Ratios!

Foundation	Higher (Q5 is hard)
Sarah mixed red and blue paint in a ratio of 3:5. If she used 15 Liters of blue paint, how much red paint did	A mixture of water and juice is in a ratio of 1:4. If there are 20 Liters of juice, how much water is in the
she use?	mixture?
The ratio of boys to girls in a class is 4:7. If there are 28 boys, how many girls are in the class?	The ratio of boys to girls in a school is 5:7. If there are 280 girls, how many boys are there in the school?
A recipe requires a ratio of 2 cups of flour to 3 cups of sugar. How much flour is needed if you have 15 cups of sugar?	There are 50 litres of water in a tub. The water flows out of the tub at a rate of 150 millilitres per second. (1 Litre = 1000 millilitres). Work out the time it takes to fully empty the tub in seconds. Try working it out in hours for a stretch.
In a bag of marbles, the ratio of red to blue marbles is 3:7. If there are 42 red marbles, how many blue marbles are there?	A shop sells bagels and breads. The ratio of the number of bagels sold to the number of loafs sold is 7:2. The shop sells a total 180 bagels and loafs in one week. Work out the number of loafs and bagels sold in that week.
A map scale indicates that 1 centimetre represents 5 kilometres. If the distance between two cities on the map is 15 centimetres, what is the actual distance in kilometres?	The ratio of the lengths of two sides of a rectangle is k:3, where k is a positive constant. If the shorter side has a length of 6 meters, and the difference between the lengths is equal to one-third of the length of the shorter side, what is the length of the longer side? Go on to find the value of k.

Solutions!

Foundation	Higher (Q5 is hard)
Sarah mixed red and blue paint in a ratio of 3:5. If she	A mixture of water and juice is in a ratio of 1:4. If
used 15 Liters of blue paint, how much red paint did she use?	there are 20 Liters of juice, how much water is in the mixture?
We need to find the amount of red paint used by Sarah.	We need to find the amount of water in the mixture.
Let x represent the amount of red paint used in Liters.	Let x represent the amount of water in the mixture.
According to the given ratio, the ratio of red to blue paint is 3:5. So, we can set up the equation:	According to the given ratio, the ratio of water to juice is 1:4. So, we can set up the equation:
$\frac{3}{5} = \frac{15}{r}$	$\frac{1}{4} = \frac{x}{20}$
Now, let's solve for x:	Now, let's solve for x,
Cross-multiply:	Cross-multiply:
$3 \times 15 = 5 \times x$	$4x = 1 \times 20$ $4x = 20$
45 = 5x Divide by 5:	Divide by 4:
$x = \frac{45}{5}$	$x = \frac{20}{4}$
x = 9	$x = \overline{5}$
Therefore, Sarah used 9 Liters of red paint.	Therefore, there are 5 Liters of water in the mixture.
The ratio of boys to girls in a class is 4:7. If there are	The ratio of boys to girls in a school is 5:7. If there
28 boys, how many girls are in the class?	are 280 girls, how many boys are there in the school?
We need to find the number of girls in the class.	We need to find the number of boys in the school.
Let x represent the number of girls in the class.	Let x be the number of boys in the school. According to the given ratio, the number of boys to
According to the given ratio, the ratio of boys to girls is 4:7. So, we can set up the equation:	the number of girls is 5:7. So, we can set up the equation:
$\frac{4}{7} = \frac{28}{r}$	$\frac{5}{7} = \frac{x}{280}$
Now, let's solve for x:	7 280 Now, let's solve for x, (Cross-multiply):
Cross-multiply:	$7x = 5 \times 280$ $7x = 1400$
$4x = 7 \times 28$ $4x = 196$	Divide by 7:

Divide by 4:	1400
196	$x = \frac{1100}{7}$
$x = \frac{196}{4}$	x = 200
x = 49	
	Therefore, there are 200 boys in the school.
Therefore, there are 49 girls in the class.	
A recipe requires a ratio of 2 cups of flour to 3 cups of	There are 50 litres of water in a tub. The water flows
sugar. How much flour is needed if you have 15 cups	out of the tub at a rate of 150 millilitres per second.
of sugar?	(1 Litre = 1000 millilitres). Work out the time it takes
	to fully empty the tub in seconds. Try working it out
We need to find the amount of flour needed for 15	in hours for a stretch.
cups of sugar.	
Let x represent the amount of flour needed in cups.	There are 50 litres of water in a tub, which is equal
According to the given ratio, the ratio of flour to sugar	to:
required is 2:3. So, we can set up the equation:	$E0 \times 1000 - E0.000 \text{ millitrag}$
2 r	$50 \times 1000 = 50,000 \text{ mililitres}$
$\frac{2}{3} = \frac{x}{15}$	Let t represent the time it takes to fully empty the
5 15	tub in seconds.
Now, let's solve for x:	The rate of water flow out of the tub is 150 millilitres
Cross-multiply:	per second. So, we can set up the equation:
	Rate of water flow = Volume / Time
$2 \times 15 = 3 \times x$	50,000 stilliture
30 = 3x	150 millilitres per second = $\frac{50,000}{t}$ millilitres
Divide hu 2	Now, let's solve for t:
Divide by 3:	
$x = \frac{30}{3}$	$t = \frac{50,000 \text{ mililitres}}{150 \text{ mililitres per second}}$
x = 10	150 mililitres per second
	t = 333.33 (2.d.p)
Therefore, you will need 10 cups of flour if you have	To convert the time to hours, divide by 3600 seconds
15 cups of sugar for the recipe.	(since there are 60 seconds in a minute and 60
	minutes in an hour):
	t (in hours) = 333.33 seconds / 3600 seconds per
	hour
	t (in hours) ≈ 0.0926 hours
In a bag of marbles, the ratio of radio blue marbles to	A shap calls bagale and brands. The ratio of the
In a bag of marbles, the ratio of red to blue marbles is	A shop sells bagels and breads. The ratio of the
3:7. If there are 42 red marbles, how many blue marbles are there?	number of bagels sold to the number of loafs sold is 7:2. The shop sells a total 180 bagels and loafs in one
וומוטוכא מוכ נווכוכ:	7:2. The shop sells a total 180 bagels and loafs in one week. Work out the number of loafs and bagels sold
We need to find the number of blue marbles in the	in that week.
bag.	
	Let the number of bagels sold be 7x , and the number
Let x represent the number of blue marbles in the	of loaves of bread sold be 2x , where x is a positive
bag.	constant representing the common factor in the

	ratio.
According to the given ratio, the ratio of red to blue	
marbles is 3:7. So, we can set up the equation:	According to the given ratio, the number of bagels
	sold to the number of loaves of bread sold is 7:2. So,
$\frac{3}{7} = \frac{42}{x}$	we can set up the equation:
$\overline{7} = \frac{1}{x}$	
	(7x) + (2x) = 180
Now, let's solve for x:	
	9x = 180
Cross-multiply:	
$3x = 7 \times 42$	Divide by 9:
$3x = 7 \times 42$ $3x = 294$	100
Divide by 3:	$x = \frac{180}{9}$
	9
$x = \frac{294}{3}$	<i>x</i> = 20
$x = \frac{1}{3}$	λ - 20
x = 98	Now that we have the value of x, we can find the
	number of bagels and loaves of bread sold:
Therefore, there are 98 blue marbles in the bag.	
	Number of bagels = $7x = 7 * (20) = 140$
	Number of loaves of bread = $2x = 2 * (20) = 40$
A map scale indicates that 1 centimetre represents 5	The ratio of the lengths of two sides of a rectangle is
kilometres. If the distance between two cities on the	k:3, where k is a positive constant. If the shorter side
map is 15 centimetres, what is the actual distance in	has a length of 6 meters, and the difference between
kilometres?	the lengths is equal to one-third of the length of the shorter side, what is the length of the longer side?
	Go on to find the value of k.
Let d represent the actual distance between the two	Let's solve the problem step by step:
cities in kilometres.	Let's solve the proviet step by step.
	Given:
According to the map scale, 1 centimetre on the map	- Ratio of the lengths of two sides of the
represents 5 kilometres. So, we can set up the	rectangle is k:3 , where k is a positive
proportion:	constant.
	- Length of the shorter side is 6 meters.
1 centimeter _ 15 centimeters	-
$\frac{1}{5 \text{ kilometers}} = \frac{1}{d \text{ kilometers}}$	Let x be the length of the longer side.
Now, let's solve for d:	According to the given ratio, the lengths of the two
	sides are in the ratio k:3 . So, we can set up the
	equation:
	$\frac{k}{-}=\frac{6}{-}$
	$\frac{1}{3} = \frac{1}{x}$

Cross-multiply:

$$1 \times d = 5 \times 15$$
$$d = 75$$

Therefore, the actual distance between the two cities is **75 kilometres**

Now, let's incorporate the information about the difference between the lengths. The **difference between the lengths** is equal to **one-third of the length of the shorter side**. Therefore, we have:

$$x - 6 = \left(\frac{1}{3}\right) \times 6$$

$$x - 6 = 2$$

Now, let's solve for x:

$$\begin{array}{c} x = 2 + 6 \\ x = 8 \end{array}$$

Now, we can substitute the value of x to find the value of k.

$$\frac{k}{3} = \frac{6}{8}$$
$$k = 3 \times \frac{6}{8}$$
$$k = \frac{9}{4}$$

Sometimes you can get tricky questions, but you can tackle them by remembering to Always have clear working to avoid making mistakes!