

# 05-Solar Resource Part 1

ECEGR 4530

Renewable Energy Systems

# ➤ Overview

- Solar Characteristics
- Extraterrestrial Solar Irradiance
- Angle of Incidence
- Solar Irradiance

# → Introduction

- Most renewable energy systems convert energy whose source is ultimately the sun
  - 3.8 YJ ( $1 \times 10^{24}$ )/yr pass through the atmosphere
  - approx. 10,000 the amount of energy used by fossil fuels and nuclear per year
- In this lecture we investigate the nature of solar energy

# → Solar Characteristics

- Solar energy originates from the sun
- Driven by nuclear fusion of hydrogen into helium
- Surface temperature approximately 5500°C

# → Solar Characteristics

- Heat is transferred from the sun to the Earth via electromagnetic radiation
  - also called solar radiation
- Nature of the electromagnetic radiation is a function of the temperature and emissivity

## » Solar Characteristics

- Solar radiation from a blackbody (the sun can be approximated by a blackbody) is related to temperature from the Stefan-Boltzmann Law

$$G = \sigma T^4$$

- where
  - $G$ : irradiance or solar irradiance ( $\text{W}/\text{m}^2$ )
  - $\sigma$ : Stefan-Boltzmann constant  
 $\sigma = 5.67 \times 10^{-8} \text{ J}/(\text{sm}^2\text{K}^4)$

## » Exercise

- Calculate the irradiance of the sun (approximate as a blackbody at a temperature of 5500°C) at its surface

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## Exercise

- Calculate the irradiance of the sun (approximate as a blackbody at a temperature of 5500°C) at its surface

$$G = \sigma T^4$$

$$\sigma = 5.67 \times 10^{-8} \text{ J}/(\text{sm}^2\text{K}^4)$$

$$G = (5.67 \times 10^{-8})(5500 + 273)^4 = 6.3 \times 10^7 \text{ W}/\text{m}^2$$

- If the sun was the temperature of a candle it would be:

$$G = (5.67 \times 10^{-8})(1000 + 273)^4 = 1.50 \times 10^5 \text{ W}/\text{m}^2$$

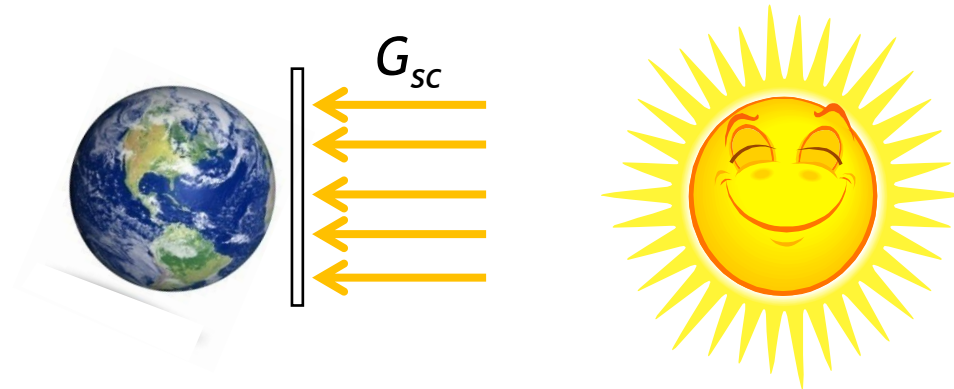


## → Solar Irradiance

- Unit of  $G$  ( $\text{W}/\text{m}^2$ ) is power density
- Integrate  $G$  over time to find irradiation, the energy density ( $\text{J}/\text{m}^2$  or  $\text{kwh}/\text{m}^2$ )
- Insolation (not insulation): irradiation whose source is the sun

# → Solar Irradiance

- The accepted average solar irradiance value for the top of the Earth's atmosphere (extraterrestrial) is  $1367 \text{ W/m}^2$ 
  - based on satellite data
  - plane normal to the sun
  - $G_{sc} = 1367 \text{ W/m}^2$  defined as a *Solar Constant*



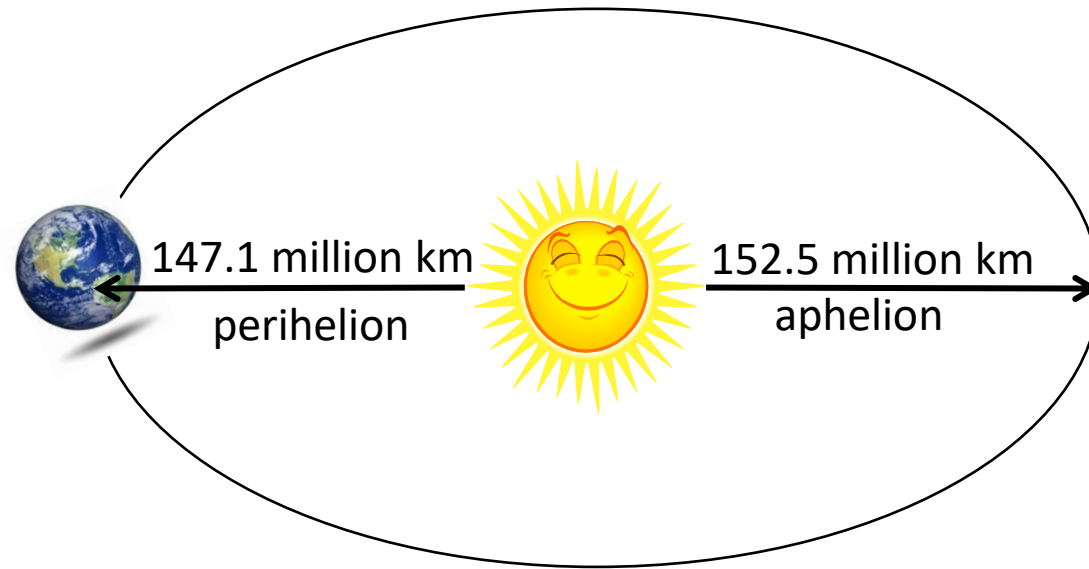
# → Solar Astronomy

- $G_0$ : extraterrestrial irradiance on horizontal surface ( $\text{W}/\text{m}^2$ )
- $G_{0n}$ : extraterrestrial irradiance on a plane normal to the radiation
- $G_{0T}$ : total extraterrestrial irradiance on a surface, accounting for surface tilt, if any ( $\text{W}/\text{m}^2$ )
- Subscript 0 means extraterrestrial (top of the atmosphere)

See Lecture 0X-Solar Nomenclature

# → Solar Astronomy

Earth's orbit is nearly circular



a “tilted” view is shown

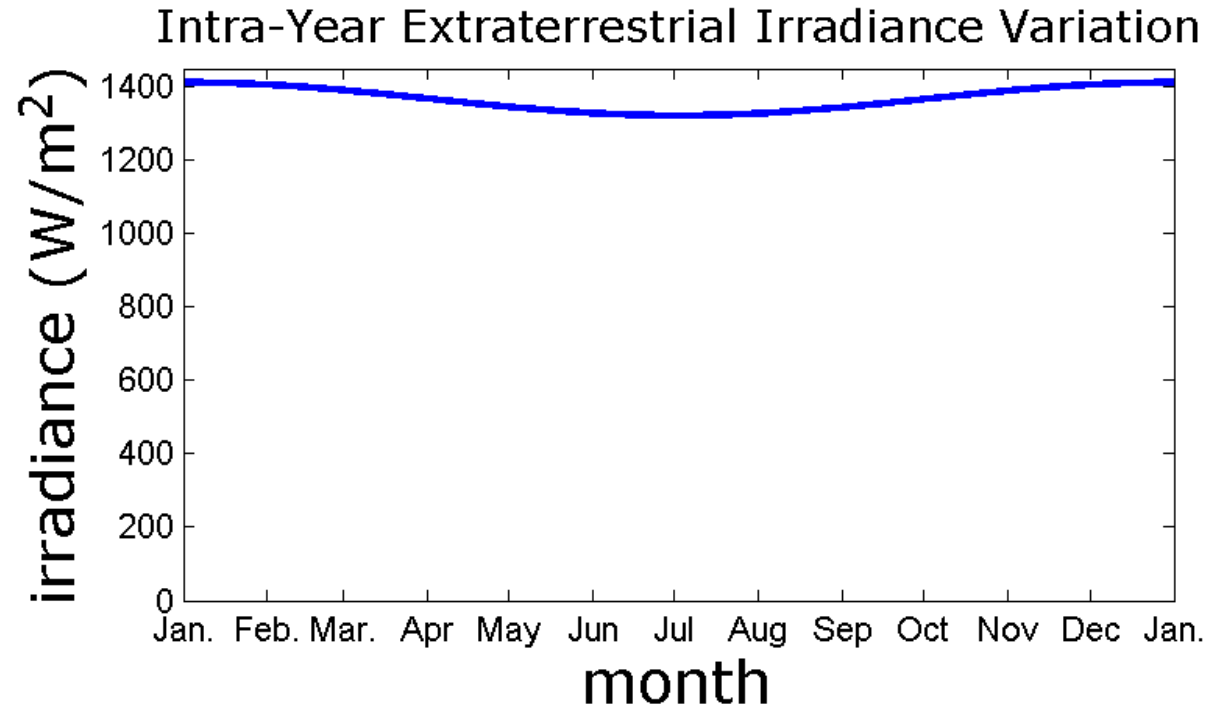
## »» Astronomy Trivia

- What day of the year is the Earth closest to the Sun (perihelion)?
  - A. December 21<sup>st</sup>
  - B. June 21<sup>st</sup>
  - C. September 21<sup>st</sup>
  - D. March 21<sup>st</sup>
  - E. January 4<sup>th</sup>
  - F. June 4<sup>th</sup>
  - G. October 18<sup>th</sup>

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  - G. October 18<sup>th</sup>
- Seasons have nothing to do with the distance from the sun

# Extraterrestrial Irradiance



# → Extraterrestrial Irradiance

- We can account for the distance from the sun:

$$G_{on}(d) = G_{sc} \left[ 1 + 0.033 \cos \left( 2\pi \left( \frac{d}{365} \right) \right) \right]$$

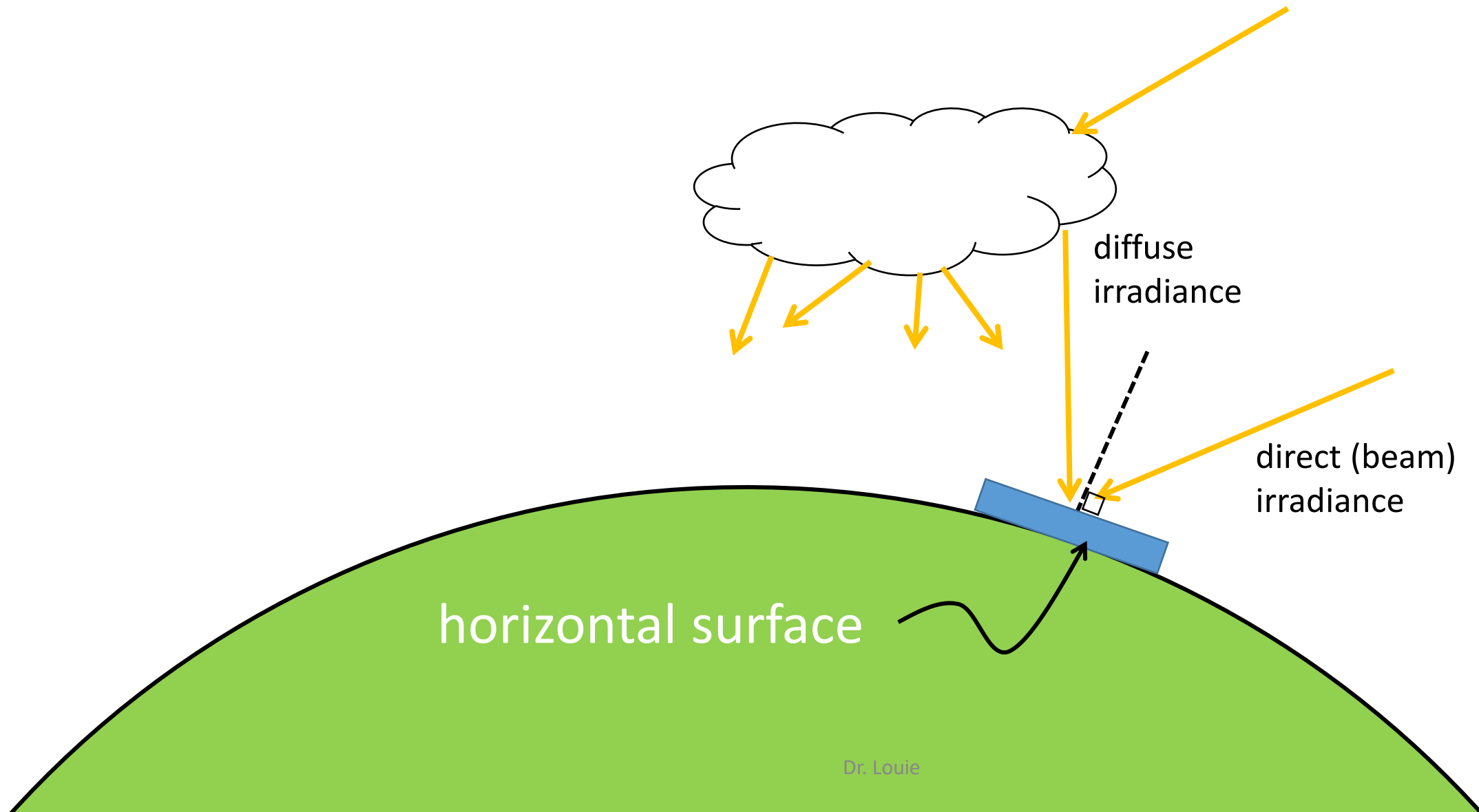
- $d$  is the day of year ( $d = 1$  on January 1)
- This is an **approximate** equation
- Peak-to-peak variation is small ( $<7\%$ )



# » Solar Irradiance

- Design of solar renewable energy systems requires knowing:
  - Irradiance, insolation
  - Direction of sunlight
  - If the sunlight is diffuse or direct
- We want to be able to quantify the nature of the solar irradiance on a given **surface** on the Earth
- First consider horizontal surfaces

# Solar Irradiance



## » Solar Irradiance

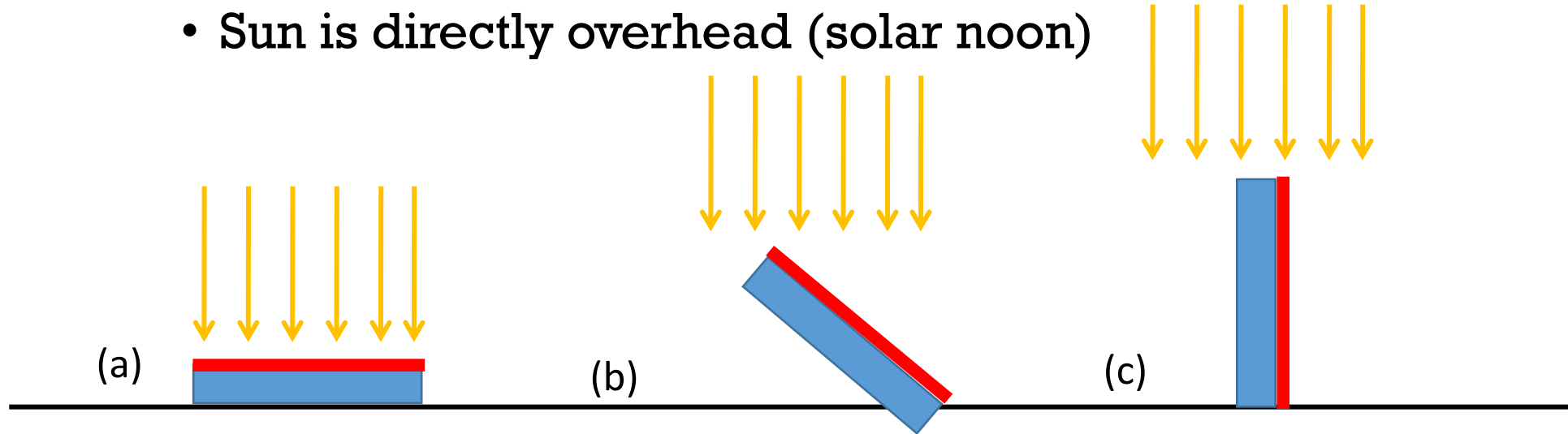
- Direct (beam) irradiance: solar irradiance received from the sun directly. It has not been scattered by the atmosphere.
  - Subscript b is used
- Diffuse irradiance: solar irradiance received from the sun after it has been scattered by the atmosphere
  - Implies change in direction
  - Subscript d is used
- Unless specified elsewhere, assume  $G_b$  and  $G_d$  are referenced to a horizontal surface

## » Solar Irradiance

- Global irradiance: sum of beam and diffuse irradiance
  - $G_{\text{GHI}} = G_{\text{b}} + G_{\text{d}}$
- Global Horizontal Irradiance (GHI): global irradiance on a horizontal surface
- GHI is a commonly measured quantity, from which  $G_{\text{b}}$  and  $G_{\text{d}}$  are estimated (more on this in a later lecture)

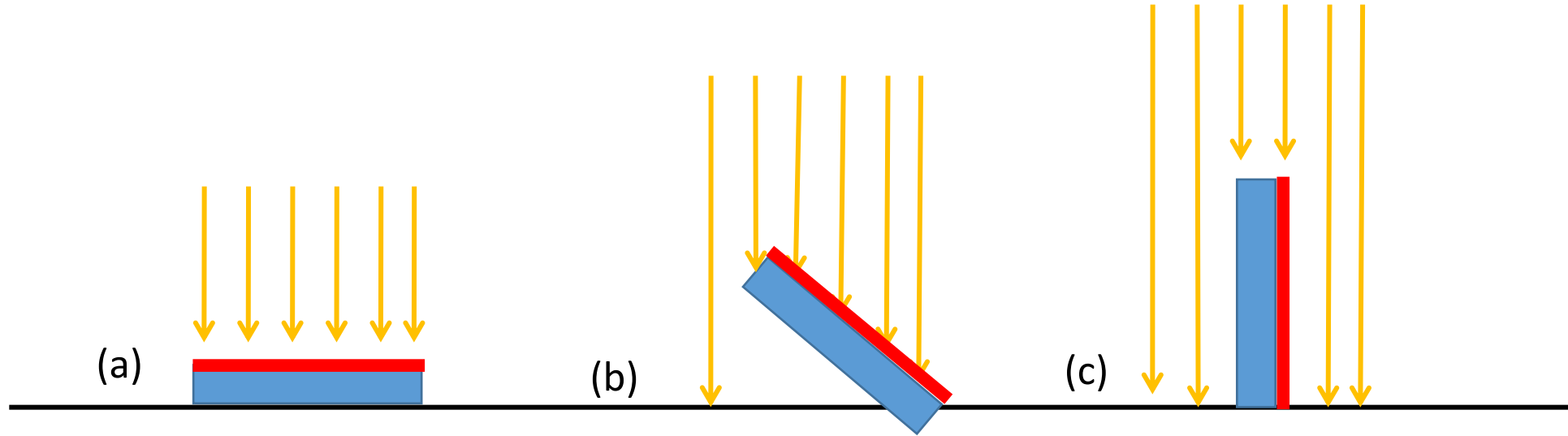
# Accounting for Angle of Incidence

- Which surface receives the most irradiance,  $G$ ?
- Assume:
  - No atmosphere, no ground reflectance
  - Only irradiance on the face counts
  - Sun is directly overhead (solar noon)



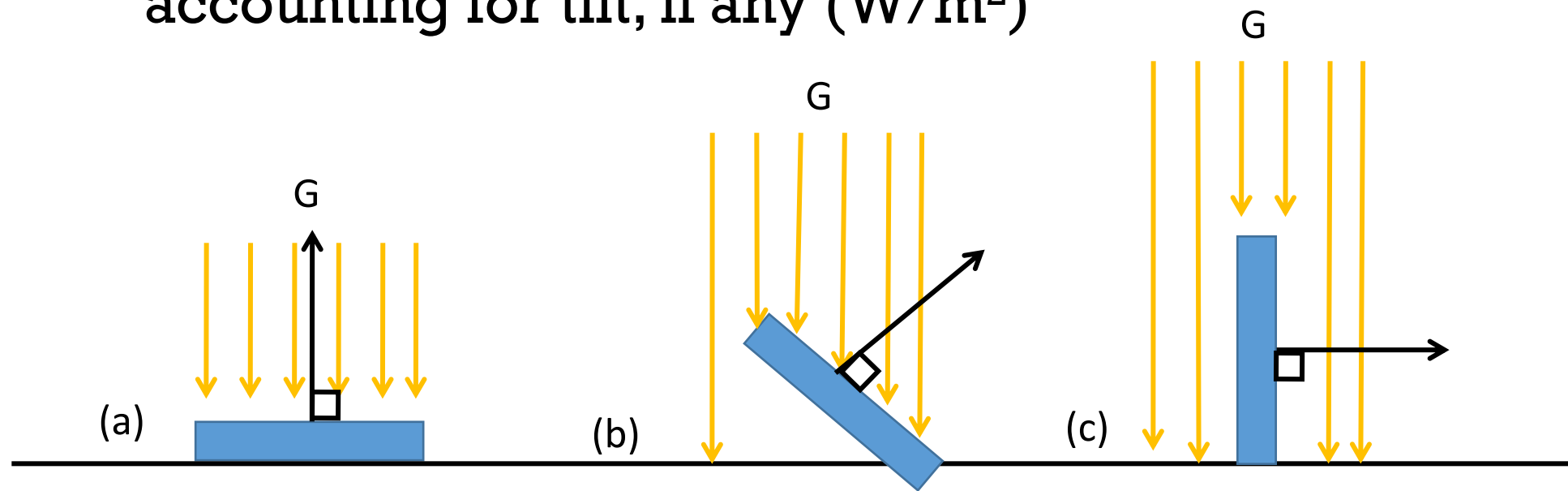
## Accounting for Angle of Incidence

- Surface (a): receives all irradiance
- Surface (b): receives a portion of the irradiance
- Surface (c): receives no irradiance



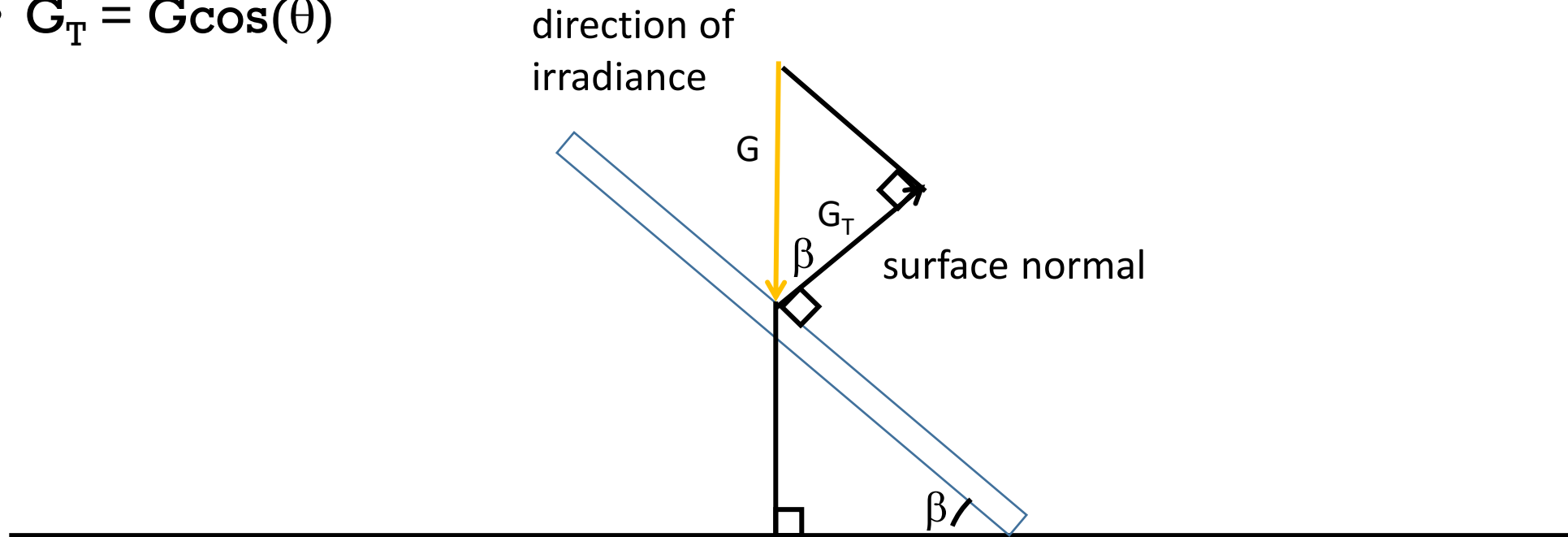
## Accounting for Angle of Incidence

- Compute the projection of  $G$  onto the normal of the surface
- $\theta$ : angle of incidence, degrees
- $G_T$ : total irradiance received on a surface, accounting for tilt, if any ( $\text{W}/\text{m}^2$ )



## Accounting for Angle of Incidence

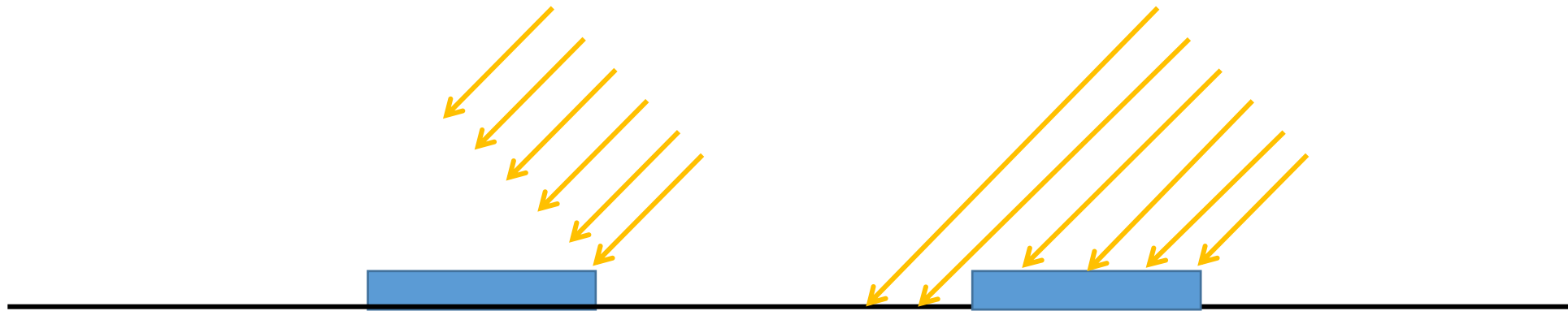
- Let  $\beta$ : tilt of the surface, degrees
- Under assumptions given  $\theta = \beta$ 
  - $G_T = G \cos(\theta)$





## Accounting for Angle of Incidence

- Similar derivation if the surface is horizontal, but the irradiance is at an angle



## Accounting for Angle of Incidence

- The angle between the sun and a horizontal surface is the zenith angle,  $\theta_z$
- VERY IMPORTANT!!!
- Zenith angle is the angle of incidence for a horizontal surface (special case)



## → Accounting for Angle of Incidence

- Top of the atmosphere irradiance for horizontal surfaces:
  - $G_0 = G_{0n} \cos(\theta_z)$
- Accounting for surface tilt, if any:
  - $G_{0T} = G_{0n} \cos(\theta)$

## → Accounting for Angle of Incidence

- Compute the extraterrestrial irradiance on a horizontal surface on October 18 when the Zenith angle is  $60^\circ$ , accounting for intra-year irradiance variability. [hint: October 18 is the 291<sup>st</sup> day of the year]

## Accounting for Angle of Incidence

- Compute the extraterrestrial irradiance on a surface on October 18 when the Zenith angle is  $60^\circ$ .

- $G_0 = G_{0n} \cos(\theta_z)$

$$G_{on}(d) = G_{sc} \left[ 1 + 0.033 \cos \left( 2\pi \left( \frac{291}{365} \right) \right) \right] = 1380$$

$$G_0 = 1380 \cos(60) = 690 \text{ W/m}^2$$

## → Accounting for Angle of Incidence

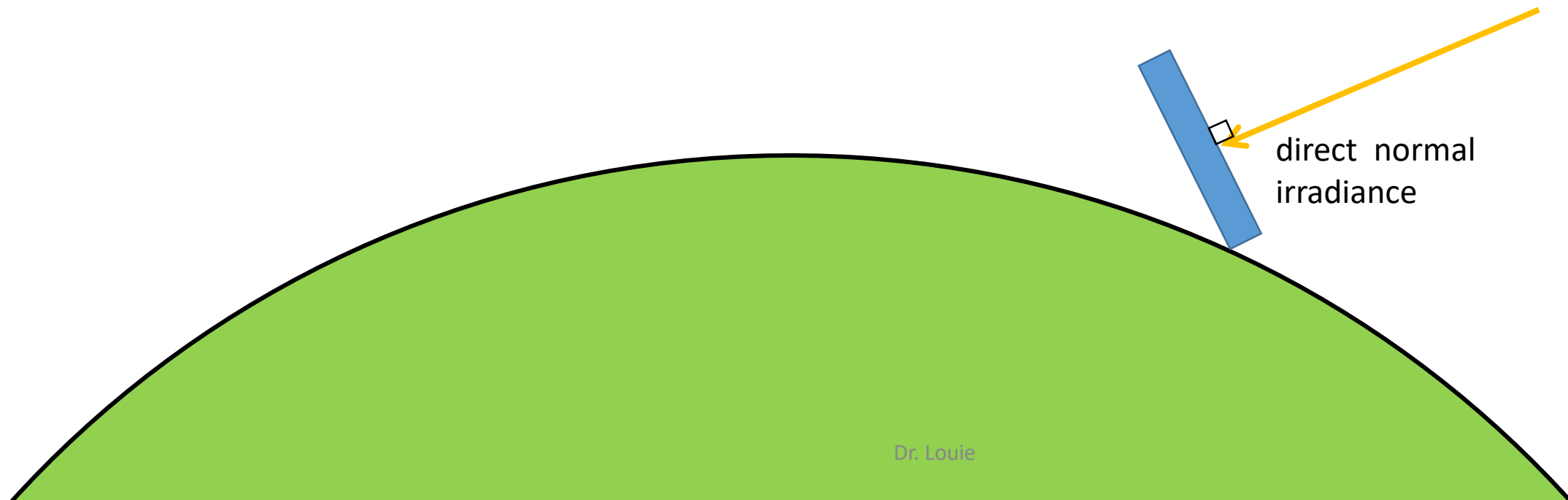
- Angle of incidence is implicitly accounted for when GHI is measured
  - $G_b$  and  $G_d$  must also account for angle of incidence

## » Solar Irradiance

- Concentrating Solar Power (CSP) systems can only utilize beam irradiance
- CSP receivers also track the sun to maximize energy
  - Receiver face stays normal to the sun for most hours
  - Direct Normal Irradiance (DNI): beam irradiance received by a surface normal to the irradiance ( $G_{\text{DNI}}$ )
- Possible (but cumbersome) to estimate DNI from GHI

# Solar Irradiance

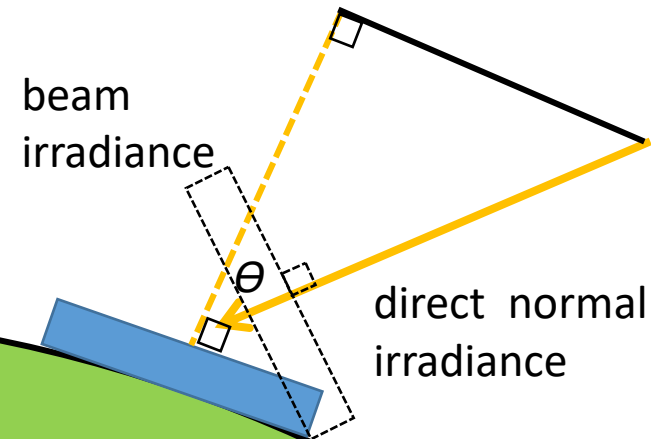
Direct Normal Irradiance: beam irradiance on a surface that is normal to the beam





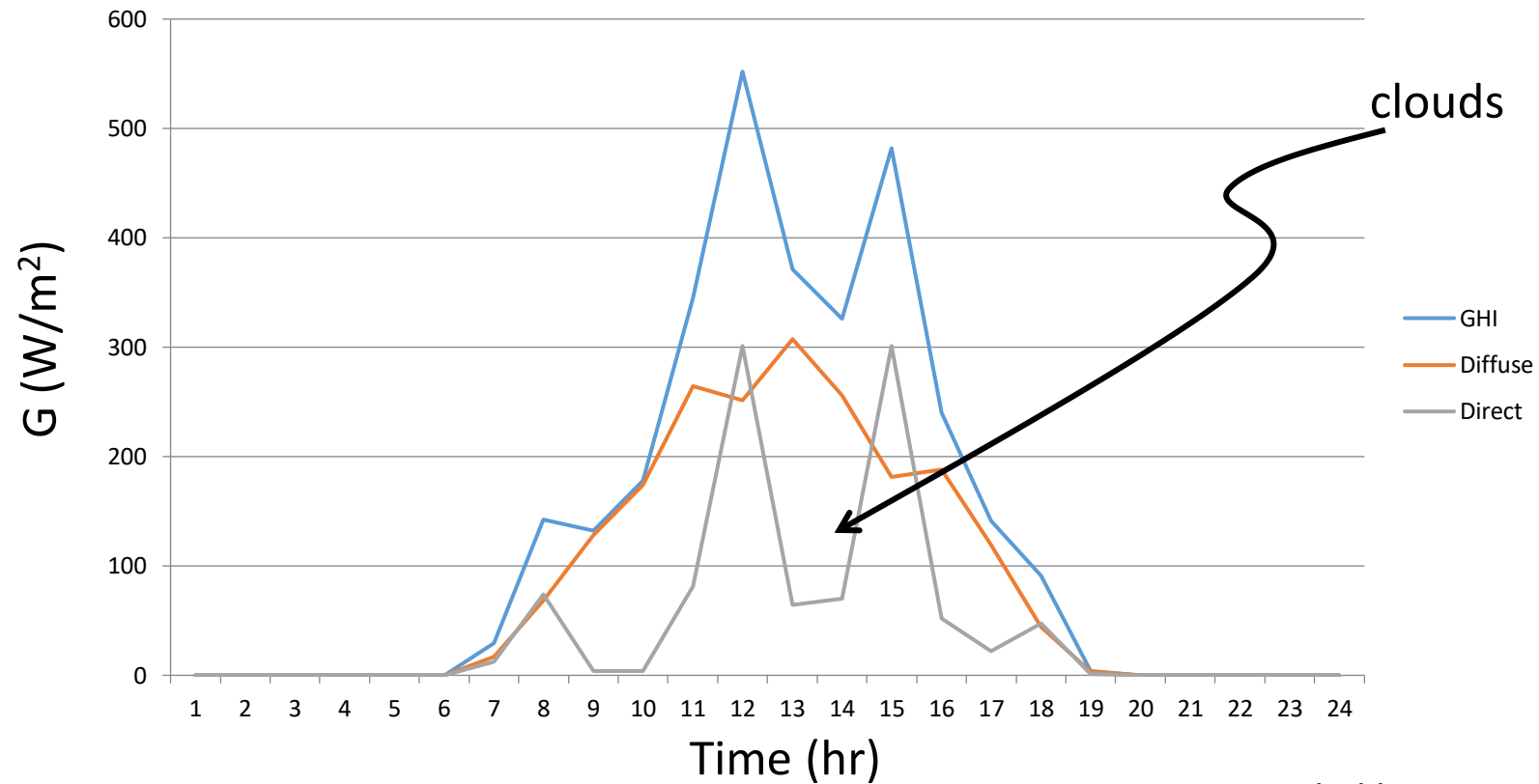
# Solar Irradiance

- DNI is related to beam irradiance by:
  - $G_b = G_{\text{DNI}} \cos(\theta)$



# » Solar Irradiance

Irradiance on 3/21/1997  
in Renton, WA

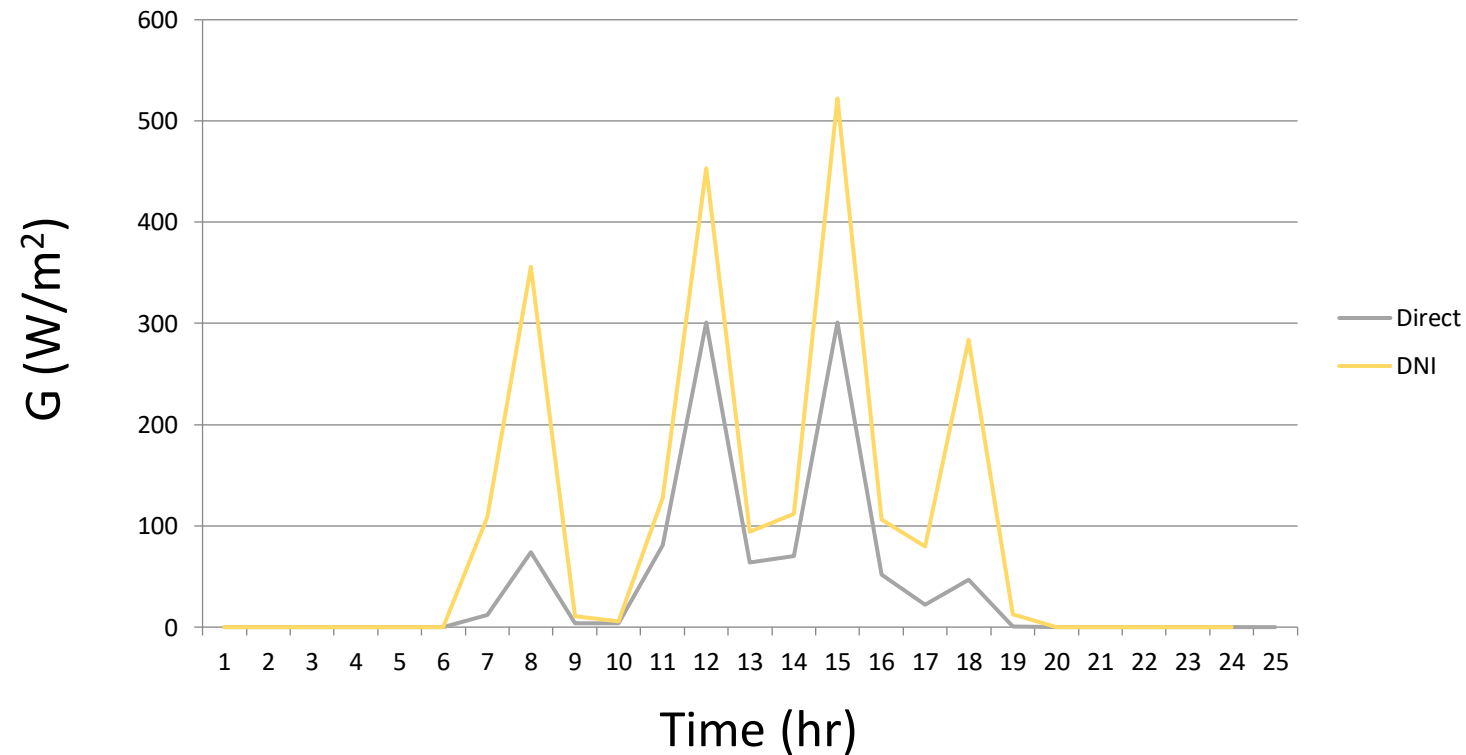


Data provided by: 3TIER

# → Solar Irradiance

Not a constant scaling.  
 $\cos(\theta)$  varies throughout the day

Irradiance on 3/21/1997  
in Renton, WA



Data provided by: 3TIER

# → Solar Irradiance

- For a given surface
  - $G_{\text{GHI}} = 240 \text{ W/m}^2$
  - $G_{\text{d}} = 188 \text{ W/m}^2$
- What is  $G_{\text{b}}$ ?

## → Solar Irradiance

- For a given surface
  - $G_{\text{GHI}} = 240 \text{ W/m}^2$
  - $G_{\text{d}} = 188 \text{ W/m}^2$
- What is  $G_{\text{b}}$ ?
  - $G_{\text{b}} = G_{\text{GHI}} - G_{\text{d}} = 52 \text{ W/m}^2$

## → Solar Irradiance

- GHI will always be greater than or equal to DNI
  - True
  - False
- GHI will always be less than or equal to DNI
  - True
  - False

## » Solar Irradiance

- GHI will always be greater than or equal to DNI
  - True
  - False
    - On clear days and with certain angles of incidence,  $\text{DNI} > \text{GHI}$
- GHI will always be less than or equal to DNI
  - True
  - False
    - On cloudy days and with certain angles of incidence,  $\text{GHI} > \text{DNI}$