

Q1

P2

	A	B	C
P1	0, 0	60, 132	0, 104
	132, 60	52, 52	12, 70
	104, 0	70, 12	24, 24

a.)

For P1: A is dominated by C.

For P2: A is dominated by C.

b.)

	B	C
B	52, 52	12, 70
C	70, 12	24, 24

c.) For both P1 & P2,
B is dominated by C.

Q2.

a.) Let the highest bid be b .

If $b > 100$, then

$$\pi(b_{100}) = \pi(b_{95}) = 0.$$

If $95 < b < 100$, then

$$\pi(b_{100}) = 0 = \pi(b_{95}).$$

If $b < 95$, $\pi(b_{100}) = 0$ &

$$\pi(b_{95}) = 5.$$

Hence b_{95} weakly dominates b_{100} .

b.) If $b > 95$, $\pi(b_{95}) = \pi(b_{100}) = 0$

If $60 < b < 95$, $\pi(b_{95}) = 5$,

$\pi(b_{60}) = 0$.

If $b < 60$, $\pi(b_{60}) = 40$, $\pi(b_{95}) = 5$

$\Rightarrow b_{60}$ does not dominate b_{95}

and b_{95} does not dominate b_{60} .

3.) $V_1 > V_2$, $b_1 = V_1$, $V_2 < b_2 < V_1 = b_1$

Player 1 wins and gets $\pi_1 = V_1 - b_2 > 0$. Player 2 gets $\pi_2 = 0$.

Player 1 has no incentive to bid $b_2 < b_1 < V_1$ or $b_1 > V_1$

because π_1 is still $V_1 - b_2$. Player 1

has no incentive to decrease $b_1 < b_2$

since π_1 becomes 0.

Player 2 has no incentive to increase $b_2 > b_1$ since

$\pi_2 = V_2 - b_1 < 0$. Also, $b_2 < V_2$ would result

to $\pi_2 = 0$.

$\rightarrow V_2 < b_2 < V_1 = b_1$ is N.E.

b.) $V_2 < b_2$ is weakly dominated by $\hat{b}_2 = V_2$

because:

in if $\hat{b}_2 = V_2 < b_2 < b_1 \rightarrow \pi(\hat{b}_2) = \pi(b_2) = 0$.

(2) If $\hat{b}_2 = v_2 < b_1 < b_2 \rightarrow \pi(b_2) = v_2 - b_1 < 0$
 $\pi(\hat{b}_2) = 0$

(3) If $b_1 < \hat{b}_2 = v_2 < b_2 \rightarrow \pi(b_2) = \pi(\hat{b}_2) = v_2 - b_1 > 0$
 $\rightarrow \hat{b}_2$ weakly dominates b_2 .

4c)

		g		$1-g$	
		h		t	
p	H	$1, -1$	$-1, 1$	$-1, 1$	$1, -1$
	T	$-1, 1$	$1, -1$	$1, -1$	$-1, 1$

No PSNE.

$$EU_1(H) = g + (1-g)(-1)$$

$$EU_1(T) = -g + (1-g)(1)$$

I is indifferent when: $g - 1 + g = -g + 1 - g$
 $\rightarrow g = \frac{1}{2}$

Likewise, $EU_2(h) = EU_2(t) \rightarrow p = \frac{1}{2}$.

$\Rightarrow$ MSNE: $p = \frac{1}{2}, g = \frac{1}{2}$.

or: play H $\frac{1}{2}$ of the time; T $\frac{1}{2}$ of the time
 play h $\frac{1}{2}$ of the time; t $\frac{1}{2}$ of the time.

$\rightarrow$

g	$1-g$
-----	-------

5.)

		q	1-q
		h	t
p	H	0, 0	4, 1
1-p	D	1, 4	2, 2

$$EU(H) = 0q + 4(1-q)$$

$$EU(D) = 1q + 2(1-q)$$

$$EU(H) = EU(D) \Rightarrow 4(1-q) = q + 2(1-q)$$

$$\Rightarrow q = 2/3$$

$$EU(h) = EU(d) \Rightarrow 0p + 4(1-p) = 1p + 2(1-p)$$

$$\Rightarrow p = \frac{2}{3}$$

$$b) EU_1 = \frac{2}{3} \cdot \frac{2}{3} \cdot (0) + \frac{2}{3} \cdot \frac{1}{3} \cdot 4 + \frac{1}{3} \cdot \frac{2}{3} \cdot 1 + \frac{1}{3} \cdot \frac{1}{3} \cdot 2$$

$$= \frac{8}{9} + \frac{2}{9} + \frac{2}{9} = \frac{12}{9} = \frac{4}{3}$$

$$EU_2 = \frac{2}{3} \cdot \frac{2}{3} \cdot 0 + \frac{2}{3} \cdot \frac{1}{3} \cdot 1 + \frac{1}{3} \cdot \frac{2}{3} \cdot 4 + \frac{1}{3} \cdot \frac{1}{3} \cdot 2$$

$$= 4/3$$

6.)

		q	1-q
		L	R
p	U	a, 0	0, b
1-p	D	0, c	d, 0

$$1-p \quad \overline{D} \quad | \quad 0, c \quad | \quad d, 0$$

$$EU(L) = EU(D) \Rightarrow aq = d(1-q) \rightarrow q = \frac{d}{a+d}$$

$$EU(L) = EU(R) \Rightarrow c(1-p) = bp \rightarrow p = \frac{c}{b+c}$$

$$EU_1 = a \cdot p \cdot q + d(1-p)(1-q) - a\left(\frac{d}{a+d}\right)\left(\frac{c}{b+c}\right) + d\left(\frac{a}{a+d}\right)\left(\frac{b}{b+c}\right) > 0$$

$$EU_2 = c(1-p)q + b(1-q)p = c\left(\frac{b}{b+c}\right)\left(\frac{d}{a+d}\right) + b\left(\frac{a}{a+d}\right)\left(\frac{c}{b+c}\right) > 0$$

Pareto Efficient since $EU_1, EU_2 > 0$ while any outcome result to either $U_1 = 0$ or $U_2 = 0$.

7.)

		q	$1-q$
		S	W
p	m	$-m, w^0$	$-m, w^*-e$
$1-p$	N	$-w^*, w^*$	$0, w^*-e$

$$EU(m) = EU(N) \Rightarrow -m = -w^*q + 0 \rightarrow q = \frac{m}{w^*}$$

$$EU(S) = EU(W) \rightarrow w^0q + w^*(1-p) = w^*-e$$

$$\rightarrow p = \frac{-e}{w^0 - w^*} = \frac{e}{w^* - w^0}$$

b.) As $m \uparrow$, $q \uparrow$. As $w^* \downarrow$, $q \uparrow$.

As $e \uparrow$, $q \uparrow$. As $w^* - w^0 \uparrow$, $p \downarrow$.

Shirking rises when cost of monitoring (m) rises and when efficiency wage falls.

Monitoring rises when effort (e) rises or when job becomes more difficult. As gap in wage ($w^* - w^0$) falls, more monitoring is needed.

c.) Yes, since the probability of monitoring would fall as the cost m rises. In this model, p is not a function of m . It is a function of effort and wages. $p = \frac{e}{w^* - w^0}$.