

# 21-Micro Hydro Power Systems

*Off-Grid Electrical Systems in Developing Countries*  
Chapter 6.3

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## Learning Outcomes

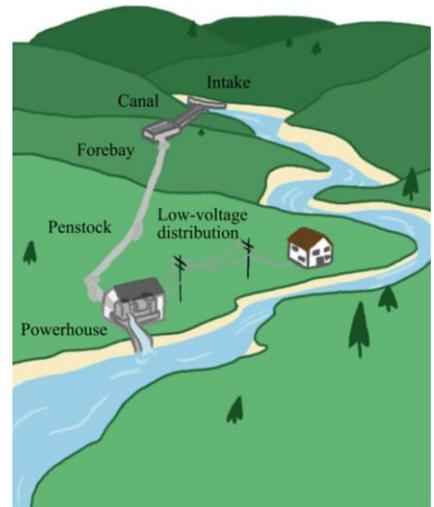
At the end of this lecture, you will be able to:

- ✓ understand the basic operating principles of microhydro power systems
- ✓ identify and describe the components of a MHP system
- ✓ estimate the power potential of a hydro resource

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## Micro Hydro Power (MHP)

- Turbines convert energy in water into mechanical energy to power a turbine
- Mature technology
- Requires suitable water resource and terrain
- Can be AC-coupled or DC-coupled
- Civil works are required



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## Hydro Resource

- Power potential of a hydro resource depends on:
  - Head (m)
  - Flow rate ( $m^3/s$ )
  - Conveyance system loss estimate
- Desirable characteristics
  - Steep surrounding terrain (reduces penstock length and losses)
  - Water intake at high elevation compared to powerhouse location
  - Consistent, predictable seasonal flow

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# Bernoulli's Equation

- From Bernoulli, the energy in a volume of water depends on its
  - Velocity
  - Elevation (above reference plane)
  - Pressure
- Energy from pressure and velocity usually ignored

$$\frac{1}{2} \rho_{wa} v_{wa}^2 + \rho_{wa} g z + p_{wa} = K$$

$\rho_{wa}$ : density of water, ~1000 kg/m<sup>3</sup>  
 $v_{wa}$ : velocity of water, m/s  
 $g$ : gravitational constant, 9.81 m/s<sup>2</sup>  
 $z$ : elevation, m  
 $p_{wa}$ : pressure, Pa  
 $K$ : constant, J/m<sup>3</sup>

# Bernoulli's Equation

As water flows down a slope in open air, assuming no friction losses and ignoring the small change in atmospheric pressure, the velocity increases and the elevation decreases so that  $K$  remains unchanged

$$\frac{1}{2} \rho_{wa} v_{wa}^2 + \rho_{wa} g z + p_{wa} = K$$

# Bernoulli's Equation

What happens if water is flowing through a pipe, and a valve is closed so that the velocity suddenly drops to zero?

$$\frac{1}{2} \rho_{wa} v_{wa}^2 + \rho_{wa} g z + p_{wa} = K$$



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# Total Head

Divide Bernoulli's equation by  $\rho_{wa}$  and  $g$  to yield:

$$\frac{1}{2} \rho_{wa} v_{wa}^2 + \rho_{wa} g z + p_{wa} = K$$

$$\frac{1}{2g} v_{wa}^2 + z + \frac{p_{wa}}{\rho_{wa} g} = H_t$$

Units of each term are meters

Velocity Head

Elevation Head

Pressure Head

Total Head

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## Total Head

- We can conceptually replace a water resource with certain velocity, elevation and pressure and volume with an equivalent volume of water at no pressure, no velocity at an elevation equal to the total head
- This makes energy calculations and comparisons easier
- A water resource with greater total head has greater energy density than one with a lower total head

## Energy in Water

- Recall that potential energy of an elevated mass is:

$$E = m \times g \times h = (\rho \times V) \times g \times z$$

- The total energy in water with volume  $V_{wa}$  is:

$$E_{wa,total} = \rho_{wa} \times V_{wa} \times g \times H_t$$

$m$ : mass, kg  
 $\rho$ : density, kg/m<sup>3</sup>  
 $V_{wa}$ : volume, m<sup>3</sup>

Don't confuse this with velocity

## Example

Compute the total head and energy of two cubic meters of water whose velocity is 1 m/s and is located 38 meters above the reference plane. Assume the water is exposed to atmospheric pressure (101.325 kPa)

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## Example

Compute the total head and energy of two cubic meters of water whose velocity is 1 m/s and is located 38 meters above the reference plane. Assume the water is exposed to atmospheric pressure (101.325 kPa)

$$H_t = \frac{1}{2g} v_{wa}^2 + z + \frac{p}{\rho g} = \frac{1}{2 \times 9.8} 1^2 + 38 + \frac{101,325}{1000 \times 9.8} = 0.05 + 38 + 10.33 = 48.39\text{m}$$

Note that the total head is independent of the volume

Most of the total head is due to the elevation head

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## Example

Compute the total head and energy of two cubic meters of water whose velocity is 1 m/s and is located 38 meters above the reference plane. Assume the water is exposed to atmospheric pressure (101.325 kPa)

$$E_{\text{wa,total}} = \rho_{\text{wa}} \times V_{\text{wa}} \times g \times H_t = 1000 \times 2 \times 9.8 \times 48.39 = 0.95 \text{ MJ}$$

## Effective Head

- **Effective Head:** the head available to a hydro turbine for energy conversion
  - Effective Head < Total Head
- **Difference between effective and total head arise from:**
  - friction and conveyance system losses
  - velocity head is usually low compared to the elevation head and assumed unavailable to the turbine
  - water at the turbine outlet is at atmospheric pressure, so this energy is not available to the turbine

## Effective Head

- If we ignore the losses in the conveyance system, then the effective head is

$$\cancel{\frac{1}{2g}v_{wa}^2} + z + \cancel{\frac{p_{wa}}{\rho_{wa}g}} = H$$

The effective head is equal to the elevation head

- Including losses:

$$H = z - H_f = z\eta_{\text{convey}}$$

$H$ : effective head, m

$\eta_{\text{convey}}$ : conveyance system efficiency

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## Hydro Resource

- Useable energy in a volume of water

$$E_{wa} = g \times H \times m_{wa} = g \times H \times \rho_{wa} \times V_{wa}$$

- Power in falling water

$$P_{wa} = \frac{dE_{wa}}{dt} = \rho_{wa} \times g \times H \times Q$$

$g$ : gravitational constant, 9.8 m/s<sup>2</sup>

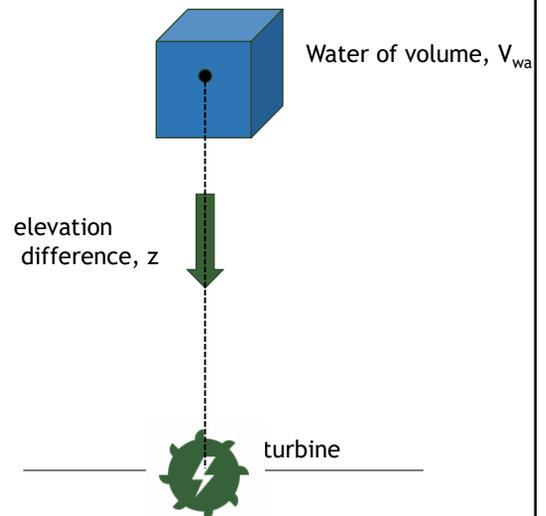
$H$ : effective head, m

$m_{wa}$ : mass of water, kg

$V$ : volume of water, m<sup>3</sup>

$\rho_{wa}$ : density of water, 1000 kg/m<sup>3</sup>

$Q$ : water flow rate, m<sup>3</sup>/s



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## Exercise

The water resource for a MHP scheme has an effective head of 38 m. The flow rate is 0.005 m<sup>3</sup>/s (5 liters per second). Compute power available to the input of the turbine.

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The water resource for a MHP scheme has an effective head of 38 m. The flow rate is 0.005 m<sup>3</sup>/s (5 liters per second). Compute power available to the input of the turbine.

$$P_{wa} = \rho_{wa} \times g \times H \times Q$$

$$P_{wa} = 1000 \times 9.8 \times 38 \times 0.005 = 1862 \text{ W}$$

# Power Extracted by Turbine

Hydro turbines, if properly designed and operated, are highly efficient, but the losses should be considered.

The mechanical power extracted (developed) by the turbine is:

$$P_{d,turbine} = P_{wa} - P_{outlet} = \eta_{turbine} P_{wa}$$

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# Water Intake

Only a portion of the stream is diverted for MHP use



(courtesy Joe Butchers)



(courtesy Joe Butchers)



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## Intake



Removeable boards  
to clear silt/debris



Water passes through  
grate into penstock  
(not visible)

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## Penstock

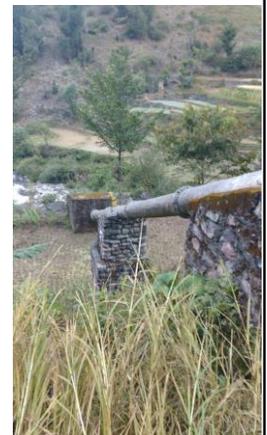
- Conveys water from intake to turbine
- Above- or below-ground pipe
- Should be straight and short



(courtesy Joe Butchers)



(courtesy Joe Butchers)



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## Turbine Types

Pelton



Francis



Crossflow



Turgo



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## Turbine coupled to generator



*(courtesy Joe Butchers)*



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## Turbine Selection

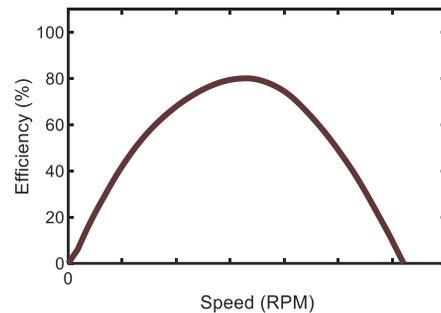
- Several types of hydro turbines
- Most water resources for MHP are high head or medium head

High Head	Medium Head	Low Head
Pelton	Crossflow	Crossflow
Pelton (Multi-jet)	Turgo	Propeller
Turgo	Pelton (Multi-jet), Francis	Kaplan

## Turbine Selection

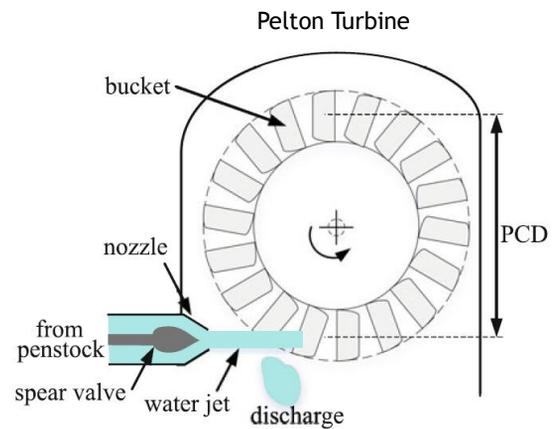
- Select turbine that will operate most efficiently given the power and rotational speed requirements, and the water resource speed and head
  - Turbine Application Chart
  - Calculate using “specific speed”

Illustrative efficiency curve for Pelton Turbine

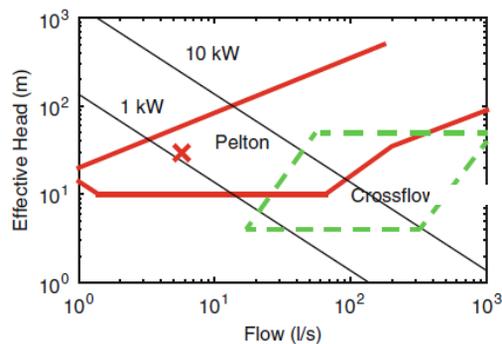


## Speed Matters

- Velocity of water jet depends on head
- Efficiency is maximized when water jet speed is 1/2 the tangential speed of the bucket
- Bucket must rotate at certain RPM to produce desired voltage frequency
- Mismatch of resource and turbine lowers efficiency

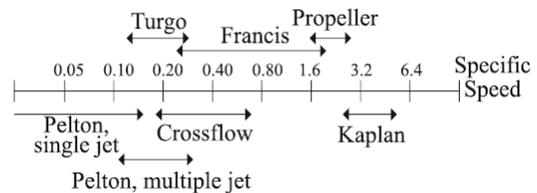


## Turbine Application Chart



## Specific Speed (Dimensionless)

$$S = \frac{\omega_m \sqrt{Q}}{(gH)^{3/4}} = \frac{\omega_m \sqrt{P_{d,turbine} / \rho_{wa}}}{(gH)^{5/4}}$$



$\omega_m$ : rotational speed of turbine, rad/s  
 g: gravitational constant, m/s<sup>2</sup>  
 H: effective head, m  
 Q: water flow rate, m<sup>3</sup>/s

Caution: several other “dimensioned” specific speeds are used and reported by turbine manufacturers.

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## Exercise

Compute the dimensionless specific speed for a water resource with an effective head of 30 m. Assume the turbine will rotate at 1500 RPM with a developed mechanical power of 1.25 kW.

$$S = \frac{\omega_m \sqrt{P / \rho_{wa}}}{(gH)^{5/4}} = \frac{\frac{2\pi}{60} \times 1500 \sqrt{1250 / 1000}}{(9.8 \times 30)^{5/4}} = 0.144$$

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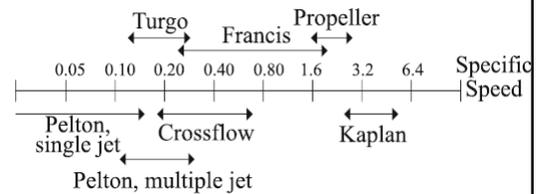
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## Exercise

Compute the dimensionless specific speed for a water resource with an effective head of 30 m. Assume the turbine will rotate at 1500 RPM with a developed mechanical power of 1.25 kW.

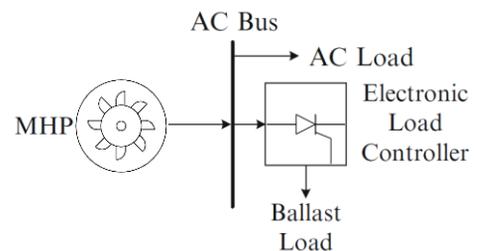
$$S = \frac{\omega_m \sqrt{P / \rho_{wa}}}{(gH)^{5/4}} = \frac{2\pi}{60} \times 1500 \sqrt{1250 / 1000} / (9.8 \times 30)^{5/4} = 0.144$$



Here we see that either a Pelton (single or multiple jet) or Turgo is an appropriate turbine

## Turbine Control

- Can be AC- or DC- coupled
- Frequency Regulation
  - Spear valve: adjust water flow to turbine
  - Electronic load controller: adjust electrical power to ballast (dummy) load to keep electrical power constant
- Voltage Regulation
  - Automatic Voltage Regulator (synchronous generator)
  - Impedance controller (self-excited induction generators)
- Do not suddenly remove load (overspeed can result)



# Micro Hydro Power



- Relatively inexpensive
- Simple to operate
- No fuel costs
- Long operational life
- Consistent power production---no need for batteries
- Renewable resource
- No emissions
- Mature technology



- Adequate water resource not widely available
- High up-front costs
- Water resource characteristics (flow rate, head, and effects of seasonality) must be assessed
- Must be custom-designed
- Commercially-available turbines might not match the site characteristics
- Many stakeholders affected—permits and permissions might be required

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# Contact Information

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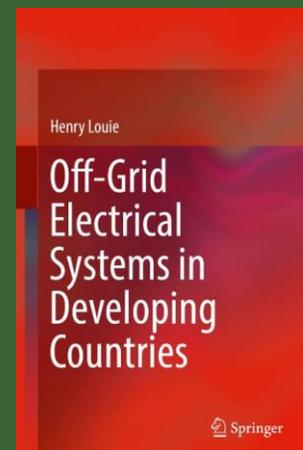
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