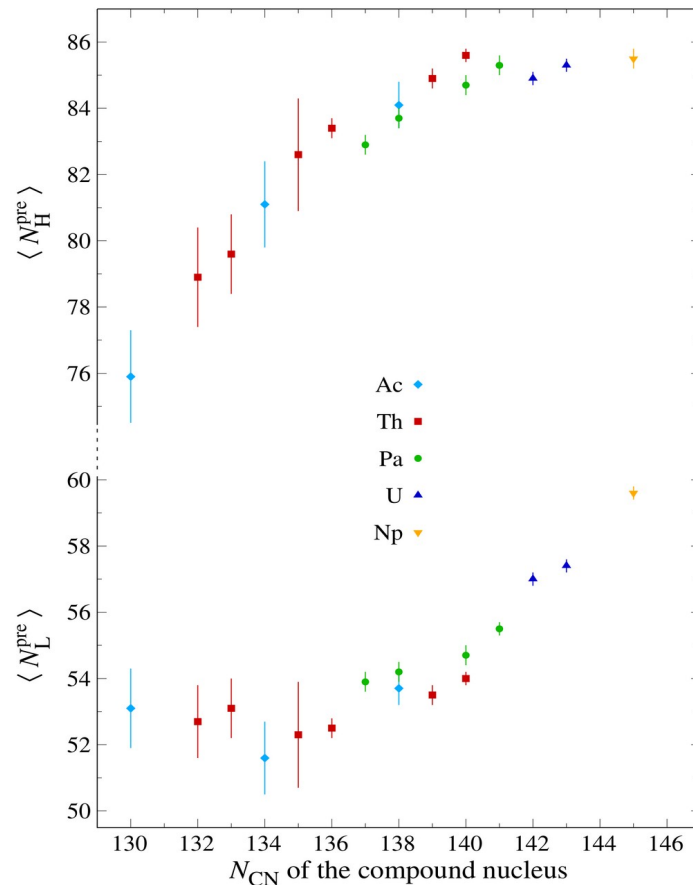
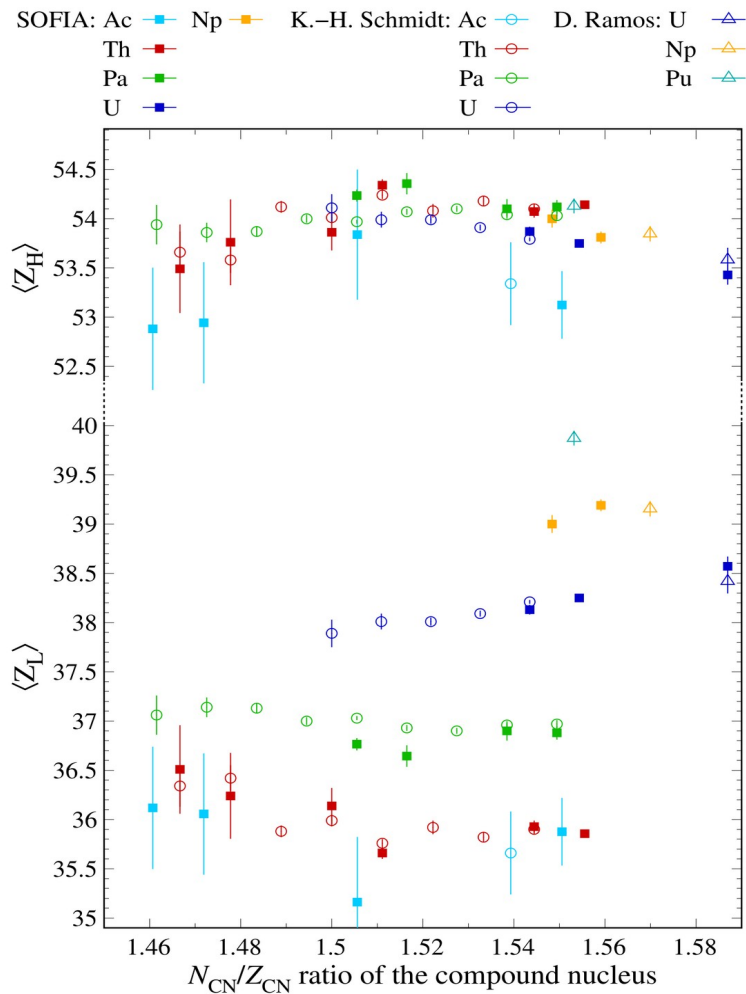
## ■ More information in references: PRC 104 044602 (2021) and PRC 106 024618 (2022)



$\langle Z_{\text{pre}} \rangle_{L,H}$

&

$\langle N_{\text{pre}} \rangle_{L,H}$



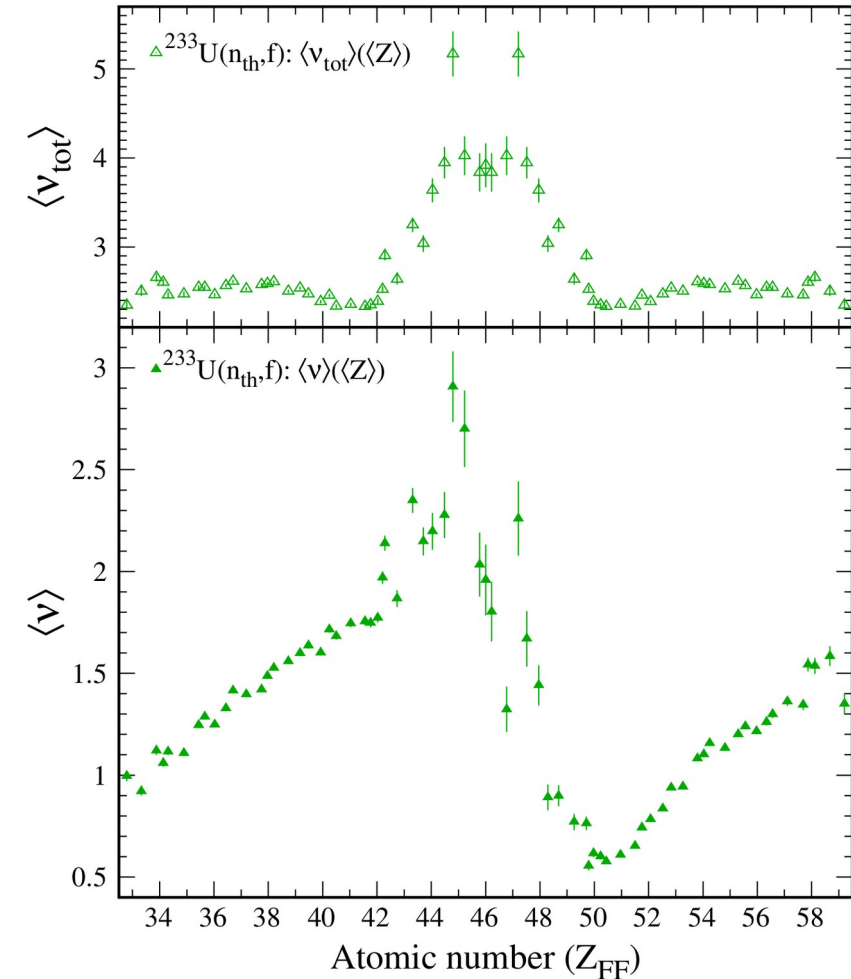
- From Th (Z=90) to Pu (Z=94)  
 $\langle Z_{\text{H}} \rangle \sim 54$
- This effect becomes weak for Ac isotopes (Z=89)
- For neutron deficient isotopes, stabilisation around  $\langle N_{\text{L}} \rangle \sim 54$

# Th chain: $\langle \nu_{\text{tot}} \rangle$ sharing to extract $\langle N_{\text{pre}} \rangle_{\text{L,H}}$

## ■ Method 2: Based on combination of experimental data only

### 1/ Neutron-induced fission data $^{233}\text{U}(n_{\text{th}},f)$

K. Nishio et al. *J. Nucl. Sci. Technol.* 35, 631 (1998)



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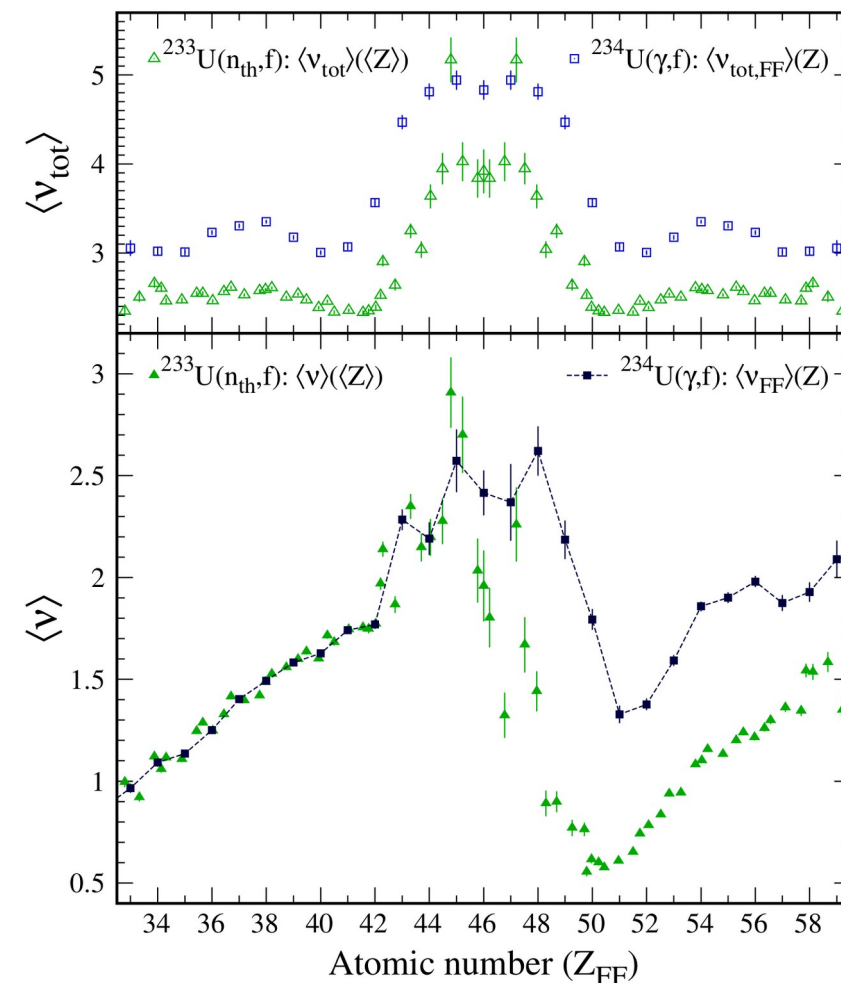
### 2/ SOFIA : Coulomb-induced fission of $^{234}\text{U}$

### 3/ Any increase of $E^*$ translates into additional neutron emission in the heavy fission fragment only

R. Müller *et al.*, *PRC* 29, 885 (1984)

A. A. Naqvi *et al.*, *PRC* 34, 218 (1986)

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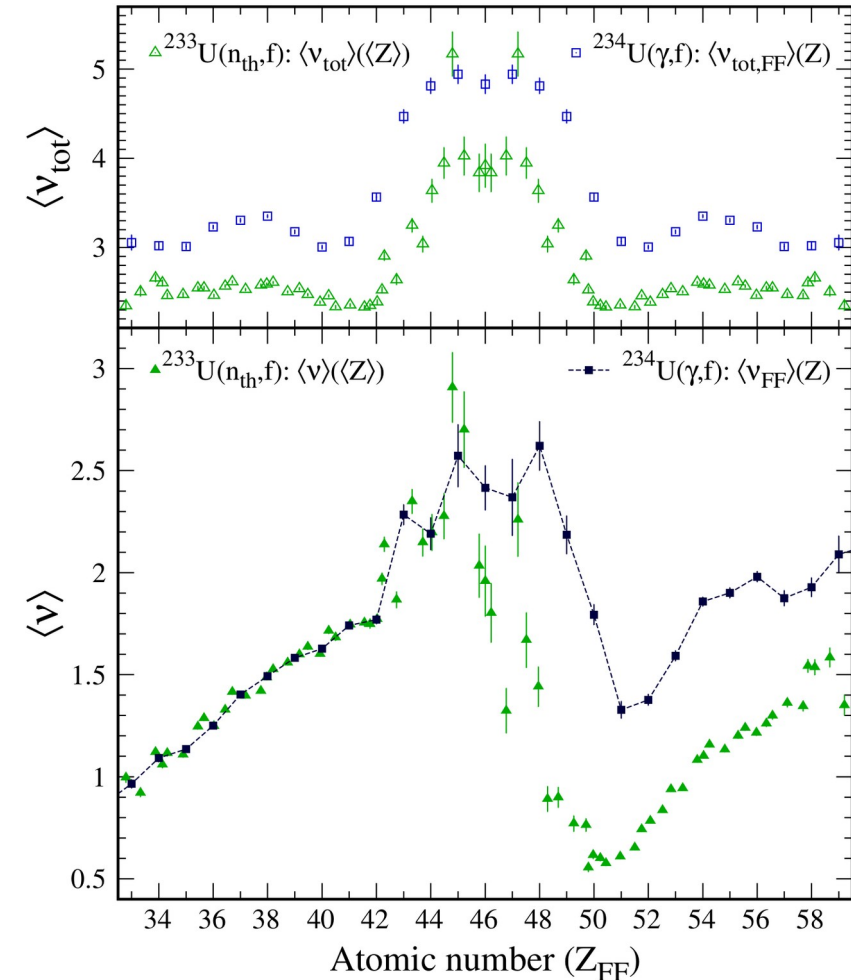
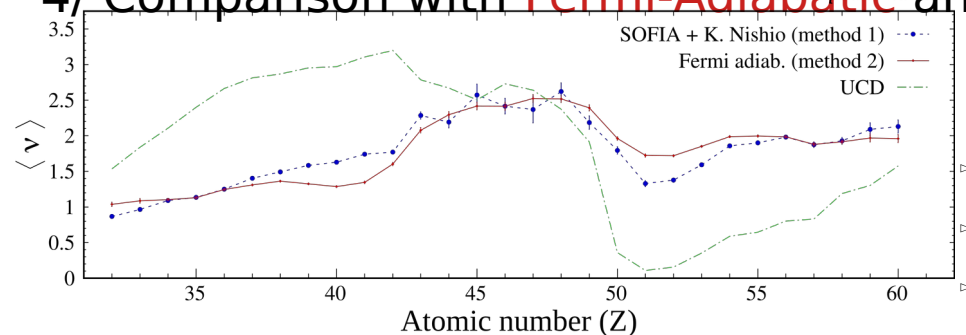
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### 4/ Comparison with Fermi-Adiabatic and UCD



Excellent agreement between both methods

Maximum discrepancy of 0.4 neutrons around st1 mode

UCD introduces a significant bias in the neutron emission