

13-Battery Voltage and Current Characteristics

Off-Grid Electrical Systems in Developing Countries

Chapter 8.5

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Learning Outcomes

At the end of this lecture, you will be able to:

- ✓ define the nominal voltage of a battery
- ✓ describe the I-V curve of a battery and explain why it is non-linear
- ✓ develop and apply a circuit model for a battery

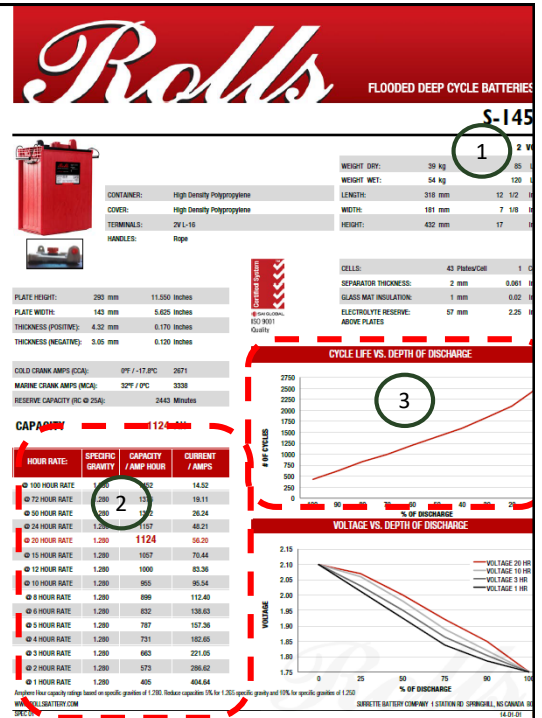
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Battery Specification Sheets

- Provide technical information on battery characteristics and performance
- Not always easy to interpret
- Most important characteristics
 1. Nominal Voltage
 2. Capacity
 3. Cycle life

We will discuss these in a later lecture

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Nominal Voltage

- Nominal voltage: approximately equal to the average battery voltage during a charge and discharge cycle
 - Not: open-circuit voltage when fully charged or discharged
- Lead-acid batteries typically have nominal voltages of 2V, 6V, 12V or 24V
- Nominal voltage of a lithium-ion cell typically between 3.2V and 3.8V (depending on the chemistry used)
- Open-circuit voltage for a fully-charged lead-acid cell is approximately 2.10 V

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Nominal Voltage

A lead-acid battery with 24V nominal voltage (12 cells in series) will have a fully-charged open-circuit voltage of approximately $12 \times 2.11 = 25.32\text{V}$

Open-circuit cell voltage	Approximate state-of-charge (%)										
	0	10	20	30	40	50	60	70	80	90	100
Flooded (V/cell) (V/cell)	1.90	1.92	1.94	1.96	1.99	2.01	2.03	2.05	2.07	2.09	2.11
AGM (V/cell)	1.94	1.96	1.98	2.00	2.02	2.04	2.06	2.08	2.10	2.12	2.14

Open-Circuit Voltage

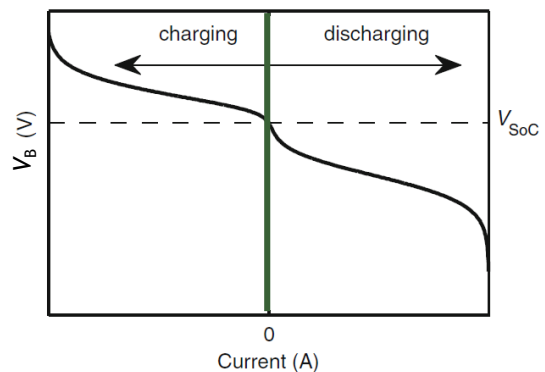
- Open-circuit voltage refers to the voltage between the positive and negative terminals of a cell, battery, or battery bank
- Remember that batteries exhibit non-linear, temperature-dependent behavior, and have long time constants (before steady-state is reached)

Open-Circuit Voltage

- Open-circuit voltage can only reliably be used to estimate state-of-charge if the battery has been open-circuited, not hot or cold, and given enough time to “rest”
 - Resting allows the chemicals within the battery to mix/re-distribute, avoiding localized concentrations which affect voltage
 - Resting time required can be several minutes to several hours

I-V Characteristic

- I-V characteristic shows how the *terminal* voltage (V_B) of the battery (cell) varies with charge/discharge current
- Note:
 - plot assumes the state-of-charge is constant at each point along the curve
 - non-linear dependence of terminal voltage with current
 - Asymmetry

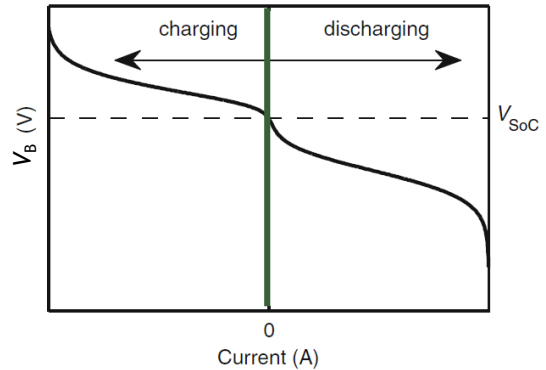


V_{SoC} : open-circuit voltage (State-of-Charge)

Don't confuse the x-axis with time

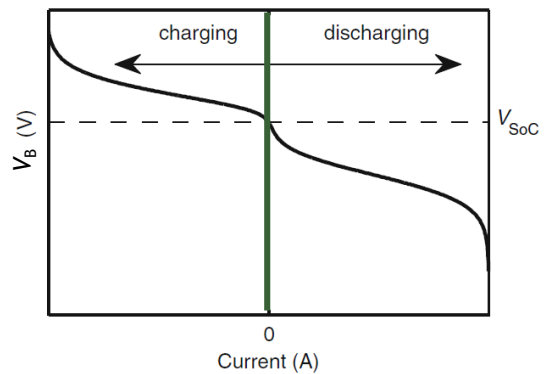
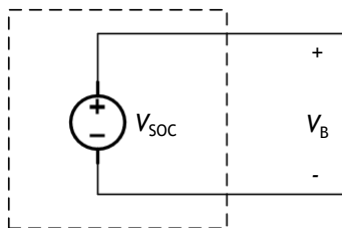
I-V Characteristic

- Important:
 - Charging: terminal voltage is increased from open-circuit
 - Discharging: terminal voltage is decreased from open-circuit voltage



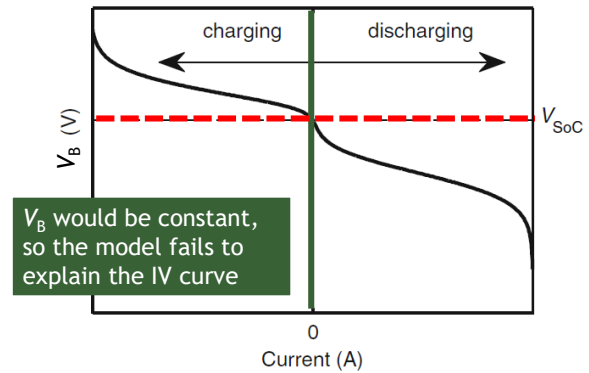
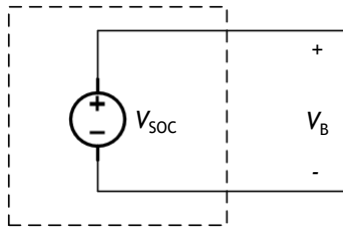
How can we explain the I-V curve?

What about this model?



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What about this model?



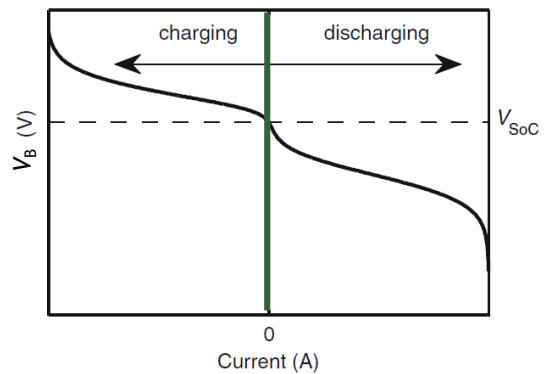
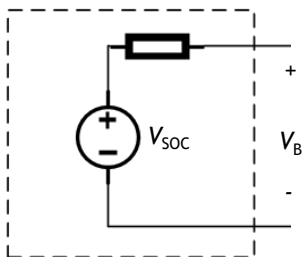
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How can we explain the I-V curve?

What about this model?
Sketch the I-V curve.



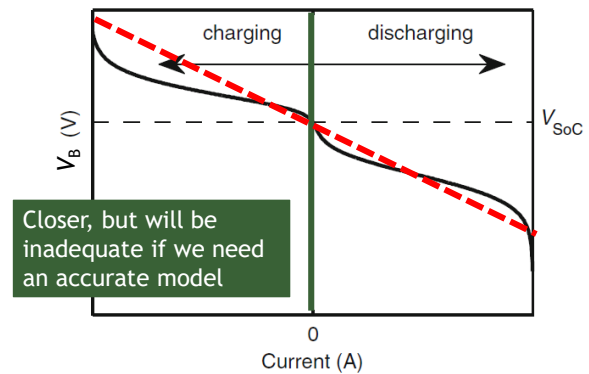
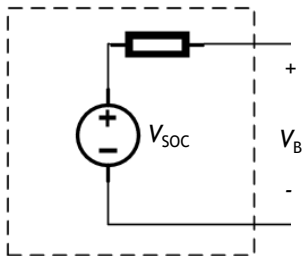
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How can we explain the I-V curve?

What about this model?
Sketch the I-V curve.



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Polarization

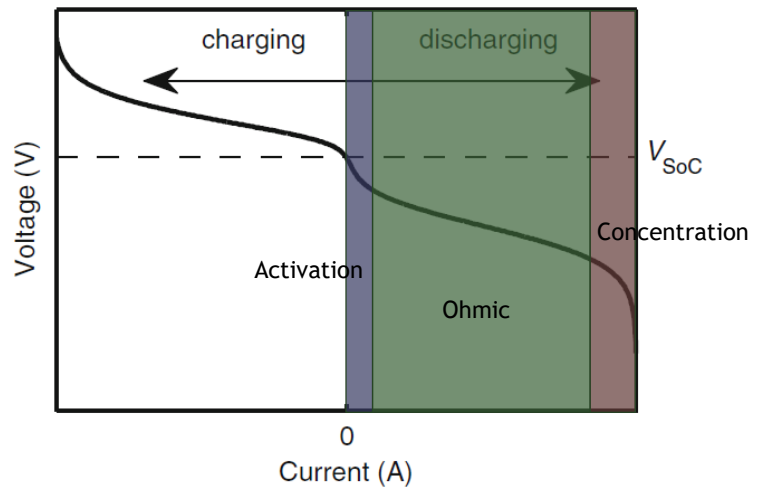
- Non-linearity of I-V curve can be attributed to three mechanisms (*polarizations*)
- *Ohmic*: voltage drop caused by the battery current passing through the electrode resistance and electrolyte resistance (difficulty of ions moving through electrolyte)
- *Activation*: related to the kinetics of the reactions, for there to be current the equilibrium balance of chemical and electrostatic potential must be upset (decreased voltage when discharging, increased when charging)
- *Concentration*: at higher current, localized depletion or accumulation of ions can occur, which, per the Nernst equation will affect the cell voltage

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Polarizations



Only discharging shown, but analogous effects are present when charging

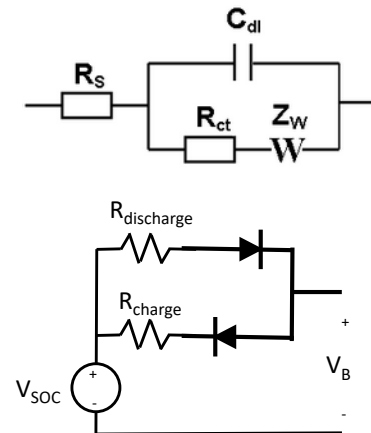
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Cell Circuit Model

- Several circuit models of battery cells have been proposed and used
- Selection depends on what characteristics are of interest (e.g. steady-state, dynamics, etc.)



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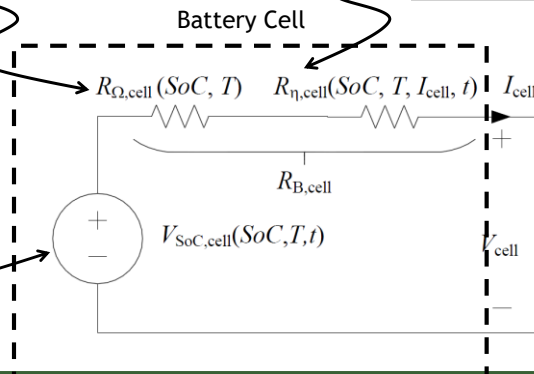
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Circuit Model of a Battery Cell

Ohmic polarization, dependent on:
state-of-charge, temperature

Activation and concentration
polarization dependent on:
state-of-charge, temperature,
current magnitude and polarity,
time (since charged/discharged)

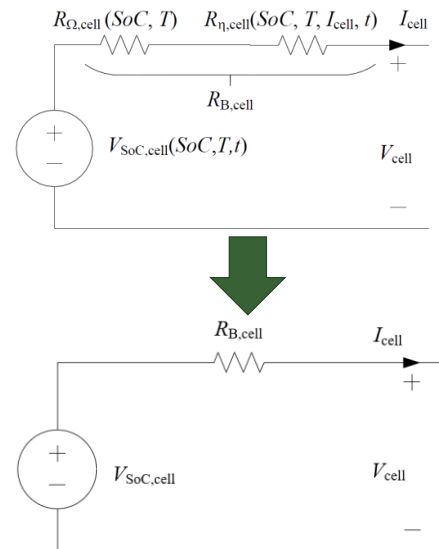
State-of-charge voltage,
dependent on:
state-of-charge, temperature,
time (since
discharged/charged)



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Cell Circuit Model

- Combine the resistances into a single quantity $R_{\text{B,cell}}$ which we will call the “battery resistance”
- Keep in mind:
 - $R_{\text{B,cell}}$ models the Ohmic, activation and concentration polarizations
 - $R_{\text{B,cell}}$ depends on many factors, and so there is no single $R_{\text{B,cell}}$ for a battery, rather we assume that $R_{\text{B,cell}}$ refers to the resistance at the present state of the battery
 - $R_{\text{B,cell}}$ is not the “internal resistance” sometimes reported on spec sheets, the reported value is usually the Ohmic resistance only



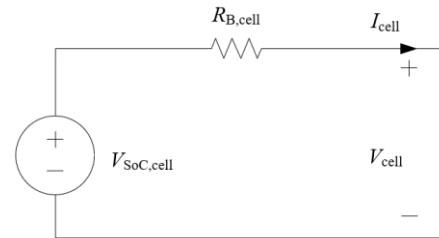
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Cell Circuit Model

- Analysis via KVL:

$$V_{\text{cell}} = V_{\text{SoC,cell}} - I_{\text{cell}} R_{\text{B,cell}}$$

- Voltage drop associated with $R_{\text{B,cell}}$ causes the terminal voltage to be greater than $V_{\text{SoC,cell}}$ when charging, and lower than $V_{\text{SoC,cell}}$ when discharging



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Battery Circuit Model

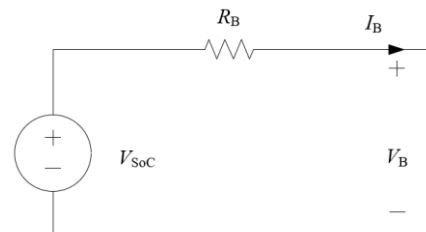
Extension of model to a battery with two or more series connected cells is straightforward

$$R_{\text{B}} = N_{\text{cells}} \times R_{\text{B,cell}}$$

$$I_{\text{B}} = I_{\text{cell}}$$

$$V_{\text{SoC}} = N_{\text{cells}} \times V_{\text{SoC,cell}}$$

$$V_{\text{B}} = V_{\text{SoC}} - I_{\text{B}} R_{\text{B}}$$



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Exercise

The equilibrium open-circuit cell voltage of a 24 V lead-acid battery is 24.96 V. An external circuit is connected to the battery that draws 21 A. Assume the battery resistance R_B under these conditions is 0.060Ω . Compute the terminal voltage.

Exercise

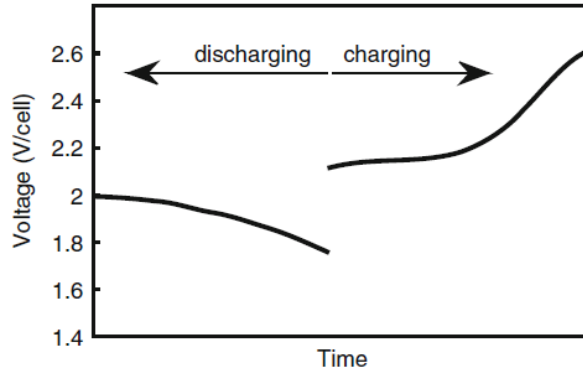
The equilibrium open-circuit cell voltage of a 24 V lead-acid battery is 24.96 V. An external circuit is connected to the battery that draws 21 A. Assume the battery resistance R_B under these conditions is 0.060Ω . Compute the terminal voltage.

$$V_B = V_{SoC} - I_B R_B$$

$$V_B = 24.96 - 21.0 \times 0.060 = 23.70 \text{ V}$$

Cell Voltage During Discharging/Charging

Curves are influenced by the dual effects of increasing V_{SoC} and changes in the polarizations as function of state-of-charge



Current magnitude is kept constant throughout

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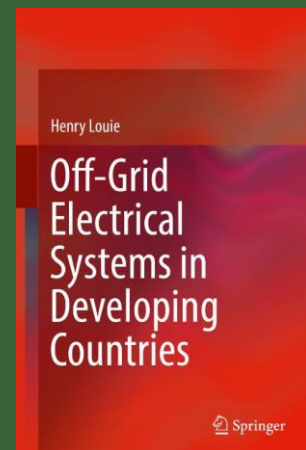
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