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ANTENNA ENGINEERING HANDBOOK



Antenna Engineering Handbook

THIRD EDITION

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Henry Jasik Editor of First Edition

McGraw-Hill, Inc.

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An internationally known authority in the antenna engineering field, Dr. Henry Jasik was highly respected for his breadth of information, keen insight, and depth of knowledge in both fundamentals and applications. He received the degree of Bachelor of Science in Electrical Engineering in 1938 from Newark College of Engineering and the degrees of Master and Doctor of Electrical Engineering in 1951 and 1953, respectively, from the Polytechnic Institute of Brooklyn.



Dr. Jasik worked in the Navy Department from 1938 to 1939 and in the Civil Aeronautics

Administration (CAA) from 1939 to 1944. While in the CAA, he worked on radio aids to air navigation, including instrument landing systems and VHF radio ranges. From 1944 to 1946, he was an officer in the United States Navy, where he worked on the development of airborne radar and communications antennas at the Naval Research Laboratories.

From 1946 to 1949, Dr. Jasik was associated with Andrew Alford, Consulting Engineers, as Senior Project Engineer and as Vice-President of the Alford Manufacturing Company. From 1949 to 1952, he was employed by the Airborne Instruments Laboratory (AIL), where he was associated with the Special Devices Section and the Antenna Section as Assistant Supervising Engineer. In 1952, he became an independent consultant.

In 1955, Dr. Jasik started Jasik Laboratories, Inc., a completely integrated operation for the design, development, and production of antennas. Under his leadership, the company grew and prospered. With design experience from simple Yagi-Uda arrays to exotic multiple-feed systems, Jasik Laboratories became widely known throughout the electronics industry as an unusually talented team of antenna specialists. They designed, manufactured, and tested a wide variety of antennas, such as dipoles, horns, log periodics, double-conical feeds, and many others. In 1969, Cutler-Hammer (which later became the Eaton Corporation) acquired Jasik Laboratories, and at the time of his death, Dr. Jasik was a Vice-President in Eaton's AIL Division.

Dr. Jasik was elected a Fellow of the Institute of Electrical and Electronic Engineers in 1958 for his contributions to "the theory and design of VHF and microwave antennas." He was a member of Sigma Xi and Eta Kappa Nu and was a registered professional engineer in New York and Massachusetts.

In the course of his distinguished career, Dr. Jasik was awarded several patents, and he designed practical antennas for U.S. Navy ships and for the FM broadcast antenna which operated for many years at the top of the Chrysler Building in New York City. He also made many important contri-

butions to the young science of radio astronomy by designing and producing improved feed structures for many paraboloidal-reflector radio telescopes. His innovative work significantly improved the tools of radio astronomers.

Dr. Jasik was Editor of the First Edition of the Antenna Engineering Handbook, published by McGraw-Hill in 1961. His vision and creative work produced the most valuable reference book for antenna engineers throughout the world. This new edition is dedicated to his memory in order to convey appreciation for his outstanding and lasting contributions to the field of antenna engineering.

Contents

INTRODUCTION AND FUNDAMENTALS

•		
1	Introduction to Antennas	1-3
	Richard C. Johnson, Georgia Institute of Technology	
2	Fundamentals of Antennas	2-1
	Henry Jasik, AIL Division of Eaton Corporation	
3	Arrays of Discrete Elements	3-1
	Mark T. Ma, National Institute of Standards and Technology	
2_	TYPES AND DESIGN METHODS	
4	Dipoles and Monopoles	4-3
•	Chen To Tai, The University of Michigan	
	Stuart A. Long, University of Houston	
5	Loop Antennas	5-1
	Glenn S. Smith, Georgia Institute of Technology	
6	Small Antennas	6-1
	Harold A. Wheeler, Hazeltine Corporation	
7	Microstrip Antennas	7-1
	Robert E. Munson, Ball Communication Systems Division	
8	Slot Antennas	8-1
	William F. Croswell and Mary Beth Selby, Harris Corporation	
9	Slot Antenna Arrays	9-1
	Hung Yuet Yee and Robert C. Voges, Texas Instruments, Inc.	
10	Leaky-Wave Antennas	10-1
	Arthur A. Oliner, Polytechnic University	
11	Long-Wire Antennas	11-1
	Edmund A. Laport, RCA Corporation	

12		12-1
	Francis J. Zucker, Rome Laboratory, Hanscom Air Force Base	
13	Helical Antennas	13-1
	Howard E. King and Jimmy L. Wong, The Aerospace Corporation	141
14	Frequency-Independent Antennas	14-1
	Raymond H. DuHamel, Antenna Consultant James P. Scherer, Loral Randtron Systems	
15	Horn Antennas	15-1
13	Allan W. Love, Rockwell International	15-1
16	Lens Antennas	16-1
10	Donald G. Bodnar, Georgia Institute of Technology	10-1
17	Reflector Antennas	17-1
1,	Kenneth S. Kelleher, Consultant	-,-
	Geoffrey Hyde, COMSAT Laboratories	
18	Electromechanical Scanning Antennas	18-1
	Kenneth S. Kelleher, Consultant	
19	Frequency-Scan Antennas	19-1
	James S. Ajioka, Hughes Aircraft Company	
20	Phased Arrays	20-1
	Raymond Tang and Richard W. Burns, Hughes Aircraft Company	
21	Conformal and Low-Profile Arrays	21-1
	Robert J. Mailloux, Rome Laboratory, Hanscom Air Force Base	
22	Adaptive Antennas	22-1
	Leon J. Ricardi, LJR, Inc.	
23	Methods of Polarization Synthesis	23-1
	Warren B. Offutt, W & B Observatory	
	Lorne K. DeSize, Consultant	
3	APPLICATIONS	
	AFFLICATIONS	
24	Low-Frequency Antennas	24-3
24	Boynton G. Hagaman, Kershner, Wright and Hagaman, P.C.	24-3
25	Medium-Frequency Broadcast Antennas	25-1
25	John A. Lundin and Ronald D. Rackley, du Treil, Lundin & Rackley, Inc.	25-1
26	High-Frequency Antennas	26-1
20	Ronald Wilensky, Technology for Communications International	20-1
27	VHF and UHF Communication Antennas	27-1
-,	Brian S. Collins, Radiation Systems International Ltd.	2,-1
28	TV and FM Transmitting Antennas	28-1
_0	Raymond H. DuHamel, Antenna Consultant	20 1
	Ali R. Mahnad, Jampro Antennas Inc.	
29	TV Receiving Antennas	29-1
	Edward B. Joy, Georgia Institute of Technology	
30	Microwave-Relay Antennas	30-1
	Charles M. Knop. Andrew Corporation	

31	Radiometer Antennas	31-1
	William F. Croswell, Harris Corporation Calvin T. Swift, University of Massachusetts	
32	Radar Antennas	32-1
	Paul E. Rawlinson, Raytheon Company Harold R. Ward, Consultant	
33	Microwave Beacon Antennas	33-1
	Phillip N. Richardson, Texas Instruments, Inc.	
34	Josh T. Nessmith, Georgia Institute of Technology	34-1
	Willard T. Patton, General Electric Company	
35		35-1
	Leon J. Ricardi, LJR, Inc.	
36	Earth Station Antennas	36-1
	James H. Cook, Jr., Scientific-Atlanta, Inc.	
37	Aircraft Antennas	37-1
	William P. Allen, Jr., Lockheed Aeronautical Systems Company Charles E. Ryan, Jr., Georgia Institute of Technology	
38	Seeker Antennas	38-1
	James M. Schuchardt, American Electronic Laboratories Dennis J. Kozakoff, Millimeter Wave Technology, Inc.	
39	Direction-Finding Antennas and Systems	39-1
	Hugh D. Kennedy and Roy B. Woolsey, Technology for Communications International	
40	ECM and ESM Antennas	40-1
	Daniel F. Yaw, Westinghouse Defense and Electronic Systems Vernon C. Sundberg, GTE Systems	
41	Radio-Telescope Antennas	41-1
	John D. Kraus, The Ohio State University	
4_	TOPICS ASSOCIATED WITH ANTENNAS	
42	Transmission Lines and Waveguides Roderic V. Lowman, Techni-Quest, Inc.	42-3
43	Impedance Matching and Broadbanding	42.1
	David F. Bowman, Antenna Consultant	43-1
44	Radomes	44.1
	Gene K. Huddleston, Martin Marietta Corporation Harold L. Bassett, Georgia Institute of Technology	44-1
45	Microwave Propagation	45 1
	Geoffrey Hyde, COMSAT Laboratories	45-1
46	Materials and Design Data	46 -
	Donald G. Bodnar, Georgia Institute of Technology	46-1

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Preface

THIRD EDITION

It has been more than three decades since Henry Jasik envisioned and edited the First Edition of the *Antenna Engineering Handbook*. During this time, many significant and far-reaching advances have been made in the field of antenna technology.

The Second Edition was published more than two decades after the First Edition, and it required many major revisions and additions. For example, it contained 15 new chapters to cover new subject areas.

Work on this Third Edition of the *Handbook* began 10 years after starting work on the Second Edition. Ten years is a long time given today's rapid advancements in antenna technology, so an update is welcome and beneficial.

This new edition again contains four major parts:

Introduction and Fundamentals Part 1 presents basic comments, defines parameters, and discusses fundamentals that are common to most antennas.

Types and Design Methods Part 2 presents the primary antenna types and design methods that currently are in use. Emphasis is on succinct descriptions, design data, and references.

Applications Part 3 discusses major applications of antennas. Emphasis is on how antennas are employed to meet electronic system requirements. Design methods which are unique to the applications are presented.

Topics Associated with Antennas Part 4 deals with topics that are closely related to antenna design. The topics are covered succinctly, but more detailed information can be found in the references.

Thanks are extended to the many publishers who have granted permission to use material from their publications. As was done in the previous editions, we have tried to credit all sources of information by references; any omissions are due to oversight rather than intent.

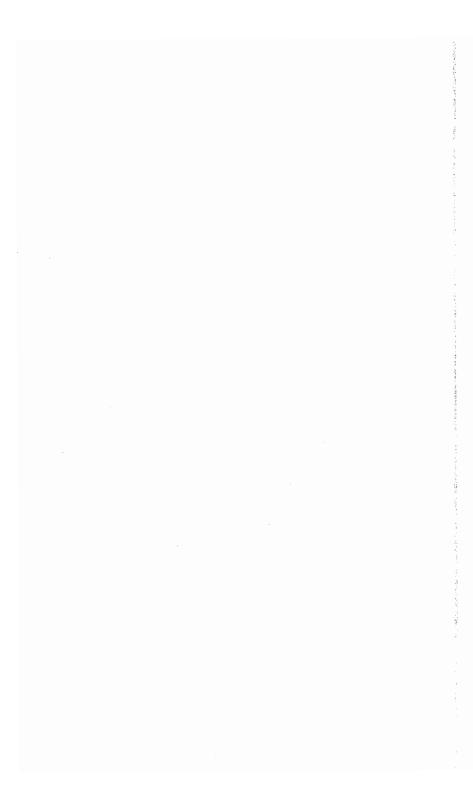
The work of many outstanding engineers who reviewed and updated the individual chapters has made this Third Edition of the *Handbook* possible. Their magnificent efforts enabled this project to be completed according to the initial schedule.

It is impossible to acknowledge all the other individuals who have made contributions to this book, so I thank them all as a group. Again, I extend special thanks to Maurice W. Long and J. Searcy Hollis, who introduced me to the fascinating world of antennas. Their keen insight and guidance helped me, in many cases, to "see" the electrical currents flowing on an antenna.

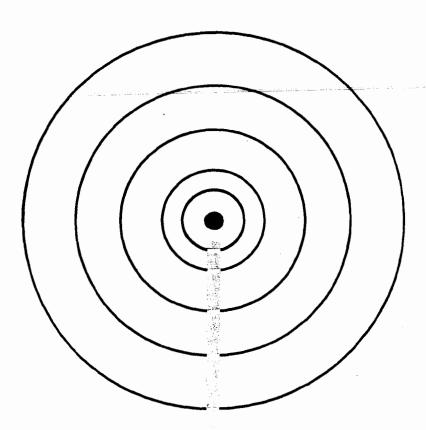
Finally, I want to acknowledge the lasting contributions of Henry Jasik, who conceived and edited the First Edition of this *Handbook*. When I took the assignment to edit the Second Edition, I considered several alternate ways to organize the subject matter; however, in the end, I concluded that Henry's outline was better than all the others. This *Handbook* is dedicated to the memory of Henry Jasik. His influence is clearly present in this Third Edition, and it probably will continue through future editions.

RICHARD C. JOHNSON

Antenna Engineering Handbook



Introduction and Fundamentals



A STANDARD TO SELECT THE SELECT SELECTION OF THE PERSON OF

Introduction to Antennas

Richard C. Johnson

Georgia Institute of Technology

- 1-1 Functions and Types 1-4
- 1-2 Basic Concepts and Definitions 1-4
- 1-3 Field Regions 1-9
- 1-4 Power Transfer 1-12
- 1-5 Radiation Patterns 1-13
- 1-6 Estimating Characteristics of High-Gain Antennas 1-15

1-1 FUNCTIONS AND TYPES

An antenna usually is defined as the structure associated with the region of transition between a guided wave and a "free-space" wave, or vice versa. The adjective free-space is in quotation marks because in practice there always is some interaction with the surroundings. On transmission, an antenna accepts energy from a transmission line and radiates it into space, and on reception, an antenna gathers energy from an incident wave and sends it down a transmission line.

When discussing an antenna, one usually describes its properties as a transmitting antenna. From the reciprocity theorem, however, we know that the directional pattern of a receiving antenna is identical with its directional pattern as a transmitting antenna, provided nonlinear or unilateral devices (such as some ferrite devices) are not employed. Thus, no distinction needs to be made between the transmitting and receiving functions of an antenna in the analysis of radiation characteristics. It should be pointed out, however, that the reciprocity theorem does not imply that antenna current distributions are the same on transmission as they are on reception.

A large variety of antennas have been developed to date; they range from simple structures such as monopoles and dipoles to complex structures such as phased arrays. The particular type of antenna selected for a certain application depends upon the system requirements (both electrical and mechanical) and, to a lesser extent, upon the experience of the antenna engineer.

1-2 BASIC CONCEPTS AND DEFINITIONS

Consider an antenna which is located at the origin of a spherical coordinate system as illustrated in Fig. 1-1. Suppose that we are making observations on a spherical shell having a very large radius r.

Assume that the antenna is transmitting, and let

- P_0 = power accepted by antenna, watts
- P_r = power radiated by antenna, watts
 - η = radiation efficiency, unitless

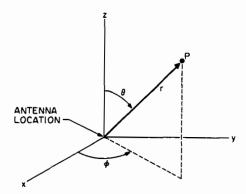


FIG. 1-1 An antenna in a spherical coordinate system.

The above quantities are related as follows:

$$\eta = \frac{P_r}{P_0} \tag{1-1}$$

Let

$$\Phi(\theta,\phi)$$
 = radiation intensity, watts/steradian

Note that since r was assumed to be very large, Φ is independent of r. This independent dence of r is a characteristic of the far-field region. The total power radiated from the antenna is

$$P_r = \int_0^{2\pi} \int_0^{\pi} \Phi(\theta, \phi) \sin \theta \ d\theta \ d\phi \tag{1-2}$$

and the average radiation intensity is

$$\Phi_{\text{avg}} = \frac{P_{\text{r}}}{4\pi} \tag{1-3}$$

Let

$$D(\theta, \phi) = \text{directivity, unitless}$$

Directivity is a measure of the ability of an antenna to concentrate radiated power in a particular direction, and it is related to the radiation intensity as follows:

$$D(\theta,\phi) = \frac{\Phi(\theta,\phi)}{\Phi_{\text{avg}}} = \frac{\Phi(\theta,\phi)}{P_r/4\pi}$$
 (1-4)

The directivity of an antenna is the ratio of the achieved radiation intensity in a particular direction to that of an isotropic antenna. In practice, one usually is interested primarily in the peak directivity of the main lobe. Thus, if one says that an antenna has a directivity of 100, it is assumed that 100 is the peak directivity of the main lobe. Let

$$G(\theta,\phi)$$
 = gain, unitless

The gain of an antenna is related to the directivity and power radiation intensity as

$$G(\theta,\phi) = \eta D(\theta,\phi)$$

$$= \frac{\eta \phi(\theta,\phi)}{P_r/4\pi}$$
(1-5)

and from Eq. (1-1),

$$G(\theta,\phi) = \frac{\Phi(\theta,\phi)}{P_0/4\pi}$$
 (1-6)

Thus, the gain is a measure of the ability to concentrate in a particular direction the power accepted by the antenna. Note that if one has a lossless antenna (i.e., $\eta = 1$), the directivity and the gain are identical. Let

$$P(\theta,\phi)$$
 = power density, watts/square meter

The power density is related to the radiation intensity as follows:

 $P(\theta,\phi) = \frac{\Phi(\theta,\phi) \ \Delta\theta \ \Delta\phi}{(r \ \Delta\theta)(r \ \Delta\phi)}$

or

$$P(\theta,\phi) = \frac{\Phi(\theta,\phi)}{r^2} \tag{1-7}$$

Substituting Eq. (1-6) into Eq. (1-7) yields

$$P(\theta,\phi) = G(\theta,\phi) \frac{P_0}{4\pi r^2}$$
 (1-8)

The factor $P_0/4\pi r^2$ represents the power density that would result if the power accepted by the antenna were radiated by a lossless isotropic antenna.

Let

$$A_{\epsilon}(\theta,\phi)$$
 = effective area, square meters

It is easier to visualize the concept of effective area when one considers a receiving antenna; it is a measure of the effective absorption area presented by an antenna to an incident plane wave. The effective area is related to gain and wavelength as follows:

$$A_{\epsilon}(\theta,\phi) = \frac{\lambda^2}{4\pi} G(\theta,\phi) \tag{1-9}$$

Many high-gain antennas such as horns, reflectors, and lenses are said to be aperture-type antennas. The aperture usually is taken to be that portion of a plane surface near the antenna, perpendicular to the direction of maximum radiation, through which most of the radiation flows. Let

- η_a = antenna efficiency of an aperture-type antenna, unitless
- A = physical area of antenna's aperture, square meters

Then,

$$\eta_a = \frac{A_e}{A} \tag{1-10}$$

The term η_a sometimes has been called aperture efficiency.

When dealing with aperture antennas, we see from Eqs. (1-9) and (1-10) that

$$G = \eta_d \frac{4\pi}{\lambda^2} A \tag{1-11}$$

The term η_a actually is the product of several factors, such as

$$\eta_a = \eta \eta_i \eta_1 \eta_2 \eta_3 \cdot \cdot \cdot \qquad (1-12)$$

The term η is radiation efficiency as defined in Eq. (1-1). The term η_i is aperture illumination efficiency (or antenna illumination efficiency), which is a measure of how well the aperture is utilized for collimating the radiated energy; it is the ratio of the directivity that is obtained to the standard directivity. The standard directivity is

obtained when the aperture is excited with a uniform, equiphase distribution. (Such a distribution yields the highest directivity of all equiphase excitations.) For planar apertures in which $A \gg \lambda^2$, the standard directivity is $4\pi A/\lambda^2$, with radiation confined to a half space.

The other factors, $\eta_1\eta_2\eta_3...$, include all other effects that reduce the gain of the antenna. Examples are spillover losses in reflector or lens antennas, phase-error losses due to surface errors on reflectors or random phase errors in phased-array elements, aperture blockage, depolarization losses, etc.

Polarization (see Refs. 2 and 3 for a more detailed discussion) is a property of a single-frequency electromagnetic wave; it describes the shape and orientation of the locus of the extremity of the field vectors as a function of time. In antenna engineering, we are interested primarily in the polarization properties of plane waves or of waves that can be considered to be planar over the local region of observation. For plane waves, we need only specify the polarization properties of the electric field vector since the magnetic field vector is simply related to the electric field vector.

The plane containing the electric and magnetic fields is called the *plane of polarization*, and it is orthogonal to the direction of propagation. In the general case, the tip of the electric field vector moves along an elliptical path in the plane of polarization. The polarization of the wave is specified by the shape and orientation of the ellipse and the direction in which the electric field vector traverses the ellipse.

The shape of the ellipse is specified by its axial ratio—the ratio of the major axis to the minor axis. The orientation is specified by the tilt angle—the angle between the major axis and a reference direction when viewed looking in the direction of propagation. The direction in which the electric field vector traverses the ellipse is the sense of polarization—right-handed or left-handed when viewed looking in the directions of propagation.

The polarization of an antenna in a specific direction is defined to be the polarization of the far-field wave radiated in that direction from the antenna. Usually, the polarization of an antenna remains relatively constant throughout the main lobe, but it varies considerably in the minor lobes.

It is convenient to define a spherical coordinate system associated with an antenna as illustrated in Fig. 1-2. The polarization ellipse for the direction (θ, ϕ) is shown inscribed on the spherical shell surrounding the antenna. It is common practice to choose \mathbf{u}_{ϕ} (the unit vector in the θ direction) as the reference direction. The tilt angle then is measured from \mathbf{u}_{ϕ} toward \mathbf{u}_{ϕ} . The sense of polarization is clockwise if the electric field vector traverses the ellipse from \mathbf{u}_{ϕ} toward \mathbf{u}_{ϕ} as viewed in the direction of propagation and counterclockwise if the reverse is true.

In many practical situations, such as antenna measurements, it is convenient to establish a local coordinate system. Usually, the u_3 axis is the direction of propagation, the u_1 axis is horizontal, and the u_2 axis is orthogonal to the other two so that the unit vectors are related by $\mathbf{u}_1 \mathbf{X} \mathbf{u}_2 = \mathbf{u}_3$. The tilt angle is measured from \mathbf{u}_1 .

When an antenna receives a wave from a particular direction, the response will be greatest if the polarization of the incident wave has the same axial ratio, the same sense of polarization, and the same spatial orientation as the polarization of the antenna in that direction. The situation is depicted in Fig. 1-3, where E_t represents a transmitted wave (antenna polarization) and E_m represents a matched incident wave. Note that the sense of polarization for E_t and that for E_m are the same when viewed in their local coordinate system. Also, note that the tilt angles are different because the directions of propagation are opposite. As depicted in Fig. 1-3, τ_t is the tilt angle

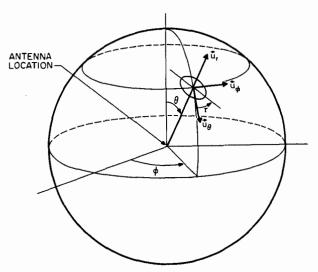


FIG. 1-2 Polarization ellipse in relation to antenna coordinate system. (After Ref. 2.)

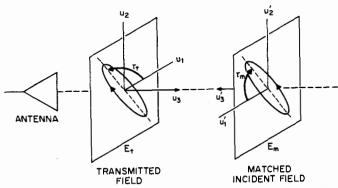


FIG. 1-3 Relation between polarization properties of an antenna when transmitting and receiving. (After Ref. 2.)

of the transmitted wave and τ_m is the tilt angle of the polarization-matched received wave; they are related by

$$\tau_m = 180^{\circ} - \tau_t$$
 (1-13)

The polarization of the matched incident wave, as described above, is called the receiving polarization of the antenna.

When the polarization of the incident wave is different from the receiving polarization of the antenna, then a loss due to polarization mismatch occurs. Let

 η_p = polarization efficiency, unitless

The polarization efficiency is the ratio of the power actually received by the antenna to the power that would be received if the polarization of the incident wave were matched to the receiving polarization of the antenna.

The Poincaré sphere, as shown in Fig. 1-4, is a convenient representation of polarization states. Each possible polarization state is represented by a unique point on the unit sphere. Latitude represents axial ratio, with the poles being circular polarizations; the upper hemisphere is for left-handed sense, and the lower hemisphere is for right-handed sense. Longitude represents tilt angles from 0 to 180°. An interesting feature of the Poincaré sphere is that diametrically opposite points represent orthogonal polarizations.

The Poincaré sphere also is convenient for representing polarization efficiency. In Fig. 1-5, W represents the polarization of an incident wave, and A_r represents the receiving polarization of the antenna. If the angular distance between the points is 2ξ , then the polarization efficiency is

$$\eta_p = \cos^2 \xi \tag{1-14}$$

1-3 FIELD REGIONS

The distribution of field strength about an antenna is, in general, a function of both the distance from the antenna and the angular coordinates. In the region close to the antenna, the field will include a reactive component. The strength of this reactive component, however, decays rapidly with distance from the antenna so that it soon

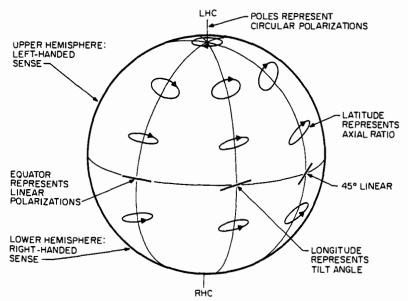


FIG. 1-4 Polarization states on the Poincaré sphere. (After Ref. 2.)

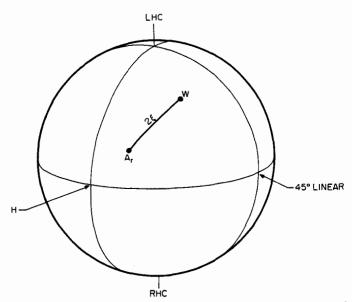


FIG. 1-5 Receiving polarization of an antenna A, and polarization of an incident wave W.

becomes insignificant compared with the strength of the radiating component. That region in space in which the reactive component of the field predominates is called the reactive near-field region, and beyond this region the radiating field predominates.

That region in which the radiating field predominates is further subdivided into the radiating near-field region and the radiating far-field region. In the radiating near-field region, the angular distribution of radiated energy is dependent on the distance from the antenna, whereas in the radiating far-field region the angular distribution of radiated energy is essentially independent of distance from the antenna.

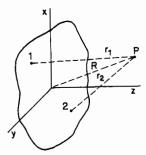


FIG. 1-6 Schematic representation of a planar-antenna aperture in the xy plane, an observation point P, and distances to the observation point from the origin and two elements of the antenna.

In the radiating near-field region. the relative phases and the relative amplitudes of contributions from various elements of the antenna are functions of the distance from the antenna. To visualize the situation refer to the schematic representation of Fig. 1-6. For simplicity, assume that the antenna is planar and is located in the xy plane; the distances to the observation point P from two arbitrary elements of the antenna are represented by \overline{r}_1 and r_2 . Notice that as the observation point is moved farther from the origin, in a fixed angular direction, the relative distance to the arbitrary elements $(r_2 \text{ minus } r_1)$ changes; this causes

the relative phases and amplitudes of contributions from elements 1 and 2 to change with distance from the antenna. By extending this argument to include all contributing elements of the antenna, one sees that the measured radiation pattern of the antenna will depend upon the radius to the observation point.

When the distance to the observation point gets very large, straight lines from any two contributing elements to the observation point $(r_1 \text{ and } r_2, \text{ for example, in Fig. 1-6})$ are essentially parallel and the relative distance to the elements $(r_2 \text{ minus } r_1)$ is essentially constant with changes in distance to the observation point. Thus, at large distances, the relative phases and amplitudes of contributions from the various elements change very slowly with distance, and the angular distribution of radiated energy measured at such large distances is essentially independent of the distances to the observation point. This condition is indicative of the radiating far-field region.

Thus, the space surrounding an antenna is composed of three regions: the reactive near-field region, the radiating near-field region, and the radiating far-field region. These three regions are shown pictorially in Fig. 1-7. The boundaries between

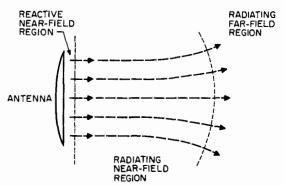


FIG. 1-7 Pictorial representation of the three regions surrounding an antenna.

the regions are not well defined, but for any antenna the reactive near-field region extends only a short distance.⁵ The commonly accepted distance to the boundary between the reactive and radiating near-field regions is $\lambda/2\pi$. For electrically large antennas of the aperture type, such as that depicted in Fig. 1-7, the commonly used criterion to define the distance to the boundary between the radiating near-field and far-field regions is⁶

$$R = \frac{2D^2}{\lambda} \tag{1-15}$$

where D is the largest dimension of the aperture and λ is the wavelength.

Although the aforementioned criterion to define distance to the far-field region is generally accepted and is used quite widely, one must always remember that it is an arbitrary choice and that it is inadequate for some special situations. For example, if one must accurately measure patterns of antennas having very low sidelobes or if one must make accurate gain measurements of pyramidal horns which have large phase deviations across their apertures, the measurement distance may have to be much longer than $2D^2/\lambda$.

Arguments have been advanced for decreasing or for increasing the accepted distance to the boundary between the near-field and far-field regions; however, $2D^2/\lambda$ seems to be the most popular choice. The situation is analogous to trying to decide the ideal height for a stepladder. Most of us might agree that 2 m is an ideal height, but there will be special jobs which require a higher ladder and other jobs in which a shorter ladder is acceptable and more convenient.

It has been customary in the past to refer to field regions as Fresnel or Fraunhofer, after the approximations described. As pointed out by Hansen,⁵ this practice should be discouraged. It is better to define field regions as reactive near field, radiating near field, and radiating far field as discussed earlier and illustrated in Fig. 1-7. Then, the terms Fresnel and Fraunhofer can be used more correctly to refer to analytical approximations.

1-4 POWER TRANSFER

Consider power that is transferred from a transmitting antenna to a receiving antenna; assume that the antennas are in free space and are separated by a large distance R (in the far field of each other).

The received power will be equal to the product of the power density of the incident wave and the effective aperture area of the receiving antenna; that is,

$$P_r = PA_e$$

Substituting from Eqs. (1-8) and (1-9),

 $P_r = \frac{G_t P_t}{4\pi R^2} \frac{\lambda^2 G_r}{4\pi}$

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$$P_r = \left(\frac{\lambda}{4\pi R}\right)^2 G_t G_r P_t \tag{1-16}$$

The subscripts r and t refer to the receiving and transmitting antennas, respectively. Note in the above case that G_t is the gain of the transmitting antenna in the direction of the receiving antenna and that G_r is the gain of the receiving antenna in the direction of the transmitting antenna. A form of this equation was presented first by Friis, and it usually is called the Friis transmission formula.

Similar arguments can be used to derive the radar equation. From Eq. (1-8), the power density at distance R from the antenna is

$$\frac{G_t P_t}{4\pi R^2}$$

The radar cross section σ of a target is a transfer function which relates incident power density and reflected power density. The term σ has units of area (e.g., m²), and one might think of the process as having the target intercepting the incident power density over an area σ and then reradiating the power isotropically. The return power density at the radar is then

$$\frac{G_t P_t}{4\pi R^2} \frac{\sigma}{4\pi R^2}$$

and the received power is

$$\frac{G_t P_t}{4\pi R^2} \frac{\sigma}{4\pi R^2} A_e$$

where A_e is the effective area (or capture area) of the receiving antenna. Using Eq. (1-9), the received power is

$$P_r = \frac{G_t P_t}{4\pi R^2} \frac{\sigma}{4\pi R^2} \frac{G_r \lambda^2}{4\pi}$$
 (1-17)

If the same antenna is used for both transmission and reception of energy, then $G_t = G_r = G$, and the received power may be written as

$$P_{r} = \frac{G^{2}\lambda^{2}\sigma}{(4\pi)^{3}R^{4}} P_{t}$$
 (1-18)

which is a simple form of the radar equation.

1-5 RADIATION PATTERNS

When the power radiation intensity $\Phi(\theta,\phi)$ and the power density $P(\theta,\phi)$ are presented on relative scales, they are identical and often are referred to as the *antenna radiation* pattern. The main (or major) lobe of the radiation pattern is in the direction of maximum gain; all other lobes are called sidelobes (or minor lobes).

There are many types of antenna radiation patterns, but the most common are the following:

- 1 Omnidirectional (azimuthal-plane) beam
- 2 Pencil beam
- 3 Fan beam
- 4 Shaped beam

The omnidirectional beam is most popular in communication and broadcast applications. The azimuthal pattern is circular, but the elevation pattern will have some directivity to increase the gain in the horizontal directions.

The term pencil beam is applied to a highly directive antenna pattern consisting of a major lobe contained within a cone of small solid angle. Usually the beam is circularly symmetric about the direction of peak intensity; however, even if it is slightly fanned, it often is still called a pencil beam. A radar pencil beam, for example, is analogous to an optical searchlight beam.

A fan beam is narrow in one direction and wide in the other. A typical use of a fan beam would be in search or surveillance radar in which the wide dimension of the beam would be vertical and the beam would be scanned in azimuth. Another use of a fan beam would be in a height-finding radar in which the wide dimension of the beam would be horizontal and the beam would be scanned in elevation.

There are a number of applications that impose beam-shaping requirements upon the antenna. One such application is in an air search radar that is located on the

ground or on a ship. The antenna for such an application is required to produce a narrow beam in azimuth and a shaped beam in elevation; azimuth coverage is obtained by scanning the beam.

The elevation shape of the beam must provide sufficient gain for detection of aircraft up to a certain altitude and angle of elevation and out to the maximum range of the system. To accomplish this without wasteful use of available power, the general shape of the coverage in the vertical plane should be as indicated in Fig. 1-8.

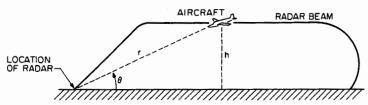


FIG. 1-8 Vertical beam shape (amplitude) of ground-based radar for detecting aircraft up to a certain altitude.

To maintain a fixed minimum of illumination on the aircraft at various points along the upper contour of the coverage diagram, it is necessary that the amplitude of the antenna pattern be proportional to the distance r from the antenna to the aircraft on the upper contour. In other words, the coverage contour of Fig. 1-8 can be taken to be the amplitude pattern of the antenna. Since $r = h \csc \theta$, the amplitude pattern must be proportional to $\csc \theta$, or the power pattern (or gain) must be proportional to $\csc^2 \theta$. Such proportionality must hold over the required coverage pattern; thus, such a pattern is said to have a \csc^2 shape.

In the case of a \csc^2 pattern, note that the gain is proportional to $\csc^2 \theta$ and the range is proportional to $\csc \theta$. Thus, we see from Eq. (1-18) that a target of constant cross section approaching at a constant altitude will produce a constant received-signal level.

Antenna radiation patterns are three-dimensional, but we have a need to describe them on two-dimensional paper. The most popular technique is to record signal levels along great-circle or conical cuts through the radiation pattern. In other words, one angular coordinate is held fixed, while the other is varied. A family of such two-dimensional patterns then can be used to describe the complete three-dimensional pattern.

Patterns usually are displayed as relative field, relative power, or logarithmic relative power versus angle on rectangular or polar diagrams. The rectangular diagram can easily be expanded along the angular axis by merely changing diagram speed relative to the angular rate of the antenna positioner; this is a big advantage when measuring patterns of narrow-beam antennas. Polar diagrams give one more realistic "pictures" of the radiation pattern, so they often are used for broad-beam antennas.

Another popular technique for displaying patterns is the *radiation distribution table*. In this type of display, signal levels are plotted in decibels at preselected intervals of the two angular coordinates, ϕ and θ . A contour appearance is obtained by printing only the even values of signal level and omitting the odd values.

With the advent of computers, a new type of "three-dimensional" pattern display

has become popular. The two orthogonal far-field angles are represented by the base of the display, and relative gain is represented by height above the base. Such pattern displays can be generated from either calculated or measured gain data.

1-6 ESTIMATING CHARACTERISTICS OF HIGH-GAIN ANTENNAS

There are many occasions when it is desirable to make quick estimates of the beamwidths and gains of aperture antennas. A convenient rule of thumb for predicting 3dB beamwidths is

$$BW_{3-dB} = k \frac{\lambda}{D}$$
 (1-19)

where k is a beamwidth constant, λ is the wavelength, and D is the aperture dimension in the plane of the pattern.

Most antenna engineers seem to use a value of $k=70^{\circ}$. This is adequate for most rough estimates; however, more accurate estimates must take into account the fact that the value of k depends upon the aperture illumination function. Generally speaking (but not always), illumination functions that yield lower sidelobes result in a larger value of k.

Komen⁸ reported on the variation of the beamwidth constant for reflector-type antennas. From computed patterns for various edge illuminations, he determined that

$$k = 1.05238I + 55.9486$$
 (1-20)

where I is the absolute value of edge illumination (including space attenuation) in decibels and k is in degrees. (In practice, one normally would calculate k to only a few significant figures.) By applying Eqs. (1-19) and (1-20) to measured data from several antennas, Komen concluded that the relationship between beamwidth and edge illumination holds regardless of frequency, reflector size, reflector type, or feed type.

The beamwidth constant and approximate sidelobe level versus edge illumination for reflector-type antennas are illustrated in Fig. 1-9. The beamwidth constants for antennas having one of several special aperture distributions are illustrated in Figs. 46-7 and 46-9 in Chap. 46.

A convenient rule of thumb for predicting gain (of a relatively lossless antenna) is

$$G = \frac{K}{\theta_1 \theta_2} \tag{1-21}$$

where K is a unitless constant and θ_1 and θ_2 are the 3-dB beamwidths (in degrees) in the two orthogonal principal planes. The correct value of K for an actual antenna depends on the antenna efficiency. A popular value used by many antenna engineers is 30,000, but many other values are in use. For example, Stutzman and Thiele¹⁰ suggest a value of 26,000, and Stegen¹¹ suggests a value of 35,000. One should subtract about $1\frac{1}{2}$ dB from the estimated gain for antennas with cosecant-squared-shaped beams.

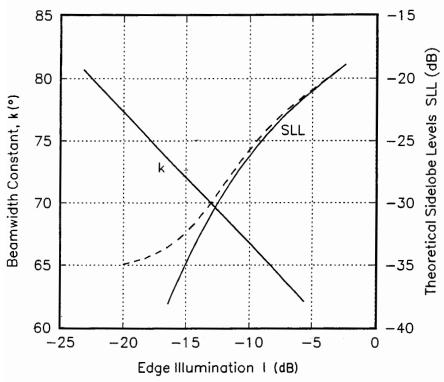


FIG. 1-9 Beamwidth constant and approximate first sidelobe level versus edge illumination (including space attenuation) for paraboloidal-reflector antennas. The SLL curve is solid for plane-wave feeds and dashed for feeds having parabolic primary patterns (dB versus angle).

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Fundamentals of Antennas *

Henry Jasik

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2-1	Radiation from Electric Current Elements 2-2
2-2	Radiation from Magnetic Current Elements 2-5
2-3	Antennas above Perfect Ground 2-7
2-4	Radiation from Apertures 2-8
	The Equivalence Principle 2-8
	Applications of the Equivalence Principle 2-10
2-5	Impedance Properties of Antennas 2-11
	Self-Impedance 2-11
	Mutual Impedance 2-13
2-6	Directivity Patterns from Continuous Line Sources 2-14
	Line-Source Distributions 2-15
2-7	Patterns from Area Distributions 2-19
	Rectangular Apertures 2-19
	Circular Apertures 2-19
	Elliptical Apertures 2-21
2-8	Effects of Phase Errors on Line Sources 2-21
2-9	Effects of Random Errors on Gain and Sidelobes 2-25
	Discrete-Element Arrays 2-27
	Continuous Apertures 2-31
	Periodic Errors in Aperture Illumination 2-32
2-10	Methods of Shaping Patterns 2-34
	Methods Useful for Linear Arrays 2-34
	Methods Useful for Reflector-Type Antennas 2-38
2-11	Gain Limitations for an Aperture of Specified Size 2-39
2-12	Scale Models of Antennas 2-40

^{*}This chapter was written by the late Henry Jasik for the first edition; it has been shortened and edited slightly by Richard C. Johnson for inclusion in this edition.

2-1 RADIATION FROM ELECTRIC CURRENT ELEMENTS

One of the types of radiators frequently used in antenna practice is some form of thin wire arranged in a linear configuration. If the current distribution on such a wire is known or can be assumed with a reasonable degree of accuracy, then the radiation pattern and the radiated power can be computed. This computation is based on the integration of the effects due to each differential element of the current along the wire. It is therefore of interest to set down the complete expressions for the fields at any distance due to a differential element of current oriented along the z axis as shown in Fig. 2-1. The rms electric and magnetic field components are given as follows:

$$E_r = 60\beta^2 I \, dz \left[\frac{1}{(\beta r)^2} - \frac{j}{(\beta r)^3} \right] \cos \theta \, e^{-j\beta r}$$

$$E_\theta = j30\beta^2 I \, dz \left[\frac{1}{\beta r} - \frac{j}{(\beta r)^2} - \frac{1}{(\beta r)^3} \right] \sin \theta \, e^{-j\beta r}$$

$$H_\phi = j \frac{\beta^2}{4\pi} I \, dz \left[\frac{1}{\beta r} - \frac{j}{(\beta r)^2} \right] \sin \theta \, e^{-j\beta r}$$

$$E_\phi = H_r = H_\theta = 0$$

where I dz = moment of differential current element (I is given in rms amperes and dz is given in meters.)

r =distance, m, to observation point

 $\beta = 2\pi/\lambda$

 λ = wavelength, m

 $j = \sqrt{-1}$

E is given in volts per meter

H is given in amperes per meter

A time factor of e^{jot} has been omitted, since for all the cases in which we are interested it is assumed that we have a sinusoidally time-varying current of constant frequency.

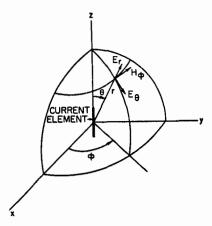


FIG. 2-1 Coordinate system for an electric dipole.

For most problems of interest it is only necessary to know the components in the far field, i.e., when r is very much greater than the wavelength. Under these conditions, the field components are simply given by

$$E_{\theta} = j \frac{30\beta I}{r} \frac{dz}{r} \sin \theta \ e^{-j\beta r}$$
$$= j \frac{60\pi I}{r\lambda} \frac{dz}{r\lambda} \sin \theta \ e^{-j\beta r}$$
$$H_{\phi} = j \frac{\beta I}{4\pi r} \frac{dz}{\sin \theta} \sin \theta \ e^{-j\beta r}$$
$$= \frac{E_{\theta}}{120\pi}$$

These expressions apply only for a very short element of current having a constant value along its length. However, they may readily be used to determine the field from any wire having a known current distribution by integrating the field due to each of the differential current elements along the length of the antenna. Taking into account the variation of current and the phase differential due to the varying distance from the observation point to each current element, the general expression for the field of any current distribution becomes

$$E_{\theta} = j \frac{60\pi \sin \theta}{r\lambda} \int_{-\epsilon/2}^{\epsilon/2} I(z) dz e^{-j\beta r(z)}$$

where both I(z) and r(z) are now functions of z and the integration takes place along the length of the antenna from $-\ell/2$ to $+\ell/2$.

For very short antennas, the above expression can be simplified to

$$E_{\theta} = j \frac{60\pi \sin \theta}{r\lambda} I_0 L_{\theta} e^{-j\beta r}$$

where I_0 = current at center of antenna

 L_e = effective length of antenna defined as

$$L_{\epsilon} = \frac{1}{I_0} \int_{-\epsilon/2}^{\epsilon/2} I(z) \ dz$$

The effective length is of interest in determining the open-circuit voltage at the terminals of a receiving antenna. It is also used on occasion to indicate the effectiveness of a transmitting antenna.

For a short top-loaded linear antenna which has uniform current distribution as shown in Fig. 2-2a, the effective length is simply equal to the physical length. For a short antenna which is much less than a half wave long, as shown in Fig. 2-2b, the current distribution is essentially triangular and its effective length is one-half of its physical length.

For antennas with an overall length greater than about a quarter wavelength, the variation of the phase term cannot be neglected and the integral must be evaluated by taking this term into account. The method will be very briefly illustrated for the case of a thin half-wave radiator which can be assumed to have a sinusoidal current

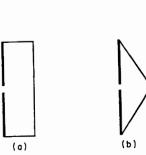


FIG. 2-2 Current distribution on a short linear antenna. (a) With top loading. (b) Without top loading.

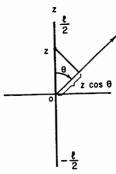


FIG. 2-3 Coordinates for computing radiation from a half-wave dipole.

distribution so that I(z) is given by $I_0 \cos \beta z$. The geometry for finding r(z) is shown in Fig. 2-3, from which it is readily seen that

$$r(z) = r - z \cos \theta$$

The field for a half-wave dipole is then given by

$$E_{\theta} = j \frac{60\pi \sin \theta}{r\lambda} I_0 e^{-j\beta r} \int_{-\ell/2}^{\ell/2} \cos \beta z \ e^{j\beta z \cos \theta} \ dz$$

which reduces to

$$E_{\theta} = j \frac{60I_0}{r} e^{-j\beta r} \frac{\cos\left(\frac{\pi}{2}\cos\theta\right)}{\sin\theta}$$

The relative-radiation pattern for a half-wave antenna is shown in solid lines in Fig. 2-4. For comparison purposes, the relative-radiation pattern of a very short dipole is shown in dotted lines. The patterns shown are those in a plane which contains the axis for the antenna. The pattern in the plane perpendicular to the antenna is perfectly circular because of symmetry.

There are a number of other properties for the half-wave dipole which are of considerable interest, such as radiation resistance, gain, and input impedance. These properties are discussed in Chap. 4.

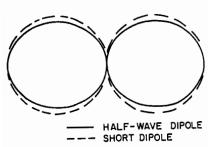


FIG. 2-4 Radiation patterns.

The method of computing radiation patterns for thin linear radiators is basic regardless of the length or complexity of shape. As a matter of interest, the following formula gives the radiated field from a center-fed thin wire of arbitrary length ℓ with an assumed sinusoidal current distribution:

$$E_{\theta} = j \frac{60I_0 e^{-j\beta r}}{r} \frac{\cos\left(\frac{\beta \ell}{2}\cos\theta\right) - \cos\frac{\beta \ell}{2}}{\sin\theta}$$

It will be noted that the radiated field perpendicular to the antenna continues to increase as the length is increased until the overall length is about 1½ wavelengths. Beyond this point the field starts falling off. When the overall length is two wavelengths, the field is zero normal to the axis of the antenna. For this length, the radiation pattern has broken up into two major lobes which are directed off the normal to the antenna. For a still longer length the antenna pattern will continue to break up into a large number of lobes whose positions depend on overall length of the antenna (Chaps. 4 and 11).

2-2 RADIATION FROM MAGNETIC CURRENT ELEMENTS

Another basic radiator which is frequently used in antenna practice is a magnetic current element. Although magnetic currents do not exist in nature, a number of configurations produce fields identical with those which would be produced by a fictitious magnetic current. For instance, a circular loop carrying electric current whose diameter is very small in terms of wavelengths will produce fields which are equivalent to those of a short magnetic dipole. The fields for any distance are given by the following expressions:

$$E_{\phi} = 30\beta^{3} dm \left[\frac{1}{\beta r} - \frac{j}{(\beta r)^{2}} \right] \sin \theta \ e^{-j\beta r}$$

$$H_{r} = \frac{\beta^{3}}{2\pi} dm \left[\frac{j}{(\beta r)^{2}} + \frac{1}{(\beta r)^{3}} \right] \cos \theta \ e^{-j\beta r}$$

$$H_{\theta} = -\frac{\beta^{3}}{4\pi} dm \left[\frac{1}{\beta r} - \frac{j}{(\beta r)^{2}} - \frac{1}{(\beta r)^{3}} \right] \sin \theta \ e^{-j\beta r}$$

$$E_{r} = E_{\phi} = H_{\phi} = 0$$

where the coordinate system is as shown in Fig. 2-5, and dm is defined as the differential magnetic dipole moment. For a small-diameter loop, the magnetic moment of the loop is equal to the electric current I flowing through the loop times its area A.

For the far field, when r is very much greater than the wavelength, the field components reduce to

$$E_{\phi} = \frac{30\beta^2 dm}{r} \sin \theta \ e^{-j\beta r}$$

$$H_{\theta} = -\frac{\beta^2 dm}{4\pi r} \sin \theta \ e^{-j\beta r}$$

$$= -\frac{E_{\phi}}{120\pi}$$

It will be noted that the field expressions for the magnetic current element are almost exactly analogous to those for the electric current element except for the interchange of electric and magnetic quantities. The radiation of a short magnetic dipole or a small-diameter loop is also a doughnut pattern, as in the case of an electric dipole. For a small loop the radiation pattern in the plane of a loop is perfectly circular, while

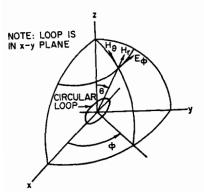


FIG. 2-5 Coordinate system for a magnetic dipole.

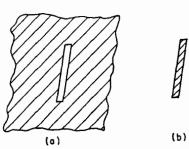


FIG. 2-6 (a) Thin slot in ground plane. (b) Complementary dipole.

the pattern in the plane through the axis of the loop is a figure of eight whose amplitude is proportional to $\sin \theta$. The expressions given are accurate for loop diameters which are considerably less than one-tenth wavelength. As a matter of fact, for very small loops, the radiation pattern does not depend on the exact shape of the loop, which may be square, rectangular, or some other shape, provided the overall circumference remains much less than a quarter wavelength.

For loops whose diameter is of the order of the wavelength, the radiation pattern can deviate considerably from the doughnut form, depending on the nature of the current distribution along the loop and diameter of the loop. These considerations are treated in Chap. 5.

Another antenna whose radiation characteristics are essentially similar to those of a magnetic dipole consists of a very thin slot in an infinitely large metallic ground plane, as shown in Fig. 2-6a. For this type of antenna, the electric field is applied across the narrow dimension of the slot. It is possible to show that the field radiated by this slot is exactly the same as would be radiated by a fictitious magnetic dipole with a magnetic current distribution M which is numerically equal to the distribution of electric voltage V across the slot. Thus the radiation pattern of a thin rectangular slot is identical with the radiation pattern of the complementary electric dipole which would just fill the slot, as shown in Fig. 2-6b. The only difference between the two types of radiators is the fact that the electric and magnetic quantities have been interchanged. This complementary relationship has been treated in considerable length in technical literature and will not be elaborated on in this section.

It is pertinent to point out a few precautions concerning the application of these complementary relationships. For one thing, the complementary relationship is based on the assumption that only electric field exists within the slot and that no magnetic field is present. This is true only for vanishingly thin slots. For slots whose width is appreciable in comparison with their length, the above assumption is no longer valid and the radiation pattern will be somewhat modified as compared with the case of the very thin slot. Another assumption on which the complementary relationship is based is that the size of the conducting ground plane is infinitely large. This, of course, is never true in practice, and for finite ground planes the size of the ground plane may exert a large influence on the radiation pattern, particularly at angles close to the

plane of the sheet. Even for sheets which are fairly large in terms of wavelength, there are some minor modifications of radiation pattern.

It might also be mentioned that the complementary relationship holds only when the slot is cut in a large flat ground sheet. For slots cut in circular cylinders, the pattern can be considerably different from that predicted by the complementary relationship, particularly in the plane perpendicular to the axis of the cylinder. However, use of the complementary relationship is still very useful to engineers as an intuitive guide, and while in many cases the results will not be exact, they will certainly give a first approximation to the actual radiation pattern.

2-3 ANTENNAS ABOVE PERFECT GROUND

The characteristics of antennas operating near ground level will be modified by the effect of ground reflections. This is particularly true of antennas operating at frequencies below 30 MHz when the height of the antenna above ground may be less than one or two wavelengths. For airborne antennas or for large-aperture, narrow-beam antennas, in which the main beam is elevated upward at least several beamwidths, the ground may play a relatively small role. In all cases, the ground will play a part in the propagation between transmitter and receiver, and to compute its effect the characteristics of the ground and the geometry of the propagation path, as well as the pattern characteristics of the receiving and transmitting antennas, must be known.

For antennas at relatively small heights above ground, the ground is a basic part of the antenna system and will affect not only the radiation pattern of the antenna but also its impedance properties. To obtain a first-order estimate of the effect of ground, simple image theory can be applied to the case of a perfectly conducting ground surface. It is well known from electromagnetic theory that the tangential field on a perfect conductor must be zero and that the electric field must be normal to the conducting surface. To satisfy this requirement, a conducting charge above a conducting plane will induce a charge distribution on the plane exactly equivalent to that which would be produced by an equal charge of the opposite sign at the same distance below the plane, as shown in Fig. 2-7a. Since current is a movement of charge, it is readily possible to deduce the direction of the images for vertical, horizontal, and inclined wires above ground, as shown in Fig. 2-7b-d. The image for any other configuration can readily be determined by using the rule that vertical components are in the same direction while horizontal components are in opposite directions.

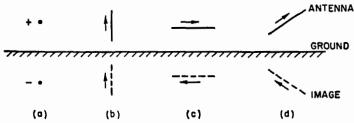


FIG. 2-7 Images above a perfectly conducting ground plane. (a) Point charge. (b) Vertical wire. (c) Horizontal wire. (d) Inclined wire.

The field in any direction above the ground plane can easily be determined by replacing the ground plane by the image and computing the resulting field due to the antenna plus its image. This is valid above the ground plane, since for a perfect conductor the field below the ground plane is zero.

Although the above method is rigorously true only for antennas above highly conducting ground, it does give good results in many cases of interest. The same technique can be used when the ground has arbitrary values of conductivity and dielectric constant by assuming an image current which is related to the antenna current by the ratio of the complex-reflection coefficient for the appropriate angle of incidence.

The effect of the ground on the impedance of an antenna can also be determined by image theory. For instance, the input impedance of an antenna above perfectly conducting ground is simply the input impedance of the antenna in free space plus the mutual impedance due to the image antenna. For arbitrary ground, the same sort of relation is still true except that the mutual impedance due to the image must be multiplied by the complex-ground-reflection coefficient for normal incidence.

A special case of considerable interest occurs when one end of the antenna above ground is exactly one-half of the input impedance of the antenna plus its image when driven in free space. For example, the input impedance of a quarter-wave dipole above ground is exactly one-half that of a half-wave dipole in free space.

2-4 RADIATION FROM APERTURES

The computation of radiation patterns for linear-wire antennas is relatively simple if the current distribution on the wire is known. The current distribution is not usually known exactly except for a few special cases. However, physical intuition or experimental measurement can often provide a reasonable approximation to the current distribution, and for many engineering purposes a sufficiently accurate result can be obtained. In theory, of course, an exact result can be derived from a boundary-value solution if the nature of the exciting sources is known. From a practical point of view, the amount of labor involved in obtaining numerical results is excessive even for those cases in which the geometry is relatively simple and a rigorous solution can be expressed in terms of a series of tabulated functions. It is therefore necessary in many situations to be able to compute the radiation pattern by alternative methods based on a reasonable assumption of the nature of the electromagnetic fields existing in the vicinity of an antenna structure.

The Equivalence Principle

One powerful technique for simplifying this type of computation makes use of an equivalence principle given by Schelkunoff.^{1,2} Briefly stated, this principle supposes that a given distribution of electric and magnetic fields exists on a closed surface drawn about the antenna structure. These fields are then canceled by placing a suitable distribution of electric and magnetic current sheets on the closed surface so that the fields inside the closed surface are zero. The radiation is then computed from the electric and magnetic current sheets and, except for a difference in sign, is identical to the radiation which would have been produced by the original sources inside the closed surface. It will be noted that this principle is essentially a more rigorous for-

mulation of Huygens' principle. If the fields on the closed surface are known exactly, then the resulting computation is also exact. The degree of approximation which can be obtained by this technique depends only on how accurately the fields across the closed surface may be estimated.

When the electric and magnetic field strengths are respectively given by E and H, then the equivalent densities are given by

Electric current density:

 $J = n \times H$

Magnetic current density:

 $M = -n \times E$

where both J and H are expressed in amperes per meter and M and E are expressed in volts per meter.

The vector cross product has been used to show that the electric current is perpendicular to direction of propagation and to the magnetic field vector. If the initial E and H fields are as shown in Fig. 2-8a, then the resulting electric and magnetic currents are directed as shown in Fig. 2-8b.

One way of visualizing the effect of a small portion of the wavefront is to consider the physical equivalent of the electric and magnetic current sheets. The electric current is equivalent to a short electric dipole, while the magnetic current is equivalent to a short magnetic dipole or a small electric current loop, as was discussed in Sec. 2-

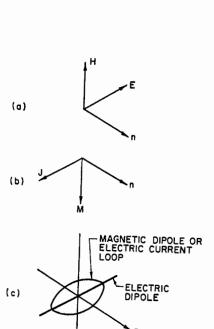
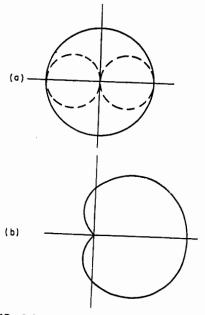


FIG. 2-8 Current sheet relations. (a) Initial E and H fields. (b) Resulting electric and magnetic currents. (c) Orientation of electric dipole and electric current loop.



2-10

2. The electric dipole is oriented in the direction of the electric field E, while the electric current loop is located in the plane defined by the electric field E and the direction of propagation n, as shown in Fig. 2-8 c.

If we look at the radiation pattern in the plane of the loop, the component due to the electric dipole will have a $\cos \theta$ type of variation while the component due to

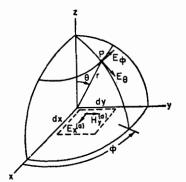


FIG. 2-10 Coordinates for current sheet computation.

of variation while the component due to the electric current loop will have a circular pattern as shown in Fig. 2-9a. For a portion of wavefront in free space in which the E and H fields are related as

$$E = 120\pi H$$

the relative amplitudes of the two components will be such that the radiation pattern of the combination is given by $(1 + \cos \theta)$ or a cardioid pattern as shown in Fig. 2-9b.

Although the concept of the electric and magnetic current sheets is most useful for derivation purposes and for obtaining a physical picture of radiation from apertures, it is possible to compute the reradiated field from an aperture directly in terms of the tangential electric

and magnetic field components in the aperture itself. With reference to Fig. 2-10, the aperture lies in the xy plane with field components $E_x^{(a)}$ and $H_y^{(a)}$. At a distant point P, the radiation components of the electric field are given by

$$E_{\theta} = -j[E_x^{(a)} + 120\pi H_y^{(a)} \cos \theta] \frac{\cos \phi}{2\lambda r} dx dy e^{-j\theta r}$$

$$E_{\phi} = + j [E_x^{(a)} \cos \theta + 120\pi H_y^{(a)}] \frac{\sin \phi}{2\lambda r} dx dy e^{-j\theta r}$$

The above is true for an aperture in which $E_x^{(a)}$ and $H_y^{(a)}$ take on arbitrary values. An important special case is that in which the field components are the same as exist in a free-space plane wave. For this case

$$E_x^{(a)} = 120\pi H_y^{(a)}$$

and the distant fields are now given by

$$E_{\theta} = -jE_{x}^{(a)}(1 + \cos\theta) \frac{\cos\phi}{2\lambda r} dx dy e^{-j\theta r}$$

$$E_{\phi} = jE_{x}^{(a)}(1 + \cos\theta) \frac{\sin\phi}{2\lambda r} dx dy e^{-j\theta r}$$

Applications of the Equivalence Principle

One typical application of these results is to the problem of determining the radiation patterns from an electromagnetic horn.³ The tangential fields at the aperture of such a horn can be approximated by assuming that the fields at the aperture plane are the

same as would be obtained if the guiding surfaces of the horn were extended to infinity. Although not exact, this assumption is quite good when both linear dimensions of the aperture are greater than one or two wavelengths. After this assumption of the electric and magnetic fields at the aperture, the far-field relationships are then formulated by taking the fields across the aperture and integrating over the aperture, taking into account the amplitude and phase variations of the field incident on the aperture and the phase differential due to the varying distance from the observation point to each area element of the aperture.

The above method gives results which are good to a high degree of approximation, particularly for large-aperture horns. The equivalence principle can also be used with small-aperture horns, but caution must be exercised with regard to the assumptions of the relative values of electric and magnetic field strengths. In small horns, it is not true that the aperture fields are those which would exist if the waveguide were extended to infinity. For instance, in a waveguide radiator whose *E*-plane width is small, the field at the aperture will be predominantly electric and the magnetic field may be quite small. For this condition, the equivalent current sheet will consist mainly of magnetic current, and for a small aperture this will have a substantial effect on the radiation pattern, particularly in the *E* plane. For those cases in which it is possible to measure the standing waves in the waveguide leading to the aperture, it is possible to estimate the relative values of electric and magnetic field strength at the aperture and to make a first-order correction to the radiation-pattern computation.

The equivalence principle can also be used to determine the radiation from the open end of a coaxial line. For this case, the field at the aperture is predominantly electric, with only a small component of magnetic field. The field variation in the aperture is assumed to be that of the dominant mode in the coaxial line. The problem is readily formulated in cylindrical coordinates.⁴

Another problem which can be solved by using the equivalent-current-sheet method is the case of reflection from a conducting sheet such as paraboloidal reflector or a plane reflector as employed in microwave relay applications. To formulate this problem, the tangential fields that would have existed if the reflector were not present are determined by using only the magnetic field term for the aperture field and integrating over the surface, taking into account variations of the aperture field amplitude and phase and the phase differential to the observation point.

2-5 IMPEDANCE PROPERTIES OF ANTENNAS

Seif-Impedance

The input impedance of an antenna is a characteristic of considerable interest to engineers since they are concerned with the problem of supplying the antenna with the maximum amount of transmitter power available or in abstracting the maximum amount of received energy available from the antenna. Except for the simplest types of antenna configuration, the theoretical computation of the input impedance is an extremely arduous task, and for a large number of antenna types it is usually easiest to make a direct experimental measurement of the input impedance. However, for linear antennas which are relatively small in size, it is possible to make some reasonably good estimates as to the magnitude of the input resistance. It is also possible to assess, with a reasonable degree of accuracy, the mutual impedance between linear

radiators for the purpose of estimating the input impedance of an individual element in an array of radiators.

In most practical cases, the input impedance of even a simple antenna is affected to a considerable degree by the terminal conditions at the point where the transmission line feeds the radiator. For most accurate results, it is therefore necessary to measure the various impedances involved and to use the calculated values primarily as a guide during the design procedure.

For very short wire dipoles, the radiation resistance is a quantity which is closely allied with the resistive component of the input impedance. The radiation resistance is normally defined as the ratio of the total power radiated by an antenna divided by the square of the effective antenna current referred to a specified point. For short antennas this is a useful quantity because it enables one to estimate the overall radiation efficiency of the antenna by separating the radiation component of the input resistance from the loss resistance due to the ground system or the loss resistance due to the impedance-matching elements.

To compute the radiation resistance, it is necessary to know the radiation field pattern of the antenna in terms of the current flowing at the point to which the radiation resistance is referred. The total radiated power is then computed by integrating the total power density passing through a sphere surrounding the antenna. This computation will be carried through very briefly for the case of a very short dipole having an effective length L_{ϵ} and carrying a current I_0 . The electric field intensity for this antenna is given in Sec. 2-1 as

$$|E_{\theta}| = \frac{60\pi I_0 L_e}{r\lambda} \sin \theta$$

The power density in the far field is given by the Poynting vector, which is equal to $E_{\theta}^{2}/120\pi$, where the electric field is given in rms volts per meter and the power density is expressed in watts per square meter. Integrating over a large sphere surrounding the antenna, we then obtain

$$P = \int_0^{\pi} \frac{E_{\theta}^2}{120\pi} 2\pi r^2 \sin \theta \ d\theta$$
$$= \frac{80\pi^2 I_0^2 L_{\theta}^2}{\lambda^2}$$

Dividing this result by I_0^2 , we obtain

$$R_e = 80\pi^2 \frac{L_e^2}{\lambda^2}$$

where R_{ϵ} is a radiation resistance in ohms. It will be noted that the important variable is the ratio of the effective length L_{ϵ} to the wavelength and that the larger this ratio the greater the radiation resistance. Thus for a short antenna of physical length ℓ which is top-loaded so as to give a uniform current distribution, the effective length will be equal to the physical length and the radiation resistance will be $80\pi^2\ell^2/\lambda^2$. For an antenna with no top loading, the current distribution will be triangular (Sec. 2-1), and the effective length will be equal to one-half of the physical length, so that the radiation resistance will be $20\pi^2\ell^2/\lambda^2$. It can be seen that the radiation resistance for the uniform-current case is thus equal to 4 times that obtained in the case of triangular

current distribution, despite the fact that the radiation pattern and directivity are the same for both antennas since their length is small with respect to the wavelength.

The problem of computing the input impedance of a dipole of finite diameter whose length is of the order of a half wavelength is one that has been considered at great length by a number of writers. The subject is treated in detail in Chap. 4, where a considerable amount of measured data is presented.

For the case of a very thin half-wave dipole, the input resistance may be computed by assuming a sinusoidal current distribution and integrating the total power radiated over the surface of a large sphere, in the same fashion as just described for the short current element. Using the far field for the half-wave dipole as given in Sec. 2-1 and performing the appropriate operations, the input resistance of the half-wave thin dipole is found to be 73.1 Ω . The reactive component of the input impedance cannot be determined by the far-field method since the reactance is governed primarily by the electromagnetic fields in the vicinity of the antenna itself. The input reactance is also a function of the relative diameter of the dipole and of the terminal conditions at the driving point.

Mutual Impedance

In an array of antennas, the driving-point impedance of an individual element may differ considerably from its self-impedance because of the effect of mutual coupling with other elements of the array. In a multielement array, the relations between the currents and voltages are given by

$$V_{1} = I_{1}Z_{11} + I_{2}Z_{12} + \cdots + I_{n}Z_{1n}$$

$$V_{2} = I_{1}Z_{12} + I_{2}Z_{22} + \cdots + I_{n}Z_{2n}$$

$$\vdots \qquad \vdots \qquad \vdots$$

$$\vdots \qquad \vdots \qquad \vdots$$

$$V_{n} = I_{1}Z_{1n} + I_{2}Z_{2n} + \cdots + I_{n}Z_{nn}$$

where V_n = impressed voltage at nth element

 I_n = current flowing in nth element

 Z_{nn} = self-impedance of *n*th element

 $Z_{mn} = Z_{nm}$ = mutual impedance between mth and nth elements

The driving-point impedance for element 1, for instance, is found from the ratio of the impressed voltage to the current and is obtained from the above equations as

$$Z_{\text{linput}} = \frac{V_1}{I_1} = Z_{11} + \frac{I_2}{I_1} Z_{12} + \cdots + \frac{I_n}{I_1} Z_{1n}$$

It is readily seen that the input impedance or driving-point impedance of a particular element is not only a function of its own self-impedance but also a function of the relative currents flowing in the other elements and of the mutual impedance between elements. In an array in which the current distribution in the elements is critical because of pattern requirements, it is necessary to determine the input impedance from the above relationship and to design the transmission-line coupling system to match the input impedance rather than the self-impedance. Some examples of this are given in Ref. 6.

An alternative method for accurately controlling the current distribution in certain types of arrays is to use a transmission-line distribution system which forces the required current to flow in an antenna element regardless of the effect of mutual impedance. For instance, the constant-current properties of a quarter-wave line are such that the current in a load at the end of a quarter-wave line is equal to the driving voltage divided by the characteristic impedance of the quarter-wave line regardless of the load impedance. This property is also true for a line whose length is an odd number of quarter wavelengths. Thus, for example, in order to feed an array of four dipole elements with exactly equal currents regardless of mutual coupling, the length of transmission line from the dipole to the junction would be an odd number of quarter wavelengths. By making use of the constant-voltage properties of a half-wavelength transmission line, it is possible to build up a distribution system to feed a large number of antenna elements by means of combinations of half-wave and quarter-wave lines. It is worth mentioning that although the uniform half-wave line behaves as a voltage transformer with a transformation ratio of 1, it is possible to obtain other transformation ratios by constructing the half-wave line of two quarter-wave sections of differing characteristic impedances.

In many situations it is not possible to sidestep the effects of mutual coupling and it is necessary to have a reasonably accurate estimate of the value of mutual impedance between antenna elements. It is possible to calculate the mutual impedance for very thin dipoles, and the results are given in Chap. 4 for several cases of interest. Although the finite diameter of a dipole does have some effect on the magnitude of the mutual impedance, the effect is a second-order one and for many computations may be neglected. This is not true for self-impedance, whose value is very definitely a function of the dipole diameter.

For antenna elements other than the simple dipole or slot radiator, little theoretical work is available on the magnitude of mutual-coupling effects and it is necessary to use experimental methods for determining the mutual impedance. Even in the case of dipole elements, it is frequently desirable to measure the mutual impedance, particularly for a dipole whose diameter is not small compared with its length.

Several experimental methods are available. When the antenna elements are identical and reasonably small physically, one simple method is to measure the input impedance when the element is isolated and then to repeat the measurement when a ground plane is placed near the element to simulate the effect of an image. The difference between the two impedance measurements is the mutual impedance for a distance corresponding to the distance between the driven element and its image. An alternative method when two elements are available is to measure the input impedance when one element is isolated, and then to repeat the measurement when the second element is in place and has a short circuit across its terminals.

2-6 DIRECTIVITY PATTERNS FROM CONTINUOUS LINE SOURCES

For antenna systems that have apertures which are very large in terms of wavelength, it is frequently desirable to use a continuous type of aperture distribution because of the relative simplicity, as compared with a discrete-element type of array which requires a large number of driven elements. For instance, a common form of large-

aperture antenna is a paraboloidal reflector illuminated by a point-source feed. To replace an aperture of the order of 100 wavelengths in diameter by a discrete-element array would require more than 5000 individual radiating elements, each of which must be fed with current of the correct amplitude and phase.

For very large apertures it is apparent that a reflector type of antenna is considerably simpler than a discrete-element array. In addition, the reflector can be made to operate over a wide range of frequency simply by changing the feed, while a discrete-element array can operate efficiently only over a small bandwidth, on the order of 15 to 40 percent at most. Where very low sidelobe levels are required, discrete arrays have a substantial advantage over reflector-type structures since it is possible to obtain sidelobe levels of 40 dB down and greater by exercising considerable care in designing and constructing discrete-element arrays. By comparison, reflector-type antenna systems have sidelobe levels in the range of 18 to 25 dB down, and at the present state of the art it seems unlikely that sidelobe levels much lower than 35 dB down can be achieved with a reflector system. Use of a two-dimensional folded reflector system will offer some improvement because of the elimination of blocking by the feed and its supports, but even for this type of structure special techniques are necessary to achieve sidelobe levels lower than 30 dB down.

Although the continuous-aperture type of antenna has practical limitations with regard to very low sidelobe performance, it nevertheless is widely used because of its relative simplicity. For this reason, it is desirable to know what can be expected of various types of ideal distribution functions since these in effect place an upper limit on the potential performance of a continuous antenna. Also, for very long arrays of discrete elements, the continuous distribution may be used to obtain an excellent approximation to the element excitation coefficients.

Line-Source Distributions

For line sources, the current distribution is considered to be a function of only a single coordinate. The directivity pattern E(u) resulting from a given distribution is simply related to the distribution by a finite Fourier transform, ⁷⁻⁹ as given below:

$$E(u) = \frac{\ell}{2} \int_{-1}^{+1} f(x) e^{jux} dx$$

where f(x) = relative shape of field distribution over aperture as a function of x

 $u = (\pi \ell/\lambda) \sin \phi$

 ℓ = overall length of aperture

 ϕ = angle measured from normal to aperture

 $x = \text{normalized distance along aperture } -1 \le x \le 1$

The simplest type of aperture distribution is the uniform distribution where f(x)= 1 along the aperture and is zero outside of the aperture. The directivity pattern is given as

$$E(u) = \ell \frac{\sin u}{u} = \ell \frac{\sin \left[\left(\frac{\pi \ell}{\lambda} \right) \sin \phi \right]}{\left(\frac{\pi \ell}{\lambda} \right) \sin \phi}$$

This type of directivity pattern is of interest because of all the constant-phase distributions the uniform distribution gives the highest gain.⁷ As in the case of the discrete-element uniform distribution, it also has high sidelobe levels, the intensity of the first sidelobe being 13.2 dB down from the maximum.

The intensity of the sidelobe levels can be reduced very considerably by tapering the aperture distribution in such a way that the amplitude drops off smoothly from the center of the aperture to the edges. There are an unlimited number of possible distributions. However, a few simple types of distributions are typical and illustrate how the beamwidth, sidelobe level, and relative gain vary as a function of the distribution. Table 2-1 gives the important characteristics of several distributions having a simple mathematical form.

TABLE 2-1 Line-Source Distributions

TYPE OF DISTRIBUTION -I≤ x≤I	DIRECTIVITY PATTERN E (u)		HALF POWER BEAMWIDTH IN DEGREES	ANGULAR DISTANCE TO FIRST ZERO	INTENSITY OF Ist SIDELOBE db BELOW MAX.	GAIN FACTOR
-i 0 +i	2 sin u u		50.8 ½	57.3 \delta	13.2	1.0
	Δ=	1.0	50.8 }	57.3 ∆	13.2	1.0
	1(1+1) sin u	.8	52.7 \(\lambda \)	60.7 \(\lambda \) \(\lambda \) \(\lambda \)	15.8	.994
	$\chi = (1-\Delta)\frac{d^2}{du^2}$.5	55.6 ∆	65.3 ∆	17.1	.970
$f(x)=1-(1-\Delta)x^2$			65.9 } ∕	81.9 }	20.6	.833
$\begin{array}{c c} -i & 0 & +i \\ \hline -\cos\frac{\pi x}{2} \end{array}$	$\frac{\pi I}{2} \frac{\cos u}{\left(\frac{\pi}{2}\right)^2 - u^2}$		68.8 À	85.9 \(\)	23	.810
-i 0 +i cos ² $\frac{\pi X}{2}$	1 sin u 2 2 u 2 2 2 2		83.2 ½	1 4.6 λ	32	.667
-i 0 +i	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \		73.4 ½	114.6 ½	26.4	.75

Of considerable interest is the manner in which the sidelobes fall off as the angle from the main beam increases or as u increases. For the uniform distribution which has a discontinuity in both the function and its derivatives at the edge of the aperture, the sidelobes decrease as u^{-1} . For the gable distribution or for the cosine distribution, both of which are continuous at the edge of the aperture but which have a discontinuous first derivative, the far-out sidelobes fall off as u^{-2} . For the cosine-squared distribution which has a discontinuous second derivative, the far-out sidelobes fall off as u^{-3} .

Many distributions actually obtained in practice can be approximated by one of the simpler forms or by a combination of simple forms. For instance, suppose that it were desired to find the directivity pattern of a cosine-squared distribution on a pedestal, i.e., a combination of a uniform distribution and a cosine-squared distribution as given by

$$f(x) = C + \cos^2 \frac{\pi x}{2}$$

The resulting directivity pattern is then obtained directly by adding the two functions for the directivity pattern as follows:

$$E(u) = C\ell \frac{\sin u}{u} + \frac{\ell}{2} \frac{\sin u}{u} \frac{\pi^2}{\pi^2 - u^2}$$

It should be noted that the sidelobes and other characteristics of the pattern must be obtained from the new directivity pattern and cannot be interpolated from Table 2-1. It is of some interest to note that by choosing the proper relative intensities of a uniform distribution and a cosine-squared distribution, it is possible to obtain a theoretical sidelobe level which is very low. For instance, if C = 0.071, then the intensity of the largest sidelobe will be 43 dB below the maximum of the main beam with a half-power beamwidth given by $76.5\lambda/\ell$, a value which is somewhat lower than that for the cosine-squared distribution by itself.

In recent years, work has been done on line-source distributions which produce patterns approaching the Chebyshev type of pattern in which all the sidelobes have a constant level. Van der Maas¹⁰ has shown that it is possible to find the element excitations for a discrete array with a large number of elements by determining the shape of the envelope function as the number of elements is increased indefinitely.

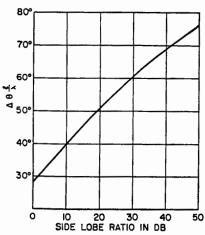


FIG. 2-11 Half-power beamwidth (multiplied by the aperture-to-wavelength ratio) versus sidelobe ratio for an ideal space factor.

This problem has also been investigated in detail by Taylor¹¹ for the case of a continuous line-source distribution. Of considerable interest is the relationship between the half-power beamwidth versus the sidelobe ratio for the ideal space factor (i.e., the equal-sidelobe type of space factor) since this relationship represents the limits of the minimum beamwidth that can be obtained for a given sidelobe level. Figure 2-11 is taken from Taylor's paper. For the details of computing the desired space factor, the reader is referred to the original paper.¹¹

For many applications the equalsidelobe-level pattern may be undesirable, and a more suitable pattern would be one in which the sidelobes decrease as the angle from the main beam, or the parameter u, increases. Work on this form of distribution has been carried out by Taylor¹² in an unpublished memorandum. Basically, the approach is to represent the directivity pattern by a function of the form

$$E(u) = \frac{\sin \sqrt{u^2 - \pi^2 B^2}}{\sqrt{u^2 - \pi^2 B^2}}$$

where the ratio of the main beam to the first sidelobe is given by

$$R = 4.603 \frac{\sinh \pi B}{\pi B}$$

When B is equal to zero, the directivity pattern reduces to the familiar $\sin u/u$ for the case of a uniform distribution and the first sidelobe ratio is 4.603, or 13.2 dB.

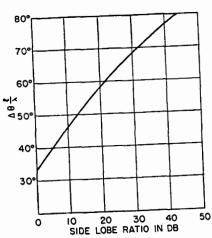


FIG. 2-12 Half-power beamwidth (multiplied by the aperture-to-wavelength ratio) versus sidelobe ratio for space factor defined by

$$E(u) = \frac{\sin \sqrt{u^2 - \pi^2 B^2}}{\sqrt{u^2 - \pi^2 B^2}}$$

As B is increased in value, the sidelobe ratio increases, and by the appropriate choice of B a theoretical sidelobe level as low as desired can be chosen. It will be noted that because of the expression for the directivity, at large values of u the sidelobes decrease as 1/u. Hence we have a directivity pattern whose sidelobes decrease in a similar fashion to that of the uniform distribution but has the property that the maximum sidelobe level can be arbitrarily chosen.

Fortunately, the aperture distribution function for this type of pattern has a relatively simple form and is given by

$$f(x) = J_0(j\pi B\sqrt{1-x^2}) \quad |x| \le 1$$

= 0 $|x| > 1$

 J_0 is a Bessel function of the first kind with an imaginary argument. Tables of this function are readily available.^{13,14}

Taylor has tabulated the important characteristics of this type of distribution, and some of these data have been plotted in Fig. 2-12. By comparing Fig. 2-11 with Fig. 2-12 it can be seen that for

a given maximum sidelobe level the half-power beamwidth of the distribution producing a decreasing sidelobe pattern is approximately 12 to 15 percent greater than the percent half-power beamwidth of the distribution which produces an equal-sidelobe pattern. This nominal loss in theoretical performance is a small price to pay when sidelobe levels must decrease as the angle from the main beam increases. When a decreasing sidelobe level which falls off inversely as the first power of the angle is desired, this type of distribution will result in a narrower beamwidth than that obtained by distributions which produce sidelobes falling off as a higher inverse power of the angle.

2-7 PATTERNS FROM AREA DISTRIBUTIONS

Rectangular Apertures

The directivity pattern of an area distribution is found in a similar manner to that used for line-source distributions except that the aperture field is integrated over two dimensions instead of one dimension. If the aperture distribution is given by f(x,y), where x and y are the two coordinates, then the directivity pattern is given by

$$E(\theta,\phi) = \iint f(x,y)e^{j\beta \sin \theta (x \cos \phi + y \sin \phi)} dx dy$$

The difficulty of evaluating this expression will depend on the form of the distribution function. For many types of antennas, such as the rectangular horn, for example, the distribution function is separable; that is,

$$f(x,y) = f(x)f(y)$$

The directivity patterns in the principal planes are readily determined for the separable case since the pattern in the xz plane is identical with the pattern produced by a line-source distribution f(x), while the pattern in the yz plane is identical with the pattern produced by a line-source distribution f(y). If the distribution function is not separable, the integral must be evaluated either analytically or graphically.

Circular Apertures

An antenna that is frequently used in microwave applications is a paraboloid having circular symmetry. The radiation pattern may be computed by projecting the field distribution on the paraboloid to a plane at the opening of the paraboloid and computing the directivity pattern due to the plane aperture.

If the field in the aperture plane is a function of the normalized radius r and the aperture angular coordinate ϕ' , then the directivity pattern is given by⁷

$$E(u,\phi') = a^2 \int_0^{2\pi} \int_0^1 f(r,\phi') e^{jur \cos{(\phi-\phi')}} r \ dr \ d\phi'$$

where a = radius at outside of aperture

 ρ = radius at any point of aperture

 $r = \rho/a$

 $u = (2\pi a/\lambda) \sin \theta = (\pi D/\lambda) \sin \theta$

D = 2a = aperture diameter

and $f(r,\phi')$ is the normalized aperture distribution function. The coordinates are as shown in Fig. 2-13.

The simplest forms of aperture distributions to evaluate are those in which the distribution is not dependent on the angular coordinate ϕ' but depends only on the radial coordinate r. The integral for the directivity pattern then becomes

$$E(u) = 2\pi a^2 \int_0^1 f(r) J_0(ur) r \ dr$$

When the distribution is constant, the integral becomes

$$E(u) = 2\pi a^2 \frac{J_1(u)}{u}$$

It is frequently desired to evaluate the directivity pattern for an illumination which tapers down toward the edge of the aperture. One function which is convenient for representing the aperture distribution is

$$f(r) = (1 - r^2)^p$$

This function behaves in a similar fashion to the *n*th-power distributions as discussed for the line-source case (Sec. 2-6). When the exponent increases, the distribution becomes more highly tapered and more concentrated in the center of the aperture. When the exponent decreases and approaches zero, the distribution approaches uniform illumination.

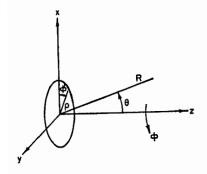


FIG. 2-13 Coordinates for a circular aperture.

TABLE 2-2 Circular-Aperture Distributions

I ADLE 2-2	Circular / Fertile					
TYPE OF DISTRIBUTION O≤ r ≤1	DIRECTIVITY PATTERN E(u)	HALF POWER BEAMWIDTH IN DEGREES	ANGULAR DISTANCE TO FIRST ZERO	INTENSITY OF 1st SIDELOBE db BELOW MAX.	GAIN FACTOR	
$-10 + 1$ $f(r) = (1-r^2)^0 = 1$	#a ² J _I (u)	58.9 ½	6 9.8	17.6	1.00	
-1 0 +1 f(r)=(1-r ²)	2#a ² J ₂ (u)	72.7 \(\frac{\lambda}{D} \)	93.6 <u>λ</u>	24.6	0.75	
- 0 + f(r)=(-r ²) ²	- 8#0 ² J ₃ (u)	84.3 ½	116.2 ½	30.6	0,56	

Evaluating the directivity pattern, we have

$$E(u) = 2\pi a^2 \int_0^1 (1 - r^2)^p J_0(ur) dr$$

= $\pi a^2 \frac{2^p p! J_{p+1}(u)}{u^{p+1}} = \frac{a^2}{p+1} \Lambda_{p+1}(u)$

Both the Bessel functions $J_{p+1}(u)$ and the lambda function $\Lambda_{p+1}(u)$ are available in tabular form.¹³

The principal characteristics of the directivity patterns are given in Table 2-2 for the cases p=0,1,2. Comparison of the patterns of the uniformly illuminated circular aperture (i.e., when p=0) with the results for the uniformly illuminated line source (Sec. 2-6) shows that the circular aperture has a lower sidelobe level and a broader beamwidth. This would be expected since projection of the circular-aperture illumination onto a line would produce an equivalent line source which is no longer uniform but has some degree of tapering.

Elliptical Apertures

In some applications an elliptically shaped reflector is used to permit control of the relative beamwidth in the two principal planes and to control the sidelobes by shaping the reflector outline. Computation of the directivity patterns for this aperture shape can be carried out from a knowledge of the Fourier components of the illumination function over the aperture.

2-8 EFFECTS OF PHASE ERRORS ON LINE SOURCES

The discussions on aperture distributions in Secs. 2-6 and 2-7 were concerned only with those aperture distributions in which the field was in phase across the entire array. In certain types of antenna systems, particularly those in which the beam is to be tilted, deviations from a uniform phase front do occur, so that it is desirable to evaluate the effects of phase errors on the directivity pattern.

For simplicity, the following discussions are limited to the case of a line-source distribution. Results will be first derived for the simple uniform amplitude distribution, and graphical results will be presented for a tapered amplitude distribution.

The most common phase-front errors are the linear, quadratic, and cubic phase errors. The linear phase error is expressed simply by

$$\Phi(x) = \beta_1 x$$

where β_1 = phase departure at edge of aperture

x = aperture coordinate as defined in Sec. 2-6

The directivity pattern is given by

$$E(u) = \frac{\ell}{2} \int_{-1}^{1} f(x)e^{jux}e^{-j\beta_1 x} dx$$

For a uniform illumination, the result is

$$E(u) = \ell \frac{\sin (u - \beta_1)}{u - \beta_1}$$

Thus the directivity pattern has the same form as for the in-phase case except that the pattern maximum is shifted in angle as defined by

$$u = \beta_1$$
 or $\sin \phi_0 = \frac{\beta_1 \lambda}{\pi \ell}$

For other than a uniform illumination, the patterns will also be the same as for the in-phase case, except that $u - \beta_1$ is substituted for u in the expression for the directivity.

In the vicinity of the main beam, the directivity pattern is the same as that of an aperture tilted by ϕ_0 whose length is $\ell \cos \phi_0$. The half-power beamwidth is increased by the factor $1/\cos \phi_0$, while the gain is decreased by $\cos \phi_0$. For small angles of beam tilt, the pattern and gain are affected by only a minor amount.

The quadratic, or square-law, phase error is inherent in flared horn antennas. It also occurs in lens-type antennas and reflector antennas when the feed is defocused along the axis of symmetry. This type of phase error also appears when the directivity pattern of an antenna is measured at a finite distance.

The quadratic phase error is expressed by

$$\Phi(x) = \beta_2 x^2$$

and the directivity pattern is expressed by

$$E(u) = \frac{\ell}{2} \int_{-1}^{1} f(x)e^{jux}e^{-j\beta_1 x} dx$$

The integral is not readily evaluated except when f(x) is constant or one of the cosine distributions. For these cases, the directivity can be expressed in terms of the Fresnel integrals. The directivity pattern for the uniformly illuminated case is given by 1,2

$$E(u) = \frac{\ell}{2} \sqrt{\frac{\pi}{2\beta_2}} \{ C(m_2) - C(m_1) - j[S(m_2) - S(m_1)] \}$$

where

$$m_2 = \sqrt{\frac{2\beta_2}{\pi}} \left(1 - \frac{u}{2\beta_2} \right)$$

$$m_1 = \sqrt{\frac{2\beta_2}{\pi}} \left(-1 - \frac{u}{2\beta_2} \right)$$

and the Fresnel integrals are defined by

$$C(m) = \int_0^m \cos\left(\frac{\pi}{2}y^2\right) dy$$
$$S(m) = \int_0^m \sin\left(\frac{\pi}{2}y^2\right) dy$$

The expressions for the cosine and higher-order cosine distributions become increasingly complicated, and the problem of computation becomes exceedingly laborious. Some simplification in the computation problem can be obtained by the use of operational methods as developed by Spencer⁸ and also by Milne.¹⁵ Figure 2-14a-c is reproduced from Milne's paper.

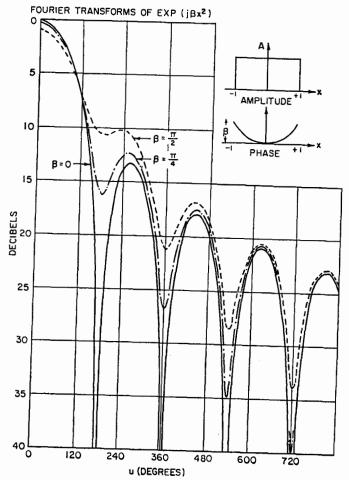


FIG. 2-14a Effects of square-law phase error in radiation patterns for uniform aperture illumination.

It will be noted that the principal effects of a quadratic phase error are a reduction in gain and an increase in sidelobe amplitude on either side of the main beam. For moderate amounts of phase error, the nulls between the sidelobes disappear and the sidelobes blend into the main beam, appearing as shoulders rather than as separate

The cubic phase error is expressed by

$$\Phi(x) = \beta_3 x^3$$

Computation of the directivity integrals for the cubic phase error becomes even more laborious than for the quadratic phase error, although the use of operational methods for computation simplifies the formal handling of the problem. Some typical results from Milne's paper are given in Fig. 2-15a-c.

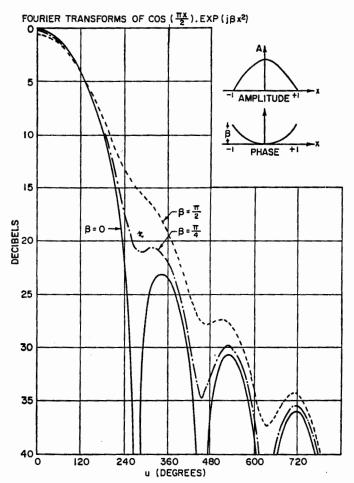


FIG. 2-14b Effects of square-law phase error in radiation patterns for cosine aperture illumination.

It will be observed that the cubic phase error produces a tilt of the beam in addition to a loss in gain. The sidelobes on one side of the beam increase in amplitude, while those on the other side diminish.

In general, when the feed is moved off axis to tilt the beam, both a linear phase term and a cubic phase term appear. The linear phase term causes a beam tilt which is a function of the geometry of the antenna system. For the case of a parabolic reflector, the cubic phase term causes a lesser amount of tilt in the opposite sense so that the resulting beam tilt is somewhat less than would be computed from geometrical considerations. For this case, the sidelobe increase appears on the side of the beam toward the axis.

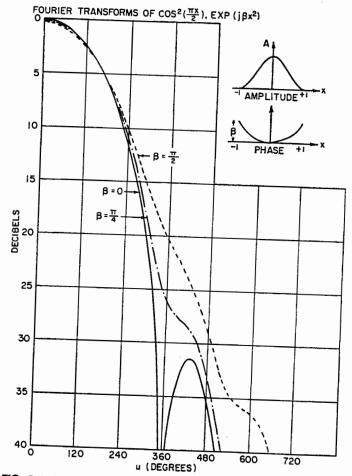


FIG. 2-14c Effects of square-law phase error in radiation patterns for cosine-squared aperture illumination.

2-9 EFFECTS OF RANDOM ERRORS ON GAIN AND SIDELOBES

The preceding section has discussed the effect of systematic phase errors on several different types of aperture distributions. In general, some of these errors are inherent in a given design and are a function primarily of the geometry of the antenna. In addition to systematic errors, a problem which commonly arises is that caused by random errors in both the phase and the amplitude across the aperture because of manufacturing tolerances.

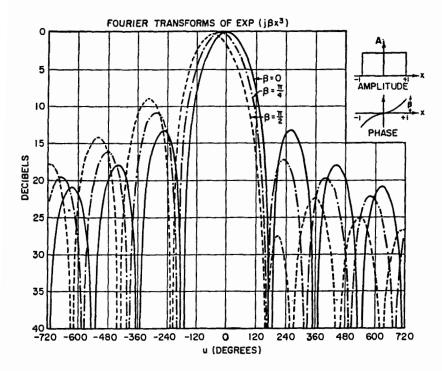


FIG. 2-15a Effects of cubic phase error on radiation pattern for uniform aperture illumination.

An estimate of the effect of random errors can be made in at least three different ways. The first method is to measure directly the radiation performance of the antenna in question. By comparison with the computed performance, it is possible to estimate the magnitude of the errors in the field distribution across the antenna.

The second method is to measure the amplitude and phase of the field distribution across the aperture. From these data, the effect of the errors on the antenna performance can be computed.

A third method is to compute the effect of manufacturing tolerances on the desired aperture distribution and from this, in turn, to compute the effect on the radiating properties of the antenna. This method is of considerable interest to the antenna designer, who must specify what sort of tolerances are necessary to achieve a desired result. As is true in all fabrication work, extremely tight tolerances result in excessive costs, while tolerances that are too loose can result in inadequate performance or failure of operation. It is therefore desirable to know how much accuracy is required for a given level of performance.

A theory of random errors is necessarily based on statistical considerations, so that the results predicted will not be on an absolute basis but rather in terms of a given probability level. The main use of this theory is to estimate what the effect will be on the average performance of a large number of antennas when a given tolerance level is specified.

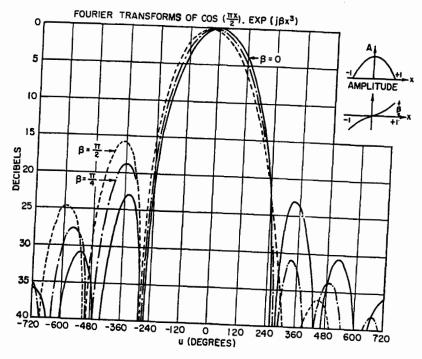


FIG. 2-15b Effects of cubic phase error on radiation pattern cosine aperture

Discrete-Element Arrays

The problem of the discrete-element array starts off with the premise that the ideal radiation pattern desired is specified by a uniformly spaced array of N elements, with each element carrying a specified current. If we denote the current in the nth element by I_n and the actual current by $I_n + \epsilon_n I_n$, then the radiation pattern due to the desired

$$E(\phi) = \sum_{n=1}^{N} I_n \exp \left(j \frac{2\pi nd}{\lambda} \sin \phi \right)$$

where d = spacing between elements

 ϕ = angle measured from normal to array

The radiation pattern due to the error terms is given by

$$R(\phi) = \sum_{n=1}^{N} \Delta_{n} I_{n} \exp (j\delta_{n}^{\prime})$$

where $\delta'_n = \delta_n + (2\pi nd/\lambda) \sin \phi$

 $\Delta_n = \text{ratio error of } m \text{th current}$

 $\delta_n = \text{phase error}$

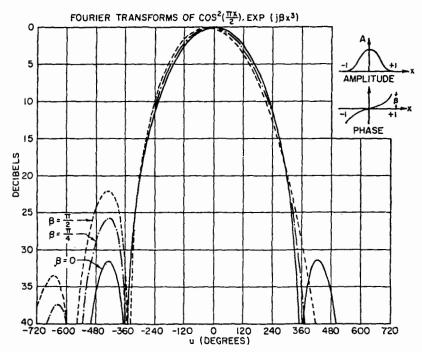


FIG. 2-15c Effects of cubic phase error on radiation pattern for cosine-squared aperture illumination.

It can readily be seen that the desired radiation pattern $E(\phi)$ is altered by the addition of the error-term radiation pattern $R(\phi)$. If measured data are available for the individual element currents, then it is possible to compute $R(\phi)$ exactly, even though this may be a rather laborious process.

As is often the case, experimental data are not available beforehand, and it is desirable to know what degree of precision is required in driving the array in order to achieve a given performance. For a large number of elements and for small errors, it is reasonable to assume that the individual errors are independent of one another and are distributed as a normal, or gaussian, distribution. The problem has been treated on a statistical basis by Ruze, 16 who has computed the sidelobe-level probabilities in terms of the rms error in the current values.

In statistical analysis, it is not possible to predict the exact pattern of a particular array with errors but rather the average pattern of a large number of similar arrays. If $\overline{P(\phi)}$ denotes the power pattern for an "average system" and $P_0(\phi)$ the power pattern for an antenna without errors, we have

$$\overline{P(\phi)} = P_0(\phi) + S(\phi)\overline{\epsilon^2} \frac{\sum I_n^2}{(\sum I_n)^2}$$

where $S(\phi)$ = a slowly varying function closely related to the power pattern of a sin- $\frac{\text{gle element}}{\epsilon^2} = \frac{\overline{\Delta}^2}{\overline{\Delta}^2} + \frac{\overline{\delta}^2}{\overline{\delta}^2}$

$$\overline{\epsilon^2} = \overline{\Lambda^2} + \overline{\delta^2}$$

 ϵ^2 = total mean square error

 $\overline{\Delta^2}$ = mean square amplitude error

 $\overline{\delta^2}$ = mean square phase error, rad²

On the average, then, the effect of the random errors is to add to the pattern a constant power level which is proportional to the mean square error. For individual arrays and in particular directions, the sidelobe radiation will differ from this constant level in a fashion governed by the probability distribution for the particular array.

It is of interest to note that the spurious radiation is approximately proportional to 1/N, so that for a given mean square error lower sidelobe levels are more readily obtained with larger antennas.

Computations have been made for a Dolph-Chebyshev type of array consisting of 25 elements with a design sidelobe level of 29 dB below the main beam. For an angular position where the no-error minor lobes have maxima, Fig. 2-16 shows the

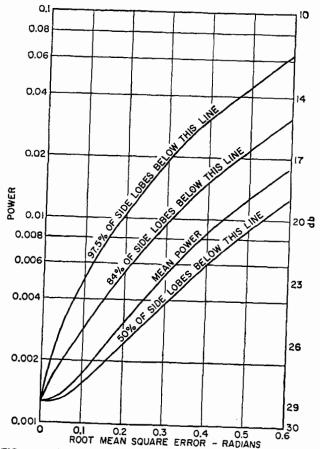


FIG. 2-16 Sidelobe distribution for 25-element broadside array, designed for 29-dB sidelobe suppression and computed at design-lobe maxima.

probability that the radiation will be below a specified number of decibels when a given mean error exists in the antenna currents.

As a check on the above theory, Ruze has computed the actual pattern of the 25-element antennas with a specific set of error currents. For a 0.40-rms error in each element with random phase, the radiation pattern was computed. Figure 2-17 shows the theoretical patterns for the cases with and without error. Analysis of the sidelobe magnitudes on this figure shows that their distribution compares very well with the theoretical distribution obtained on a statistical basis.

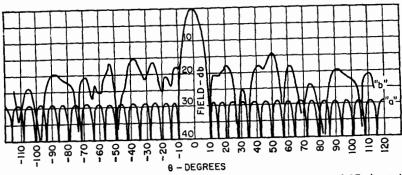


Fig. 2-17 Theoretical effect of error currents on radiation pattern of 25-element broadside array designed for 29-dB sidelobe suppression. (a) No error. (b) 0.40-rms error in each element at random phase.

The loss in gain can also be determined from this analysis. An excellent approximation for the actual gain G with errors as compared with the theoretical gain G_0 when no errors are present is given by

$$\frac{G}{G_0} \approx \frac{1}{1 + \left(\frac{3\pi}{4}\right) \left(\frac{d}{\lambda}\right)^2 \vec{\epsilon}^2}$$

where d = spacing between elements

 λ = wavelength

The above analysis has concerned itself only with the accuracy of the current values required for the array. To translate these results into mechanical tolerances for a given antenna system depends on the nature of the individual elements, the type of feed system used, and a variety of other factors. One particular array which readily lends itself to this type of analysis is a waveguide-fed shunt-slot linear array. Some results for an X-band waveguide array have been obtained in Refs. 17 and 18. In the latter reference, computations for the probable sidelobe level have been made for a manufacturing tolerance with a standard deviation of 0.002 in (0.0508 mm) in a Dolph-Chebyshev array. The effect of the design sidelobe level and the number of elements is readily shown in Table 2-3.

It should be noted that the figures in Table 2-3 are based on a normal distribution in which the tolerances can take on all values but have a standard deviation of 0.002 in. In actual manufacturing practice, physical dimensions are not allowed to deviate

TABLE 2-3

Desi	gn sidelobe level, dB			
Number of elements		20	30	40
12		18.6	25.9	29.1
24		19.0	26.7	31.8
48		19.1	27.3	33.3

NOTE: 84 percent of the sidelobe levels will be less than the tabulated value.

from the design value by more than an arbitrary amount so that the tolerance distribution is actually a truncated normal distribution. For this condition, the deterioration in sidelobe level is somewhat less than that given.

Two conclusions can be drawn regarding the effect of random errors in discreteelement arrays:

- 1 For a given sidelobe level, the effect of random errors becomes somewhat less critical as the number of elements in an array increases.
- 2 For a given number of array elements, the effect of random errors becomes more critical as the required sidelobe level is further suppressed.

As a practical matter, when designing low-sidelobe-level arrays, it is usually necessary to overdesign the array in order to be certain of achieving the desired sidelobe level in the presence of random errors. For instance, to attain a 26-dB sidelobe level, it may be desirable to design the aperture distribution for a 32-dB sidelobe level. Actually, the amount of overdesign required depends on a compromise between economical manufacturing tolerances and the loss in aperture efficiency due to the overdesign.

Continuous Apertures

The statistical analysis of continuous apertures, such as reflector-type antennas, is similar to that for discrete-element arrays, except for two important differences. For the discrete array, the error in one element has been assumed to be independent of the errors in adjacent elements. However, for a continuous-aperture array, a large error at one point implies that the error will be large in the immediate area around that point since the error could be due to warping of the reflector or a bump in the reflector. Also, the error will be purely a phase error since the amplitude distribution will be essentially unaffected by moderate changes in the reflector surface.

The fact that an error will extend over an area makes it convenient to use the concept of a correlation interval c. On the average, c is that distance in which the errors become essentially independent of one another. For instance, an error consisting of a bump extending over a large area implies a large value of c, while errors consisting of a number of bumps, each of which covers a small area, imply a small value of c.

In an analysis similar to that for the discrete array it has been shown¹⁶ that the power pattern for an "average" system with small errors is given by

$$\overline{P}(\phi) = P_0(\phi) + S(\phi) \frac{4c^2\pi^2\overline{\delta^2}}{\lambda^2 G_0} \exp\left(-\frac{\pi^2c^2\sin^2\phi}{\lambda^2}\right)$$

where the symbols have the same meaning as used earlier in this section, except for c, which is defined as the correlation interval. The effects of random errors on the side-lobes and gain of a circular paraboloid have been computed by Ruze. Some of his results for the case of a cosine-squared illumination are shown in Figs. 2-18 and 2-19.

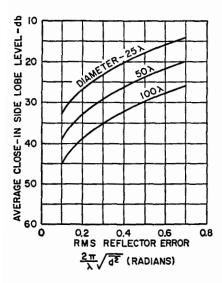


FIG. 2-18 Spurious radiation of paraboloid with cosine-squared illumination. Correlation interval $c = \lambda$.

The relationships for the loss in gain have also been worked out by Ruze. For small errors, simplified formulas have been obtained for the limiting cases of small and large correlation intervals, as follows:

$$\frac{G}{G_0} \approx 1 - \frac{3}{4} \, \overline{\delta^2} \, \frac{c^2 \pi^2}{\lambda^2}$$
 when $\frac{c}{\lambda} \ll 1$

and

$$\frac{G}{G_0} \approx 1 - \overline{\delta^2}$$
 when $\frac{c}{\lambda} \gg 1$

Some results for the loss in gain are given in Fig. 2-20.

Periodic Errors in Aperture Illumination

In addition to random errors introduced in the manufacturing process, certain types of antennas may also introduce periodic errors due to the particular technique used in fabricating the antenna. For instance, in certain types of reflectors using the bulkhead-

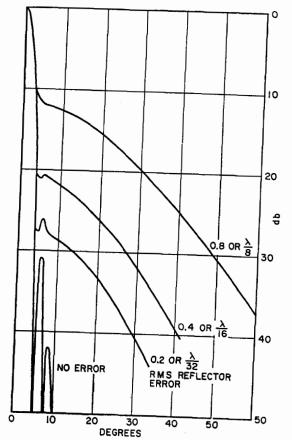


FIG. 2-19 Average system pattern for circular paraboloid with cosine-squared illumination. Correlation interval $c = \lambda$ calculated for reflector 24 λ in diameter.

and-trusswork type of construction, mechanical stresses set up during fabrication are such that the surface has periodic errors at roughly equal intervals along the surface. This results in a periodic phase error along the aperture.

The effect of a sinusoidal phase error on the sidelobes has been treated in Ref. 19, which points out that a sinusoidal phase error will produce two equal sidelobes whose amplitude relative to the main-beam amplitude is equal to one-half of the peak phase error expressed in radians. The two sidelobes are symmetrically located on either side of the main beam at an angular distance of $m\lambda/\ell$ rad from the main beam, where m is the number of cycles of phase error along the aperture, ℓ is the total length of the aperture, and λ is the wavelength expressed in the same units as ℓ .

The effect of any type of phase error on the antenna gain has been treated by Spencer, 20 who shows that the fractional loss in gain is equal to the mean square phase error from the least-square plane-wave approximation to the phase front. Since a peri-

odic phase error would not alter the direction of the unperturbed phase front, the loss in gain is equal to the mean square value of the periodic phase error. It is interesting to note that this represents the limiting case for random errors as shown in

Fig. 2-20.

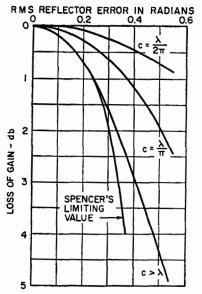


FIG. 2-20 Loss of gain for paraboloid as function of reflector error and correlation interval.

Another type of distribution error which can occur under certain conditions is a periodic amplitude error.21 The sidelobe behavior of the amplitude-modulated distribution is very similar to that for the case of the sinusoidal phase error. Two equal sidelobes on either side of the main beam will appear for each sinusoidal component of the amplitude modulation. For a uniform-amplitude distribution with a sinusoidal ripple, the amplitude of each sidelobe due to the ripple will have a value relative to the mainbeam amplitude which is equal to onehalf of the ratio of the ripple amplitude to the amplitude of the constant term. As was true for the periodic phase error, the periodic amplitude error will produce two symmetrically located sidelobes on either side of the main beam at an angular distance of $m\lambda/\ell$ rad, where m is the number of cycles of amplitude variation across the aperture whose total length is ℓ.

2-10 METHODS OF SHAPING PATTERNS

A variety of radar system applications require that the radiation pattern of the antenna be shaped to meet certain operational requirements. One common requirement for the vertical-plane pattern is the cosecant-squared pattern, which produces a uniform ground return echo from an airborne radar antenna. There are, of course, other shapes of interest, but the basic principles of obtaining shaped beams are the same for a wide variety of shapes.

Methods Useful for Linear Arrays

One of the techniques useful with slot arrays or dipole arrays is to determine what aperture distribution will produce the desired radiation pattern and then design the array feed system so as to achieve the required aperture distribution.

There are several methods in use for determining the form of the aperture distribution. Historically, the first method is based on the Fourier approximation to a given function. ²² For an equally spaced array of radiating elements, the radiated field due to the array can be represented by a finite trigonometric series with a direct relationship between the current in each element and the coefficients of the trigonometric

series. If the required radiation pattern is analyzed by standard Fourier methods, the coefficients of the Fourier series then determine the current amplitudes and phase for the array elements. The accuracy with which the finite series approximates the desire function depends on how many terms are used, that is, on how large an aperture i used. For a fixed number of terms, it is well known from the theory of Fourier series that the approximation is best in the sense that the mean square deviation is least. It is also a property of the Fourier approximation that at a point of discontinuity the function takes on a value that is the average of the value existing on either side of the discontinuity; i.e.,

$$\frac{1}{2}[E(\phi + 0) + E(\phi - 0)]$$

A second method of approximating the desired radiation pattern is one that enables the pattern to be specified exactly at a fixed number of points. This method, which was independently proposed by Woodward²³ and by Levinson, is particularly appealing in that it gives the designer some physical insight into the way in which the pattern is synthesized and in addition allows some control of the pattern at points of discontinuity.

Basically, the method consists of superposing a series of uniform-amplitude, linear-phase distributions across the aperture in such a way that the sum of the patterns produced by each of the distributions adds up to the desired pattern. The required aperture distribution is then found by adding up, in proper phase, the individual uniform distributions.

To simplify matters, the following discussion will deal with the case of a continuous aperture. The extension to the case of a uniformly spaced discrete-element array will be obvious from the discussion. As pointed out in Sec. 2-6, the radiation pattern for a uniform in-phase illumination is given by

$$E(\phi) = \frac{\sin u}{u}$$

where

$$u = \frac{\pi \ell}{\lambda} \sin \phi$$

The pattern will pass through zero whenever $\sin \phi = n\lambda/\ell$, n = 1, 2, 3, 4, etc., and the pattern has its maximum when $\phi = 0$. For a case in which $\ell = 10\lambda$, the pattern plotted against $\sin \phi$ will appear as in Fig. 2-21a.

It will be noted that when the pattern is plotted against $\sin \phi$, the zeros of the pattern are equally spaced except for the two zeros on either side of the main beam, which occupy two spaces. The width of one space is equal to λ/ℓ , the reciprocal of the aperture width in wavelengths.

A uniform illumination with a linear phase variation will have a field pattern given by

$$E(\phi) = \frac{\sin(u - \beta_n)}{u - \beta_n}$$

where β is one-half of the total phase variation across the aperture ℓ . The maximum of this pattern occurs when

$$\sin \phi_n = \frac{\beta_n \lambda}{\pi \ell}$$

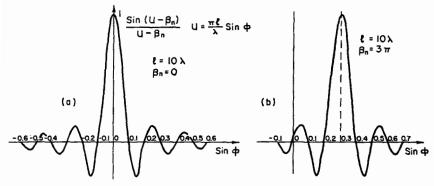


FIG. 2-21 Radiation pattern of uniformly illuminated aperture 10 λ long. (a) $\beta_n = 0$. (b) $\beta_n = 3\pi$.

If the phase variation is chosen so that $\beta_n = n\pi$, then the pattern will be shifted by $n\lambda/\ell$, or *n* spaces when plotted against $\sin \phi$. A typical pattern for $\ell = 10\lambda$ and $\beta_n = 3\pi$ is shown in Fig. 2-21 *b*.

By combining a number of patterns shifted by integral numbers of spaces, it is possible to synthesize a pattern which can be uniquely specified at 2m + 1 points for an aperture which is m wavelengths in extent. The total radiation pattern is given by

$$E(\phi) = \sum_{n} C_n \frac{\sin(u - \beta_n)}{u - \beta_n} = \sum_{n} C_n \frac{\sin(u - n\pi)}{u - n\pi}$$

and the corresponding normalized aperture distribution is given by

$$f(x) = \sum_{n} C_{n}e^{-j\beta_{n}x} = \sum_{n} C_{n}e^{-jn\pi x}$$

where $-1 \le x \le +1$.

As an illustration of this method, let us consider a problem in which it is desired to specify that the pattern have a cosecant shape over the range in sin ϕ from 0.1 to 1.0 and that it have no radiation for negative values of $\sin \phi$. For an aperture length of 10 wavelengths, $\sin \phi$ is divided into spaces one-tenth wide from -1 to +1 and ordinates erected at each division with a height equal to $E(\phi)$. For the problem at hand, $E(\phi)$ is proportional to csc ϕ . A plot of the $E(\phi)$ diagram is shown in Fig. 2-22, where at each division an individual pattern is to be specified with a maximum value equal to each ordinate. The summation of the individual patterns is shown in Fig. 2-23, while the resulting total aperture distribution, consisting of the sum of each of the indi-

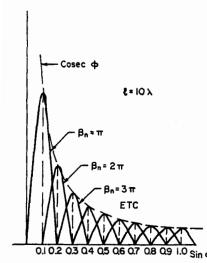


FIG. 2-22 $E(\phi)$ pattern for cosecant

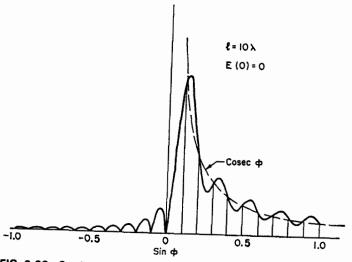
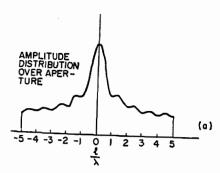


FIG. 2-23 Synthesis of cosecant pattern for E(0) = 0.



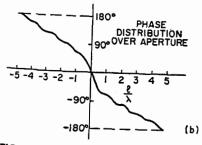


FIG. 2-24 Aperture distribution for Fig. 2-23. (a) Amplitude distribution. (b) Phase distribution.

vidual aperture distributions, is shown in Fig. 2-24.

For the case shown, E(0) has been chosen to equal zero, and it will be noted that the resulting pattern has a fair amount of ripple in it. If the value of E(0) is chosen to be 0.8, then the resulting pattern shown in Fig. 2-25 is considerably smoother although the aperture distribution is somewhat more peaked, as seen from Fig. 2-26.

This particular method of synthesis is quite useful because of the flexibility in arriving at the final radiation pattern and the designer's ability to adjust the theoretical pattern by graphical procedures. Although the example discussed has used only real values for C_n to simplify the calculations, there is nothing in the procedure which prevents the use of complex values for C_n . It is quite possible that a judicious choice of the phase angles for the C_n 's might have given as effective a control over the ripple as did the changing the value of E(0).

One note of caution should be added. Although beams can be added for values of $|\sin \phi| > 1$ in order to control

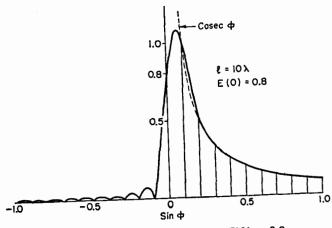


FIG. 2-25 Synthesis of cosecant pattern for E(0) = 0.8.

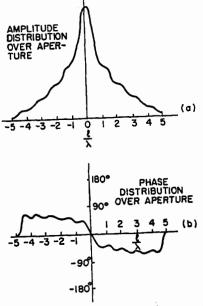


FIG. 2-26 Aperture distribution for Fig. 2-25. (a) Amplitude distribution. (b) Phase distribution.

the amplitude at points intermediate between the ordinates, the energy in these "imaginary beams" (when ϕ is complex) is primarily of a reactive nature and can result in large amounts of stored energy in the aperture, with consequent reduction of bandwidth and increase of losses. It is therefore desirable to minimize or eliminate those beams which radiate in directions specified by $|\sin \phi| > 1$.

Methods Useful for Reflector-Type Antennas

There are several methods useful for producing shaped patterns with reflector-type antennas. One technique, which is readily applied to a standard paraboloidal reflector, combines a number of narrow beams to form a wider beam, shaped in the vertical plane by the use of an extended feed system. In some respects, this technique has a certain similarity to the Woodward-Levinson method discussed earlier in the section.

In applying this technique, a rectangular or elliptical section of a full para-

boloid is used as the reflector surface. The horizontal dimension of the reflector section is chosen to give the desired horizontal beamwidth, while the vertical dimension is

chosen to control the rate of cutoff of the vertical beam. The vertical dimension also influences the feed-system problem, particularly if a small value is chosen, since the feed horn or dipole for each beam would have to have a sizable vertical dimension. The aspect ratio of the reflector commonly has a value in the range of 2:1 to 4:1.

A considerable amount of experimental effort is necessary in the design of an extended feed system. The basic principles can be seen from Fig. 2-27. For each feed in the vertical plane, there is a corresponding vertical beam whose position is related

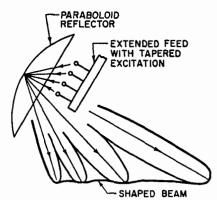


FIG. 2-27 Schematic of extended feed system for pattern shaping.

to the feed position. By exciting each feed with the appropriate amplitude and by choosing the feed separation and phasing, it is possible to obtain a fairly smooth vertical-plane pattern.

A number of examples of this technique are given in Ref. 7. Although most of the structures built to date have used reflector structures for collimating each beam, the same technique of combining beams is also applicable to lens-type antennas.

Another approach to the problem of generating shaped beams is the use of shaped-reflector systems. One method uses a line source to feed a shaped reflector, while a second method uses a point-source feed with a double-curvature

reflector. The shaped-reflector approach is treated in Chap. 17, so no further discussion will be given here.

2-11 GAIN LIMITATIONS FOR AN APERTURE OF SPECIFIED SIZE

It has been shown that the gain of a uniformly illuminated aperture-type antenna without losses is expressed by

$$G = \frac{4\pi A}{\lambda^2}$$

where A is the area of the aperture. The value of gain obtained from this expression normally represents an upper limit which can be realized with practical structures.

Certain classes of aperture distributions offer the theoretical possibility of higher values of directivity than can be obtained with uniform distribution. In general, these theoretical distributions are characterized by reversals of phase over a distance short compared with the wavelength. One common feature of these superdirective distributions is the large amount of stored energy in the aperture region since very high values of field intensity are necessary to produce the same radiated field as would be produced by a uniformly illuminated aperture with much lower values of field intensity.

The large values of stored energy in the aperture region of a superdirective antenna cause a number of engineering problems which are severe enough to make this type of antenna completely impractical. The first problem is that of extremely high Q's, which limit the operating bandwidth to extremely small values. For instance, it has been stated by Taylor²⁴ that an antenna designed within a sphere of 50 wavelengths diameter will have a beamwidth of approximately 1°. If the same beamwidth is to be maintained while the diameter of the sphere is reduced to 45 wavelengths, the Q will rise to a value of 500. If the diameter is reduced to 40 wavelengths, the Q will rise to a value of P0. For further reductions in diameter, the value of P1 rises to astronomical values. Since the bandwidth is of the order of the inverse of P2, it can be seen that the bandwidth diminishes rapidly.

As a result of the high stored energy, large values of circulating current flow in the antenna structure, and a point is very quickly reached at which the ohmic losses completely nullify any gain increase due to increased directivity.

Another concomitant of the superdirective antenna is the extreme precision required to achieve any substantial increase in directivity.

There is an abundant literature on the topic of superdirective antennas, and the antenna designer who may be tempted to build such antennas should consult these references.²⁵⁻²⁷

Lest the situation be considered completely hopeless, it should be mentioned that for certain end-fire arrays in which the values of gain are modest some increase in gain can be achieved. One particular design in which a four-element end-fire array has achieved a modest increase in gain and directivity at the expense of bandwidth has been given in the literature. However, aside from the special case of end-fire arrays, the designer is to be discouraged from attempting to construct arrays which have gains higher than the value given for the uniform-illumination case. This caution is particularly true for broadside antennas in which the aperture is large in terms of wavelengths.

2-12 SCALE MODELS OF ANTENNAS

One of the most useful tools of antenna engineers is the ability to scale their designs. It is a direct consequence of the linearity of Maxwell's equations that an electromagnetic structure which has certain properties²⁹ at a given frequency f will have identically the same properties at another frequency nf, provided all linear dimensions are scaled by the ratio 1/n. Thus an antenna design which works in one range of frequencies can be made to work at any other range of frequencies without additional redesign, provided an exact scaling of dimensions can be accomplished.

Quite aside from the ability to transfer design relationships is the ability to make radiation-pattern studies on scale models which are convenient in size. The aircraft antenna field is one in which full-size radiation studies are extremely awkward, time-consuming, and expensive. The possibility of studying aircraft antennas on a scale model³⁰ which may be as small as one-twentieth or one-fortieth of full size brings such studies within the realm of the laboratory rather than requiring an elaborate flight operation.

For most types of antennas, scaling is a relatively simple matter. Table 2-4 shows how the dimensions and electromagnetic properties vary as a function of the scale

TABLE 2-4

Quality	Full-scale system	Model system
Length	L_{P}	$L_M = L_F/n$
Frequency	f_F	$f_{M} = nf_{F}$
Dielectric constant	€ _F	$\epsilon_M = \epsilon_F$
Conductivity	σ_F	$\sigma_M = n\sigma_P$
Permeability	μ_F	$\mu_M = \mu_P$

factor. It will be noted that all the quantities except conductivity can be satisfactorily scaled. If the full-size antenna is constructed of copper or aluminum, then it is not possible to obtain materials which have conductivities that are an order of magnitude higher. Fortunately, conductivity losses affect the operation of most antennas to only a minor degree, so that the inability to scale the conductivity is not usually serious. This is not true for devices such as cavity resonators, for which the losses may be appreciable. For a few types of antennas, such as very long wire antennas, in which the conductivity losses of the antenna and of the ground may play a part in the radiating properties of the antenna, it may be necessary to proceed with considerable caution before making scale-model studies.

While it is true that an exact scale model will have exactly the same radiation patterns and input impedance as the full-scale antenna, it is not always possible to achieve perfect scaling. This is particularly true for such items as transmission lines, screw fastenings, etc. Slight discrepancies in scaling will usually affect the impedance properties much more than the radiation properties. It is therefore wise to consider scale-model impedance studies as primarily qualitative in nature, even though it is valid to consider scale-model radiation patterns as being highly accurate. Usually the general trend of impedance characteristics is determined from the scale model, but final impedance-matching work can be completed only on the full-size antenna.

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Arrays of Discrete Elements*

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3-1 Introduction 3-2
3-2 Uniform Linear Arrays 3-2
Broadside Arrays of Isotropic Elements 3-3
Broadside Arrays with Practical Antennas as
Elements 3-7
Ordinary End-Fire Arrays of Isotropic
Elements 3-10
Ordinary End-Fire Arrays of Practical
Antennas as Elements 3-12
3-3 Yagi-Uda Arrays 3-13
3-4 Improved End-Fire Arrays 3-15
3-5 Linear Arrays with Tapered Excitations—Equal
Sidelobes 3-17
A New Approach for Treating Optimum
Broadside and End-Fire Arrays 3-18

Optimum Broadside Arrays When d <
λ/2 3-24
Optimum End-Fire Arrays When d Is Less
Than the Maximum Allowable Spacing 3-26
3-6 Array of Arrays 3-29

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A practical objective of directive communication is an improvement in received signal as measured relative to the prevailing noise. More precisely, directivity improves the signal-to-noise ratio. This improvement may be accomplished either at the transmitter side by using an antenna that projects the transmitted wave power in the form of a concentrated beam toward the distant receiver, or it may be accomplished at the receiver side by using a similar antenna to intercept a maximum wave power. Thus, any desired signal improvements may be taken either at the transmitter or at the receiver or be shared between the two.

One of the common methods of obtaining directive antenna characteristics is an arrangement of several individual antennas of the same kind so spaced and phased that their individual contributions add in one preferred direction while they cancel in others. Such an arrangement is known as an array of discrete antennas. The individual antennas, called elements, in an array may be arranged in various configurations such as straight lines, squares, rectangles, circles, ellipses, arcs, or other more innovative geometries. Years of experience have reduced the number of configurations that are considered practical to a relatively few.

Improvements in radiation characteristics by arraying may be described in a variety of ways. Sometimes the result takes the form of a plotted pattern which shows, at a glance, the relative signal level in various directions. In other cases the result is measured in terms of directivity or power gain. For purposes of this chapter, directivities or power gains are generally referenced to some accepted standard such as an isotropic source or an array element.

One of the practical arrays consists of a number of individual antennas set up along a straight line known as the *linear array*. For this particular configuration, the individual elements may be excited by currents in phase with equal or tapered amplitudes. Under this condition, radiation proceeds both forward and backward in directions perpendicular to the lines of the array. Such an array is said to be *broadside*. It may be made essentially unidirectional by adding a second identical array to the rear of the first and exciting the second array with appropriate phase difference.

The elements of a linear array may also be driven by currents with phase progressively varying along the array axis in such a way as to make the radiation substantially unidirectional. This array is referred to as an end-fire array. Both the broadside and the end-fire arrays of different elements are presented in Secs. 3-2 through 3-5. Necessary formulas without detailed derivations are given together with the first-hand design curves or tables with the number of elements, interelement spacings, amplitudes, phases, and other array characteristics as the parameters. A special array of arrays known as the curtain antenna is briefly discussed in Sec. 3-6.

When the general principle of arrays with isotropic elements is presented, no consideration of the mutual-coupling problem is needed. For the case involving simple practical antennas such as the short Yagi-Uda array (a small number of dipoles) for which methods of computing the mutual impedances between elements are available, the mutual impedances will be duly included.

3-2 UNIFORM LINEAR ARRAYS

When the identical elements of a linear array are equally spaced along the array axis and excited with uniformly progressive phases as shown in Fig. 3-1, the array pattern

3-3

in free space may be considered, assuming that the principle of pattern multiplication applies, ^{1,2} as a product of the element pattern and an array factor,

$$E(\theta,\phi) = f(\theta,\phi)S(\theta)$$
 (3-1)

where $E(\theta,\phi)$ is the far-field pattern expressed in terms of the ordinary spherical coordinates (θ,ϕ) , $f(\theta,\phi)$ is the element pattern determined by the particular antenna ele-

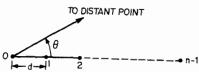


FIG. 3-1 A linear array of *n* equally spaced elements.

ment used in the array, and $S(\theta)$ is the array factor for a linear array placed along the z axis with θ measured from the array axis.

The array factor $S(\theta)$ may be explicitly written as

$$S(\theta) = \sum_{i=0}^{n-1} I_i \exp(jiu)$$
 (3-2)

where I_i represents the current amplitude excitation of the *i*th element and

$$u = kd(\cos\theta - \cos\theta_0) \tag{3-3}$$

with k being the wave number $(2\pi/\lambda, \lambda)$ being wavelength), d the interelement spacing in wavelength, θ_0 the desired direction of the maximum radiation, and n the total number of elements in the array.

When $I_i = 1$, i = 0, 1, ..., (n - 1), a uniform linear array results, yielding

$$S_u(\theta) = \sum_{i=0}^{n-1} \exp(jiu) = \frac{1 - \exp(jnu)}{1 - \exp(ju)}$$
 (3-4)

where the subscript u should not be confused with the symbol defined in Eq. (3-3).

Broadside Arrays of Isotropic Elements

If, in addition, the elements are isotropic and the desired maximum radiation is in the broadside direction, we have $f(\theta,\phi)=1$, $\theta_0=\pi/2$, $u=kd\cos\theta$, and $E(\theta,\phi)=S_u(\theta)$. The basic characteristics of this array may be summarized as follows.

Beam Maximum It is clear that $S_{\mu}(\theta)_{\text{max}} = n$ (the total number of elements) when $\theta = \pi/2$ or u = 0.

Nulls If we express Eq. (3-4) in a different form such as

$$|S_u|^2 = S_u S_u^* = \frac{1 - \cos nu}{1 - \cos u} = \frac{\sin^2(nu/2)}{\sin^2(u/2)}$$
 (3-5)

it is easy to see that the null positions $(S_u = 0)$ are given by

$$nu_m/2 = m\pi ag{3-6a}$$

or

$$\cos \theta_m = m\lambda/nd, m = \pm 1, \pm 2, \dots, \pm M \le nd/\lambda$$
 (3-6b)

where $\theta_1, \theta_2, \ldots, \theta_M$ are the angular null positions on one side of the beam maximum in the forward direction and $\theta_{-1}, \theta_{-2}, \ldots, \theta_{-M}$ are null positions on the other side of

the beam maximum, also in the forward direction. Of course, $\theta_{\pm m}$ are symmetrically located with respect to the beam maximum. It is clear from Eq. (3-6a) that $u=\pm \pi$ are always possible null positions when n is even and $d \ge \frac{1}{2}\lambda$. The exact number and locations of null positions as given by Eq. (3-6b) depend on n and d/λ (or approximately the overall array length). A designer may have choices of different arrays to produce a null in a particular direction in order to minimize possible interferences at this direction. For example, the arrays of four elements with $d=3\lambda/8$ or $3\lambda/4$, of six elements with $d=\lambda/4$, $\lambda/2$ or $3\lambda/4$, etc., may be used to satisfy the purpose of having a null at $\theta=48.19^{\circ}$ (or 41.81° from the main beam). The final choice among these possibilities should be made from other design or cost considerations.

First-Null Beamwidth One way of showing the directive pattern of a uniform broadside array is by the *first-null beamwidth*, which is defined as the angular space between the first nulls on each side of the main beam,

$$(BW)_1 = \theta_{-1} - \theta_1 = 2\left(\frac{\pi}{2} - \theta_1\right)$$
 rad (3-7a)

OΓ

$$(BW)_1 = 2(90^{\circ} - \theta_1) \tag{3-7b}$$

where θ_1 in Eq. (3-7a) is in radians while that in Eq. (3-7b) is in degrees. For very large arrays, we approximately have

$$(BW)_1 \simeq \begin{cases} 2\lambda/nd & \text{in radians} \\ 360\lambda/\pi nd & \text{in degrees} \end{cases}$$
 (3-8)

Half-Power Beamwidth Another more commonly used beamwidth is the angular space between the half-power points on each side of the main beam. The half-power point u_h may be determined by solving

$$|S_u(u_h)|^2 = \frac{\sin^2{(nu_h/2)}}{\sin^2{(u_h/2)}} = n^2/2$$
 (3-9)

which, in turn, yields the corresponding θ_h in accordance with

$$\cos \theta_h = u_h/kd \tag{3-10}$$

The half-power beamwidth then becomes

$$(BW)_h = \begin{cases} 2\left(\frac{\pi}{2} - \theta_h\right) & \text{in radians} \\ 2(90^{\circ} - \theta_h) & \text{in degrees} \end{cases}$$
 (3-11)

Sample results for (BW) are presented in Fig. 3-2.

Sidelobes Precise locations of the sidelobes of the uniform linear broadside arrays may be found by setting the derivative of Eq. (3-5) to zero, yielding³

$$n \tan (u/2) = \tan (nu/2)$$
 (3-12)

It is clear that $u = \pm \pi$ are possible sidelobe positions when n is odd and $d \ge \lambda/2$. Other solutions of Eq. (3-12) for u in degrees are presented in Table 3-1. The corre-

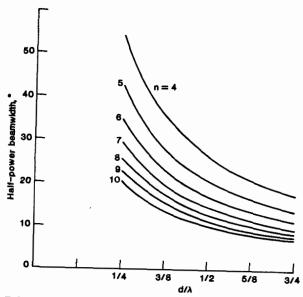


FIG. 3-2 Half-power beamwidths for uniform broadside arrays of isotropic elements.

sponding angular sidelobe positions in terms of θ can be determined by $u = kd \cos \theta$ when the element spacing is known.

The level of the *i*th sidelobe at u_i relative to the beam maximum may be computed as $|S_u(u_i)|/S_u(0) = |S_u(u_i)|/n$. The sidelobe levels in decibels are also included in Table 3-1.

Note from Table 3-1 that the sidelobe positions approach $u_i = \pm (2i+1)\pi/n$ rad or $\pm (2i+1)180^{\circ}/n$, $i=1, 2, 3, \ldots$ (or halfway between nulls) and that the sidelobe levels approach $|S_u(u_i)|/n = 2/(2i+1)\pi$ for arrays with a very large number of elements. In particular, the first sidelobe level of large uniform arrays is $\%\pi$ or -13.46 dB.

Directivity The directive gain of an array in a given direction is defined as the ratio of the radiation intensity in that direction to the average intensity,

$$G(\theta,\phi) = \frac{|E(\theta,\phi)|^2}{W_0/4\pi} = 4\pi |E(\theta,\phi)|^2/W_0$$
 (3-13)

where W_0 representing the total power radiated by the array is given by

$$W_0 = \int_0^{2\pi} \int_0^{\pi} |E(\theta, \phi)|^2 \sin \theta \ d\theta \ d\phi$$
 (3-14)

The directivity of the array is the maximum value of the directive gain,

$$D = G(\theta, \phi)_{\text{max}} = 4\pi |E(\theta, \phi)|_{\text{max}}^2 / W_0$$
 (3-15)

TABLE 3-1 Sidelobe Locations and Levels for Uniform Linear Broadside Arrays of Isotropic Elements

Level, dB

Position, (u_4)

Level, dB

Position, (u_3)

Fourth

Third

Second

First

Sidelobe

	Position,	Level, dB	Position, (u_2)	Level, dB	Position, (u_3)	dB dB	. (u,)	₽ 8
4 4 6 6 6 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	±131.81 ±104.48 ± 86.66 ± 74.08 ± 64.71 ± 57.45 ± 51.66	-11.30 -12.04 -12.43 -12.65 -12.80 -12.90	± 180.00 ± 149.12 ± 127.42 ± 111.28 ± 98.79 ± 88.84	-13.98 -15.25 -15.98 -16.43 -16.73	±180.00 ±157.14 ±139.48 ±125.41	-16.90 -17.89 -18.54 -18.99	± 180.00 ± 161.82	- 19.08 - 19.89
Very large	±540/n	-13.46	u/006∓	-17.90	±1260/n	-20.82	±1620/n	-23.01

For the uniform linear broadside array of isotropic elements considered here, we have $f(\theta,\phi) = 1$, $|E(\theta,\phi)|^2 = |S_u|^2$, $u = kd \cos \theta$, and $|E(\theta,\phi)|^2_{\max} = n^2$. The directivity becomes

$$D_b = \frac{(kd)n^2}{(nkd) + 2\sum_{m=1}^{n-1} \frac{n-m}{m} \sin(mkd)}$$
 (3-16)

Note that when $kd = p\pi$ or $d = p\lambda/2$, $p = 1, 2, ..., D_b = n$. It implies that under this condition the directivity is numerically equal to the total number of elements in the array. For other values of kd, the results are presented in Table 3-2. For a given

TABLE 3-2 Directivities for Uniform Linear Broadside Arrays of Isotropic Elements

n d/λ	1/6	1/4	%	1/2	%	3/4	7∕8	1
4	1.28	2.16	3.11	4.00	4.84	5.58	5.29	4.00
5	1.45	2.70	3.83	5.00	6.12	6.97	7.68	5.00
6	1.67	3.17	4.63	6.00	7.30	8.54	9.52	6.00
7	1.93	3.64	5.34	7.00	8.61	10.10	11.22	7.00
8	2.20	4.16	6.10	8.00	9.84	11.55	12.82	8.00
9	2.48	4.68	6.86	9.00	11.07	12.99	14.42	9.00
10	2.74	5.17	7.59	10.00	12.41	14.43	16.10	10.00

n, the directivity is almost linearly proportional to d/λ in the range of $\% \le d/\lambda \le \%$ and then drops to n when $d = \lambda$ where the grating lobe at the same level as that of the main beam appears. For this reason, the element spacing for a fixed-beam broad-side array is normally kept at less than a full wavelength. For arrays designed with beam-scanning capabilities, the element spacing is even smaller. However, the element spacing should not be chosen to be too small for the obvious reasons of obtaining a respectable directivity and minimizing the mutual coupling among the array elements. Thus, the actual value for the element spacing is usually a compromise of the above considerations.

Broadside Arrays with Practical Antennas as Elements

Broadside arrays with practical antennas may be achieved by placing the antenna elements in such a way that the maximum radiation of the element coincides with the desired broadside direction of the array. One example is to place the half-wave or short dipoles collinearly along the array axis as in the case for the well-known Marconi-Franklin antenna. There are, of course, many other arrangements that satisfy the requirement. We consider only the specific example mentioned above.

Arrays of Half-Wave or Short Dipoles The particular arrangement is shown in Fig. 3-3. Although the current distribution on two or more antennas in an array environment is not the same as when the elements are isolated because of the influence of

mutual couplings, the mutual impedance of collinear dipoles is, however, relatively small, and therefore the change in current distribution is not large. This is especially true when the element dipole length is near or less than $\lambda/2.4$ Under the assumption of no mutual coupling, the element pattern may be written as3.4

$$f(\theta,\phi) = \frac{\cos{(kh\cos{\theta})} - \cos{kh}}{\sin{\theta}}$$
 (3-17)

where h is the half length of the individual dipole in wavelength.

For half-wave dipoles, $h = \lambda/4$, $kh = \pi/2$, the element pattern reduces to

$$f(\theta,\phi) = \frac{\cos\left(\frac{\pi}{2}\cos\theta\right)}{\sin\theta}$$
 (3-18)

The maximum radiation of Eq. (3-18) occurs at $\theta = \pi/2$, thus satisfying the requirement. The overall array pattern is then given by

$$E(\theta,\phi) = \frac{\cos\left(\frac{\pi}{2}\cos\theta\right)}{\sin\theta} |S_u|$$
 (3-19)

where S_u is the array factor given in Eq. (3-4).

The null positions remain the same as those determined by Eq. (3-6) except for the introduction of additional nulls at $\theta = 0$ and π owing to the element pattern. Thus, the first-null beamwidth also remains unchanged. Locations and levels of the first few sidelobes do not change much either. The half-power beamwidth becomes naturally somewhat smaller than that with isotropic elements. The directivity is somewhat higher because the directivity for a single half-wave dipole is approximately 1.64 rather than 1.00 for the isotropic case.

For very short dipoles, $h \le \lambda/16$, $kh \le \pi/8$, the element pattern may be shown approximately to be proportional to

$$f(\theta,\phi) = \sin\theta \tag{3-20}$$

Thus, the overall array pattern is proportional to

$$E(\theta,\phi) = \sin\theta |S_u| \tag{3-21}$$

which, again, is not much different from S_u . The directivity in this case can be expressed as3,5

$$D_s = n^2/W_{0s} {(3-22)}$$

where
$$W_{0s} = \frac{2n}{3} + \frac{4}{k^3 d^3} \sum_{m=1}^{n-1} \frac{n-m}{m^3} \sin(mkd)$$
$$-\frac{4}{k^2 d^2} \sum_{m=1}^{n-1} \frac{n-m}{m^2} \cos(mkd)$$
 (3-23)

It is clear that the directivities for $d = \lambda/2$ and $d = \lambda$ are no longer equal to each other. Furthermore, the grating lobe at $\theta = 0$ for $d = \lambda(kd = 2\pi)$ owing to the array factor S_u is now eliminated by the null of the element pattern. The directivity for $d = \lambda$ is therefore expected to be higher than that for $d = \lambda/2$ in this case. Representative results for D_t with n = 4, 5, and 6 are presented in Table 3-3.

Note that the directivities for various cases given in Table 3-3 are numbers, which can be converted into decibels with respect to the isotropic element (dBi) by taking 10 log D_s . The directivity can also be expressed relative to that of a single element. Since the directivity of a single short dipole is 1.5, the directivity of arrays with short dipoles relative to a single short dipole in decibels is then given by $D_{sr} = 10 \log (D_s/1.5)$. Directivities for arrays with a larger number of short dipoles in this latter unit are given in Fig. 3-4.

TABLE 3-3 Directivities for Uniform Broadside Arrays of Collinear Short Dipoles

n d/λ	1/4	3 %	1/2	%	3/4	%	1
4	2.45	3.39	4.29	5.21	6.05	6.84	6.95
5	2.94	4.05	5.30	6.45	7.55	8.59	8.86
6	3.44	4.87	6.29	7.81	9.15	10.37	10.77

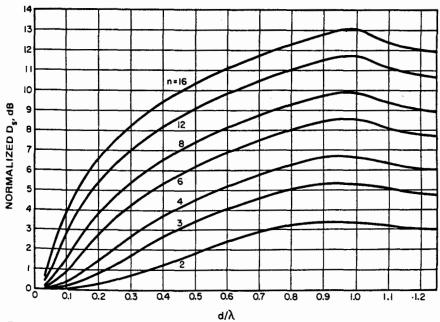


FIG. 3-4 Directivities for a broadside array of collinear short dipoles (relative to a single element).

Ordinary End-Fire Arrays of Isotropic Elements

When the condition $\theta_0 = 0$ is imposed upon Eq. (3-3), an ordinary end-fire array results. The visible range for u = kd (cos $\theta - 1$) corresponding to $0 \le \theta \le 180^{\circ}$ is then $-2kd \le u \le 0$. The basic characteristics for the uniform ($I_l = 1$) ordinary end-fire array of isotropic elements $[f(\theta) = 1]$ are again summarized first and then are compared with those for the broadside array presented in the subsection "Broadside Arrays of Isotropic Elements." Samples of end-fire arrays with properly phased practical elements or parasitic elements (short Yagi-Uda arrays of small number of dipoles) are discussed in the following subsection.

Beam Maximum Since the array factor in terms of u remains unchanged, the beam maximum is still numerically equal to n, which occurs at u = 0 or $\theta = 0$.

Nulls The expression [Eq. (3-6a)] for determining the null positions still applies provided that $m = -1, -2, \ldots$ The exact number of nulls depends on n and d/λ . In terms of θ , the null positions are given by

$$\cos \theta_m = 1 + \frac{m\lambda}{nd}, m = -1, -2, \dots$$
 (3-24)

First-Null Beamwidth The first-null beamwidth for the ordinary end-fire array is defined as

$$(BW)_1 = 2\theta_{-1} = 2 \cos^{-1} \left(1 - \frac{\lambda}{nd}\right)$$
 (3-25)

For very large arrays, θ_{-1} is small, yielding

$$(BW)_1 \simeq 2 \sqrt{\frac{2\lambda}{nd}}$$
 rad (3-26)

By comparing Eqs. (3-26) and (3-8), we conclude that the first-null beamwidth for the ordinary end-fire array is always wider than that for the broadside array with the same n and d/λ .

Half-Power Beamwidth Equation (3-9) is still valid for determining the half-power point u_h (taking the smallest negative solution), which in turn gives

$$\cos\theta_h = 1 + \frac{u_h}{kd} \tag{3-27}$$

The half-power beamwidth thus becomes

$$(BW)_h = 2\theta_h = 2\cos^{-1}\left(1 + \frac{u_h}{kd}\right)$$
 (3-28)

Sample results for (BW), for the uniform ordinary end-fire array are given in Fig. 3-5.

Comparing Fig. 3-5 with Fig. 3-2 also reveals that when the beam position changes from the broadside direction ($\theta_0 = 90^{\circ}$) to the end-fire direction ($\theta_0 = 0$), the half-power beamwidth becomes broader for an array with the same n and d/λ .

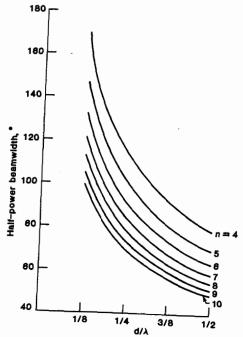


FIG. 3-5 Half-power beamwidths for uniform ordinary end-fire arrays of isotropic elements.

The degree of beam broadening depends on the array length and θ_0 (the position of the beam maximum). For beam-scanning applications in which θ_0 is being changed gradually, beam broadening should be an important factor to consider in the design. Changes in half-power beamwidths with respect to θ_0 are presented in Fig. 3-6 for n = 10 and various element spacings. The limit of scanning is also indicated in the figure.

Sidelobes Equation (3-12) and the first few sidelobes (positions and levels) given in Table 3-1 for the uniform broadside array are also good for the end-fire array, with the understanding that only the negative solutions for u are to be taken from Eq. (3-12) or Table 3-1. The corresponding sidelobe positions in terms of θ are then obtained from u = kd (cos $\theta - 1$). The element spacing d is normally kept less than $\lambda/2$ for an end-fire array because the grating lobe will appear with this particular value of d.

Directivity The directivity for the uniform ordinary end-fire array may be expressed as³

$$D_{e} = \frac{(kd)n^{2}}{nkd + \sum_{m=1}^{n-1} \frac{n-m}{m} \sin(2mkd)}$$
 (3-29)



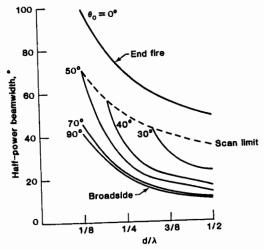


FIG. 3-6 Half-power beamwidths for a uniform array of 10 isotropic elements as a function of beammaximum position.

Note that the second term in the denominator of Eq. (3-29) vanishes when $kd = p\pi/2$ or $d = p\lambda/4$, $p = 1, 2, \ldots$ Under this condition, $D_e = n$. For other values of kd, the results of D_e can be easily obtained from D_b given in Table 3-2. For the same n, D_e for a value of d is equal to D_b for 2d. For example, for n = 4, $D_e(d = \lambda/8) = D_b(d = \lambda/4)$, which is 2.16 in accordance with Table 3-2. This fact is obvious if Eqs. (3-16) and (3-29) are carefully examined.

Ordinary End-Fire Arrays of Practical Antennas as Elements

End-fire arrays of practical elements may be realized by proper arrangements of the antenna elements. One example which will be discussed here is to place short dipoles

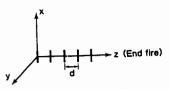


FIG. 3-7 An equally spaced linear array of parallel short dipoles.

parallel to the x axis, forming an array along the z axis as shown in Fig. 3-7. Another method is to excite only one antenna element and leave the other elements unexcited (parasitic) with appropriate antenna lengths and spacings to produce approximate phase distributions among the elements required for end-fire radiation. This latter arrangement is known as the Yagi-Uda array.

Since the current amplitudes on the elements of a Yagi-Uda array are no longer the same $(I_i \neq 1)$, the array cannot, strictly speaking, be considered as a uniform array. For this reason, characteristics of short Yagi-Uda arrays (with a small number of dipoles) are presented in a separate section. Long Yagis treated from the viewpoint of surface-wave antennas are given in Chap. 12.

For the array of parallel short dipoles as shown in Fig. 3-7, the general element pattern is given by $f(\theta,\phi) = (1 - \sin^2\theta \cos^2\phi)^{1/2}$. The element pattern in the xz plane $(\phi = 0)$ reduces to $f(\theta) = \cos\theta$, which does have the maximum radiation at the end-fire direction $(\theta = 0)$. When the elements are excited with equal amplitude and progressive phases, an end-fire array results. The overall array pattern then, neglecting the mutual-coupling effect, becomes

$$E(\theta) = \cos \theta |S_u(u)| \qquad (3-30)$$

where $u = kd (\cos \theta - 1)$.

Clearly, the element pattern produces a null at $\theta = \pi/2$ which may or may not be a null for S_{ν} . Since $E_{\text{max}} = E(0) = n$, we obtain, using Eq. (3-15), the directivity as^{3.5}

$$D_p = n^2/W_{0p} ag{3-31}$$

where

$$W_{0p} = \frac{2n}{3} + \frac{1}{kd} \sum_{m=1}^{n-1} \frac{n-m}{m} \left(1 - \frac{1}{m^2 k^2 d^2} \right) \sin(2mkd)$$

$$+ \frac{2}{k^2 d^2} \sum_{i=1}^{n-1} \frac{n-m}{m^2} \cos^2(mkd)$$
(3-32)

Representative results for D_p are presented in Table 3-4. Directivities relative to that of a single element, which are shown in Fig. 3-8, may be compared with those in Fig. 3-4.

TABLE 3-4 Directivities for Uniform Ordinary End-Fire Arrays of Parallel Short Dipoles.

$n \frac{d}{\lambda}$	1/6	14	%	1/2
4	3.21	5.21	6.89	4,71
5	3.83	6.26	8.33	5.74
6	4.31	7.33	9.99	6.77

3-3 YAGI-UDA ARRAYS

The typical Yagi-Uda array consists of many parallel dipoles with different lengths and spacings as shown in Fig. 3-9. Only one of the dipoles is driven. All the other elements are parasitic and may function respectively as a reflector or as a director. Arrays of this kind were first described in Japanese by S. Uda⁷ and subsequently in English by H. Yagi. In general, the longest element, of the order $\lambda/2$ in length, is the reflector. The director elements are always shorter than the driven element in length. Although there may, in principle, be many reflectors, experience shows that little is gained by having more than one reflector. The reflector is usually spaced $\lambda/4$ to the

rear of the driven element. Considerable gain can be realized by adding numerous directors. The simplest Yagi-Uda has only one director, making a three-element array.

Since the element patterns for each dipole are different, the principle of pattern multiplication certainly does not apply. The element pattern of the *i*th dipole in the xz plane is given by³

$$f_i(\theta) = \frac{\cos(kh_i \sin \theta) - \cos kh_i}{\cos \theta}$$
 (3-33)

where h_i is the half length of the *i*th dipole.

The overall array pattern may be written as

$$E(\theta) = \sum_{i=1}^{n} I_i f_i(\theta) \exp(jkd_{i-1}\cos\theta)$$
 (3-34)

where n is the total number of dipoles in the array, $d_0 = 0$, and I_l is the maximum current amplitude of the *i*th dipole, which may be determined by the available method.³

The power gain may be computed by $G(\theta,\phi) = 60|E(\theta)|^2/P_{\rm in}$, where $P_{\rm in} = \frac{1}{2} |I_{b2}|^2 R_{\rm in}$ represents the input power. $R_{\rm in}$ is the input resistance, and I_{b2} is the base current of the driven element. As an example, the normalized pattern with n=3, $h_1=0.26\lambda$, $h_2=0.25\lambda$, $h_3=0.23\lambda$, $d_1=0.25\lambda$, $d_2=0.45\lambda$ and dipole radius of 0.001 m is shown in Fig. 3-10 to demonstrate that the Yagi-Uda is indeed designed as an end-fire array (beam maximum at $\theta=0$). For this example, the normalized base currents in amperes, with the assumption of a three-term current distribution, θ are

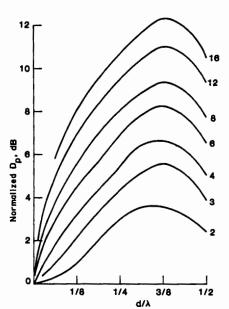


FIG. 3-8 Directivities for ordinary end-fire arrays of parallel short dipoles (relative to a single element).

$$I_{b1}/V_2 = 0.0038334 \exp(j 69.86^{\circ})$$

$$I_{b2}/V_2 = 0.014546 \exp(-j 43.16^\circ)$$

$$I_{b3}/V_2 = 0.009361 \exp(j 166.97^{\circ})$$

We see here that I_{b2} has an approximate phase lag of 113° relative to I_{b1} , although the phase difference should ideally be $-kd_1 = -90^\circ$. Similarly, the phase difference between I_{b3} and I_{b1} is approximately -263° rather than $-kd_2 = -162^\circ$. Nevertheless, it is because of this kind of phase distribution approximately in the right direction over the Yagi-Uda elements that the end-fire pattern is pro-

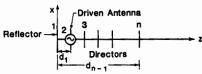


FIG. 3-9 A typical Yagi-Uda array.

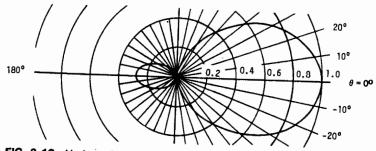


FIG. 3-10 Horizontal pattern for a three-element Yagi-Uda array with $h_1=0.26\lambda$, $h_2=0.25\lambda$, $h_3=0.23\lambda$, $d_1=0.25\lambda$, $d_2=0.45\lambda$, and dipole radius = 0.001 m.

duced. The input resistance for this example is approximately $R_{\rm in} = 50.1~\Omega$, and the power gain is about G = 5.01 or 7.0 dBi.

As another example, for n = 4, $h_1 = 0.26\lambda$, $h_2 = 0.25\lambda$, $h_3 = h_4 = 0.23\lambda$, $d_1 = 0.25\lambda$, $d_2 = 0.52\lambda$, $d_3 = 0.88\lambda$, and dipole radius = 0.001 m, we obtain $R_{\rm in} = 82.8 \,\Omega$, and G = 5.92 or 7.72 dBi.

An analytical method, as well as perturbational procedures, is available for maximizing the Yagi-Uda gain by adjusting the dipole lengths and spacings. ^{10,11} A gain in the order of 10 dBi can be easily designed with only a moderate number of dipoles in the array. Yagi-Uda arrays with a large number of dipoles are treated in Chap. 12 as surface-wave antennas.

3-4 IMPROVED END-FIRE ARRAYS

The ordinary end-fire array with u = kd (cos $\theta - 1$) has been presented in Sec. 3-2. It has been known that an increase in directivity may be realized by increasing the progressive phase lag beyond that for an ordinary end fire by a phase quantity $\delta > 0.12$ More specifically, it was concluded that a maximum directivity which may be realized is given approximately by

$$D_m \cong \frac{7.28nd}{\lambda} \tag{3-35}$$

when

$$\delta \cong \frac{2.94}{n-1} \quad \text{rad} \tag{3-36}$$

which is known as the Hansen-Woodyard condition for maximizing the directivity of end-fire arrays and was reached on the basis of a formulation for line-aperture arrays with a continuous excitation. Its applicability to the equally spaced discrete array is therefore subject to the conditions that the number of elements in the array is very large and that the overall array size, (n-1)d, is much greater than a wavelength. An exact formulation for determining the required optimum additional phase lag δ for the discrete array was made later to obtain the maximum directivity for any n and d.

For the purpose of clarity, we have designated the one considered in the subsec-

tion "Ordinary End-Fire Arrays of Isotropic Elements" as the ordinary end-fire and call the case being presented here as the improved end-fire array.

The array factor in terms of u for the improved uniform ($I_t = 1$) end-fire array remains the same as that in Eq. (3-5). That is,

$$|S_u|^2 = \frac{\sin^2{(nu/2)}}{\sin^2{(u/2)}}$$
 (3-37)

provided that

$$u = kd (\cos \theta - 1) - \delta \tag{3-38}$$

which is herein called the improved end-fire condition.

From Eq. (3-38), it can be seen that the location of the beam maximum has been shifted to $u = -\delta$, which corresponds to $\theta = 0$. The beam-maximum strength thus becomes

$$(S_u)_{\text{max}} = \frac{\sin(n\delta/2)}{\sin(\delta/2)}$$
 (3-39)

which is smaller than n for the ordinary end-fire case. Naturally, for a given n, δ cannot be too large in order to have a respectable $(S_u)_{max}$.

Null and sidelobe positions are similarly shifted. More specifically, the first-null position is determined by

$$\theta_1 = \cos^{-1}\left(1 - \frac{\lambda}{nd} + \frac{\delta}{kd}\right) \tag{3-40}$$

The half-power point u_h can be obtained from

$$\frac{\sin^2{(nu_h/2)}}{\sin^2{(u_h/2)}} = \frac{\sin^2{(n\delta/2)}}{2\sin^2{(\delta/2)}}$$
 (3-41)

which, in turn, yields

$$\theta_h = \cos^{-1}\left(1 + \frac{u_h + \delta}{kd}\right) \tag{3-42}$$

Again the selection of the smallest negative solution from Eq. (3-41) is understood. Since $\delta > 0$, both the first-null and half-power beamwidths, $(BW)_1 = 2\theta_1$ and $(BW)_h = 2\theta_h$, obtained respectively from Eqs. (3-40) and (3-42), should be smaller than those for the ordinary end fire, where $\delta = 0$. Numerical results for $(BW)_h$ are shown in Fig. 3-11.

Although the sidelobe levels relative to the main beam are increased slightly, the overall directivity is always increased because of the improvement in beamwidth. For the improved uniform end-fire array of isotropic elements, the directivity may be computed as follows:³

$$D_{l} = \frac{kd \frac{\sin^{2}(n\delta/2)}{\sin^{2}(\delta/2)}}{nkd + 2 \sum_{m=0}^{n-1} \frac{n-m}{m} \sin(mkd) \cos(mkd + m\delta)}$$
 (3-43)

Sample results for D_i with a typical element spacing of $d = \lambda/4$ are presented in Table 3-5, where the optimum δ required to produce the maximum directivity can be easily

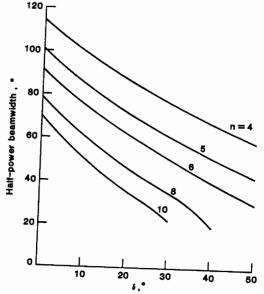


FIG. 3-11 Half-power beamwidths for improved endfire arrays with $d = \lambda/4$.

TABLE 3-5 Directivities for Uniform Improved End-Fire Arrays of Isotropic Elements with $kd=\pi/2$ (δ in Degrees)

\ .					,	Degl ees	• • • • • • • • • • • • • • • • • • • •	
$\frac{\delta}{2}$	0	10	20	30	40	50	60	70
	3 4 5 6	3.45 4.92 6.37 8.10	3.90 5.89 7.72 10.06	4.29 6.72 8.68 10.56	4.71 7.04 8.37 7.20	4.98 6.30 5.57	5.03	4.68

observed. For larger numbers of elements, the directivities relative to those for the ordinary end-fire arrays are given in Fig. 3-12. The corresponding phases satisfied by the Hansen-Woodyard condition [Eq. (3-36)] are also indicated in the figure for comparison purposes.

3-5 LINEAR ARRAYS WITH TAPERED EXCITATIONS—EQUAL SIDELOBES

The first sidelobe level realized from linear arrays with a constant amplitude excitation approaches $2/(3\pi)$ or -13.46 dB when n is very large, as indicated in Table 3-1. If this sidelobe level is considered too high for specific applications, nonuniform amplitude or tapered excitations are normally used to reduce the sidelobe to an accept-

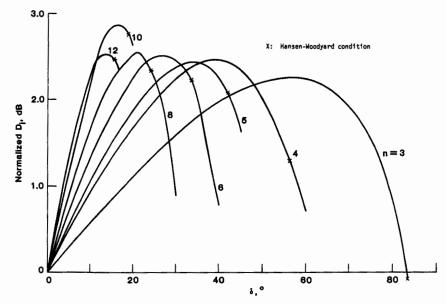


FIG. 3-12 Normalized directivities (relative to the ordinary end fire) for uniform improved end-fire arrays of isotropic elements with $d = \lambda/4$.

able level. One method for achieving this objective is the well-known Dolph-Chebyshev array, ¹⁴ in which all the sidelobes are set at the same level. This array is considered optimum in the sense that the first-null beamwidth is minimum for a specified sidelobe level or that the sidelobe level is minimum for a specified first-null beamwidth. However, the above statement is true for broadside arrays only with an element spacing no less than one-half wavelength or for ordinary end-fire arrays in which the element spacing is no less than one-quarter wavelength.¹⁵ Many others have also devised methods for optimizing the sidelobe and first-null-beamwidth relationship for special cases.^{16,17} All these methods are essentially based on manipulation of Chebyshev polynomials.

A New Approach for Treating Optimum Broadside and End-Fire Arrays

An alternative unified approach is to deal with the power pattern in the form of a polynomial of (n-1)th degree with real coefficients, ^{3,18} where n is the total number of elements in the array. This approach has advantages that it not only applies to the array yielding equal sidelobes with a specialized tapered amplitude excitation but also is valid for other linear arrays including the uniform array considered in Sec. 3-2. Basically, the power pattern for a linear array with n equally spaced isotropic elements may be expressed as

$$P(y) = \sum_{m=0}^{n-1} A_m y^m$$
 (3-44)

where
$$y = 2 \cos u$$
 $u = kd (\cos \theta - \cos \theta_0)$ (3-45)

and the coefficients A_m are real. When, in addition, the array has a symmetrical amplitude excitation, as is the case in practice, the power pattern takes the following product forms:

$$P_0(y) = \prod_{m=1}^{(n-1)/2} (y + b_m)^2$$
 for odd n (3-46)

or

$$P_e(y) = (y + 2) \prod_{m=1}^{(n-2)/2} (y + b_m)^2$$
 for even n (3-47)

where all b_m 's are real.

Note that both $P_0(y)$ and $P_e(y)$ are nonnegative in the visible range $-2 \le y \le 2$, as representing the power pattern they should be. In addition, if the *m*th null is visible, we require $|b_m| < 2$. If all the nulls do not coincide, b_m 's must also be distinct. Thus, there are at most (n-1)/2 independent real nulls for odd n and n/2 independent real nulls for even n. Further, if y=2 or u=0 is the desired beam-maximum position, the combination of b_m 's cannot be arbitrary.

The required amplitude excitations for the power patterns in Eqs. (3-46) and (3-47) may be shown as the coefficients of the following array polynomials:

$$S_0(z) = \prod_{m=1}^{(n-1)/2} (1 + b_m z + z^2)$$
 for odd n (3-48)

and

$$S_{\epsilon}(z) = (1+z) \prod_{m=1}^{(n-2)/2} (1+b_m z + z^2)$$
 for even n (3-49)

where

$$z = \exp(ju) \tag{3-50}$$

For an example, when n = 7 (odd), we have

$$P_0(y) = (y + b_1)^2 (y + b_2)^2 (y + b_3)^2$$
 (3-51)

and

$$S_0(z) = (1 + b_1 z + z^2)(1 + b_2 z + z^2)(1 + b_3 z + z^2)$$

$$= 1 + (b_1 + b_2 + b_3)z + (3 + b_1 b_2 + b_2 b_3 + b_1 b_3)z^2$$

$$+ (2b_1 + 2b_2 + 2b_3 + b_1 b_2 b_3)z^3 + (3 + b_1 b_2 + b_2 b_3 + b_1 b_3)z^4$$

$$+ (b_1 + b_2 + b_3)z^5 + z^6$$
(3-52)

Thus, the required amplitude excitations for the linear array of seven elements are respectively

1,
$$(b_1 + b_2 + b_3)$$
, $(3 + b_1b_2 + b_2b_3 + b_1b_3)$, $(2b_1 + 2b_2 + 2b_3 + b_1b_2b_3)$, ... (3-53)

Note that the excitation coefficients are symmetrical.

As another example, when n = 6 (even), we have

$$P_{\epsilon}(y) = (y+2)(y+b_1)^2(y+b_2)^2$$
 (3-54)

and

$$S_e(z) = (1+z)(1+b_1z+z^2)(1+b_2z+z^2)$$
 (3-55)

which yields, after expansion, the required amplitude excitations as

1,
$$(1 + b_1 + b_2)$$
, $(2 + b_1 + b_2 + b_1b_2)$, ... (3-56)

Again, the excitations are symmetrical.

With Eqs. (3-46) and (3-47), a variety of arrays may be synthesized. For example, one may wish to produce three distinct nulls at desired directions, which essentially specifies b_1 , b_2 , and b_3 for an array of seven elements. From Eq. (3-52) or Eq. (3-53), the required amplitude excitations can be easily determined. Of course, the other array characteristics such as the sidelobe locations and levels and the directivity are also fixed accordingly. As a second example, if a uniform excitation is desired for an array of six elements, it equivalently requires, in accordance with Eq. (3-56), that $b_1 + b_2 = 0$ and $b_1b_2 = -1$. The solutions are simply $b_1 = -1$ and $b_2 = 1$. This implies that the first two nulls are given by $y = 2 \cos u_1 = 1$ and $y = 2 \cos u_2 = -1$, which yields respectively $u_1 = \pm 60^\circ$ and $u_2 = \pm 120^\circ$. From Eq. (3-54), we see that a third null is given by y = -2 or $u_3 = \pm 180^\circ$. The corresponding angular null positions and the other array characteristics can also be computed once the element spacing d and the beam-maximum position θ_0 are known or specified. The results of this example agree, of course, with those presented in Sec. 3-2.

Equations (3-46) and (3-47) can also be used to synthesize arrays with equal sidelobes. Locations for the sidelobes may be obtained by setting dP(y)/dy = 0. Thus, $dP_0(y)/dy = 0$ for the odd-n case gives (n-3)/2 values of y_i 's, namely, $y_1, y_2, \ldots, y_{(n-3)/2}$. Note that $y_i \neq -b_m$, $m = 1, 2, \ldots, (n-1)/2$, which have already been identified as the nulls. Note further that y = -2 ($u = \pm 180^\circ$) is another sidelobe as evidenced by Eq. (3-12). To ensure that all the sidelobes are at the same level, we then set

$$P_0(y_1) = P_0(y_2)$$

 $P_0(y_2) = P_0(y_3)$ (3-57)

$$P_0(y_{(n-5)/2}) = P_0(y_{(n-3)/2})$$

and

$$P_0(y_{(n-3)/2}) = P_0(-2)$$

or a total of (n-3)/2 independent equations. If we require that $P_0(2)$ be the beam maximum (which is normally true) and have another condition such as $P_0(2)/P_0(-2) = K^2$ representing a desired sidelobe level relative to the main beam or, alternatively, a value for b_1 representing a desired first null, we will have enough equations to solve for the (n-1)/2 unknowns, namely b_m , $m=1, 2, \ldots, (n-1)/2$.

Similarly, for the even-n case $dP_e(y)/dy = 0$ gives (n-2)/2 values of y_i 's, namely, $y_1, y_2, \ldots, y_{(n-2)/2}$. Again $y_i \neq -b_m$. Note that y = -2 ($u = \pm 180^\circ$) is a null in this case. We then set

$$P_{\epsilon}(y_1) = P_{\epsilon}(y_2)$$

$$P_{\epsilon}(y_2) = P_{\epsilon}(y_3)$$

and

$$P_{\epsilon}(y_{(n-4)/2}) = P_{\epsilon}(y_{(n-2)/2})$$
 (3-58)

which consist of a total of (n-4)/2 independent equations to ensure equality of all the sidelobes. If we also have another condition $P_e(2)/P_e(y_1) = K^2$ or a value for b_1 as in the odd-n case above, we then can solve for the (n-2)/2 unknowns, namely, b_m , $m=1,2,\ldots,(n-2)/2$.

Since the sidelobes are set to be equal, the null positions $(y = -b_m)$ and the sidelobe positions $(y = y_l)$ are all related. Specifically, we expressed all the parameters in the following condensed ratio form,

$$(2-b_1):(2-b_2): \dots : (2-b_{(n-1)/2}):(2+y_1):(2+y_2): \dots : (2+y_{(n-3)/2})$$

$$= \cos^2\left(\frac{\pi}{2(n-1)}\right):\cos^2\left(\frac{3\pi}{2(n-1)}\right): \dots : \cos^2\left(\frac{(n-2)\pi}{2(n-1)}\right):\cos^2\left(\frac{\pi}{n-1}\right):$$

$$\cos^2\left(\frac{2\pi}{n-1}\right): \dots : \cos^2\left(\frac{(n-3)\pi}{2(n-1)}\right) \quad \text{for odd } n$$
(3-59)

and

$$(2 - b_1):(2 - b_2): \dots :(2 - b_{(n-2)/2}):(2 + y_1):(2 + y_2): \dots :(2 + y_{(n-2)/2})$$

$$= \cos^2\left(\frac{\pi}{2(n-1)}\right):\cos^2\left(\frac{3\pi}{2(n-1)}\right): \dots :\cos^2\left(\frac{(n-3)\pi}{2(n-1)}\right):\cos^2\left(\frac{\pi}{n-1}\right):$$

$$\cos^2\left(\frac{2\pi}{n-1}\right): \dots :\cos^2\left(\frac{(n-2)\pi}{2(n-1)}\right) \quad \text{for even } n$$
(3-60)

where we have arranged the null and sidelobe positions in the following order:

$$2 > -b_1 > y_1 > -b_2 > y_2 > \dots > y_{(n-3)/2} > -b_{(n-1)/2} > -2$$
 for odd n (3-61)

and

$$2 > -b_1 > y_1 > -b_2 > y_2 > \dots > -b_{(n-2)/2}$$

> $y_{(n-2)/2} > -2$ for even n (3-62)

It is convenient to express, for a given n, b_m ($m \ge 2$) and y_i (all i) in terms of b_1 first. For the case in which K^2 is specified, this reduces the entire problem to only one equation, $P_0(2)/P_0(-2) = K^2$ or $P_e(2)/P_e(y_1) = K^2$, representing the desired sidelobe level, from which b_1 may be solved numerically. This should not be a difficult task since $y = -b_1$ represents the first null. For a very large n, b_1 is close to -2. On the other hand, for the case in which a desired first null (b_1) is specified, all the other b_m 's and y_i 's can be easily determined from Eq. (3-59) or Eq. (3-60), and the resultant sidelobe level can be obtained by computing $P_0(2)/P_0(-2)$ or $P_e(2)/P_e(y_1)$.

It is instructive to demonstrate in Fig. 3-13 how b_1 varies with K^2 and n. In general, for a given n, b_1 always increases with K^2 . For one extreme situation when the sidelobe level is set to be minus infinity in decibels or equivalently when K^2 approaches infinity, b_1 and, in fact, all the other b_m 's will approach 2 as their limits. Under this condition, the power pattern P(y) will approach $(y + 2)^{n-1}$. The required amplitude excitations, according to Eq. (3-48) or Eq. (3-49), will be the expansion coefficients of $(1 + z)^{n-1}$, which is the so-called binomial array. Thus, the arrays of equal sidelobes discussed herein include the binomial array as a special case in which all the sidelobes are equal to $-\infty$ decibels with respect to the beam maximum. Cer-

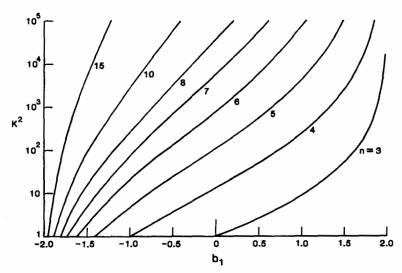


FIG. 3-13 First-null positions and sidelobe-level relationships for arrays with equal sidelobes.

tainly, the accomplishment of a very low sidelobe level is at the expense of wide beamwidth and highly tapered amplitude excitations. The other extreme situation occurs when the sidelobe level is set at a very high level or when K^2 approaches unity. Under this condition, the sidelobes are at the same level as that for the main beam. The value for b_1 may be determined from Fig. 3-13, and the other b_m 's and y_i 's can be obtained from Eq. (3-59) or Eq. (3-60). The required amplitude excitations computed from Eq. (3-48) or Eq. (3-49) will vanish except for the first and last elements, exhibiting a so-called edge distribution.² For the practical case, the sidelobes, beamwidths, and required amplitude excitations are somewhere between these two extremes.

The first-null position in θ can be determined easily from b_1 when the element spacing d and the beam-maximum direction θ_0 are known. That is,

$$kd(\cos\theta_1 - \cos\theta_0) = \cos^{-1}(-b_1/2)$$
 (3-63)

For the broadside array ($\theta_0 = 90^{\circ}$) with $d \ge \lambda/2$ and the ordinary end-fire array ($\theta_0 = 0$) with $d \ge \lambda/4$, the first-null and sidelobe-level relationship shown in Fig. 3-13 is known as the optimum in the sense defined by Dolph. ¹⁴ Of course, the element spacing cannot be allowed to be too large in order to avoid the appearance of a grating lobe. For single-frequency operation, the maximum allowable element spacings for the optimum broadside array (i.e., equal sidelobes) are given in Table 3-6. The maximum allowable element spacings for the corresponding ordinary end-fire arrays of equal sidelobes are just one-half of those listed in Table 3-6.

The amplitude excitations required to produce the optimum array characteristics shown in Fig. 3-13 for n=3 through 8, with the condition on the element spacing satisfied, are presented in Table 3-7. The results are valid for either broadside or ordinary end-fire arrays.

TABLE 3-6 Maximum Allowable Element Spacing in Wavelengths for an Optimum Broadside Array with Equal Sidelobes

n K ²	10 (— 10-dB sidelobe level)	10² (— 20-dB sidelobe level)	10³ (— 30-dB sidelobe level)	10 ⁴ (-40-dB sidelobe level)
3	0.7438	0.6402	0.5796	0.5450
4	0.8179	0.7249	0.6566	0.5452
5	0.8601	0.7813	0.7169	0.6081
8	0.9182	0.8679	0.8216	0.6653
10	0.9365	0.8960	0.8584	0.7794 0.8227

TABLE 3-7 Amplitude Excitations for Optimum Arrays with Equal Sidelobes

n K2	1	10	102	40°	
<u>" \</u>			10²	10³	104
	1	1	1	1	1
3	0	1.039	1.636	1.877	1.960
	1	1	1	1	1
	1	1	1	1	1
4	0	0.879	1.736	2.331	2.669
		sym	metrical		2.007
	1	1	1 .	1	1
5	0	0.724	1.609	2.413	3.013
	0	0.790	1.932	3.140	4.149
		symr	netrical		
	1	1	1	1	1
6	0	0.608	1.437	2.312	3.087
	0	0.681	1.850	3.383	4.975
		symn	netrical		
	1	1	1	1	1
_	0	0.519	1.277	2.151	3.008
7	0	0.586	1.684	3.306	5.269
	0	0.610	1.839	3.784	6,275
		symm	etrical		
	1	1	1	1	1
	0	0.452	1.139	1.978	2.861
8	0	0.510	1.509	3.097	5.200
	0	0.541	1.725	3.815	6.848
		symm	etrical		

The directivity for the array with equal sidelobes may also be computed in accordance with Eq. (3-15). In terms of y, we have

$$D = \frac{2P(2)}{\int_0^{\tau} P(y) \sin \theta \ d\theta} = 2kd \ P(2)/W$$
 (3-64)

where

$$W = \int_{y_a}^{y_b} \frac{P(y)}{\sqrt{4 - y^2}} \, dy \tag{3-65}$$

and

$$y_b = 2 \cos [kd(1 + \cos \theta_0)], y_a = 2 \cos [kd(1 - \cos \theta_0)]$$
 (3-66)

For the broadside array, $\theta_0 = 90^{\circ}$, $y_a = y_b$, Eq. (3-65) should be replaced by

$$W = 2 \int_{y_c}^{2} \frac{P(y)}{\sqrt{4 - y^2}} dy$$
 (3-67)

$$v_c = 2\cos kd \tag{3-68}$$

The directivity for the optimum broadside array with various sidelobe levels has been extensively computed.²⁰ Sample results for $d = \lambda/2$ are presented in Fig. 3-14, from which we may conclude (1) that, for a specified sidelobe level, the directivity always increases with the total number of elements in the array and (2) that, for a given n, the directivity does not always increase when the sidelobe level is decreased. The results shown in Fig. 3-14 are, of course, also valid for the ordinary end-fire array with equal sidelobes and with $d = \lambda/4$.

Optimum Broadside Arrays When $d<\lambda/2$

It was noted previously that the first-null and sidelobe-level relationship shown in Fig. 3-13 is optimum in Dolph's sense for the broadside array of equal sidelobes only when

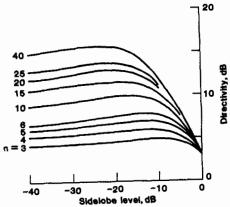


FIG. 3-14 Directivities for optimum broadside arrays of equal sidelobes when $d = \lambda/2$.

the element spacing is no less than one-half wavelength. When $d < \lambda/2$, the visible range of u will be $-\pi < -kd < u < kd < \pi$. Consequently, some of the nulls and sidelobes will disappear into the invisible region so that the final radiation pattern does not contain the maximum possible number of nulls and sidelobes. For this reason, the results shown in Fig. 3-13 and Table 3-7 no longer yield optimum characteristics (first-null-position and sidelobe-level relationships) for the broadside array. If, however, a transformation such as

$$y' = A_1 y + A_2 (3-69)$$

with

$$A_1 = \frac{1}{2}(1 - \cos kd)$$
 and $A_2 = 1 + \cos kd$ (3-70)

is applied so that all the possible nulls and sidelobes originally existing under the condition $d = \lambda/2$ remain in the shrunk visible region of u, the array characteristics obtained after this transformation are still optimum in Dolph's sense.³ The power pattern $P_0(y)$ for the odd-n case and the required amplitude excitations $S_0(z)$ will become respectively

$$Q_0(y') = \prod_{m=1}^{(n-1)/2} (y' + B_m)^2$$
 (3-71)

and

$$S_0'(z) = \prod_{m=1}^{(n-1)/2} (1 + B_m z + z^2)$$
 (3-72)

where

$$B_m = A_1 b_m - A_2, m = 1, 2, ..., (n-1)/2$$
 (3-73)

and b_m 's are still related in accordance with Eq. (3-59).

Note that B_m , since it involves A_1 and A_2 , is now a function of d, although b_m is not.

The directivity becomes

$$D' = \frac{kd Q_0(2)}{\int_{y_c}^2 \frac{Q_0(y') dy'}{\sqrt{4 - y'^2}}}$$
 (3-74)

where
$$y_c' = 2 \cos kd \tag{3-75}$$

Numerical examples are now given to illustrate the point. If the excitation coefficients given in Table 3-7 are still maintained without using the transformation suggested in Eq. (3-69), the directivities for the broadside arrays with equal sidelobes for n = 5 and 7 are presented as solid curves in Fig. 3-15. Clearly, the directivity decreases rather fast when the element spacing becomes smaller than one-half wavelength. The corresponding directivities after the transformation [Eq. (3-69)] is used are presented as dashed curves. Although the directivity still decreases with d, it does not now decrease as fast. To achieve this improvement in directivity for small d, the required new excitation coefficients obtained in accordance with Eq. (3-72) are given

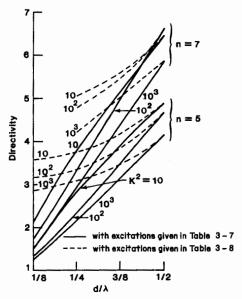


FIG. 3-15 Directivities for broadside arrays of equal sidelobes.

in Table 3-8 and may be compared with the corresponding cases in Table 3-7. The prices paid for the improvement in directivity are, therefore, the possible phase reversal for the even-numbered elements in the array, the requirement of higher accuracies in computing and maintaining the excitation coefficients, and much lower radiation intensities in the broadside direction. Thus, the overall radiation efficiency is very low for this kind of superdirective array.³ Furthermore, the severe mutual couplings among the elements when they are so closely spaced will make the accurate maintenance of desired excitations more difficult. The practicality of superdirective arrays is therefore quite limited unless special care is exercised.²¹ Superdirective arrays for the even-n case are not possible.³

The first-null beamwidths for n = 5 and 7 with and without the transformation [Eq. (3-69)] are given in Table 3-9 for reference purposes.

Optimum End-Fire Arrays When *d* Is Less Than the Maximum Allowable Spacing

The characteristics shown in Fig. 3-13 are also optimum for the ordinary end-fire array with equal sidelobes, provided that the element spacing is no less than $\lambda/4$ and no greater than the maximum allowable element spacing (d_{max}) which is required to avoid the grating lobe. The d_{max} values for the ordinary end-fire arrays with various n and K^2 are just one-half of those presented in Table 3-6. Under the above conditions, the sidelobe and first-null relations shown in Fig. 3-13 can be realized by the excitations listed in Table 3-7. Naturally, for single-frequency operation, we should always use d_{max} to obtain the narrowest beamwidth for a given sidelobe level. When the actual

TABLE 3-8 Amplitude Excitations for Optimum Broadside Arrays with Equal Sidelobes when $d < \lambda/2$

n	K	10	10²	10³
	<i>d</i> = %λ	1 0.0324 1.0231 symmetrical	1 0.7874 1.6343	1 1.4734 2.3130
5	<i>d</i> = ½λ	1 1.6378 2.3350 symmetrical	1 -1.1956 2.1787	1 -0.7937 2.0788
	<i>d</i> = %λ	1 3.3081 4.7072 symmetrical	1 -3.1786 4.5106	1 -3.0609 4.3355
7	<i>d</i> = %λ	1 -0.4354 1.2395 -0.6091 symmetrical	1 0.2151 1.6635 0.3336	1 0.9561 2.4046 1.6577
	<i>d</i> = ½λ	1 -2.7403 4.8773 -5.6712 symmetrical	1 -2.3593 4.3917 -4.8402	1 -1.9252 3.9266 -3.9165

TABLE 3-9 First-Null Beamwidth in Degrees for Broadside Arrays with Equal Sidelobes

	tra [1	Withou Insform Eq. (3-6	ation		With nsform q. (3-6		
$n \stackrel{K^2}{\longrightarrow}$	10	10²	10³	10	10²	10³	
5	59.1 95.4	82.3 161.5	107.4	53.6 61.0 65.2	73.3 82.5 87.3	92.4 102.5 107.4	$d = \frac{1}{\lambda}\lambda$ $d = \frac{1}{\lambda}\lambda$ $d = \frac{1}{\lambda}\lambda$
7	39.1 60.3	54.8 87.3	71.2 121.7	35.9 41.0 44.2	49.9 56.6 60.8	64.1 72.5 77.1	$d = \frac{1}{\lambda}\lambda$ $d = \frac{1}{\lambda}\lambda$ $d = \frac{1}{\lambda}\lambda$

element spacing is less than d_{\max} for scanning or other considerations, parts of the maximum possible number of nulls and sidelobes will be shifted to the invisible region, yielding a wider beamwidth. Thus, the resultant array characteristics are no longer optimum in the Dolph sense. A method for optimizing the array characteristics even when $d < d_{\max}$ is also available.^{3,22} Basically, a nonordinary end-fire condition such as

$$u = kd\cos\theta + \alpha \quad \alpha \neq -kd \tag{3-76}$$

is used together with the transformation [Eq. (3-69)] so that the maximum possible number of nulls and sidelobes under the condition $d = d_{\text{max}}$ is still kept. The required phase α and the transformation coefficients A_1 and A_2 for Eq. (3-69) are given respectively by

$$\tan (\alpha/2) = \cot^2 (kd_{\text{max}}/2) \tan (kd/2)$$
 (3-77)

$$A_1 = -\sin^2\left(\frac{\alpha + kd}{2}\right) \tag{3-78}$$

and

$$A_2 = 2(1 + A_1) = 2\cos^2\left(\frac{\alpha + kd}{2}\right)$$
 (3-79)

Thus, given the total number of elements n and a desired sidelobe level represented by K^2 , we determine first the maximum allowable element spacing d_{max} . The actual element spacing d and d_{max} so determined are used in Eq. (3-77) to obtain α . These values of α and d are then used in Eqs. (3-78) and (3-79) to compute the required transformation coefficients A_1 and A_2 . After the above procedures are completed and Eq. (3-69) is applied, the power pattern given in Eq. (3-46) for the odd-n case remains in the same form as Eq. (3-71). Therefore, the required excitations can still be computed by expanding Eq. (3-72). For the even-n case, the power pattern given in Eq. (3-47) will become

$$Q_s(y') = (2 - y') \prod_{m=1}^{(n-2)/2} (y' + B_m)^2$$
 (3-80)

where B_m is also related to b_m by Eq. (3-73) but with m = 1, 2, ..., (n-2)/2. The required excitations are then obtained by expanding

$$S'_{\epsilon}(z) = (1-z) \prod_{m=1}^{(n-2)/2} (1+B_m z + z^2)$$
 (3-81)

Once the transformation [Eq. (3-69)] has been obtained, the computation of directivity [Eq. (3-15)] for n both odd and even can be achieved. Since the beam maximum is at $\theta = 0$, or $u = kd + \alpha$, or $y' = 2\cos(kd + \alpha)$, the directivity may be expressed as

$$D' = \frac{2kdQ(y'_a)}{\int_{y'_a}^{y'_b} \frac{Q(y') dy'}{\sqrt{4 - y'^2}}}$$
(3-82)

where $y'_a = 2 \cos(kd + \alpha)$ corresponds to $\theta = 0$ and $y'_b = 2 \cos(-kd + \alpha)$ corresponds to $\theta = \pi$ and where Q(y') can be either $Q_0(y')$ or $Q_s(y')$.

Sample results for this newly formulated optimum end-fire array are presented in Figs. 3-16 through Fig. 3-18. First, the directivities computed for the end-fire array

with equal sidelobes of -20 dB ($K^2 = 100$) in accordance with Eq. (3-82) are given in Fig. 3-16 (solid lines). The points marked with x correspond to the cases in which

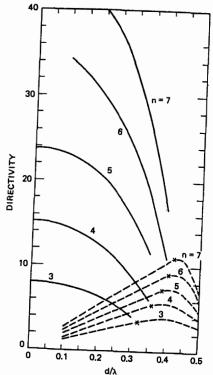


FIG. 3-16 Directivities for end-fire arrays with equal sidelobes of -20 dB ($K^2 = 100$). (After Ref. 3.)

 $d = d_{max}$. More specifically, $d_{max} = 0.3201\lambda$, 0.3625λ , 0.3906λ , 0.4099λ , and 0.4235λ respectively for n = 3, 4, 5, 6, and 7. Corresponding results for the ordinary end-fire array where $u = kd(\cos \theta - 1)$ are also included in the figure (dashed lines) for comparison purposes.

Next, the first-null beamwidths for the optimum and ordinary end-fire arrays of equal sidelobes with $K^2 = 100$ are given in Fig. 3-17. Note that the beamwidth decreases with d for the optimum end-fire array (solid curves) and that it increases when d is decreased for the ordinary end fire (dashed curves).

The required phases α obtained from Eq. (3-77) are presented in Fig. 3-18. It can be easily verified that $\alpha \neq -kd$

The excitations required to produce these characteristics are given in Table 3-10 and are quite different from the corresponding excitations in Table 3-7. Once again, the improvements in directivity and beamwidth for the small element spacings are made possible by the requirement of highly tapered amplitude excitations.

Thus far we have discussed various equally spaced linear arrays. Arrays with nonuniform spacings have also been designed for the purposes of reducing the

average sidelobe level, eliminating the grating lobe, minimizing the total number of elements needed in the array, or broadening the frequency bandwidth. However, this subject is not pursued here.

This section presents extensively the method of producing equal sidelobe level under various conditions. Another popular method with tapered excitations for controlling the sidelobe level is the Taylor distribution. It yields a certain number of equal sidelobes near the main beam with the levels of the remaining sidelobes monotonically decreasing. Details on this method can be found elsewhere. Limited information on this also has been presented in Chaps. 2 and 20.

3-6 ARRAY OF ARRAYS

It often is desirable in practice to form an array out of a number of identical arrays, resulting in a two-dimensional array. If the mutual-coupling effect is again neglected and the principle of pattern multiplication applies when the same kind of antenna

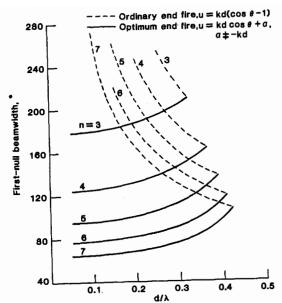


FIG. 3-17 First-null beamwidths for end-fire arrays with equal sidelobes of -20 dB ($K^2 = 100$).

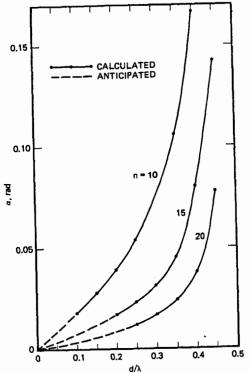


FIG. 3-18 Phases required for optimum end-fire arrays with equal sidelobes of -20 dB. (After Ref. 3.)

TABLE 3-10	Amplitude Excitations for the Optimum End-Fire
Arrays with Eq	ual Sidelobes of -20 dB

$n d/\lambda$	0.4	0.35	0.3	0.25	0.2	0.15
	· · · ·		1	1	1	1
3	••••		1.6418 symi	1.6923 metrical	1.7724	1.8586
		1	1	1	1	1
4		1.7430	1.8791	2.1106	2.3726	2.6212
			symi	metrical		
		1	1	1	1	1
5		1.7279	2.0686	2.5033	2.9579	3.3756
		2.1011	2.6035	3.2867	4.0516	4.8000
			sym	netrical		
	1	1	1	1	1	1
6	1.4496	1.7621	2.2938	2.9195	3.5576	4.1379
	1.8699	2.3831	3.3460	4.6242	6.0889	7.5623
			symr	netrical		
	1	1	1	1	1	1
	1.3587	1.8457	2.5513	3.3571	4.1707	4.9077
7	1.8202	2.6974	4.1787	6.1746	8.5194	10.9290
	1.9972	3.0395	4.8749	7.4641	10.6410	14.0312
			symn	netrical		

elements are used to form an array in the xy plane, the two-dimensional pattern may be simply written as

$$E(\theta,\phi) = f(\theta,\phi)S_x(\theta,\phi)S_y(\theta,\phi)$$
 (3-83)

where $f(\theta,\phi)$ is the element pattern, $S_x(\theta,\phi)$ is the array factor for the x-directed linear array, and $S_y(\theta,\phi)$ is the array factor for the y-directed linear array.

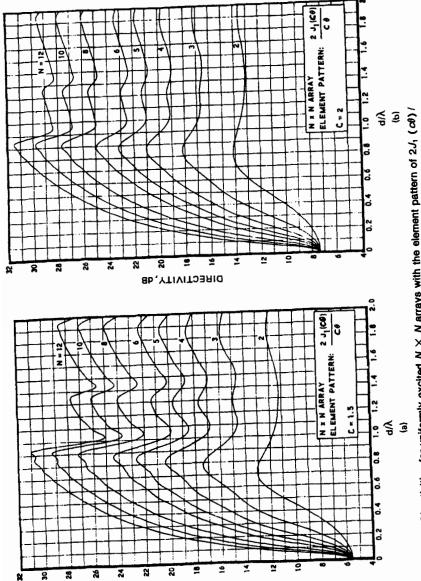
When, in addition, all the elements are equally excited and spaced to produce a beam maximum in the broadside direction ($\theta = 0$), Eq. (3-83) reduces to

$$E(\theta,\phi) = f(\theta,\phi) \frac{\sin(Mu_x/2)}{\sin(u_x/2)} \frac{\sin(Nu_y/2)}{\sin(u_y/2)}$$
 (3-84)

where
$$u_x = kd_x \sin \theta \cos \phi$$
 $u_y = kd_y \sin \theta \sin \phi$ (3-85)

 d_x and d_y are respectively the element spacings for the x- and y-directed arrays, and M and N are respectively the number of elements in x and y directions. Thus, the total number of elements in the planar array is MN.

Arrays of this kind are sometimes referred to as curtains of antennas. The element pattern of various unidirectional types of practical radiating elements such as a



DIRECTIVITY, 4B

FIG. 3-19 Directivities for uniformly excited $N \times N$ arrays with the element pattern of $2J_1(\mathcal{O})/(\mathcal{O})$. (After Ref. 23.) (a) c=1.5. (b) c=2.

dipole in front of a reflector or a slot, helix, or log-periodic type may be adequately approximated by $2J_1(c\theta)/(c\theta)$, where c is a parameter and J_1 is the Bessel function of the first order. On the basis of this approximation, the directivity has been computed for a uniform square array $(M = N \text{ and } d_x = d_y = d)$ as a function of the element spacing d. Sample results are given in Fig. 3-19 to show a designer how to choose an array aperture to realize a desired level of directivity.

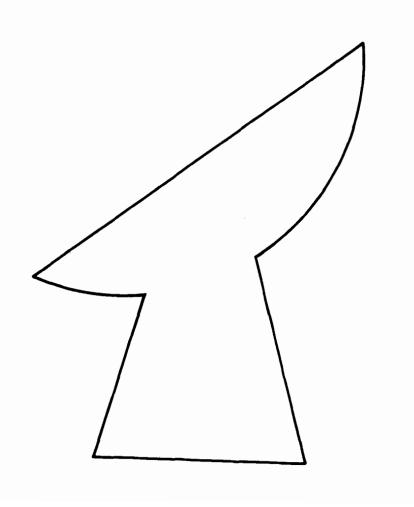
Two-dimensional phased arrays of closely spaced waveguides with thin walls in which the mutual coupling cannot be neglected are discussed in Chap. 20 and elsewhere. ²⁴ Other two-dimensional arrays taking the form of a circle, concentric circles, or an ellipse are also possible. Details of these arrays may be found from the references. ^{3,25-27}

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Types and Design Methods



Dipoles and Monopoles

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4-1 Introduction 4-4

4-2 Cylindrical Dipoles 4-4
Impedance as a Function of Length
and Diameter 4-4
Effect of Terminal Conditions 4-6
Equivalent Radius of Noncircular
Cross Sections 4-7
Patterns as a Function of Length
and Diameter 4-10

4-3 Biconical Dipoles 4-12
 Impedance as a Function of Length and Cone Angle 4-12
 Patterns of the Biconical Dipole 4-12

4-4 Folded Dipoles 4-13
Equivalent Circuit of a Folded
Dipole 4-13
Impedance Transformation as a
Function of the Ratio of
Conductor Sizes 4-17

4-5 Sleeve Dipoles 4-18

Equivalent Circuit of a Sleeve Dipole 4-18 Open Folded Sleeve Monopole 4-20

4-6 Effective Height of Antennas 4-23
General Formula and Its Role in the
Theory of Transmitting and
Receiving Antennas 4-23

4-7 Coupled Antennas 4-24
Circuit Relationships of Radiating
Systems 4-24

4-8 Monopole Antennas 4-26
Relationship to Balanced Antennas
4-26
Effect of Finite-Size Ground Plane
on Impedance and Pattern 4-27
Radiation Pattern of a Monopole on
a Circular Ground Plane 4-27
Monopole Mounted on the Edge of
a Sheet 4-30

Monopole Mounted on a Conducting Box 4-32 Since the publication of the first edition of this handbook several sections in the original chapter on linear antennas have become outdated and have been deleted in this edition. The availability of computer programs¹ for finding the impedance and other characteristics of antennas, particularly linear antennas, makes parametric tabulation of limited usage. Only some essential formulas and design data are therefore included in this chapter.

For the entire subject of linear antennas, the book by R. W. P. King² remains authoritative. Another book³ by the same author on the tables of antenna characteristics contains the most comprehensive data on the characteristics of cylindrical antennas. Calculations on circular-loop antennas and some simple arrays are also found there.

A section on the effective height of antennas is included in this chapter. The usage of this parameter in describing the transmitting and receiving characteristics of linear antennas and other simple structures is discussed in detail. In addition, material on the general formulation of receiving antennas is included so that engineers can apply the formulation for design purposes or for estimation of the coupling effect between elements made up of both linear and other types of antennas.

Antennas in lossy media are of great current interest. Unfortunately, the subject cannot be covered in this chapter because of limited space. The book by King and Smith⁴ on antennas in matter can be consulted for this subject, particularly for linear antennas embedded in a lossy medium.

4-2 CYLINDRICAL DIPOLES

impedance as a Function of Length and Diameter

The impedance characteristics of cylindrical antennas have been investigated by many writers. Theoretical work has mainly been confined to relatively thin antennas (length-to-diameter ratio greater than 15), and the effect of the junction connecting the antenna proper and the transmission line is usually not considered. Among various theories, the induced-emf method⁵ of computing the impedance of a cylindrical antenna based upon a sinusoidal distribution is still found to be very useful. The formula derived from this method is extremely simple. It is, however, valid only when the half length of a center-driven antenna is not much longer than a quarter wavelength. In practice, this is the most useful range. To eliminate unnecessary computations, the formula has been reduced to the following form:⁶

$$Z_{i} = R(k\ell) - j \left[120 \left(\ln \frac{\ell}{a} - 1 \right) \cot k\ell - X(k\ell) \right]$$
 (4-1)

where Z_i = input impedance, Ω , of a center-driven cylindrical antenna of total length 2ℓ and of radius a

 $k\ell=2\pi(\ell/\lambda)=$ electrical length, corresponding to ℓ , measured in radians The functions $R(k\ell)$ and $X(k\ell)$ are tabulated in Table 4-1 and plotted in Fig. 4-1 for the range $k\ell \le \pi/2$. For calculation purposes, these two functions can be approximated to within 0.5 Ω by the following simple third-order polynomials:

$$R(k\ell) = -0.4787 + 7.3246k\ell + 0.3963(k\ell)^2 + 15.6131(k\ell)^3$$
$$X(k\ell) = -0.4456 + 17.0082k\ell - 8.6793(k\ell)^2 + 9.6031(k\ell)^3$$

TABLE 4-1 Functions $R(k\ell)$ and $X(k\ell)$ Contained in Formula of the Input Impedance of a Center-Driven Cylindians	the rical
No. of the Control of	

kl	R(kl)	X(kl)	kl	$R(k\ell)$	X(kl)
0 0.1 0.2 0.3 0.4 0.5 0.6 0.7	0 0.1506 0.7980 1.821 3.264 5.171 7.563 10.48 13.99	0 1.010 2.302 3.818 5.584 7.141 8.829 10.68 12.73	0.9 1.0 1.1 1.2 1.3 1.4 1.5 π/2	18.16 23.07 28.83 35.60 43.55 52.92 64.01 73.12	15.01 17.59 20.54 23.93 27.88 32.20 38.00 42.46

When the length of the antenna is short compared with a wavelength but still large compared with its radius, the same formula reduces to

$$(Z_i)_{\text{short}} = 20(k\ell)^2 - j120(k\ell)^{-1} \left(\ln \frac{\ell}{a} - 1 \right)$$
 (4-2)

For antennas of half length greater than a quarter wavelength, a number of refined theories provide formulas for the computation of the impedance function. None of them, however, is simple enough to be included here. As far as numerical computation is concerned, Schelkunoff's method' is relatively simpler than Hallén's. It should be emphasized that all these theories are formulated by using an idealized model in which the terminal condition is not considered.

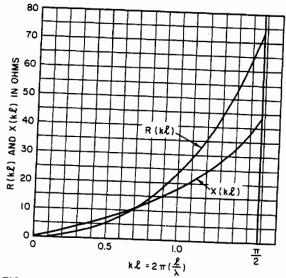


FIG. 4-1 The functions $R(k\ell)$ and $X(k\ell)$.

In practice, the antenna is always fed by a transmission line. The complete system may have the appearances shown in Fig. 4-2. The effective terminal impedance

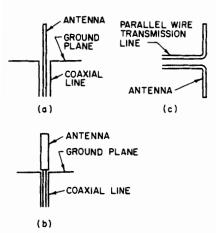


FIG. 4-2 Driving an antenna by transmission lines.

of the line (often referred to as the antenna impedance) then depends not only upon the length and the diameter of the antenna but also upon the terminal condition. In cases a and b, the impedance would also be a function of the size of the ground plane. For a given terminal condition the variation of the impedance of a cylindrical antenna as a function of the length and the diameter of the antenna is best shown in the experimental work of Brown and Woodward.8 The data cover a wide range of values of the length-to-diameter ratio. Two useful sets of curves are reproduced in Figs. 4-3 and 4-4. The impedance refers to a cylindrical antenna driven by a coaxial line through a large circular ground plane placed on the surface of the earth. The arrangement is similar to the one

・ 大学の名の一般の主義をあることが、アイスのは、アイスのできるのできる。

sketched in Fig. 4-2a. The length and diagneter of the antenna are measured in degrees; i.e., a length of one wavelength is equivalent to 360°. If the effects due to the terminal condition and finite-size ground plane are neglected, the impedance would correspond to one-half of the impedance of a center-driven antenna (Fig. 4-2c). In using these data for design purposes, one must take into consideration the actual terminal condition as compared with the condition specified by these two authors. In particular, the maximum value of the resistance and the resonant length of the antenna may change considerably if the base capacitance is excessive.

Effect of Terminal Conditions

Many authors have attempted to determine the equivalent-circuit elements corresponding to different terminal conditions. Schelkunoff and Friis have introduced the concepts of base capacitance and near-base capacitance to explain the shift of the impedance curve as the terminal condition is changed. Similar interpretations have been given by King¹⁰ for a cylindrical antenna driven by a two-wire line or by a coaxial line and by Whinnery11 for a biconical antenna driven by a coaxial line. The importance of the terminal condition in effecting the input impedance of the antenna is shown in Figs. 4-5 and 4-6. They are again reproduced from Brown and Woodward's paper. Because of the large variation of the effective terminal impedance of the line with changes in the geometry of the terminal junction, one must be cautious when using the theoretical results based upon isolated antennas. For junctions possessing simple geometry, the static method of Schelkunoff and Friis, King, and Whinnery can be applied to estimate the shunt capacitance of the junction. The latter then can be combined with the impedance of the antenna proper to evaluate the resultant impedance. For intricate junctions, accurate information can be obtained only by direct measurement.

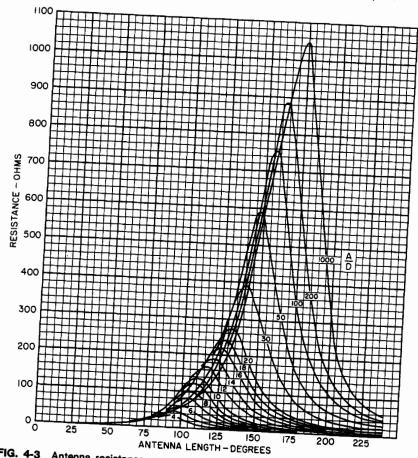


FIG. 4-3 Antenna resistance versus antenna length A when a constant ratio of length to diameter A/D is maintained. Here the length and diameter are held constant while the frequency is changed.

Equivalent Radius of Noncircular Cross Sections

As far as the impedance characteristics and radiation pattern are concerned, a thin cylindrical antenna with a noncircular cross section behaves like a circular cylindrical antenna with an equivalent radius. In stating this characteristic, the terminal effect is, of course, not considered. The equivalent radius of many simply shaped cross sections can be found by the method of conformal mapping. For an elliptical cross section the following simple relation exists:

$$a_{eq} = \frac{1}{2}(a+b) \cdot \tag{4-3}$$

where a = major axis of ellipseb = minor axis of ellipse

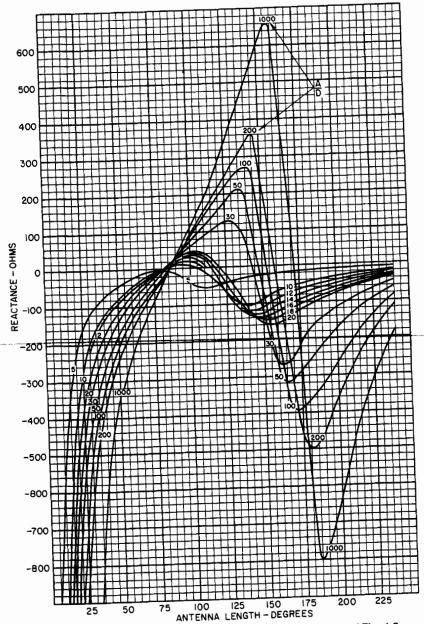


FIG. 4-4 Reactance curves corresponding to the resistance curves of Fig. 4-3.

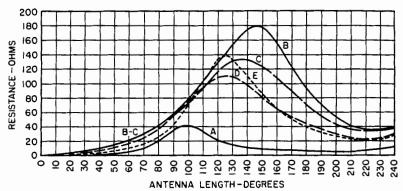


FIG. 4-5 Resistance as a function of antenna length A. The diameter D is 20.6°. Curve A: The arrangement shown in Fig. 4-2b. Curve B: The arrangement of Fig. 4-2a with the diameter of the outer conductor equal to 74°. The characteristic impedance of the transmission line is 77.0 Ω . Curve C: The outer-conductor diameter is 49.5°, and the transmission line has a characteristic impedance of 52.5 Ω . Curve D: The diameter of the outer conductor is 33°. The characteristic impedance is 28.3 Ω . Curve E: This curve was obtained by tuning out the base reactance with an inductive reactance of 65.0 Ω .

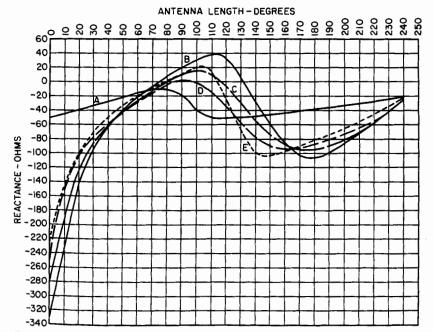


FIG. 4-8 Reactance curves corresponding to the resistance curves of Fig. 4-5.

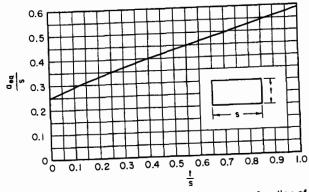


FIG. 4-7 Equivalent radius a_{eq} of a rectangle as a function of the ratio of thickness t to width s.

For a rectangular cross section the result is plotted in Fig. 4-7. In the case of a strip, Eq. (4-3) and Fig. 4-7 give the identical result. When the cross section has the form of a regular polygon, the result is tabulated in Table 4-2. The equivalent radius of two parallel cylinders of radius ρ_1 and ρ_2 separated by a distance d between the centers is given by¹³

$$\ln \rho_e = \frac{1}{(\rho_1 + \rho_2)^2} (\rho_1^2 \ln \rho_1 + \rho_2^2 \ln \rho_2 + 2\rho_1 \rho_2 \ln d)$$
 (4-4)

Formulas for the equivalent radius of three cylinders and an angle strip are found in Ref. 13.

Patterns as a Function of Length and Diameter

In this subsection only the radiation pattern of center-driven cylindrical antennas is discussed. For base-driven antennas, the patterns depend very much upon the size of the ground plane. The subject will be discussed in Sec. 4-8.

The radiation pattern of a center-driven cylindrical antenna in general depends upon its length and thickness. The terminal condition which plays an important role in determining its impedance has a negligible effect on the pattern. For thin antennas, the calculated pattern obtained by assuming a sinusoidal current distribution is a good

TABLE 4-2 Equivalent Radius of a Regular Polygon

w				
n	3	4	5	6
a_{eq}/a	0.4214	0.5903	0.7563	0.9200

n = number of sides.

a = radius of the outscribed circle.

approximation of the actual pattern. Thus, with an assumed current distribution of the form

$$I(z) = I_0 \sin k(\ell - |z|) \qquad +\ell \ge z \ge -\ell \tag{4-5}$$

the radiation field, expressed in a spherical coordinate system, is given by

$$E_{\theta} = \frac{j\eta I_0 e^{lkR}}{2\pi R} \left[\frac{\cos(k\ell \cos \theta) - \cos k\ell}{\sin \theta} \right]$$
 (4-6)

where $\eta = (\mu/\epsilon)^{1/2} = 120\pi$ Ω

 θ = angle measured from axis of dipole, or z axis

The field pattern is obtained by evaluating the *magnitude* of the term contained in the brackets of Eq. (4-6). Some of the commonly referred-to patterns are sketched in Fig. 4-8. Comparing those patterns with the actual patterns of a thin cylindrical antenna

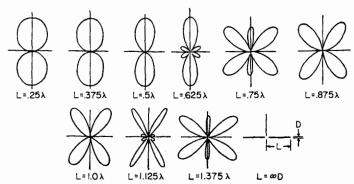


FIG. 4-8 Radiation patterns of center-driven dipoles if sinusoidal current distribution is assumed.

obtained by measurement, one finds that the theoretical patterns based upon a sinusoidal current distribution do not contain the following information:

- 1 The nulls between the lobes, except the *natural null* in the direction of the axis, are actually not vanishing.
- 2 The phase of the field varies continuously from lobe to lobe instead of having a sudden jump of 180° between the adjacent lobes.
- 3 The actual patterns vary slightly with respect to the diameter of the antenna instead of being independent of the thickness.

Depending upon the particular applications, some of the fine details may require special attention. In most cases, the idealized patterns based upon a sinusoidal current distribution give us sufficient information for design purposes.

When the half length ℓ of the antennas is less than about one-tenth wavelength, Eq. (4-6) is well approximated by

$$E_{\theta} = \frac{j\eta I_0(k\ell)^2 e^{jkR}}{4\pi R} \sin\theta \tag{4-7}$$

The figure-eight pattern resulting from the plot of the sine function is a characteristic not only of short cylindrical antennas but also of all small dipole-type antennas. Equations (4-6) and (4-7) are also commonly used to evaluate the directivity of linear antennas. The directivity is defined as

$$D = \frac{\text{maximum radiation intensity}}{\text{average radiation intensity}}$$
 (4-8)

For a short dipole, D is equal to 1.5. The directivity of a half-wave dipole ($\ell = \lambda/4$) is equal to 1.64. The half-wave dipole is often used as a reference antenna to describe the gain of more directive antennas, particularly arrays made of dipoles.

4-3 BICONICAL DIPOLES

Impedance as a Function of Length and Cone Angle

When the angles of a symmetrical biconical antenna (Fig. 4-9) are small, the input impedance of the antenna can be calculated by using Schelkunoff's formula.⁷ Some



FIG. 4-9 A biconical dipole.

sample curves are shown in Fig. 4-10. While the biconical antenna is an excellent theoretical model for studying the essential property of a dipole-type antenna, smallangle biconical antennas are seldom used in practice. Wide-angle biconical antennas or their derived types such as discones, however, are frequently used as broadband antennas. The broadband impedance characteristics occur when the angle of the cones, θ_0 of Fig. 4-9, lies between 30 and 60°. The exact value of θ_0 is not critical. Usually it is chosen so that the characteristic impedance of the biconical dipole matches as closely as possible the characteristic impedance of the line which feeds the antenna. The characteristic impedance of a biconical dipole as a function of the angle is plotted in Fig. 4-11. For a conical monopole driven against an infinitely large ground plane, the characteristic impedance and the input impedance of the antenna are equal to half of the corresponding values of a dipole. Several formulas 15 are available for computing the input impedance of wide-angle biconical antennas. Actual computation has been confined to a very few specific values of θ_0 . 16,17 More complete information is available from the experimental data obtained by Brown and Woodward. 18 Two curves are reproduced in Figs. 4-12 and 4-13. The case corresponding to $\alpha = 0^{\circ}$ represents a cylindrical antenna having a diameter of 2.5 electrical degrees at a frequency of 500 MHz, since the feed point was kept fixed at that diameter.

Patterns of the Biconical Dipole

The radiation patterns of biconical dipoles have been investigated theoretically by Papas and King. ¹⁹ Figure 4-14 shows the patterns of a 60°-flare-angle ($\theta_0 = 30^\circ$) conical dipole for various values of ka, where $k = 2\pi/\lambda$ and a = half length of the

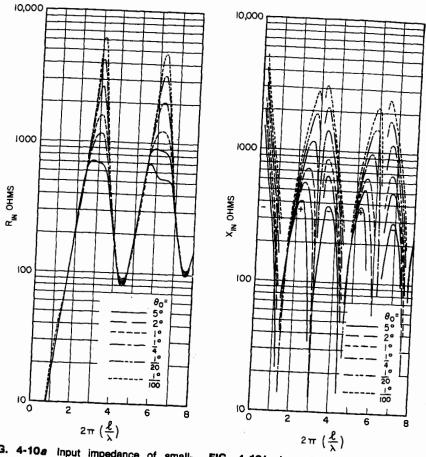


FIG. 4-10a Input impedance of small-angle biconical antennas (resistance).

FIG. 4-10b Input impedance of small-angle biconical antennas (reactance).

dipole, which is the same as the ℓ used in Fig. 4-9. Similar curves corresponding to different values of the flare angle have been obtained experimentally by Brown and Woodward.¹⁸

4-4 FOLDED DIPOLES

Equivalent Circuit of a Folded Dipole

A folded dipole is formed by joining two cylindrical dipoles at the ends and driving them by a pair of transmission lines at the center of one arm as shown in Fig. 4-15. The diameters of the two arms can be either identical or different. A simple analysis, based upon a quasi-static approach, of the operation of a folded dipole of arbitrary dimension has been given by Uda and Mushiake.¹³ According to their method, the

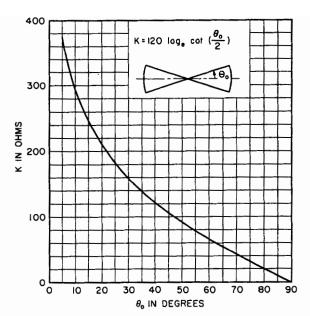


FIG. 4-11 Characteristic impedance of a biconical dipole.

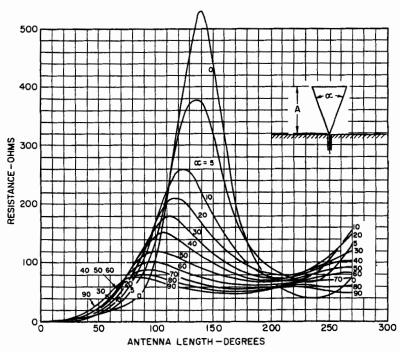


FIG. 4-12 Measured resistance curves of the conical unipole versus length in electrical degrees for various flare angles.

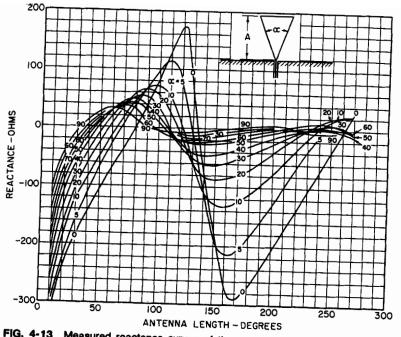


FIG. 4-13 Measured reactance curves of the conical unipole versus length in electrical degrees for various flare angles.

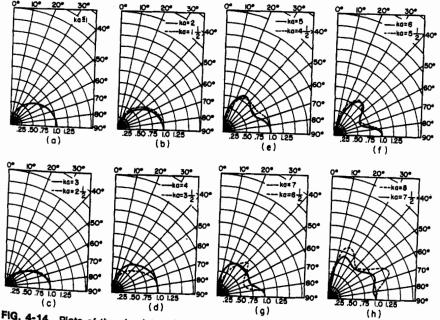


FIG. 4-14 Plots of the absolute values of the far-zone electric field as a function of the zenithal angle θ for various values of ka and with a flare angle equal to $60^{\circ}(\theta_0 = 30^{\circ})$.

FIG. 4-15 Folded dipole.

excitation of a folded dipole can be considered as a superposition of two modes as shown in Fig. 4-16. The impedance of the symmetrical mode, characterized by two equal driving voltages, can be calculated by making use of the equivalent radius of

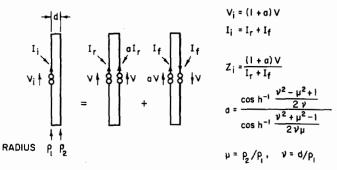


FIG. 4-16 Decomposition of the folded dipole into two fundamental modes.

two conductors as discussed in Sec. 4-2. The equivalence is shown in Fig. 4-17. The impedance function Z_r , is therefore the same as the impedance of a cylindrical dipole with an equivalent radius ρ_r given by

$$\ln \rho_e = \ln \rho_1 + \frac{1}{(1+\mu)^2} (\mu^2 \ln \mu + 2\mu \ln \nu)$$
 (4-9)

where the various parameters are explained in Fig. 4-16. The impedance of the asymmetrical mode, characterized by equal and opposite currents on the two arms, is the same as the shorted section of transmission line of length equal to ℓ ; that is,

$$Z_f = \frac{(1+a)V}{2I_f} = jZ_0 \tan k\ell$$
 (4-10)

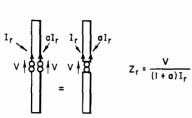


FIG. 4-17 The equivalent representation of the symmetrical mode in computing Z_n

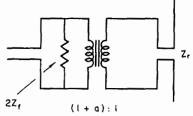


FIG. 4-18 Equivalent circuit of a folded dipole.

The state of the s

where Z_0 is the characteristic impedance of the two-wire line. Expressed in terms of Z_r and Z_f , the input impedance of a folded dipole is given by

$$Z = \frac{V_i}{I_i} = \frac{(1+a)V}{I_r + I_f} = \frac{2(1+a)^2 Z_r Z_f}{(1+a)^2 Z_r + 2Z_f}$$
(4-11)

An equivalent circuit based upon Eq. (4-11) is shown in Fig. 4-18. For a folded dipole of length ℓ equal to $\lambda/4$, Z_f is very large compared with $(1 + a)^2 Z_r$; hence

$$Z_{\lambda/4} = (1 + a)^2 Z_r$$
 (4-12)

Impedance Transformation as a Function of the Ratio of Conductor Sizes

The step-up impedance ratio $(1 + a)^2$ as a function of μ and ν has been calculated by Mushiake. The diagram is reproduced in Fig. 4-19 by using the formula for a given

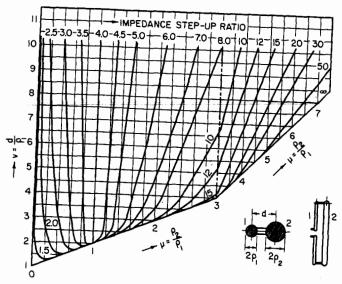


FIG. 4-19 Step-up transformation chart for a folded dipole.

in Fig. 4-16. When ρ_1 and ρ_2 are small compared with d, the value of a is given to a good approximation by

$$a = \frac{\ln{(d/\rho_1)}}{\ln{(d/\rho_2)}}$$
 (4-13)

This formula was first derived by Guertler.21

Another presentation²² of the transformation ratio $(1 + a)^2$ in a logarithmic scale as a function of ρ_2/ρ_1 and d/ρ_1 is given in Figs. 4-20 and 4-21.

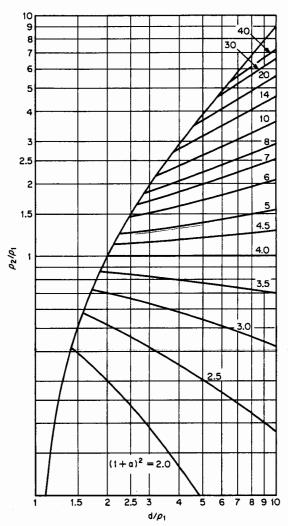


FIG. 4-20 ρ_2/ρ_1 versus impedance transformation ratio and d/ρ_1 . (© 1982 IEEE.)

4-5 SLEEVE DIPOLES

Equivalent Circuit of a Sieeve Dipole

The geometrical shape of a sleeve antenna, or a sleeve monopole, is sketched in Fig. 4-22a. If the image of the structure is included, then we have a sleeve dipole as shown in Fig. 4-22b. A sleeve dipole can therefore be considered as a doubly fed antenna in which the current is a relative maximum at the center of the dipole or at the base of the monopole. Antiresonances of the antenna impedance function take place when S

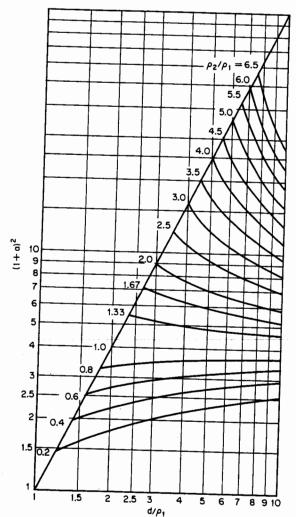


Fig. 4-21 impedance transformation ratio versus ρ_2/ρ_1 and d/ρ_1 . (© 1982 IEEE.)

is approximately equal to an odd multiple of a quarter wavelength or L is a multiple of a half wave. A special case of interest is that in which L+S is equal to a quarter wavelength. Then the current distribution along the structure is approximately cosinusoidal. At resonance the input resistance of the sleeve monopole or the sleeve dipole is approximately given by

$$R_S = R \left(\csc \frac{2\pi L}{\lambda} \right)^2 \tag{4-14}$$

where R denotes either the input resistance of a resonant quarter-wave monopole or that of a half-wave dipole. The sleeve in this case plays the role of an impedance transformer.

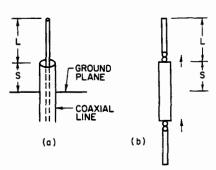


FIG. 4-22 The sleeve antenna.

Wong and King²³ have shown experimentally that open-sleeve dipoles properly designed exhibit a broadband voltage-standing-wave-ratio (VSWR) response and unidirectional radiation patterns over nearly an octave bandwidth when placed above a reflector. Figure 4-23 shows the VSWR response of open-sleeve dipoles for various dipole and sleeve diameters. Figure 4-24 shows the same with sleeve spacing as the parameter.

Open Folded Sleeve Monopole

The work of Uda and Mushiake¹³ on folded dipoles can be extended to include a

load at the unexcited arm as shown schematically in Fig. 4-25. The impedance of the loaded dipole is given by

$$Z_{l} = \frac{(Z_{a} + Z_{L})Z_{s} + \left(\frac{a}{1+a}\right)^{2} Z_{L}Z_{a}}{Z_{s} + Z_{L} + \frac{1}{(1+a)^{2}} Z_{a}}$$
(4-15)

where $Z_a = jZ_c \tan \frac{2\pi\ell}{\lambda}$

$$Z_c = \frac{Z_0}{2\pi} \left[\cosh^{-1} \frac{1}{2\gamma} \left(1 + \gamma^2 - \mu^2 \right) + \cosh^{-1} \frac{1}{2\gamma\mu} \left(-1 + \gamma^2 + \mu^2 \right) \right]$$

 Z_s = input impedance of the folded dipole when it is driven simultaneously by a common voltage at the base. It is approximately equal to that of a dipole with an equivalent radius ρ_s given by Eq. (4-4).

The parameter a in Eq. (4-15) and the parameters γ and μ in the expression for the characteristic impedance Z_c of a transmission line made of wires of unequal radius are the same as those defined for Fig. 4-16.

In the special case in which Z_L approaches infinity, Eq. (4-15) reduces to

$$Z_t = Z_S + \left(\frac{a}{1+a}\right)^2 Z_a \tag{4-16}$$

The structure then corresponds to an open folded dipole or monopole. Josephson²⁴ studied this structure both theoretically and experimentally. However, his analysis is correct only if the wires are of the same size. A sleeve version of an open folded monopole was also investigated by Josephson. The two structures are shown in Figs. 4-26 and 4-27.

The open folded monopole with a displaced feed point is equivalent to a folded

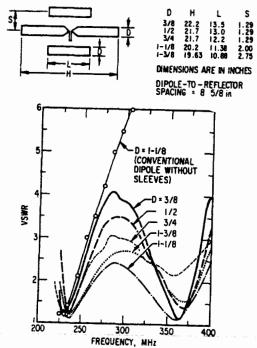


FIG. 4-23 VSWR response of open-sleeve dipoles for various dipole and sleeve diameters.

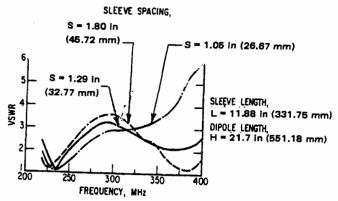


FIG. 4-24 VSWR for a %-in- (19-mm-) diameter open-sleeve dipole with sleeve spacing as the parameter.

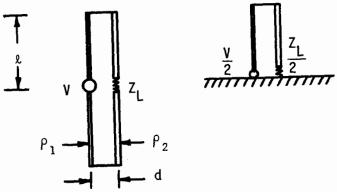


FIG. 4-25 Loaded folded dipole and monopole.

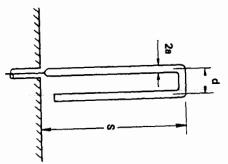


FIG. 4-26 Open folded monopole.

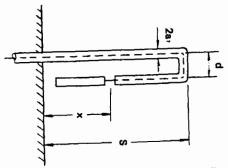


FIG. 4-27 Open folded monopole with a displaced feed point.

sleeve monopole. The input resistance at resonance of the open folded sleeve monopole is given approximately by

$$R_x = R_0 \left(\sin \frac{4\pi s}{\lambda} \right)^2 / \left(\sin \frac{2\pi x}{\lambda} \right)^2$$
 (4-17)

where R_0 denotes the resonant input resistance of the open folded monopole and R_x is the input resistance of the folded sleeve monopole. The precise value of R_0 depends on the radius of the wires and their separation. A typical value is about 10Ω . The open folded sleeve monopoles made of arms with different sizes are useful models in designing aircraft trail antennas or fin-type antennas on vehicles as illustrated by Josephson.

4-6 EFFECTIVE HEIGHT OF ANTENNAS

General Formula and Its Role in the Theory of Transmitting and Receiving Antennas

The radiation field of any antenna can always be written in the form

$$\mathbf{E} = \frac{-jKZ_0I_ie^{-jkR}}{4\pi R}\mathbf{h} \tag{4-18}$$

where $Z_0 = (\mu_0/\epsilon_0)^{1/2}$

 $k = 2\pi/\lambda$

h = effective height of antenna

 $I_i = input current to antenna$

The effective height of an antenna was originally introduced by Sinclair.²⁵ It is related to the radiation vector defined by Schelkunoff to characterize the radiation field of an antenna, i.e.,

$$N_t = I_t h \tag{4-19}$$

where N_t denotes the transversal part of Schelkunoff's radiation vector. The effective height is a very useful parameter in antenna engineering. For example, the open-circuit voltage of a receiving antenna can be expressed as

$$V_{\rm op} = \mathbf{E}_i \cdot \mathbf{h} \tag{4-20}$$

where E_i denotes the incident electric field. It is also an important parameter involved in the polarization-matching factor of a receiving antenna. In the theory of receiving antennas the receiving cross section or the effective aperture is defined by²⁶

$$A = \frac{\lambda^2}{4\pi} Dpq \tag{4-21}$$

where λ = operating wavelength

D = directivity of antenna

p = polarization-matching factor

 $= \frac{|\mathbf{h} \cdot \mathbf{E}_i|^2}{|\mathbf{h}|^2 |\mathbf{E}_i|^2}$

q = impedance-matching factor

$$=1-\left|\frac{Z_L-Z_I^*}{Z_L+Z_I}\right|^2$$

 Z_i = input impedance of antenna

 $Z_L = load impedance$

The polarization-matching factor again involves the effective-height function. The effective-height function of a center-driven short dipole, if a linear current distribution along the dipole is assumed, is given by

$$\mathbf{h} = -\ell \sin \theta \hat{\theta} \tag{4-22}$$

where ℓ denotes the half length of the dipole which is assumed to be pointed in the vertical direction and θ denotes the polar angle measured between the axis of the dipole and the direction of observation or the direction of radiation. For a linearly polarized incident field making a skew angle α with the axis of the dipole, the polarization-matching factor is given by

$$p = \cos^2 \alpha \tag{4-23}$$

The effective-height functions for other simple antenna elements are listed below:

Antenna type	Effective height
Short dipole of length 2ℓ	$-\ell$ sin $ heta\hat{ heta}$
Half-wave dipole	$-\frac{\lambda}{\pi} \frac{\cos\left(\frac{\pi}{2}\cos\theta\right)}{\sin\theta} \hat{\theta}$
Small loop of radius a pointed in the z direction	$j\frac{2\pi^2a^2}{\lambda}\sin\theta\hat{\phi}$
Half-wave folded dipole	$-\frac{2\lambda}{\pi}\frac{\cos\left(\frac{\pi}{2}\cos\theta\right)}{\sin\theta}\hat{\theta}$

4-7 COUPLED ANTENNAS

Circuit Relationships of Radiating Systems

When several antennas are coupled to each other, the input voltage and input currents to the antennas follow the same relationship as ordinary coupled circuits. ²⁷ For a system of n antennas, the relationships are

$$V_i = \sum_{j=1}^n Z_{ij}I_j$$
 $i = 1, 2, ..., n$ (4-24)

where Z_{ii} is called the self-impedance of antenna i and Z_{ij} or Z_{ji} is called the mutual impedance between antenna i and antenna j. In the case of linear radiators, Carter's method, or the induced-emf method based upon sinusoidal current distribution, is the simplest one to use in determining the various Z's. The method applies only to anten-

nas shorter than a half wavelength. The self-impedance determined by this method is the same as that given by Eq. (4-1). The formulas for the mutual impedance of two parallel antennas of equal size are found in Carter's original paper or in Kraus's book.²⁸ Figure 4-28 shows the mutual impedance of two parallel half-wave antennas

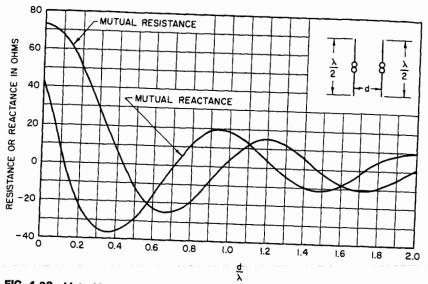


FIG. 4-28 Mutual impedance between two parallel half-wave antennas placed side by side.

placed side by side. Figure 4-29 shows the mutual impedance of two parallel collinear half-wave antennas. Mutual impedances of two parallel antennas of unequal sizes have been investigated by several authors. ²⁹⁻³¹ The induced-emf method has also been applied to crossed or skewed antennas ^{32,33} to evaluate their mutual impedance. Refined calculations based upon Hallén's integral-equation technique are found in the works of Tai, ³⁴ Bouwkamp, ³⁵ and Uda and Mushiake. ¹³ The last two authors also evaluated the self-impedance and mutual impedance of parallel antennas of unequal sizes, which ultimately applies to the design of Yagi-Uda arrays.

For dipoles separated by a distance which is large compared with a wavelength, the mutual impedance between the two dipoles can be calculated by using the asymptotic formula

$$Z_{12} = \frac{jkZ_0e^{-jkR}}{4\pi R}(\mathbf{h}_1 \cdot \mathbf{h}_2)$$
 (4-25)

where $k = 2\pi/\lambda$

 $Z_0 = (\mu_0/\epsilon_0)^{1/2}$

R =distance between centers of dipoles

 \mathbf{h}_1 , \mathbf{h}_2 = effective height of dipoles

The formula is quite accurate for half-wave dipoles with a separation barely greater than one wavelength.

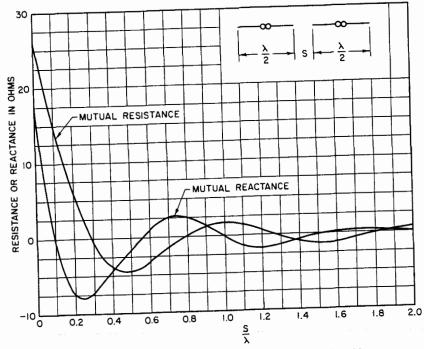


FIG. 4-29 Mutual impedance between two collinear half-wave antennas.

4-8 MONOPOLE ANTENNAS

Relationship to Balanced Antennas

When a monopole is mounted on an ideally infinite ground plane, its impedance and radiation characteristics can be deduced from that of a dipole of twice its length in free space. For a base-driven monopole, its input impedance is equal to one-half that of the center-driven dipole, and the radiation pattern above the infinite ground plane is identical with the upper half of the radiation pattern of the corresponding dipole. When the ground plane is of finite size, the image theorem does not apply.

Several methods have been devised to investigate the characteristics of a monopole mounted on a finite-size ground plane. The first method is due to Bolljahn, ³⁶ who considers the problem from the point of view of symmetrical components. The decomposition is shown in Fig. 4-30a, in which the ground plane is assumed to be of the form

$$= \frac{z_0}{\frac{1}{2}I} + \frac{\Delta z}{\frac{1}{2}I} + \frac{1}{2}I$$

FIG. 4-30a Monopole and finite-size ground plane and its decomposition into two modes of excitation.

of an infinitely thin conducting disk. For the symmetrical mode of excitation the presence of the disk has no effect upon the radiation of the two elements. The problem is therefore the same as if the two elements were placed in free space. The antisymmetrical pair of current elements excites equal currents on the top and the bottom sides of the disk. This mode is responsible for the variation of the input impedance of the antenna as a function of the disk diameter. It is also responsible for the asymmetry of the resultant radiation pattern with respect to the ground plane. Bolljahn's original work was developed by assuming a short monopole on a disk. The entire analysis is found in Schelkunoff's book Advanced Antenna Theory. His study of the characteristics of large ground planes was later extended by Storer³⁷ to monopoles of arbitrary length.

Effect of Finite-Size Ground Plane on impedance and Pattern

According to Storer, who used a variational method to formulate the problem, the change of the input impedance of a base-driven monopole erected upon a large circular ground plane can be written as

$$\Delta Z = Z - Z_0 = j \frac{60}{kd} e^{-jkd} \left| k \int_0^k \frac{I(z)}{I(0)} dz \right|^2$$
 (4-26)

where Z_0 = impedance of monopole referred to an infinite ground plane, Ω

d = diameter of circular ground plane

 $k = 2\pi/\lambda$

h = height of monopole

I(z) = current-distribution function of monopole

I(0) = base current or input current

The function $j(60/kd)e^{-jkd}$, which is independent of the current distribution, is plotted in Fig. 4-30b. The real and the imaginary parts of the function are respectively equal to $(R - R_0) / \left| k \int_0^h \frac{I(z)}{I(0)} dz \right|^2$ and $(X - X_0) / \left| k \int_0^h \frac{I(z)}{I(0)} dz \right|^2$. For a quarter-

wave monopole, if we assume $I(z) = I(0) \cos kz$, then

$$\left| k \int_0^k \frac{I(z)}{I(0)} dz \right| = 1$$

Thus, with a ground plane of a diameter greater than 10 wavelengths, it is seen from Fig. 4-30b that the variation of the resistance and of the reactance of a quarter-wave monopole is less than 1 Ω .

Radiation Pattern of a Monopole on a Circular Ground Plane

While the effect of a ground plane upon the impedance of a monopole is not very great, the radiation pattern is affected considerably. The pattern of such a composite antenna

^{*}The material contained in this subsection is condensed from a communication from Dr. Robert G. Kouyoumjian exclusively prepared for this handbook. The help of Dr. Kouyoumjian is gratefully acknowledged.

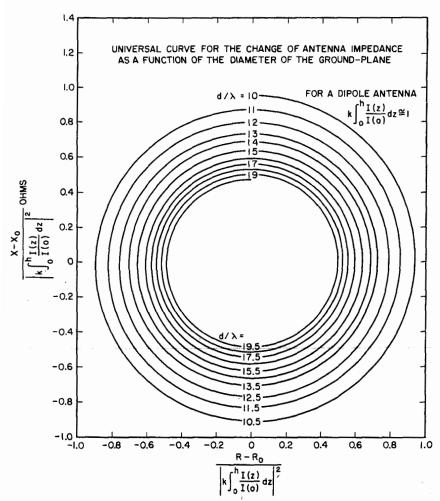


FIG. 4-30b Universal curve for the change of antenna impedance as a function of the diameter of the ground plane.

can be obtained quite accurately from the solution of the uniform geometrical theory of diffraction (GTD). 38,39 For a short monopole of length h positioned at the center of

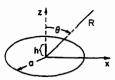


FIG. 4-31 A monopole on a circular disk.

a circular disk of radius a, as shown in Fig. 4-31, the current on the monopole is assumed to be

$$I(z) = I_0 \frac{\sin k(h-z)}{\sin kh}$$
 (4-27)

If the point of observation is not near the vertical axis (θ not close to 0 or π), the

radiation field can then be expressed in the form

$$\mathbf{E} = (E_0 + E_{d1} + E_{d2})\hat{\theta}$$
 (4-28)

where E_0 is the geometrical optics field given by

$$E_0 = \begin{cases} \frac{jZ_0I_0e^{-jkR}}{2\pi R\sin kh} \left[\frac{\cos(kh\cos\theta) - \cos kh}{\sin\theta} \right], & 0 \le \theta < \frac{\pi}{2} \\ 0, & \frac{\pi}{2} < \theta \le \pi \end{cases}$$
 (4-29)

and E_{d1} and E_{d2} represent, respectively, the singly and doubly diffracted field. They are given by

$$E_{d1} = -\frac{E_0\left(a, \frac{\pi}{2}\right)a}{2\sqrt{2\pi ka \sin \theta}} \left\{ F\left[2ka \cos^2\left(\frac{\pi}{4} + \frac{\theta}{2}\right)\right] \sec\left(\frac{\pi}{4} + \frac{\theta}{2}\right)\right]$$

$$e^{J[ka \sin \theta - (\pi/4)]} + \sec\left(\frac{\pi}{4} - \frac{\theta}{2}\right) e^{-J[ka \sin \theta - (\pi/4)]} \right\} \frac{e^{-JkR}}{R}$$
 (4-30)

$$E_{d2} = -\frac{E_0\left(a, \frac{\pi}{2}\right)a}{2\sqrt{2\pi k a \sin \theta}} \frac{e^{-K2ka - \pi/4}}{2\sqrt{\pi k a}} \cdot \left\{ F\left[2ka \cos^2\left(\frac{\pi}{4} + \frac{\theta}{2}\right)\right] \sec\left(\frac{\pi}{4} + \frac{\theta}{2}\right)\right\}$$

$$e^{j[ka\sin\theta-(\pi/4)]} \mp \sec\left(\frac{\pi}{4}-\frac{\theta}{2}\right)e^{-j[ka\sin\theta-(\pi/4)]}\right\}\frac{e^{-jkR}}{R} \quad \textbf{(4-31)}$$

where

$$F(x) = 2j\sqrt{x} e^{jx} \int_{\sqrt{x}}^{\infty} e^{-jt^2} dt$$
 (4-32)

$$E_0\left(a, \frac{\pi}{2}\right) = \frac{jZ_0I_0e^{-jka}}{2\pi a \sin kh} (1 - \cos kg)$$
 (4-33)

In Eqs. (4-30) and (4-31), the upper sign associated with the secant functions is for $0 \le \theta < \pi/2$, and the lower sign is for $\pi/2 < \theta \le \pi$. Although the uniform GTD is a high-frequency method, which implies that $ka \gg 1$, in practice the result is valid even for ka as small as 2π . When the argument of the transition function F(x) is greater than 10 or so, F(x) is approximately equal to 1; then the sum of E_{d1} and E_{d2} yields

$$E_{d1} + E_{d2} = -E_{0}(a,\pi/2) \frac{a}{4} \sqrt{\frac{2}{\pi k a \sin \theta}} \left\{ \sec \left(\frac{\pi}{4} + \frac{\theta}{2} \right) e^{f[ka \sin \theta - (\pi/4)]} + \sec \left(\frac{\pi}{4} - \frac{\theta}{2} \right) e^{-f[ka \sin \theta - (\pi/4)]} \left[1 + \frac{e^{-f[2ka - (\pi/4)]}}{2\sqrt{\pi k a}} \right] \right\} \frac{e^{-fkR}}{R}$$
 (4-34)

In the axial region (θ close to 0 or π), the pattern can be found by means of an equivalent edge current.^{39,40} The total diffracted field in this case is given by

$$E_{d1} + E_{d2} = \mp jE_0 \left(a, \frac{\pi}{2} \right) \frac{a}{2} \sec \frac{\pi}{4} J_1(ka \sin \theta) \left[1 + \frac{e^{-J(2ka - \pi/4)}}{2\sqrt{\pi ka}} \right]$$
 (4-35)

This approximately equals E_{d1} and E_{d2} given by Eqs. (4-30) and (4-31) at $ka \sin \theta \approx 5$ for $\theta \ll \pi/2$. Thus, the pattern calculated from Eq. (4-35) joins smoothly with that calculated by Eqs. (4-31) and (4-32) when ka > 5.

Figure 4-32 shows a typical pattern based on Eq. (4-28), the solid line, and Eq. (4-35),

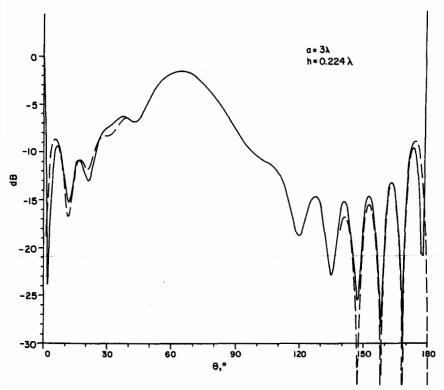


FIG. 4-32 The radiation pattern of a monopole above a circular disk having a radius of three wavelengths.

the dashed line. For practical purposes the term E_{d2} due to the doubly defracted rays is much smaller compared with E_{d1} except in the region where θ is close to $\pi/2$. By using a hybrid moment method jointly with GTD, it is possible to determine the input impedance of a monopole centered on a perfectly conducting circular disk.⁴¹

Monopole Mounted on the Edge of a Sheet

When a monopole is driven against an infinitely large conducting half sheet, the problem can be formulated conveniently with the aid of the dyadic Green's function pertaining to the half sheet. 42 By transforming the resultant series into definite integrals, Sawaya, Ishizone, and Mushiake 43 have been able to calculate the impedance of a monopole mounted on a half sheet in several orientations. Their results are shown in Figs. 4-33 and 4-34.

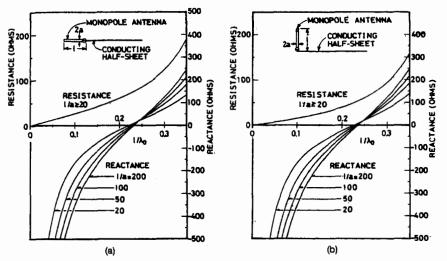


FIG. 4-33 Impedance of a horizontal (a) and of a vertical (b) monopole antenna as a function of ℓ/λ_0 . (© 1981 IEEE.)

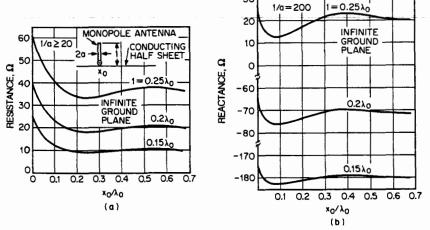


FIG. 4-34 Impedance of vertical monopole antenna on conducting half sheet as function of x_0/λ_0 , where x_0 is the distance from the edge of the half sheet to the base of the monopole. (a) Resistance. (b) Reactance. (© 1981 IEEE.)

These theoretical data can be used to estimate the impedance of monopoles mounted on large but finite conducting sheets. These authors also calculated the impedance of a notch antenna cut on a half sheet. The radiation patterns of short dipoles and small loops mounted on a half sheet are found in Ref. 42. Other work also has been reported by Pozar and Newman⁴⁴ and by Marin and Catedra⁴⁵ for the impedance and radiation patterns of monopoles located near the edges of finite half sheets or disks.

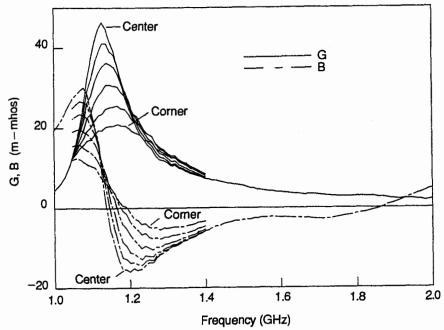


FIG. 4-35 Admittance versus frequency of a 6-cm monopole mounted on a cubical conducting box with edge length 10 cm for various locations between the center and corner. (© 1987 IEEE.)

Monopole Mounted on a Conducting Box

Recent investigations by Bhattacharya et al.⁴⁶ and Chu et al.⁴⁷ have reported the impedance and radiation patterns of a monopole mounted at arbitrary locations on a conducting box that is comparable in size to a wavelength. Figure 4-35 shows the behavior of the admittance of a monopole as a function of frequency as the position of the monopole is moved from the center of the box face to one corner.⁴⁶

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Loop Antennas

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- 5-1 Introduction 5-2
 5-2 Electrically Small 1
- 5-2 Electrically Small Loops 5-2 Transmitting Loop 5-2

Receiving Loop 5-4

Ferrite-Loaded Receiving Loop 5-6

5-3 Electrically Large Loops 5-9
Circular-Loop Antenna 5-9
Resonant Circular Loop 5-13

Circular Loop with Planar Reflector 5-15

- Coaxial Arrays of Circular Loops 5-16
- 5-4 Shielded-Loop Antenna 5-195-5 Additional Topics 5-21

The single-turn loop antenna is a metallic conductor bent into the shape of a closed curve, such as a circle or a square, with a gap in the conductor to form the terminals. A multiturn loop or coil is a series connection of overlaying turns. The loop is one of the primary antenna structures; its use as a receiving antenna dates back to the early experiments of Hertz on the propagation of electromagnetic waves.¹

The discussion of loop antennas is conveniently divided according to electrical size. Electrically small loops, those whose total conductor length is small compared with the wavelength in free space, are the most frequently encountered in practice. For example, they are commonly used as receiving antennas with portable radios, as directional antennas for radio-wave navigation, and as probes with field-strength meters. Electrically larger loops, particularly those near resonant size (circumference of loop/wavelength ≈ 1), are used mainly as elements in directional arrays.

The following symbols are used throughout the chapter:

 λ = wavelength in free space at the frequency $f = \omega/2\pi$, where the complex harmonic time-dependence exp $(j\omega t)$ is assumed

 $\beta = 2\pi/\lambda = \text{propagation constant in free space}$

 $\zeta = \sqrt{\mu_0/\epsilon_0}$ = wave impedance of free space ($\approx 377 \Omega$)

b = mean radius of a circular loop or mean side length of a square loop

a = radius of loop conductor (All results presented are for thin-wire loops, $a/b \ll 1$.)

A = area of loop

N = number of turns

 ℓ_c = length of solenoidal coil

5-2 ELECTRICALLY SMALL LOOPS

The axial current distribution in an electrically small loop is assumed to be uniform; that is, the current has the same value I_0 at any point along the conductor. For single-turn loops and multiturn loops that are single-layer solenoidal coils, measurements suggest that this is a good assumption provided the total length of the conductor ($N \times \text{circumference}$) is small compared with the wavelength in free space, typically $\lesssim 0.1\lambda$, and the length-to-diameter ratio for the solenoidal coil is greater than about $3 (\ell_c/2b \gtrsim 3.0)$. With a uniform current assumed, the electrically small loop antenna is simply analyzed as a radiating inductor.

Transmitting Loop

The electromagnetic field of an electrically small loop antenna is the same as that of a magnetic dipole with moment $m = I_0 NA$:

$$E_{\phi} = \frac{\zeta \beta^2 m}{4\pi r} \left(1 - \frac{j}{\beta r} \right) e^{-j\beta r} \sin \theta$$
 (5-1)

$$B_{\theta} = \frac{-\mu_0 \beta^2 m}{4\pi r} \left(1 - \frac{j}{\beta r} - \frac{1}{\beta^2 r^2} \right) e^{-j\beta r} \sin \theta$$
 (5-2)

$$B_r = \frac{\mu_0 \beta^2 m}{2\pi r} \left(\frac{j}{\beta r} + \frac{1}{\beta^2 r^2} \right) e^{-j\beta r} \cos \theta$$
 (5-3)

where the plane of the loop is normal to the polar axis of the spherical coordinate system (r, θ, ϕ) centered at the loop, as shown in Fig. 5-1. In the far zone of the loop ($\lim \beta r \to \infty$), only the leading terms in Eqs. (5-1) and (5-2) are significant, and the

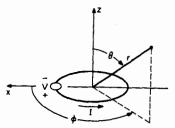


FIG. 5-1 Loop antenna and accompanying spherical coordinate system.

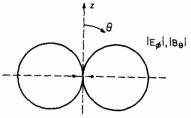


FIG. 5-2 Far-zone vertical-plane field pattern of an electrically small loop.

field pattern for both E_{\bullet} and B_{\bullet} in the vertical plane is the simple figure eight shown in Fig. 5-2.

The driving-point voltage and current are related through the input impedance of the loop, $V = ZI_0$. For electrically small loops, the impedance is the series combination of the reactance of the external inductance L^{ϵ} with the radiation resistance R^{ϵ} and the internal impedance of the conductor $Z^{\epsilon} = R^{\epsilon} + j\omega L^{\epsilon}$:

$$Z = R' + Z' + j\omega L' = R' + R' + j\omega (L' + L')$$
 (5-4)

In the equivalent circuit for the small loop, a lumped capacitance C is sometimes placed in parallel with Z to account for the distributed capacitance between the sides of a single turn and between the turns of a solenoid, as shown in Fig. 5-3. This capacitance is omitted here, since in practice a variable capacitance is usually placed in parallel with the loop to tune out its inductance; the capacitance of the loop simply decreases the value of the parallel capacitance needed. Note that a loop with a truly

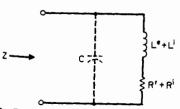


FIG. 5-3 Equivalent circuit for input impedance Z of an electrically small loop.

uniform current distribution would have no capacitance, since from the equation of continuity there would be no charge along the conductor of the loop.

The radiation resistance of the small loop is proportional to the square of the product of the area and the number of turns:

$$R' = \frac{\zeta}{6\pi} \beta^4 (NA)^2 \qquad (5-5)$$

For single-turn loops and solenoidal coils whose turns are not too closely spaced, the internal impedance is approximately

$$Z^i = z^i \times \text{total length of conductor}$$
 (5-6)

where z^l is the internal impedance per unit length of a straight conductor with the same cross section as the loop conductor.⁴ If the turns of the coil are closely spaced, the proximity effect must also be included in determining $Z^{l,5}$

The external inductance is determined from one of the many formulas available for the inductance of coils:⁶

For a single-turn circular loop

$$L' = \mu_0 b [\ln (8b/a) - 2]$$
 (5-7)

and for a single-turn square loop

$$L^{\epsilon} = \frac{2\mu_0 b}{\pi} \left[\ln \left(b/a \right) - 0.774 \right]$$
 (5-8)

The external inductance of a tightly wound single-layer solenoidal coil of length ℓ_c and a radius b is often approximated by Lorenz's formula for the inductance of a circumferentially directed current sheet. Numerical results from this formula can be put in a form convenient for application:

$$L' = K\mu_0 N^2 A/\ell_c \tag{5-9}$$

where the factor K, known as Nagaoka's constant, is shown as a function of the ratio $\ell_c/2b$ (length of the coil to the diameter) in Fig. 5-4. Note that, for a long coil ($\ell_c/2b \gg 1$), $K \approx 1$. The use of Eq. (5-9) assumes that the turns of the coil are so closely spaced that the winding pitch and insulation on the conductors can be ignored; if highly accurate calculations of L^c are necessary, corrections for these factors are available in the literature.

Receiving Loop

When the electrically small loop is used as a receiving antenna, the voltage developed at its open-circuited terminals V_{CC} is proportional to the component of the incident magnetic flux density normal to the plane of the loop B_z^l :

$$V_{OC} = j\omega NAB_x^i \tag{5-10}$$

where the incident field is assumed to be uniform over the area of the loop. This simple relation between V_{OC} and B_x^l makes the small loop useful as a probe for measuring the magnetic flux density. If a relation between the incident electric and magnetic fields at the center of the loop is known, V_{OC} can be expressed in terms of the magnitude of the incident electric field E^l and an effective height h_e . This is the case for an incident plane wave with the wave vector \mathbf{k}_l and the orientation shown in Fig. 5-5:

$$V_{OC} = j\omega NAB^{i} \cos \psi_{i} \sin \theta_{i} = h_{\epsilon}(\psi_{i}, \theta_{i})E^{i}$$
 (5-11)

where
$$h_{\epsilon}(\psi_i, \theta_i) \equiv V_{OC}/E^i = j\beta NA \cos \psi_i \sin \theta_i$$
 (5-12)

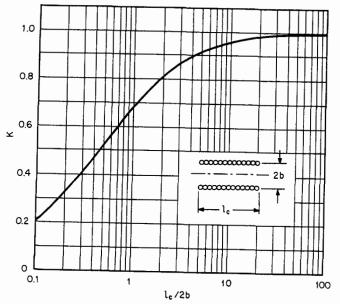


FIG. 5-4 Nagaoka's constant K for a solenoidal coil as a function of the coil length to the diameter, $\ell_c/2b$.

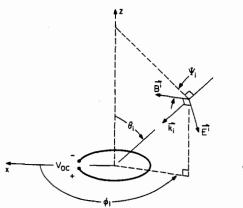


FIG. 5-5 Plane-wave field incident on receiving loop.

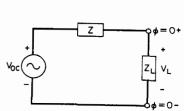


FIG. 5-6 Thévenin equivalent circuit for the receiving loop.

The voltage across an arbitrary load impedance Z_L connected to the terminals of the loop with input impedance Z is determined from the Thévenin equivalent circuit in Fig. 5-6:

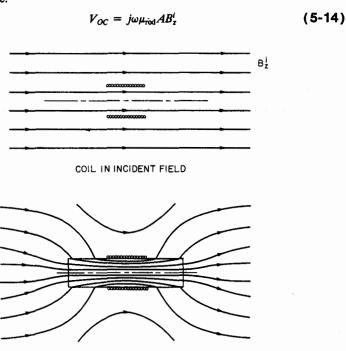
$$V_L = V_{OC}Z_L/(Z + Z_L)$$
 (5-13)

Ferrite-Loaded Receiving Loop

The open-circuit voltage at the terminals of the electrically small receiving loop can be increased by filling the loop with a core of permeable material, usually a ferrite. The effect of the core is to increase the magnetic flux through the area of the loop, as illustrated in Fig. 5-7 for a solenoidal coil with a cylindrical core placed in a uniform axial magnetic field.

The ferrite material is characterized by a complex relative initial permeability $\mu_r = \mu/\mu_0 = \mu'_r - j\mu''_r$ and a relative permittivity $\varepsilon_r = \varepsilon/\varepsilon_0$.* The material is usually selected to have a loss tangent $p_m = \mu''_r/\mu'_r$ which is small at the frequency of operation, and consequently μ''_r is ignored in the analysis except when the power dissipated in the core is being calculated. The dimensions of the core are also assumed to be small compared with the wavelength in the ferrite $\lambda_m \approx \lambda/\sqrt{\varepsilon_r\mu'_r}$ to prevent internal resonances within the core.⁷

The open-circuit voltage for a single-turn loop at the middle of a ferrite cylinder of length ℓ , and radius b is increased by the factor $\mu_{\rm rod}$ over the value for the same loop in free space:



COIL WITH FERRITE CORE IN INCIDENT FIELD

FIG. 5-7 Effect of a cylindrical ferrite core on the magnetic flux through a solenoidal coil.

^{*}The initial permeability is the derivative dB/dH in the limit as H is reduced to zero. Dielectric loss in the ferrite is ignored here, and the permittivity is assumed to be real.

Here the radius of the loop conductor a is ignored, and the mean radius of the loop and the core are assumed to be the same value b. The graph in Fig. 5-8 shows the apparent permeability $\mu_{\rm rod}$ as a function of the length-to-diameter ratio for the rod $\ell_r/2b$ with the relative initial permeability of the ferrite μ_r as a parameter. Similar graphs for the apparent permeability of solid and hollow spheroidal cores are in the literature.

For a single-layer solenoidal coil of length ℓ_c centered on the rod, an averaging factor F_V must be included in the open-circuit voltage to account for the decrease in the flux along the length of the coil from the maximum at the middle:

$$V_{OC} = j\omega\mu_{\rm rod}F_{\nu}NAB_{z}^{i} \tag{5-15}$$

The empirical factor F_{ν} , determined from an average of experimental results, is shown in Fig. 5-9 as a function of the ratio ℓ_c/ℓ_r (length of the coil to length of the rod). ^{10,11} For a long rod of moderate permeability $(\ell_r/2b \gg 1, \mu_{\rm rod} \approx \mu_r')$ covered by a coil of

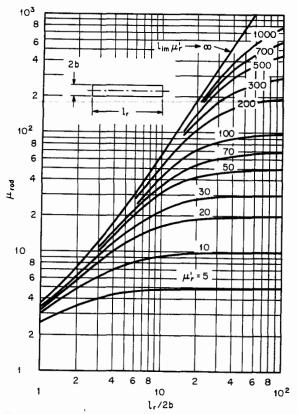


FIG. 5-8 The apparent permeability $\mu_{\rm rod}$ at the middle of a cylindrical rod as a function of the length-to-diameter ratio $\ell_r/2b$ with the initial permeability μ_r' as a parameter.

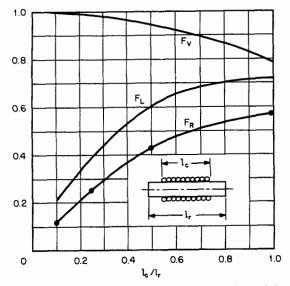


FIG. 5-9 The factors F_V , F_L , and F_R as functions of the ratio ℓ_c/ℓ_r (length of the coil to length of the rod). These factors were determined from averages of experimental data.

equal length $(\ell_c/\ell_r = 1)$, the open-circuit voltage is increased by approximately the factor 0.8 μ_r over the open-circuit voltage for the same coil without the core.

The equivalent circuit for the impedance of the ferrite-loaded solenoidal coil is that in Fig. 5-3 with an additional series resistor R^m included to account for the power dissipated in the core. The elements in the circuit are:

the radiation resistance

$$R^{r} = \frac{\zeta}{6\pi} \beta^{4} (\mu_{\rm rod} F_{\nu} N A)^{2}$$
 (5-16)

the resistance due to core loss

$$R^{m} = \omega (\mu_{rod}/\mu_{r}')^{2} \mu_{r}'' \mu_{0} F_{R} N^{2} A / \ell_{c}$$
 (5-17)

the external inductance of the loaded solenoidal coil

$$L^{\epsilon} = \mu_{\text{rod}} F_L \mu_0 N^2 A / \ell_c \tag{5-18}$$

The internal impedance of the conductor Z^i is assumed to be the same as that for the unloaded loop. The empirical factors F_R and F_L in Eqs. (5-17) and (5-18), like F_V , were determined from an average of experimental results and are also shown as a function of the ratio ℓ_c/ℓ_r in Fig. 5-9.^{10,11} It should be emphasized that the graphs for the three factors F_V , F_R , and F_L represent typical measured values and show only the dependence on the ratio ℓ_c/ℓ_r ; some dependence on the other parameters describing the coil and the rod is to be expected.

Equations (5-15) through (5-18) provide a complete description of the electrically small ferrite-loaded receiving loop (single-layer solenoidal coil with a cylindrical core); other parameters of interest, such as the Q of the antenna, can be determined

from these results. The permeability of a specific ferrite can be obtained from the manufacturer or from the extensive tables and charts in Ref. 11. The many parameters that are to be chosen for the ferrite-loaded loop, such as μ'_{r} , ℓ_{r} , ℓ_{r} , ℓ_{r} , ℓ_{r} , offer a great deal of flexibility in its design. There are several discussions in the literature that determine these parameters to optimize the performance for a particular application. 12

The electromagnetic field of the ferrite-loaded transmitting loop is given by Eqs. (5-1) to (5-3) with the moment $m = \mu_{\rm rod} F_{\nu} I_0 NA$. The ferrite-loaded loop, however, is seldom used as a transmitting antenna because of the problems associated with the non-linearity and the dissipation in the ferrite at high magnetic field strengths.¹³

5-3 ELECTRICALLY LARGE LOOPS

As the electrical size of the loop antenna is increased, the current distribution in the loop departs from the simple uniform distribution of the electrically small loop. For single-turn loops, this departure has a significant effect on performance when the circumference is greater than about 0.1 λ . For example, the radiation resistance of an electrically small circular loop with a uniform current, as predicted by Eq. (5-5), is about 86 percent of the actual resistance when $\beta b = 2\pi b/\lambda = 0.1$ and only about 26 percent of the actual resistance when $\beta b = 0.3$.

Of the possible shapes for an electrically large loop antenna, the single-turn thinwire circular loop has received the most attention, both theoretical and experimental. The popularity of the circular loop is due in part to its straightforward analysis by expansion of the current in the loop as a Fourier series:

$$I(\phi) = I_0 + 2 \sum_{n=1}^{m} I_n \cos n\phi$$
 (5-19)

where the angle ϕ is defined in Fig. 5-1.¹⁴ Measurements on electrically large loops with other shapes, such as the square loop, show that their electrical performance is qualitatively similar to that of the circular loop; therefore, only the circular loop will be discussed here.¹⁵

Circular-Loop Antenna

The theoretical model for the circular-loop antenna generally assumes a point-source generator of voltage V at the position $\phi = 0$, making the input impedance of the loop $Z = R + jX = V/I(\phi = 0)$. In practical applications, the full-loop antenna is usually driven from a balanced source, such as a parallel-wire transmission line, and the half-loop antenna, the analog of the electric monopole, is driven from a coaxial line, as in Fig. 5-10. The point-source generator of the theoretical model contains no details of the geometry of the feed point, and it is not strictly equivalent to either of these methods of excitation. However, theoretical current distributions, input impedances, and field patterns computed with the point-source generator and 20 terms in the Fourier series [Eq. (5-19)] are generally in good agreement with measured values.* Thus, the theory serves as a useful design tool.

^{*}The theoretical results in Figs. 5-11, 5-12, 5-14 to 5-18, and 5-20 were computed by the author by using 20 terms in this series.

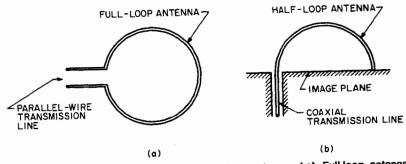


FIG. 5-10 Methods of driving the circular-loop antenna. (a) Full-loop antenna driven from parallel-wire transmission line. (b) Half-loop antenna driven from coaxial transmission line.

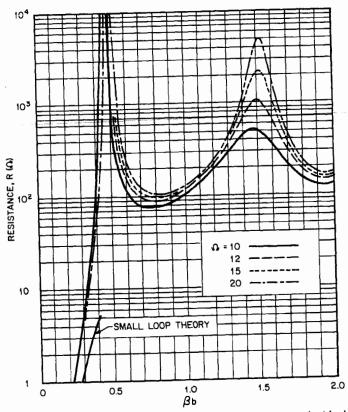


FIG. 5-11 Input resistance of circular-loop antenna versus electrical size (circumference/wavelength).

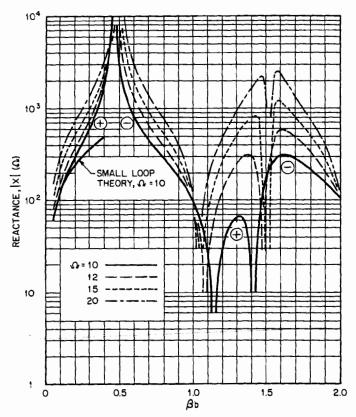


FIG. 5-12 Input reactance of circular-loop antenna versus electrical size (circumference/wavelength).

For the half-loop antenna (Fig. 5-10b), an accurate analysis, based on the Fourier series, is available that includes the details of the feeding coaxial line. ¹⁶ Results from this analysis are in excellent agreement with measurements and show such things as the change in the input impedance of the half-loop antenna with a change in the characteristic impedance of the feeding coaxial line.

In Figs. 5-11 and 5-12, the input impedance of a loop constructed from a perfect conductor is shown as a function of the electrical size of the loop $\beta b = 2\pi b/\lambda$ (circumference/wavelength) for various values of the radius of the conductor, indicated by the *thickness parameter* $\Omega = 2 \ln{(2\pi b/a)}$. These impedances are for full-loop antennas; for half-loop antennas with the same radius and conductor size, impedances are approximately one-half of these values. The reactance X is seen to be zero at points near $\beta b = \frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$, ... (antiresonant points) and $\frac{1}{2}$ and $\frac{1}{2}$ and $\frac{1}{2}$ and relative minima near the points of resonance. Impedances computed from Eqs. (5-5) and (5-7), which apply to electrically small loops, are also shown in Figs. 5-11 and 5-12; the inaccuracy of these formulas with increasing βb is evident.

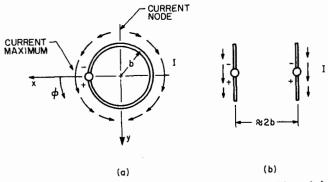


FIG. 5-13 Schematic of current distribution in resonant loop (a) and in the approximately equivalent pair of dipoles (b).

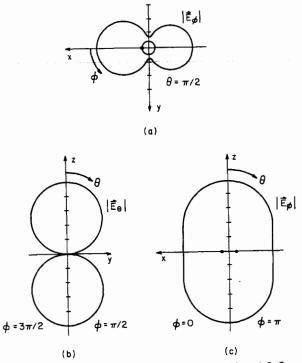


Fig. 5-14 Far-zone electric field for loop with $\beta b = 1.0$, $\Omega = 10$. (a) Horizontal-plane field pattern $|\mathbf{E}_{\phi}|$, $\theta = \pi/2$. (b) Vertical-plane field pattern $|\mathbf{E}_{\phi}|$, $\phi = \pi/2$, $3\pi/2$. (c) Vertical-plane field pattern $|\mathbf{E}_{\phi}|$, $\phi = 0$, π .

When the electrical size of the loop is near that for resonance $(\beta b = 1, 2, 3, ...)$, the dominant term in the Fourier series for the current [Eq. (5-19)] is the one with $n = \text{integer } (\beta b)$. For example, near the first resonance $\beta b \approx 1$, the current in the loop is approximately $I(\phi) = 2I_1 \cos \phi$, and the loop is commonly referred to as a resonant loop. The resonant loop $(\beta b \approx 1)$ is the most frequently used electrically large loop. It has a reasonable input resistance, $R \approx 100 \Omega$, for matching to a transmission line, particularly when compared with the resistance of the antiresonant loop $(\beta b \approx 0.5)$, which may be larger than $10 \text{ k}\Omega$.

Resonant Circular Loop

The current in the resonant loop has maxima at the generator, $\phi = 0$, and at the diametrically opposite point, $\phi = \pi$, with nodes at $\phi = \pi/2$ and $3\pi/2$. On examination of Fig. 5-13, the current is seen to be roughly equivalent to that in a pair of parallel dipole antennas driven in phase and with a spacing approximately equal to the diameter of the loop.

The far-zone field patterns for the resonant loop shown in Fig. 5-14a-c are also similar to those for the pair of dipoles; they have little resemblance to the figure-eight pattern of the electrically small loop, Fig. 5-2. There are two components to the electric field, E_{θ} and E_{ϕ} ; E_{θ} is zero in the horizontal plane $\theta = \pi/2$ and in the vertical plane $\phi = 0$, π , while E_{ϕ} is small in the vertical plane $\phi = \pi/2$, $3\pi/2$. The amplitude patterns are symmetrical about the planes $\theta = \pi/2$ and $\phi = 0$, π owing to the geometrical symmetry of the loop, and they are nearly symmetrical about the plane $\phi = \pi/2$

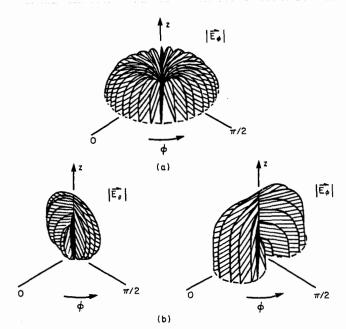


FIG. 5-15 Far-zone electric field patterns in upper hemisphere. (a) Electrically small loop, $\beta b \ll 1$. (b) Resonant loop, $\beta b = 1.0$.

 $\pi/2$, $3\pi/2$ owing to the dominance of the term $2I_1 \cos \phi$ in the current distribution. At the maxima $(\theta = 0, \pi)$ of the bidirectional pattern, the electric field is linearly polarized in the direction \hat{y} .

To help us visualize the electric field, three-dimensional amplitude patterns for the electrically small loop and the resonant loop are presented in Fig. 5-15. Each draw-

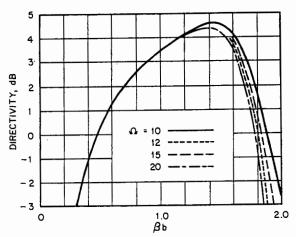


FIG. 5-16 Directivity of circular-loop antenna for $\theta=0$, π versus electrical size (circumference/wavelength).

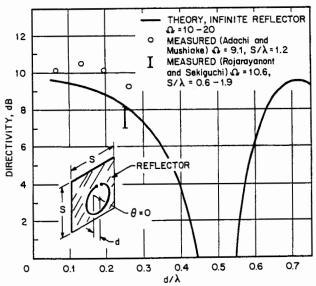


FIG. 5-17 Directivity of circular-loop antenna, $\beta b = 1.0$, for $\theta = 0$ versus distance from reflector d/λ . Theoretical curve is for infinite planar reflector; measured points are for square reflector.

ing is a series of patterns on planes of constant angle ϕ ; only the patterns in the upper hemisphere (0 $\leq \theta \leq \pi/2$) are shown, since those in the lower hemisphere are identical.

The directivity of the circular loop in the direction $\theta = 0$ or π is shown as a function of the electrical size βb in Fig. 5-16; it is about 3.4 dB for $\beta b = 1.0$ and has a maximum of about 4.5 dB for $\beta b = 1.4$. The directivity is fairly independent of the parameter Ω for $\beta b \lesssim 1.4$.

The resonant loop antenna is attractive for practical applications because of its moderate input resistance and symmetrical field pattern with reasonable directivity. The bidirectional nature of its pattern, however, is usually not desired, and a reflector or an array of loops is used to make the pattern unidirectional.

Circular Loop with Planar Reflector

The pattern of the resonant loop is made unidirectional and the directivity in the direction $\theta = 0$ is increased by placing the loop over a planar reflector. The theoretical results for an infinite perfectly conducting reflector (Fig. 5-17) show that the directivity is greater than 9 dB for spacings between the loop and the reflector in the range

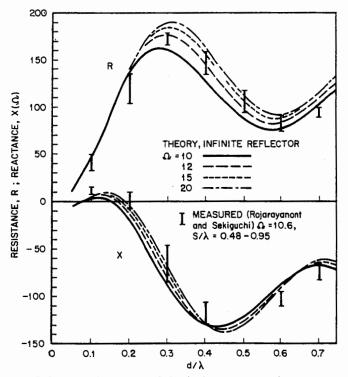


FIG. 5-18 Input impedance of circular-loop antenna, $\beta b=1.0$ versus distance from reflector d/λ . Theoretical curves are for infinite planar reflector; measured points are for square reflector.

 $0.05 \le d/\lambda \le 0.2$.¹⁷ Over this same range of spacings, the input impedance Z = R + jX (Fig. 5-18) has values which are easily matched: the resistance is reasonable $(R \le 135 \Omega)$, and the reactance is small $(|X| \le 20 \Omega)$.

The theoretical results for an infinite reflector are in good agreement with measured data for finite square reflectors of side length s. The directivities measured by Adachi and Mushiake¹⁸ (Fig. 5-17) for a reflector with $s/\lambda = 1.2$ and $d/\lambda \le 0.26$ are slightly higher than those for an infinite plane, while the input impedances measured by Rojarayanont and Sekiguchi¹⁹ (Fig. 5-18) show variations with reflector size, $0.48 \le s/\lambda \le 0.95$, but general agreement with the results for an infinite plane.

Electric field patterns measured by Rojarayanont and Sekiguchi¹⁹ for resonant loops one-quarter wavelength, $d/\lambda = 0.25$, in front of square reflectors are shown in Fig. 5-19. The shaded area in each figure shows the variation in the pattern that is a result of changing the size of the square reflector from $s/\lambda = 0.64$ to $s/\lambda = 0.95$.

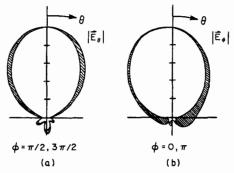


FIG. 5-19 Measured far-zone electric field patterns for loop with $\beta b=1.0$ over square reflector, $d/\lambda=0.25$. Inner curve $s/\lambda=0.95$; outer curve $s/\lambda=0.64$. (a) Vertical-plane field pattern $|\blacksquare_{\phi}|$, $\phi=\pi/2$, $3\pi/2$. (b) Vertical-plane field pattern $|\blacksquare_{\phi}|$, $\phi=0$, π . (Measured data from Rojarayanont and Sekiguchi.)

Coaxial Arrays of Circular Loops

Loop antennas, like linear antennas, can be combined in an array to improve performance. The most common array of circular loops is the coaxial array in which all the loops are parallel and have their centers on a common axis; an example of a coaxial array is shown later in the inset of Fig. 5-21. The Fourier-series analysis for the single loop is easily extended to the coaxial array when all the driven loops are fed at a common angle, e.g., $\phi = 0$ in Fig. 5-1. The current distribution in each loop is expressed as a series of trigonometric terms like that in Eq. (5-19). The simplicity of the analysis results from the orthogonality of the trigonometric terms which makes the coupling between loops occur only for terms of the same order n. Thus, if all the driven loops in the array are near resonant size, $\beta b \approx 1$, the term n = 1 is the dominant one in the current distributions for all loops; i.e., the current is approximately proportional to $\cos \phi$ in all loops.

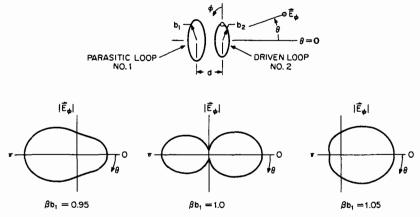


FIG. 5-20 Far-zone electric field patterns $|\mathbf{E}_{\phi}|$ in plane $\phi = 0$, π for driven loop with single parasite, $\beta b_2 = 1.0$, $d/\lambda = 0.1$, $\Omega_1 = \Omega_2 = 20$.

When all the elements in the loop array are driven, the same procedures that are used with arrays of linear elements can be applied to select the driving-point voltages to optimize certain parameters, such as directivity.²⁰ The feed arrangement needed to obtain the prescribed driving-point voltages, however, is very complex for more than a few elements in the array. As a result, a simpler and more economical arrangement, an array containing only one driven element and several parasitic loops, is often used (a parasitic loop is a continuous wire with no terminals).

When a single closely spaced parasite is used with a driven loop, the parasite may act as a director or as a reflector. This is illustrated in Fig. 5-20, in which electric field patterns are shown for a driven loop $(\beta b_2 = 1.0)$ and a parasitic loop with the spacing $d/\lambda = 0.1$. For loops of the same electrical size $(\beta b_1 = \beta b_2 = 1.0)$, the maxima in the pattern at $\theta = 0$, π are nearly equal. The parasitic loop that is slightly smaller than the driven loop $(\beta b_1 = 0.95)$ acts as a director, producing a maximum in the pattern at $\theta = \pi$, while the parasitic loop that is slightly larger than the driven loop $(\beta b_1 = 1.05)$ acts as a reflector, producing a maximum in the pattern at $\theta = 0$. This behavior is very similar to that observed for a resonant linear antenna with a closely spaced parasite.

The driven loop of electrical size $\beta b_2 = 1.2$ ($\Omega_2 = 11$, $a_1 = a_2$) with a single parasite was studied in detail by Ito et al.²¹ In that study, the optimum director was determined to be a loop with $\beta b_1 \approx 0.95$ and spacing $d/\lambda \approx 0.10$; this produced a directivity of about 7 dB at $\theta = \pi$. The optimum reflector was a loop with $\beta b_1 \approx 1.08$ and a spacing $d/\lambda \approx 0.15$; this produced a directivity of about 8 dB at $\theta = 0$. Note that, for this case, the optimum director and the optimum reflector are both smaller than the driven loop.

A Yagi-Uda array of loops with a single reflector (element 1), an exciter (the driven element 2), and several directors of equal size βb and equal spacing d/λ is shown in the inset of Fig. 5-21.* As in its counterpart with linear elements, in the

^{*}In the literature of amateur radio the Yagi-Uda array of loops, usually square loops, is referred to as a quad antenna.

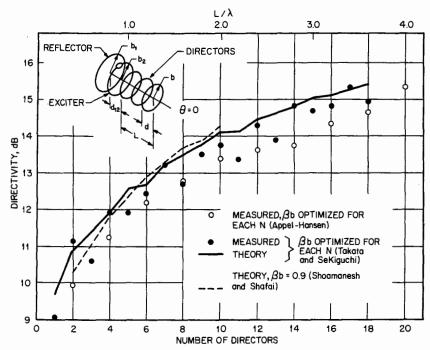


FIG. 5-21 Directivity of Yagi-Uda array of circular-loop antennas for $\theta = 0$ versus number of directors, director spacing $d/\lambda = 0.2$.

Yagi-Uda array of loops the reflector-exciter combination acts as a feed for a slow wave that propagates along the array of directors.²² The lowest-order propagating wave (mode) exists for directors less than about resonant size ($\beta b \leq 1.0$) with spacings less than about a half wavelength ($d/\lambda \leq 0.5$).²³ An array supporting this mode has an end-fire pattern with a linearly polarized electric field at the maximum, $\theta = 0$.

The procedure for designing a Yagi-Uda array of loops is the same as for an array with linear elements.²⁴ The isolated reflector-exciter combination is usually chosen to have maximum directivity in the direction $\theta = 0$. For example, the optimized two-element array described above might be used. The number, size, and spacing of the directors are then adjusted to obtain the desired performance, such as a specified end-fire directivity. The maximum end-fire directivity is determined by the electrical length of the array L/λ (L is the distance from the exciter to the last director). The larger the number of directors within the length L, the smaller the electrical size of the directors will be for maximum directivity, typically $0.8 \le \beta b \le 1.0$.

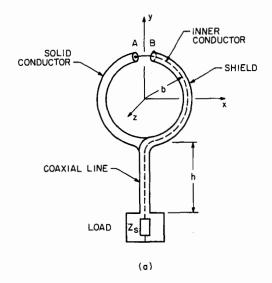
As an example, the directivity of a Yagi-Uda array of loops with the director spacing $d/\lambda = 0.2$ is shown as a function of the number of directors or the length of the array L/λ in Fig. 5-21. Two theoretical curves and two sets of measured data are

shown. All the results agree to within about 1 dB, even though they are for different reflector-exciter combinations and slightly different director sizes.*

5-4 SHIELDED-LOOP ANTENNA

For certain applications, it is desirable to position the terminals of the loop antenna precisely so as to produce geometrical symmetry for the loop and its connections about a plane perpendicular to the loop. This can often be accomplished by using the so-

^{*}The parameters used by the different investigators are: Appel-Hansen, $\beta b_1 = \beta b_2 = 1.10$, d_{12}/λ optimized for the isolated reflector-exciter, and βb optimized for each length L/λ ; Takata and Sekiguchi, $\beta b_1 = 1.05$, $\beta b_2 = 1.20$, $d_{12}/\lambda = 0.15$, and βb optimized for each length L/λ ; Shoamanesh and Shafai (1979), $\beta_1 b = 1.05$, $\beta b_2 = 1.10$, $d_{12}/\lambda = 0.1$, and $\beta b = 0.9$ for all lengths L/λ .



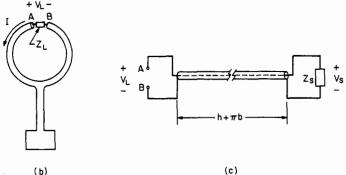


FIG. 5-22 Shielded-loop antenna (a) with equivalent antenna (b) and equivalent transmission line (c).

called shielded loop; Fig. 5-22a is an example of a shielded receiving loop whose external surface is symmetrical about the yz plane.²⁵

With reference to Fig. 5-22a, the thickness of the metal forming the shield is chosen to be several skin depths; this prevents any direct interaction between the currents on the internal and the external surfaces of the shield. The effective terminals of the loop antenna are at the ends of the small gap AB. The inner conductor and the shield form a coaxial transmission line of length $h + \pi b$ connecting the gap with the load impedance Z_S . Thus, the effective load impedance Z_L at the gap is Z_S transformed by the length of transmission line $h + \pi b$.

The receiving antenna in Fig. 5-22a is easily analyzed by considering the loop, Fig. 5-22b, and the transmission line, Fig. 5-22c, separately. The incident field produces a current on the external surface of the shield; the current passes through the effective impedance Z_L , producing the voltage V_L , which for an electrically small loop can be determined from Eqs. (5-11) and (5-13). This voltage is transmitted over the coaxial line to become V_S at the load impedance Z_S .

Other examples of the shielded loop are shown in Fig. 5-23. A balanced version of the loop in Fig. 5-22a is in Fig. 5-23a, and a method for feeding a loop in front of a planar reflector is in Fig. 5-23b.

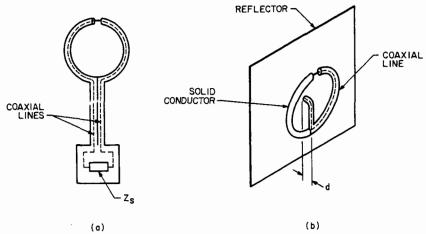


FIG. 5-23 (a) Balanced shielded-loop antenna and (b) method of feeding loop antenna in front of planar reflector.

To illustrate a typical use of the shielded loop, consider the electrically small receiving loop placed in an incident electromagnetic plane wave with the wave vector \mathbf{k}_{l} , as in Fig. 5-24. This is the same geometry as in Fig. 5-5, except that the terminals of the loop are at the angle $\phi = \phi_L$ instead of $\phi = 0$, and $\phi_l = \pi$, $\psi_l = 0$. The loop in this example might be an antenna in a direction finder with the direction of the incident wave to be determined by placing a null of the field pattern in the direction of \mathbf{k}_l .

The voltage at the open-circuited terminals of the electrically small loop, determined from the Fourier-series analysis, is approximately

$$V_{OC} = j\omega AB^{i}(\sin\theta_{i} - 2j\beta b\cos\phi_{L})$$
 (5-20)

For many applications, the second term in Eq. (5-20) is negligible, since $\beta b \ll 1$ for an electrically small loop; in this event, Eq. (5-20) reduces to Eq. (5-11) with N=1, $\psi_i=0$. In other applications, however, this term may represent a significant contri-

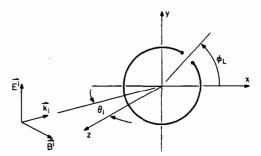


FIG. 5-24 Receiving loop in plane-wave incident field.

bution to the response. For example, the sensitivity of the antenna in the direction finder is decreased by this term because it fills in the nulls of the sin θ_I field pattern (for $\beta b = 0.1$, $\phi_L = 0$, the minima in the pattern are only 14 dB below the maxima).

The second term in Eq. (5-20) can be made insignificant by reducing the electrical size of the loop βb ; however, this will also decrease the sensitivity, since the area of the loop is decreased. An alternative is to make this term zero by placing the terminals of the loop precisely at $\phi_L = \pm \pi/2$ (cos $\phi_L = 0$); this can be accomplished by using a shielded loop as in Fig. 5-22a or Fig. 5-23a.

5-5 ADDITIONAL TOPICS

The brevity of this review requires omission of many interesting topics concerning loop antennas. In recent years, there has been considerable study of loop antennas in close proximity to or embedded in material media such as the ocean, the earth, or a plasma. The electrical characteristics of loops in these instances can be quite different from those of loops in unbounded free space, as described in this review. The major applications of this work are in the areas of subsurface communication and detection (geophysical prospecting).

The loop antenna near a planar interface separating two semi-infinite material regions, such as the air and the earth, has been investigated extensively. When the loop is electrically small, it can be approximated by an elementary magnetic dipole, and the electromagnetic field away from the loop can be determined from the classical analysis of Sommerfeld.²⁶ If the field near the electrically small loop is required, the approximation by a magnetic dipole may no longer be adequate, and a loop with a finite radius and a uniform current must be considered.²⁷ For the electrically large loop near a planar interface, an analysis that allows a nonuniform current in the loop, such as the Fourier-series analysis for the circular loop,²⁸ must be used.

The performance of a loop embedded in a material can be altered significantly by placing the loop in a dielectric cavity, such as a sphere, to form an insulated loop. The electrical size and shape of the insulating cavity and the location of the loop in the cavity can be used to control the electromagnetic field and input impedance of the antenna.²⁹

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Small Antennas

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6-1	What Is a Small Antenna? 6-2
6-2	The Radiation Power Factor 6-3
6-3	Efficiency over Losses 6-4
6-4	Efficiency over Bandwidth 6-5
6-5	The Effective Volume 6-5
6-6	The Radiation Shield 6-7
6-7	Design Procedure 6-8
6-8	Typical Small Antennas 6-9
6-9	Flush Antennas 6-11
6-10	Antennas for VLF 6-14

6-11 Symbols 6-16

A *small antenna* is here defined as an antenna occupying a small fraction of one radiansphere in space. Typically its greatest dimension is less than one-quarter wavelength (including any image in a ground plane). Some of its properties and its available performance are limited by its size and by the laws of nature. An appreciation of these limitations has proved helpful in arriving at practical designs. This chapter is a revision of the author's 1975 paper summarizing the subject.¹

The radiansphere is the spherical volume having a radius of $\frac{1}{2}$ wavelength. It is a logical reference here because, around a small antenna, it is the space occupied mainly by the stored energy of its electric or magnetic field. A small antenna is essentially an electric dipole C or a magnetic dipole L, or possibly a combination of both. $\frac{3}{4}$

Some limitations are peculiar to a passive network, in which the concepts of efficiency, impedance matching, and frequency bandwidth are essential and may be the controlling factors in performance evaluation. This discussion is directed mainly to these limitations in relation to small size. It centers in the term radiation power factor and its proportionality to volume.³

Figure 6-1 shows the principles of a small antenna exemplified by an electric dipole C. Its impedance over a bandwidth can be represented by a dummy antenna of constant parameters as follows:

- The principal reactance is $X_{\epsilon} = 1/\omega C$.
- The (much smaller) radiation resistance is $R_e \propto \omega^2$ (not indicated).
- The radiation resistance is simulated by an inductive reactance ($\omega L \ll X_e$) having in parallel a much greater constant resistance ($R \gg \omega L$). They are proportioned so that the radiation is represented by their effective series resistance, $R_e = (\omega L)^2/R \propto \omega^2$.
- The resulting (small) radiation power factor becomes:

$$p_e = R_e/X_e = \omega^3 C L^2/R \ll 1$$
 (6-1)

These relations refer to the limiting case of a small antenna. In practice, they are taken to represent the behavior at the lowest frequency (ω_1) of an operating bandwidth. They may be relaxed at the highest frequency $(\omega_2 \gg \omega_1)$ in the case of wideband operation with fixed tuning.

Figure 6-1 shows also the double tuning of the small antenna in a manner that is common and will receive further attention. It may be used to obtain a useful degree

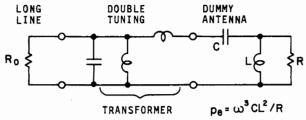


FIG. 6-1 A small antenna of C type with double tuning.

of matching of the antenna with a long line (simulated by R_0) connecting it with a transmitter and/or a receiver.

The design considerations will be presented, after which a variety of small antennas that are useful for some purposes will be described.

6-2 THE RADIATION POWER FACTOR

The term radiation power factor (PF) is a natural one introduced by the author in 1947.³ It is descriptive of the radiation of real power from a small antenna taking a much larger value of reactive power. The term is applicable to either kind of reactor, and its (small) value is limited by some measure of the size in either kind.

Here PF is equal to 1/Q, in the common parlance of networks. The term PF is preferred for describing radiation and losses because it is additive. Furthermore, the radiation PF is a positive description of what is desired (the opposite of Q).

The operating efficiency of a small antenna is limited by its radiation PF, which is proportional to its size. The nature of this limitation depends on the relative bandwidth of operation as compared with the radiation PF.

Radiation efficiency in the utilization of an antenna is relevant to transmission or reception and is defined as follows:

- In transmission, it is the fraction of available power from a generator that is radiated into space.
- In reception, it is the fraction of available power from space that is delivered to a
 load representing the receiver. It is a measure of the ability of a received signal to
 overcome the noise level in the circuits.

The generator or load is taken to have pure resistance (R_0) , which may be the wave resistance of a transmission line connecting with the antenna. In either case, the greatest efficiency of power transfer requires the familiar impedance matching suited to any situation.

Figure 6-2 shows the circuit properties of the two types of small antenna, which are identified as the electric dipole C and the magnetic dipole L. The former behaves as a capacitor and the latter as an inductor. Either is to be resonated by a reactor of the opposite kind.

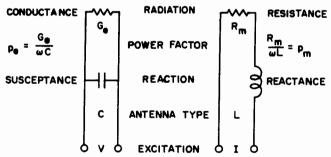


FIG. 6-2 The radiation power factor of a small antenna.

Representation of the radiation is shown in a manner consistent with circuit duality. (This is not the usual manner for C.) The radiation parameter is G_{ϵ} or R_m either one $\propto \omega^4$. Then the (small) radiation PF $\propto \omega^3$. As will be described, the power factor is proportional to the volume and may be evaluated in terms of effective volume.

Some amount of radiation PF (and hence size) may be required to achieve some measure of performance, such as radiation efficiency in transmission or its equivalent in reception. The following two situations are indicative of the two extremes:

- In narrowband operation, the relative bandwidth of operation is taken to be less than the radiation PF. Then efficiency is limited by dissipation or heat losses (loss PF) in the antenna and associated tuning reactors.
- In wideband operation, the relative bandwidth is taken to be much greater than the radiation PF. Then efficiency is limited by the ability of a passive network of fixed reactors to match the antenna to a fixed resistance.

Each of these situations will be developed by evaluating the efficiency of a model and by stating the radiation PF required for achieving this efficiency. Then a design procedure which can be adapted to an antenna of any type will be presented.

6-3 EFFICIENCY OVER LOSSES

With reference to Fig. 6-2, either type of antenna may be tuned to one frequency with an opposite reactor. Because the radiation PF is small, the efficiency may be reduced substantially by a small loss PF in the antenna and the tuning reactor.³ From the transmitter viewpoint, it is assumed that the available power can be delivered to the tuned circuit including the antenna. Then the efficiency is simply stated:

Radiation efficiency =
$$\frac{\text{radiation PF}}{\text{radiation PF} + \text{loss PF}}$$
 (6-2)

In general, greater size yields greater efficiency because it increases the radiation PF and decreases the loss PF. Conversely, a specified efficiency imposes a requirement of some size.

This situation is relevant to an antenna which has fixed or adjustable tuning to a narrowband signal. A transmitter of this type will realize this efficiency.

A simple case of this situation is the proximity fuse, in which the tuned antenna is integrated in an oscillator serving as both transmitter and receiver. The radiation efficiency becomes a measure of the reaction of a nearby object on the oscillator amplitude.

A simple case in a receiver is the tuned ferrite-core inductor used as a built-in antenna. Although the radiation efficiency is very small, it may be adequate for a purpose. In very-low-frequency (VLF) reception, the radio noise temperature is so great that the very small efficiency may be all that is useful.

6-4 EFFICIENCY OVER BANDWIDTH

A small antenna may be required to operate over a relative bandwidth (BW) much greater than its radiation PF. Matching with a line cannot be efficient over the entire BW. This is the subject of Ref. 5; it will be described here only briefly.

Over any BW $(\omega_1 \text{ to } \omega_2)$ the radiation PF at the low cutoff $(p_1 \text{ at } \omega_1)$ is the most significant property of a small antenna for impedance matching. The matching efficiency e at any frequency is the fraction of available power that is delivered from generator to load through the matching network. For double tuning, as exemplified in Fig. 6-1, the matching efficiency may vary with frequency in the manner shown in Fig. 6-3.

The objective here is taken to be the highest-level floor of e over the BW. This may be termed the *maximin* of efficiency, as indicated. It is realized by minimizing

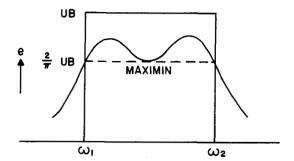


FIG. 6-3 The wideband matching efficiency.

the "useless" excess within the BW and outside. The maximin obtainable with double tuning is found to be

$$e = \frac{12p_1}{1 - (\omega_1/\omega_2)^3} \ll 1$$
 $p_1 = \frac{e}{12} [1 - (\omega_1/\omega_2)^3]$ (6-3)

A slightly higher level is obtainable by a higher order of tuning, but the theoretical upper bound (UB) is only $\pi/2$ times this level. For a required efficiency and BW, the second form gives the required radiation PF and hence the size.

6-5 THE EFFECTIVE VOLUME

For any shape of small antenna of either kind (C or L), the radiation PF at one frequency is proportional to the volume. Moreover, it is nearly equal for the two kinds if they occupy nearly equal volume. This statement needs explanation, because their configuration differs in accordance with the properties of different materials.

Figure 6-4 shows examples of the two kinds configured to occupy the space within cylinders of equal dimensions. ^{1,3} From familiar formulas for C, L, and radiation resistance, they have equal values of radiation PF except for two factors (k_a, k_b) which

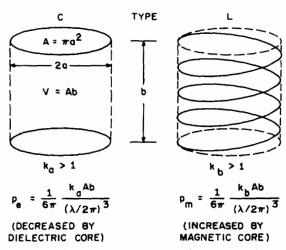


FIG. 6-4 The radiation power factor in terms of volume.

are somewhat greater than unity. Either of these factors multiplies the volume (V = Ab) to give the *effective volume* as here defined (V).

In Fig. 6-4, the effective volume is compared with the radian cube $(\lambda/2\pi)^{3.3}$ It is more logical to compare it with the volume of the radiansphere:

$$V_s = \frac{4\pi}{3} \left(\frac{\lambda}{2\pi}\right)^3 \tag{6-4}$$

Within this sphere, the stored energy or reactive power is predominant. Outside this sphere, the radiated power is predominant.

In terms of the effective volume ($V = k_a A b$ or $k_b A b$ in Fig. 6-4), the radiation becomes

$$p = \frac{%V'}{V_s} \tag{6-5}$$

(The coefficient % reflects some properties of the near field of either antenna.) The effective volume may be stated as a sphere of radius a':

$$V' = \frac{4\pi}{3} a'^3$$
 $p = \frac{2}{9} \left(\frac{2\pi a'}{\lambda} \right)^3$ $a' = \frac{\lambda}{2\pi} \left(\frac{9}{2} p \right)^{1/3}$ (6-6)

It is noted that a certain shape of self-resonant coil radiates equally from both C and L, so the total radiation is double that of either one. This is known as the helix radiator of circular polarization in the normal mode.

There is one theoretical case of a small antenna which has the greatest radiation PF obtainable within a spherical volume. Figure 6-5 shows such an antenna and its relation to the radiansphere (V_s) . It is a spherical coil with a perfect magnetic core. The effective volume of an empty spherical coil has a shape factor %. Filling with a perfect magnetic core $(k_m = \infty)$ multiplies the effective volume by 3.

$$p_m = \frac{2}{9} \frac{(3)(3/2) V}{V_s} = \frac{V}{V_s} = \left(\frac{2\pi a}{\lambda}\right)^3$$
 (6-7)

This is indicated by the shaded sphere a.

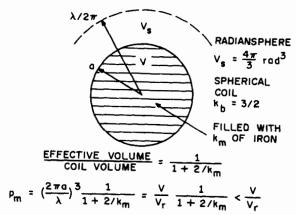


FIG. 6-5 The spherical coil with a magnetic core.

This idealized case depicts the physical meaning of the radiation PF that cannot be exceeded. Outside the sphere occupied by the antenna, there is stored energy or reactive power that conceptually fills the radiansphere, but there is none inside the antenna sphere. The reactive power density, which is dominant in the radiation within the radiansphere, is related to the real power density, which is dominant in the radiation outside.

In a rigorous description of the electromagnetic field from a small dipole of either kind, the radiation of power in the far field is accompanied by stored energy which is located mostly in the near field (within the radiansphere). The small spherical inductor in Fig. 6-5 is conceptually filled with perfect magnetic material, so there is no stored energy inside the sphere. This removes the avoidable stored energy, leaving only the unavoidable amount outside the inductor but mostly inside the radiansphere. This unavoidable stored energy is what imposes a fundamental limitation on the obtainable radiation PF.

For any actual antenna, the effective volume and its spherical radius are

$$V' = \frac{9}{2} p V_s \qquad a' = \frac{\lambda}{2\pi} \left(\frac{9}{2} p \right)^{1/3}$$
 (6-8)

This volume includes any image in an adjoining ground plane regarded as integral with the antenna. It is convenient to show any antenna configuration with its sphere of effective volume drawn to scale, as a rating of its radiation PF.

6-6 THE RADIATION SHIELD

It is difficult to measure the small radiation PF, and it is especially difficult to separate it from the loss PF of the antenna and its tuning reactor. The radiation shield was devised to separate the two.⁶

Figure 6-6 shows the concept of the radiation shield. Its purpose is to preserve the near field in the radiansphere while avoiding radiation farther out. Ideally, it is a

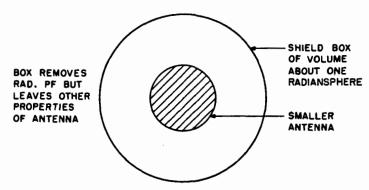


FIG. 6-6 The radiation shield for use in measuring the radiation power factor.

spherical box (of high conductivity) whose radius is $\lambda/2\pi$. Its dissipation is negligible as compared with free-space radiation.

The PF of the tuned antenna is measured with and without the shield, to give the ratio

$$\frac{\text{Loss PF only}}{\text{Loss PF + radiation PF}}$$
 (6-9)

From this ratio, the radiation PF can be evaluated as a fraction of the measured total. [See Eq. (6-2).]

The radiation shield is not critical as to size or shape. An open-ended circular or square cylinder is usually convenient. It should be large enough to avoid much disturbance of the field near the antenna and small enough to avoid cavity resonance, especially in any mode excited by the antenna. If open-ended, it should be long enough to attenuate radiation outside. A small shift of antenna resonance frequency is tolerable.

6-7 DESIGN PROCEDURE

In the design of a small antenna for operation over a frequency band (ω_1 to ω_2) a typical objective is one of these two:

- From a specified antenna, obtain the greatest efficiency by a practical circuit or less (as by economies) if sufficient for the purpose.
- To obtain specified efficiency, determine a practical circuit and antenna configuration that will require the smallest size.

For either objective, a design procedure will be outlined. Here we ignore the dissipation in the reactors of the antenna and matching network.

The properties of a specified antenna are evaluated by computation and/or measurement. The principal properties are the essential C or L and the radiation PF. The reactance is the dominant factor in designing a lossless matching network such as the

double tuning in Fig. 6-1. The result to be expected is the double-peak graph in Fig. 6-3 and the matching efficiency from Eq. (6-3).

The other objective is essentially the reverse. The required efficiency is specified, and perhaps also a tolerance of the voltage standing-wave ratio (VSWR). The network configuration is specified as a practical constraint on complication. Figure 6-1 is taken as an example.

From the specified efficiency and BW, the required radiation PF can be computed by Eq. (6-3). The required effective volume is then given by Eq. (6-8), also its spherical radius α' . These are stated in terms of the radiansphere and radianlength at the lowest frequency (ω_1) .

For any kind and shape of antenna, size is related to the effective volume or spherical radius. The latter will be shown to scale for some typical configurations.

6-8 TYPICAL SMALL ANTENNAS

A number of typical small antennas are here compared with the effective volume by diagrams showing to scale the sphere of this radius:

$$\alpha' = \frac{\lambda}{2\pi} \left(\frac{9}{2} p \right)^{1/3} \tag{6-10}$$

It is drawn as a dashed circle.

Figure 6-7 shows some examples of an electric dipole with a linear axis of symmetry. A thin wire (a) and a thick conical conductor (b) differ greatly in occupied volume but much less in effective volume. The latter is influenced most by length and less by the smaller transverse dimensions.

Figure 6-7c shows a pair of separated disks like the basic electric dipole in Fig. 6-4. Their simple rating can be preserved by the use of a tuning inductor in the form of a coil distributed between the ends as shown.

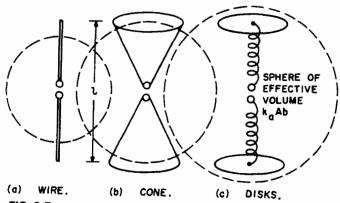


FIG. 6-7 The effective volume of an axial electric dipole.

With reference to Fig. 6-4 for a pair of disks, the area factor and the effective volume are (within 5 percent)

$$k_a = 1 + \frac{4}{\pi} b/a$$
 $V' = k_a \pi a^2 b = \pi a^2 b + 4ab^2 > 2\sqrt{4\pi a^3 b^3}$ (6-11)

Converting the last expression to the lower bound (LB) of effective radius (within 2 percent) yields

LB
$$a' = 1.19 \sqrt{ab}$$
 (6-12)

This simple formula, being noncritical as to shape, is useful for estimating purposes. For the shape shown in Fig. 6-7c, the sphere diameter is slightly greater than the length.

The thin disks shown in Figs. 6-4 and 6-7c do not make the fullest use of the occupied cylindrical space. The fullest use would be made by adding to each disk a skirt going about halfway to the neutral plane of symmetry. The decrease of effective length would be more than compensated by the increase of C, to give greater effective volume.

Figure 6-8 shows some examples of a loop inductor on a square frame. A thin wire (a) and a wide strip (b) differ rather little in effective volume, because this is influenced most by the size of the square. A multiturn loop (c) has nearly the same effective volume as one turn occupying the same space. This is one of the principal conclusions presented in the writer's first paper.³

It happens that a cubic coil has a simple length factor $(k_b = \frac{4}{3})$. The diameter of the sphere of effective volume is nearly equal to the diagonal of one face. Likewise, a spherical coil has an effective volume $\frac{4}{3}$ times its enclosed volume.

The effective volume of a square or circular coil may be stated by comparing the sphere radius with the coil radius (a = radius of circle or half side of square):

Circle: LB
$$a' = 1.12 \ a(b/a)^{1/6}$$
 (6-13)

Square: LB
$$a' = 1.25 \ a(b/a)^{1/6}$$
 (6-14)

As might be expected, the radiation PF is determined mainly by the radius.

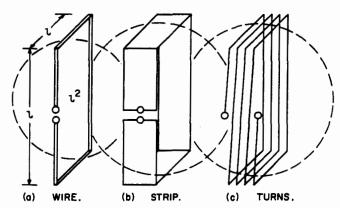


FIG. 6-8 The effective volume of a square loop.

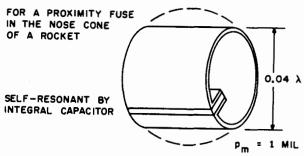


FIG. 6-9 A one-turn loop of wide strip.

Figure 6-9 shows a particularly effective small antenna with integral tuning. It is a one-turn loop of a wide strip which has remarkably small loss PF. In an extremely small size, its radiation efficiency was found to be about 50 percent.

One-half of any of these configurations can be imaged in a ground plane. The result is an equal effective volume, which may be represented as a hemisphere on the plane.

6-9 FLUSH ANTENNAS

A useful family of small antennas comprises those that are recessed in a shield surface such as a ground plane or the skin of an aircraft. Some may embody inherently flush designs, while others may be suited for operation adjacent to a shield surface, whether recessed or not. The antenna may be of the C or the L type, either radiating in a polarization compatible with the shield surface.

Figure 6-10 shows a flush disk capacitor (sometimes termed an annular slot). This capacitor in the flush mounting may be compared with a like capacitor just above the surface. The recessing somewhat reduces the radiation PF. The remaining effec-

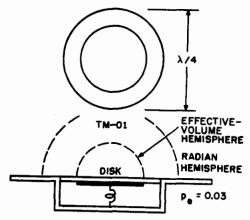


FIG. 6-10 A flush disk capacitor.

tive volume is that of a hemisphere indicated by the dashed semicircle. Its size is comparable with that of the disk. The cylindrical walls may be regarded as a short length of waveguide beyond cutoff, operating in the lowest transverse magnetic (TM) mode (circular TM-01, as shown, or rectangular TM-11). The capacitor may be resonated by an integral inductor as shown. In any cavity, there is a size and shape of disk that can yield the greatest radiation PF. The primary factor is the size of the cavity.

The evaluation of a flush antenna includes the shield surface. It is necessary first to evaluate the radiation PF by some method of computation. Then the radiation PF can be stated in terms of a volume ratio. Here we consider the half space of radiation and show the hemisphere of $\frac{1}{2}V'$, which may then be compared with the half radian-sphere, $\frac{1}{2}V'$. The radii are retained (a' and $\frac{1}{2}\pi)$. An antenna located on the surface (not recessed) could be considered with its image to yield the complete sphere of V' to be compared with the radiansphere V_1 . Then one-half of each may be shown above the shield plane, as for the flush antenna.

The disk capacitor radiates in the same mode as a small vertical electric dipole, by virtue of vertical electric flux from the disk. This is vertical polarization on the plane of the shield, with omnidirective radiation. The other examples of a flush antenna, to be shown here, radiate as a small horizontal magnetic dipole by virtue of magnetic flux leaving the cavity on one side and returning on the other side. This is vertical polarization but directive in a figure-eight pattern. Omnidirective radiation can be provided by quadrature excitation of two crossed modes in the same cavity. The radiation PF of either kind is reduced by recessing, but the magnetic dipole suffers less reduction.

Figure 6-11 shows an idealized cavity resonator which radiates as an inductor. The cavity is covered by a thin window of high-k dielectric, which serves two purposes. It completes the current loop indicated by the arrows I, and it also provides, in effect, series capacitance which resonates the current loop. The cylindrical walls and the aperture excitation may be regarded as the lowest (cutoff) transverse electric (TE) mode (circular TE-11 or rectangular TE-10 to TE-01, as shown). Each of these modes has two crossed orientations, of which one is indicated by the current loop. The con-

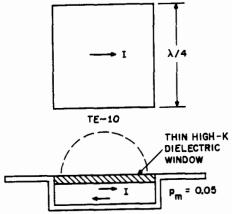


FIG. 6-11 A flush cavity inductor with a dielectric window.

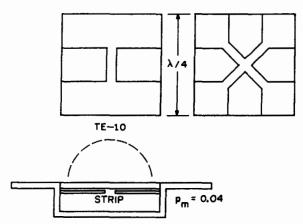


FIG. 6-12 A flush strip inductor.

tinuous dielectric sheet on a square or circular cavity resonates the two crossed modes. Because each resonance is in the lowest mode, it involves the smallest amount of stored energy relative to radiated power and therefore the greatest value of radiation PF.

Figure 6-12 shows some practical designs which yield nearly the same performance by the use of conductive strips on ordinary (low-k) dielectric windows (high-k dielectric is not required). Here the radiating inductor (strip) and the resonating series capacitor (gap) are apparent. The two alternatives, one mode and a pair of crossed modes, are shown. Practical designs about $\lambda/4$ square have been made with radiation PF about 0.04. This is about the largest size that follows the rules of a small antenna.

The required coupling with any of the resonant antennas in Figs. 6-10 to 6-12 may be provided by another (smaller) resonator located within the cavity. This enables the bandwidth of matching expected from double tuning. Each of these antennas is suited for self-resonance and requires some depth of cavity to hold down the extra amount of energy storage in this nonradiating space.

Figure 6-13 shows a flush inductor made of crossed coils on a thin magnetic disk. At medium or low frequencies (MF, LF, VLF) the available ferrite materials can provide a magnetic core that forms a return path nearly free of extra energy storage even in the thin disk. It also adds very little dissipation. The required depth of cavity is then only sufficient to take the disk thickness with some margin. The antenna is too small relative to the wavelength at the lower frequencies to enable high efficiency even at its frequency of resonance, so it is useful only for reception. A rotary coil or crossed coils can be used for a direction finder or omnidirectional reception. The principal application is on the skin of an aircraft.

Figure 6-14 shows the ferrite-rod inductor, the antenna most commonly used in a small broadcast receiver (MF, around 1 MHz). The ferrite rod greatly increases the effective volume of a thin coil, as indicated. The effective volume is then determined primarily by the length rather than the diameter of the coil. Like the ferrite disk, this antenna can be used close (parallel) to a shield surface or be recessed in the surface.

Here we may note that a long coil, with its small shape factor $(k_b \to 1)$, can have its effective volume greatly increased by a ferrite core. On the other hand, a parallel-plate capacitor, with its small shape factor $(k_a \to 1)$, can only have its effective volume decreased by a dielectric core. This is one respect in which the inductor offers greater

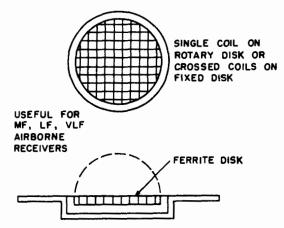
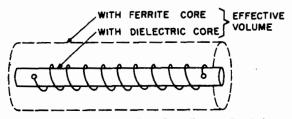


FIG. 6-13 A flush inductor on a thin ferrite disk.



MAY BE LOCATED NEAR A SHIELD PLANE (OR FLUSH)
NEARLY DOUBLING EFFECTIVE VOLUME (BY IMAGE EFFECT)

FIG. 6-14 A long coil on a ferrite rod.

opportunity in design. In another respect, the number of turns can be used to set the impedance level, a freedom that may be desired but is unavailable in a simple capacitor.

If a long coil as a magnetic dipole were filled with perfect magnetic material, its effective volume would be comparable with that of an equally long conductor as an electric dipole.

6-10 ANTENNAS FOR VLF

The greater the wavelength, the more relevant may be the concept of a small antenna. Current activities go as low as 10 kHz with a wavelength of 30 km. Even the largest of the transmitter antennas is small in terms of this wavelength, or its radianlength of 5 km.

For reception, however, a much smaller antenna is adequate for one of two reasons:

 Above the surface (ground or sea) the radio noise level is so high that it still becomes the limiting factor in a small antenna with very low efficiency of radiation. Below the surface, in salt water like the ocean, the radianlength (equal to the skin depth) is only a few meters, so a small antenna may occupy a substantial fraction of the radiansphere.

For the former purpose, the magnetic antennas in Figs. 6-13 and 6-14 are suited for VLF. For the latter purpose, different factors become relevant.

The principles of the smallest effective underwater receiving antenna will be formulated with reference to Fig. 6-15. It is similar to a retractable antenna used on a submarine, which may be submerged to a small depth. This is an inductor in a hollow cavity (radome). It has greater radiation efficiency than a capacitor because it is subject to smaller near-field losses caused by the conductivity of the water. Also, it avoids the need for conductive contact with water.

Figure 6-15 shows an idealized small antenna in a submarine cavity. 6,7 It is a spherical coil with a magnetic core, as shown in Fig. 6-5. In the water, the radianlength is equal to the skin depth (δ). At 15 kHz, this is about 2 m. The size of the cavity is much less and that of the coil still less, so it is a small antenna in this environment. The radiation PF includes two quantities, the desired coupling to the medium and the undesired dissipation in the medium. The former is proportional to the coil volume and is increased by the magnetic core. The latter is decreased by increasing the cavity radius. The coil is in the vertical plane for vertical polarization. Crossed coils may be used for omnidirective reception and direction finding.

For a transmitter antenna, the capacitor is usually chosen for vertically polarized radiation in all directions on the horizon.

For efficient transmission at lower frequencies, one of the early simple types is that shown in Figure 6-16.8 It is a flattop grid of wires forming a capacitor with ground as the lower conductor. The effective height h determines the radiation resistance. The capacitance enables the statement of an effective area (k_aA) as noted. The effective volume (k_aAh) in half space is compared with one-half radiansphere to determine the radiation PF. It is notable that the grid of many wires may provide an effective area greater than that of the grid despite the much smaller area of the conductor.

A large transmitting antenna for radiating high power presents different prob-

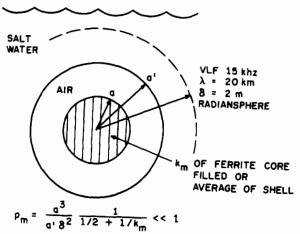


FIG. 6-15 An inductor in a radome submerged in seawater.

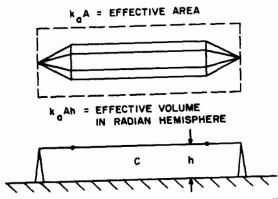


FIG. 6-16 A large flattop capacitor which is still small relative to the wavelength.

lems relating to power, current, and voltage. The compromise solutions of these problems require size as measured in these three ways:

- Effective volume for radiation PF to operate over a bandwidth and to compete with any loss PF
- Effective height squared for radiation of power proportional to current squared
- Effective area for radiation of power proportional to voltage squared

The first is the principal topic of this chapter. The second and third have been presented in Ref. 8 and are stated here as design requirements.

$$h = \frac{\lambda}{2\pi I} \sqrt{P/40} \qquad k_a A = \pi \left(\frac{\lambda}{2\pi}\right)^2 \left(\frac{3}{V}\right) \sqrt{40P} \qquad (6-15)$$

For example, the last relation states the effective area required if the voltage is limited by supporting insulators. If, in addition, the average voltage gradient on the wires is restricted by corona discharge to a value E_a (rms volts/meter), the required surface area of the wires (A_a) is proportional to the current (or \sqrt{P}):

$$A_a = \pi \left(\frac{\lambda}{2\pi}\right)^2 \frac{3}{hE_a} \sqrt{40P}$$
 (6-16)

Large VLF antennas are the principal topic of Chap. 24. Some are described in Refs. 1 and 9. The largest are the Navy stations at Cutler, Maine (NAA), and North West Cape, Australia (NWC). These qualify as small antennas by a large margin at their lowest frequencies of operation.

6-11 SYMBOLS

p = 1/Q = radiation power factor (PF)

X = reactance

C =capacitance of a small electric dipole antenna

L = inductance of a small magnetic dipole antenna

R =series resistance

G = parallel conductance

 $\omega = 2\pi f = \text{radian frequency}$

 $\lambda/2\pi$ = radianlength

 λ = wavelength

 $e = 1 - \rho^2 = \text{matching efficiency}$

A =area of cylinder

a = radius of cylinder or sphere

a' = effective radius of sphere of effective volume

b = axial length of cylinder

 $V_s = (4\pi/3)(\lambda/2\pi)^3$ = volume of radiansphere

V' = effective volume of C or L

 k_a = shape factor for effective area of a cylindrical capacitor

 k_h = shape factor for effective axial length of a cylindrical or spherical inductor

 k_m = magnetic constant (relative permeability)

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Microstrip Antennas

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7-1 Introduction 7-2
7-2 Microstrip-Antenna-Element Design
Parameters 7-2
Microstrip-Antenna Impedance 7-3
Microstrip-Element Antenna Patterns 7-5
Microstrip-Antenna Bandwidth 7-7
Microstrip-Antenna Mutual Coupling 7-9
Microstrip-Antenna Efficiency 7-10
Circularly Polarized Microstrip Elements 7-14
Dual-Frequency, Dual-Polarization Microstrip-Antenna Element 7-16

7-3 Microstrip-Array Design Principles 7-19
Omnidirectional Microstrip Arrays 7-19
Fixed-Beam Microstrip Arrays 7-23
Microstrip Phased Arrays 7-25
Series-Fed Microstrip Arrays 7-26
Monolithic Phased Arrays 7-29

Microstrip-antenna elements radiate efficiently as devices on microstrip printed-circuit boards. Microstrip-antenna arrays consist of microstrip-antenna elements, feed and phasing networks, and any other microstrip devices. Both microstrip-antenna elements and microstrip arrays are discussed in this chapter.

7-2 MICROSTRIP-ANTENNA-ELEMENT DESIGN PARAMETERS

This section can be used as a guide in selecting and designing microstrip elements which can be used alone as single radiators or as elements of microstrip phased arrays, which are discussed in Sec. 7-3.

The most commonly used microstrip element consists of a rectangular element that is photoetched from one side of a printed-circuit board (Fig. 7-1). The element is fed with a coaxial feed. The length L is the most critical dimension and is slightly less than a half wavelength in the dielectric substrate material.

$$L \approx 0.49 \lambda_d = 0.49 \frac{\lambda_0}{\sqrt{\epsilon_r}}$$

where L = length of element

 ϵ_r = relative dielectric constant of printed-circuit substrate (The exact value is critical and is usually specified and measured by the manufacturer.)

 λ_0 = free-space wavelength

The variation in dielectric constant and feed inductance makes it hard to predict exact dimensions, so usually a test element is built to determine the exact length.

The thickness t is usually much less than a wavelength (usually on the order of $0.01\lambda_0$). The selected value of t is based on the bandwidth over which the antenna must operate; it is discussed in greater detail later. The exact value of t is determined by commercially available board thicknesses, such as 0.005 in (0.127 mm), 0.010 in (2.54 mm), $\frac{1}{100}$ in (0.397 mm), $\frac{1}{100}$ in (1.588 mm), $\frac{1}{100}$ in (1.191 mm), $\frac{1}{100}$ in (3.175 mm), etc. Teflon-fiberglass boards are commercially available from Rogers Corporation, ARLON, and Oak Industries.

The width W must be less than a wavelength in the dielectric substrate material

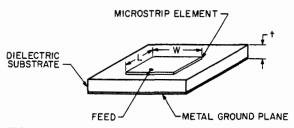


FIG. 7-1 Rectangular microstrip-antenna element.

so that higher-order modes will not be excited. An exception to this constraint, in which multiple feeds are used to eliminate higher-order modes, is discussed later.

Most microstrip elements are fed by a coaxial connector which is soldered to the back of the ground plane; the feed pin is soldered to the microstrip element as shown

in Fig. 7-2. A direct-contact feed (rather than a probe, as in waveguide feeds) is always used. It is important that the feed pin be securely soldered to the microstrip element since most failures of microstrip antennas occur at this point.

A second microstrip-antenna element commonly used is the quarter-wave microstrip-antenna element (Fig. 7-3). It consists of a photoetched element in which the length L is about a quarter

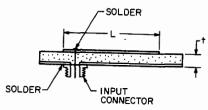


FIG. 7-2 Side view of microstrip element with coaxial-feed connection.

wavelength in the substrate material. Such an element is used for its broader E-plane beamwidth. A third microstrip-antenna element is a full-wavelength element, which is similar to that in Fig. 7-1 except that the feed is at the center and the length L is a full wavelength in the substrate material. Its radiation pattern is similar to that of a monopole. This element can also be round and of equal area to the equivalent square element.

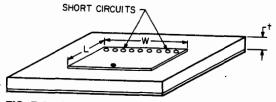


FIG. 7-3 Quarter-wave microstrip element.

Microstrip-Antenna impedance

The surprising feature of a microstrip antenna is its efficient radiation despite its low profile. As the thickness of a microstrip antenna is reduced, its radiation resistance approaches a constant value. The source of radiation for the rectangular microstrip radiator shown in Fig. 7-1 is the electric field (Fig. 7-4) that is excited between the edges^{1,2} of the microstrip element and the ground plane (excitation of a nearly infinitesimal slot with uniform E field). The fields are excited 180° out of phase between the opposite edges.

The input impedance of the microstrip element can be calculated from the equivalent circuit in Fig. 7-5; R_R (the radiation resistance of each slot) can be calculated for a uniformly excited slot as a function of width by

$$R_R = 120\lambda_0/W$$

Since the microstrip element consists of two slots that combine in parallel, the input impedance is given as

$$R_{\rm in} = 60\lambda_0/W$$

The susceptance of the slots is shown to combine at resonance to cause a shortening

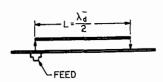


FIG. 7-4 Side view of rectangular microstrip electric fields.

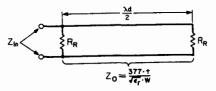


FIG. 7-5 Equivalent circuit for determining input impedance of rectangular microstrip element.

of the microstrip element to values typically less than a half wavelength, such as $L = 0.49\lambda_d$.

The input impedance can be matched to $50~\Omega$ by using one of two techniques. For an element that is to be employed individually, a coaxial input connector is used. The $50-\Omega$ -impedance point may be obtained by varying the distance from the edge of the element to the feed location ℓ , as shown in Fig. 7-6. Note that the impedance of the element goes essentially to zero at the center of the element. Sometimes it is necessary to ground a microstrip element; the use of a rivet or a plated-through hole at the center of the element results in negligible effects on patterns and a small change in resonant frequency. Likewise, for air-loaded microstrip elements a metal support is used at the center of the element. When an element is to be used in a microstrip array, it is fed at the edge, and a

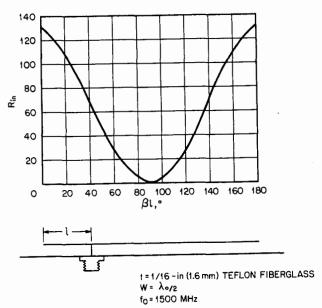


FIG. 7-6 Input-impedance variation as a function of feed location for a rectangular microstrip element (side view).

quarter-wave transformer is used to convert the input impedance to any desired level (Fig. 7-7).

The quarter-wave microstrip element has an impedance twice that of the rectangular microstrip element. The input impedance can be calculated from the equivalent

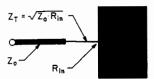


FIG. 7-7 Matching a rectangular microstrip element by using a monolithic quarterwave transformer (top view).

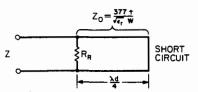


FIG. 7-8 Equivalent circuit for a quarterwave microstrip element.

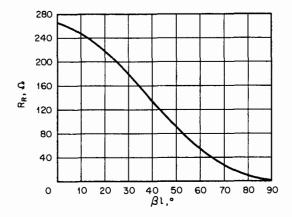
circuit shown in Fig. 7-8. At resonance (when the distance from the short circuit to the radiating slot is a quarter wavelength) the short circuit transforms a quarter wavelength to become an open circuit. The open circuit combines in parallel with R_R , the radiation resistance of the single slot. The resulting input impedance is given by $Z_{in} = R_R = 120\lambda_0/W$.

For a quarter-wavelength element that is a half wavelength wide the radiation resistance and input impedance are 240 Ω . This is very high, and a 5:1 voltage standing-wave ratio (VSWR) would occur if a 50- Ω coaxial connector were directly connected to the edge of the element. Therefore, the feed point is inset a distance ℓ from the edge or slot as shown in Fig. 7-9. The input impedance of a quarter-wave element may also be matched by using a quarter-wave transformer as discussed for the rectangular microstrip element. Sometimes the line widths of a quarter-wave transformer become too narrow, so an inset monolithic feed is used as shown in Fig. 7-10. The distance ℓ given in Fig. 7-9 is used as a starting point, but exact dimensions are usually determined experimentally.

Microstrip-Element Antenna Patterns

Microstrip antennas have radiation patterns that can be accurately calculated. The key to accurate calculation is the fact that the source of radiation is the electric field across a small gap formed by the edge of the microstrip element and the ground plane directly below. Since its dimension $t \ll \lambda_d/4$, the individual slots cannot exhibit any directionality. Each slot therefore radiates an omnidirectional pattern into the half space above the ground plane. Figure 7-11 shows a side view of a rectangular microstrip element and its associated source and radiating E fields.

The opposing slots are excited out of phase, but their radiation adds in-phase normal to the element. This occurs because the slots are inverted. The radiation of two slots excited in phase with equal amplitude is given by



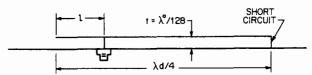


FIG. 7-9 Measured input impedance as a function of ℓ (ℓ is the distance to which the feed is inset into a $\lambda_d/4$ element).

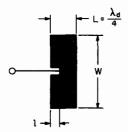


FIG. 7-10 Monolithic feed for a quarterwave microstrip.

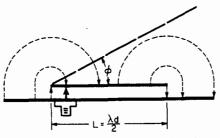


FIG. 7-11 Side view of a rectangular microstrip element and associated radiation.

$$E = K \cos \left(\frac{\pi L}{\lambda_0} \cdot \cos \phi \right)$$

Since the microstrip element is resonant at a half wavelength in the dielectric under the element,

$$E_{\phi} = K \cos \left(\frac{\pi}{2\sqrt{\epsilon_r}} \cdot \cos \phi \right)$$

This formula is valid for $0^{\circ} < \phi < 180^{\circ}$ (above the ground plane). The formula is not exact near the ground plane. Edge radiation from the end of the ground plane usually reduces theoretical radiation by 6 dB at $\phi = 0^{\circ}$ and 180° . Some radiation also will occur in the aft hemisphere $180^{\circ} < \phi < 360^{\circ}$. The exact amount of afthemisphere radiation diminishes rapidly as the ground plane becomes large in wavelengths. The theoretical *E*-plane patterns for two commonly used rectangular microstrip elements are shown in Fig. 7-12*a* and *b*.

The quarter-wavelength microstrip element radiates from a single slot; thus its E-plane radiation is uniform $(E_{\phi} = K)$ for $0^{\circ} < \phi < 180^{\circ}$ for an infinite perfect conducting ground plane. The measured pattern for a quarter-wavelength element centered on a $6\lambda_0$ ground plane is shown in Fig. 7-13. Note that the radiation is reduced by about 6 dB at $\phi = 0^{\circ}$ and 180°. The backlobes and ripple in the radiation pattern would be reduced as the ground plane got larger.

The H-plane patterns of the rectangular and quarter-wavelength microstrip elements are given by the formula for a uniformly excited radiator:

$$E_H = K \tan \theta \sin \left(\frac{\pi W}{\lambda_0} \cdot \cos \theta \right)$$

where θ = angle above ground plane in the H plane.

The full-wavelength element has a radiation pattern similar to that of a monopole. The pattern of this element is given by

$$E_{\phi} = K \sin \left(\frac{\pi}{\sqrt{\epsilon_r}} \cdot \cos \phi \right)$$

The pattern of a center-fed, air-loaded, $\epsilon_r = 1.0$ element is shown in Fig. 7-14. The radiation pattern of a round full-wavelength microstrip element fed at the center is given by

$$E = KJ_1\left(\frac{2\pi}{\lambda_0} \cdot a \cdot \sin\theta\right)$$

where J_1 = Bessel function of first kind

a = radius of element

The round full-wavelength microstrip element has essentially the same pattern as the square full-wavelength microstrip element of equivalent area and identical dielectric-constant substrate.

Microstrip-Antenna Bandwidth

The bandwidth of microstrip antennas is proportional to the thickness of the substrate used. Since most substrates are very thin in terms of wavelengths $(t \ll \lambda_0/4)$, the

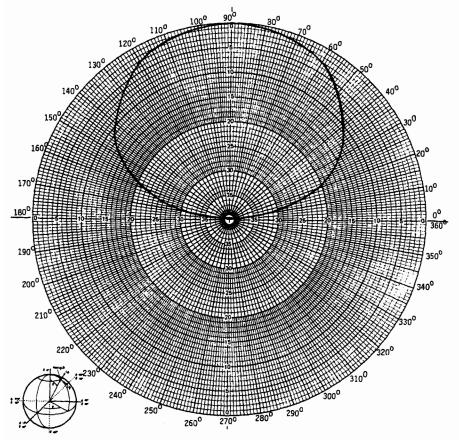


FIG. 7-12a Theoretical E-plane pattern of a rectangular microstrip element for $\epsilon_r = 1.0$.

bandwidth is usually narrow. A useful formula for determining expected microstrip-element bandwidth is given by

$$BW = 4f^2 \left(\frac{t}{1/32}\right)$$

where BW = bandwidth, MHz, for a VSWR less than 2:1

f =operating frequency, GHz

t = thickness, in [Most board thicknesses are available in steps of ½ in (0.794 mm).]

Since the feed networks used to feed most microstrip arrays are low-Q, the bandwidths of most arrays are given by the preceding formula. Exceptions are large seriesfed microstrip arrays and microstrip phased arrays. With these two types of arrays, the pattern often degrades before the VSWR increases.

Broadbanding techniques discussed in Chap. 43 have been applied to microstrip elements. In most cases, the bandwidth has been doubled, but it is very difficult to increase the bandwidth beyond this point. It is much easier to increase the thickness

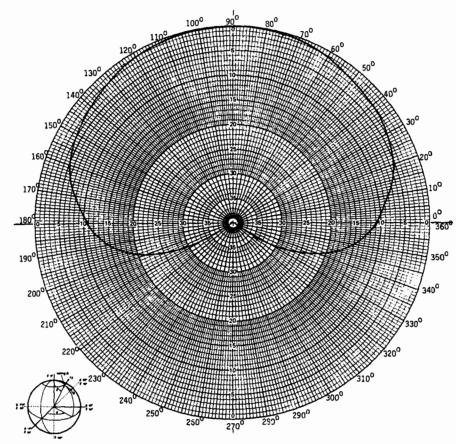


FIG. 7-12b Theoretical E-plane pattern of a rectangular microstrip element for $\epsilon_r \approx 2.45$.

of the microstrip element. It seems certain that the bandwidth of a microstrip element is related directly to its volume.

Microstrip-Antenna Mutual Coupling

When microstrip elements are used in arrays, ultimate performance is attained for each design if mutual coupling is minimized. Three methods of coupling exist:

- 1 Coupling between microstrip elements (Figs. 7-15 and 7-16)
- 2 Coupling between microstrip transmission lines and microstrip elements (Figs. 7-17 and 7-18)
- 3 Coupling between microstrip transmission lines (Table 7-1)

The coupling between microstrip elements in Figs. 7-15 and 7-16 affects the pattern shape of the elements, radiated power and phase, and input VSWR. The coupling

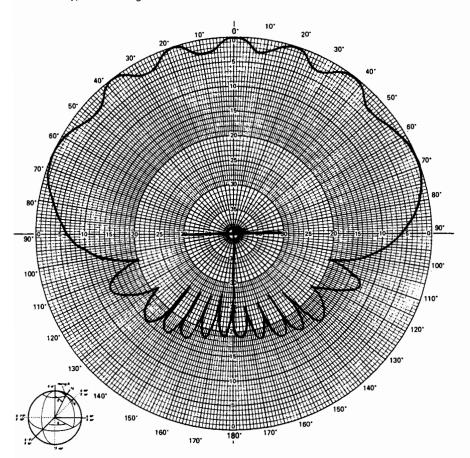


FIG. 7-13 Measured *E*-plane pattern of a quarter-wavelength element on a $6\lambda_o$ ground plane.

between feed lines and microstrip elements affects the radiation patterns, radiation phase and amplitude, antenna impedance, and microstrip transmission-line match. The coupling between transmission lines affects the transmission-line match.

If the separations are maintained so that coupling is less than 20 dB (usually three substrate thicknesses t), the gain and VSWR of the antenna are not degraded. For a low-sidelobe antenna, isolations of 30 dB or more are required.

Microstrip-Antenna Efficiency

For a microstrip element, efficiency is defined as the power radiated divided by the power received by the input to the element. Factors that reduce efficiency are the dielectric loss, the conductor loss, the reflected power (VSWR), the cross-polarized loss, and the power dissipated in any loads involved in the elements. Most microstrip elements are between 80 and 99 percent efficient. For very thin elements the Q of the microstrip cavity becomes so high that the current losses become excessive, and the

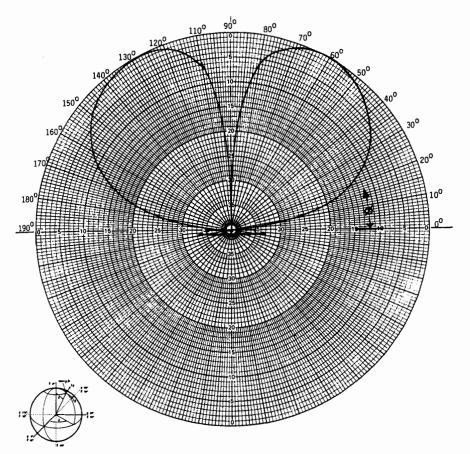


FIG. 7-14 Theoretical radiation pattern of the full-wavelength element for $\epsilon_r = 1.0$.

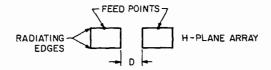
thickness t becomes so small that the conductance across the cavity yields excessive dielectric losses. This usually occurs when the thickness is reduced to about $\lambda_0/1000$. At this thickness, the resonance VSWR can be matched to 50 Ω , but the very narrow bandwidth leads to temperature instabilities; i.e., a slight change in temperature causes the VSWR to rise rapidly, and reflection losses reduce efficiency.

Dielectric losses are eliminated by using air as a substrate. Since most of these elements have a large separation between the element and ground plane t, the Q is also reduced and so are conductor and VSWR losses. Most of these elements have an efficiency of 95 to 99 percent. Air-loaded elements are usually built as separate entities and are not photoetched in large arrays. A single metal part, rivet, or bolt is used at the center of the element for support. To build a photoetched array by using a nearly air substrate, a honeycomb core is employed to separate the microstrip elements and feed network from the ground plane. A 35-ft by 8-ft (10.7-m by 2.4-m) array was built on a honeycomb core for the Seasat satellite program (1978) with an aperture efficiency of 60 percent. (This included all feed-network losses.)

Microstrip elements are not efficient if solid epoxy fiberglass is used as a sub-

TABLE 7-1 Isolation (dB) of Parallel Microstrip Transmission Lines

Board thickness, in	Board spacing (number of thicknesses)	Frequency			
		2.0 GHz	2.7 GHz	3.4 GHz	4.0 GHz
Же	1	8.0	12.5	8.0	3.0
	2	11.0	13.0	12.5	5.0
	3	17.5	18.0	17.5	10.0
İ	4	25.0	25.0	26.0	17.5
⅓₂	1	10.0	12.0	10.0	2.5
	2	12.5	15.0	13.5	5.0
	3	17.5	17.5	15.0	9.5
	4	25.0	25.0	27.5	16.5
1/64	1	10.0	10.0	11.5	2.5
	2	10.0	12.5	12.0	5.0
	3	17.5	16.0	22.5	10.0
	4	25.0	24.0	22.5	17.5



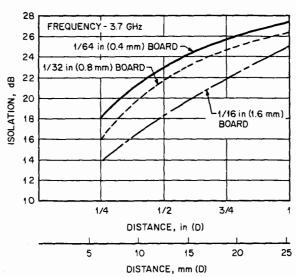
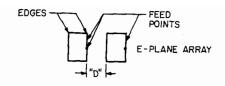


FIG. 7-15 Isolation of two half-wave microstrip patch radiators as a function of their H-plane separation.



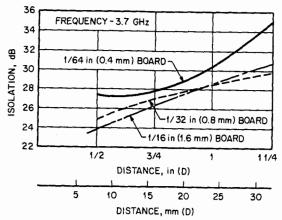


FIG. 7-16 Isolation of two half-wave microstrip patch radiators as a function of their *E*-plane separation.

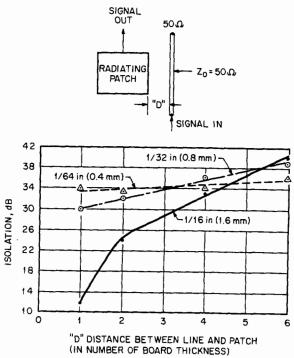
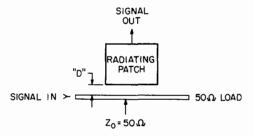


FIG. 7-17 Isolation between radiating patch and feed line along *H* plane.



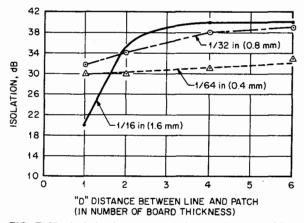


FIG. 7-18 Isolation between radiating patch and feed line along \boldsymbol{E} plane.

strate. Repeated attempts to circumvent the use of expensive Teflon-fiberglass substrates have resulted in antenna elements with efficiencies of 10 percent.

The efficiency of microstrip phased arrays depends upon microstrip-element efficiency, feed-network losses, and phase and amplitude distribution. These efficiencies are discussed later.

Circularly Polarized Microstrip Elements

Microstrip elements are probably the simplest and thinnest devices for producing circular polarization. Three methods for producing circular polarization have been developed. A microstrip element (Fig. 7-19) that is square with L and W equal to $\lambda_d/2$ will have two modes of radiation, vertical and horizontal. If these two modes are excited 90° out of phase with a monolithic hybrid, the square microstrip element will radiate vertical and horizontal polarization 90° out of phase. One input to the 90° hybrid power divider will result in right-hand circular polarization, while the other port of the 90° hybrid will have left-hand circular polarization. If the right-hand circular input is driven and the left-hand circular port is terminated in a 50- Ω load, the input VSWR will remain low for a bandwidth that extends beyond the bandwidth of the element. The reflected power is absorbed by the load. A spinning linear pattern of a circular polarized element is shown in Fig. 7-20. Note that the axial ratio remains low out to wide angles.

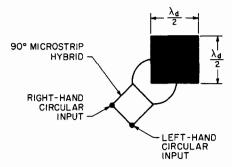


FIG. 7-19 Circularly polarized square microstrip element with 90° hybrid feed.

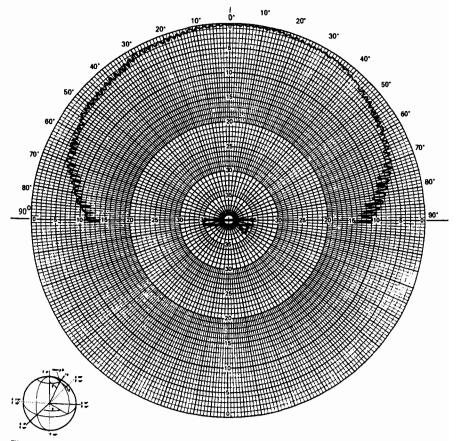


FIG. 7-20 Spinning dipole radiation pattern of a square microstrip element fed with a hybrid.

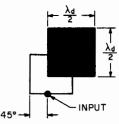


FIG. 7-21 Circularly polarized microstrip element with 45° offset feed.

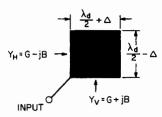


FIG. 7-22 Circularly polarized microstrip element with conjugate impedance matching and a single feed.

Another method for exciting circular polarization is shown in Fig. 7-21. This square element is fed in two orthogonal modes (vertical and horizontal) with a microstrip line. The phase of excitation of the microstrip-element modes is offset by 90° by offsetting the microstrip feed by 45°; i.e., a 90° lag is induced in the feed network. This design has a narrow circularly polarized bandwidth, and the VSWR bandwidth is about twice as wide as the element bandwidth.

A third method for exciting circular polarization is the microstrip element shown in Fig. 7-22. This element is adjusted slightly off resonance by $+\Delta$ in the vertical plane

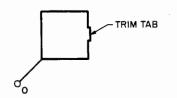


FIG. 7-23 Circularly polarized microstrip element with trim tab added.

and $-\Delta$ in the horizontal plane. If the vertical dimension is 1 percent longer than $\lambda_d/2$, the horizontal dimension is adjusted to be 1 percent shorter than $\lambda_d/2$. This results in an increase in mode susceptance. The admittance in the vertical and horizontal planes respectively is given by

$$Y_V = G + jB$$
 and $Y_H = G - jB$

When B = G, the feed applies a uniform voltage to conjugate impedances. The two resulting modes of radiation are excited with equal power and are 90° out of phase. Exact dimensions for a design are determined empirically by trimming a square element or an element as shown in Fig. 7-23. The tab is added for ease of trimming to achieve circular polarization.

Dual-Frequency, Dual-Polarization Microstrip-Antenna Element

Dual-frequency microstrip elements may be stacked microstrip elements fed in series as shown in Fig. 7-24a. The most important feature to note in Fig. 7-24a, b, and c is that off resonance the microstrip element looks like a short circuit. This allows the resonant microstrip element to work independently of the nonresonant element since the nonresonant element's impedance adds in series with the resonant element as a short circuit (see Fig. 7-25). Microstrip elements cannot be stacked as dual-frequency elements if their resonant frequencies are separated by less than 10 percent (except for very-high-Q elements) or if their resonant frequencies are harmonically related.

Multiple elements can be stacked and fed in series to get a 3, 4, or N multiresonant microstrip array. It is important that each element be centered so that it is

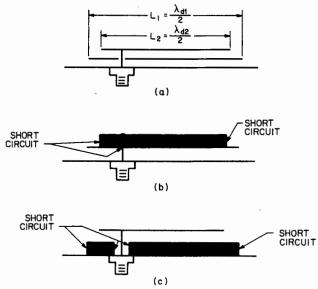


FIG. 7-24 Dual-frequency microstrip element (side view). (a) Fed in series. (b) Impedance model at f_1 . (c) Impedance model at f_2 .

fed at its 50-Ω-input point. Quarter-wavelength elements as well as full-wavelength elements can also be fed in series.

The exact dimension of a series-fed element and its feed-point location must be defined experimentally by an iterative process. This process usually consists of building an element to the dimensions defined by the design equations given for a rectangular microstrip element. The resonant

frequency and impedance are measured; usually they differ slightly from prediction because of a variety of effects:

- 1 Mutual coupling
- 2 Feed-probe inductance
- 3 Slight effect owing to short-circuit approximation for impedance of nonresonant element
- 4 Dielectric-constant variation

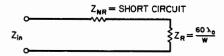


FIG. 7-25 Equivalent circuit of a stacked dual-frequency rectangular microstrip element. $Z_{NR} = \text{impedance of nonresonant rectangular microstrip element. } Z_R = \text{impedance of resonant rectangular microstrip element.}$

A linear adjustment of microstrip-element size and feed-point location is made to correct the resonant frequency and feed impedance. Multiple iterations may be required, but usually only one or two are necessary.

Dual-frequency circularly polarized microstrip elements can be built by feeding stacked circularly polarized microstrip elements along the diagonal of each element as shown in Fig. 7-26.

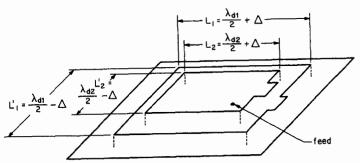


FIG. 7-26 Dual-frequency circularly polarized microstrip element.

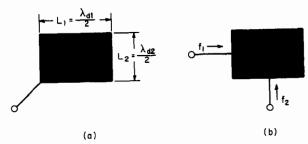


FIG. 7-27 Rectangular dual-polarization microstrip element. (a) Horizontal at f_1 , vertical at f_2 (same input). (b) Horizontal at f_1 , vertical at f_2 (separate feeds).

Dual-polarized microstrip elements are rectangular microstrip elements in which the two dimensions are picked as resonant dimensions. As shown in Fig. 7-27a, the two dimensions are picked so that L_1 equals a half wavelength in the dielectric at the

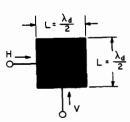


FIG. 7-28 Dual-polarized square microstrip element.

first resonant frequency and L_2 equals a half wavelength in the dielectric at the second resonant frequency. The element can also be fed with two independent feeds at the midpoint of each side as shown in Fig. 7-27 b. In both cases, f_1 will radiate horizontal polarization and f_2 will radiate vertical polarization.

A square microstrip element can be excited in two orthogonal modes as shown in Fig. 7-28. It is important that the two feeds be located at the midpoint of the

edge of the element, for this is the low-impedance point for the orthogonal mode in each case. Coupling of 25 dB between ports is typical for square elements fed in this manner.

7-3 MICROSTRIP-ARRAY DESIGN PRINCIPLES

Section 7-2 dealt with microstrip elements, which can be used individually or in microstrip arrays. A microstrip array is the integration of microstrip elements with a microstrip feed network consisting of power dividers, transmission lines, phase lines, and active components, etc. The active components are devices such as phase shifters, amplifiers, oscillators, receivers, mixers, etc. It is important to note that microstrip feed lines are connected directly to a microstrip radiating element, affecting neither the radiation pattern nor the impedance of the radiator. The feed line, being near the ground plane, is perpendicular to the electric field emanating from the microstrip radiator. Therefore, the feed line is a septum of equipotential, and radiating fields cannot excite currents in the feed lines.

The real advantages of microstrip antennas appear when all the elements of the array along with feed network are monolithically etched from one side of a printed-circuit board. At least four distinct advantages can be identified:

- 1 The process of photoetching hundreds or even thousands of microwave components in one process results in a low-cost antenna array.
- 2 The resulting printed-circuit board is very thin. Since the array is designed to operate from the ground plane on the back of the printed board, its performance is unaffected by mounting to a metallic surface such as an aircraft or a missile. The resulting design is doubly conformal. It is conformal to the underlying structure to which it can be bolted or laminated, and it is externally conformal aerodynamically because of minimum protrusion.
- 3 Microstrip arrays have high performance because an infinite variety and quantity of antenna elements, power dividers, matching sections, phasing sections, etc., can be added to the printed-circuit board without any cost impact (except the cost per square foot of the board). This gives the design engineer many components (for instance, 110-Ω quarter-wave transformers or unequal power dividers) that are not commercially available in separate packages.
- 4 The microstrip array is very reliable since the entire array is one continuous piece of copper. Other types of antennas most commonly have failed at interconnections within the antennas and at their input connectors.⁶

Omnidirectional Microstrip Arrays

Microstrip arrays were first used as omnidirectional arrays on missiles.³ Two types of antennas are used:

- A continuous radiator for linear axial polarization (Fig. 7-29).
- An array of discrete radiators for omnidirectional circular polarization (Fig. 7-30).
 (Eight of the circularly polarized arrays in Fig. 7-30 fit end to end and are fed in phase to provide a large circularly polarized omnidirectional array.)

The antenna shown in Fig. 7-29 was designed to give omnidirectional linear (axial) polarization coverage. The printed antenna is shown wrapped around the 8-in (203-

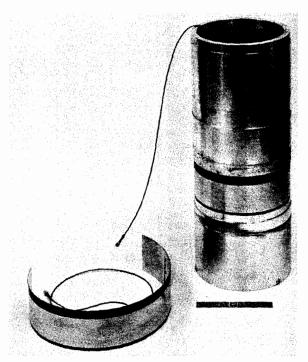


FIG. 7-29 Continuous-radiator microstrip antenna for linear polarization.

mm) cylinder. Note that a 1/2-in- (0.794-mm-) deep lathe cut has been made in the 8-in cylinder so that the antenna presents a flush surface when wrapped around and attached to the cylinder.

The design procedure for the 8-in wraparound operating at 2270 MHz (Fig. 7-31) is calculated as follows:

- 1 The resonant length of the radiator is $L = \lambda_0/2\sqrt{\epsilon_r} = 5.2/(2\sqrt{2.45}) = 1.66$ in (42.16 mm).
- 2 The width of the radiator is $W = \pi D = \pi 8 = 25.1$ in (637.54 mm).
- 3 The number of feeds required N_F is at least 1 per wavelength in the dielectric, and a binary number 2, 4, 8, 16 ... is used to accommodate a corporate-feed network. The width of the element in terms of wavelengths in the dielectric is given by

$$W_{\lambda d} = W/\lambda_0/\sqrt{\epsilon_r} = 7.5$$

Since the width in wavelengths does not exceed 8, the number of feeds required N_F is 8 (at least 1 feed per λ_d).

4 The input impedance R_{in} of the antenna at each feed point is the total impedance of the radiator times the number of feeds:

$$R_{\rm in} = N_F \cdot 60 \cdot \lambda_0 / W = 99 \,\Omega$$

5 The feed network is used to match the antenna while dividing the power. A quarter transformer is used next to the element to match the antenna impedance R_{in} to 100 Ω :

$$Z_0$$
 quarter-wave transformer = $\sqrt{R_{in} \cdot 100}$ = 99.5 Ω

At the first junction a the two 100- Ω impedances combine to give 50 Ω . A quarter-wavelength ($Z_0 = 70 \Omega$) transformer is used to transform the 50- Ω impedance to

100 Ω . This impedance is transferred down a 100- Ω line to junction b, where the process at junction a is repeated. At junction c the two 100- Ω impedances combine to provide a 50- Ω input for a coaxial input attached to the back of the printed-circuit board.

Microstrip-Antenna Pattern Coverage for Omniapplications The pattern coverage for the omniantenna shown in Figs. 7-29 and 7-31 depends on the diameter of the missile. The limiting factor in omnidirectional pattern coverage is a singular hole at the tip and tail of the missile (Fig. 7-32) which gets narrower as the diameter of the missile increases. For instance, a 15-in-diameter antenna produces a null along the missile axis of radius 1° at the -8-dB-gain level. The fractional area with gain below -8 dB is 0.0002. Conversely, the fraction of the area with gain above -8 dB is 0.9998, or 99.98 percent. The percent coverage increases without limit for larger diameters until a nearly perfect coverage is attained for a single linear polarization. The percent coverage is only a function of

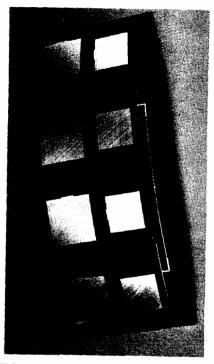


FIG. 7-30 One-eighth of a circularly polarized omnidirectional array.

diameter and wavelength and is independent of antenna thickness. The theoretical and experimental pattern coverages, at S band, for microstrip antennas on a smooth cylinder are given in Fig. 7-33 for gain levels greater than -8 dB.

The roll-pattern variation for a circularly polarized wraparound microstrip antenna is a function of center-to-center element separation as shown in Fig. 7-34. For a uniform roll-plane pattern, the separation between elements should not exceed $0.7\lambda_0$. For separations approaching $0.35\lambda_0$ the mutual coupling between elements makes it difficult to obtain circular polarization with a tolerable axial ratio. The input impedance of an element is measured, and a corporate-feed network is designed, by using the procedure discussed earlier.

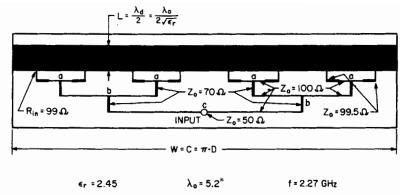


FIG. 7-31 Printed-circuit-board design for an 8-in- (203-mm-) diameter cylinder.

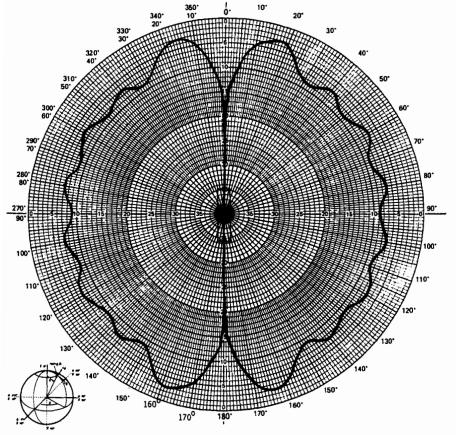


FIG. 7-32 Measured E-plane pattern of the 8-in (203-mm) wraparound microstrip antenna shown in Fig. 7-29. The antenna pattern is a figure of revolution about the missile axis.

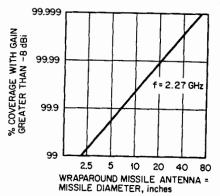


FIG. 7-33 Coverage versus diameter for an omnidirectional microstrip array.

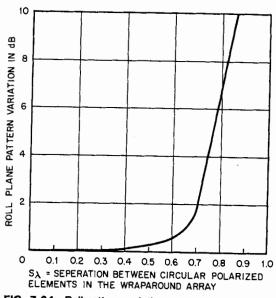
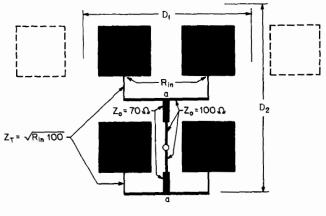


FIG. 7-34 Roll-pattern variation versus element spacing. (Courtesy of Cliff Garvin, Ball Aerospace Systems Division.)

Fixed-Beam Microstrip Arrays

High-gain directional fixed-beam antennas can be photoetched from one side of a printed-circuit board (Fig. 7-35). Most arrays of this type have a single beam perpendicular to the plane of the array. The microstrip elements are spaced slightly less than a free-space wavelength to prevent grating lobes. Spacings of less than a half free-space wavelength are generally not used because of feed-line crowding.

The example shown in Fig. 7-35 consists of four rectangular microstrip elements



INPUT IMPEDANCE = 50 Q

FIG. 7-35 Directional fixed-beam microstrip antenna.

in a two-by-two array. Each element is matched with a quarter-wavelength transformer to match its input impedance $R_{\rm in}$ to $100~\Omega$. Each pair of $100~\Omega$ inputs is combined to give $50~\Omega$ at point a. The $50~\Omega$ impedance is transformed to $100~\Omega$ by a $70~\Omega$ quarter-wavelength transformer. The two $100~\Omega$ -impedance transmission lines maintain the $100~\Omega$ impedance until they are combined in parallel to provide $50~\Omega$ at the input.

A fixed-beam microstrip array can be expanded to any 2ⁿ-by-2^m array. The corporate-feed network is expanded to provide equal power and phase split; the symmetrical line length from the input to the microstrip elements forces all the elements to be fed in phase. Variations of frequency or dielectric constant do not cause a differential phase taper over the array when a corporate-feed network is used.

The maximum gain of a fixed-beam microstrip phased array is given by

$$G_{\text{dB}} = 10 \log \left(\frac{4\pi A}{\lambda_0^2} \right) - \alpha \cdot (D_1 + D_2)/2$$

where $A = D_1 \cdot D_2$

 D_1 = effective width of the uniformly spaced array [It is defined as the sum of the distance between the centers of the edge elements plus one interelement spacing; $(n + 1) \times \text{horizontal spacing.}$]

 D_2 = height of array defined in the same manner as D_1 [$(m + 1) \times \text{vertical spacing}$].

 α = attenuation, dB per unit length, of a 50- Ω transmission line being used in the monolithic feed [A typical value of α is 0.4 dB/ft for a 50- Ω microstrip line on %-in (0.794-mm) Teflon fiberglass at 2.2 GHz.]

Unequal line lengths can be used to produce phase tapers which yield fixed beams that are scanned away from broadside. Phase tapers are also used to compensate for curvature of microstrip arrays that conform to the cylindrical surface of aircraft or missiles.

Microstrip Phased Arrays

A C-band microstrip phased array is shown in Fig. 7-36. This array is similar to the fixed-beam microstrip arrays discussed above except that a phase shifter has been added to the input of each microstrip element. The microstrip phase shifters, microstrip radio-frequency chokes, and direct-current bias lines are all photoetched on the same piece of copper as the radiators and the corporate-feed network.

Quarter-wavelength microstrip elements are used as radiators for two reasons. First, they require less area than the other types of microstrip radiating elements. Second, they have a uniform radiation pattern in the E plane and therefore do not contribute to loss of gain as a function of scan angle because of the element factor roll-off.

The array shown in Fig. 7-36 has a 3-bit phase shifter at the corporate-feed input to each element. Each 3-bit phase shifter consists of a 90° and an 180° switched-line phase shifter and a 45° loaded-line phase shifter. The phase shifters (Fig. 7-37) are pin-diode phase shifters. Forward bias short-circuits the upper two diodes and causes the signal to travel down the upper-path length $L+\phi$, and reverse bias short-circuits the lower two diodes and causes the signal to travel the shorter path L. The differential length is ϕ the desired phase shift. The 45° loaded-line phase shifter (Fig. 7-37b) is

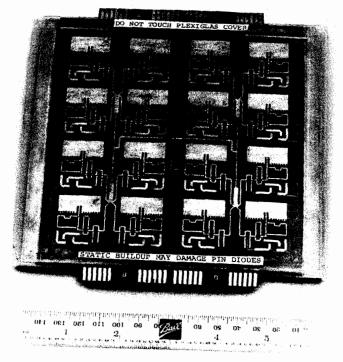


FIG. 7-36 Monolithic 5-GHz phased array. (Courtesy of Frank Cipolla, Ball Aerospace Systems Division.)

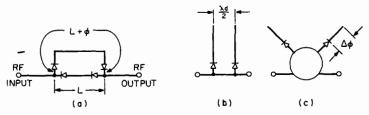


FIG. 7-37 Microstrip phased-array phase shifters. (a) Switched-line phase shifter. (b) Loaded-line phase shifter. (c) 90° hybrid phase shifter.

used for 45° or less induced phase shifts. These phase shifters are used because of their compact size and the fact that only two diodes are required. Each inductive stub produces half of the total loaded-line phase shift. The quarter-wavelength spacing between the stubs minimizes the reflection coefficient, and an impedance match is maintained. For more information on switched-line and loaded-line phase shifters, a more extensive reference on phase-shifter design should be consulted before attempting a design. 7.8 The 90° hybrid phase shifter (Fig. 7-37c) is not useful in monolithic microstrip phased arrays because of its large size.

The gain of a microstrip phased array of the type shown in Fig. 7-36 is given by

$$G = 10 \log \left(\frac{4\pi A}{\lambda_0^2}\right) - \frac{\alpha}{2} (D_1 + D_2) - 1 \text{ dB} - 10 \log (\cos \theta_E \cdot \cos^2 \phi_H)$$
aperture gain feed-line 3-bit phase-shifter loss

where D_1 , D_2 , α , and A = dimensions as defined in preceding subsection

 θ_E = scan angle in the E plane

 ϕ_H = scan angle in the H plane

Although the array shown in Fig. 7-36 had measured gain⁹ that agreed with the preceding formula, larger arrays should consider additional mutual-coupling VSWR losses.

Series-Fed Microstrip Arrays

Two types of series-fed microstrip arrays are feasible: the resonant, or broadside, series-fed microstrip array and the nonresonant, or traveling-wave, series-fed microstrip phased array.

A resonant series-fed microstrip array is shown in Fig. 7-38 a. The array is fed at its input with a 90° offset near the center so that radiation of both halves of the array will be in phase. The elements of the array are separated by a wavelength in the effective dielectric of the transmission line; the line consists of the radiating elements and the series-connected microstrip lines. For Teflon-fiberglass boards, the effective wavelength will be approximately $\lambda_0/\sqrt{\epsilon_r}$ in the elements and $1.2\lambda_0/\sqrt{\epsilon_r}$ in the microstrip transmission line. This will result in an effective separation S_{λ} of $\lambda_d \approx 1.1\lambda_0/\sqrt{\epsilon_r}$. Exact values are usually measured experimentally by constructing a test array and varying the frequency until the beam is centered at broadside. The conductance of each element is a function of its width. For a perfectly lossless feed, the power

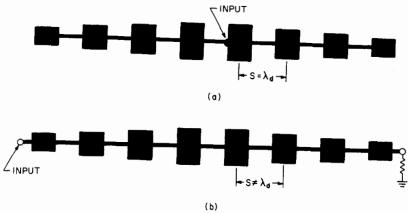


FIG. 7-38 Series-fed microstrip phased array. (a) Resonant series-fed microstrip array. (b) Traveling-wave series-fed microstrip array.

radiated by each element will be its conductance divided by the total sum of the conductance of all elements.

The sidelobe level and the beamwidth at resonance can be used to deduce the amplitude taper existing over the array. Near-field probe techniques can also be used to measure the amplitude taper. At resonance, the array has a beam at broadside with sidelobes of -20 to -30 dB. Off resonance, the main beam splits into two identical beams that scan away from broadside as a function of frequency.

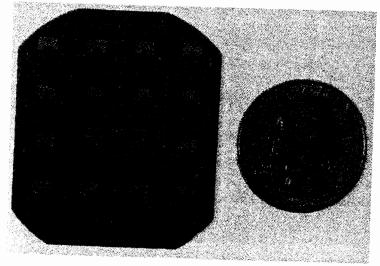


FIG. 7-39 A 17.5-GHz, 16-microstrip-element monolithic array.

A traveling-wave series-fed microstrip array is shown in Fig. 7-38b. The array is fed at one end, and varying widths of elements are used to control the radiation. The radiation from each element is proportional to the width of the element. The elements are separated by a dimension not equal to the effective dielectric constant of the traveling-wave array. For a separation S_{λ} less than an effective wavelength, the beam will be scanned backfire (toward the feed from broadside). For a separation greater than a wavelength, the array will produce an end-fire beam (scanning away from broadside as the frequency is increased). A grating lobe will appear for the end-fire beam.

Traveling-wave arrays have very good input impedance since the reflection coefficient due to each element cancels in the reverse direction. The dimensions of a series-

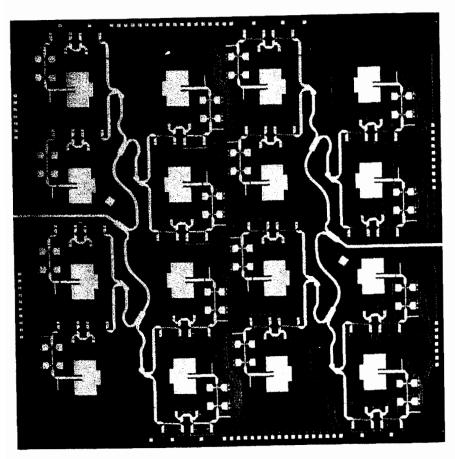


FIG. 7-40 A 44-GHz active (distributed power amplifiers) 16-microstrip-element phased array.

fed array are predicted by the following authors: Derneryd, ¹⁰ Metzler, ^{11,15} Bahl, ¹² Campi, ¹³ Huebner, ¹⁴ and Sanford. ¹⁶

Monolithic Phased Arrays

At millimeter frequencies, it is possible to combine multiple radiators, phase shifters, power dividers, driver circuitry, and amplifiers on one side of a gallium arsenide or silicon chip. The semiconductor junction (phase shifter and amplifiers) is first formed on the top surface of the chip. Next, the metal circuitry required for radiators, phase shifters, amplifiers, power dividers, and driver circuitry is deposited on the chip. This architecture results in a significant cost and thickness reduction. Working models of two monolithic phased arrays are shown in Figs. 7-39 and 7-40.

In Fig. 7-39, each microstrip radiator has a 3-bit (45°, 90°, and 180°) phase shifter between the 16-way power divider and the radiator. The phase shifters used pin diodes formed on a high-resistivity silcon substrate. In Fig. 7-40, each element has a 3-bit phase shifter and a two-stage power amplifier between the two 8-way power dividers and the microstrip radiators. The phase shifters and power amplifiers are fabricated monolithically using GaAs MESFET devices. The metal circuitry is added to the GaAs chip after the semiconductor junctions have been fabricated.

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Slot Antennas

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- 8-1 Introduction 8-2
- 8-2 Slotted-Waveguide Antennas 8-2
- 8-3 Tapered and Flared Slot Antennas 8-4
- 8-4 Cavity-Backed Rectangular Slot Antennas 8-7
- 8-5 Waveguide-Fed Slot Antennas 8-9
- 8-6 Slot Antennas on Finite and Curved Ground Planes 8-14
- 8-7 Slot Antennas on Cylinders, Cones, and Spheres 8-16

This chapter deals with the radiation characteristics of slot antennas and includes the effects of finite and curved surfaces, dielectric coatings, cavity backing, and single slots fed by waveguides. The simplest example of such an antenna consists of a rectangular slot cut in an extended thin flat sheet of metal with the slot free to radiate on both sides of this sheet, as shown in Fig. 8-1. The slot is excited by a voltage source such as a balanced parallel transmission line connected to the opposite edges of the slot or a coaxial transmission line.

The electric field distribution in the slot can be obtained from the relationship between the slot antennas and complementary wire antennas, as established by Booker. It has been shown that the electric field distribution (magnetic current) in the slot is identical

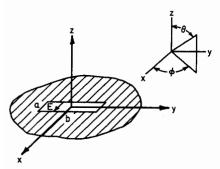


FIG. 8-1 Rectangular slot.

with the electric current distribution on the complementary wire. In the illustrated rectangular slot, the electric field is perpendicular to the long dimension, and its amplitude vanishes at the ends of the slot.

The electric field is everywhere normal to the surface of the slot antenna except in the region of the slot itself. The theoretical analysis of this configuration shows that the radiation of the currents in the sheet can be deduced directly from the distribution of the electric field in the slot. Consequently, the radiated field of an elementary magnetic moment within

the slot boundaries should include the contributions of the electric current flowing on a metal surface.

A slot-antenna design will often require that the slot be cut in something other than an extended flat sheet surface. Whatever the surface is, the electric field will be everywhere normal to it except in the region of the slot. The field due to the electric currents on this metal surface can be deduced from the exciting magnetic currents² in the slot, just as in the case of the flat metal sheet. This field can be combined with the exciting field so that the result is the total field due to a magnetic current on the given boundary surface. Thus the field of a thin rectangular slot cut in a circular cylinder differs from that of a slot cut in a flat metal sheet because the distribution of electric currents is different for the two cases.

In general, the slot antenna is not free to radiate on both sides of the surface on which it is cut because one side is either completely enclosed, e.g., the slotted cylinder antenna, or it is desired that the radiation on one side be minimized. In these cases, the influence of the enclosed cavity region on the excitation and impedance of the slot antenna is significant to the antenna design.

8-2 SLOTTED-WAVEGUIDE ANTENNAS

Slotted-waveguide antennas have significant applications in the areas of missile, spacecraft, and airborne radar. Broad-wall slotted-waveguide antennas have been studied extensively. Oliner,³ following research by Stevenson,⁴ has derived equivalent circuit representations for this type of antenna. These circuits allow accurate computation of the normalized conductance, susceptance, resistance, reactance, and resonant frequency of broad-wall slots. The types of slots and the equivalent networks are given in Chap. 9. Accurate analysis for edge-wall slots is not available; therefore, their parameters must be determined experimentally.

Dielectric-covered broad-wall slots also have been characterized thoroughly. Bailey has summarized significant findings. The general problem discussed by Bailey extends Oliner's work to include the effects on broad-wall slots radiating into a multilayer dielectric medium (Fig. 8-2). The basic effect that occurs by adding a dielectric layer over slots in a waveguide is to produce a downward shift in resonant frequency. For dielectric layers whose thickness is greater than 0.2λ , where $\lambda = \lambda_0 \sqrt{\epsilon}$, the approximate resonant shift is given in Fig. 8-3, where λ is the wavelength in the dielectric, λ_0 is the wavelength in free

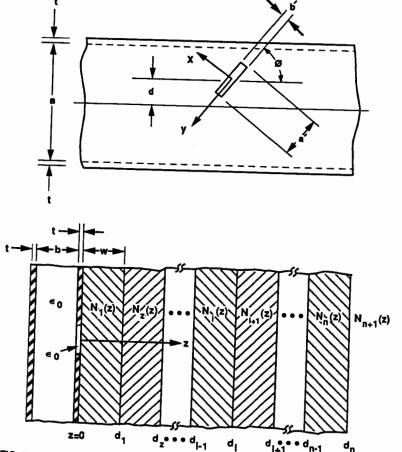


FIG. 8-2 Narrow slot in the broad face of a rectangular waveguide with multilayered inhomogeneous external medium. (After Bailey, Ref. 5.)

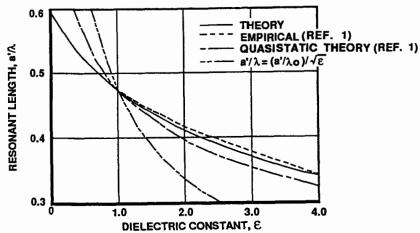


FIG. 8-3 Resonant length of a dielectric-covered shunt slot in WR-90 (RG 52/U) waveguide ($b^1 = 0.0625$ in, t = 0.050 in, a = 0.900 in, b = 0.400 in). (After Bailey, Ref. 5.)

space, and ϵ is the dielectric constant. Further analysis, and comparison with experimental data, is also available, as shown in Fig. 8-4.

The typical polarization of most slotted-waveguide antennas is linear. However, several slotted-waveguide elements have been designated that produce circular polarization. 7.8

8-3 TAPERED AND FLARED SLOT ANTENNAS

Tapered slot antennas (TSAs) were first introduced in the late 1950s. It was then that Eberle et al. produced a waveguide-fed flared slot antenna for use in aircraft skins where conventional antennas could not be easily integrated. Gibson then developed the stripline-fed exponentially tapered slot antenna, which he called the *Vivaldi aerial*. His design was the first recognized TSA that showed symmetric *E*- and *H*-plane beamwidths, low sidelobes, and moderate gain.

Since then, with the increased interest in MIC (microwave integrated circuit) antennas for applications ranging from satellite communications to remote sensing, tapered slot antennas have been studied extensively, both empirically and theoretically. In general, the performance one can expect to achieve from a typical TSA includes

- 1 Broadband operation
- 2 Moderate gain
- 3 Low sidelobes

These radiation characteristics make TSAs suitable elements for reflector feeds or as stand-alone antennas.

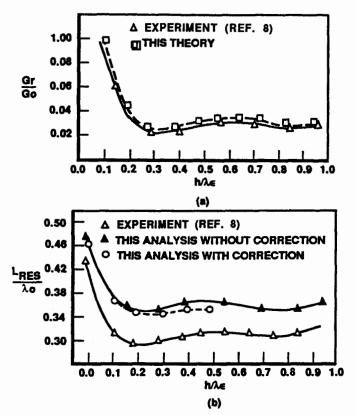
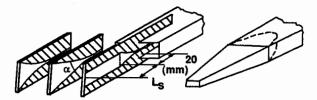


FIG. 8-4 Resonant conductance (a) and resonant length (b) versus layer thickness, e, = 3.31. (After Katehi, Ref. 6.)

The current form of a typical TSA is planar in nature, etched on a thin, low-dielectric-constant microwave substrate, and fed by a strip-line, fin-line, or slot-line configuration, as shown in Fig. 8-5. As a result of the typical substrates used in TSA designs, it is important to consider the possibility of the feedline itself radiating or coupling with the antenna element. Work at Harris Corporation has addressed this problem and resulted in a bilateral stripline feed as one solution (Fig. 8-6).

TSAs are a type of traveling-wave antenna. Their operation is based on a traveling wave propagating along the surface of the antenna taper with a phase velocity less than the speed of light. Under this condition, endfire radiation results. Zucker reviews properties of traveling-wave antennas in Chap. 12.

Yngvesson et al. 11,12 empirically investigated three groups of TSAs: the linear tapered slot antenna, the constant-width slot antenna, and the Vivaldi or exponentially tapered slot antenna. Their work included assessment of the effect of dielectric constant, effective dielectric thickness, and taper shape on beamwidth, sidelobe level, and pattern bandwidth. They compared their results with Zucker's predictions for standard traveling-wave antennas and found that for certain conditions (i.e., thin substrates with low dielectric



VIVALDI LTSA CWSA

DIELECTRIC ROD ANTENNA

FIG. 8-5 Three different types of endfire tapered slot antennas along with a dielectric-rod antenna shown for comparison. (After Yngvesson et al., Ref. 11.)

constants), TSAs were well-behaved traveling-wave antennas. They determined that in order to remain as well-behaved TWAs, the effective dielectric thickness t_{eff} , given by

$$t_{\rm eff}/\lambda_0 = (\sqrt{\epsilon_r} - 1)(t/\lambda_0)$$

was the most important design parameter and should be on the order of 0.005 to 0.03 wavelengths for 4 to $10\lambda_0$ antennas. Antennas outside of these dimensions quickly diverge from traveling-wave antenna characteristics. From this work, Yngvesson et al. arrived at an empirical set of rules for designing these type of antennas (Table 8-1).

In 1987, Janaswamy and Schaubert¹³ took TSAs one step further by introducing a theoretical model for predicting radiation characteristics of smooth-tapered TSAs. Their analysis predicts what previously was only obtainable through empirical studies of TSA

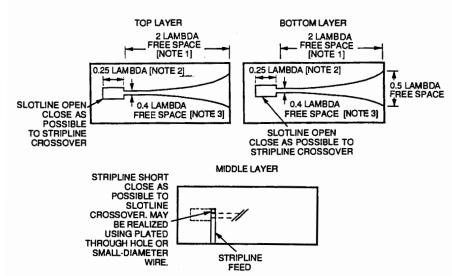


FIG. 8-6 Stripline designs of the bilateral slotline-fed antenna. Note 1: Length of taper is proportional to gain; maximum gain approximately 10 dB. Note 2: Quarter wave calculated using dielectric constant of material. Note 3: May be narrower than 0.4 to obtain desired slotline impedance. Taper rate: $y = a[\exp(kx)]$, where a = 0.5 slotline width, k = constant, x = length of flair.

TABLE 8-1 Typical Properties of Endfire Traveling-Wave Antennas¹¹

Optimum (max. gain)	Low sidelobes/ broad bandwidth
$10 \log \left(10 \frac{L}{\lambda}\right)$	$10 \log \left(4 \frac{L}{1}\right)$
$55/\sqrt{L/\lambda_0}$	$77/\sqrt{L/\lambda_0}$
$c/v_{\rm ph} = 1 + \frac{1}{2L/\lambda_0}$	
	(max. gain) $10 \log \left(10 \frac{L}{\lambda_0}\right)$ $55/\sqrt{L/\lambda_0}$ $c/v = 1 + \frac{1}{\lambda_0}$

Note: L = physical length of antenna.

performance. The theory is developed by first determining the aperture distribution of the tapered slot through a stepped approximation of the taper. This is accomplished by dividing the antenna into numerous sections of uniform width and determining the aperture distribution of each individual section by solving an eigenvalue problem for each section. Then the individual section boundary discontinuities are determined at each section junction. Necessary slot parameters are obtained through the Galerkin method in the spectral domain. Finally, radiated far fields are determined using half-plane Green's functions. Doing this, they arrive at the following expressions for field patterns in the E and E planes:

$$E_{\theta}^{i}(\theta) = \tilde{E}_{a}^{i}(k_{0}W^{i}\cos\theta)\sqrt{\frac{2}{\sin\theta}}\left\{e^{-jk_{0}c^{i}L}\left[\frac{F^{*}(u_{h}^{i}) - F^{*}(u_{l}^{i})}{\sqrt{c^{i} - \sin\theta}}\right] + \Gamma e^{jk_{0}c^{i}L}\left[\frac{F(\bar{u}_{h}^{i}) - F(\bar{u}_{l}^{i})}{\sqrt{c^{i} + \sin\theta}}\right]\right\}$$

$$E_{\theta}^{i}(\phi) = \tilde{E}_{a}^{i}(0)\left(\frac{e^{-jk_{0}c^{i}L}}{c^{i} + \cos\phi}\left\{\sin\phi[F(p_{h}^{i})e^{jr_{h}} - F(p_{l}^{i})e^{jr_{l}}]\right] + \sin\frac{\phi}{2}\sqrt{2(c^{i} - 1)}\left[F^{*}(q_{h}^{i}) - F^{*}(q_{l}^{i})\right]\right\}\right)$$

$$-\Gamma\tilde{E}_{a}^{i}(0)\left(\frac{e^{jk_{0}c^{i}L}}{c^{i} - \cos\phi}\left\{\sin\phi[F(p_{h}^{i})e^{-jr_{h}} - F(p_{l}^{i})e^{-jr_{l}}]\right] - \sin\frac{\phi}{2}\sqrt{2(c^{i} + 1)}\left[F(\bar{q}_{h}^{i}) - F(\bar{q}_{l}^{i})\right]\right\}\right)$$
(8-1)

Definitions of the terms in Eqs. (8-1) and (8-2) are given in Ref. 13.

8-4 CAVITY-BACKED RECTANGULAR SLOT ANTENNAS

The electric field on the coaxially fed, cavity-backed rectangular slot (Fig. 8-7a) is neither sinusoidal nor complementary to a ribbon dipole antenna. This antenna is a cavity resonator, energized by the coaxial transducer, which radiates from the slot aperture. The field distribution in the slot, therefore, is dependent on the excitation of higher cavity

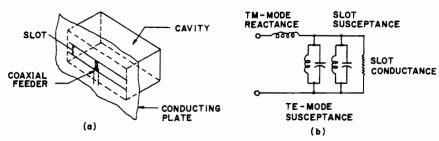


FIG. 8-7 Cavity-backed rectangular slot. (a) Pictorial representation. (b) Equivalent circuit.

modes as well as the principal mode (TE₁₀). The equivalent circuit of a cavity-backed slot antenna is shown in Fig. 8-7b; the shunt conductance is the radiation conductance of the slot. The conductance of the cavity-backed resonant half-wave slot is half the open slot, free to radiate on both sides. That is, the shunt resistance is at least 800 rather than 400 Ω . ¹⁴⁻¹⁶ The parallel susceptance shown in the equivalent circuit is the sum of the shunt susceptance of the slot radiator and the TE-mode susceptances of the cavity. The series-resonant circuit is the result of the energy stored in the TM modes in the cavity and feed structure.

To obtain the maximum radiation conductance, a sinusoidal distribution of electric field (magnetic current) must be generated. This distribution will be achieved when the energy stored in the cavity in the vicinity of the slot is primarily in the TE_{10} mode, i.e., by making the cavity dimensions big enough so that the dominant mode is above cutoff. For small cavities, edge loading as in a highly capacitive slot will improve the field distribution.

An important design parameter is the antenna Q, which is minimum when the stored energy is only in the dominant mode. The Q limits the inverse voltage-standing-wave-ratio (VSWR) bandwidth product; for a small cavity, it is:

$$Q>\frac{3}{4\pi^2}\left(\frac{1}{V}\right) \tag{8-3}$$

where V is the volume of the cavity expressed in cubic free-space wavelengths. This minimum Q is realized when the series reactance is eliminated through efficient feed and cavity design. For the simple capacitive slot-loaded cavity shown in Fig. 8-7a, higher TE and TM modes will be generated with attendant high Q.

A broadband cavity-backed antenna can be realized by using a T-bar feed¹⁷ as shown in Fig. 8-8. A flat T bar instead of the illustrated circular cross section will generate the same impedance if its width is equal to the diameter D.

The nominal input impedance to the T bar is 125Ω (approximate). To achieve the available bandwidth, a broadband impedance transformer is needed between the $50-\Omega$ coaxial transmission line and the T-bar junction.

The dimensions for a broadband flat T bar covering the frequency range 0.5 to 1.2 GHz are shown in the diagram of Fig. 8-8. The VSWR does not exceed 3:1 in the frequency band and is less than 2:1 over 90 percent of the band.

The resonant frequency can be lowered by the use of dielectric or ferrite loading in the cavity.¹⁸ The reduction in cavity volume and aperture size results in increased Q, smaller bandwidth, and lower efficiency.

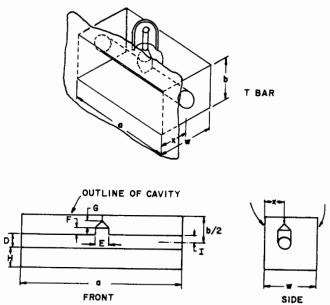


FIG. 8-8 Cavity-backed T-bar-fed slot anterina. Typical dimensions in inches (millimeters) for a frequency range of 0.5 to 1.2 GHz: *a*, 12.00 (304.8); *b*, 4.00 (101.6); *x*, 3.25 (82.55); *w*, 6.75 (171.45); *D*, 2.25 (57.15); *E*, 0.75 (19.05); *F*, 0.63 (16.00); *G*, 0.19 (5.826); *H*, 0.25 (6.35).

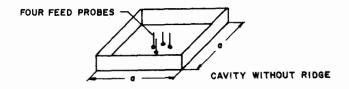
A shallow ridged-cavity crossed-slot antenna¹⁹ has been developed for wide-angle coverage in the ultrahigh-frequency range. The VSWR is dependent on the slot width, slot length, and cavity depth at the low end of the band. The ridge parameters tune the antenna in the midband and high-band frequencies. The VSWR is less than 2.7:1 from 240 to 279 MHz and under 2.1:1 from 290 to 400 MHz for cavity dimensions of 33 by 33 by 4 in.

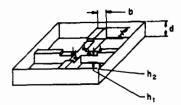
An experimental square cavity-slot antenna (half scale) with crossed slots cut along the diagonal dimensions of the cavity is shown in Fig. 8-9. The cavity configuration, ridges, and crossed-slot arrangement are illustrated. The slots are excited by four symmetrically located feed probes near the center of the cavity. Each opposite pair is connected to a wideband 180° hybrid. For circular polarization, the input ports of the two 180° hybrids are connected to a wideband 90° hybrid. The 3-dB beamwidth varies from 120° at the low end of the band to about 40° at the high end.

An earlier narrowband cross-slot antenna was developed with a cavity depth of 2 in. ²⁰ A stripline version of the cavity-backed slot antenna has been designed. ²¹ This design was used for many years as a low-profile antenna for rocket payloads.

8-5 WAVEGUIDE-FED SLOT ANTENNAS

The waveguide opening onto a ground plane is commonly used in phased arrays and as a single element on curved as well as flat ground planes. An early analysis and experiment²² has been used extensively for checking various analytical methods. This early work has





CAVITY WITH RIDGE

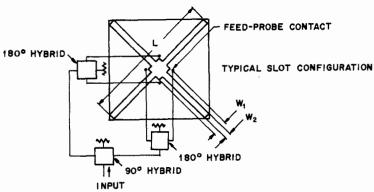


FIG. 8-9 Cavity-slot configuration with circular polarization of a ridged-cavity crossed-slot antenna. Typical dimensions in inches (millimeters) for a frequency range of 480 to 800 MHz: a, 16.00 (406.4); d, 2.00 (50.8); b, 1.25 (31.75); W_1 , 2.50 (73.5); W_2 , 0.65 (16.51); h_1 , 1.50 (38.1); h_2 , 1.75 (44.45); L, 22 (558.8).

been extended to include a dielectric medium outside the slot, ²³ as shown in Fig. 8-10. Also given in Fig. 8-10 are calculations and measurements that agree with those in Ref. 22. It is noted in Ref. 23 that substantial energy is coupled into the dielectric slab in the form of surface waves. Another extension of this work includes dielectric plugs flush mounted to the ground plane just inside the waveguide. ²⁴ Dielectric plugs are very useful, but one must be careful of certain dielectric constants and plug thicknesses that can generate very significant higher-order aperture modes.

Similar analysis has been performed for circular waveguides.²⁵ The basic admittance of a typical TE₁₁-mode excited slot is given in Fig. 8-11. This TE₁₁ excitation mode tends to couple less energy into the dielectric slab in the form of surface-wave modes. Hence the circular waveguide antenna was used in many early rocket reentry payload designs employing dielectric ablation materials.

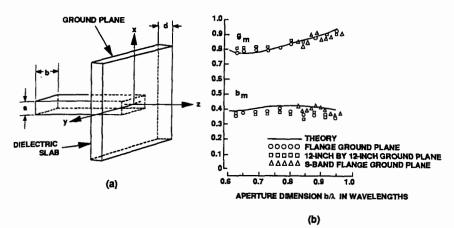


FIG. 8-10 (a) Rectangular waveguide in a ground plane covered by a dielectric slab. (b) Effect of ground-plane size on the free-space admittance. (After Croswell et al., Ref. 23.)

The TEM mode coaxial line with fairly large dimensions is also a very useful waveguide-fed slot antenna. The radiation characteristics of any annular slot (cut in an infinite ground screen) are identical with those of a complementary wire loop with electric and magnetic fields interchanged. In the case of the small slot, the radiation diagram is close to that of a small electric stub in the ground screen.

Consider a thin annular slot as shown in Fig. 8-12. The polar axis of a spherical coordinate system being normal to the plane of the slot, the magnetic component of the radiated field is

$$H_{\phi} = \frac{aV e^{-jkr}}{120\pi\lambda r} \int_0^{2\pi} \cos\left(\phi - \phi'\right) e^{jka\sin\theta\cos\left(\phi - \phi'\right)} d\phi'$$
 (8-4)

where a = radius of slot

V = voltage across slot

 $k=2\pi/\lambda$

For small values of a, that is, $a < \lambda/2\pi$,

$$H_{\phi} = j \frac{V e^{-jkr}}{60r} \frac{A}{\lambda^2} \sin \theta \qquad \text{A/m}$$
 (8-5)

where $A = \pi a^2$ is the included area of the annular slot. Equation (8-5) is valid for small slots of arbitrary shape.

The integral in Eq. (8-4) can be evaluated exactly as

$$H_{\phi} = j \frac{aV e^{-jkr}}{60r} J_1(ka \sin \theta)$$
 (8-6)

where J_1 is the Bessel function of the first kind and the first order.

The radiation characteristics on a large but finite ground screen are closely approximated by Eqs. (8-5) and (8-6). There are slight perturbations because of edge effects that result in energy radiated into the shadow region plus modulation of the main radiation pattern.

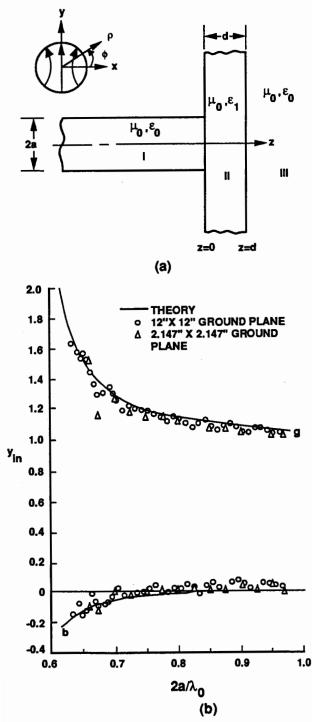


FIG. 8-11 (a) Circular waveguide opening onto a dielectric-coated ground plane. (b) Input admittance of a circular waveguide radiating

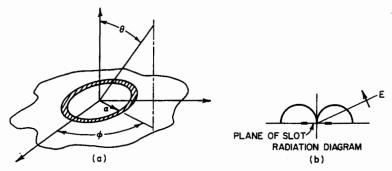


FIG. 8-12 Annular slot. (a) Coordinate system. (b) Vertical-plane pattern for a small-diameter slot.

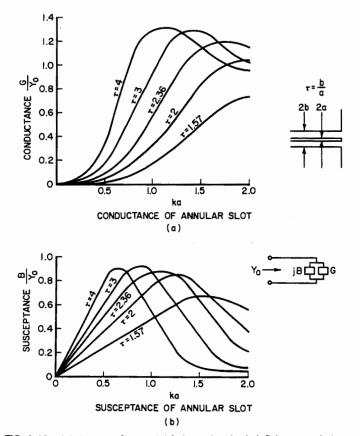


FIG. 8-13 Admittance of a coaxial-fed annular slot in infinite ground plane.

The optimum excitation of an annular slot, i.e., least stored energy and lowest Q, results when the magnetic current distribution is uniform around the slot. One method for obtaining this result is to feed the annular slot by a coaxial transmission-line structure which has the same inner and outer diameters as the annular structure. Figure 8-13 consists of graphs of the conductance and susceptance in the plane of the aperture relative to the characteristic admittance of the feed line as a function of the radian length ka of the inner radius a. It is seen that the slot is at all times nonresonant and has a capacitive susceptance.

8-6 SLOT ANTENNAS ON FINITE AND CURVED GROUND PLANES

The annular slot is commonly used on aircraft as a UHF antenna because it produces a pattern similar to a short vertical dipole. Early research on annular slot antennas for the space shuttle has been conducted and reported. This analysis is an extension of the moment method to semi-infinite strips in an integral equation formulation. It was determined that for many cross sections through the body shape, the ϕ plane pattern was similar for either a two- or three-dimensional complex shape, as shown in Fig. 8-14.

Additional extensive research has been performed for slot antennas on finite and curved ground planes. The early work done by Jones and Richmond²⁶ using integral equation solutions to determine the *E*-field distribution has been extended to apply to patches of surface instead of strips. This type of EM analysis, commonly referred to as the method of moments (MOM), however, is limited to small surface volumes due to limitations in computers. An asymptotic method, the geometrical theory of diffraction (GTD), has been developed which is not limited by the ground-plane size in wavelengths.

The GTD is an extension of geometrical optics (GO), which is demonstrated in Fig. 8-15. If we consider GO only, there are no fields in region III past the shadow boundary.

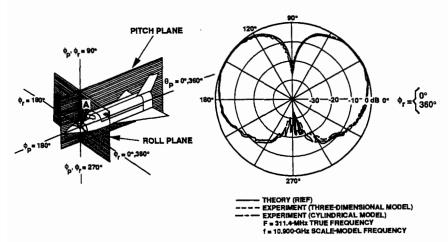


FIG. 8-14 Roll-plane pattern of annular-slot antenna mounted on a model of the space shuttle. (After Jones and Richmond, Ref. 26.)

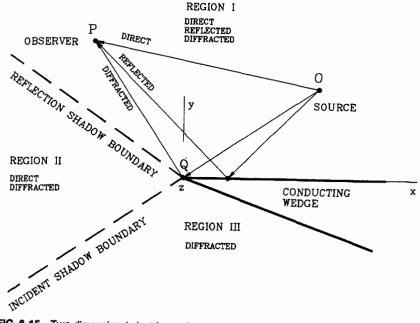


FIG. 8-15 Two-dimensional electric conducting wedge and field regions. (After Balanis, Ref. 27.)

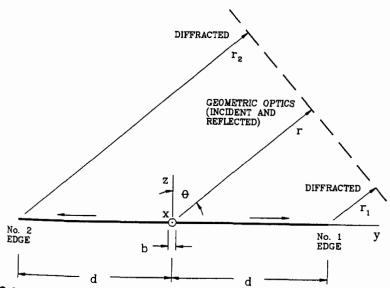


FIG. 8-16 Aperture geometry in the principal-plane *E*-plane ($\phi = \pi/2$). (After Balanis, Ref. 27.)

Actually the diffracted fields do exist and can be computed by GTD.²⁷ A simple example of the use of GTD is depicted in Fig. 8-16. Following Balanis,²⁷ the total fields in all regions can be summarized as

$$E_{t} = E_{go}(r, \theta) + E_{1}^{d}(\theta) + E_{2}^{d}(\theta)$$
(8-7)

where

$$E_{go}(r,\theta) = E_0 \left[\frac{\sin\left(\frac{ka}{2}\sin\theta\right)}{\frac{ka}{2}\sin\theta} \right] \frac{e^{-jkr}}{r} \qquad 0 \le \theta \le \frac{\pi}{2}$$

$$E_{1}^{d}(\theta) = \frac{E_{0} \sin\left(\frac{ka}{2}\right)}{\frac{ka}{2}} V_{B}^{i,r}(d, \beta = \theta + \pi/2, 2) e^{jkd \sin\theta} \frac{e^{-jkr}}{r}$$
 (8-8)

$$E_{2}^{d}(\theta) = -\frac{E_{0} \sin\left(\frac{ka}{2}\right)}{\frac{ka}{2}} V_{B}^{i,r}(d, \beta, 2) e^{jkd \sin \theta} \frac{e^{-jkr}}{r}$$
 (8-9)

where

$$\beta = \begin{cases} \pi/2 - \theta & 0 \le \theta \le \pi/2 \\ 5\pi/2 - \theta & \pi/2 \le \theta \le \pi \end{cases}$$

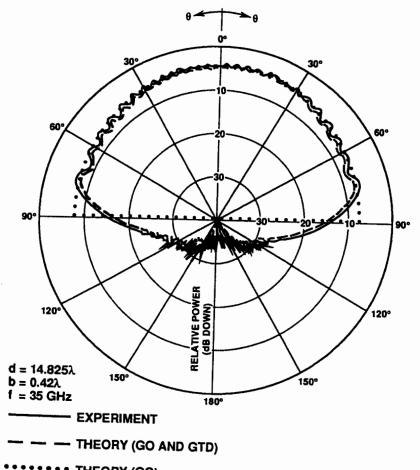
and V_b^{fr} are the wedge diffraction coefficients. A typical result for a slot on a finite ground plane is given in Fig. 8-17.

This work has been extended to slots opening to both square and elliptical cylinders, ²⁸ as shown in Fig. 8-18. Note that the patterns are qualitatively similar except for the ripple caused by diffractions at the edges of the rectangular cylinder. Further applications of GTD to three-dimensional surfaces for slot-antenna pattern calculations have been extensively pursued. Some work is described in Chap. 37.

8-7 SLOT ANTENNAS ON CYLINDERS, CONES, AND SPHERES

A common design problem for spacecraft, aircraft, and rocket antennas is to determine the pattern and impedance of such antennas when located on curved dielectric-coated surfaces where the conformal dielectric is a radome, a reentry ablator, and/or an absorber. In order to obtain first-order results, it has been found useful to consider the radiation characteristics of slot antennas on cylinders, cones, and spheres.

The best early summary for slots on cylinders is a book by Wait.²⁹ Accurate calculations of the patterns of a slot on an uncoated cylinder have been published by Knop and Battista,³⁰ a few of which are given in Fig. 8-19; note that c = ka. If a coating is applied to the cylinder surface, a series of azimuthal surface waves can be excited that can produce major ripples in the pattern depending on dielectric constant and thickness. An estimate



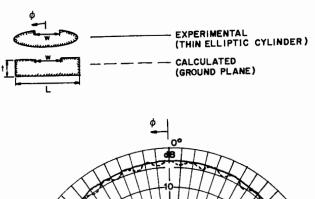
**** THEORY (GO)

FIG. 8-17 Principal E-plane amplitude patterns of an aperture antenna mounted on a finitesize ground plane. (After Balanis, Ref. 27.)

of such modes can be made using equations in Ref. 23. Measured patterns of a coated azimuthal slot on a cylinder are available.31 Similar effects were noted for axial slots on dielectric-coated cylinders (unpublished notes).

The admittance of a slot on a coated cylinder also has been computed. 32 The admittance is about the same as that on a flat coated ground plane with

$$ka = \frac{2\pi a}{\lambda} \ge 3 \text{ to } 4$$



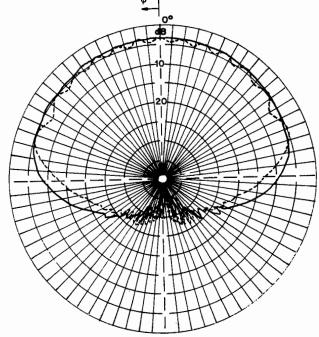


FIG. 8-18 Radiation patterns of a thin elliptical cylinder and finite ground plane (TEM mode).

An interesting fact is that about 2ka terms are required to compute a convergent value of conductance. However, the susceptance requires about 75 to 100 terms regardless of ka. The susceptance in this formulation represents the near field of the slot.

A major problem on early satellites was to design an antenna having a quasiisotropic radiation pattern on spherical-shaped surfaces with large values of ka. Early data were available for small spheres, but patterns for larger spheres excited by a parallel-plate waveguide were first considered by Bugnolo,³³ who took great care to make precise measurements. More practical forms of the large spherical antenna excited by a slotted waveguide and a modified parallel-plate waveguide have been repeated.^{31,34}

Another slot antenna of great interest for missiles and aircraft is the slotted cone. This problem is dominated by the tip diffraction.³⁵ Additional results for a slot on a cylinder fed by a cavity are given in Ref. 36. Antennas similar to this were mounted on sphere-tipped cones and used for telemetry antennas on reentry payloads.

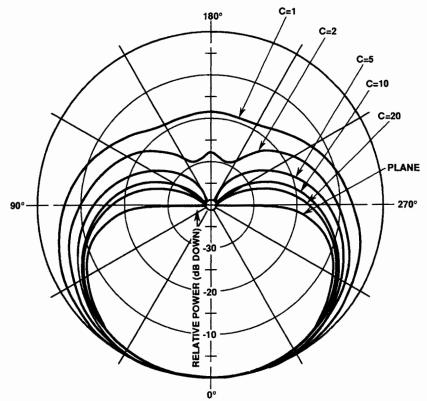


FIG. 8-19 Equatorial-plane power patterns for a half-wavelength slot on an uncoated cylinder. (After Knop and Battista, Ref. 30.)

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Slot-Antenna Arrays

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Texas Instruments, Inc.

9-1	Introduction 9-2
9-2	Slot Radiators 9-2
	Equivalent-Impedance
	Representation 9-5
	Scattering-Matrix Representation
	0.6

- 9-3 Computation Methods for Slot Characterization 9-6 Stevenson's Solution 9-6 Variational Technique 9-7 Scattering Modal Analysis 9-9 Moment Method 9-10
- 9-4 Design Parameters 9-10
 Longitudinal Shunt Slots 9-11
 Edge-Wall Slots 9-11
 Series Slots 9-15
- 9-5 Basic Slotted-Waveguide Array
 Design Methods 9-16
 Active Slot Admittance 9-17
 Equivalent Self-Admittance 9-18
 Incremental Conductance 9-18
 Semiempirical Admittance 9-19

- 9-6 Resonant Slotted-Waveguide Array
 Design 9-20
 Linear Array 9-20
 Planar Array 9-22
- 9-7 Traveling-Wave Slot-Array Design 9-25 Uniformly Spaced Traveling-Wave

Slot-Array Design 9-27 Nonuniform Traveling-Wave Slot-Array Design 9-29

- 9-8 Power-Handling Capabilities of Slotted-Waveguide Arrays 9-31
- 9-9 Tolerance and Fabrication Techniques 9-33
- 9-10 Recent Developments 9-35
 Broad-Wall Longitudinal Slots 9-35
 Narrow-Wall Slots 9-36
 Ridge-Waveguide-Fed
 Longitudinal Slots 9-37

Geometric simplicity, efficiency, reliability, and light weight make slot-antenna arrays attractive for many radar and communication applications. Either resonant or traveling-wave slot-antenna arrays allow accurate control of aperture excitation amplitude and phase. The demands of lower sidelobe levels and greater efficiency in recent slotted-array applications require more accurate knowledge of slot characteristics, improved modeling of array effects, and greater manufacturing accuracies. A resonant slot-antenna array can produce a pencil beam with sidelobe levels less than —28 dB over a 4 percent frequency bandwidth using today's design and fabrication techniques. The traveling-wave slotted arrays usually outperform the resonant arrays with lower sidelobe levels, but at the expense of lower efficiency and a scanning beam with frequency.

This chapter focuses on rectangular waveguide-fed slot arrays. Alternative slot-antenna array configurations employ circular-waveguide-fed, ridge-waveguide-fed,¹ or strip-transmission-line-fed (triplate or microstrip) slots. ^{1a,2,3} Single-plane, wide-angle scanned phased arrays take advantage of the small waveguide spacing allowed with ridge-waveguide-fed slots. However, the higher fabrication cost limits the use of ridge-waveguide-fed slots in single-plane scanned phased arrays. The advantages of strip-transmission-line-fed slots are manufacturing simplicity, low cost, and low profile. Excessive transmission-line loss, low power handling, and performance dependence on dielectric-material variations limit the use of strip-line-fed slots to low-performance applications.

Both resonant and nonresonant (traveling-wave) waveguide-fed slot-antenna arrays can be configurated into either linear or planar arrays. Many recent airborne radar antennas have used planar resonant-slot arrays. Kaminow and Stegen^{4,5} reported the design of linear traveling-wave slot arrays with uniform element spacing. Nonuniformly spaced array designs have received little attention and will be discussed here in greater detail.

The following sections begin by introducing various slot radiators with basic operating theories and mathematical representations. Subsequent discussions include analytical methods for slot characterization and the design of resonant-waveguide slotted arrays and traveling-wave slotted arrays with uniformly or nonuniformly spaced slots. We emphasize practical design methods which include mutual coupling effects and use of typical characteristics for slots cut in a standard X-band RG52/U waveguide with a 1.5875-mm (0.0625-in) slot width and a frequency of 9.375 GHz. The practical aspects of power-handling capacity, tolerance effects, and fabrication techniques are included. Finally, we review the recent developments in the method-of-moments (MOM) solution for slotted arrays and ridge-waveguide-fed slots.

9-2 SLOT RADIATORS

The slot is a commonly used radiator in antenna systems. An attractive feature is that slots can be integrated into the array feed system, such as a waveguide or stripline system, without requiring a special matching network. Low-profile high-gain antennas can be easily configured by using slot radiators, although their inherent narrow-frequency bandwidth can limit antenna performance in some applications.

A slot cut into the waveguide wall which interrupts the flow of currents will couple power from the waveguide modal field into free space. Depicted in Fig. 9-1 are the surface currents flowing along the rectangular-waveguide inner wall when only the TE₁₀ mode is excited in the waveguide. A singly moded waveguide is required for a

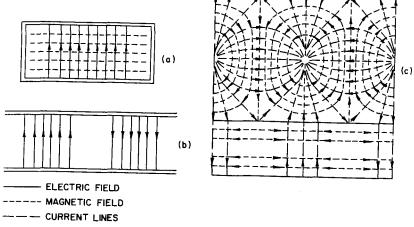


FIG. 9-1 Surface-current distribution for rectangular waveguide propagating TE₁₀ mode. (a) Cross-sectional view. (b) Longitudinal view. (c) Surface view.

slotted-waveguide array design to control the aperture illumination. Commonly used slot types are shown in Fig. 9-2. Slots cut in the rectangular waveguide as shown in Fig. 9-3 are nonradiating because they are parallel to the surface-current vector.

Slots are conveniently classified by shapes, locations in the rectangular waveguide, and equivalent-network representations. Edge-wall slots (slots b and c in Fig.

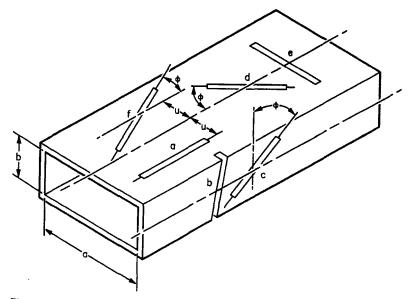


FIG. 9-2 Radiating slots cut in the walls of a rectangular waveguide.

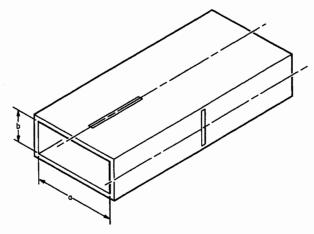


FIG. 9-3 Nonradiating slots cut in the walls of a rectangular waveguide.

9-2) are cut into the narrow wall and wrapped around the broad wall of the rectangular waveguide, where the resonant slot length is determined by the depth of the cutting. In designing a planar array using edge slots, the wrap around the broad wall contributes to both design and fabrication difficulties. In this circumstance, folded edge-wall slots such as C and I slots (see Fig. 9-4) can be used to replace the simple edge slot.

A longitudinal shunt slot (slot a in Fig. 9-2) and an inclined series slot (slot d in Fig. 9-2) are cut on the rectangular-waveguide broad walls; they are distinguished by their equivalent-impedance representations. A rectangular slot shape is convenient for analytical investigation, but in most applications the shape is chosen to simplify the

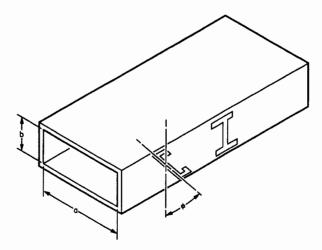


FIG. 9-4 Configurations of C and I slots.

fabrication process. Many arrays of broad-wall slots employ a rectangular shape with round ends formed by the milling process.

To design a slotted-waveguide antenna array, the basic characteristics for a given slot geometry, such as the radiated-field amplitude and phase plus mutual-coupling effects between slots and within the feed network, are needed. From the standpoint of array design and simple analysis, equivalent impedance is the most convenient slot characteristic. However, the scattering-matrix representation is required in the analysis and design of certain large slotted-waveguide arrays in which complicated feed networks and the slots are coupled.

Equivalent-Impedance Representation

The design of large slotted-waveguide arrays frequently uses the simple single-element equivalent circuit representation. This single-element impedance representation is valid

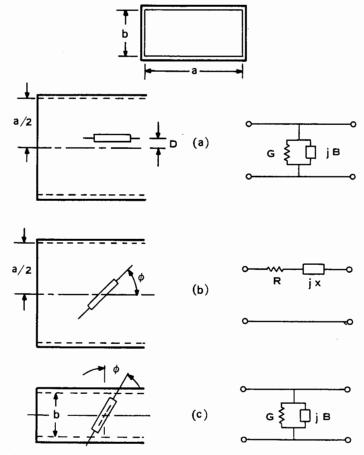


FIG. 9-5 Equivalent-network representations of slot radiators.

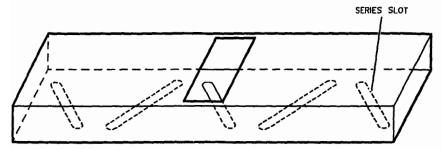


FIG. 9-6 Typical waveguide section with series slots.

only for slot widths that are small compared with slot lengths and slot lengths less than one waveguide wavelength; otherwise, the more complicated equivalent T or pi network is required. Large-offset longitudinal slots in waveguides with heights less than one-quarter wavelength require special attention. 64

Narrow slots such as slots a, b, and c in Fig. 9-2 interrupt only the transverse currents and are represented by a simple two-terminal shunt admittance; therefore, they are identified as shunt slots. Similarly, slots d and e interrupt only the longitudinal currents and are represented by a simple series impedance; they are referred to as series slots. Slot f is coupled to both longitudinal and transverse currents, and a T-or pi-network representation is necessary even for a narrow slot width. The equivalent circuits for three frequently used slots are shown in Fig. 9-5.

Scattering-Matrix Representation

Waveguide-fed slots can also be represented by scattering matrices. A scattering-matrix representation is convenient for analyzing slot-antenna performance by taking into account the coupling of slots to other slots or to the feed network. An example is a resonant waveguide section with several series slots cut on the broad wall fed by an E-plane T junction as shown in Fig. 9-6. The characterization of the series feed with a series slot directly above the T junction requires a scattering-matrix representation. Let the waveguide-fed slot be represented by a stub guide branching out from the main guide. If the slot is facing a T junction on the opposite side of the guide, a four-port scattering matrix representing the T junction and the stub guide can be derived by solving the physical problem. Combining this scattering matrix with other slot scattering matrices, the power coupled out from each slot can be computed by taking into account the coupling between the slot and the feed junction.

9-3 COMPUTATION METHODS FOR SLOT CHARACTERIZATION

Many authors have reported extensive analytical and experimental studies of waveguidefed slot characteristics. Applying impedance-measurement techniques⁷ to slot characterization depends on equipment development and will not be included in the following discussion. On the other hand, many recent investigations exploited theoretical computation methods for slot characteristics. This section will focus on the theoretical analysis techniques.

Stevenson's Solution

Stevenson⁸ pioneered the computation of slot characteristics by using the following assumptions: (1) a perfectly conducting thin wall, (2) a narrow slot, (3) a slot length nearly equal to half free-space wavelength, and (4) a perfectly conducting ground plane of infinite extent. Using transmission-line theory and the waveguide modal Green functions, Stevenson derived the values of the resonant resistance and conductance, normalized to the waveguide impedance, for various slots cut in a rectangular waveguide.

1 Conductance of the longitudinal shunt slot in the broad face (slot a in Fig. 9-5):

$$g = g_1 \sin^2(D\pi/a) \tag{9-1}$$

$$g_1 = (2.09 a \lambda_g/b \lambda) \cos^2(\lambda \pi/2 \lambda_g)$$
 (9-2)

where λ is the free-space wavelength, λ_g is the guide wavelength, D is the slot displacement from the guide centerline, and a and b are the waveguide width and height.

2 Resistance of the centered inclined series slot on the broad face (slot b of Fig. 9-5):

$$r = 0.131(\lambda^3/ab\lambda_g)[I(\phi)\sin\phi + (\lambda_g/2a)J(\phi)\cos\phi]^2$$
 (9-3)

$$\frac{I(\phi)}{J(\phi)} = \frac{\cos{(\pi\xi/2)}}{1-\xi^2} \mp \frac{\cos{(\pi\xi/2)}}{1-\xi^2}$$
 (9-4)

$$\begin{cases} \xi \\ \zeta \end{cases} = \frac{\lambda}{\lambda_g} \cos \phi \pm \frac{\lambda}{2a} \sin \phi \tag{9-5}$$

where ϕ is the slot inclination angle with the guide centerline.

3 Conductance of edge slot on the narrow face (slot c of Fig. 9-5):

$$g = \frac{30\lambda^3 \lambda_g}{73\pi a^3 b} \left[\frac{\sin \phi \cos (\pi \lambda \sin \phi / 2\lambda_g)}{1 - (\lambda \sin \phi / \lambda_g)^2} \right]^2$$
 (9-6)

These equations yield quite accurate results. However, they are valid only for a single-slot radiator and give no information about the reactive component. In particular, significant errors will result when these equations are applied to most two-dimensional arrays in which mutual-coupling effects cannot be neglected. Equations (9-1) through (9-6) are useful only when mutual-coupling effects are negligible.

Variational Technique

Application of the variational method to slot equivalent-circuit computation was first formulated by Oliner. This method can account for mutual coupling and also reveal the reactive component of the slot impedance. Accurate impedance solutions can be

obtained with the variational technique by using a slot-aperture field close to the actual slot field.

Consider the example of a longitudinal shunt slot in the broad face of a rectangular waveguide radiating into free space. By extending Oliner's variational formulation, an explicit impedance expression can be derived in terms of the slot-aperture admittance $Y_r = G_r + jB_r^{-10}$

Let the length and the width of the rectangular slot be a' and b' respectively. The propagation constant and the characteristic admittance of the dominant mode in the waveguide are given by $\kappa = (k^2 - (\pi/a)^2)^{1/2}$ and $Y_0 = \kappa/\omega\mu$, where $k = 2\pi/\lambda$, ω is the angular frequency, and μ is the permeability. The rectangular slot on the thick waveguide wall is regarded as a stub guide with propagation constant κ' and characteristic admittance Y_0' . The input admittance at the stub-guide junction can be determined by

$$Y_{rj} = Y_0' \frac{Y_r + jY_0' \tan \kappa' t}{Y_0' + jY_r \tan \kappa' t}$$
 (9-7)

where t is the thickness of the guide wall. From the standpoint of the feed waveguide, the equivalent circuit of a displaced longitudinal shunt slot can be represented by a shunt network as depicted in Fig. 9-7. Z_{rj} is the impedance due to the radiating aperture, while X_j is related to the stored power in the feed waveguide. Near resonance, these quantities can be approximated by the variational result¹⁰

$$\frac{R+jX}{Z_0} = \frac{Z_{rj}+jX_j}{Z_0} = \frac{a'b'}{2N_s^2} \frac{(Y_{rj}+jB_j)}{Y_0}$$
 (9-8)

$$N_s^2 = (2/ab) \frac{2\pi^2 b'}{aa'\kappa} \left[\frac{\sin(\pi D/a)\cos(\kappa a'/2)}{(\pi/a')^2 - \kappa^2} \right]^2$$
 (9-9)

where D is the displacement of the slot from the center of the waveguide. The junction susceptance B_I is given by

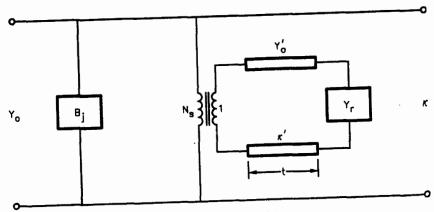


FIG. 9-7 Equivalent network of a longitudinal shunt slot.

$$B_{j} = \frac{4b'}{\omega \mu ab} \sum_{m=0}^{\infty} \left[\cos \left(\frac{m\pi}{2} + \frac{m\pi D}{a} \right) \operatorname{sinc} \left(\frac{m\pi b'}{2a} \right) \right]^{2} \operatorname{Im}(W) / (\epsilon_{m} \epsilon_{n})$$
 (9-10)

where sinc
$$(x) = \sin x/x$$
, $W = j[Q_2(m,n) + Q_3(m,n)]$
 $Q_2(m,n) = \kappa'^2/[(\pi/a)^2 - \kappa_{mn}^2]$
 $Q_3(m,n) = |2(\pi/a')^2 \frac{(m\pi/a)^2 + (n\pi/b)^2}{[(\pi/a')^2 - \kappa_{mn}^2]^2} \frac{1 + \exp(-ja'\kappa_{mn})}{ja'\kappa_{mn}}$
 $\kappa_{mn} = [k^2 - (m\pi/a)^2 - (n\pi/b)^2]^{1/2}$
 $\epsilon_0 = 2$
 $\epsilon_n = 1 \text{ if } n > 0$

Im indicates the imaginary part. This solution can account for mutual-coupling effects if the slot-aperture admittance Y_{rj} is computed under the mutual-coupling environment.

Resonance can be defined as the condition in which slot admittance is a real quantity. To compute the slot resonant length, several slot admittances corresponding to several values of a' nearly equal to one-half wavelength are computed first. The slot resonant length can then be determined by interpolating the length which yields zero imaginary part for the admittance.

Note that the above solution is applicable to rectangular slots only. For roundended slots, the resonant length can be approximated by

$$L = a' + Cb'(1 - \pi/4)$$
 (9-11)

where a' is the resonant length of the equivalent rectangular slot and C is the correction factor.¹⁰

A similar variational formulation has been applied to compute the impedance of an inclined series slot in the rectangular-waveguide broad face. The slot inclination angle replaces the variable of slot displacement from the waveguide centerline in the derivation. However, the slow convergent series in the resultant reactance expression requires special treatment in the numerical computation.

Because of the complicated slot shape and the unknown field distribution in the slot aperture, variational solutions for edge slots and folded slots have not been derived.

Scattering Modal Analysis

Using an approach similar to Frank and Chu's formulation of the *E*-plane T solution, ^{11,12} Montgomery derived the slot-characterization scattering matrices and hence the shunt-slot admittance and series-slot impedance. ¹³ This scattering modal analysis technique requires a greater computation effort than Stevenson's and the variational solutions.

Basically, the slot is assumed to be a stub guide branched out from the main guide. The slot field is conventionally expressed by a series of stub-guide modal functions. The main-guide field is represented by a series of modal Fourier integrals in which the wave number corresponding to the guide axis is the integration variable. By matching the two tangential field expressions on both sides of the slot aperture, two integral equations are obtained. The expansion coefficients and the scattering parameters can be determined by solving these two integral equations by using the Ritz-

Galerkin method. After the expansion coefficients have been computed, the junction scattering matrix of the slot in the waveguide can be calculated easily. By combining the junction scattering matrix with the slot-radiating-aperture reflection coefficient, the slot equivalent circuit can be determined.

This method has been applied to the computation of individual slot characteristics and to the analysis of coupling effects between two slots or between a slot and a waveguide junction. Numerical results of longitudinal-slot parameters computed by the variational method and the scattering modal analysis compare favorably.

Moment Method

The method of moments has been applied to characterize a narrow slot in the broad wall of a rectangular waveguide^{14,15} and can be extended to obtain the solution of folded slots in the edge wall with additional effort. The moment method requires greater computational effort than any of the three other methods discussed here.

Vu Khac and Carson¹⁴ formulate the slot characterization by using the fieldequivalent principle to replace the slot aperture by short circuits and magnetic currents. The appropriate magnetic Green's functions in the feed guide, inside the slot cavity (taking into account the finite wall thickness), and in free space are employed to derive the basic integral equations. The slot field is expressed as a series of discrete impulse functions. By matching the tangential components at the slot aperture and using the Ritz-Galerkin method, a matrix equation is derived. Then the expansion coefficients can be determined by matrix inversion. The computational effort can be greatly reduced by using the sinusoidal basis functions as shown by Lyon and Sangster. 15 The computed results obtained by using the moment method closely match the variational solution and experimental results.

When the moment method is applied to characterize the inclined series slots, a slowly convergent series is encountered in the same manner as with the variational formulation and the scattering modal analysis. All the matrix elements used in the moment method involve one or two slowly convergent series compared with only one slowly convergent series in the variational technique; therefore, the moment method requires much more computation time.

9-4 DESIGN PARAMETERS

Many slotted-waveguide arrays have been fabricated since the 1940s. Early slotantenna array designs depended primarily on measured slot characteristics. Accurately measured design data require a major effort to design and fabricate many precision test pieces. Analytical methods for characterizing broad-wall slots have since been developed into useful tools for practical slotted-waveguide array design. It requires only a few hours of computer time to obtain design parameters which would have required several months of experimentation. A planar slotted-waveguide array with more than 1000 longitudinal shunt slots has been fabricated successfully by using analytical data.

The measured and computed slot characteristics presented in this chapter, except that shown later in Fig. 9-13, are given for a standard X-band RG52/U waveguide with a 0.0625-in (1.5875-mm) slot width and a frequency of 9.375 GHz. This slot will subsequently be referred to as the baseline slot. A planar slotted-waveguide array can be designed at 9.375 GHz by using data presented in this section.

Longitudinal Shunt Slots

Watson¹⁶ and Stegen⁵ performed extensive experimental studies of isolated longitudinal shunt slots radiating into free space. From the measured data, Stegen found that the ratio of conductance to resonant conductance G/G_m and the ratio of susceptance to resonant conductance B/G_m versus the ratio of slot length to resonant length are independent of the slot displacement off the waveguide centerline. These universal curves of the baseline-slot admittance normalized by the resonant conductance versus slot length normalized by the resonant length are plotted in Fig. 9-8. The measured ratio of slot resonant length to wavelength and the measured ratio of slot resonant conductance to waveguide wave admittance versus the slot displacement off the waveguide centerline are shown in Figs. 9-9 and 9-10 respectively.

By using the variational result of Eqs. (9-7) through (9-10), the computed slot admittance normalized by the resonant conductance is also shown in Fig. 9-8. The aperture admittance of a slot radiating into the half space is approximated by the solution given by Kurss and presented in Ref. 9. Observe that the computed results agree very well with the measured data. However, the computed results show that the ratios G/G_m and B/G_m versus the normalized slot length L/L_0 are not exactly independent of the slot displacement off the guide centerline.

By using the same technique, the computed slot resonant length and resonant conductance are shown in Figs. 9-9 and 9-10 respectively for comparison with the measured results. Note that the round-ended-slot resonant length L_0 is approximated by Eq. (9-11). Choosing C equal to 0.64 and comparing the computed and measured results show that the computation method is sufficiently accurate for practical applications.

In airborne radar applications, large arrays of uniformly spaced slots are commonly used. The longitudinal-shunt-slot admittance of a slot in the central region of a uniform large array can be computed by the variational technique. ¹⁰ If the element spacing of a square grid is assumed to be equal to 0.71 wavelength, the slot-aperture admittance can be determined by an infinite array of open-ended rectangular waveguides. ¹⁷ The computed normalized admittance of the baseline slot in the array is compared with the measured results of the isolated slot in Fig. 9-11. The comparison shows that the mutual-coupling effects reduce the slot bandwidth performance.

By using the same dimensions, the resonant conductance and resonant length for a slot in a large array are shown in Figs. 9-9 and 9-10. Observe that the mutual-coupling effects also affect the slot resonant length as well as the slot resonant conductance. The small change in the slot resonant length in this case may not significantly affect antenna performance. However, an increase of the slot resonant conductance by a factor of 2 usually causes a 2:1 voltage standing-wave ratio (VSWR) at the center frequency. This has been observed in slot-antenna arrays designed by using measured single-longitudinal-slot conductances.

Edge-Wall Slots

The narrow-wall slots used for common linear slot-antenna arrays are cut into the narrow wall and wrapped around the broad wall of the rectangular waveguide (edge slots). Folded slots such as C and I slots are more convenient for planar arrays using edge-wall slots. ^{18,18a,18b} Recently, several authors derived analytical solutions for narrow-wall slot characteristics. These solutions include the inclined-edge slot, C-slot, and I-slot. All these narrow-wall slots radiate relatively high cross-polarized fields as compared with

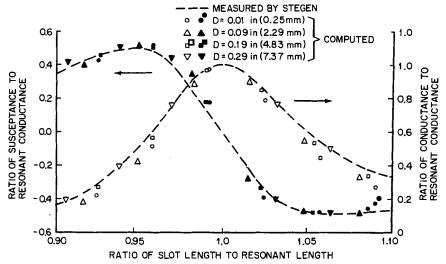


FIG. 9-8 Admittance of the baseline longitudinal shunt slot versus normalized slot length.

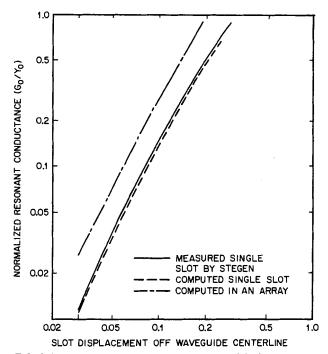


FIG. 9-9 Normalized resonant conductance of the baseline longitudinal shunt slot versus displacement off the waveguide centerline.

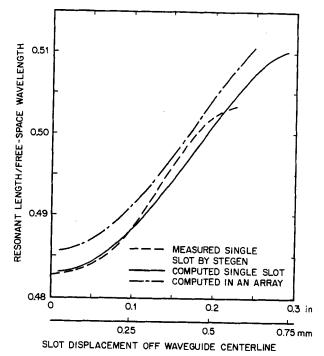


FIG. 9-10 Normalized resonant length of the baseline longitudinal shunt slot versus displacement off the waveguide centerline.

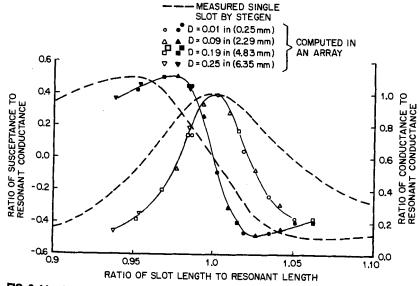


FIG. 9-11 Admittance of the baseline longitudinal shunt slot versus normalized resonant slot length. The solid curves are best fit to the computed points.

the broad-wall longitudinal slots. Experimental results must be used to characterize these slots. Fortunately, the strong mutual-coupling effects can be measured by a waveguide section with a sufficient number of identical edge-wall slots. Watson¹⁶ has defined the incremental conductance caused by the mutual-coupling effects as the increase in the conductance of a group of resonant half-wave-spaced identical edge-wall slots.

For both the edge slot and the C slot, the resonant conductance may be approximated by

$$G = G_0 \sin^2 \phi \qquad |\phi| \le 15^{\circ}$$
 (9-12)

where ϕ is the slot inclination angle. The slot resonant conductance is insensitive to the variation in the slot resonant length. Hence, if the incremental conductance is obtained by experiment for one value of angle, Eq. (9-12) can be used to obtain the resonant conductance for other slot inclination angles with reasonable accuracy.

Plotted in Fig. 9-12 are the single-slot resonant conductance and the incremental conductance for edge slots cut on the standard RG52/U rectangular waveguide measured by Guptill and Watson. ¹⁶ The incremental conductance data are sufficiently accurate for slots in a linear array far removed from the ends. The conductance of the slots near the ends of the array lies between that of the single-slot data and that of the incremental conductance.

The edge-slot admittance variation as a function of the depth of cut into the rectangular-waveguide broad faces was investigated by Watson. ¹⁶ Measurements were performed on a slot cut in the standard RG48/U waveguide. Depicted in Fig. 9-13 are the measured results for a single 15° slot with slot width equal to 0.25 in (6.35 mm) at 2.8 GHz. These results can be translated to the frequency performance of the edge slot with the conclusion that the frequency bandwidth of edge slots is greater than that of longitudinal shunt slots.

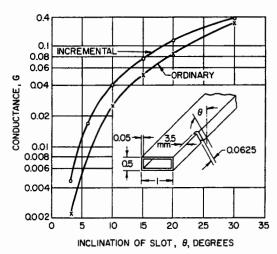


FIG. 9-12 Incremental and single-slot conductances (unmarked dimensions of waveguide section are in inches); frequency = 9.375 GHz, RG52/U waveguide.

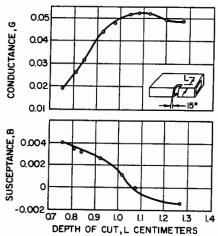


FIG. 9-13 Variation of slot admittance with depth of cut; frequency = 2.8 GHz, RG48/U waveguide.

Series Slots

Centered inclined series slots in the rectangular-waveguide broad face radiating into free space can be used as radiating elements for slot-antenna arrays. The series-slot-radiation primary polarization is the same as that of the longitudinal shunt slot, but the series-slot cross-polarization radiation is much higher than that of the shunt slot. Hence the inclined series slot is not often used as a radiating element in practical designs. However, this slot is very useful for coupling radio-frequency power from one waveguide to another in a planar slot-array design such as that shown in Fig. 9-6.

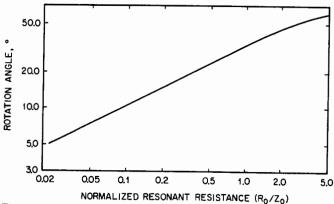


FIG. 9-14 Normalized resonant resistance versus rotation angle of a baseline inclined series slot.

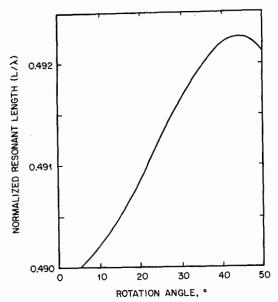


FIG. 9-15 Normalized resonant length versus rotation angle of a baseline inclined series slot.

The series-slot impedance can be computed by the variational formulation, the scattering modal analysis technique, or the moment method as described above. By using either the variational formulation or the scattering modal analysis, the slot is first considered as a branched waveguide radiating into the main waveguide. The aperture impedance of the branched waveguide can be determined by assuming a cosine distribution across the slot aperture. The slot-aperture impedance facing the other waveguide can be computed in the same manner except that the slot inclination angle is the complementary angle. Properly combining these two solutions yields the series-slot impedance and hence the slot resonant resistance and resonant length. When round-ended series slots are used in the design, the slot resonant length can be determined by setting C = 1 in Eq. (9-11).

By using the scattering modal analysis solution, the computed resonant resistance and round-ended resonant length versus the inclination angle for the baseline slot are plotted in Figs. 9-14 and 9-15. The input and output waveguides are assumed to be perpendicular to each other for these computed data.

9-5 BASIC SLOTTED-WAVEGUIDE ARRAY DESIGN METHODS

After obtaining the required slot characteristics, the slotted-waveguide array design must specify the slot locations and resonant conductances and/or resistances. Determination of the resonant conductances and/or resistances is an important part of antenna input matching and aperture illumination design.

Antenna requirements are usually specified in terms of desired gain, sidelobe level, beamwidth, bandwidth, polarization, input VSWR, cross-polarization level, power-handling capability, etc. All these requirements impact the slotted-waveguide array design. Aperture distribution is determined by aperture synthesis techniques, ^{19,20} taking the gain, sidelobe level, and beamwidth into consideration, and is assumed to be known for the following discussion.

The slot locations are governed by the relationship between the element spacing and the appearance of grating lobes. Adjacent slots are spaced apart by less than 1 free-space wavelength to avoid the appearance of grating lobes. For a resonant slotted-waveguide array, the desired aperture illumination is in phase across the aperture. To satisfy the grating-lobe restriction and the in-phase radiation requirement, the interelement spacing for slots on the same waveguide of a resonant array is therefore equal to one-half waveguide wavelength along the waveguide centerline. The interelement spacing of a nonresonant slotted-waveguide array is slightly larger or smaller than the spacing of resonant array elements, as will be detailed later.

Resonant conductances and/or resistances are determined by the given aperture illumination. To optimize bandwidth performance, the slots are designed to be resonant at midband for either resonant or nonresonant arrays. Basically, slot-radiated power is proportional to slot conductance or resistance. If P is the required fraction of slot-radiated power, normalized shunt-slot conductance and series-slot resistance are given by

$$g = 2P/V^2$$
 $r = 2P/I^2$ (9-13)

where V and I are respectively the voltage and current across the slot. The transmission-line or scattering-matrix theories can be used to determine V and I and, therefore, g and r.

After slot locations and resonant conductances or resistances have been determined, the slot-array design can be completed by using the known slot characteristics or design curves to specify the slot geometry in the waveguide. If single-slot results, such as Eq. (9-1) with slot length equal to half wavelength, or the design curves depicted in Figs. 9-9, 9-10, and 9-13 for a single shunt slot radiating into free space are used to determine the slot geometry, the array aperture illumination will not be the desired distribution and the input VSWR will be higher than the requirement because of neglect of the mutual-coupling effects. There are four known approximate techniques to overcome this difficulty. Three of these methods take advantage of the known dipole array solution^{21,22} and Babinet's principle, which relates slot-aperture admittance to the complementary dipole radiation impedance by

$$Y_r = 4b'\tilde{Z}/(\eta_0^2 a') \tag{9-14}$$

where \tilde{Z} is the dipole impedance and η_0 is the free-space intrinsic impedance. Another method is the empirical technique originated by Watson.¹⁶ The first two methods to be described apply only to longitudinal-shunt-slot arrays, while the last two methods are valid for all cases.

Active Slot Admittance

Elliott^{23,24} derives two expressions for slot-array active admittances in terms of slot excitation voltages, slot parameters, and the complementary dipole array active impedances. By combining these two expressions with the corresponding dipole array

solution, a small-array slot geometry can be specified by using the iterative procedure as described by Elliott.²³ The single-slot admittances of a single-slot radiator are used to model the slot admittance characteristics to reduce computational effort. This technique is quite accurate for small-array design as demonstrated by Elliott.²³ The required computation effort makes this technique unattractive for large-array applications.

Equivalent Self-Admittance

Slot equivalent self-admittances can be computed by Eqs. (9-7) through (9-10) by neglecting the edge effects, the small alternating displacements from the guide centerline, the slowly varying illumination, and the small slot-length variation. The aperture admittance is determined by either (1) the equivalent infinite waveguide array aperture admittance¹⁷ or (2) the substitution of the complementary dipole array self-impedance²¹ into Eq. (9-14). By using the computed admittance values corresponding to several slot lengths, the resonant conductance and resonant length versus slot displacement similar to that shown in Figs. 9-9 and 9-10 can be determined. By combining these design curves with the predetermined slot locations and resonant conductances, the slot-array antenna design is completed.

Note that these computed slot admittances take mutual-coupling effects into account but neglect edge effects, slot displacements from the guide centerline, non-uniform aperture illumination, and slot-length variation. For large arrays in general, displacements are small, illumination is slowly varying, and edge effects can be neglected. This technique is much more efficient than the active slot admittance method. For a small array, edge effects can be taken into account by several sets of resonant-conductance and resonant-length curves by using the corresponding small-dipole-array solutions. Dipole arrays corresponding to several uniformly alternating displacements can be used to compute the design curves for central elements and edge elements. For practical applications, neglecting alternating displacements in the equivalent dipole array computation results in negligible conductance error and in less than 1.2 percent resonant-length error.

A dielectric cover on the outer waveguide surface is frequently used to protect the antenna from the environment. In general, dielectric loading has little effect on the resonant conductance or resistance of a slot. However, the resonant length is greatly reduced by a dielectric cover and depends on the dielectric constant and thickness. Dielectric-loading effects can be taken into account by using the infinite waveguide array solution.¹⁷

Incremental Conductance

The two methods described above are applicable only to arrays of longitudinal shunt slots. Analytical solutions have not been well developed for edge-wall slots, and therefore the designs rely on experimentation.

Many waveguide test sections are required to characterize the slots, including mutual-coupling effects. Each of the test arrays has a sufficiently large number of identical conductance resonant slots so that the edge effects can be neglected. The moving lossy short technique has been successfully applied to the slot-characteristic measurements.^{7,25} Design curves such as resonant conductance and resonant length versus inclination angle for edge slots can be determined as shown in Fig. 9-12. Observe that this technique is adequate for large linear-array designs but that inaccurate aperture illumination will be expected when it is applied to small-array designs.

Semiempirical Admittance

The three methods discussed above are not applicable to small arrays or unequally spaced slotted arrays of edge-wall shunt slots; hence the semiempirical admittance technique can be used. Basically, the dipole array solution is combined with the following equations to obtain the semiempirical slot characteristics. This technique is also applicable to design arrays of longitudinal shunt slots. By deduction from Eqs. (9-8) and (9-14), the slot resonant conductance can be expressed by

$$g = U'/\tilde{r} \tag{9-15}$$

where \hat{r} is the complementary dipole active resistance normalized by the waveguide characteristic impedance and

$$U' = U(a,b,a',b') \begin{cases} \sin^2{(\pi D/a')} \\ \sin^2{\phi} \end{cases}$$
 (9-16)

The upper and lower expressions apply to the longitudinal shunt slot and the edge-wall shunt slots respectively. In general, the change in slot resonant length due to mutual coupling is small, and U is a slowly varying function of a'. Thus, U can be determined approximately by experimentation. By combining the approximate value of U, the complementary dipole array solution, the resonant slot conductance, and the slot-location design procedure to be described later, the slot geometry can be determined in the following steps:

Step 1 Measure the single-slot characteristics.

Step 2 By substituting the complementary single-dipole resistance (zero-order approximate value of r) and the measured single-slot resonant conductance into Eqs. (9-15) and (9-16), the values of U for a given slot length and width are determined.

Step 3 By combining the single-slot solution with the equations for specifying the slot locations and resonant conductances such as Eqs. (9-18), (9-19), and (9-32), the first-order design of the slot locations and displacements (or inclination angles) can be determined.

Step 4 The driving-point impedance of the complementary dipole array can be computed by the technique of Carter, ²¹ using the computed slot locations and displacements (or inclination angles) obtained from Step 3 or Step 5 for the lower-order approximation.

Step 5 By substituting the dipole array results from Step 4 into Eqs. (9-15) and (9-16) and combining with slot-location and conductance equations, the next-higher-order approximate solutions for slot locations and displacement (or inclination angles) can be obtained.

Step δ Repeat Steps 4 and 5 until a satisfactory convergence solution is achieved.

Note that this design procedure yields no information on the resonant lengths of the slots in the array. Fortunately, the slot admittance phase variation introduced by mutual coupling is, in general, small compared with π . Suppose that the single-dipole driving-point impedance is represented by $Z_d' = R_{d'} + jX_{d'}$ and the final solution is $Z_d = R_d + jX_{d'}$, then if the guide-wall thickness is negligibly small, the phase difference between the single-slot admittance and the admittance of the slot in the array ψ can be approximated by

$$\tan \psi = 2(X'_d - X_d)/(R'_d + R_d)$$
 (9-17)

The phase correction can be determined by experimentation or computation of the complementary dipole array by using the ratio of the incremental phase to the incre-

mental slot length near the first resonance. This quantity is almost a constant and depends only on the slot and waveguide geometry.

The above iterative procedure has been found to converge rapidly when applied to a planar array of nonuniformly spaced C slots.

9-6 RESONANT SLOTTED-WAVEGUIDE ARRAY DESIGN

Both linear and planar resonant slotted-waveguide arrays have been designed for practical applications. The planar resonant array of longitudinal shunt slots is the most common antenna used in modern airborne radar. The resonant array can be used to produce a broadside pencil beam, with options to obtain two- or four-lobe monopulse. The basic characteristics common to all resonant slotted-waveguide arrays are summarized as follows:

- 1 All slots are resonant in the array; i.e., the susceptances or the reactances of the slot equivalent circuits vanish at the center frequency.
- Waveguide standing-wave voltage maxima appear at the shunt slots and minima at the series slots.
- 3 All slots are spaced one-half waveguide wavelength away from adjacent slots in the same waveguide.
- 4 The main beam is normal to the array aperture (broadside).

In order to make two slots one-half waveguide wavelength apart radiate in phase, the adjacent longitudinal shunt slots are placed on opposite sides of the waveguide centerline; similarly, the adjacent edge-wall slots are inclined on opposite sides of the vertical centerline. When the rotational series-slot array is used to feed a group of linear arrays, the adjacent slots are rotated in the opposite direction across the longitudinal waveguide axis.

Since the planar array can be considered a composition of linear arrays, the design of a planar array is quite similar to the linear-array design. The mutual-coupling environment of these two types of antenna arrays differ; hence they are discussed separately.

Linear Array

To date the majority of linear slotted arrays have used either longitudinal shunt slots or edge-wall shunt slots as radiating elements. Longitudinal shunt slots are used to produce the radiation polarized perpendicular to the array axis, while edge-wall shunt slots are used to obtain the radiation polarized parallel to the array axis. The inclined series slot is not popular because of its high cross-polarization level compared with the longitudinal shunt slot.

There may be either one waveguide section or several waveguide sections in a linear-array design, depending on the required aperture length and frequency bandwidth. Conventionally, each waveguide section can be fed from one end or at the center as shown in Fig. 9-16. The number of slots in one waveguide section limits the frequency bandwidth in terms of input VSWR²⁶ and radiation pattern.

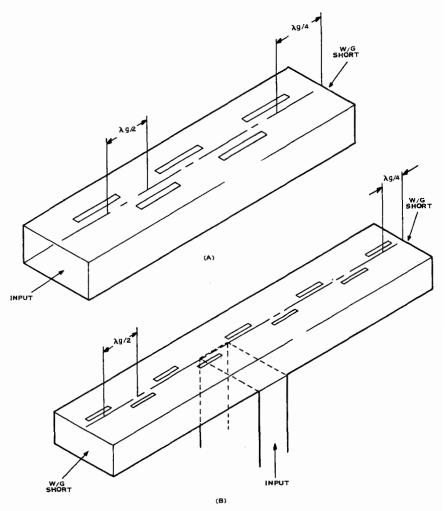


FIG. 9-16 Linear resonant slotted-waveguide arrays. (a) End feed. (b) Center feed.

To ensure that the input is perfectly matched at the center frequency and the aperture excitation is the desired illumination, the following are required:

- 1 The sum of all the normalized slot resonant conductances is equal to 1 for end feed but equal to 2 for center feed.
- 2 The slot resonant conductance is proportional to the radiating power required for a given slot location.

Mathematically, for an array of N slots we have

$$\sum_{n=1}^{N} g_n = W {(9-18)}$$

$$g_n = KA^2(n)$$
 $n = 1, 2, ... N$ (9-19)

where g_n is the normalized resonant conductance of the *n*th slot, A(n) is the given aperture voltage distribution at the *n*th-slot location, K is the normalization constant, and W equals 1 for end-fed arrays or 2 for center-fed arrays. Equations (9-18) and (9-19) can be solved for g_m and the design is completed by using either one of the design methods discussed previously to relate g_n with the physical slot geometry.

Planar Array

Physically, a planar array is constructed by placing several linear arrays side by side as shown in Fig. 9-17. A large planar array may consist of several subarrays, and each subarray may consist of several linear arrays. The element spacing d along the direction perpendicular to the waveguide axes is limited by the physical geometry and the radiation performance. In practical applications the element spacing for a longitudinal-shunt-slot array is defined by

$$a+t \le d \le \lambda \tag{9-20}$$

where λ is the free-space wavelength and a and t are the waveguide width and wall thickness respectively. Choosing $d < \lambda$ avoids the appearance of grating lobes in visible space. For an edge-wall slot array, a in Eq. (9-20) is replaced by the waveguide height b.

The resonant planar slot-array design procedure is similar to that for a resonant linear slot array except that an additional feed system is required to feed the radiation shunt-slot waveguide. Two types of slot-array antennas commonly used in planar array design are the longitudinal-shunt-slot array and the edge-shunt-slot array.

Longitudinal-Shunt-Slot Array This is the most popular slot-array antenna used in modern airborne radars. Two methods, (1) waveguide end feed and (2) series-slot central feed, have been used to feed the shunt-slot waveguides. In general, the series-slot center-feed system is a simpler and more compact design than the waveguide end feed for the same antenna size. Thus, the waveguide end feed is usually reserved for special-purpose applications such as one-dimensional electronic scan.

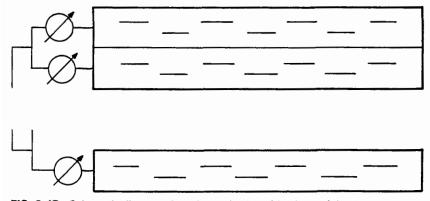


FIG. 9-17 Schematic diagram of an electronic steerable planar slot-antenna array.

Waveguide end feed Assume that the required aperture distribution A(m,n) is given, where m and n indicate the mth row and nth column in the array respectively. The aperture distribution along the direction perpendicular to the waveguide axes is achieved by the waveguide manifold design. The longitudinal-shunt-slot planar-array design is similar to the linear array except that g_n and A(n) in Eqs. (9-18) and (9-19) are replaced by $g_{m,n}$ and A(m,n) and computation of mutual-coupling effects is performed for a planar array. By using any one of the four methods described above, the desired radiation performance can be realized if the planar-array mutual-coupling effects are taken into account correctly. However, for a large array the active slot admittance technique requires excessive computing efforts, and the incremental conductance technique demands intensive experimentation to complete the design. The most convenient technique for designing a large array of longitudinal shunt slots is the equivalent self-admittance method, which will be detailed in the series-slot center-feed discussion.

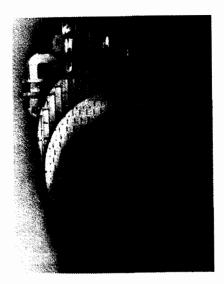


FIG. 9-18 Typical flat-plate antenna.

Again, it is assumed that the aperture distribution A(m,n) is given. The longitudinal-shunt-slot resonant-conductance design can be obtained by Eqs. (9-18) and (9-19). To achieve an accurate geometry design for a small array, the active slot admittance technique can be used.

self-admittance equivalent method is more convenient for designing a large array of longitudinal shunt slots. For simplicity, by considering the slots as stub waveguides located on the shunt waveguide axes, the infinite-array solution of open-ended waveguides can be used to compute the slot-aperture admittance. This computation yields the slotaperture admittance by taking into account approximate mutual-coupling effects (the alternating displacement of slots along the waveguide axes is neglected). By substituting the computed slot-aperture admittances for several slot

lengths into Eqs. (9-7) through (9-10) and using the simple interpolation technique, the resonant conductance and resonant length versus displacement design curves such as those shown in Figs. 9-9 and 9-10 can be easily computed. Note that this solution is valid for slots located in the array central region, and the edge effects in a large array may be neglected. Thus, by using these design curves and Eqs. (9-19) and (9-20), an array of longitudinal slots can be designed.

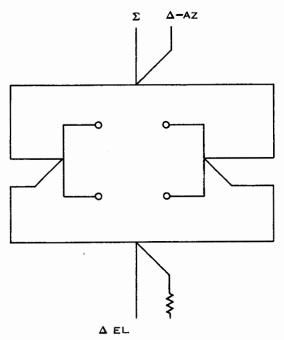


FIG. 9-19 Schematic diagram of a four-lobe monopulse comparator.

The next step in the planar-array design using the series-slot center feed is to design the series slots which feed the shunt waveguides. Before doing this, the system for feeding the waveguides which excite the series slots must be defined. Again, two feed techniques, the waveguide end feed and the E-plane T center feed, have been used by antenna designers. The E-plane T center feed yields a compact feed system with a shorter series waveguide run, but coupling between the junction and the directly coupled series slot is a problem. The waveguide end feed does not exhibit the distortion caused by coupling between the junction and the adjacent series slot.

After the series-slot feed has been chosen, the design is quite similar to the shuntslot design. By using the slot equivalent circuit and assuming that all the slots are at resonance, the series-slot resonant resistances in each series waveguide are determined by

$$\sum_{m=1}^{M} r_m = W {(9-21)}$$

$$r_m = K'B^2(m)$$
 $m = 1, 2, ... M$ (9-22)

where r_m is the normalized resonant resistance of the *m*th slot, *B* is the required series-slot excitation function, K' is the excitation normalization constant, and W = 1 for

end feed or W = 2 for center feed. B(m) is given in terms of aperture illumination A(m,n) by

$$B^{2}(m) = \sum_{n=1}^{N_{m}} A^{2}(m,n)$$
 (9-23)

where N_m is the number of shunt slots fed by the *m*th-series slot. Now, complete the series-slot design by solving Eqs. (9-21) through (9-23) for the resonant resistances and using the design curves of the slot resonant resistance and resonant length versus the inclination angle given in Figs. 9-14 and 9-15.

Edge-Wall Shunt-Slot Array The edge slot is cut into the narrow wall and wrapped around the broad walls of the rectangular waveguide. The slot length is determined by the depth cut into the broad wall. If a planar-array design using the edge slot is needed, the slot wrapped around into the broad wall can be a design and fabrication problem. Thus, planar slot-antenna arrays often use alternative approaches such as C or I slots to allow resonant slots on a planar surface.

There usually is no advantage for a planar slot-antenna array using edge-wall shunt slots. One of the few practical applications in a planar array is to achieve electronic scan in one direction when the required element spacing is too small for the longitudinal-shunt-slot design.

The edge-wall slotted waveguide fed from the center is not practical for the following reasons: (1) The shunt slot on the waveguide wall opposite the radiating shunt slot will introduce strong coupling effects and degrade antenna performance. (2) Analytical tools are not available for designing the coupling slot in this complicated geometry. Thus, the practical design uses the waveguide manifold to end-feed the slotted waveguides.

Since the analytical solution is not available for edge-wall shunt slots, the methods of active slot admittance and equivalent self-admittance used for the longitudinal slot are not applicable to design the slot geometry, and the incremental conductance method is used. Fortunately, the incremental conductance technique can be easily applied to this case since the strong mutual-coupling effects can be measured by a linear array of edge-wall slots. Also, the semiempirical admittance method can be applied in the same manner as in the case of linear-array antennas and is more efficient than the incremental conductance technique.

9-7 TRAVELING-WAVE SLOT-ARRAY DESIGN

The traveling-wave slot array differs from the resonant waveguide slot array in two ways: first, the resonant slots of the traveling-wave array are spaced by either more or less than one-half waveguide wavelength; and, second, the slotted waveguide is terminated by a matched load. As in the case of resonant waveguide slot arrays, resonant slots are used in traveling-wave arrays to maximize frequency-bandwidth performance.

Because slot spacing is close to one-half waveguide wavelength, adjacent longitudinal shunt slots are on opposite sides of the guide centerline, and adjacent edgewall shunt slots are inclined to opposite sides of the vertical centerline. The alternating

displacement or inclination with respect to the waveguide axis of successive slots may produce second-order beams. ^{27,28} If the main beam of the traveling-wave slotted array is pointing far away from broadside, the second-order beams may exceed the desired sidelobe level. The second-order beams can be effectively suppressed by choosing suitable element spacing. ^{27,28} The restrictions on element spacing given in these references can be relaxed when the element pattern is included in the computation.

The following are the basic characteristics common to all traveling-wave slotwaveguide-antenna arrays:

- 1 All slots in the array are resonant at the center frequency.
- 2 All slots in the same waveguide are spaced by either more or less than one-half waveguide wavelength from adjacent slots.
- 3 The beam pointing is off broadside and is frequency-dependent.
- 4 Matched loads are required to terminate the waveguides.
- 5 Array efficiency is less than unity.

The reflected wave from a termination with a VSWR greater than unity will produce a spurious beam scanned to the opposite side of the array normal from the main beam. Therefore, the reflected power from the termination must be kept sufficiently small so that the spurious beam is below the required sidelobe level.²⁹

Two types of traveling-wave slot-antenna arrays have been successfully designed: (1) a uniformly spaced array is used to produce a low-sidelobe pencil beam, and (2) a nonuniformly spaced array is applied to shaped-beam designs. Longitudinal shunt slots, edge-wall shunt slots, and rotational series slots can be used in both traveling-wave types.

Again, the complex aperture illumination of a traveling-wave slot-antenna array is assumed to be predetermined by aperture synthesis techniques. Consider first the design of a traveling-wave array of shunt slots. With reference to Fig. 9-20, the *i*th-slot normalized conductance related to its radiated power as derived by Stegen⁴ is

$$g_i = g_i^+ P_i / P_i^+$$
 (9-24)

$$P_i = P_{i+1}^{-} [e^{2\alpha \ell} i + 2|\Gamma_{i+1}|^2 \sin(2\alpha \ell_i)/(1 - |\Gamma_{i+1}|^2)]$$
 (9-25)

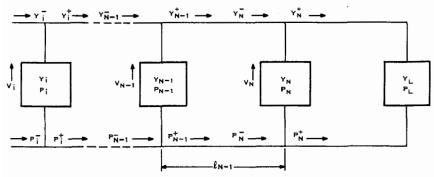


FIG. 9-20 Equivalent-network representation of a shunt-slot array.

The superscripts $^+$ and $^-$ indicate the quantity at the outgoing and incoming sides of the slot, $\gamma = \alpha + j\kappa$ is the complex propagation constant of the waveguide, ℓ_i is the interelement spacing, and Γ_i is the reflection coefficient at the *i*th element. By using the known aperture illumination, the design curves, Eqs. (9-24) and (9-25), and the transmission-line equation which relates the normalized admittances and element spacing,

 $y_{i}^{+} = g_{i}^{+} + jb_{i}^{+} = \frac{y_{i+1}^{-} \cos h\gamma \ell_{i} + \sinh \gamma \ell_{i}}{\cos h\gamma \ell_{i} + y_{i+1}^{-} \sinh \gamma \ell_{i}}$ (9-26)

where $y_i^- = y_i + y_i^+ |\Gamma_i| = |(1 - y_i)/(1 + y_i)|$ (9-27)

the slot conductances of a traveling-wave-antenna array of shunt slots can be specified. When the need for a traveling-wave array of series slots arises, Eqs. (9-24) through (9-27) are applicable, provided that the normalized admittance y is replaced by the normalized impedance z = r + jx. Other design procedures are similar to the ones used for the shunt-slot array design.

If the array aperture is sufficiently large so that each slot radiates only a small fraction of the incident power, a simplified method due to Dion²⁹ can be used to specify slot conductances or resistances. In this approximate method, both the waveguide losses and reflections from slots are neglected in the computation. Under this assumption

$$P_{i-1}^+ \approx P_i + P_i^+$$

This equation can be used to replace Eqs. (9-25) through (9-27) to design a traveling-wave array with a large number of slots.

Uniformly Spaced Traveling-Wave Slot-Array Design

A uniformly spaced traveling-wave slot array can be designed to produce a low-side-lobe pencil beam with larger bandwidth than that of the resonant waveguide slot array in terms of the array radiation pattern and input VSWR. If the reflections between elements are negligible, a constant phase difference between elements results in a progressive phase shift along the array aperture. The resulting phase front is inclined at an angle θ given by

$$\sin\theta = \lambda/\lambda_{\rm f} - \lambda/2\ell \tag{9-28}$$

where ℓ is the interelement spacing. In most traveling-wave slot-array designs, 2ℓ is chosen greater than λ_g and the beam moves in angle toward the load end as frequency is increased. For special situations such as limited aperture space, the array interelement spacing is chosen so that 2ℓ is less than λ_g and the beam moves in angle toward the feed end as the frequency is increased. Hence, the beam peak position of a traveling-wave array is frequency-dependent.

The nonresonant array achieves its large impedance bandwidth by virtue of the phase differences between the reflections from the various slots. The phase differences which arise from nonresonant spacing cause the resultant sum of all the reflected waves to be quite small. When the slot spacing is approaching one-half waveguide wavelength and the beam peak is very close to the broadside position, the input VSWR will increase rapidly as the slot admittances add in phase so that the input-impedance magnitude is much larger than unity. The matched load termination will absorb a

fraction of the input power. The amount of absorption is a function of the frequency and slot conductances and is usually chosen to be about 5 to 10 percent of the input power at midband.

The design procedure for determining the slot conductances and locations of a general uniformly spaced traveling-wave array using resonant shunt slots is summarized as follows:

- 1 Determine the proper interelement spacing by Eq. (9-28) and the beam-scanning range and set $y_N^+ = y_L = 1$.
- **2** Choose the appropriate percentage of power delivered to the load; that is, set P_N^+ (usually equal to 0.05).
- 3 By substituting these values and the predetermined percentage of power radiated by the Nth slot into Eq. (9-24), the resonant conductance of the slot closest to the load can be determined.
- **4** By using Eqs. (9-25) and (9-26), the incident power P_{N-1}^+ and the admittance termination of the second slot from the load y_{N-1}^+ are computed.
- 5 Repeat Steps 3 and 4 by replacing the subscript N by i until the resonant conductance of the slot nearest the feed is computed.

This design procedure is applicable to a general uniformly spaced series-slot array provided that the conductance and admittance are replaced by the resistance and impedance.

For a long array with many slots and negligible waveguide losses, the approximate method of Dion is applicable and the design is much simpler. In this approximate method, the nth-slot resonant conductance is given by

$$g_i = P_i / \left(1 - \sum_{n=1}^{i-1} P_n\right)$$
 (9-29)

where $\Sigma P_n = 1 - P_L$. Note that this approximate design is valid only if the largest slot resonant conductance g_{mx} satisfies the following relationship:

$$|g_{mx} \csc \kappa \ell| < 0.447 \tag{9-30}$$

Through the proper choice of P_L the resultant slot conductances can usually be made to satisfy the criterion of Eq. (9-30), although undesirably high power may be dissipated at the termination.

In general, there are many slots in a traveling-wave array. Therefore, the active admittance technique is not very efficient for determining the slot-array configuration, and the equivalent self-admittance and the semiempirical techniques discussed previously are more attractive. The incremental conductance technique using the design curve shown in Fig. 9-12 is applicable with reasonable accuracy. By using a traveling-wave array of series slots to feed a resonant planar array of longitudinal shunt slots, the slot configuration can be completed by the design curves shown in Figs. 9-14 and 9-15. The longitudinal-shunt-geometry design is the same as in the resonant slot-array design, provided that the progressive phase shift is taken into account in computing the mutual-coupling effects.

Nonuniform Traveling-Wave Slot-Array Design

Antenna arrays that produce shaped beams are desired for some special applications. The aperture illumination of a shaped beam requires, in general, both amplitude and phase variation across the aperture. Again, this complex aperture distribution is assumed to be determined by some aperture synthesis technique.²⁰ A slot-array antenna which produces a shaped beam can be easily designed by using a properly fabricated manifold to feed a group of linear slot arrays. These linear slot arrays can be designed by the methods discussed in connection with the planar slot-array design provided that the phase variation is included in the computation. The manifold is designed to account for the required aperture amplitude and phase variations.

There are some special applications, such as in air traffic control, for which the shaped beam is required to scan over a required sector. Also, occasionally a linear array producing a shaped beam is desired. In these situations, it is desirable to know whether and how a linear slot array can produce a desired shaped beam.

As seen from the above discussion, the aperture illumination amplitude can be controlled by the slot conductances. However, phase variation could be introduced either by varying slot reactance or by slot spacing. Variation in slot admittance gives only limited phase control and results in a narrow frequency bandwidth. A better method for varying the phase is the use of resonant slots and nonuniform interelement spacing. The resonant slot conductance or resistance controls the aperture illumination amplitude, while the nonuniform element spacing provides the required phase distribution across the aperture.

Assume that a complex aperture illumination of a nonuniformly spaced slottedwaveguide array is given by

$$A(v) = A(v) \exp [j\psi(v)]$$
 (9-31)

where A and ψ are the complex aperture illumination amplitude and phase and v is the spatial coordinate along the waveguide axis. To simplify the presentation, waveguide losses and reflection from the slots are assumed to be negligible. Under these assumptions, the illumination phase distribution can be achieved by recognizing that

$$\psi(v_n) = \pi[2v_n/\lambda_g \pm (n-N)] \tag{9-32}$$

where n signifies the nth slot and the choice of a + or a - sign depends on the phase taper reference. In general, a closed form for the slot locations cannot be derived from Eq. (9-32) for a general illumination phase function. Iterative techniques such as the design procedure listed below are required to determine the slot locations for a non-uniformly spaced slotted array.

Based on Eq. (9-32) and an iteration technique, a procedure for computing the slot locations of a nonuniformly spaced slotted array is practical:

- Normalize the given illumination phase function so that the phase at the slot nearest the load is zero. Using this normalization and Eq. (9-32) yields the coordinate reference $v_N = 0$.
- Set the nominal interelement spacing $\ell_i = \lambda/2$ for all i to compute the zero-order approximate values of slot locations.
- 3 By substituting the previously determined slot locations into the right-hand side of Eq. (9-32), the slot radiation phases are calculated.

- 4 Comparing these slot radiation phases with the desired illumination phase at these locations yields the incremental phase errors $\Delta \psi_n$.
- 5 The next-higher-order approximated slot locations can be obtained by

$$v_n^{(i)} = v_n^{(i+1)} + \Delta \psi_n \lambda_g / (2\pi)$$
 (9-33)

where the superscripts indicate the order of approximation.

6 Repeat Steps 3 through 5 until convergent slot locations are obtained.

The rate of convergence is quite rapid for the iterative procedure if the desired illumination phase function is a slowly varying function such as the phase function used in a cosecant-squared-beam synthesis. After the slot locations have been determined, the slot resonant conductances can be computed by Eq. (9-29) in the same manner as for the uniform traveling-wave array.

If the waveguide losses or the reflections from the slots are not negligible, Eq. (9-32) does not yield the correct radiation phase. In this circumstance, the transmission-line models of radiation phases and Eqs. (9-24) through (9-27) are required. The simple solutions obtained by neglecting the reflection from the slots and waveguide losses are employed as the first-order approximation in the iteration procedure. This iteration procedure is similar to the one based on Eq. (9-32), except that Eq. (9-32) is replaced by the transmission-line theory to compute the phases and Eq. (9-29) is replaced by Eqs. (9-24) through (9-27) to compute the slot resonant conductances. This general iteration procedure can be summarized as follows:

- 1 By substituting the previously determined slot locations and resonant conductances into transmission-line equations, the slot radiation phases can be computed.
- 2 By comparing these radiation phases with the desired illumination phases at these locations, the incremental phase errors $\Delta \psi_n$ are determined.
- 3 By substituting these incremental phase errors into Eq. (9-33), the approximate slot locations are calculated.
- 4 Compute the slot resonant conductances by Eqs. (9-24) through (9-27) by using the approximate slot locations, and repeat Steps 1 and 2 to obtain the new incremental phase errors.
- 5 By applying the linear interpolation or extrapolation to the two successive slot locations and incremental phase errors, the next-higher-order approximation of the slot locations is computed, and hence the slot resonant conductances.
- 6 Repeat Steps 1 through 5 until convergent results are obtained.

The slot geometry can be realized by the semiempirical method discussed above after the slot locations and resonant conductances have been determined. A compatible nonuniformly spaced dipole array solution, together with Eqs. (9-14) through (9-17), can be used to determine the slot configurations.

In general, if the nominal value of the unequal element spacing is larger than one-half free-space wavelength, higher sidelobes will appear in the region far off broadside. Therefore, it is recommended that nominal interelement spacing be less than one-half waveguide wavelength for the nonuniformly spaced slotted array.

9-8 POWER-HANDLING CAPABILITIES OF SLOTTED-WAVEGUIDE ARRAYS

Slotted-waveguide arrays are required to operate at high-power levels in many applications. In some cases the slot-antenna arrays can handle the high power without undue difficulty at sea-level atmospheric pressure, but they may fail to withstand the power at high altitudes where atmospheric pressure is much lower. When high-power capacity is required for an airborne antenna, the power-handling capability at the desired high altitude must be used in the designs.

The power-handling capacity of a slotted-waveguide array depends on both waveguide manifold design and slot design. Following the procedure established by Gould, 30 the waveguide manifold power-handling capability can be estimated with reasonable accuracy. As as example, consider a standard X-band RG52/U waveguide operating at a frequency of 9.375 GHz. On the basis of Gould's data, the continuous-wave power and the power of a 1-µs rectangular pulse versus the altitude are shown in Fig. 9-21. Observe that the maximum power level which can be handled by the waveguide decreases rapidly when the altitude increases and the waveguide pressure

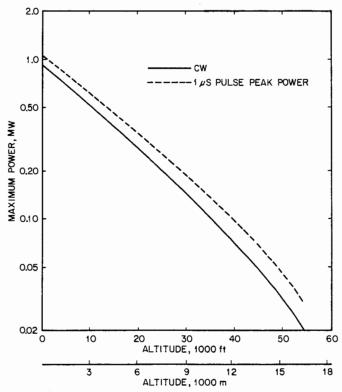


FIG. 9-21 Power-handling capacity of an RG52/U waveguide at 9.375 GHz.

follows the altitude pressure. Also note that these results apply to room temperature for a perfectly matched waveguide section. If this is not the case, the pressure at other temperature ρ is required for computing the maximum power level where

$$\rho = \rho_0(293/T) \tag{9-34}$$

T is the absolute temperature (degrees Kelvin), and ρ_0 is the pressure at room temperature.

The electric field strength E across the slot aperture for a given slot-radiated power P is needed to compute the slot power-handling capacity. By using Eq. (9-14), the electric field strength across the slot aperture is approximated by

$$E = (\eta_0/b')\sqrt{P/2R}$$
 (9-35)

where R is the complementary dipole driving-point resistance. The baseline slot at 9.375 GHz is used to illustrate the slot power-handling capability. By combining Gould's results³⁰ with Eq. (9-35), the maximum continuous-wave and peak power versus the altitude for the baseline slot is computed and shown in Fig. 9-22. Equation (9-34) should be used for a temperature other than room temperature.

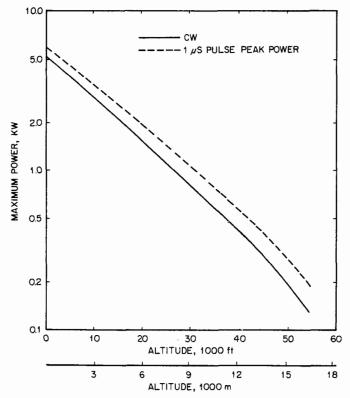


FIG. 9-22 Power-handling capacity of the baseline slot in the planar array.

Techniques which can be used to increase power-handling capability are as follows:

- 1 Avoid capacitive windows and sharp corners in the waveguide manifold.
- 2 Increase the slot width.
- 3 Cool and pressurize the antenna system.

The most effective technique for increasing power-handling capability is pressurization.³¹ If a slot-antenna array is wholly encapsulated in a pressurized housing, the increase in power-handling capability is proportional to the achievable pressure. Occasionally, freon is used for pressurization, further increasing power-handling capability through the higher dielectric strength of this substance. This technique adds to the complexity of the mechanical design and fabrication of the antenna.

Alternatively, instead of using a fully pressurized housing, the antenna can be partially pressurized in only those areas where power levels are highest. This can be achieved by using pressure windows in the waveguides or dielectric covers on the slots. Dielectric covers, when used, must be taken into account in slot design. For a large array of longitudinal shunt slots, a dielectric cover can easily be included in the computation of the slot-aperture admittance by the infinite array of rectangular waveguides.

9-9 TOLERANCE AND FABRICATION TECHNIQUES

In practice, an antenna will include errors introduced by inaccuracies in the manufacturing process since high precision in manufacturing generally increases antenna costs. Thus, a systematic allocation of dimensional tolerances is usually a worthwhile part of a design.

The tolerance for waveguide width can be established easily by computing the incremental phase per unit change in the manifold and feed waveguide width. To determine the required dimensional tolerance for slots, the incremental conductance (or impedance) per unit change in the slot length from the resonant length is needed. These incremental values per unit change of slot parameters can be determined from given slot parameters discussed in preceding sections. Listed in Table 9-1 are the incremental phases of baseline shunt and series slots and the S-band edge slot due to the decrease of 1 percent slot length from resonant lengths. Note that the tolerance requirement for edge-slot arrays is less critical than for other slot arrays.

TABLE 9-1 Slot Incremental Phase Change with 1 Percent Change in Slot Length from Resonant Length

Longitudinal shunt slot		Rotational	Edge slot	
Single	Coupled	series slot	Coupled	
8.1	19.3°	17.1*	2.7*	

The difference in the incremental phase change indicates that the mutual-coupling effects reduce the longitudinal shunt-slot frequency-bandwidth performance and increase tolerance requirements. Sidelobe performance can be greatly degraded by a 1 percent variation in the slot length in a planar array of longitudinal shunt slots.

Fabrication of the commonly used edge-slot array is quite different from that of other slot arrays. Since the edge slot is cut into the narrow wall and wrapped around the broad faces of a rectangular waveguide, an edge-slot array can be easily fabricated by cutting (sawing) the slots at the proper angle and depth. The results are, in general, quite good. To generate a planar edge-slot array, slotted-waveguide sections are manifolded and assembled side by side to form a planar aperture.

To fabricate a planar array of longitudinal shunt slots or edge-wall folded shunt slots, a milling machine may be used to cut the slot on a thin, flat plate (face plate) such as shown in Fig. 9-18. The back plate is milled out of a thick metal plate. Two narrow walls of the shunt and series waveguides are fabricated on the opposite sides of the metal plate, and the series slots are cut on the common walls of the shunt and series guides. The shunt waveguides are formed by assembling the back plate to the face plate, and the series waveguides by securing the feed covers on the back plate.

Basically, there are three techniques for assembling the face plate to the back plate array of broad-wall slots:

- 1 Welding Both laser welding and electron-beam welding can be used to join the face plate to the back plate. Electron-beam welding has been successfully applied to manufacture antennas made of magnesium. Because of the inherent properties of aluminum, applying the electron-beam welding technique to this metal in assembling the flat-plate antenna requires additional investigative effort. Laser welding of the face plate to the back plate is possible, but the process is better suited to welding very thin metal cross sections and has limited application to flat-plate antennas.
- 2 Brazing Dip brazing has been widely used to secure two aluminum objects together. Many aluminum slotted-waveguide arrays are assembled by using dip brazing. The disadvantages of this technique are that the residue deposits left in the waveguides and on the slots and the overall material shrinkage must be accounted for. The fluxless-brazing technique for joining the aluminum face and back plates together in a retort with inert atmosphere has been investigated with successful results.³²
- 3 Bonding There are three commonly used bonding techniques: (a) thin-film bonding, (b) conductive-epoxy bonding, and (c) diffusion bonding. Thin-film bonding and conductive-epoxy bonding are quite popular in flat-plate-antenna applications.

Other miscellaneous techniques such as screw fasteners and twist tabs have been employed to join the face and back plates together. These two methods are either limited as to application or less accurate, adversely affecting antenna performance when compared with the above three assembling techniques.

The linear array is subjected to fewer tolerance and assembly problems than the planar array. To fabricate and assemble a planar array such as the flat-plate antenna, both before and after the process of joining the face and back plates together, attention must be paid to keep the antenna aperture flat and the plates aligned accurately. A 1

percent free-space wavelength warpage of an antenna can significantly degrade side-lobe performance, and an 0.7 percent misalignment of the free-space wavelength of the front and back plates will produce a grating-lobe level higher than $-20~\mathrm{dB}$. Slotlength tolerance depends on the desired radiation performance.

Although a slot-antenna array can be designed and fabricated by using the design information given in this chapter, antenna performance may be less than expected. Some of the second-order effects, such as the slot alternating displacements, alternating inclined angles, edge effects, nonuniform aperture illumination, slot-length errors, and internal coupling through higher-order waveguide modes have not been addressed. The combined effects of neglecting second-order effects, manufacturing tolerances, and inaccurate manifold design usually significantly degrade practical slotted-array performance. For instance, a -35-dB-sidelobe-level array design may have only -28-dB sidelobes in practice. Thus, a thorough error analysis is recommended to define dimensional tolerances and to determine aperture illumination errors. Normally, overdesign is used to allow for design and manufacturing deficiencies, the degree of overdesign usually being determined by experience. Note that some of the degradation factors will be more noticeable for a -30-dB-sidelobe-level array design than for a -20-dB design.

9-10 RECENT DEVELOPMENTS

Method-of-moments (MOM) analysis of slotted-waveguide antennas progressed rapidly during the past decade. Applications include the characterization of broad-wall longitudinal slots, edge-wall inclined slots, ³³ I-slots, ^{18b} and ridge-waveguide-fed slots. ¹ Single slot characterizations are easily extended to finite-array solutions.

Broad-Wall Longitudinal Slots

Stern and Elliott^{6a} investigated the resonant characteristics of broad-wall longitudinal slots using the MOM formulation. They found that the single-shunt lump-circuit representation for a longitudinal slot is valid only if the slot offset is not too large and the waveguide height is greater than one-tenth of a wavelength.

Based on the sinusoidal representation of the slot aperture field near the first resonance, Elliott³⁴ improved the small-array design technique to include dielectric-filled slots. An array of magnetic currents derived from the sinusoidal-slot aperture fields replaces the dipole-array solution in the original formulation to account for the external mutual-coupling effects. The internal field formulation is modified accordingly.

The global basis functions in the MOM formulation of a finite array of longitudinal slots yields accurate results in comparison with measured data. The single lumped admittance representation of the slots in the MOM solution verifies that the infinite-array solutions shown in Figs. 9-9 through 9-11 are accurate for a finite array as small as 25 elements. Figure 9-23 shows the comparison of longitudinal-slot resonant conductances and resonant lengths computed by infinite-array approximation and the finite-array MOM results. The nominal array element spacing is 0.71 wavelength in a square lattice. The finite-array results apply to uniform square arrays of N by N elements. Thus infinite-array equivalent admittances yield practical large slotted-waveguide arrays designs.

Narrow-Wall Slots

To account for the external field in the inclined-slot analysis, Jan et al.³³ modified the 90° wedge Green's function to approximate the thick-edge-wall Green's function. They used the point-matching technique in the MOM formulation of the inclined narrow-wall slots. The point-matching-technique formulation for the waveguide field usually results in a divergent series for inclined slots. Nevertheless, their computed results of single slots agree with the experimental data shown in Figs. 9-12 and 9-13 and follow the same trend as computed by Eq. (9-12).

Employing the Galerkin's method in the MOM formulation, Yee and Stellitano^{18b} obtained an MOM solution for symmetric edge-wall I-slots on an infinite ground plane. They analyze each I-slot as three rectilinear slots tied together and use sinusoidal basis functions in each rectilinear slot. In contrast to adding a set of junction basis functions, it takes advantage of the natural solution to determine the field in the overlapped regions. The computed and measured results show that (1) the I-slot can be approximately represented by a shunt admittance with an additional shunt capacitive load, (2) the cross-polar-

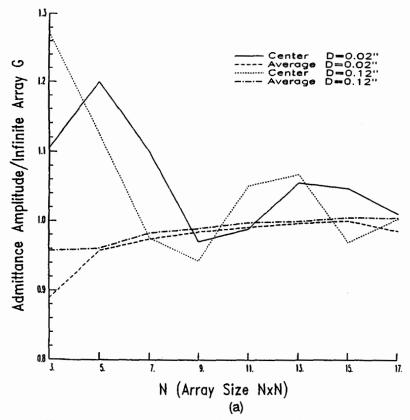
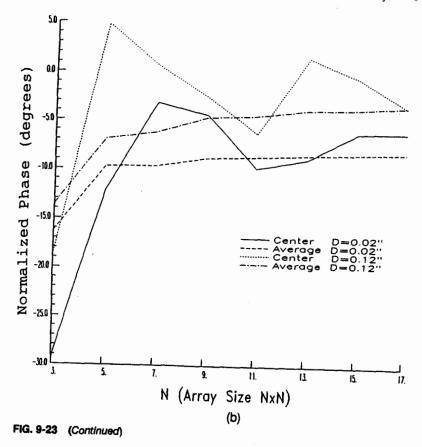


FIG. 9-23 Slot admittances computed by finite array of $N \times N$ elements normalized by infinite array results. (a) Admittance amplitude. (b) Admittance phase.



ization of an I-slot is about the same as other edge-wall slots (inclined slot, C-slot, etc.), and (3) the I-slot produces a sufficiently large dynamic range of radiated power for practical array design through changing the cross-branch offset.

Ridge-Waveguide-Fed Longitudinal Slots

Single-plane wide-angle scanned phased arrays often employ ridge-waveguide-fed slots because of the small ridge-waveguide spacing. Before Falk¹ formulated the MOM solution for a ridge-guide slot, the design of these arrays relied entirely on empirical method. A preferred approach for the design of these arrays utilizes the semiempirical technique as discussed in Sec. 9-5. Replacing the factor U in Eq. (9-16) by the computed characteristics of the isolated slot, one follows the procedure described previously to determine the slot-array configuration including the mutual-coupling effects. A similar technique also allows the performance analysis of this array. Without the analytical tools, a patient designer can use experimental techniques to design a planar array of ridge-waveguide-fed slots such as shown by Green et al.³⁵

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Leaky-Wave Antennas

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10-1 Introduction 10-2 General Principles 10-2 Two Types of Leaky-Wave Antennas: Uniform and Periodic 10-4 Relation to Surface-Wave Antennas and Slot Arrays 10-5 10-2 Design Principles for Uniform Leaky-Wave Antennas 10-7 Beam Direction, Beamwidth, and Radiation Efficiency 10-7 Scan-Angle Behavior 10-8 Radiation Pattern 10-10 Control of Aperture Distribution to Reduce Sidelobes 10-10 10-3 Design Principles for Periodic Leaky-Wave Antennas 10-13 Effect of Periodicity on Scan Behavior 10-13 Beam Direction, Beamwidth, and Radiation Efficiency 10-14 Feed Considerations 10-15 10-4 Specific Structures: Overview 10-15 Specific Structures Based on Closed

Waveguides 10-17

Long Slits in Rectangular

Waveguide 10-18

Long Slits in Circular Waveguide 10-20 Closely Spaced Holes or Slots in Rectangular Waveguide 10-20 Array of Closely Spaced Wide Transverse Strips 10-22 Planar Structures 10-24 10-6 Specific Structures Based on Periodic Open Waveguides 10-25 Early Structures 10-25 Periodic Dielectric Waveguides 10-26 Design Theory for Wide Periodic Dielectric Antennas 10-28 Design Theory for Narrow Periodic Dielectric Antennas 10-30 Periodic Leaky-Wave Antennas Based on Microstrip Line 10-30 Periodic Arrays of Microstrip Patches or Dielectric Resonators Fed by Open Dielectric Waveguides 10-32 10-7 Specific Structures Based on Uniform

Open Waveguides 10-33

Trough Waveguide

Antenna 10-33

Early Structure: Asymmetrical

Foreshortened-Top NRD Guide Antenna 10-35 Asymmetrical NRD Guide Antenna 10-38 Some Antennas Based on Groove Guide 10-39 Stub-Loaded Rectangular Waveguide Antenna 10-41 Printed-Circuit Version of Stub-Loaded Rectangular Waveguide Antenna 10-44 Asymmetrical Slitted Ridge Waveguide Antennas 10-49 10-8 Arrays That Scan in Two
Dimensions 10-50
Principle of Operation 10-50
Analytical Approach 10-51
Array of Asymmetrical NRD
Guide Line Sources 10-52
Array of Printed-Circuit Uniform
Line Sources 10-53
Array of Printed-Circuit Periodic
Line Sources 10-54

10-1 INTRODUCTION

General Principles

A leaky-wave antenna is basically a waveguiding structure that possesses a mechanism that permits it to leak power all along its length. The earliest example of such an antenna is a rectangular waveguide with a continuous slit cut along its side, 1,2 as shown in Fig. 10-1. Since leakage occurs over the length of the slit in the waveguiding structure, the whole length constitutes the antenna's effective aperture unless the leakage rate is so great that the power has effectively leaked away before reaching the end of the slit. Because of the leakage, the leaky waveguide has a complex propagation wave number, with a phase constant β and a leakage constant α ; α is large or small depending on whether the leakage per unit length is large or small. A large α implies that the large leakage rate produces a short effective aperture, so that the radiated beam has a large beamwidth. Conversely, a low value of α results in a long effective aperture and a narrow beam, provided the physical aperture is sufficiently long.

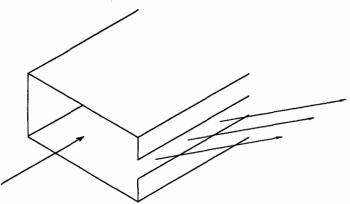


FIG. 10-1 The earliest example of a leaky-wave antenna: a rectangular waveguide with a continuous slit cut along one of its sides.

When the antenna aperture is finite and fixed beforehand and the leakage rate α is small, the beamwidth is determined primarily by the fixed aperture, and the value of α influences the beamwidth only secondarily. What is affected strongly by the value of α under those conditions is the efficiency of radiation. One tries to design a leaky-wave antenna so that its value of α allows about 90 percent of the power in the guide to be leaked away (radiated) by the time the wave reaches the end of the antenna aperture. The remaining power is absorbed by a matched load placed at the end of the waveguide. A typical leaky-wave antenna might be about 20 wavelengths long, so that the beamwidth of the radiation would be about 4° or so if the beam direction is about 45° from the leaky waveguide axis.

Because the phase constant β changes with frequency, the beam direction also changes with frequency, and the leaky-wave antenna can be *scanned* by varying the *frequency*. The precise ways in which changes in frequency affect the various properties of leaky-wave antennas are considered in detail later.

Since power is radiated continuously along the length, the aperture field of a leaky-wave antenna with strictly uniform geometry has an exponential decay (usually slow), so that the sidelobe behavior is poor. The practice is then to vary the value of α slowly along the length in a specified way while maintaining β constant, so as to adjust the amplitude of the aperture distribution to yield the desired sidelobe performance. This tapering procedure is well known and is discussed later.

An individual leaky-wave antenna is clearly a line-source antenna; the design produces the desired beam behavior (usually a narrow beam) in the scan plane, but the radiation pattern in the cross-plane is just a fan beam whose detailed beam shape depends on the cross-sectional dimensions of the leaky-wave antenna. Techniques are available for narrowing the beam in the cross-plane, such as the use of a horn or placing the line-source antenna in an array. Examples are given later.

As indicated above, the radiated beam of the leaky-wave antenna may be frequency scanned, producing a fan beam narrow in the scan plane. Recent studies have employed a linear array of such leaky-wave line sources to produce a pencil beam and to permit independent scanning in two dimensions. The scanning in the cross-plane requires some mechanism other than a change in frequency, however, and phase scanning seems best. Examples of antennas that scan in two dimensions are presented at the end of this chapter.

Leaky-wave antennas have been known and used for more than 30 years. Almost all the early antennas were based on closed waveguides which were made leaky by introducing a cut along the side of the waveguide (or something similar to that) to permit the power to leak away along the length of the waveguide. The newer millimeter-wave waveguides are actually already open, often in order to reduce the attenuation constants of such waveguides due to metal or dielectric losses. Examples are various kinds of dielectric waveguide, groove guide, NRD guide, microstrip line, etc.; of course, some of these guides are less lossy than others. The dominant modes on these open waveguides are generally purely bound, but a physical cut will not make them leak; instead, some new techniques are necessary, such as the introduction of asymmetry or some other modification of the geometry. Several examples are presented later.

The last remarks in this subsection relate to some confusion in the literature regarding the physics of leaky waves. The limited space available here will permit only a few words of explanation, but an examination of the wave numbers shows that the amplitude of a forward leaky wave increases transversely away from guiding structure so that the wave violates the boundary condition at infinity in the transverse direction. Leaky waves have therefore been called "improper" or "nonspectral." Although all this is true, these

features of leaky waves do not complicate the design of leaky-wave antennas; the design principles, which are presented below, are actually quite simple and straightforward. Some simple considerations show that the leaky wave is actually defined only in a sector of space near the leaky-wave antenna and never reaches infinity in the transverse direction because the antenna itself is finite. The leaky-wave concept serves to provide the details of the aperture distribution and some of the main properties of the beam, but the radiation field itself is found in the usual fashion as the Fourier transform of the aperture field. There are some sophisticated mathematical aspects regarding the improper (nonspectral) nature of leaky waves, 3-5 but some of the considerations referred to above can be explained in simple geometric terms.²

Two Types of Leaky-Wave Antennas: Uniform and Periodic

There are two different basic types of leaky-wave antennas, depending on whether the geometry of the guiding structure is uniform or is periodically modulated along its length. These two types are actually similar in principle to each other, but their performance properties differ in several ways and they face somewhat different problems in their designs. The two types are therefore treated separately in the discussions that follow.

The first type, the uniform leaky-wave antenna, is uniform along the length of the guiding structure, as opposed to possessing some periodic modulation. (As mentioned above, we recognize that the uniform leaky-wave antenna has a small taper along its length in order to improve and control the sidelobe level.)

All leaky-wave line sources of the uniform type radiate into the forward quadrant and can scan in principle from broadside to end fire, with the beam nearer to end fire at the higher frequencies. In practice, however, one cannot get too close to end fire or to broadside, but how near those limits can be approached depends on the specific structure. For example, suppose the cross section of the guiding structure contains dielectric material in part and air in part, and has a slow-wave range $(\beta > k_0)$ and a fast-wave range $(\beta < k_0)$, where k_0 is the free-space wave number in air. Then, the transition between the two ranges is usually a rapid one, occurring at end fire (when $\beta = k_0$), and the beam can be scanned very close to end fire. An additional virtue of this structure is that a wide scan-angle range can usually be covered with only a relatively small frequency range. An example is given later. When the structure is filled with air only, on the other hand, one must stay about 10 or 15° away from both broadside and end fire, and the frequency sensitivity is more sluggish, particularly near end fire. An important virtue possessed by such single-medium leaky-wave antennas, however, is that the beamwidth remains exactly constant as the beam is scanned with frequency.

In the second type of leaky-wave antenna, the periodic type, some periodic modulation of the guiding structure is introduced, and it is this periodicity that produces the leakage. The periodic modulation itself is uniform along the structure's length, again except for the small taper of the periodic properties along the length to control the sidelobes. Again, a complex propagation wave number results, with β and α ; large or small values of α are related to the beamwidth and the radiation efficiency in the same manner as that found for uniform leaky-wave antennas. A typical example of a periodic leaky-wave antenna is a dielectric rectangular rod on which a periodic array of metal strips is placed, as seen in Fig. 10-2.

An important difference between uniform and periodic leaky-wave antennas is that the dominant mode on the former is a fast wave that therefore radiates whenever the structure is open. On the other hand, the dominant mode on a periodic leaky-wave antenna is a slow wave that does not radiate even though the structure is open. Introduc-

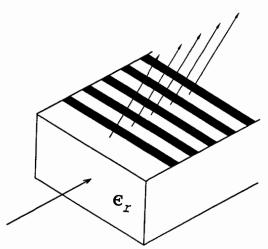


FIG. 10-2 A typical and important example of a periodic leaky-wave antenna: a rectangular dielectric rod (which may or may not be situated on a metal plane) on which is placed a periodic array of metal strips. This antenna can radiate into either the forward or backward quadrants.

tion of the periodic array produces an infinity of space harmonics, some of which may be fast while the rest are slow; the fast space harmonics would radiate. Since one desires an antenna that radiates only a single beam, the structure is designed so that only the first space harmonic (n=-1) is fast. The relevant design considerations are presented in Sec. 10-3. It is also shown there that the scan range for this class of antennas is from backward end fire through broadside into part of the forward quadrant, except for a narrow region around broadside, where an "open stop band" occurs.

In general terms, therefore, we see that the scan range is completely different from that for the uniform leaky-wave antennas. There the beam scans in the forward quadrant only; also, it cannot approach broadside too closely, and sometimes it cannot be used too near to end fire. For the periodic leaky-wave antenna, one can scan over almost all the backward quadrant and into some of the forward quadrant as well.

Relation to Surface-Wave Antennas and Slot Arrays

Surface-wave antennas, leaky-wave antennas, and slot arrays are all members of the family of traveling-wave antennas, yet they are treated in this *Handbook* in separate chapters (Chaps. 12, 10, and 9, respectively). They are similar to each other in some evident respects (e.g., the basic structure in each case is a waveguide of some sort), but they all differ from each other in important ways that lead to different design procedures and to different performance expectations.

Surface-wave antennas are purely end-fire antennas, whereas leaky-wave antennas and slot arrays do not radiate well in the end-fire direction and, in fact, are designed either to radiate in some other direction or to scan over a range of angles. The basic guiding structure for surface-wave antennas is an open waveguide (such as a dielectric rod) whose

dominant mode (the surface wave) is purely bound, so that the surface wave will radiate only at discontinuities, such as the very end of the waveguide. It does not radiate along the length of the guide because the surface wave is a slow wave (except for some small leakage into the almost-end-fire direction if the surface-wave antenna is tapered), whereas a uniform leaky-wave antenna, which supports a fast wave, leaks power all along the length of the waveguide.

Periodic leaky-wave antennas, however, are often based on surface waveguides. There the basic waveguide can be an open structure whose dominant mode is a surface wave that is a slow wave, and the radiation is produced by placing a periodic array of discontinuities on the guide in such a way that the first space harmonic becomes fast. The resulting leaky wave may therefore be viewed as arising from a surface-wave-excited array. There is thus a strong kinship between the basic structures employed for surface-wave antennas and those for periodic leaky-wave (or surface-wave-excited) arrays, and, for this reason, periodic leaky-wave antennas were, in the first two editions of this Handbook, included within the same chapter as surface-wave antennas. On the other hand, since the performance properties of periodic leaky-wave antennas, and the design procedures to achieve those properties, are very different from those for surface-wave antennas of both types are currently incorporated into the present chapter.

The differences between *periodic* leaky-wave antennas and *slot arrays* are more subtle but still very significant. A visually evident difference is that most slot arrays are fed from air-filled rectangular waveguides whose dominant mode is fast; in order to suppress the radiation from this fast dominant (n = 0) space harmonic while retaining that from the n = -1 space harmonic, it is necessary to place successive slots on alternate sides of the guide centerline or to alternately tilt the slots to produce phase reversals. Periodic leaky-wave antennas do not need such phase reversals because the (slow) n = 0 space harmonic does not radiate. However, this distinction is *not* fundamental, as may be noted when the slot-array rectangular waveguide is dielectric-filled and the alternation of slots is no longer needed. The structures then resemble each other in principle.

The basic distinction between periodic leaky-wave antennas and slot arrays lies in the nature of the individual discontinuities, and, therefore, in the basic design approaches. The intention in the leaky-wave antennas is to produce a slow leakage per unit length; thus each discontinuity element in the periodic array of elements produces a small loading on the basic waveguide mode. The individual elements are intentionally made nonresonant. As a result, the design procedure views the leaky-wave antenna as an equivalent "smooth" structure with a complex propagation wave number, where the array of discontinuity elements is considered as a whole in the analysis.

In contrast, the slots in a slot array are considered *individually*, and then mutual coupling effects are taken into account when the array itself is formed. Furthermore, the individual slots are usually *resonant*. Variations in the loading on the basic waveguide mode are achieved by rotating the slots or by moving them closer to the guide centerline. The design approach thus becomes quite different from that for leaky-wave antennas, thereby warranting inclusion in a separate chapter.

The resonant loading in slot arrays, as opposed to the nonresonant loading in periodic leaky-wave antennas, also influences performance. For example, slot arrays are more frequency-dependent, which can be good if one wishes to scan more rapidly with frequency, but the tradeoff is that the scan range is narrowed. Most slot arrays are not intended for a large scan range, however. On the other hand, if slot arrays are built with nonresonant slots, their behavior would be very similar to that of periodic leaky-wave

antennas. The question then would be whether the customary slot-array design or the leaky-wave design would be more suitable. One last observation relates to the fact that the treatment in Chap. 9 is restricted to slot arrays fed by rectangular waveguide. The design approach described for such arrays could be applied equally well to arrays of other resonant elements, e.g., the two-wire line with proximity-coupled dipoles.⁶

10-2 DESIGN PRINCIPLES FOR UNIFORM LEAKY-WAVE ANTENNAS

The physical structure of a leaky-wave antenna consists of a leaky waveguide with a length L along which the leakage occurs. The propagation characteristics of the leaky mode in the longitudinal (z) direction are given by phase constant β and leakage constant α , where α is a measure of the power leaked (and therefore radiated) per unit length. The length L then forms the aperture of the line-source antenna, and the amplitude and phase of the traveling wave along the aperture are determined by the values of β and α as a function of z. When the leaky waveguide is completely uniform along its length, β and α do not change with z, and the aperture distribution has an exponential amplitude variation and a constant phase. Such an aperture distribution results in a high sidelobe level, so that the design of a practical leaky-wave antenna will include a variation of α with z in order to control the sidelobes in some specified fashion. More is said about this later in this section.

The values of β and α will depend on the precise cross-sectional geometry of the leaky waveguide, and the determination of β and α , whether theoretically or experimentally, is in most cases the most difficult part of the design. Their knowledge, however, is essential to any systematic design procedure.

Once β and α are known as a function of frequency and cross-sectional geometry, the principal behavioral features of a leaky-wave antenna follow very quickly. Such features include the beam direction, the beamwidth, the radiation efficiency, the variation of the scan angle with frequency, and the taper in α required to control the sidelobes.

Beam Direction, Beamwidth, and Radiation Efficiency

These major behavioral features follow directly once the values of β and α are known, and they are given to a good approximation by a set of very simple relations. We first consider the beam direction and the beamwidth:

$$\sin \theta_m \approx \frac{\beta}{k_0} \tag{10-1}$$

$$\Delta\theta \approx \frac{1}{(L/\lambda_0)\cos\theta_m} \tag{10-2}$$

Here θ_m is the angle of the maximum of the beam, measured from the broadside direction (perpendicular to the leaky waveguide axis), L is the length of the leaky-wave antenna, $\Delta\theta$ is the beamwidth, and k_0 is the free-space wave number (= $2\pi/\lambda_0$). Both θ_m and $\Delta\theta$ are in radians in Eqs. (10-1) and (10-2). The beamwidth $\Delta\theta$ is determined primarily by the antenna length L, but it is also influenced by the aperture field amplitude distribution. It is narrowest for a constant aperture field and wider for sharply peaked distributions. Equation (10-2) is a middle-of-the-range result. For a constant aperture distribution, the unity factor in the numerator should be replaced by 0.88; for a leaky-

wave structure that is maintained uniform along its length, consistent with 90 percent radiation, the factor should be 0.91; for a tapered distribution that is sharply peaked, the factor could be 1.25 or more (see Table 2-1 for examples).

The antenna length L is usually selected, for a given value of α , so that 90 percent (or at most 95 percent) of the power is radiated, with the remaining 10 percent or so absorbed by a matched load. Attempting to radiate more than 90 percent or so creates two problems: First, the antenna must be made longer, and second, the variation in $\alpha(z)$ required to control the sidelobes becomes extreme. For 90 percent of the power radiated, we find

$$\frac{L}{\lambda_0} \approx \frac{0.18}{\alpha/k_0} \tag{10-3}$$

This simple but useful relation follows from writing

$$\frac{P(L)}{P(0)} = \exp(-2\alpha L) = \exp[-4\pi(\alpha/k_0)(L/\lambda_0)]$$
 (10-4)

where P(L) is the power remaining in the leaky mode at z = L and P(0) is the power input at z = 0.

If both L and α are specified independently, the percentage of power radiated can deviate significantly from the desired 90 percent. In fact, α is a function of frequency, so that the radiation efficiency will change somewhat as the beam is frequency scanned. The 90 percent figure is usually applied to the middle of the scan range. Using Eq. (10-4), however, one can easily obtain an expression for the percentage of power radiated:

Percentage of power radiated =
$$100[1 - P(L)/P(0)]$$

= $100\{1 - \exp[-4\pi(\alpha/k_0)(L/\lambda_0)]\}$ (10-5)

Equation (10-5) assumes an exponentially decaying aperture distribution. If the aperture distribution has been changed in order to control sidelobes, as is customary, Eq. (10-5) is still useful as a good approximation.

Scan-Angle Behavior

There are two different types of uniform leaky-wave antennas that are similar in principle but that differ somewhat in their scan-angle behavior. The guiding structures for these two types differ in that they are air-filled for one type and partially dielectric-filled for the other.

Typical air-filled guiding structures would include open rectangular waveguide and groove guide, for which the dominant modes are fast relative to the free-space velocity. Guiding structures that are partially dielectric-filled include nonradiative dielectric (NRD) guide and open dielectric-loaded rectangular waveguide. Depending on the frequency and the geometry, the dominant modes on these guiding structures can be fast or slow, but when they are used as leaky-wave antennas, it is necessary to operate them in the fast-wave range ($\beta/k_0 < 1$), of course.

There are advantages and disadvantages in performance when the guiding structures are air-filled or when they are partially loaded with dielectric. With respect to the variation of beamwidth with scan angle, the air-filled structures are superior. Because the transverse wave number is then a constant, independent of frequency, the beamwidth of the radiation remains exactly constant as the beam is scanned by varying the frequency. With partial dielectric loading, on the other hand, the beamwidth changes with scan angle. With respect to frequency sensitivity, i.e., how quickly the beam angle scans as the frequency is

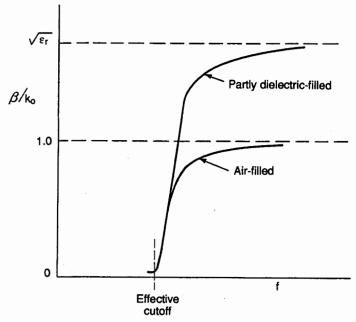


FIG. 10-3 The variations of the normalized wave number β/k_0 with frequency for uniform leaky-wave antennas that are air-filled or are partly filled with dielectric material. These variations explain their different scan-angle behaviors.

varied, the partly dielectric-loaded structure can scan over a larger range of angles for the same frequency change and is therefore preferred.

The reason for these differences in behavior between the air-filled and partly dielectric-loaded cases is shown in Fig. 10-3. Let us first recall a few features. We begin with Eq. (10-1), where θ_m is the angle of the maximum of the beam, measured from broadside. Then we note that the line $\beta/k_0 = 1$ corresponds to end fire, and $\beta/k_0 = 0$ corresponds to broadside. The β/k_0 variation near to cutoff (near to broadside) is seen to be much the same whatever the filling factor of the guiding structure. The big difference occurs near end fire. The variation with frequency for the air-filled case is seen to be quite slow near the $\beta/k_0 = 1$ line because the curve asymptotically approaches that line as the frequency becomes large. For the partly dielectric-filled case, on the other hand, the curve goes quite rapidly to the $\beta/k_0 = 1$ line and above it. As a result, the variation of scan angle with frequency is more rapid overall for the partly dielectric-filled case, and one can approach end fire rather closely in the scan-angle range. In contrast, one cannot approach end fire closely when the guiding structure is air-filled.

It was indicated above that for air-filled guiding structures the beamwidth $\Delta\theta$ remains constant as the beam is scanned by varying the frequency. This statement is easily proved once we recall that for such air-filled structures the transverse wave number k_t is a constant (k_c) independent of frequency. Using Eq. (10-1), we find

$$\cos^2 \theta_m = 1 - \sin^2 \theta_m = 1 - (\beta/k_0)^2$$

Then, since

$$k_0^2 = \beta^2 + k_c^2$$

for air-filled guiding structures, we may write

$$1 - (\beta/k_0)^2 = 1 - [1 - (k_c/k_0)^2] = (k_c/k_0)^2$$

so that

$$\cos \theta_m = k_c/k_0 \tag{10-6}$$

Substituting Eq. (10-6) into Eq. (10-2) yields

$$\Delta\theta \approx \frac{2\pi}{k_c L} = \frac{\lambda_c}{L}$$
 in radians (10-7)

which is independent of frequency. When the guiding structure is partly filled with dielectric, the transverse wave number k_i is a function of frequency, so that $\Delta\theta$ changes as the beam is frequency scanned.

Radiation Pattern

As usual, the radiation pattern can be found by taking the Fourier transform of the aperture distribution. When the geometry of the leaky-wave antenna is maintained constant along the antenna length, the aperture field distribution consists of a traveling wave with a constant β and α , meaning that the amplitude distribution is exponentially decaying. If the antenna length is infinite, one finds that the radiation pattern $R(\theta)$ is given by

$$R(\theta) \sim \frac{\cos^2 \theta}{(\alpha/k_0)^2 + (\beta/k_0 - \sin \theta)^2}$$
 (10-8)

which does not exhibit any sidelobes. If the antenna length is finite, the expression for $R(\theta)$ becomes more involved, and the pattern possesses sidelobes that modify the basic shape for infinite length.

The preceding comments are illustrated well in a paper on dielectric-grating leaky-wave antennas by Schwering and Peng. They present several examples of such patterns, two of which are shown in Fig. 10-4a and b. The length of the antenna in Fig. 10-4a, which clearly exhibits sidelobes, is $10\lambda_0$. As the antenna length increases, the amplitude of the sidelobe variations decreases. For the radiation pattern in Fig. 10-4b, which shows a smooth pattern only, the antenna length is $150\lambda_0$, which is evidently effectively infinite. Although the leaky-wave antenna for which these calculations were made is periodic rather than uniform, the basic features are identical. Reference 7 contains an extended discussion of radiation-pattern considerations, including equations and other figures.

The radiation pattern in Fig. 10-4a is seen to possess first sidelobes that are only about 13 dB down, which is generally undesirable. In order to greatly reduce the sidelobe level and to control the pattern in other ways, it is customary to appropriately taper the amplitude of the aperture distribution, as is discussed next.

Control of Aperture Distribution to Reduce Sidelobes

The procedure to design the leaky-wave antenna so that it produces a final desired radiation pattern is straightforward, though somewhat complicated, involving the following steps. First, the final desired radiation pattern is specified, and then the corresponding

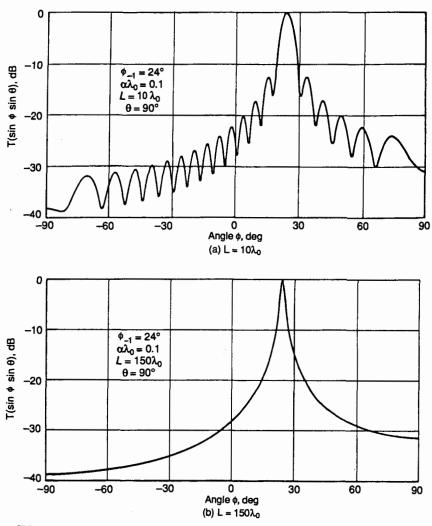


FIG. 10-4 Radiation patterns of dielectric grating leaky-wave antennas, showing the changes in the sidelobe behavior with antenna length. These antennas are not tapered to control the sidelobes. (a) Antenna length $L = 10\lambda_0$ (sidelobes clearly present). (b) Antenna length $L = 150\lambda_0$ (no sidelobes). (After Schwering and Peng, $^7 © 1983$ IEEE.)

aperture amplitude distribution is determined by standard antenna techniques. Next, by using the expression derived below, the values of α/k_0 are computed as a function of position along the antenna length in accordance with the aperture amplitude distribution that was just determined. At the same time, β/k_0 must be maintained constant along the length so that the radiation from all parts of the aperture point in the same direction. Finally, from the theory that relates α and β to the geometry of the structure, we compute the tapered geometry as a function of position along the antenna length.

When we change the local cross-sectional geometry of the guiding structure to

modify the value of α at some point z, however, it is likely that the value of β at that point is also modified slightly. However, since β must not be changed, the geometry must be further altered to restore the value of β , thereby changing α somewhat as well. In practice, this difficulty requires a two-step process for most leaky-wave antennas, which is not bad. Because of this added complexity, one seeks leaky-wave structures for which one can vary geometric parameters that change β and α essentially independently.

The first design step mentioned above, i.e., determining the required aperture amplitude distribution for the selected desired radiation pattern, is a standard antenna procedure not specifically related to leaky-wave antennas. The second step, calculating the values of $\alpha(z)$ corresponding to the aperture amplitude distribution found from the first step, is directly pertinent to leaky-wave antennas, and we therefore present now a derivation of the expression needed for this second step.

The power distribution along the antenna can be expressed in the form

$$P(z) = P(0) \exp \left[-2 \int_0^z \alpha(\zeta) \, d\zeta \right]$$
 (10-9)

where P(0) is the power at the input point, z = 0, and ζ is the integration variable. Upon differentiation of Eq. (10-9), we obtain

$$-\frac{dP(z)}{dz} = 2\alpha(z)P(z)$$
 (10-10)

Suppose now that the desired aperture distribution (which would achieve the specified radiation pattern) is $A(z) \exp(-j\beta z)$. We may then write

$$-\frac{dP(z)}{dz} = c|A(z)| \tag{10-11}$$

where c is a constant of proportionality. Comparison of Eqs. (10-10) and (10-11) yields

$$2\alpha(z) = \frac{c|A(z)|^2}{P(z)}$$
 (10-12)

Upon integration of Eq. (10-11), we obtain, corresponding to two sets of limits of integration, the following:

$$c \int_0^L |A(\zeta)|^2 d\zeta = P(0) - P(L)$$
 (10-13)

$$c \int_0^z |A(\zeta)|^2 d\zeta = P(0) - P(z)$$
 (10-14)

We next use Eq. (10-14) to substitute for P(z) in Eq. (10-12), and then we employ Eq. (10-13) to eliminate the proportionality constant c. In a straightforward fashion, we then obtain the desired result:

$$2\alpha(z) = \frac{|A(z)|^2}{\frac{P(0)}{P(0) - P(L)} \int_0^L |A(\zeta)|^2 d\zeta - \int_0^z |A(\zeta)|^2 d\zeta}$$
(10-15)

The units of $\alpha(z)$ in Eq. (10-15) are nepers per unit length. To obtain $\alpha(z)$ in decibels per unit length, one multiplies by 8.68. If P(L), the power remaining at the end of the aperture,

is allowed to approach zero, we note from Eq. (10-15) that $\alpha(z)$ then becomes very large for points near to the end of the aperture, i.e, for z approaching L. This is the main reason why it is common for P(L)/P(0) to be equal to 0.1 or so, but not much smaller, with the remaining power being absorbed in a matched load to avoid the presence of any backlobe.

10-3 DESIGN PRINCIPLES FOR PERIODIC LEAKY-WAVE ANTENNAS

As discussed in Sec. 10-1, periodic leaky-wave antennas differ from uniform ones in that the waveguiding structure is modulated periodically along its length instead of being completely uniform (again, except for the small taper for both types to control the side-lobes). The dominant mode on uniform antennas is fast relative to free-space velocity, whereas the one on periodic antennas is slow, so that the dominant mode itself does not radiate and it needs the periodic modulation to produce the radiation. Since the physical processes that produce the radiation are different, these two antenna types have different scan ranges. On the other hand, most of the design principles for the uniform leaky-wave antennas discussed in Sec. 10-2 also apply to the periodic ones. The treatment below indicates in what ways changes in design are necessary. First, however, we summarize how the periodicity produces the leakage and, in that context, why the scan ranges are different for the two types.

Effect of Periodicity on Scan Behavior

In order to explain the source of the leakage and to understand the scan behavior as a function of frequency, we invoke the concept of space harmonics. Suppose we first take a uniform dielectric waveguide, and then we place an array of metal strips periodically along its length (as in Fig. 10-2). Before the metal strips are added, we choose the guide dimensions and frequency so that only the dominant mode is above cutoff; furthermore, $\beta > k_0$ for this mode, so it is purely bound. When the periodic array of strips is added, the periodicity introduces an infinity of space harmonics, each characterized by phase constant β_n and related to each other by

$$\beta_n d = \beta_0 d + 2n\pi \tag{10-16}$$

where d is the period and β_0 , the fundamental space harmonic, is simply the original β of the dominant mode of the uniform dielectric waveguide, but perturbed somewhat in value because of the addition of the strips. As seen from Eq. (10-16), β_n can take on a large variety of values, so that these space harmonics can be forward or backward in nature, and be slow or fast. Since the structure is open, a space harmonic that is fast will radiate. To say it in another way, since the space harmonics are all tied together, and all of them together comprise the dominant mode of the loaded structure, the whole mode becomes leaky if one or more of the space harmonics becomes fast.

We recall that for a space harmonic to be fast, we need $\beta_n/k_0 < 1$; we also know that $\beta_0/k_0 > 1$. If we rewrite Eq. (10-16) in the form

$$\frac{\beta_n}{k_0} = \frac{\beta_0}{k_0} + \frac{2n\pi}{k_0 d} = \frac{\beta_0}{k_0} + \frac{n\lambda_0}{d}$$
 (10-17)

we see that $|\beta_n/k_0|$ can readily be less than unity if n is negative and λ_0/d is suitably chosen. For a practical antenna, we want only a single radiated beam, so we choose n = -1.

If we follow this line of thinking further (the details will not be given here), we will find that when the frequency is low, all the space harmonics are slow and there are no radiated beams. When the frequency reaches the critical value for which the n=-1 space harmonic first becomes fast, the radiating beam just emerges from backward end fire. As the frequency is increased, the beam swings up from backward end fire but is still radiating into the backward quadrant. Further increases in the frequency will swing the beam toward broadside, then through broadside, and then into the forward quadrant. The amount by which the forward quadrant is penetrated depends on other properties of the antenna, in this case primarily on the dielectric constant. On the other hand, the antenna is useful only if a single, controllable beam is radiated, and the range in the forward quadrant is usually limited by the emergence of the n=-2 beam from backward end fire, or by the next waveguide mode coming above cutoff.

A special problem is present for the periodic structures near broadside. A narrow region around broadside corresponds to an "open stop band" region, where the value of α becomes large and then zero for a structure of infinite length. In a practical antenna, this means that within this narrow angular region the amount of radiation drops substantially, and a large VSWR is encountered (power is reflected back to the source rather than being radiated). This effect is well known, and it also occurs when slot arrays are scanned through broadside. There are techniques, not widely used, that permit these arrays to scan through broadside, however. One of them^{8,9} uses pairs of strips rather than single strips, where the spacing between the elements of each pair is $\lambda_{80}/4$ at the broadside frequency, so that the wave reflected at broadside by the first element of each pair will be canceled, or nearly so, by the wave reflected by the second element.

Beam Direction, Beamwidth, and Radiation Efficiency

The discussion in Sec. 10-2 under this heading shows that these major behavioral features are given to a good approximation by a set of very simple relations. All the considerations presented there for uniform leaky-wave antennas apply as well to periodic leaky-wave antennas provided that we make one simple change, which takes into account the main difference between the two antenna types. That main difference relates to the fact that radiation from *periodic* leaky-wave antennas is due to the n = -1 space harmonic. In Eq. (10-1), therefore, β must be replaced by β_{-1} , to yield

$$\sin \theta_m \approx \frac{\beta_{-1}}{k_0} \tag{10-18}$$

where

$$\beta_{-1} = \beta_0 - 2\pi/d \tag{10-19}$$

consistent with Eq. (10-16). When we substitute Eq. (10-19) into Eq. (10-18), we obtain

$$\sin \theta_m \approx \frac{\beta_0}{k_0} - \frac{2\pi}{k_0 d} = \frac{\lambda_0}{\lambda_{g0}} - \frac{\lambda_0}{d}$$
 (10-20)

Thus, depending on how λ_0/d , where d is the period, compares with λ_0/λ_{s0} (or β_0/k_0), the beam can point in the backward quadrant or in the forward quadrant, in accordance with the discussion in the preceding subsection.

Equations (10-2) through (10-6), and the discussions relating to them, also apply to periodic leaky-wave antennas when the distinction relating to β_{-1} is kept in mind.

The considerations in Sec. 10-2 relating to the radiation pattern, as well as to the steps required to control the aperture distribution, are also valid here.

Feed Considerations

When the antenna aperture is tapered appropriately in accordance with the design steps outlined in Sec. 10-2 in the subsection "Control of Aperture Distribution to Reduce Sidelobes," very beautiful radiation patterns, with very low sidelobes, can be achieved on paper. These fine results can also be obtained in practice when proper attention is also paid to the way the leaky-wave antennas are fed.

For uniform leaky-wave antennas that are formed by opening up initially closed waveguides, concerns relating to the feed are usually negligible or nonexistent. The reason for this lies in the taper process for controlling the sidelobes. The taper is such that the aperture radiates very little at its ends, and therefore the discontinuity between the closed feed waveguide and the antenna aperture when it first begins is extremely small in most cases. There is therefore negligible spurious radiation from that feed junction. There is also no appreciable impedance mismatch at that feed junction, of course.

When the feeding structure is an open waveguide, we must examine the situation more carefully. This is particularly true for those periodic leaky-wave antennas that are basically surface-wave-excited. The problem then lies with the way the basic surface wave is produced, rather than with the transition to the periodic modulation, which again begins very slowly due to the taper. Surface waves are often formed by a tapered transition from a closed waveguide, with resultant spurious radiation associated with the transition. Such problems are well known with respect to surface-wave antennas. When such transitions form part of the overall feed system, their contributions to the radiation pattern may be significant and may spoil the initial careful paper design.

In many cases, spurious feed radiation is not a problem with leaky-wave antennas, and this is one of their important virtues, but the feed mechanism must be looked at carefully in the design to make sure that it does not introduce its own contribution to the radiation pattern.

10-4 SPECIFIC STRUCTURES: OVERVIEW

Leaky-wave antennas are formed by perturbing an initially bound mode on a waveguiding structure in a way that produces leakage all along the length of the guiding structure. As might be expected, all the very early leaky-wave antennas were based on *closed waveguides*, and the leakage was achieved by physically cutting into a wall of the waveguide, in the form of a longitudinal slit or a series of closely spaced holes. The first known leaky-wave antenna, shown in Fig. 10-1 and invented by W. W. Hansen¹ in 1940, was in fact a long slot in a rectangular waveguide.

The next section presents several of the more important leaky-wave antennas based on *closed* waveguides. These structures are usually very simple in cross section, so that it was possible to obtain accurate expressions for the complex wave number $(\beta - j\alpha)$ in terms of the frequency and the geometry of the cross section. Since very little spurious radiation occurs because of the feed junction, the theoretically derived radiation patterns,

based on designs that yielded low sidelobes, agreed extremely well with the measured radiation patterns. A dramatic example of excellent agreement is given in Sec. 10-5. Many of the early theoretical expressions and the designs based on them are still of practical value today, and are indeed so good that the initial designs were often the final ones, without the need for any empirical adjustments.

The data relating the wave-number behavior to the geometric parameters are usually plotted as β/k_0 or λ_0/λ_g , where λ_g is the guide wavelength in the propagation direction (z), and as α/k_0 or $\alpha\lambda_0$, where α is the leakage constant. In previous editions of this Handbook, plots were presented in the form of λ/λ_z and $\alpha_z\lambda$, where α_z , λ , and λ_z are written instead of α , λ_0 , and λ_g . Where the discussion and graphical plots in the present chapter employ material taken from the previous edition, the previous notation is carried over. It is essential that such information be available for any specific antenna structure because the correct taper for low sidelobes cannot be designed without it. A last general remark to be made in connection with leaky-wave structures based on closed waveguides is that some of the structures employ a series of round holes or small (nonresonant) slots. These holes or slots, however, are closely spaced, so that the structures should be viewed as quasi-uniform rather than periodic, even though these holes are periodically spaced. The radiation produced by them radiates the n=0 space harmonic and not the n=-1 space harmonic.

The next stage in the development of specific leaky-wave antennas involved those based on *open* waveguides. Some of these antennas are uniform structures that employ open waveguides on which the dominant mode is initially purely bound, and others are periodic structures that are excited by surface waves and radiate via the n=-1 space harmonic. These two categories are considered separately in Secs. 10-7 and 10-6, respectively.

The best-known examples of surface-wave-excited *periodic* leaky-wave antennas are dielectric rectangular rods (or slabs), with or without ground planes, that have on their tops or on one of their sides a periodic array of grooves or a periodic array of metal strips. Another large group is based on microstrip line. These antennas have been studied rather extensively, both experimentally and, more recently, theoretically. Together with other, similar structures, they are discussed in Sec. 10-6. An important problem for this class of structures is the incorporation of a feed mechanism that does not contribute spurious radiation.

Uniform leaky-wave antennas based on open waveguides offer a special challenge. Since the guide is already open, it cannot be cut to induce radiation, and other approaches are needed. The most common one is the appropriate introduction of asymmetry, but other mechanisms, such as the use of a leaky higher mode or some modification in the geometry, also have been found useful. The first, and only early, example of such a leaky-wave antenna based on an open waveguide was invented by W. Rotman in the late 1950s. This pioneering study 10,11 involved several versions of a form of trough waveguide whose dominant mode is purely bound but was made leaky by introducing asymmetry. The design procedure for this antenna was successful and practical, but the approach was not pursued further until about 20 years later, in the context of a new need that emerged in connection with millimeter waves.

As interest in millimeter waves revived during the 1970s, it was recognized that new forms of leaky-wave antennas were needed because of the smaller wavelengths involved and because the usual waveguides had higher loss at those higher frequencies. Since these smaller wavelengths caused fabrication problems due to smaller dimensions, simpler structures were sought; in fact, the latest structures are designed to permit the complicated portion of the structure, including the taper for sidelobe control, to be deposited photo-

lithographically, in printed-circuit form, by using a mask. Because of the loss considerations, the new antennas are often based on new lower-loss waveguides designed for millimeter-wave applications.

These include nonradiative dielectric (NRD) guide, groove guide, and rectangular dielectric rods, sometimes used in conjunction with microstrip in novel ways. Unfortunately, these last-mentioned structures were difficult to analyze theoretically, so their designs were empirical only; as a result, the experimental radiation patterns showed poor sidelobe performance, leading some people to conclude unfairly that poor sidelobe behavior was a necessary consequence of this class of antennas. However, many other leakywave antennas in this class were analyzed accurately, primarily by Oliner and his colleagues, and their results agreed very well with measurements. Some of the more promising of these new millimeter-wave antennas are described in Sec. 10-7.

The most recent development relating to leaky-wave antennas is their incorporation into arrays that permit scanning in two dimensions. The arrays are essentially a linear phased array of leaky-wave line-source antennas, where the scanning in elevation is obtained in leaky-wave fashion by varying the frequency, and the scanning in azimuth is achieved by varying the phase difference between the successive parallel leaky-wave line sources. The architecture underlying this approach is described in Sec. 10-8, and several examples are given of specific antenna structures in this category. A partial motivation for this approach is to achieve a lower-cost substitute for phased-array antennas in some applications.

10-5 SPECIFIC STRUCTURES BASED ON CLOSED WAVEGUIDES

The earliest example of a leaky-wave antenna was the one due to W. W. Hansen, for which he was granted a patent. He had proposed during the late 1930s that an antenna could be created by cutting a rectangular waveguide longitudinally, as shown in Fig. 10-1, thereby producing a long slit in the side of the initially closed guide, out of which power could leak away. His concept was not pursued at that time because of the success of slot arrays, but the simplicity of the structure remained attractive, and it was reexamined about a decade later. The 1950s, in fact, represented a very active period during which many leaky-wave antennas based on closed waveguides were proposed, analyzed, measured, and utilized. Several excellent references exist which summarize in detail the state of the art in this class of antennas as of the middle 1960s, including a comprehensive book 12 by C. H. Walter, a chapter by F. J. Zucker in the First Edition of this Handbook, a chapter by T. Tamir 14 in Part II of the book Antenna Theory, edited by R. E. Collin and F. J. Zucker, and a summary by A. A. Oliner and R. G. Malech 15 in Volume II of the book Microwave Scanning Antennas, edited by R. C. Hansen.

All these specific structures based on closed waveguides are "uniform" leaky-wave antennas, so the principles for their design are those discussed above in Sec. 10-2. The remaining information required in order to complete the design involves the expressions for $\beta/k_0 (=\lambda/\lambda_z)$ and α/k_0 (or $\alpha_z\lambda$) as a function of the frequency and geometric parameters of the specific structure. Since the period before the middle 1960s predates the computer era, theoretical expressions had to be simple to be considered practical. Fortunately, the structures themselves were simple, leading automatically to relatively simple

expressions that were accurate, but, in addition, many of the expressions were further simplified by the use of perturbation relations.

In some cases, these values of α and β were measured rather than calculated, and then employed in the design. Two experimental methods are outlined in Walter's book.¹⁶

Long Slits in Rectangular Waveguide

Radiation from long slits in rectangular waveguide can be accomplished in several ways, where the leakage rate can be adjusted by changing the slit width, and the polarization of the radiated beam can be selected by changing the waveguide mode. Some examples are illustrated in Fig. 10-5.

The best-known example in this well-known category is the narrow slit in the side wall of rectangular waveguide shown in Fig. 10-1, or the same structure with a ground plane seen in Fig. 10-5a. The antenna shown in Fig. 10-5a also differs from the structure in Fig. 10-1 in that it is rotated by 90° and the slit is shown tapered (in exaggerated fashion) to remind us that in the design the slit width is varied to control the sidelobes in the radiation pattern. (The rectangular waveguide dimensions h and w correspond, of course, to the usual a and b, respectively.)

For this antenna, with the ground plane present but with the slit uniform, simple theoretical expressions are available for the relations between λ/λ_z and $\alpha_z\lambda$ and the frequency and the geometry. These expressions were derived by Goldstone and Oliner¹⁷ using a transverse resonance approach together with a simple perturbation procedure. The results agreed very well with measurements. The expressions (with the notation differing somewhat from that in Ref. 17 to be consistent with Fig. 10-5a) are

$$\frac{\lambda}{\lambda_z} = \frac{\lambda}{\lambda_{z0}} \left(1 - \frac{\lambda_{z0}^2}{2\pi^2 h w} \frac{p}{1 + p^2} \right) \tag{10-21}$$

and

$$\alpha_z \lambda = \frac{\lambda \lambda_{z0}}{\pi h w} \frac{1}{1 + p^2}$$
 (10-22)

where

$$p = \frac{2}{\pi} \left[\ln \left(\csc \frac{\pi \delta}{2w} \right) + \ln \left(1.526 \frac{h}{\delta} \right) \right]$$
 (10-23)

and λ_{x0} is the guide wavelength, that is,

$$\lambda_{20} = \lambda / \sqrt{1 - (\lambda/2h)^2}$$
 (10-24)

in the unperturbed waveguide ($\delta = 0$). Zero ground-plane thickness is assumed. Although λ/λ_z and $\alpha_z\lambda$ are not strictly separable, λ/λ_z is controlled primarily by variations in h (through λ_{z0}), and $\alpha_z\lambda$ by variations in δ . For operation at frequencies near cutoff, one should use the exact solution (also in Ref. 17) instead of the perturbation form given above. When the rectangular waveguide is dielectric-filled, Eqs. (10-21) to (10-24) must be modified appropriately; such expressions are given in Ref. 12, on pages 189 and 190.

Although expressions corresponding to Eqs. (10-21) through (10-24) are also available in Ref. 17 for the structures in Fig. 10-5b and d, and in Ref. 12 for that in Fig. 10-5c, results for these structures are displayed graphically in Fig. 10-5 to illustrate how the numerical values for normalized β and α vary with frequency. Theoretical expressions for these long slit structures have also been derived by Rumsey¹⁹ and by Hines, Rumsey, and Walter¹⁸ using a variational approach. Modifications of the theoretical expressions given in Ref. 17 for these structures when dielectric loading is present are contained in Chap. 5 of Ref. 12.

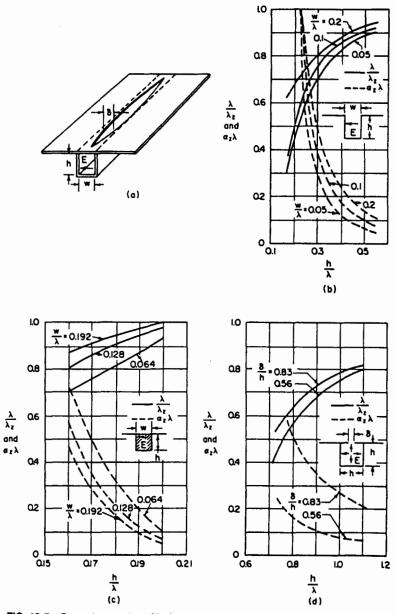


FIG. 10-5 Several examples of leaky-wave antennas based on long slits in rectangular waveguide. (a) Narrow slit in the narrow wall, shown with an exaggerated taper. The remaining figures show the relative guide wavelength λ/λ_x and the relative leakage constant $\alpha_x\lambda$ for (b) the channel-guide antenna, (c) the dielectric-filled channel, for $\epsilon_r = 2.56$, and (d) a narrow slit in square guide. The dominant mode excites the slit in the first three cases, while the TM₁₁ mode excites the slit in the last case. (After Goldstone and Ollner of and Hines, Rumsey, and Walter.)

It should be recognized that the slit fields in the structures in Fig. 10-5a, b, and c have $E_z = 0$, and that the transverse electric field in the aperture is equivalent to a longitudinal (z-directed) magnetic current. The resulting radiation pattern is horizontally polarized. In contrast, the slit in the structure in Fig. 10-5d has $H_z = 0$ and primarily constitutes a longitudinal electric current, so that the antenna radiates with vertical polarization.

The configurations in Fig. 10-5b and c, for which the slit has been opened up to the full guide width (w), are generally referred to as channel-guide antennas. 20,21 Because the slit is so wide, however, the leakage constant can become large rather easily. Even in the structure in Fig. 10-5a, however, the slit cuts directly across the electric field lines, corresponding to the logarithmic dependence seen in Eq. (10-23), so that the leakage rate will never be very small. If a leaky-wave antenna with a very narrow beam is required, therefore, one needs to go to a structure like that containing the series of closely spaced holes described later in this section.

Measurements have been taken on all these structures, and the agreement with theory has been excellent. However, most of these measurements have been on untapered slits. Measurements on tapered-slit antennas have been reported, e.g., in Refs. 18 and 21. For the antenna in Fig. 10-5a, good control over the sidelobes has been achieved, ¹⁸ a typical result being that a gaussian amplitude distribution produces low sidelobes over an almost 2:1 frequency range in which the beam swings from 38 to 18° off end fire.

Recently, a modified long-slot structure has been proposed and analyzed²² that is claimed to provide radiation patterns with very low sidelobes within a relatively short length and with high efficiency. The long slot is located on the top wall of rectangular waveguide, and it moves from the centerline of the top wall out to near the side wall and back to the centerline in a very strong, but specified, curved fashion. The designers call this variation their *meander* contour. There is no experimental verification at this time.

Long Slits in Circular Waveguide

The radiation properties of leaky-wave antennas based on long slits in circular waveguide are qualitatively similar to those for long slits in rectangular waveguide, as discussed above. Three independent theoretical analyses appear to be available. The first two, due to Harrington²³ and to Rumsey,¹⁹ employ a variational approach, and the authors present accurate results that agree very well with their independently obtained measurements. The third analysis, by Goldstone and Oliner,²⁴ uses a transverse resonance approach in the radial direction and develops expressions for the slit using radial transmission-line theory. The authors obtain explicit expressions for the phase and leakage constants in a relatively simple, explicit form, in contrast to the other two theories, and these expressions are also much simpler to compute from. The results also agreed well with Harrington's measurements.²³

Numerical results for air-filled circular waveguides supporting the TE_{11} mode and the TM_{01} mode, to furnish opposite types of polarization, are presented in Fig. 10-6a and b, respectively. Explicit expressions for air-filled guides are given in Ref. 24, and the modifications in those expressions for the dielectric-filled case are included in Chap. 5 of Ref. 12.

Closely Spaced Holes or Slots in Rectangular Waveguide

A problem relating to the structures in Fig. 10-5a to c is that the opening directly disrupts the current lines, so one cannot, with such a geometry, obtain a very narrow radiated

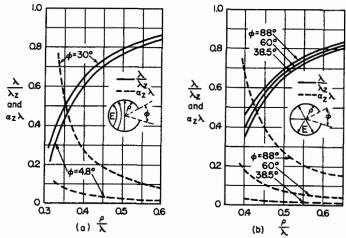


FIG. 10-6 Long slits in circular waveguide. (a) TE₁₀ mode excitation. (b) TM₀₁ mode excitation. (After Harrington²³ and Goldstone and Oliner. ²⁴)

beam. A way to surmount this difficulty is to replace the long slit (or the channel-guide geometry) with a series of closely spaced small holes, as shown in Fig. 10-7a. Then the current lines are simply pushed aside by the holes, and they can go around them. Since the holes perturb the initially closed guide much less than the long slit does, the resulting value of α is much smaller. Finally, since the holes are closely spaced together, the structure is quasi-uniform and the design principles in Sec. 10-2 apply.

The antenna employing a series of closely spaced round holes was proposed and measured at the Ohio State University, 25 and it became known as the OSU "holey guide." By varying the diameter d of the holes and, to a lesser extent, the hole spacing s and the

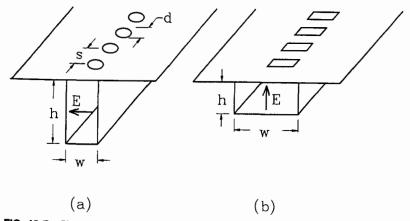


FIG. 10-7 Closely spaced apertures in rectangular waveguide to permit narrow radiated beams. (a) Closely spaced round holes in the narrow wall ("holey guide"). (After Hines and Upson.25) (b) Closely spaced slots in the broad wall. (After Hyneman.26)

guide width w, a very large range in the values of $\alpha\lambda_z$ was found experimentally. This structure was also analyzed by Goldstone and Oliner, ¹⁷ by employing small aperture procedures for the series of holes, together with a transverse resonance approach. Using a perturbation form for the result, they obtained the following simple expressions [using the notation in Eqs. (10-21) and (10-22)]:

$$\frac{\lambda}{\lambda_z} = \frac{\lambda}{\lambda_{z0}} \left[1 + \frac{\lambda_{z0}^2}{4\pi h^2} X' \right]$$
 (10-25)

and

$$\alpha_z \lambda = \frac{\lambda \lambda_{z0} R'}{2h^2} \tag{10-26}$$

where

$$X' = \frac{B'}{(G')^2 + (B')^2} \qquad R' = \frac{G'}{(G')^2 + (B')^2}$$
 (10-27)

$$G' = \pi w/2h \tag{10-28}$$

$$B' = 6hws/\pi d^3 {10-29}$$

$$\lambda_{z0} = \lambda/\sqrt{1 - (\lambda/2h)^2} \tag{10-30}$$

Calculations from these expressions agreed very well with measurements made both at the Ohio State University (Ref. 12, Chap. 5) and the Polytechnic Institute of Brooklyn. ¹⁷ When the frequency of operation is near to cutoff, these perturbation expressions become inaccurate, and one should instead solve the transverse resonance relation ¹⁷ exactly.

A second structure in this general category employs a series of closely spaced slots²⁶ located in the broad wall of rectangular waveguide, as shown in Fig. 10-7b. This antenna produces vertically polarized radiation, in contrast with the horizontally polarized radiation obtained from the series of round holes in the narrow wall (Fig. 10-7a). Again, λ/λ_z can be controlled by changing the guide width w, and the value of $\alpha_z\lambda$ can be changed by varying the slot width d primarily. A third example in this category is the "serrated" waveguide, ^{27,28} which looks like the structure in Fig. 10-7b but has a thick top wall, whose thickness is varied to control $\alpha_z\lambda$. Both theory and measurements are available, but this antenna has not found application because closely spaced thick slots are difficult to manufacture.

Array of Closely Spaced Wide Transverse Strips

This array of transverse strips, sometimes called an *inductive-grid antenna* and due to R. C. Honey, ²⁹ is shown in Fig. 10-8a. The antenna consists of a parallel-plate waveguide operated in its first higher (TE_1) mode, with its upper plate composed of an array of closely spaced transverse strips, and fed from a reflector arrangement so as to fill the space with the field having the polarization shown in Fig. 10-8a. The upper plate can be photoetched on a thin laminate and then be supported by polyfoam, or it can consist of a grid of transverse round wires.

The structure was analyzed²⁹ by using the transverse resonance method, which yielded simple and accurate expressions for the λ/λ_z and $\alpha_z\lambda$ values. From these expressions one can compute the design curves presented in Fig. 10-8b and c. The design procedure is to first select the desired λ/λ_z and $\alpha_z\lambda$ and then to read from the curves in Fig. 10-8b the corresponding abscissa value. The curves in Fig. 10-8c then yield the value of d for the design wavelength corresponding to the abscissa value obtained from Fig. 10-8b. Now, in a design for low sidelobes in some specified fashion (see Sec. 10-2), $\alpha_z\lambda$ must vary

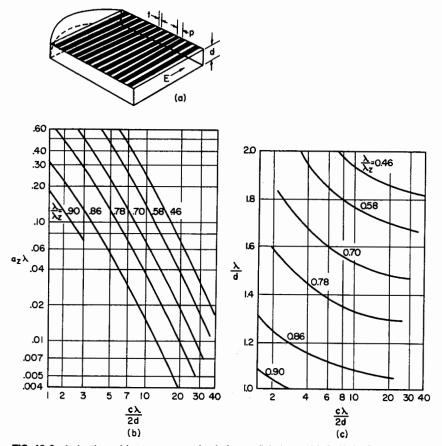


FIG. 10-8 Inductive-grid antenna comprised of a parallel-plate guide fed in its first higher TE mode and with its upper plate consisting of a series of closely spaced wide transverse strips. (a) Structure. (b) Relative leakage constant with the relative guide wavelength as a parameter. (c) A plot to aid in the design procedure (see text). Quantity c, which appears in the abscissas of parts (b) and (c), is defined as $c = 2\pi d/p$ In [csc $(\pi t/2p)$]. (After Honey.²⁹)

from point to point in a tapered fashion along the longitudinal direction, while λ/λ_z must remain the same at each point. The plot in Fig. 10-8b then tells us how c can be varied, by changing the strip width t, to obtain the desired different values of $\alpha_z\lambda$ while trying to maintain λ/λ_z constant. However, λ/λ_z will change somewhat as t is varied, since it is not independent of t, and the plot in Fig. 10-8c then indicates how d can be modified in order to change λ/λ_z back to the desired constant value.

In his final design, Honey²⁹ found that it was necessary to flex the bottom plate slightly along the longitudinal direction, and he built his structure accordingly. He was also meticulous with respect to both the accuracy of his theory and the details of the structure to be measured. As a result, the correspondence between his theoretical and measured radiation patterns was *remarkably good*, down to almost -40 dB, as may be observed in Fig. 10-9.

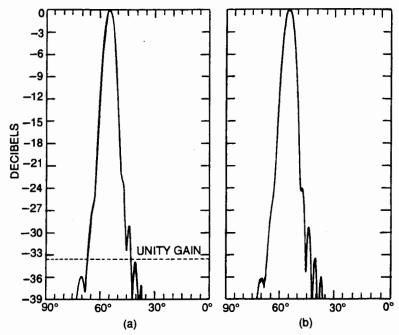


FIG. 10-9 Theoretical (a) and measured (b) radiation patterns for the inductive-grid antenna shown in Fig. 10-8a. The accurate theoretical design and the carefully fabricated experimental structure both took into account the taper for low sidelobes. The agreement between the two patterns is seen to be remarkable. [After Honey,²⁶ © 1959 IRE (now IEEE).]

Planar Structures

The array of transverse strips discussed above is an example of a planar structure, but it was treated separately because of its systematic and careful design procedure and its careful comparison between measurement and theory. Results are available for several other planar structures, however.

We comment first on a planar array of longitudinal strips, or slits, also examined by Honey. This structure is essentially an array of rectangular waveguides placed next to each other, with a longitudinal slit in the narrow wall of each guide. This structure also was analyzed in Ref. 17, and simple explicit formulas for its performance are given there.

Planar structures that look like, but are not, two-dimensional versions of the "holey" waveguide described earlier also have been built. One version consists of a parallel-plate waveguide in which the top plate has a two-dimensional array of small round holes and which is operated in the TEM mode. Another version is the Babinet dual of the top plate, in which the holes are replaced by round disks; this second version has been called a mushroom antenna because the disks can be supported by metal stems. These antenna structures have their problems and are not recommended.

A third planar structure is comprised of a series of thick transverse slots that go all the way across the top walls of an array of parallel rectangular waveguides. ³² These transverse slots constitute a strong perturbation on the individual waveguides because they cut all the

way across the current lines on the top guide walls. The slot spacings on the original structure varied over a large range, so that the performance behavior was not always clear. Furthermore, the analysis assigned each slot a conductance value, so that the approach used resembled that for a slot array more than that for a leaky-wave antenna. Nevertheless, if the slots are spaced sufficiently closely to be viewed as quasi-uniform, this structure can furnish an interesting, but limited, leaky-wave antenna.

The reason lies in the function of the slot thickness. If the slot is a quarter-wave thick electrically, then the normalized impedance value at the waveguide interface becomes its inverse at the air interface above. Furthermore, since these slots, when their thickness is zero, are known to heavily load the waveguides (because they cut across the current lines), it is difficult for them to furnish narrow beams. When the slots are electrically a quarter-wavelength thick, however, the effective loading on the waveguides becomes small so that low values of $\alpha_r \lambda$, and therefore narrow beams, can be readily achieved.

10-6 SPECIFIC STRUCTURES BASED ON PERIODIC OPEN WAVEGUIDES

The design principles for leaky-wave antennas based on periodic open waveguides are presented in Sec. 10-3. The important points to recall are that the basic open waveguide supports a slow wave, which does not radiate, and that the period of the structural modulation is selected relative to the wavelength so that the n=-1 space harmonic, and only that one, radiates the power. In contrast, the periodic structures discussed in Sec. 10-5, such as the closely spaced series of round holes in rectangular waveguide, are based on a fast wave and are quasi-uniform so that only the n=0 space harmonic radiates. Furthermore, the beam radiated from the periodically modulated slow-wave structures may be scanned throughout most of the backward quadrant and into part of the forward quadrant, whereas the beam radiated from the uniform or quasi-uniform structures is restricted to the forward quadrant only.

The two most common open waveguides that support dominant modes and which serve as the basis for periodic leaky-wave antennas are rectangular dielectric rods, with or without ground plane, and microstrip line. The class of dielectric rods includes a variety of known waveguides, such as dielectric image guide, insular guide, inset guide, and so on. Since the leaky wave is fast and the basic surface wave (or microstrip dominant mode) is slow, one must be careful about the feed arrangement to make sure that little spurious radiation is introduced.

Many of these periodic leaky-wave antennas have been known (measured and used) for some years, but accurate theories for β and α , suitable for careful design purposes, have become available only recently.

Early Structures

A few pioneering examples in this class were proposed and studied as far back as the late 1950s, but the ideas behind them were not pursued then. When they did reemerge, a decade or two later and in a somewhat different form, most people did not recognize the relationship with the past. Two examples of this early novel thinking are presented here.

The first structure is based on the original dielectric image guide, due to D. D. King, 33 which consists of the top half of a round dielectric rod placed on a ground plane. The fields

of the dominant mode on the rod (the TE₁₁ mode) extended substantially into the air region transversely, as did the current lines on the ground plane. In the leaky-wave antenna configuration³⁴ based on this guide, a two-dimensional array of slots was cut into the ground plane on each side of the rod. In this way, the (loosely bound) surface wave guided by the rod excites each row of slots in phase, with an illumination corresponding to the transverse decay rate of the field, and each column of slots in accordance with the propagation wave number β . Depending on the type, orientation, and spacing of the slots, a variety of radiation patterns can be obtained. A summary of the possibilities, together with sketches of some slot configurations, appear on pages 16-33 and 16-34 of Ref. 13. This antenna was proposed for application to millimeter waves, but its concept was not reintroduced until interest in millimeter waves was revived some 15 years or so later.

The second antenna structure was called the sandwich-wire antenna, and its configuration was an outgrowth of stripline. There are two versions. In the first configuration, 35 the top and bottom plates and the center strip of stripline are each reduced to wires, and the center wire is then snaked along its length in periodic fashion. The periodicity is selected so that the n = -1 space harmonic can radiate. A second configuration 36 looks more like a suspended microstrip line that is cavity-backed, with a strip mounted on a cavity-backed thin dielectric layer, to support the strip, and with the strip undulating sinusoidally back and forth along the dielectric layer. Again, the n = -1 space harmonic radiates, and measurements were made to determine the performance properties. Diagrams of the structures and curves for some measurements may be found on pages 16-36 and 16-38 of Ref. 13. A limitation on the usefulness of this antenna approach is that dimensional changes that affect β affect α as well. For example, a good approximation for the relative phase velocity is obtained by assuming that the wave velocity along the undulating strip is that of light. Thus, if the amplitude of the undulation is increased, the value of β will be increased. However, the value of α is changed most easily by varying that same amplitude.

Periodic Dielectric Waveguides

Periodic dielectric waveguides are uniform dielectric waveguides with a periodic surface perturbation. Several types of uniform dielectric waveguides are shown in cross section in Fig. 10-10a through e. Rectangular shapes are preferred for antennas of this class. The type in Fig. 10-10a is a simple rectangular rod of rectangular shape, the type in Fig. 10-10b is a rectangular form of dielectric image guide, and the type in Fig. 10-10c, the insular guide, has an extra dielectric layer on the ground plane so as to reduce the ground-plane losses. The types in Fig. 10-10d and e, the trapped image guide³⁷ and the inset guide,³⁸ respectively, lend themselves to a flush-mounted arrangement and reduce radiation losses from bends. The two most common dielectric waveguides are the types in Fig. 10-10a and b.

The most common periodic modulation methods are a grating of grooves, a grating of metal strips, and, to a lesser extent, a series of metal disks. These perturbations are ordinarily placed on the top surface (the wide dimension) of these guides, but they also may be placed on the sides, when accessible. Dielectric image-guide antennas with a grating of grooves and with a grating of metal strips appear in Fig. 10-11a and b, respectively. These gratings are shown as uniform; in practice, the gratings would be tapered so that the groove depths and the metal strip widths would be very small at the beginning and the end in each case.

The antennas in Fig. 10-11a and b were first proposed around 1960, but systematic

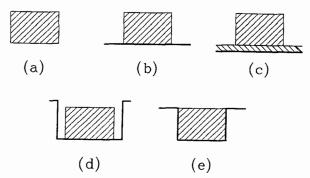


FIG. 10-10 Cross sections of several types of uniform dielectric waveguides. (a) Rectangular rod of rectangular shape. (b) Rectangular form of dielectric image guide. (c) The insular guide, with an extra dielectric layer of lower ϵ_r on the ground plane. (d) Trapped image guide. (e) Inset guide.

investigations of their behavior, both experimental and theoretical, were not carried out until the late 1970s. Most of the early studies were conducted by the army at Ft. Monmouth, on grooved antennas ³⁹⁻⁴¹ and on antennas with metal strips. ⁴²⁻⁴⁴ Experimental studies on the metal-strip antennas were also performed at the University of Illinois ⁴⁵⁻⁴⁷ during this period on dielectric image guide, and by Itoh and Adelseck ⁴⁸ on trapped image guide. One important conclusion from the Ft. Monmouth studies was that in practice there is an upper limit to the value of leakage constant obtainable with grooved gratings;

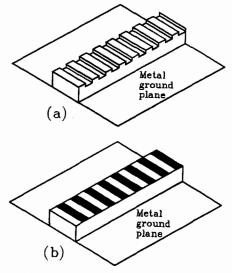


FIG. 10-11 Dielectric image guide with (a) a grating of grooves and (b) a grating of metal strips.

antennas employing grooved gratings were therefore limited to narrow radiated beams. It was found that the metal-strip gratings were more versatile, permitting both wide and narrow beams.

Studies also were concerned with how these antennas could be fed without causing spurious radiation at the feed. 46.49 Reference 49 utilizes slots cut into the ground plane under the dielectric rectangular rod to effect a smooth transfer of power from the feed line.

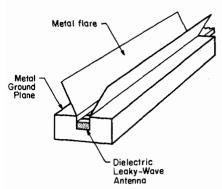


FIG. 10-12 The use of a flared hom in conjunction with the structure in Fig. 10-11b in order to narrow the beamwidth in the crossplane. (After Trinh, Mittra, and Paleta, 47 © 1981 IEEE.)

The radiation pattern in the crossplane depends on the width of the dielectric structure. The waveguide is excited in its dominant mode, and its width is usually chosen to be comparatively small so as to avoid excitation of higher modes. Alternatively, if one wishes to narrow the beam in the cross-plane, the dielectric width may be made large, but then single-mode excitation must be ensured by an appropriate feed arrangement. Another technique⁴⁷ is shown in Fig. 10-12. The grating structure is embedded in a rectangular metal trough. which is then attached to a flared-horn configuration; design details are included in Ref. 47.

Design Theory for Wide Periodic Dielectric Antennas

It is only within the last decade that accurate theoretical analyses became available that permit the systematic design of this class of leaky-wave antennas. For antennas employing a grating of grooves, thorough and detailed studies were performed by Schwering and Peng, 7,39,40 based in part on earlier analytical work by Peng and Tamir. 50,51 The two best sources for systematic design information are Refs. 7 and 52. Corresponding, but less thorough, design information on metal-strip-grating antennas comes mostly from work by Guglielmi and Oliner, 53 based on earlier analyses by them $^{54-56}$ of scattering by metal-strip gratings on a dielectric substrate. Another accurate method of analysis for these antennas was presented by Encinar. 57 Many of the general conclusions appropriate to grooved antennas, however, apply as well to those with metal-strip gratings. The detailed expressions for β/k_0 and α/k_0 are different, of course.

The theoretical design information referred to above is applicable directly to dielectric image guides, i.e., structures for which a ground plane is present under the rectangular dielectric layer. The procedure is readily extendable to structures without a ground plane, however, by some suitable, basically straightforward modifications. The numerical values presented in Refs. 7 and 52 assume that the dielectric material has an ϵ , = 12, corresponding to Si or GaAs, so that the antenna performance can be controlled, if desired, by semiconductor devices.

For the antenna employing a grating of grooves, the groove depth must be chosen to lie within a certain range if we wish to optimize the leakage constant α . The reason for this can be understood physically in a simple way. Consider the structure shown in the inset in Fig. 10-13, where the height of the uniform dielectric region is h and the groove depth is t. Suppose that we maintain the sum of h+t constant and we increase the groove depth t.

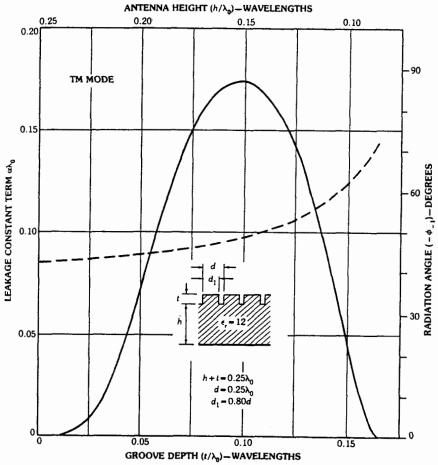


FIG. 10-13 Calculations for the relative leakage constant and the radiation angle as a function of groove depth for the dielectric image guide with a grating of grooves shown in Fig. 10-11a. (After Schwering and Peng,⁷ © 1983 IEEE.)

Although the total antenna height is fixed, the effective dielectric constant ϵ_{eff} of the structure is decreased as t is increased, because the groove region is now partly air-filled. This value of ϵ_{eff} , combined with the height h+t, may be viewed as an "effective height," and is an important design parameter. When the effective height is small, most of the guided energy travels in the air region above the antenna, and the grooves would cause little radiation. When the effective height is large, on the other hand, the energy is confined primarily to the interior of the antenna, and again the grooves will have little effect. An intermediate effective height thus exists for which the energy density in the grooved region reaches a peak value. We would therefore expect that α can be maximized by an optimal combination of groove depth and effective height. The curve of $\alpha \lambda_0$ versus t/λ shown in Fig. 10-13 illustrates precisely such behavior for the structure treated there. Similar qualitative reasoning applies to other periodically modulated open dielectric structures.

Design Theory for Narrow Periodic Dielectric Antennas

The theoretical results referred to in this subsection make the assumption that the dielectric structures have infinite width w. It has been found, however, that they apply quite accurately to "wide" structures, for which $w > \lambda_0 / \sqrt{\epsilon_{eff}} - 1$. If $\epsilon_{eff} = 2$, for example, these results are applicable to antennas for which $w > \lambda_0$. For $\epsilon_{eff} = 6$, on the other hand, w need satisfy only $w > 0.45\lambda_0$. Thus the theory for "infinite" width can actually be applied with good accuracy to structures that are fairly narrow. When the antennas are narrower than the criterion above will allow, a correction scheme is available that yields accurate results for them as well.

For antennas of narrow width $(w < \lambda_0/\sqrt{\epsilon_{eff}-1})$, the value of β can be derived in a simple way with good accuracy by using the EDC (equivalent dielectric constant) procedure, but α can no longer be approximated by that of an infinitely wide antenna with the same dielectric constant as the finite antenna. As w decreases, the phase velocity of the leaky mode increases, so that an increasing portion of the guided energy now travels in the air regions on both sides in the neighborhood of the perturbing mechanism, whether grooves or metal strips. As a result, the leakage constant α of the narrower antenna becomes smaller.

A simple procedure has been developed⁵⁸ that employs the EDC method to replace the antenna of finite width by an equivalent antenna of infinite width, but with a lower effective dielectric constant. As a result, a lower value of α is obtained. This procedure has produced numerical values for α and β that have agreed very well with measured results for a quite narrow antenna, with $\epsilon_r = 16$ and w = 1.3 mm, in the frequency range from 30 to 36 GHz. Some details regarding this procedure may also be found in Ref. 52, pages 17-64 to 17-68.

Periodic Leaky-Wave Antennas Based on Microstrip Line

A wide variety of possible traveling-wave periodic array antennas can be achieved employing microstrip line. As examples, one can employ a series of resonant patch antennas connected by the microstrip line, as seen in Fig. 10-14a, or a series of array elements coupled by proximity to the microstrip line, as shown in Fig. 10-14b. Top views of the structures are presented. Another wide class of possibilities is illustrated in Fig. 10-15a through c, and these involve periodic meanderings of the microstrip line strip itself. These last structures are reminiscent of the sandwich-wire antenna^{35,36} described above in the subsection "Early Structures." These and other traveling-wave arrays based on microstrip line are discussed in detail in the two comprehensive books ^{59,60} on microstrip antennas by James, Hall, and Wood and by James and Hall, respectively. The original references for the antennas in Fig. 10-14a and b are Refs. 61 and 62, respectively.

No theory is available for most of these antennas. For the few structures, such as the one shown in Fig. 10-14a, for which some theory is available, the theory is of the type used to describe the behavior of slot arrays. All the thinking, in fact, parallels that employed for slot arrays. For example, the array elements are usually assumed to be individually resonant, although there is no reason why they need to be. The theory then treats each element as loading the line individually, instead of viewing the structure in leaky-wave fashion. (See the discussion in Sec. 10-1 on the relation between leaky-wave antennas and slot arrays.) Furthermore, in many cases the arrays are designed to be resonant (standing wave rather than traveling wave). The array in Fig. 10-14a is specified as a resonant one, but an interesting traveling-wave modification, that contains additional phase shift between

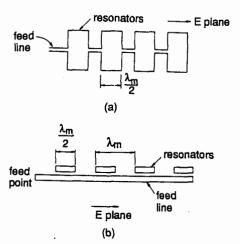


FIG. 10-14 Top views of traveling-wave periodic array antennas based on microstrip line. (a) Series of resonant patch antennas connected by microstrip line. (b) Series of elementary radiators, resonant or not, coupled by proximity to the microstrip line. (From James, Hall, and Wood.⁵⁹)

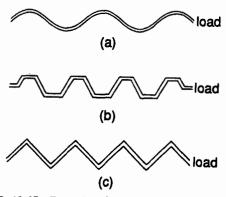


FIG. 10-15 Examples of periodic leaky-wave antennas based on microstrip line where the microstrip line itself is meandered periodically. (a) Sinusoidal, (b) trapezoidal, (c) zig-zag. (After James, Hall, and Wood.⁵⁹)

successive elements to reduce the frequency change needed to cover a given range of scan angle, has been reported. 63

These same structures can be transformed into standard leaky-wave antennas by simply making the individual radiating elements nonresonant (so each loads the line less strongly) and changing the spacing between elements to produce a traveling-wave rather

than a standing-wave array. Then the structure would lend itself to a leaky-wave analysis, although such an analysis has not yet appeared anywhere.

Periodic Arrays of Microstrip Patches or Dielectric Resonators Fed by Open Dielectric Waveguides

Since microstrip line becomes increasingly lossy as the frequency is raised, several investigators have built and measured antennas designed for use at millimeter wavelengths in which the microstrip line is replaced by a dielectric waveguide as the transmission line that feeds the periodic radiating elements. The point of view is that the feed line can be considered separately from the radiating elements, so that a less lossy feed line can be employed at the higher frequencies. The resulting antennas are indeed less lossy, but they sometimes become hybrid in character.

An example of such antennas is shown in Fig. 10-16. The radiating elements here are microstrip patch resonators, and they are fed by a low-loss open dielectric waveguide in the form of insular guide. The fringing fields of the dielectric guide excite the microwave patches. It is interesting that this mechanism is the same as the one used many years ago³⁴ with dielectric image line, discussed above in the subsection "Early Structures." In addition to low loss, this antenna has the advantage of simplicity. In an experimental design, ^{64,65} the distance between the metal patches and the dielectric guide is varied along the length to produce a taper to control the sidelobe level, as seen in Fig. 10-16b. Nevertheless, the design was purely empirical, since no theory was available, and the resulting radiation-pattern performance was only mediocre.

At about the same time, another study⁶⁶ replaced the microstrip patches by dielectric resonators, which may take the form of small rectangular or cylindrical dielectric blocks. The same type of open dielectric waveguide served as the feed transmission line. Again, however, the design was only empirical, and the pattern performance was therefore only passable.

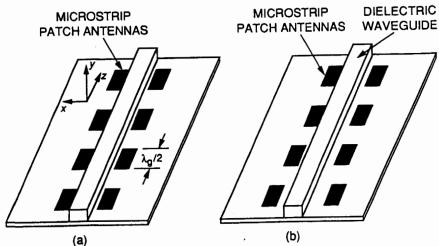


FIG. 10-16 A hybrid form of periodic leaky-wave antenna in which microstrip patch resonator arrays are fed by a dielectric image guide. (a) Basic configuration. (b) Configuration including a taper to control the sidelobes. (After James and Henderson.⁸⁵)

10-7 SPECIFIC STRUCTURES BASED ON UNIFORM OPEN WAVEGUIDES

As indicated in Sec. 10-5, almost all the early uniform leaky-wave antennas were based on initially closed waveguides. Those antennas were conceptually simple, and they worked very well. It was only much later, in response to requirements at millimeter wavelengths, that thought was given to leaky-wave antennas based on uniform *open* waveguides. There exists one notable exception, and that case is discussed below in the subsection "Early Structure: Asymmetrical Trough Waveguide Antenna."

There were two reasons why new types of leaky-wave antennas were sought for the millimeter-wave region. The first relates to the small wavelengths in this region; to minimize fabrication difficulties, the new antennas had to be *simple* in configuration, and *uniform* guiding structures satisfied this condition. The second reason was that the usual waveguides had higher *loss* at these higher frequencies; as a result, the new antennas were generally based on new lower-loss waveguides that had been studied specifically for application to the millimeter-wave region. These waveguides were *open* so that part of the field extended into the air region outside, thereby reducing the energy density and the loss. The principal waveguides in this category were nonradiative dielectric (NRD) guide and groove guide.

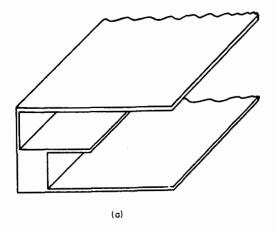
Because of the open nature of these waveguides, new mechanisms had to be found to produce the leakage. A physical cut is not meaningful because the structure is already open. Three main mechanisms were employed: (1) introducing asymmetry in the structure so that a radiating component of field is created, (2) foreshortening some dimension in the cross section, and (3) using a higher mode that is leaky in itself, rather than the bound dominant mode. The mechanism most commonly employed then and today is asymmetry.

Many geometric arrangements can be devised that satisfy the preceding requirements and make use of one of the leakage mechanisms listed, but we must remember that the resulting structures also must be analyzable so that the antennas can be designed systematically and not simply on an empirical basis, as is true for some of the more novel periodic open leaky-wave antennas discussed in the preceding subsection. All the uniform open antennas described in this section have been analyzed accurately, and theoretical expressions for their design are available in the literature. Most of the antennas discussed here are due to Oliner, as part of a systematic cooperative investigation with principal colleagues Lampariello of Italy and Shigesawa of Japan. Summaries of their contributions appear in two books 52,67 and in a review article 68; details are contained in individual papers referenced later and in a comprehensive two-volume report. 69

Early Structure: Asymmetrical Trough Waveguide Antenna

The first open waveguide that was made leaky by introducing asymmetry in the cross section was the trough waveguide. The antenna structure, shown in Fig. 10-17 in full view and in cross section, was invented and measured by Rotman⁷⁰ and analyzed by Oliner⁷¹ about 30 years ago. It was a practical antenna, widely used, and it is still useful today. It appears to be the only early example of the class of uniform leaky-wave antennas based on open waveguides.

The trough waveguide itself, when operated as a nonradiating transmission structure, is symmetrical about the center fin and is derived from symmetrical strip transmission line by placing a short-circuiting plate at its midplane. The dominant mode in the



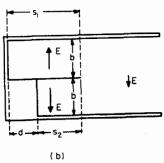


FIG. 10-17 The uniformly asymmetrical trough waveguide antenna. (a) Full view. (b) Cross section for zero-thickness center fin showing the electric field orientations. [After Rotman and Oliner, 71 © 1959 IRE (now IEEE).]

trough waveguide is therefore identical with the first higher mode in strip line. Trough waveguide therefore combines the mechanical simplicity of a strip line with the frequency characteristics of a waveguide, and its bandwidth for single-mode propagation is greater than that for rectangular waveguide by about 50 percent. It also can be coupled smoothly to a coaxial line, a feature that makes it convenient for use at lower frequencies.

Despite the fact that trough waveguide is open on one side, it is nonradiating when the structure is symmetrical. The introduction of asymmetry, however, will produce radiation in a leaky-wave fashion. In fact, one virtue of this type of leaky-wave antenna is the simple means by which radiation can be controlled. The asymmetry can be varied, for example, by placing a metal insert in one of the halves of the line, as shown in Fig. 10-17, and adjusting its thickness d.

A theoretical analysis⁷¹ employing transverse resonance together with a perturbation treatment yields the following simple expressions for the leaky-wave propagation characteristics:

$$\frac{\lambda}{\lambda_g} = \frac{\lambda}{\lambda_{g0}} - \frac{\lambda}{2\pi} \frac{\lambda_{g0}}{\lambda_{c0}} \operatorname{Re} (\Delta \kappa)$$
 (10-31)

and
$$\alpha = \frac{\lambda_{g0}}{\lambda_{c0}} \operatorname{Im} (\Delta \kappa)$$
 (10-32)

where
$$\operatorname{Re}(\Delta \kappa) = \frac{\pi d}{4L_1L_2} \left(1 - \frac{d}{L_1 + L_2} \right)$$
 (10-33)

and Im
$$(\Delta \kappa) = \frac{(\pi d)^2}{8L_1L_2(L_1 + L_2)}$$
 (10-34)

with
$$L_1 = s_1 + \frac{2b}{\pi} \ln 2$$
 (10-35) and $L_2 = s_2 + \frac{2b}{\pi} \ln 2$

The structural dimensions s_1 , s_2 , d, and b are indicated in Fig. 10-17; λ_{c0} and λ_{s0} are the cutoff wavelength and guide wavelength, respectively, of the symmetrical and therefore nonradiating trough waveguide.

These expressions have been found to give rather good agreement with measured values, 71 especially for narrow radiated beams. For wider beams, it is better to use the transverse resonance expression itself (without the perturbation simplifications), which is also given and derived in Ref. 71. Numerical data for various parameter combinations, and corrections to be made for center fins of appreciable thickness, are also found in this reference.

An interesting antenna that can be scanned through broadside is produced by varying the asymmetrical base periodically between alternate sides of the center fin and adding small posts in a periodic fashion. This modification of the asymmetrical trough waveguide antenna just discussed is illustrated in Fig. 10-18. The structure is no longer an example of an antenna based on a uniform open waveguide but is more in the class of the periodic open antennas treated in Sec. 10-6. It is actually even closer to the family of slot arrays because the period is about a half-guide wavelength long and the blocks are alternated to suppress the n=0 space harmonic and permit only the n=-1 space harmonic to radiate. The additional posts are of particular note because they introduce compensating reactances that permit the beam to scan through broadside without the usual pattern and input impedance deterioration at exactly broadside suffered by both slot arrays and the periodic antennas discussed in Sec. 10-6. Further details concerning the design of this antenna are given in Refs. 71 and 72. The latter reference also contains design information on other variations that can produce radiation from the trough waveguide structure.

Foreshortened-Top NRD Guide Antenna

Nonradiative dielectric (NRD) guide is a low-loss open waveguide for millimeter waves that was first proposed and described in 1981.⁷³ It is a modification of H guide where the spacing between the metal plates is less than $\lambda_0/2$ so that all junctions and discontinuities

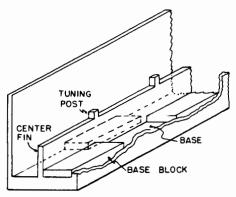


FIG. 10-18 Modifications in the asymmetrical trough waveguide antenna shown in Fig. 10-17, by alternating the asymmetrical base blocks periodically and introducing tuning posts, in order to permit scanning through broadside. [From Rotman and Oliner, 71 © 1959 IRE (now IEEE).]

that maintain symmetry become purely reactive instead of possessing radiative content. The waveguide structure is shown on the left-hand side of Fig. 10-19. The dielectric material in the center portion confines the main part of the field, and the field decays exponentially in the vertical direction in the air region away from the dielectric-air interfaces. Two new leaky-wave antennas are based on this waveguide: the foreshortened-top NRD guide antenna and the asymmetrical NRD guide antenna. The former antenna is discussed now, and the latter one is treated in the next subsection.

When the vertical metal plates in the NRD guide are sufficiently long, as shown on the left-hand side of Fig. 10-19, the dominant mode field is completely bound, since the field has decayed to negligible values as it reaches the upper and lower open ends. If the upper portion of the plates is foreshortened, as seen on the right-hand side of Fig. 10-19, the field is still finite at the upper open end (but negligible at the lower open end). A traveling-wave field of finite amplitude then exists along the length of the upper open end,

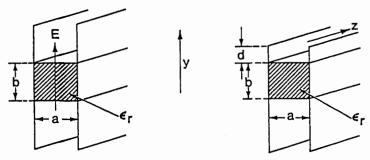


FIG. 10-19 The nonradiative dielectric (NRD) guide, on the left-hand side, and the foreshortened-top leaky-wave antenna based on it, on the right-hand side. (After Sanchez and Oliner, 74 © 1987 IEEE.)

and, if the dominant NRD guide mode is fast (it can be fast or slow depending on the frequency), power will be radiated away at an angle from this open end.

An accurate theory was developed by Sanchez and Oliner, ⁷⁴ in which an accurate transverse equivalent network was developed for the cross section of the antenna, and the dispersion relation for the values of α and β was obtained from the resonance of this network. All the elements of this dispersion relation are in closed form, thus permitting easy calculation. The leakage constant α is determined simply by the amount of foreshortening, measured by d, and β is essentially unaffected by changes in d unless d becomes very small. Thus, α and β can be adjusted independently, to a great extent, which is very desirable because the procedure for sidelobe control is then simplified.

Careful measurements were taken by Yoneyama⁷⁵ at 50 GHz, and by Han, Oliner, and Sanchez⁷⁶ in the vicinity of 10 GHz on a scaled structure. Excellent agreement between measurement and theory was found over the range of parameter values examined, and results for one case are given on Fig. 10-20. One also can see that α can be varied over an extremely wide range, permitting narrow beams or wide beams, simply by altering the value of d.

The amplitude distribution in the radiating aperture can be controlled by varying the distance d as a function of the longitudinal coordinate z. This may be accomplished either

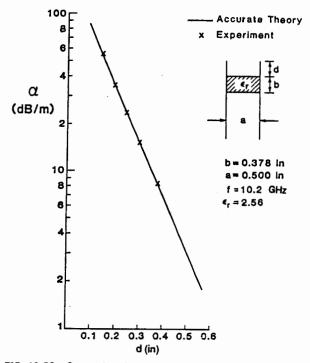


FIG. 10-20 Comparison between measurement and theory for the leakage constant as a function of the length d of the foreshortened top for the NRD guide leaky-wave antenna shown in Fig. 10-19. (From Han, Ollner, and Sanchez, 6 © 1987 IEEE.)

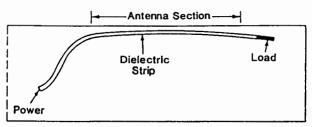


FIG. 10-21 Side view of the foreshortened-top NRD guide leakywave antenna, showing how the value of α can be tapered very easily to reduce the sidelobes. (*From Sanchez and Ollner*, ⁷⁴ © 1987 IEEE.)

by appropriately shaping the upper edge of the metal plates or by slightly curving the dielectric strip so that its distance from the edge of the plates varies in a prescribed fashion with z; the edge in this case would be straight. The latter procedure leads to a very simple and easy-to-build antenna configuration, which is indicated in Fig. 10-21. Furthermore, the antenna is directly compatible with transmit and receive circuits designed in NRD guide technology. The antenna radiates with vertical polarization in the principal plane.

Asymmetrical NRD Guide Antenna

The leakage mechanism for this NRD guide antenna is different from that for the antenna described above, since this one is based on asymmetry, as shown in Fig. 10-22. The structure is first bisected horizontally to provide radiation from one end only, since the electric field is purely vertical in this midplane, the field structure is not altered by the bisection. An air gap is then introduced into the dielectric region, as shown, to produce asymmetry. As a result, a small amount of net horizontal electric field is created, which produces a mode in the parallel-plate air region akin to a TEM mode. This mode then propagates at an angle between the parallel plates until it reaches the open end and leaks away. It is necessary to maintain the parallel plates in the air region sufficiently long that the vertical electric field component of the original mode has decayed to negligible values at the open end. Then the TEM-like mode, with its horizontal electric field, is the only field left, and the field polarization is then essentially *pure*. (The discontinuity at the open end does not introduce any cross-polarized field components.)

The asymmetry mechanism applied to the NRD guide in this way furnishes another leaky-wave antenna of simple configuration, but now with pure horizontal polarization. The air gap does not have to be large to produce a significant leakage rate. The geometry can thus be controlled easily to achieve a large range of values for α and, therefore, a large range of desired beamwidths. Furthermore, the air gap affects β only slightly, so that β and α can be controlled relatively independently. Of course, the guide must be operated in the fast-wave range to produce radiation.

The theory^{77,78} for this structure employs mode matching at the air-dielectric interfaces, and numerical results were obtained as a function of the geometric parameters. A detailed presentation of the theory and various numerical results appears in Chap. III of a comprehensive report.⁶⁹ No measurements have been taken to verify the theory.

There are many ways in which asymmetry can be introduced; this one was chosen for inclusion here because theoretical results are available for it. Measurements are available

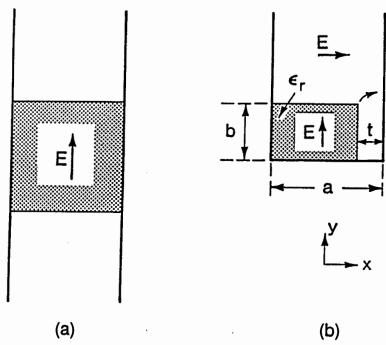


FIG. 10-22 (a) The NRD guide. (b) The asymmetrical NRD guide leaky-wave antenna produced by creating an asymmetrical air gap of thickness t and bisecting the NRD guide horizontally. The modifications introduced in the electric fields are also shown. (From Oliner. 69)

for a structure in which the asymmetry was produced by sloping the upper dielectric-air interface rather than introducing an air gap. The measurements ⁷⁹ showed that radiation indeed occurs and that good patterns result, but parameter optimization has not yet been accomplished and no theory is available.

Some Antennas Based on Groove Guide

Groove guide is a low-loss open waveguide for millimeter waves somewhat similar to the H guide or NRD guide; the dielectric central region is replaced by an air region of greater width. The fields are again strongest in the central region, and they decay exponentially vertically in the regions of narrower width above and below, as summarized in Fig. 10-23.

The earliest leaky-wave antenna based on groove guide employed the mechanism of asymmetry to produce leakage, by placing a narrow longitudinal horizontal metal strip on one of the vertical groove guide walls just outside the central region, parallel to the propagation direction. The strip lay in the exponentially decaying field region and therefore offered only a small perturbation, affecting β only weakly but permitting leakage. A net horizontal electric field was introduced, which excited a TEM mode that in turn propagated at an angle to the open ends and radiated power with horizontal polarization. The location and width of the strip controlled α .

An accurate theory was developed for this antenna, including detailed design

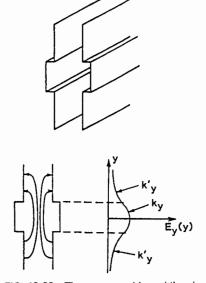


FIG. 10-23 The groove guide and the electric field of its dominant mode. (*From Oliner*. ⁶⁸)

considerations. 80-82 The antenna was not pursued further, however, because it was not easy to fabricate, and other, simpler structures followed soon after it. It nevertheless established an approach and served to focus thinking.

The next antenna based on groove guide is called the L-shaped antenna. This antenna turns out to be the simplest in configuration, but also one that lacks versatility. It exploits the fact that all groove-guide higher modes are leaky and is based on the first higher antisymmetric mode. The electric field of that higher mode is sketched on the full groove guide on the far left of Fig. 10-24. Because of the symmetry of the structure and the directions of the electric field lines, the structure can be bisected twice to yield the greatly simplified structure on the far right. The final structure is seen to resemble an L with an open top. The L-shaped structure also may be viewed as a rectangular waveguide with a large off-

center stub fed by its dominant mode, but it was not derived from that direction.

The L-shaped antenna has been analyzed theoretically, and numerical values have been obtained for its performance characteristics. 80 Details are included in Chap. VI of Ref. 69.

The configuration of the L-shaped leaky-wave antenna is indeed simple, and it can be easily fed when we view it as derived from a rectangular waveguide. It suffers from an important limitation, however, in that it leaks very strongly. This antenna is therefore useful only for applications that require wide beams.

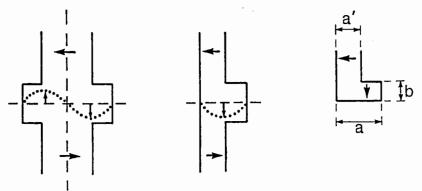


FIG. 10-24 The transition, from left to right, from the n=2 mode (which is leaky) in the full groove guide to the L-shaped antenna. The transition involves two successive bisections, neither of which disturbs the field distributions. The arrows represent electric field directions. (*From Oliner*.⁶⁹)

The next challenge to be addressed was how to devise a structure that would retain most of the simplicity of the L-shaped antenna but provide the versatility with respect to beamwidth that the L-shaped structure lacked. The answer was found in what was originally called the offset-groove-guide antenna. The offset groove guide itself is defined in Fig. 10-25, where it is also seen that net horizontal electric field lines are created by the offset that will result in power leakage. The final antenna, shown in Fig. 10-26, is created by simply bisecting the offset groove guide horizontally. It also resembles a rectangular waveguide with an offset stub—a point of view that shows how the antenna can be easily fed.

This antenna has many virtues, but it will be discussed in detail in the next subsection under a different name because it is better to view it that way despite how it was derived.

Stub-Loaded Rectangular Waveguide Antenna

The leaky-wave antenna whose cross section is given in Fig. 10-26 was derived from groove guide, and its early name was the offset-groove-guide antenna. Under that name, several presentations were made, 81-83 and a comprehensive description was given in Chaps. VII and VIII of Ref. 69. Numerical results were derived for several different cross-sectional aspect ratios, and some of the best performance was found for an aspect ratio corresponding to that for rectangular waveguide. The structure is also easy to feed from rectangular waveguide. For these reasons, the name was changed to the stub-loaded rectangular waveguide antenna, and a pair of companion papers 84,85 are being written with the new name.

One of the virtues of this antenna is its versatility, which may be understood from the following considerations. When the stub is centered, the structure becomes that of nonradiating groove guide (bisected); alternatively, it may be viewed as a slotted section cut in

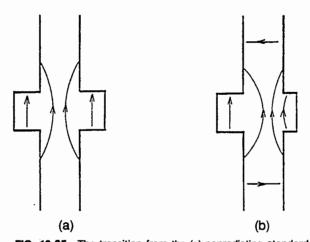


FIG. 10-25 The transition from the (a) nonradiating standard groove guide (dominant mode is bound) to the (b) leaky offset groove guide (dominant mode becomes leaky). (From Ollner. 69)

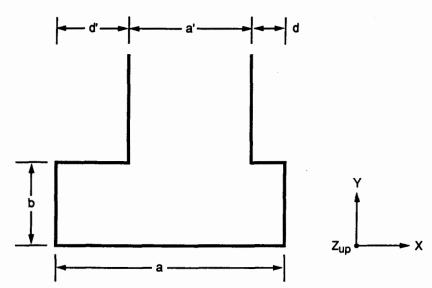


FIG. 10-26 Cross section of the offset-groove-guide antenna after bisecting the structure on the right-hand side of Fig. 10-25 to ensure radiation in the upward direction only. This antenna was later called the stub-loaded rectangular waveguide antenna. (*From Oliner*. ⁶⁹)

rectangular waveguide. When the stub is placed all the way to one end, the result is the L-shaped structure that was found to radiate very strongly. Thus, for small off-center positions of the stub, the leakage rate will be small, yielding radiated beams of narrow width. When the offset is increased, α will increase, and the beamwidth will increase. We therefore have a relatively simple leaky-wave antenna, easily fed from a rectangular waveguide, that permits great versatility with respect to beamwidth by simply adjusting the location of the stub guide.

In addition, it is found that the value of β changes very little as the stub is moved and α varies over a very large range. This feature, β remaining almost constant while α varies, makes it easy to taper the antenna aperture to control sidelobes. Thus it should be easy with this antenna to design beams with low sidelobe levels.

An additional advantage follows from the fact that the antenna is filled with only one medium, namely, air. As was shown in Sec. 10-2, the beamwidth then remains constant when the beam is scanned in elevation as one changes the frequency.

The antenna was analyzed using a transverse equivalent network based on a new E-plane T-junction network. 86 This T-junction network is notable in that the expressions for the network elements are all in simple closed form and yet are very accurate. The resulting transverse equivalent network for the antenna is seen in Fig. 10-27. Since the network elements are in closed form, the resonance relation for the complex propagation wave number is also in closed form, making calculations quick and easy.

The expressions for the elements of the network in Fig. 10-27 may be written as

$$\frac{B_a}{Y_0} = -\frac{\pi}{16} \frac{a'}{b} \frac{k_x a'}{2} J_0^2 \left(\frac{k_x a'}{2}\right)$$
 (10-36)

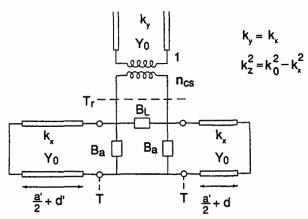


FIG. 10-27 The transverse equivalent network for the antenna structure in Fig. 10-26. Closed-form expressions for the network elements are given in the text.

where J_0 is the Bessel function of zero order,

$$\frac{B_L}{Y_0} + \frac{1}{2} \frac{B_a}{Y_0} = \frac{1}{n_c^2} \left(\frac{k_x b}{\pi} \right) \left[\ln \left(1.43 \frac{b}{a'} \right) + \frac{1}{2} \left(\frac{k_x b}{\pi} \right)^2 \right]$$
 (10-37)

$$n_c = \frac{\sin(k_x a'/2)}{k_z a'/2} \tag{10-38}$$

$$n_{cc}^2 = n_c^2(a'/b) \tag{10-39}$$

$$\frac{B_L}{Y_0} = \frac{1}{n_c^2} \left(\frac{k_x b}{\pi} \right) \left[\ln \left(1.43 \frac{b}{a'} \right) + \frac{1}{2} \left(\frac{k_x b}{\pi} \right)^2 \right]
+ \frac{\pi}{32} \frac{a'}{b} \left(\frac{k_x a'}{2} \right) J_0^2 \left(\frac{k_x a'}{2} \right)$$
(10-40)

so that the dispersion relation for the transverse wave number k_x becomes

$$\frac{1}{n_{cs}^{2}} + j \frac{B_{L}}{Y_{0}} + j \frac{\left[\frac{B_{a}}{Y_{0}} - \cot k_{x} \left(\frac{a'}{2} + d\right)\right] \left[\frac{B_{a}}{Y_{0}} - \cot k_{x} \left(\frac{a'}{2} + d'\right)\right]}{2 \frac{B_{a}}{Y_{0}} - \left[\cot k_{x} \left(\frac{a'}{2} + d\right) + \cot k_{x} \left(\frac{a'}{2} + d'\right)\right]} = 0$$
 (10-41)

where wave number k_x is related to k_z , the result that is needed, by

$$k_z = \beta - j\alpha = \sqrt{k_0^2 - k_x^2}$$
 (10-42)

These expressions, and the transverse equivalent network in Fig. 10-27, assume that the stub guide is infinite in length. In practice, of course, the stub length is finite, and it should only be long enough that the vertical electric field (represented in the stub guide by the below-cutoff TM₁ mode, viewed vertically) can decay to negligible values, permitting essentially pure horizontally polarized radiation. Usually, the stub length need only be about a half wavelength or less if the stub is narrow. The finite stub length can be readily

taken into account, and a detailed treatment of its effects are reported in Ref. 69, but it produces only a small change in the numerical values obtained from the procedure given above.

As an independent check on the accuracy of these expressions, the values of α and β were calculated using an entirely different theoretical approach, that of mode matching. As shown in Fig. 10-28, where the dashed lines represent values obtained using the network and the solid lines represent those derived via the mode-matching procedure, the agreement is seen to be very good. We also can see from this figure that, as the stub is shifted laterally, β remains almost constant as α varies monotonically from zero to large values.

Measurements were also taken of the values of α and β and of the radiation patterns over the frequency range from 40 to 60 GHz.⁸³ A photograph of the cross section of the structure appears in Fig. 10-29. The Japanese 500-yen coin (26.5 mm in diameter) is seen to dwarf the antenna cross section.

Figure 10-30 presents the comparisons between theoretical and experimental values for both α and β , and the agreements are seen to be very good. It is also seen that the proper mode was excited, and not a competing mode, the channel guide leaky mode.

The stub-loaded rectangular guide leaky-wave line-source antenna is thus an attractive structure for millimeter wavelengths, since it is simple in configuration, easily fed, versatile in beam width, suitable for low-sidelobe-level designs, and capable of furnishing essentially pure horizontally polarized radiation. In addition, a simple and accurate theory is available for it that has been verified by an alternative, totally different computational approach, as well as by measurements.

Printed-Circuit Version of Stub-Loaded Rectangular Waveguide Antenna

If the versatile leaky-wave antenna just described could be made in printed-circuit form,

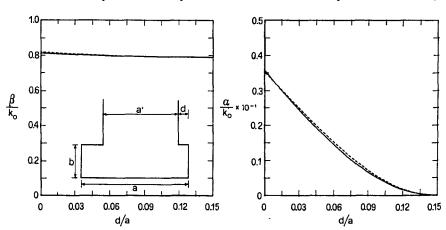


FIG. 10-28 Comparison of numerical results for the offset-groove-guide antenna, later named the stub-loaded rectangular guide antenna, obtained via two completely different theoretical methods. Additionally, we see that by varying the offset d we can change α over a wide range of values while affecting β very little. Such independence makes it easy to taper the aperture distribution in order to control the sidelobes. f = 28 GHz, a = 1.0 cm, a' = 0.7 cm, b = 0.3 cm. (From Oliner. ⁶⁸)

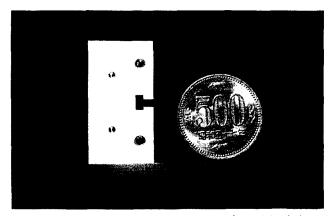


FIG. 10-29 Photograph of the cross section of a stub-loaded rectangular guide antenna that was measured at millimeter wavelengths. A 500-yen Japanese coin (26.5 mm in diameter) is shown for size comparison. (*From Oliner*. ⁶⁹)

the fabrication process could make use of photolithography, and the taper design for sidelobe control could be handled automatically in the fabrication. That is, the location and width of the stub, and their variations along the antenna length in conformity with the sidelobe design requirements, could all be accomplished at the same time by either depositing the metal or etching some away to produce the gap. With this goal in mind, a printed-circuit version of the structure in Fig. 10-26 took the shape shown in Fig. 10-31.

The principal change is that the rectangular guide portion is now dielectric-filled so that the metal widths d' and d and the gap a' can be fabricated photolithographically. Also, the vertical baffle portions are now moved to the sides of the guide, as extensions of the guide side walls.

The basic physics of the leakage is same as that for the antennas in Fig. 10-26. The rectangular guide, now dielectric-filled, is fed from one end with the electric field vertical inside the guide. This vertical E field excites the asymmetrically located longitudinal slot such that the resultant field in the slot has both vertical and horizontal components. These field components in turn excite the TM_1 mode (viewed vertically) and the TEM mode (at an angle), respectively, in the parallel-plate air-filled stub region. The separation a between the stub walls is less than a half wavelength, so that the TM_1 mode is below cutoff; the TEM mode, being above cutoff, propagates at an angle to the upper end and radiates. The stub dimension c must then be sufficiently long that the field in the TM_1 mode can decay to negligible values. As a result, the radiated power is polarized horizontally, with negligible cross-polarization. It would be nice to eliminate the vertical stub walls, but they are necessary for eliminating the vertical electric field component.

The transverse equivalent network for this new antenna structure is slightly more complicated than the one in Fig. 10-27, and the expressions for the network elements must be modified appropriately to take the dielectric medium into account. The modified network appears in Fig. 10-32, and the expressions for the corresponding network elements are

$$\frac{B_a}{Y_{0m}} = -\frac{\pi}{16} \frac{a'}{b} \left(k_x \frac{a'}{2} \right) J_0^2 \left(k_x \frac{a'}{2} \right)$$
 (10-43)

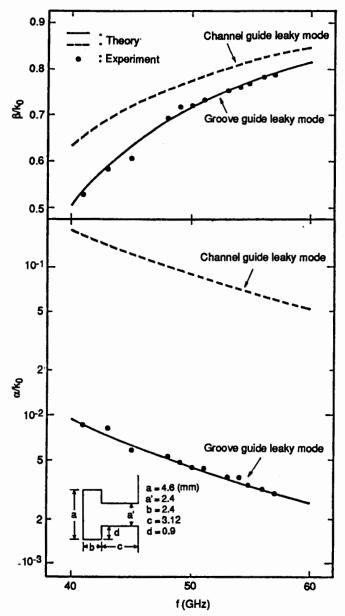


FIG. 10-30 Comparisons between theoretical and measured values of the propagation properties of the antenna shown in Fig. 10-29 over a wide frequency range, from 40 to 60 GHz. Also shown is the theory for a possible competing mode, indicating that the measured mode is indeed the desired one. (From Oliner. 69)

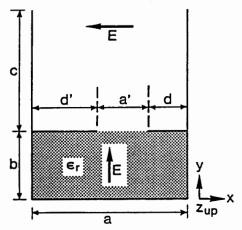


FIG. 10-31 Printed-circuit version of the stubloaded rectangular guide antenna shown in Fig. 10-26. This version has the advantage that the tapering to control sidelobes can be effected photolithographically all at one time. (After Ollner. ⁶⁹)

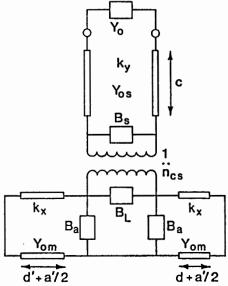


FIG. 10-32 Transverse equivalent network for the printed-circuit antenna in Fig. 10-31, which is a modification of that in Fig. 10-27, to account for the dielectric filling of the feed rectangular guide. (From Ollner. 69)

$$\frac{B_L}{Y_{0m}} = \frac{\epsilon_r}{n_c^2} \left(\frac{k_x b}{\pi}\right) \left[\ln\left(1.43 \frac{b}{a'}\right) + \frac{1}{2} \left(\frac{k_x b}{\pi}\right)^2 \right] + \frac{\pi}{32} \frac{a'}{b} \left(k_x \frac{a'}{2}\right) J_0^2 \left(k_x \frac{a'}{2}\right)$$
(10-44)

with

$$n_c = \frac{\sin(k_x a'/2)}{k_x a'/2} \tag{10-45}$$

$$\frac{B_s}{Y_{0s}} = \frac{k_y b}{\pi} \ln \left[\csc \frac{\pi a'}{2a} \csc \frac{\pi}{2a} (a' + 2d') \right]$$
 (10-46)

$$n_{cs} = n_c \sqrt{a/b} \tag{10-47}$$

where n_c is given by Eq. (10-45).

$$Y_{0x}/Y_{0m} = k_y/k_x \tag{10-48}$$

$$k_x^2 = k_0^2 \epsilon_r - k_z^2$$
 (10-49)

$$k_{\nu}^2 = k_0^2 - k_{\tau}^2 \tag{10-50}$$

The stub and main guides are no longer the same, so their wave numbers and characteristic admittances are also different, as indicated above. As in the previous antenna, the network in Fig. 10-32 assumes that the stub length is infinite. However, as before, the numerical values change little for finite stub length, and an appropriate value for that length is about a half wavelength or so, depending on the width of the stub region. The detailed derivation of these expressions appears in Chap. X of Ref. 69.

Again, α can be varied by changing the slot location d. However, it was found that a' is also a good parameter to change for this purpose. The variations in beam-elevation angle θ_m and beamwidth $\Delta\theta$ with relative slot width a'/a are presented in Fig. 10-33. One

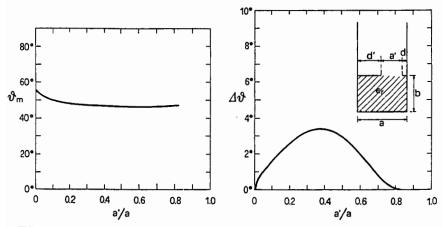


FIG. 10-33 Variations of the beam angle θ_m and the beamwidth $\Delta\theta$ as a function of relative slit width for the printed-circuit structure in Fig. 10-31. It is seen that as a'/a varies from about 0.4 to about 0.8 the beamwidth changes over a wide range while the beam angle remains almost constant, showing that a' is a good parameter to vary in order to reduce the sidelobes. f=50 GHz, $\epsilon_r=2.56$, a=2.25 mm, b=1.59 mm, d=0.20 mm. (From Oliner.99)

can see that, as a'/a varies from about 0.4 to about 0.8, the beamwidth changes from about 4° to nearly zero but that the beam location moves hardly at all over that range. Slot width a' therefore represents a good parameter to vary in order to control the sidelobes.

This antenna structure has not yet been examined experimentally, but it appears to be a very promising one.

Asymmetrical Slitted Ridge Waveguide Antennas

An interesting variation of the structures shown in Figs. 10-26 and 10-31 has been developed and analyzed recently.⁸⁷ It is based on a ridge waveguide rather than a rectangular waveguide; the structures, both air-filled and dielectric-filled, respectively, are shown in Fig. 10-34a and b. In the structures based on rectangular waveguide, the asymmetry was achieved by placing the stub guide, or locating the longitudinal slot (or slit), off-center on the top surface. Here the top surface is symmetrical, and the asymmetry is created by having unequal stub lengths on each side under the main guide portion.

The transverse equivalent networks shown in Figs. 10-27 and 10-32, together with the associated expressions for the network elements, were adapted and extended to apply to these new structures. Using this approach, numerical values were obtained for a variety of parameter modifications.

An analysis of the antenna behavior indicates that this geometry effectively permits independent control of the angle of maximum radiation (θ_m) and the beamwidth $(\Delta\theta)$. Let us define two geometric parameters: (1) the relative average arm length b_m/a , where $b_m = (b_l + b_r)/2$, and (2) the relative unbalance $\Delta b/b_m$, where $\Delta b = (b_l - b_r)/2$. See Fig. 10-34 for the indicated lengths b_l and b_r . It then turns out that by changing b_m/a one can adjust the value of β/k_0 without altering α/k_0 much and that by changing $\Delta b/b_m$ one can

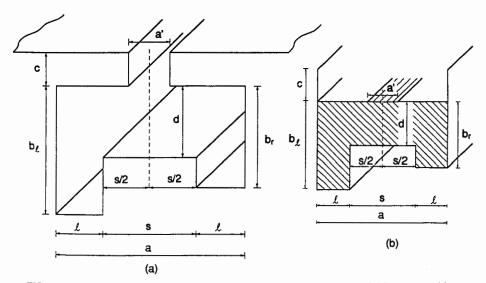


FIG. 10-34 Uniform leaky-wave antennas based on slitted asymmetrical ridge waveguide, where the values of α and β can be varied essentially independently by adjusting combinations of the vertical stubs b_r , and b_r , as described in the text. (*From Frezza, Guglielmi, and Lampariello*, ⁸⁷ © 1993 IEEE.)

vary α/k_0 over a large range without affecting β/k_0 much. In this way, by changing only the stub lengths, one can exercise essentially independent control over β and α . The taper design for controlling the sidelobe level would therefore involve only the relative unbalance, $\Delta b/b_m$.

The air-filled structure (Fig. 10-34a) may therefore have a constructional advance regarding sidelobe control over the simpler structure shown in Fig. 10-26. However, the dielectric-filled antenna, in Fig. 10-34b, lacks the important advantage offered by the printed-circuit version in Fig. 10-31, for which one can make a mask that permits the whole upper surface, including the taper for sidelobe control, to be realized photolithographically.

10-8 ARRAYS THAT SCAN IN TWO DIMENSIONS

All the leaky-wave antennas discussed so far in this chapter are line-source antennas. They can scan in elevation (or azimuth if they are rotated, of course) as the frequency is varied, with their beamwidths narrow in elevation but wide in the cross-plane. General comments along these lines were made above, and it was pointed out that the beamwidth in the cross-plane could be narrowed by using a horn or by arranging a parallel set of these line sources in an array. Such arrays, however, do not scan in the cross-plane.

This section describes the most recent development involving leaky-wave antennas, where an array of leaky-wave line sources is so arranged that it can scan in both elevation and azimuth. Such an array is really a linear phased array of leaky-wave line-source antennas, where scanning in elevation is obtained in the usual leaky-wave fashion by varying the frequency, and scanning in the cross-plane (or azimuth) is achieved by varying the phase difference between the successive parallel leaky-wave line sources. The approach itself is not new, but the specific structures are. As will be seen, these arrays have some unusual virtues: essentially no cross-polarization, no grating lobes, no blind spots within the scan volume, and simplicity of structure. In addition, they should cost less than phased arrays because phase shifters are needed in only one dimension. Three different array structures are discussed, but first we present the principle of operation (the basic architecture for such arrays) and some comments about the analytical approach, which takes into account all mutual coupling effects.

Principle of Operation

This class of scanning arrays achieves scanning in two dimensions by creating a onedimensional phased array of leaky-wave line-source antennas. The individual line sources are fed from one end and are scanned in elevation by varying the frequency (or by electronic means if and when available). Scanning in the cross-plane, and therefore in azimuth, is produced by phase shifters arranged in the feed structure of the onedimensional array of line sources. This frequency-phase scan architecture is illustrated schematically in Fig. 10-35.

The radiation will therefore occur in pencil-beam form and will scan in both elevation and azimuth in a conical-scan manner. The spacing between the line sources is chosen such that no grating lobes occur, and accurate analyses show that no blind spots appear anywhere. The leaky-wave line-source antennas employed in the three examples of arrays described here are ones we have already discussed earlier or are modifications of

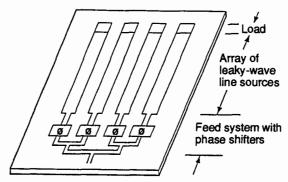


FIG. 10-35 Schematic of the recent approach to simpler two-dimensional scanning, involving a linear phased array of leaky-wave line sources, with frequency scanning in elevation and phase scanning in azimuth. (From Oliner. 65)

them. They also offer suitability for millimeter wavelengths because they are simpler in structure and are based on low-loss waveguides. The advantage of negligible cross-polarization at all angles follows from the fact that the individual line-source antennas possess that feature and that the array arrangement does not introduce any cross-polarized components.

In principle, a large variety of different leaky-wave line sources can be used in this array architecture. In fact, however, one must be very selective here, because the line sources must be integrated into the overall geometry if the resulting antenna is to remain simple in configuration. The list is further limited to those structures amenable to analysis because systematic design requires a theoretical basis. If the radiating portion of a suitable structure in this class can be fabricated by photolithographic means, using a mask, the costs can also be kept down, and the method is amenable to mass-production techniques. Two of the three arrays to be described fall into this category.

Analytical Approach

The arrays to be described have been analyzed accurately by a unit-cell approach that takes into account all mutual coupling effects. Each unit cell incorporates an individual line-source antenna, but in the presence of all the others. These individual line-source antennas were analyzed using a transverse equivalent network in which the radiating open end was representative of the environment of the single lone line source. In the array of such line sources, the radiating environment is, of course, quite different, and it will, in fact, change as the array is scanned in azimuth.

The treatment of the periodic external environment by a unit-cell approach automatically accounts for all mutual coupling effects and provides information on all the effects of scan. The radiating termination on the unit cell modifies the transverse equivalent network, and the resonances of this transverse network yield the properties of the leaky wave guided along the line sources. A key new feature of the array analysis is therefore the determination of the active admittance of the unit cell in the two-dimensional environment as a function of scan angle. This active admittance is the input admittance to the external radiating region, and it is appended to the remainder of the

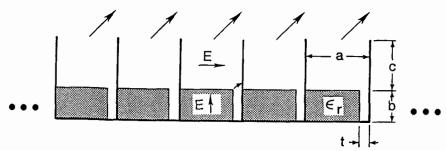


FIG. 10-36 Cross section of linear phased array of asymmetrical NRD guide leaky-wave line sources. The individual line source appears in Fig. 10-22. (From Oliner.®)

transverse equivalent network, the latter being different for each of the arrays to be discussed.

Array of Asymmetrical NRD Guide Line Sources

A cross-sectional view of the linear phased array of asymmetrical NRD guide leaky-wave line sources appears in Fig. 10-36. By comparison with the individual line-source antenna in Fig. 10-22, it is clear that the array consists of a number of these line sources placed directly next to each other. The line sources provide the elevation pattern, modified by their presence in the array, and the geometry in the plane shown specifies the cross-plane

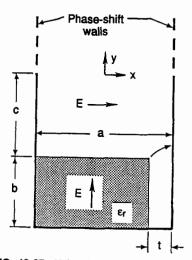


FIG. 10-37 Unit cell of the linear array of NRD guide line-source antennas shown in Fig. 10-36. The phase-shift walls change with scan angle, and their use leads to an analytical approach that takes all mutual coupling effects into account automatically. (From Oliner. 9)

behavior, with the angle of scan determined by the phase shift imposed between successive line sources.

The unit cell for this array is shown in Fig. 10-37, where the phase-shift-wall properties depend on the scan angle in the cross-plane. Thus the discontinuity at the end of the stub of length c, and therefore the values of β and α , depend on that scan angle. The analysis proceeds, therefore, by knowing the imposed phase shift between line sources, and, from it and the unit-cell network, by finding β and α in the axial direction. Everything else follows directly from this information.

If the values of β and α did not change with phase shift, the scan would be exactly conical. However, it is found that these values change only a little, so that the deviation from conical scan is small.

We next consider whether or not blind spots are present. Blind spots refer to angles at which the array cannot radiate or receive any power; if a blind spot occurred at some angle, therefore, the value of α would rapidly go to zero at that angle of

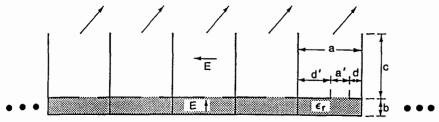


FIG. 10-38 Cross section of the linear phased array of printed-circuit *uniform* leaky-wave line sources. The individual line source appears in Fig. 10-31. (From Lampariello and Oliner. 89)

scan. To check for blind spots, we would then look for any sharp dips in the curves of α/k_0 as a function of scan angle. No such dips were ever found. Typical data of this type exhibit fairly flat behavior for α/k_0 until the curves drop quickly to zero as they reach the end of the conical scan range, where the beam hits the ground.

The theoretical analysis and many numerical results appear in Chap. IV of Ref. 69. A presentation was made, 88 and a paper is in the process of being written.

Array of Printed-Circuit Uniform Line Sources

If the leaky-wave line sources in the array were in printed-circuit form, the fabrication process could make use of photolithography, and the taper design for sidelobe control could be handled automatically in the fabrication. The array structure shown in Fig. 10-38 fits into this category. It may be seen that the line-source elements in this array are exactly the printed-circuit version of the stub-loaded rectangular waveguide antenna appearing in Fig. 10-31. The leakage rate, and therefore the beamwidth, can again be controlled by varying the width or location of the gap within each element. And again, the value of β remains almost constant as the gap width or location is varied, so that a taper design for sidelobe control is easy to implement.

The metal fins that project vertically, which may alternatively be called *baffles* or *stubs*, serve two purposes. The first purpose is to ensure *essentially pure horizontally polarized radiation*, with negligible cross-polarization. As explained in the discussion associated with Fig. 10-31, the fins form a stub guide that is below cutoff for the vertical electric field, thereby permitting only the horizontal electric field to radiate.

The second purpose of the stubs is to *eliminate blind spots*. With the stubs present, we have never found any, and it is known that arrays of this sort with dielectric layers often exhibit them when there are no stubs. A careful examination shows that the stub length should be roughly a half wavelength, which means that the projection is actually rather small, particularly at millimeter wavelengths.

The transverse equivalent network for the unit cell representing the array in Fig. 10-38 is very similar to the one in Fig. 10-32 for the isolated line-source antenna, and differs from it only in the terminating admittance placed on the end of the stub line. This difference is important, however, in that the terminating admittance is a function of scan angle and takes into account the mutual coupling effects of all the neighbors in the array.

As in the case of the array of asymmetrical NRD guide line sources, the value of β/k_0 changes very little with the phase shift between successive line sources, so that, as a result, there is little deviation from conical scan. Also, the curve of α/k_0 as the phase shift is changed does not show any sharp dips but remains fairly flat until it drops as the beam approaches the ground at the end of the scan range. Thus no blind spots have ever been



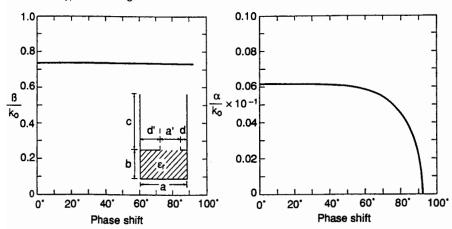


FIG. 10-39 Variations of the normalized phase constant and leakage constant with crossplane scan for the array appearing in Fig. 10-38, showing conical scan and no blind spots. f = 50 GHz, $\epsilon_r = 2.56$, a = 2.25 mm, a' = 1.00 mm, b = 1.59 mm, c = 6.00 mm, d = 0.25 mm. (From Lampariello and Ollner. Fe)

observed. Calculated curves for one set of geometric parameters that demonstrate this behavior are given in Fig. 10-39.

A summary of the results obtained for this array appears in Ref. 89; further results and the details of the theoretical derivation are contained in Chap. X of Ref. 69. In addition, a pair of papers is in the process of being written.

Array of Printed-Circuit Periodic Line Sources

The purpose of employing arrays with *periodically* loaded leaky-wave line sources, instead of *uniform* ones like the two discussed above, is *to increase the scan-angle coverage*, as will be explained. An example of such an array is given in Fig. 10-40. This array can be fed by using a series of dielectric-filled rectangular guides placed on their sides, so that the periodic elements are excited with a horizontal electric field and the array will radiate with pure horizontal polarization.

The individual leaky-wave line sources in this array may at first look like the periodic metal-strip antenna shown in Fig. 10-2 and discussed in Sec. 10-6, but they are not the same because these are excited by a horizontal electric field, parallel to the strips, whereas the antenna in Fig. 10-2 is excited by an electric field that is primarily vertical.

The structure in Fig. 10-40 is shown with stub guides, or baffles, present. For this array, the stubs are not necessary to ensure pure horizontally polarized radiation because no component of vertical field is excited. On the other hand, they also ensure that no blind spots will occur. It is possible that no blind spots will be present when the stubs are removed, but we do not know the answer. Certainly, the structure is simpler and easier to fabricate without the stubs. Either way, the printed-circuit nature of the strips on the dielectric surface permits the detailed metal circuit, including the tapering for sidelobe control, to be deposited photolithographically on the dielectric surface.

As discussed elsewhere in this chapter, leaky-wave antennas with uniform apertures can radiate only into the forward quadrant, and they cannot scan too close to broadside or end fire. In the present periodically loaded array, the dominant mode is chosen to be slow

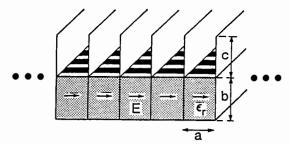


FIG. 10-40 Linear phased array of printed-circuit *periodic* leaky-wave line sources, which is capable of a greater scan range than is possible with the arrays containing uniform line sources. (From Oliner. 69)

so that it is purely bound; the period is then selected relative to the wavelength so that only the n=-1 space harmonic becomes radiating. As a result, the array provides greater scan coverage, since the n=-1 beam can scan over the complete backward quadrant and part or all of the forward quadrant, depending on the parameters (except for a narrow angular region around broadside).

In the design of this array, it should be remembered that these small slits radiate very weakly. The discussion with respect to both theory and numerical results in Chap. XI of Ref. 69 is restricted to such narrower slits and, therefore, narrower beams. A presentation on this antenna was given, 90 and a paper is being written that incorporates results for wider beams.

The three arrays described above are examples of how a linear phased array of leaky-wave line sources can be arranged to provide two-dimensional scanning of a pencil beam over a restricted sector of space. In addition, these three arrays possess certain special virtues. They provide essentially pure horizontally polarized radiation, and they exhibit no blind spots or grating lobes.

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Long-Wire Antennas

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11-2	Single Long whe as a Onk Radiator 11-2						
	Radiation Patterns 11-2						
	Equations for the Field-Strength						
	Patterns 11-5						
11-3	Horizontal Rhombic Antenna 11-7						
11-4	Stereographic Computing Aids 11-10						
11-5	Optimum Design and Bandwidth for Horizontal						
	Rhombic Antennas 11-11						
11-6	Land-Saving Arrangements for Multiple						
	Rhombic Antennas 11-12						
11-7	Sidelobe Reduction and Gain Improvement						
	with Double-Rhomboid Antennas 11-12						

11-8 Importance of Physical and Electrical

11-12 Terminating Resistance and Terminal-Power

11-14 Beverage Receiving Antenna for Low Frequencies 11-17

Symmetry 11-13
11-9 Crosstalk between Feeders 11-14
11-10 Circuital Properties of Rhombic
Antennas 11-15
11-11 Feed-Point Impedance 11-15

Loss 11-15
11-13 Rhombic Arrays 11-16

11-1 Introduction 11-2

11-1 INTRODUCTION

Long-wire antennas were in active development during the height of the high-frequency era, before 1940, and many different forms evolved. Since then development has been quiescent, the only surviving extant form being the horizontal rhombic antenna. Its continued popularity stems from its simple construction, low cost, and wideband capabilities. The rhombic antenna is uniquely adapted to the propagation of high frequencies via the ionosphere. Such later developments as have occurred have been in methods of engineering design either by graphical methods or by machine computation.

The configurations comprising many obsolete long-wire antennas, including the vertical Franklin arrays and the resonant horizontal types, are now history and can be found in the literature.

Some space in this chapter will be devoted to the Beverage antenna, which has desirable applications to the directive reception of low and very low frequencies.

11-2 SINGLE LONG WIRE AS A UNIT RADIATOR

Radiation Patterns

The following basic facts about the radiation patterns of long wires isolated in free space with idealized natural current distributions are useful for reference:

- 1 There is a lobe in the radiation pattern for each half wavelength of wire length. Each lobe is a cone of radiation centered on the wire.
- 2 With respect to the middle of the wire as center of the polar radiation pattern, half of the lobes are tilted forward and half of them backward. If the wire is an odd number of half wavelengths long, there is an odd number of lobes; so one of them will be normal to the wire.
- 3 The direction of the electric field reverses in each successive lobe. This is analogous to the reversals of phase of the currents in successive half-wavelength portions of the wire.
- 4 Between successive lobes are regions of little or no radiation, called nulls or zeros. Practically, these are minima because the field strengths at these angles never actually go to zero. These zeros are related analogously to the current zeros in the standing-wave current distribution or to the phase reversals in a traveling-wave distribution.
- 5 The angles of the zeros are symmetrically distributed about the plane normal to the middle of the wire.
- 6 For a given electrical length, the angles of the zeros are the same for both standing- and traveling-wave current distributions.
- 7 In the first quadrant the angles of the maxima for both current distributions are virtually coincident. The only exception applies to the direction of the main (first) lobe for wire lengths less than three wavelengths, as may be seen in Fig. 11-1.

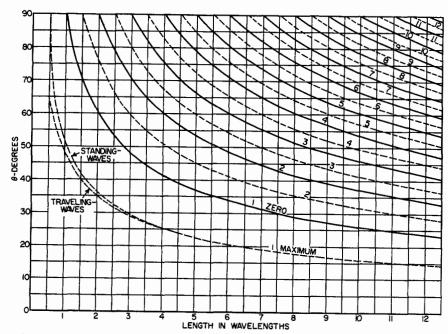


FIG. 11-1 Angles of maxima and zeros in the radiation patterns for isolated long wires with natural current distribution.

- 8 The largest lobe in the radiation pattern is the one forming the smallest angle (θ_1) to the wire. For the traveling-wave case, this lobe is in the direction of current flow only. For the standing-wave case the radiation pattern is symmetrical with respect to the middle of the wire and so has a complementary major lobe toward the other end of the wire.
- With a standing-wave current distribution an integral number of half wave-lengths long, the envelope of the polar plot of the field-strength distribution pattern is a straight line parallel to the wire or, more correctly, a concentric cylinder. For a nonintegral number of half wavelengths, the middle lobes are further decreased in amplitude. The maximum depression of inner lobes occurs when the current distribution consists of an odd integral number of quarter wavelengths (Fig. 11-2).
- With traveling waves, the field-strength pattern has lobes of diminishing amplitude, the smallest being in the direction opposite that of current flow.
- 11 Typical deviations from idealized current distributions modify the relative lobe amplitudes slightly and fill in the zeros slightly but do not affect the angles of the maxima or the zeros in the radiation pattern.
- 12 The ratios of the amplitudes of successive lobes are higher for a traveling-wave system than for the equivalent standing-wave system (compare Figs. 11-3 and 11-4).

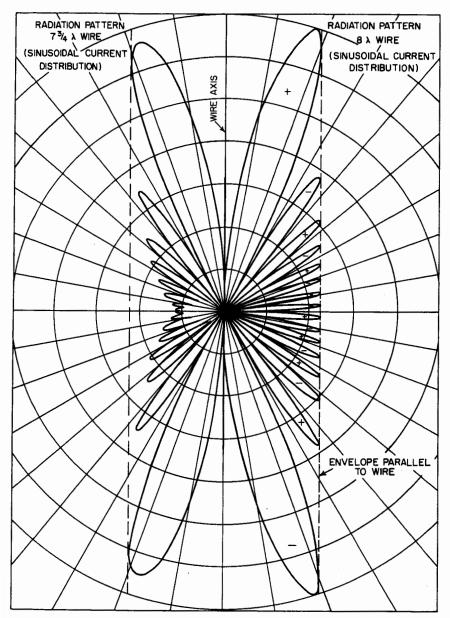


FIG. 11-2 Comparison between the polar radiation patterns of 7.75 λ - and an 8 λ -long wire with standing-wave current distribution, in terms of relative field strength.

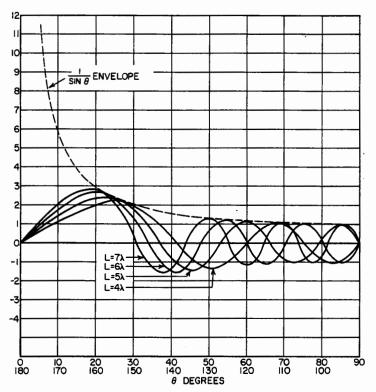


FIG. 11-3 Field-strength radiation patterns for standing-wave current distributions.

Equations for the Field-Strength Patterns

The far-field pattern for a long straight wire in free space with pure sinusoidal (standing-wave) current distribution is expressed by

$$E_{\theta} = \frac{60I}{r} \left[\frac{1}{\sin \theta} \frac{\cos \left(\frac{\pi L}{\lambda} \cos \theta \right)}{\sin \left(C \right)} \right] \qquad \text{V/m}$$
(11-1)

(Cosine or sine in factor C is used when the number of half wavelengths is odd or even respectively.)

The coefficient (factor A) relates field strength to the antinode current I in amperes and the distance r in meters from the center of the wire. If I is expressed in rms values, the field strengths will also be expressed in rms values. The factor B by itself gives the envelope for the pattern lobes, θ being the angle to the wire axis. Factor C by itself oscillates from +1 to -1 and contains the information about the angles

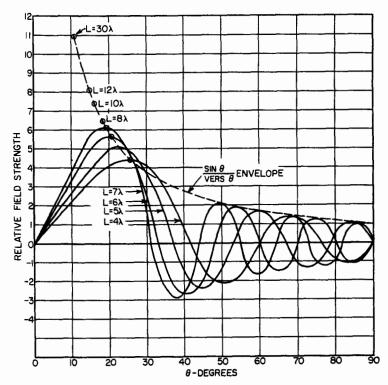


Fig. 11-4 Field-strength radiation patterns for traveling-wave current distributions.

of the zeros in the pattern. B and C together describe the shape of the pattern. The power flow at any angle θ is given by

$$W = \frac{E\theta^2}{377}$$
 = power density, W/m²

For the case of a perfect unattenuated traveling-wave current distribution of any length,

$$E\theta = \frac{60I}{r} \frac{\sin \theta}{\text{vers } \theta} \sin \left(\frac{\pi L}{\lambda} \text{ vers } \theta \right) \qquad \text{V/m}$$
(11-2)

As before, A is a scale factor. Factor B is the envelope factor, with vers $\theta \equiv 1 - \cos \theta$. Factor C ranges in value from +1 to -1 and contains the information on the locations of the lobes and zeros. B and C together describe the complete shape of the pattern.

In these equations L is the wire length in meters and λ the wavelength in meters. Although the C factors in both equations are not identical, they do in fact have iden-

tical zeros, and the first quadrant maxima are virtually coincident, with the exception noted above.

The following equations are more convenient for the determinations of the angles of maxima and zeros in the far-field radiation patterns for long straight wires with traveling-wave current distributions.

For the angles of the series of maxima of diminishing amplitude starting with the largest at θ_{m1} nearest to the forward axis of the wire,

$$\theta_{mm} = \text{hav}^{-1} \frac{K}{2L/\lambda}$$

where K has successive values of 0.371, 1.466, 2.480, 3.486, and 4.495; then $m - \frac{1}{2}$ in order.

For the angle θ_{0m} for the mth zero with respect to the wire axis, from θ_{01} to 180°,

$$\theta_{0m} = \text{hav}^{-1} \frac{m}{2L/\lambda}$$

Haversines [$\equiv (1 - \cos \theta)/2$] are tabulated in *Handbook of Chemistry and Physics*, CRC Press, Boca Raton, Florida, and in many navigation handbooks.

Comparisons between standing-wave and traveling-wave field-strength patterns can be seen in Figs. 11-3 and 11-4, which plot the relative values of E_{θ} from Eqs. (11-1) and 11-2), using factors B and C only. They illustrate some basic differences between the two current distributions.

11-3 HORIZONTAL RHOMBIC ANTENNA

This antenna is constructed as an elevated diamond with sides from two to many wavelengths long. It is used for transmission and reception of high-frequency waves propagated via the ionosphere. When terminated with a resistance equal to its characteristic impedance at its forward apex, it functions as a traveling-wave antenna; the termination suppresses reflections of transmitted power and absorbs signals from the contrary direction.

Figure 11-5 illustrates optimum electrical parameters and the limits of frequency ratios within which performance is not unreasonably compromised. Note that with less than two wavelengths per leg the effectiveness of a rhombic antenna is generally regarded as unacceptable because its gain is too low, and in transmission a high percentage of the input power must be dissipated in a terminal resistor. With legs of seven and eight wavelengths, the terminal loss is down to 18 to 24 percent because of the radiation efficiency of such structures.

A resistance-terminated rhombic becomes essentially a transmission line, but this analogy is compromised by the expansion of the line toward the sides and its reconvergence to the forward apex. To improve the uniformity of distributed line constants and to reduce the rhombic's characteristic impedance to convenient values such as 600Ω , three wires expand from and to each apex on each side. They are at their greatest spread at the sides. The side angles disturb the propagation of currents enough to cause small reflections, but these usually are negligible.

For receiving, many rhombics are made with a single wire for each leg. Such

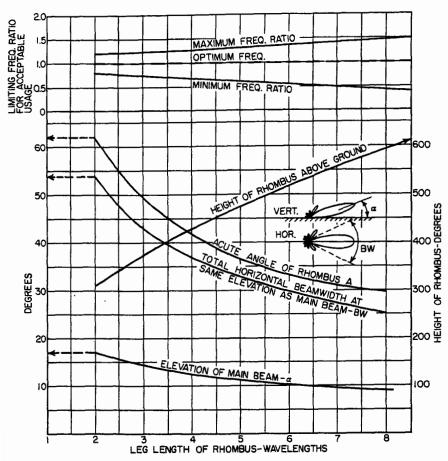


FIG. 11-5 Optimum design parameters for high-frequency horizontal rhombic antennas.

systems have characteristic impedances of the order of 800 Ω . If each apex is impedance-matched to a receiver, the same antenna can serve reciprocal directions.

Unless expense is a controlling factor, most professional operators prefer to use the three-wire rhombus for reception also, especially when the site is subject to severe precipitation static from sandstorms or hard-driven dry snow. In extremely noisy environments it is desirable to use insulated wires for all antenna and transmission lines so that charged particles cannot discharge directly to an exposed metallic surface. The lower impedance also contributes to static-noise reduction.

One can design a horizontal rhombic directly from data plotted in Fig. 11-5. If the design must be compromised for reasons of cost or for land restrictions, the use of stereographic charts enables the engineer to choose options wisely. Table 11-1 provides an idea of the relative amplitudes of the sidelobes for an idealized dissipationless rhombic element of various sizes.

Structures of poles, masts, wires, and standard electrical rigging hardware are

TABLE 11-1	Amplitudes of Secondary Lobes, in Decibels, Relative to a
Fully Formed N	lain Beam, for Free-Space Rhombus

Order of maxima	Order of maxima for second side								
for first side	1	2	3	4	5	6	7	8	9
1	0								
2	5.27	-10.6							
3	-7.7	-12.8	-15.6						
4	-9.0	-14.3	-16.5	-18.0					
5	-10.1	-15.4	-17.6	-19.1	-20.2				
6	-11.0	-16.3	-18.5	-20.0	-21.1	-21.9			
7	-11.7	-17.0	-19.2	-20.7	-21.8	-22.7	-23.4		
8	-12.3	-17.6	-19.9	-21.3	-22.3	-23.3	-24.0	-24.6	
9	-12.9	-18.1	-20.4	-21.9	-23.0	-23.8	-24.6	-25.2	-25.7

used in conventional ways. There is need for a direct ground wire between the center of the terminal resistance and a ground rod to act as a static drain on antenna and feeder.

It is usually not necessary to break up guy wires and stays with insulators. The external fields near the antenna are very weak except in the beam direction.

As a directive antenna, the rhombic is used for power gain. Best gain is realized when the side lengths, height factor, and angles are selected to produce in-phase fields in the desired direction at the design frequency. Gain is degraded at other frequencies. Figure 11-5 provides some guidance on reasonable tolerances. Beyond the indicated frequency ratios, the radiation patterns degrade rapidly.

The realized gain of a receiving rhombic would be identical to that of a transmitting antenna with the same parameters and frequency, provided the incoming equiphase wavefronts were ideally plane and were arriving along the main axis. High-frequency ionospherically propagated waves arrive with all degrees of turbulence and directions of arrival. Therefore, an areally extensive antenna such as a rhombic receives unequal illumination from the incoming waves in its various parts, and the induced currents are not coherent. Typically, then, the realized gain for receiving is highly variable, at moments approaching zero. Therefore, space-diversity reception is often essential for high-grade communication service.

A simple method for estimating the gain of a free-space rhombus is the following: Take the total electrical length of one side (two legs) in degrees (360° per wavelength) and multiply that by the average current throughout its length, accounting for attenuation due to radiation, to obtain a value of degree-amperes that produces the maximum field strength on the main beam. The antenna input current will be $I = \sqrt{w/Z_0}$, where W is the input power and Z_0 is the input impedance, but this current, ideally, decreases exponentially to the far end of the antenna.

Since it is demonstrable (Ref. 1, page 4) that a doublet with a moment of one degree-ampere (1 $^{\circ}$ · A) produces a maximum free-space field strength at 1 mi (1.6 km) of 325 \times 10⁻⁶ V/m, the field strength produced by the rhombic (E_r) will be the product of its effective degree-amperes and 325 \times 10⁻⁶ V/m on the nose of the beam.

This value, compared with that from a half-wave dipole with equal power input, gives the relative gain through the relation

$$G_{dB} = 20 \log \frac{E_r}{E_d}$$

 E_d (dipole) with 1000-W input produces a field strength of 0.1376 V/m at 1 mi in free space. This is derived as follows: a half-wave dipole has a moment of $180^{\circ} \times 0.636 = 114.48^{\circ} \cdot \text{A}$ for 1 A of antenna current. With 1000 W radiated into a thin dipole having a radiation resistance of 73.1 Ω , the antenna current would be 3.699 A. The total moment with 1000 W radiated becomes $3.699 \times 114.48 = 423.467^{\circ} \cdot \text{A}$. This value multiplied by $325 \times 10^{-6} \text{ V/m}$ at 1 mi gives the value 0.1376 V/m presented above.

11-4 STEREOGRAPHIC COMPUTING AIDS

Before the days of digital computers in every engineering office, the complicated multilobed radiation patterns for long-wire antennas were best computed graphically. The

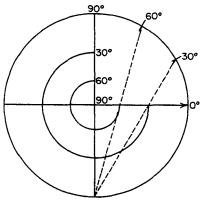


FIG. 11-6 Derivation of stereographic elevation angles from circular azimuth angles.

Foster² stereographic charts, giving a visual display of pattern formation and design-parameter adjustment, were developed for that purpose. Even now nothing could be simpler.

Stereographic projection of a sphere to a plane is conformal, meaning that all angular relationships are precisely maintained in the plane. Figure 11-6 illustrates the construction of a stereographic plane with latitude intervals of 30°.

Figure 11-7 illustrates the radiation pattern for a wire 4.5 wavelengths long in free space in stereographic coordinates. The wire is located on the diameter; for the case of a traveling wave with current flowing in the direction of the arrow, the resulting cones of radiation are shown by broken lines, their successive maxima

being marked M_1 (main lobe), M_2 , etc. The intervening zeros are shown in solid lines. Along the diameter are ticks at 10° intervals in the third dimension, with 90° at the pole of the figure.

It is convenient to speak of the zeros, but physically they are in fact deep minima. The stereographic charts for any wire length can be plotted from the data of Fig. 11-1.

The free-space radiation pattern is seen when a transparent pair of stereographic charts is overlaid at the acute angle of the rhombus (or V). This is illustrated in Fig. 11-8, which is for 5.5-wavelength legs and an acute angle of 33°, producing a main beam of 13° from the plane of the rhombus.

Swinging the apex angle will show how the main-beam angle can be adjusted as desired at one frequency. If the apex angle is too wide, the main beam will shrivel and perhaps disappear.

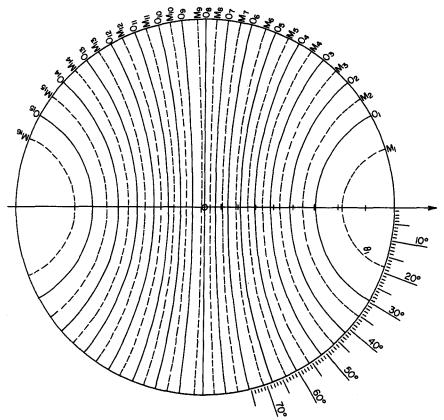


FIG. 11-7 Free-space radiation pattern for a straight wire with traveling-wave current distribution in stereographic coordinates.

Combining patterns stereographically is mathematically equivalent to multiplying the two patterns. A zero in one produces a zero in the combined pattern. This is also true if the height factor is included when locating the rhombus parallel to the ground to complete the horizontal rhombic antenna. The main beam is then horizontally polarized, whereas the various secondary lobes off the main axis are obliquely polarized.

Height factors for horizontal polarization can also be charted stereographically and used visually with the rhombus charts to show the full three-dimensional pattern.

11-5 OPTIMUM DESIGN AND BANDWIDTH FOR HORIZONTAL RHOMBIC ANTENNAS

This section will emphasize the electrical limitations of rhombic antennas. The frequency bandwidth for essentially uniform input impedance is vastly greater than the bandwidth for acceptable radiation patterns. Attempts to use the antenna over too broad a frequency band lead to excessive emissions in useless directions or employ-

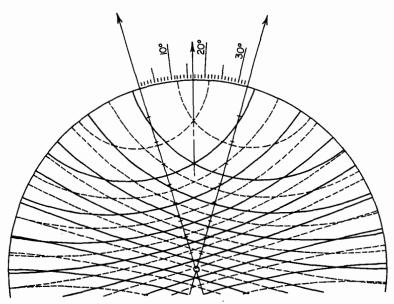


FIG. 11-8 Radiation patterns for a 5.5λ rhombus with an acute angle of 33°.

ment of excessive power to compensate for deficiencies in the antenna pattern. A sound operations rule is not to use a rhombic antenna over more than a 2:1 frequency range. New operators coming into old stations need to be made aware of such practices so as not to misuse the facilities.

11-6 LAND-SAVING ARRANGEMENTS FOR MULTIPLE RHOMBIC ANTENNAS

Large high-frequency radio stations employing many rhombic antennas can economize on land area and feeder lengths in at least two ways: (1) a small rhombic can be located inside the area of a large one having about the same orientation, and (2) common supports can be used for two or three antennas (at the corners).

These savings are possible because the mutual impedances between travelingwave antennas are very much lower than for resonant systems.

11-7 SIDELOBE REDUCTION AND GAIN IMPROVEMENT WITH DOUBLE-RHOMBOID ANTENNAS

Particular high-frequency communication conditions that require the bandwidth of a rhombic antenna, but with substantial reduction in sidelobes and a gain improvement of 3 dB, may benefit by means of the double-rhomboid antenna.³ This is a form of array employing either two coaxial rhombics of different sizes fed from a common

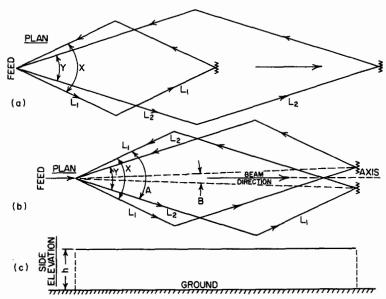


FIG. 11-9 Double-rhombic and double-rhomboid antennas having the same radiation patterns.

apex or the same leg lengths connected as two complementary rhomboids, which reduces the array length. The two geometries are illustrated in Fig. 11-9.

The radiation pattern is designed with stereographic charts, using two pairs for two different leg lengths. By choosing lengths that cause a better distribution of zeros in the sidelobe regions while aligning the main lobes, the growth of sidelobes is inhibited substantially. An example of a design that was scale-modeled and later constructed for transatlantic military traffic is shown in Fig. 11-10. Multipath transmission is reduced by transmitting with low beam angles that are essentially free of sidelobes. This assures fewer teleprinted-character errors and statistically better circuit reliability.

The input impedance of a double-rhomboid antenna is about half that of a single rhombus having the same wire structure.

11-8 IMPORTANCE OF PHYSICAL AND ELECTRICAL SYMMETRY

The proper operation of a rhombic antenna and its feeder depends on balanced potentials from all parts of the system to ground. Any unbalance produces a component of field operating against ground. Radiation from unbalanced components compromises the basic system performance. Care is needed to maintain symmetry through switching systems and in bends and corners in the feeders. Electrical balance is obtained only through structural symmetry, since there are no wideband methods of correcting unbalance otherwise.

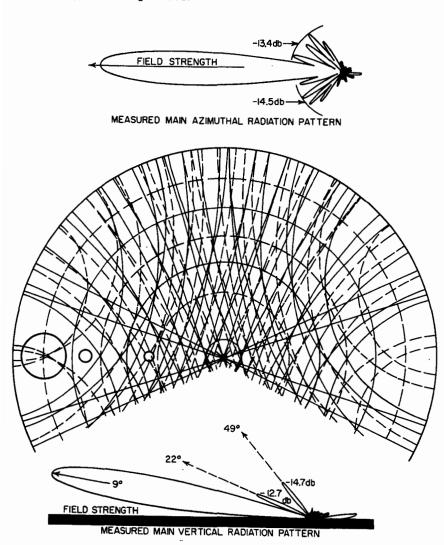


FIG. 11-10 Comparison of measured and stereographically computed radiation patterns for the array of Fig. 11-9b when $L_1 = 3.5\lambda$, $L_2 = 6.0\lambda$, $X = 50^\circ$, and $Y = 35^\circ$.

11-9 CROSSTALK BETWEEN FEEDERS

Long parallel feeder runs, nearby or on the same supports, can lead to crosstalk between feeders with consequent radiation of crosstalk power on the wrong frequency and antenna. Such systems lack the selectivity of resonant systems to filter out cross-

talk. Therefore, precautions to control crosstalk must be included in system design, such as by transpositions or by rotating the plane of an adjacent open-wire feeder. For receiving, coaxial feeders matched to the antenna with balance-to-unbalance transformers are often employed.

11-10 CIRCUITAL PROPERTIES OF RHOMBIC ANTENNAS

Ideally, the antenna feeder matches the impedance of the antenna at all frequencies. The input impedance of the antenna varies somewhat with frequency owing to small internal reflections, but it remains close to resistive. The variations are minimized by using three spread side wires and by adjusting the far-end terminal resistance.

Balanced open-wire transmission lines can be configured for characteristic impedances from 200 to 650 Ω by appropriate combinations of sizes of wire, line cross sections, and numbers of wires (Ref. 1, pages 422-425). When a wideband transformer is needed to make a match between two different impedances, this can be done in a short length with an exponentially tapered line section. A linear taper may also make a satisfactory match if the tapered section is of sufficient length. Such transformations are usually performed in the vertical feed to the antenna input.

11-11 FEED-POINT IMPEDANCE

The input impedance for a one-wire rhombic is usually about 800Ω . The conventional three-wire rhombus has an input impedance of the order of 600Ω , and the two-wire intermediate design has an impedance of about 700Ω . All these impedances are for terminated rhombics with optimum-value termination. (See Refs. 4 and 5 for good guiding values for well-constructed systems.)

11-12 TERMINATING RESISTANCE AND TERMINAL- POWER LOSS

Unradiated power arriving at the forward apex of a rhombic antenna will be reflected back to the input unless it is absorbed passively. If radiation loss is 8 dB on a long antenna, complete reflection of excess power will be attenuated by another 8 dB on the way back to the input. Whereas that loss may not change the input impedance intolerably, this backward power is radiated in a contrary direction, which could be disturbing to others.

If the terminal power is small, a fixed resistor of correct value may suffice, though it is preferable for the resistor to be composed of two units with the midpoint wires connected to a ground rod. Ceramic resistors of high impact strength are needed to withstand lightning impulses.

High-power transmissions often leave substantial power to be dissipated in the terminal resistance. For dissipating this power, sections of open iron-wire transmission lines of high dissipative capacity per unit length (obtained with high-µ iron wire) have been used. Length should be sufficient to have an attenuation of 6 or 13 or more. The far ends are then connected together to ground. Total residual reflection from the ground connection is attenuated sufficiently before it reaches the antenna.

Since most of the power to be dissipated is lost at the input end of the dissipation

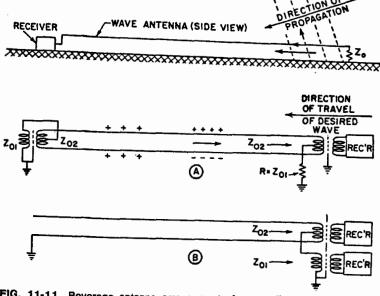
line, it is not unusual for that portion to be heated to a glow.

11-13 **RHOMBIC ARRAYS**

Arrays of rhombics may be useful in special circumstances. Because of the large spatial spread of one unit, the synthesis of an array must take account of centers of radiation to produce coherent array radiation patterns.

The largest rhombic-antenna array known, built during the days of the highfrequency transatlantic radiotelephone, was the multiple-unit steerable array described by Polkinghorn.6

> ELECTRIC VECTORS OF EQUIPHASE WAVE FRONT



Beverage antenna arrangements for one direction of reception, reversed-direction reception, and two-way reception.

11-14 BEVERAGE RECEIVING ANTENNA FOR LOW FREQUENCIES

This antenna, developed by Beverage, Rice, and Kellogg, is unique as a directive antenna for reception of low and very low frequencies. It was the first such antenna to use the traveling-wave principle.

It consists, in its simplest form, of a single-wire transmission line running in the direction of expected wave arrival and terminated in its characteristic impedance with a receiver at its near end. Reception depends on the tilt of the arriving vertically polarized wavefront caused by local ground losses. The electric vector of the equiphase front, tilted forward, produces a component of electric force parallel to the wire, inducing a current in the wire. This flows toward the receiver and is reinforced throughout the length of the antenna.

Wave tilt increases with frequency and with ground resistivity. The length of antenna depends on the available land, up to the limit at which induced currents tend to be out of phase with the advancing wavefront. Directivity increases with length up to the above limit. The wave transmitted along the antenna is a transverse magnetic wave.

Figure 11-11 illustrates the principles for antennas adapted for reception from either or both directions. The most extensive use of Beverage antennas was in an array of four units for overseas reception on the first transatlantic radiotelephone system operating at 50 and 60 kHz.⁷

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Surface-Wave Antennas*

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12-1 Introduction 12-2

12-2 Properties and Measurement of

Surface Waves 12-2

Interrelationship of

Parameters 12-3

Calculation of Surface-Wave

Parameters 12-6

Measurement of Surface-Wave

Parameters 12-7

12-3 Surface-Wave Antennas: Design Principles 12-8

Radiation of Surface-Wave

Antennas 12-8

Design for Maximum Gain 12-11

Design for Minimum

Reamwidth 12-14

Design for Minimum Sidelobe

Level 12-15

Design for Broad Pattern

Bandwidth 12-15

Feeds 12-16

Arrays of Line Sources 12-18

Effect of Finite Ground Plane on

Radiation Pattern 12-19

12-4 Surface-Wave Antennas: Specific

Structures 12-20

Dielectric Rod 12-21

Dielectric Channel Guide 12-22

Yagi-Udas 12-23

Dielectric Sheets and Panels 12-23

^{*}This chapter was prepared by Richard C. Johnson using material previously written by Francis J. Zucker.

12-1 INTRODUCTION

The two types of traveling-wave antennas discussed in this chapter are illustrated in Fig. 12-1. In Fig. 12-1a, a surface wave (also called a trapped wave because it carries its energy within a small distance from the interface) is launched by the feed F and travels along the dielectric rod to the termination T. Since a surface wave radiates only at discontinuities, the total pattern of this antenna (normally end-fire) is formed by the interference between the feed and terminal patterns. The dielectric material could alternatively be an artificial one, e.g., a series of metal disks or rods (the Yagi-Uda antenna). On the other hand, discontinuities can be placed all along the surface-wave structure, producing radiation in the manner of a slotted waveguide except that the wave propagates on an open, not a shielded, guide. The array of dipoles proximity-coupled to a two-wire transmission line in Fig. 12-1b illustrates this second antenna type; here we are evidently using the term surface wave loosely to designate any wave mode that propagates along an open interface without radiating.

Two closely related antenna structures are discussed in other chapters: the helix (which involves a surface wave in one of its modes of operation; Chap. 13) and the frequency-independent antennas (Chap. 14). The short Yagi-Uda, in whose design surface waves play no role, is covered in Chap. 3. An additional discussion of surfacewave antennas can be found in Ref. 2.

Surface-wave antennas lend themselves to flush, or at least low-silhouette, installation. Their gain normally does not exceed 20 dB, and control over their pattern shape (including sidelobes) is very limited. Bandwidth is generally narrow. Frequency coverage extends from the popular Yagi-Udas at very high frequencies (VHF) to printed microwave (and perhaps millimeter-wave) antennas. By contrast, arrays excited by surface waves produce patterns that can in principle produce as high gain and be controlled as accurately as the patterns of nonresonant slot arrays.

12-2 PROPERTIES AND MEASUREMENT OF SURFACE WAVES

For design purposes, a surface wave is sufficiently characterized by one of its parameters, for example, the wavelength in the direction of propagation along the interface. The various parameters will now be defined and formulas given for their interrelationship; it will then be shown how they can be calculated if the surface impedance is known or how they can be determined by measurements.

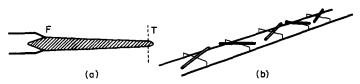


FIG. 12-1 Surface-wave-antenna types. (a) Dielectric rod. (b) Array of proximity-coupled dipoles (thin lines are dielectric supports).

Interrelationship of Parameters

The governing relation is the separability condition for the wave equation. In rectangular coordinates (Fig. 12-2a),

$$k_x^2 + k_y^2 + k_z^2 = k^2$$
 (12-1)

where the k's, called wave numbers, are in general complex; for example, $k_x = \beta_x - j\alpha_x$, with β_x the phase constant in radians per unit length (inches, centimeters, or meters), and α_x the attenuation in nepers per unit length. The wave number k is that of the medium in which the wave travels, $k = \omega \sqrt{\epsilon_0 \mu_0}$, with ω the angular frequency, ϵ_0 the dielectric constant, and μ_0 the permeability. In air, k is pure real; it is related to the wavelength λ by $k = \beta = 2\pi/\lambda$ and to the phase velocity of light c by $k = \omega/c$. Similarly, the phase constant β_z along the surface is related to the surface wavelength λ_z by $\beta_z = 2\pi/\lambda_z$ and to the surface phase velocity v_z by $\beta = \omega/v_z$. The following ratios are therefore equivalent:

$$\frac{\beta_z}{k} = \frac{\lambda}{\lambda_z} = \frac{c}{v_z} \tag{12-2}$$

When this ratio is greater than 1, we speak of a "slow" wave (i.e., slower than light, because $v_z < c$); when less than 1, of a "fast" wave ($v_z > c$). The surface wavelength λ_z of slow waves is shorter than λ ; that of fast waves, longer than λ (as in shielded waveguide).

A surface wave is one that propagates parallel to the interface and decays vertically to it; that is, the phase constant β_x is zero, and $k_x = -j\alpha_x$ (pure attenuation), with α_x positive. Assume first that the wave extends indefinitely in the transverse direction so that $k_y = 0$ (Fig. 12-2a). Equation (12-1) requires that k_z be pure real;

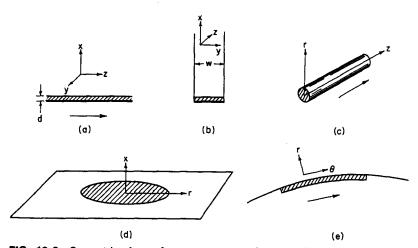


FIG. 12-2 Geometries for surface-wave propagation over dielectric sheets. (a) Infinite-plane sheet-on-metal. (b) Rectangular duct. (c) Axial-cylindrical rod. (d) Radial-cylindrical sheet-on-metal. (e) Azimuthal-cylindrical or spherical cap. Heavy lines indicate metal surfaces. Arrows point in the direction of propagation.

that is, there can be no attenuation in the direction of propagation, and we obtain the simple but basic relation

$$\beta_r^2 = k^2 + \alpha_r^2$$
 (12-3a)

or equivalently, by using Eq. (12-2),

$$\frac{\lambda}{\lambda_x} = \frac{c}{v_x} = \sqrt{1 + \left(\frac{\alpha_x \lambda}{2\pi}\right)^2}$$
 (12-3b)

from which it follows that this is a slow wave. Equation (12-3b) is plotted as the dashed line in Fig. 12-3b. Slower-than-light surface waves are used chiefly in end-fire antenna design (Secs. 12-3 and 12-4). Figure 12-3a illustrates constant-phase and constant-amplitude fronts, which are at right angles to each other provided only that the medium above the interface is lossless. (Ohmic losses in the surface produce a

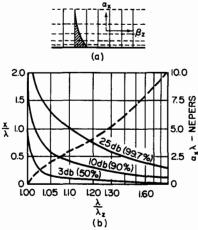


FiG. 12-3 Phase and amplitude contours of a plane surface wave. (a) Solid lines indicate constant-phase fronts; lines, constant-amplitude fronts; shaded region shows amplitude decay. (b) Solid lines indicate height x/λ above surface of 3dB, 10-dB, and 25-dB constant-amplitude or power contours as a function of relative surface wavelength λ/λ_z (use left-hand ordinate); numbers in parentheses refer to the percentage of total energy carried by the surface wave between the interface and each contour. The dashed line indicates the relation between relative surface wavelength and vertical attenuation $\alpha_x \lambda$ according to Eq. (12-3b) (use right-hand ordinate).

slight forward tilt in the phase front and a small α_x .) The more closely the surface phase velocity approaches that of light, the smaller is α_x [Eq.(12-3b)] and the larger, therefore, the vertical extent of the surface wave in Fig. 12-3a.

All components of the total electromagnetic field of the surface wave, for example, E_z , are of the form

$$E_z(x,z,t) = E_z e^{-\alpha_x x} e^{-j\beta_z z} e^{j\omega t} \qquad (12-4)$$

The vertical decay of the E_z , E_x , and H_y components of a TM surface wave ($H_z =$ 0) is shown in Fig. 12-4a, and the composite electric field lines over a full wavelength interval (longitudinal section) in Fig. 12-4b. It can be shown that E_x is in phase with H_y, E_x in phase quadrature. The first two components therefore carry all the power along the interface, while E_x and H_y form a vertically pulsating storage field. The dielectric slab-on-metal below the interface in Fig. 12-4 is used as an example. Since the form of Eq. (12-4), and thus of the surface-wave field lines, does not depend on the detailed structure of the medium below the interface, a multilayer dielectric or a corrugated sheet, etc., could have been shown equally well.

The field (or power) decay in decibels is plotted as a function of height x/λ above the surface in Fig. 12-3b [based on Eq. (12-3a)]. If we assume a relative surface wavelength λ/λ_z (or relative

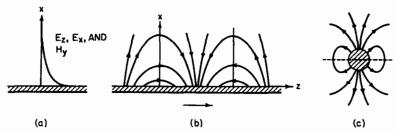


FIG. 12-4 Surface-wave field structure above interface. (a) TM-wave components on plane surface. (b) Composite electric field lines over a one-wavelength interval (arrow points in the direction of propagation). (c) Composite electric field lines of HE₁₁ wave on an axial-cylindrical surface (cross section). Dashed line shows the electric-image plane (Sec. 12-4).

phase velocity c/v_x) equal to 1.1, for example, the field at height $x = \lambda$ has decayed by 25 dB below its value at the interface.

Assume next that two parallel walls are erected normal to the surface, forming a duct in the z direction (Fig. 12-2b). (Examples other than the dielectric-loaded channel in this figure are the channel with a corrugated bottom and the trough guide.) The transverse wave number is fixed by the duct width w as in conventional waveguide theory; from Eq. (12-1) we now have, instead of Eq. (12-3a),

$$\beta_z^2 = k^2 + \alpha_x^2 - \left(\frac{n\pi}{w}\right)^2$$
 $n = 0, 1, 2, \cdots$ (12-5a)

If n = 0 (no variation in y direction), Eqs. (12-3), and therefore also Fig. 12-3b, still apply. If n = 1 (half a sinusoid in y direction),

$$\frac{\lambda}{\lambda_z} = \frac{c}{v_z} = \sqrt{1 + \left(\frac{\alpha_x \lambda}{2\pi}\right)^2 - \left(\frac{\lambda}{2w}\right)^2}$$
 (12-5b)

Since the second term is usually smaller than the third, it follows that the wave is usually, though not necessarily, faster than light. Fast as well as slow surface waves can be used to excite arrays of discrete elements. The field and power decay still follows Fig. 12-3a and b, provided that the abscissa in Fig. 12-3b is relabeled $\sqrt{(\lambda/\lambda_z)^2 + (\lambda/2w)^2}$ to account for the difference between Eqs. (12-3b) and (12-5b). The heights x/λ corresponding to the 25-dB contour in Fig. 12-3b are useful for estimating the extent to which the duct walls, which theoretically must be infinite in height, may be lowered without perturbing the surface wave.

Surface-wave geometries other than rectangular are shown in Fig. 12-2c-e. 1 he separability condition for the wave equation in axial- and radial-cylindrical coordinates (Fig. 12-2c and d) reads

$$k_r^2 + k_z^2 = k^2 ag{12-6}$$

(note that k_{i} does not appear), which is formally identical with Eq. (12-1) for the case $k_{i} = 0$. The interrelationships of the surface-wave parameters given in Eqs. (12-3)

still hold if k, is substituted for k. Above the surface, the field components decay like Hankel functions; in the axial-cylindrical case, for example,

$$E_z(r,z,t) = E_z H_0^{(2)}(\alpha_r r) e^{-j\beta_z z} e^{j\omega t}$$
 (12-7)

The circumferential field dependence in the case of the HE₁₁ mode—the one of principal interest in this geometry—is one full sinusoid. Composite E lines for this hybrid wave (so called because of the presence of both E_z and H_z) are shown in Fig. 12-4c. [The structure inside the circular interface could equally well be a metal rod with a dielectric mantle, an array of circular disks (cigar antenna), or even an array of dipoles (Yagi-Uda).] For large radii, the Hankel function is asymptotic to the exponential, and Eq. (12-7) differs negligibly from Eq. (12-4). As a consequence, the 25-dB contours in Fig. 12-3b still hold and the 10-dB contours nearly so; these curves are useful in estimating the degree of coupling between adacent end-fire line sources. In the radial-cylindrical case, the field components decay exponentially away from the surface so that Fig. 12-3b applies exactly. But the constant-amplitude fronts will now no longer be parallel to the surface because the field components decay radially like Hankel functions (asymptotically like $1/\sqrt{r}$), bringing the fronts closer to the surface with increasing r.

In the azimuthal-cylindrical or spherical case it can be shown that the wave numbers are always complex so that these surface waves are no longer completely trapped. Because the radius of curvature is usually large, it is convenient to treat azimuthal waves as a perturbation of Eqs. (12-3) for flat surfaces.

Calculation of Surface-Wave Parameters

Surface waves are modes on unshielded waveguides. As in the case of shielded waveguides, the boundary-value problem is often conveniently stated in terms of the *transverse resonance condition*, which requires that the equivalent network of a transverse section through the waveguide be resonant. With Z_x the impedance looking straight up from the interface and Z_x the surface impedance looking straight down, the resonance condition reads

$$Z_x + Z_s = 0 {(12-8)}$$

 Z_x depends on the geometry and the mode; in rectangular coordinates,

$$Z_x = \frac{k_x}{\omega \epsilon_o}$$
 for TM waves (12-9a)

$$Z_x = \frac{\omega \mu_o}{k_x}$$
 for TE waves (12-9b)

In the case of a surface wave, $k_x = -j\alpha_x$; Z_x is therefore capacitive in Eq. (12-9 a) and inductive in Eq. (12-9 b). It follows from Eq. (12-8) that the TM surface wave requires an inductive surface, $Z_s = jX_s$, and the TE surface wave a capacitive surface, $Z_s = -jX_s$ (X_s positive). Equation (12-8) now reads

$$\frac{\alpha_x}{k} = \frac{X_s}{R_C} \qquad \text{for TM waves} \qquad (12-10a)$$

$$\frac{\alpha_x}{k} = \frac{R_c}{X_s} \qquad \text{for TE waves} \tag{12-10b}$$

where $R_c = \sqrt{\mu_0/\epsilon_0} = 377 \Omega$. β_z or λ/λ_z follows immediately from Eqs. (12-3).

Knowledge of the surface impedance thus solves the boundary-value problem. It is instructive to calculate this impedance for two simple cases: surface waves on a dielectric slab-on metal and on a corrugated-metal sheet. Looking down from the air-dielectric interface in Fig. 12-2a, one sees a dielectric-loaded region short-circuited at the end. By using transmission-line theory, assuming that the wave is TM, and noting that a wave that is TM in the direction of propagation is also TM transverse to it,

$$X_{s} = \frac{k_{x}}{\omega \epsilon_{1}} \tan k_{x} d \qquad (12-11)$$

where k_x is the vertical wave number in the slab of dielectric constant ϵ_1 . Since X_x must be positive real, $k_x = \beta_x$. [One could now write the field components below the interface in the form of Eq. (12-4), with a sinusoidal variation in x replacing the exponential decay; the field configuration below the interface, however, is rarely of interest to the engineer.] Substitution of Eq. (12-11) in Eq. (12-10a) gives one equation in two unknowns, α_x and β_x . α_x is a function of β_z through Eq. (12-3a); β_x can also be expressed as a function of β_z , since Eq. (12-1) reads

$$\beta_x^2 + \beta_z^2 = k_1^2$$

in the dielectric medium $(k_1 = \omega \sqrt{\mu_1 \epsilon_1})$. The solution⁴ shows that the lowest TM mode has no cutoff and that the phase velocity of the surface wave lies between c and $c \sqrt{\epsilon_1/\epsilon_0}$, approaching the free-space velocity in air for very thin sheets and the free-space velocity in the dielectric for thick sheets (numerical results are in Sec. 12-4). The analysis for a TE wave uses Eq. (12-10b) and results in a lowest mode that does have a cutoff. It is worth pointing out that below cutoff a surface wave does not become evanescent but ceases to exist altogether.

The interface of the corrugated-metal sheet (Fig. 12-5) is an imaginary plane through the top of the teeth. X_s is zero over the teeth and equals R_c tan kd over the

grooves, which are short-circuited parallel-plane transmission lines (inductive in the range $0 < kd < \pi/2$). If there are many grooves per wavelength, the surface impedance over the teeth and grooves may be averaged; that is, $X_s \cong [g/(g+t)]R_c$ tan kd. Substitution in

FIG. 12-5 Corrugated-metal surface. Arrow points in the direction of propagation.

Eq. $(12-10\,a)$ gives one equation in one unknown. The results of this approximation turn out to be good provided there are at least five grooves per wavelength. A more exact calculation takes into account the higher-order (below-cutoff) modes at the mouth of the grooves, which produce higher-order waves along the interface that modify the field lines sketched in Fig. 12-4a and b only in the close vicinity of the teeth.

Measurement of Surface-Wave Parameters

In the case of surface waves, a vertical metal plate large enough to reflect at least 90 percent of the incident energy (use Fig. 12-3b to determine the minimum size) pro-

duces deep nulls at half-wavelength intervals along the surface. Because of turbulence in the aperture field near the feed, measurements should be made at a minimum distance from the feed given by

$$d_{\min} \simeq \frac{0.17\lambda}{(\lambda/\lambda_z) - 1}$$

If the frequency is so low that reflector size becomes a problem, the distance between nulls is found by feeding the probe signal into a phase-comparison circuit (using magic T and attenuator) that measures the traveling-wave phase with respect to a reference signal.

The probe used in these measurements should have a small cross section so as not to perturb the field. It needs chokes to suppress antenna currents on its outer conductor, and it must couple only into the E or the H field, with good discrimination against the unwanted one. A coaxially fed monopole or a waveguide horn pinched at the mouth (with dielectric loading to keep it above cutoff)⁵ is very satisfactory; loops and horizontal dipoles, less so. The distance between probe and aperture should be as small as possible without perturbing the aperture field, and it should be held constant by providing a rigid probe carriage.

12-3 SURFACE-WAVE ANTENNAS: DESIGN PRINCIPLES

Radiation of Surface-Wave Antennas

Before presenting design principles (for optimum gain, beamwidth, sidelobe level, and bandwidth), it is useful to examine how surface-wave antennas radiate. Two typical structures are shown in Fig. 12-6. The feed F (consisting of a monopole and reflector

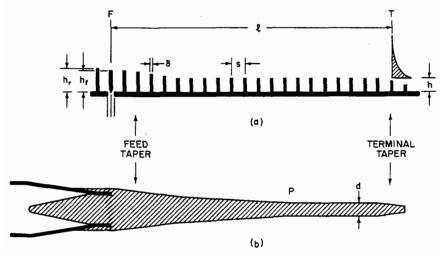


FIG. 12-6 Surface-wave antenna structures. (a) Yagi-Uda (row of monopoles) on ground plane, excited by dipole-reflector combination. (b) Dielectric rod, excited by circular or rectangular waveguide (broad wall in plane of paper).

in Fig. 12-6a and of a circular or rectangular waveguide in Fig. 12-6b) couples a portion of the input power into a surface wave, which travels along the antenna structure to the termination T, where it radiates into space. The ratio of power in the surface wave to total input power (efficiency of excitation) is usually between 65 and 75 percent. Power not coupled into the surface wave is directly radiated by the feed in a pattern resembling that radiated by the feed when no antenna structure is in front of it.

The tapered regions in Fig. 12-6 serve diverse purposes. The feed taper increases the efficiency of excitation and also affects the shape of the feed pattern. The body taper (extending to point P in Fig. 12-6b) suppresses sidelobes and increases bandwidth. Because a reflected surface wave spoils the pattern and bandwidth of the antenna, a terminal taper is employed to reduce the reflected surface wave to a negligible value.

The surface wave illuminates the terminal aperture (plane perpendicular to the antenna axis through T) in a circular region whose radius increases as the transverse attenuation of the surface wave diminishes or, equivalently, as the surface phase velocity approaches that of light [Eq. (12-3b)]. The larger the illuminated region, the higher the gain produced in the radiation pattern. Since the surface-wave phase front

lies in the aperture plane, the pattern peaks in the end-fire direction. A simple but only approximate expression^{2,6} for the terminal radiation pattern $T(\theta)$ is

$$T(\theta) \cong \frac{1}{(\lambda/\lambda_s) - \cos \theta}$$
 (12-12)

where θ is the angle off end fire and λ_x is the surface wavelength at T (just to the left of the terminal taper, to be precise). This pattern has neither nulls nor side-lobes and, as expected, falls off more rapidly the closer λ/λ_x is to 1. More accurate expressions^{2,7-9} and an experimental determination¹⁰ indicate that the pattern is actually about 20 percent narrower than in Eq. (12-12). The dashed line in Fig. 12-7 shows this corrected terminal radiation pattern for $\lambda/\lambda_x = 1.08$, which is the optimum relative phase velocity for a maximum-gain antenna 4λ long [Eq. (12-14b)].

The radiation pattern of the feed shown in Fig. 12-6a is quite broad (approximately a cardioid in polar coordinates). In combination with the terminal radiation $T(\theta)$, it produces the total

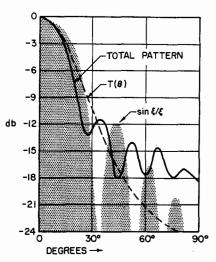


FIG. 12-7 Radiation pattern of 4λ -long surface-wave antenna adjusted for maximum gain in accordance with Eq. (12-14b) ($\lambda/\lambda_z=1.08$). $T(\theta)$ is the H-plane pattern of the surface-wave distribution in the terminal plane. For comparison, $\sin \xi/\xi$ is also shown (shaded region).

surface-wave antenna pattern, shown by the solid line in Fig. 12-7 (experimental data for antenna length $\ell=4\lambda$, $\lambda/\lambda_z=1.08$). In the vicinity of end fire, the terminal pattern predominates; as θ increases, interference with the feed pattern first narrows the beam and then produces a sidelobe at 35°; beyond 45° the feed pattern predominates.

inates. Patterns of all surface-wave antennas adjusted for maximum gain look like those in Fig. 12-7, except that for antennas longer than 4λ the pattern spreads less in θ (first sidelobe closer to end fire than 35°) and for shorter structures it spreads more. The field beyond the first sidelobe falls off more rapidly the larger the end-fire gain of the feed radiation.

The curves in Fig. 12-7 are for the H plane, in which the element pattern of the Yagi-Uda monopoles (Fig. 12-6a) is omnidirectional. In the E plane, $T(\phi)$ (ϕ is the angle off end fire) is narrowed by multiplication with the E-plane element factor (a dipole pattern modified by the effects of mutual impedance), which for $\phi < 60^{\circ}$ approximates $\cos \phi$ and then decays more gradually (no null at $\phi = 90^{\circ}$). The total pattern in the E plane is therefore also narrower than in the H plane, and sidelobes are lower by 2 to 3 dB.

In the case of the HE_{11} mode on a dielectric rod (Fig. 12-6b), the E- and H-plane element factors, and consequently the beamwidths and sidelobe levels, are more nearly the same. The sidelobe level is now usually *higher* by 0.5 to 1.5 dB in the E-plane than in the H plane, the precise amount depending on the relative shape of the E- and H-plane feed patterns.

Instead of being regarded as a combination of feed and terminal radiation, the surface-wave antenna pattern can be viewed as an integral over the field distribution along the antenna structure. What this distribution looks like can be seen in Fig. 12-8: the amplitude A(z) along the row of monopoles (Fig. 12-6a) starts with a hump near the feed and flattens out as the surface wave peels itself out of the near field of feed and feed taper. The surface wave is well established at a distance ℓ_{min} from the feed where the radiated wave from the feed, propagating at the velocity of light, leads the surface wave by about 120°:

$$\ell_{\min}k_z - \ell_{\min}k = \frac{\pi}{3} \tag{12-13}$$

The location of ℓ_{\min} on an antenna designed for maximum gain is seen in Fig. 12-8 to be about halfway between feed and termination. Since the surface wave is fully devel-

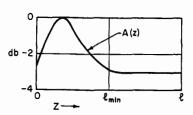


FIG. 12-8 Amplitude A(z) of field along the surface-wave antenna structure.

oped from this point on, the remainder of the antenna length is used solely to bring feed and terminal radiation into the proper phase relation for maximum gain. (In the absence of a feed taper, ℓ_{\min} occurs closer to F and the hump is higher.)

Were there no hump at all, the surface-wave antenna would radiate the familiar $\sin \xi/\xi$ pattern $[\xi = (\pi \ell/\lambda)(\lambda/\lambda_x - \cos \theta)]$ produced by constant-amplitude illumination. This pattern is shown

for comparison in Fig. 12-7 (shaded region); it is an unnatural pattern for parasitically excited antennas, which necessarily have feed turbulence.

Low-sidelobe and broadband designs require tapers that extend over a substantial part of the antenna (Fig. 12-6b). Although the field along one particular taper has been examined in detail, ^{11,12} the effect of tapers on the total radiation pattern is not well understood. When the taper is very gradual, the phase velocity at each point has

the value one would expect from the local surface impedance; when it is sharp, a leaky wave which fills in the minima of the pattern, widens the beam, and reduces sidelobes is produced.

Design for Maximum Gain

The phase velocity along the antenna and the dimensions of the feed and terminal tapers in the maximum-gain design of Fig. 12-6a must now be specified.

If the amplitude distribution in Fig. 12-8 were flat, maximum gain would be obtained by meeting the Hansen-Woodyard condition (strictly valid only for antenna lengths $\ell \gg \lambda$), which requires the phase difference at T between the surface wave and the free-space wave from the feed to be approximately 180°:

$$\ell k_z - \ell k = \pi$$

or, equivalently,

$$\frac{\lambda}{\lambda_r} = 1 + \frac{\lambda}{2\ell} \tag{12-14a}$$

which is plotted as the upper dashed line in Fig. 12-9.

Since the size and extent of the hump are a function of feed and feed-taper construction, the optimum terminal phase difference for a prescribed antenna length cannot easily be calculated. Experimental work on Yagi-Uda antennas (but without feed taper) by Ehrenspeck and Poehler¹³ and Ehrenspeck¹⁴ has shown that the optimum terminal phase difference lies near 60° for very short antennas, rises to about 120° for ℓ between 4 λ and 8 λ , then gradually approaches 180° for the longest antenna measured (20 λ). Therefore

$$\frac{\lambda}{\lambda_z} = 1 + \frac{\lambda}{p\ell} \tag{12-14b}$$

with p starting near 6 for $\ell=\lambda$ and diminishing to approximately 3 for ℓ between 3λ and 8λ and to 2 at 20λ . This relation is plotted as the solid curve in Fig. 12-9. In the presence of a feed taper, the optimum λ/λ_z values lie slightly below this curve.

If the efficiency of excitation is very high, interference between feed and terminal radiation is of minor importance, and the antenna need just be long enough so that the surface wave is fully established; that is, $\ell = \ell_{\min}$ in Fig. 12-8. From Eq. (12-13),

$$\frac{\lambda}{\lambda_r} = 1 + \frac{\lambda}{6\ell} \tag{12-14c}$$

which is plotted as the lower bound of the shaded region in Fig. 12-9.

Because feeds are more efficient when exciting slow surface waves than when the phase velocity is close to that of light, the solid line starts near the lower bound and ends at the upper. As long as λ/λ_r falls within the shaded region, its precise adjustment is not critical; with $\ell=4\lambda$ and in the presence of a feed taper, the gain drops only 1 dB if λ/λ_r lies on the dashed lower bound instead of just below the solid upper bound.

Although this technique for maximizing the gain has been strictly verified only for Yagi-Uda antennas, data available in the literature on other structures suggest that optimum λ/λ_r values lie on or just below the solid curve in all instances. To pro-

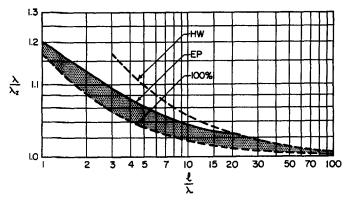


FIG. 12-9 Relative-phase velocity $c/v = \lambda/\lambda_x$ for maximum-gain surface-wave antennas as a function of relative antenna length ℓ/λ . HW = Hansen-Woodyard condition, Eq. (12-14b); EP = Ehrenspeck and Poehler experimental values, Eq. (12-14b); 100 percent = idealized perfect excitation, Eq. (12-14c).

duce these optimum values, the dependence of λ/λ_r on the structural parameters of the antenna must be calculated, measured, or sought in the literature.

The feed taper should begin at F with λ/λ_r between 1.2 and 1.3 and extend over approximately 20 percent of the full antenna length. Its exact shape is not important as long as a smooth transition is made to the main body of the antenna. The terminal taper should be approximately 0.5 λ long, and to match the surface wave to space, λ_r at the end of the taper should be as close as possible to λ . In the case of a polyrod (ϵ = 2.56), for example, Fig. 12-16 shows that λ_r is reasonably close to λ when

$$d/\lambda = 0.23$$

and the end of the rod is therefore blunt rather than pointed.

The gain above an isotropic radiator of a long $(\ell \gg \lambda)$ uniformly illuminated end-fire antenna whose phase velocity satisfies Eq. (12-14a) was shown by Hansen and Woodyard to be approximately

$$G \simeq \frac{7\ell}{\lambda}$$

If the design is based on the optimal phase velocities and taper dimensions just described, the gain for ℓ between 3λ and 8λ is

$$G \cong \frac{10\ell}{\lambda} \tag{12-15}$$

which is 1.5 dB above the Hansen-Woodyard gain. For shorter lengths the gain may be 30 percent higher; for longer lengths, the proportionality factor slowly decreases because of ohmic loss and the difficulty of designing an efficient feed. Maximum gains reported in the literature are plotted in decibels as a function of ℓ/λ in Fig. 12-10 (solid-line margin of shaded region marked "gain"). These gains involve a slight degree of superdirectivity but not enough to produce excessively narrow bandwidths or high ohmic loss.

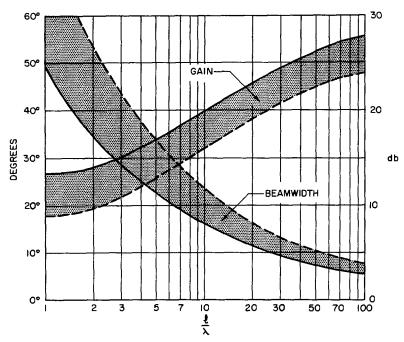


FIG. 12-10 Gain and beamwidth of a surface-wave antenna as a function of relative antenna length ℓ/λ . For gain (in decibels above an isotropic source), use the right-hand ordinate; for beamwidth, the left-hand ordinate. Solid lines are optimum values; dashed lines are for low-sidelobe and broadband design.

The half-power beamwidth BW of a maximum-gain design is approximately

$$BW = 55 \quad \sqrt{\frac{\lambda}{\ell}} \quad \text{degrees} \qquad (12-16)$$

which lies just above the lower (solid-line) margin of the shaded region marked "beamwidth" in Fig. 12-10. Equation (12-16) gives an average figure, the beamwidth usually being slightly narrower in the E plane and slightly wider in the H plane.

The *sidelobe* level, for ℓ between 3λ and 8λ , is about 11 dB in the H plane and 10 or 14 dB in the E plane of a dielectric rod or Yagi-Uda, respectively (cf. above). For shorter antennas the sidelobes are somewhat higher; for longer antennas, lower.

The bandwidth within which the gain drops at most 3 dB is between ± 10 percent and ± 15 percent; below the design frequency, gain slowly decreases as beamwidth widens; above it, the pattern deteriorates rapidly as the main beam splits and sidelobes rise.

By comparing Eq. (12-15) with the gain of a paraboloidal dish (equal sidelobe level is assumed), the surface-wave-antenna length is found to be related to the diameter d of an equal-gain dish by

$$\frac{\ell}{\lambda} \cong \left(\frac{d}{\lambda}\right)^2 \tag{12-17}$$

This trade-off between a broadside and an end-fire structure becomes very disadvantageous to the latter as ℓ/λ increases, and surface-wave antennas longer than 10λ are rarely used. This limits the gain of surface-wave line sources in practice to 20 dB. (Arrays of line sources and end-fire area sources are practical for much higher gains.)

The gain predicted by Eq. (12-15) is for feeds of the type shown in Fig. 12-6, with radiation patterns that are not very directive. Increasing the feed directivity increases the total antenna gain. For feeds whose radial extent is not much larger than the antenna cross section, it has been found experimentally that a 1- or 2-dB increase in the end-fire gain of the feed produces an approximately equal increase in the total antenna gain. If the feed is much larger than the antenna cross section, the gain continues to rise, though at a slower rate. A large horn aperture, corner reflector, or dish can add as much as 3 or 4 dB. Structures of this sort are part surface-wave, part aperture antenna.

The backfire antenna, which also combines these two features, produces a gain

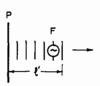


FIG. 12-11 Backfire antenna. (After Ref. 16.)

about 4 dB above that of Eq. (12-15). It consists of a surface-wave line source (for example, a Yagi-Uda, Fig. 12-11) terminated by a flat circular plate P, which reflects the surface wave launched by the feed back toward F, where it radiates into space. Its radiation mechanism is not completely understood. The optimum phase velocity is chosen with the aid of the solid curve in Fig. 12-9, but ℓ in this

context must be reinterpreted as twice the physical antenna length ℓ' of the backfire antenna, since the surface wave traverses the antenna twice. By using Eq. (12-14b), the relation between surface phase velocity and ℓ' (for ℓ' between 1.5 λ and 4 λ) is $\lambda/\lambda_z=1+\lambda/6\ell'$. The feed taper should be much reduced in size or omitted. The plate diameter d is related to ℓ' by

$$\frac{d}{\lambda} \cong 1.5 \quad \sqrt{\frac{\ell'}{\lambda}}$$

which implies that the plate is approximately as large as a paraboloidal dish whose gain equals that of the backfire antenna. For $\ell' = 2\lambda$, the gain is 19 dB, sidelobes are 12 dB down, and bandwidth is at least 20 percent. Easier and cheaper to build than a paraboloidal dish, the backfire antenna might be competitive for gains up to 25 dB (provided sidelobes do not have to be very low); it is superior to ordinary end-fire antennas as long as a low silhouette is not a requirement.

Design for Minimum Beamwidth

The approximate relation between E-plane beamwidth BW_E , H-plane beamwidth BW_H , and gain of a surface-wave antenna is

$$G \cong \frac{30,000}{\mathrm{BW}_{E}\mathrm{BW}_{H}}$$

The half-power beamwidth of a maximum-gain design [Eq. (12-16)] can be made 10 percent narrower by increasing the direct-feed radiation, which causes it to interfere

destructively with $T(\theta)$ at a smaller angle θ than in Fig. 12-7. This is done by starting the feed taper with λ/λ_z less than 1.25. The narrowest beamwidths reported in the literature are plotted in Fig. 12-10 as the solid-line margin of the shaded region marked "beamwidth." (Usually *E*-plane patterns are slightly narrower; *H*-plane patterns, slightly wider.) Sidelobes are about 1 dB higher than in the maximum-gain case.

Design for Minimum Sidelobe Level

The fairly high sidelobes of the maximum-gain design can be reduced by increasing λ/λ_i to 1.35 at the start of the feed taper, letting $\lambda/\lambda_z \cong 1.2$ at the end of the feed taper, and continuing to taper over a large fraction of the total antenna length (to P in Fig. 16-6b). In the constant-cross-section region between P and T, λ/λ_z is chosen to lie on the lower margin of the shaded region in Fig. 12-9. If P is two-thirds of the distance from F to T, the sidelobes of a 6λ -long antenna are down at least 18 dB in the H plane and 17 or 21 dB in the E plane of a dielectric rod or Yagi-Uda, respectively, at the cost of a 1.5-dB drop in gain and a 10 percent rise in beamwidth. ^{17,18} As in the case of the optimum-gain design, the sidelobe level decreases monotonically with increasing antenna length.

The backlobe is suppressed by increasing the end-fire directivity of the feed pattern. A 25- to 30-dB level can be achieved

without resorting to feeds that are much larger than the antenna cross section.

By tapering more sharply near F, then flattening out gradually to a value of λ/λ_z close to 1 at T, the H-plane sidelobe level can be reduced to 20 dB. ¹⁸ Gain and beamwidth then lie on the dashed margins of the shaded bands in Fig. 12-10. A further reduction to 30 dB in the H-plane sidelobe level is achieved by placing parasitic side rows on either side of the center array¹⁹ (Fig. 12-12). The side-row

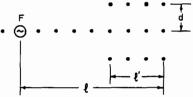


FIG. 12-12 Parasitic side rows for sidelobe suppression in one plane (top view; dots indicate dipoles or monopoles above a ground plane).

length ℓ' is slightly longer than 0.5ℓ . λ/λ_x is the same as on the center array [use Eq. 12-14b)], and the spacing d is optimum when the side rows lie just beyond the 11-dB contour of the surface wave on the center array; or, using Fig. 12-3b and Eq. (12-14b),

$$\frac{d}{\lambda} \cong 0.25 \quad \sqrt{\frac{\ell}{\lambda}}$$

The gain is the same as for maximum-gain design [Eq. (12-15)]. To reduce sidelobes in all planes, parasitic side rows would have to be placed all around the center array.

Design for Broad Pattern Bandwidth²⁰

The ± 15 percent bandwidth of most surface-wave antennas can be extended to as much as ± 33 percent (2:1) at the cost of a 2-dB gain decrease from optimum at midfrequency. At the feed, the midfrequency value of λ/λ_r should be 1.4. A uniform taper extends from the feed to the termination, as shown in Fig. 12-1a. At the low-frequency end of the band, gain and beamwidth lie close to the solid margins of the

shaded strips in Fig. 12-10; at the high-frequency end, close to the dashed margins. Thus gain is constant within ± 1.5 dB and beamwidth within ± 15 percent. On a structure 13.5 λ long at midfrequency, sidelobes were down at least 11 dB throughout the band.²⁰

The bandwidth figures just quoted apply to the polyrod ($\epsilon=2.56$) and to all surface-wave antennas whose dispersion curve (variation of λ/λ_z with frequency) resembles that of the polyrod. Dispersion increases with increasing dielectric constant; dielectric rods with $\epsilon<2.56$ are therefore more broadband and rods with $\epsilon>2.56$ less broadband than polyrods. The dispersion of artificial dielectrics varies; corrugated surfaces are comparable with polyrods, and Yagi-Udas are considerably more dispersive (precise bandwidth figures are not known).

The input impedance of most surface-wave antennas is slightly capacitive and changes slowly with frequency. A tapered dielectric section in waveguide (Figs. 12-1a and 12-6b) provides good matching over a 2:1 bandwidth if 1.5λ long at midfrequency and over a smaller bandwidth if shorter. To minimize the voltage standing-wave ratio (VSWR), an inductive iris is placed close to the insertion point of the rod. Equivalent techniques apply in the case of antennas other than dielectric rods and of input transmission lines other than waveguide.

Feeds

Design principles of feeds and feed tapers for optimum gain, sidelobes, and bandwidth have already been stated. Specific structures will now be described.

In Fig. 12-6a, the feeder and reflector monopoles are spaced 0.2λ apart, $h_r = 0.23\lambda$, and $h_f = 0.21\lambda$. These figures apply to $\delta = 0.048\lambda$; if the elements are thicker, they must be made slightly shorter. The backlobe is between 12 and 15 dB down. By replacing the reflector monopole with a semicircular plate (radius = h_r) or a small corner or paraboloidal reflector (height = h_r), one increases the gain of the feed by at least 1.5 dB and, therefore, the total antenna gain by approximately the same amount. The sidelobes are decreased by at least 2 dB; the backlobe is 25 to 30 dB down.

To couple from the dominant mode in rectangular waveguide, one replaces the feeder monopole by a metal half ring^{21} (Fig. 12-13a); the excitation efficiency of this feed, with semicircular reflector plate, is around 80 percent. Another, slightly less efficient but simpler waveguide feed uses two or more slots to couple into the surfacewave structure. The waveguide should be dielectric-loaded so that its phase velocity approximates that in the surface-wave structure, and the slots are spaced about a quarter wavelength apart in the dielectric. Instead of cutting slots, the entire broad face of a dielectric-filled waveguide can be opened (Fig. 12-13b); by tapering the height of the waveguide over the appropriate length, feed and feed taper can be combined in a single design. In low-power applications, striplines can be slot- or dipole-coupled to the antenna.²² In the absence of the ground plane one uses a center-fed dipole (coaxial input with built-in balun, Fig. 12-13c) or a folded dipole (usually preferred with two-wire input).

The coaxially fed metal cap (Fig. 12-13d), popular as a dielectric-rod feed or a cigar-antenna feed at ultrahigh frequencies (UHF) because of good efficiency combined with mechanical strength, forms the transition between feed types a and b of Fig. 12-6. Type b can handle much higher power than type a. In Fig. 12-6b the waveguide can be rectangular (with TE₁₀ mode) or circular (TE₁₁ mode). A variant of this

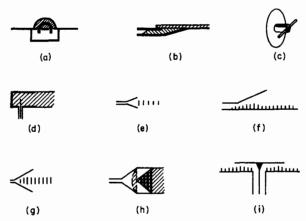


FIG. 12-13 Surface-wave-antenna feeds. (a) Semicircular wire coupled to waveguide. (After Ref. 21.) (b) Dielectric-filled waveguide with an open broad wall. (c) Dipole and reflector feed. (d) Circular waveguide cap. (e) and (f) Horn exciters. (g) Parallel-wire (distributed) feed. (After Ref. 24.) (h) Flared transition with lossy strips (with collimating lens shown in horn aperture). (After Ref. 28.) (l) Coaxial excitation of disk.

form, suitable for Yagi-Uda or cigar-antenna excitation, is shown in Fig. 12-13a. If the horn aperture is considerably larger than the antenna cross section (Fig. 12-13f), the surface-wave structure should start well inside, and it is in fact desirable to have the horn extend just beyond the end of the feed taper, as indicated. (Theoretical work shows that for their size horn apertures are not very efficient surface-wave exciters, ²³ but if the direct-feed radiation of the horn is well collimated—the design can be based on Chap. 15—a large total antenna gain will be produced.)

Patterns that closely approximate the $\sin \xi/\xi$ shape have been obtained by flaring a parallel wire into a 60°V (Fig. 12-13g)²⁴ or by running an unflared parallel wire (loaded with transverse wire stubs to reduce phase velocity) alongside the antenna;²⁵ both structures extend over a third of the antenna length. Feeds of this type are called distributed. In the hope of obtaining good phase and amplitude control over the entire antenna aperture, feeds have been studied that couple continuously from one end of the antenna to the other, for example, a waveguide slot-coupled to a dielectric slab. ^{26,27} These designs have not been very successful thus far, principally because energy flow along two such closely coupled waveguides is difficult to control. If precise aperture illumination is desired, one must abandon surface-wave antennas and turn to the end-fire structures among the surface-wave-excited arrays of discrete elements.

Variants of Fig. 12-6a and b are also used to excite surface-wave area sources. Rectangular dielectric or corrugated surfaces are fed by placing a slotted waveguide alongside, or a hog horn, or a horn with correcting lens. The last is frequently plagued by transverse standing waves, which produce sidelobes in azimuth (yz plane). To suppress these, a flared transition (1λ long at midfrequency) with transverse conducting

(Aquadag) strips can be used (Fig. 12-13h).²⁸ It keeps sidelobes below 20 dB over a frequency range of at least 2:1 at a cost of 1 or 2 dB because of the lossy strips.

Radial-cylindrical area sources (disks, Fig. 12-2d) can be center-fed with a simple monopole feeder; its efficiency of excitation turns out to be higher than with line sources. A higher-gain is shown in Fig. 12-13i, in which the coaxial input is excited in the TEM mode for vertical polarization on the disk and in the TE₀₁ mode for horizontal polarization. A completely flush installation could be achieved by coupling through two or more annular slots. All the arrangements previously described for line sources can be carried over, and the optimum design principles for feed and feed taper still apply.

Arrays of Line Sources

Yagi-Udas, dielectric rods, and other surface-wave line sources can be arranged in a plane or volume array. The surface-wave illumination in the terminal plane of a plane array is scalloped (Fig. 12-14a), the overlapping dotted circles representing the 25-dB contours of the transverse-field decay. If identical end-fire elements and negligible interaction between them are assumed, the array gain G_a is the sum of the individual gains G. By letting n be the number of elements and using Eq. (12-15),

$$G_a = nG \cong 10n \frac{\ell}{\lambda} \tag{12-18}$$

Interaction between adacent elements is found to be negligible if the crossover is at about the 12-dB contour; the minimum separation d is therefore [Fig. 12-3b and Eq. (12-14b)]

$$\frac{d}{\lambda} \cong 0.5 \quad \sqrt{\frac{\ell}{\lambda}} \tag{12-19a}$$

The exact value depends on the polarization (coupling is less in the E than in the H plane) and on the direct coupling between feeds. Too close a spacing produces a loss in gain. An upper limit on the spacing is obtained by requiring that the first principle sidelobe of the array pattern be strongly attenuated through multiplication with the element pattern. The angle with end fire of the array sidelobe must therefore be at

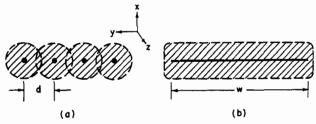


FIG. 12-14 Two-dimensional surface-wave antennas (transverse cross sections). (a) Array of line sources. (b) Area source.

least that of the first minimum in the element pattern, a criterion that corresponds to a crossover of about 22 dB, or a maximum separation

$$\frac{d}{\lambda} \cong \sqrt{\frac{\ell}{\lambda}} \tag{12-19b}$$

The principle of pattern multiplication, which has just been invoked, is useful only for a first design, since the element patterns are somewhat distorted by the presence of the other elements. The optimum spacing, which lies somewhere between the d/λ values given by Eqs. (12-19), must therefore be found empirically.

The beamwidth BW_a in the plane of the array (azimuth) is approximately

$$BW_a \cong \frac{65\lambda}{nd} \tag{12-20}$$

Sidelobes can be reduced by tapering the amplitude at the feeds. In the elevation plane, beamwidth and sidelobes are controlled by the element pattern. The bandwidth is less than for individual elements, probably about ± 5 percent.

Low-silhouette requirements often force the choice of a horizontal plane array of end-fire elements in place of a vertical cylindrical reflector (or a rectangular mattress array). The trade-off between them, if equal gain and sidelobes and equal width in the y direction (Fig. 12-14a) are assumed, is

$$\frac{\ell}{\lambda} \cong \left(\frac{h}{\lambda}\right)^2 \tag{12-21}$$

[cf. Eq. (12-17)], where ℓ is the length of the end-fire elements and h the heights (in the x direction) of the equivalent reflector or broadside array. Because of space limitations, the line sources cannot always be equal in length. Equation (12-18) is then inapplicable, but the spacing between elements is still controlled by Eqs. (12-19).

A volume array of end-fire elements occupies almost as large an area in the transverse (xy) plane as the dish it replaces and has advantages in terms of transportability, ease of erection, and minimum weight needed for mechanical strength against certain kinds of stresses. Spillover is more easily controlled than with a conventional dish, but sidelobe control becomes more difficult and the bandwidth is much narrower. In the design of these arrays, the number of end-fire elements can be reduced by increasing their length; according to Eq. (12-18), $n = G\lambda/10\ell$. This relation clarifies the trade-off between an end-fire volume array and a broadside mattress array of dipoles: though one cannot increase the total gain by replacing the dipoles with higher-gain end-fire elements, one can reduce the number of elements (and thus of separate feeds) while keeping the gain constant.

Arrays of end-fire elements can be fed in cascade from a common transmission line (like slots in waveguide), but a corporate feed structure (branching transmission lines) produces better bandwidth.

Effect of Finite Ground Plane on the Radiation Pattern

Vertically polarized surface-wave line or area sources are often mounted on a ground plane whose finite length g (Fig. 12-15a) distorts the antenna pattern in two ways: by tilting the beam through an angle ψ away from end fire and by broadening it to a half-

power beamwidth BW'. The tilt is maximum when g = 0 (no ground plane in front of antenna):^{29,30}

$$\psi_{\rm max} \cong 60 \, \frac{\lambda}{\ell}$$
 degrees

(which is a full half-power beamwidth BW of the unperturbed pattern); the beam then broadens so that the 3-dB level lies in the end-fire direction, and BW' is slightly over

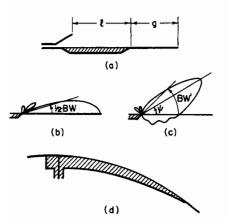


FIG. 12-15 Effect of finite ground plane on the radiation pattern of an end-fire antenna. (a) Finite ground plane. (b) Pattern on infinite ground plane. (c) Pattern in the absence of ground plane. (d) Antenna on a curved ground plane.

twice as wide as the unperturbed BW (Fig. 12-15b and c). The tilt can be reduced by slowing the surface wave down from its infinite-ground-plane optimum, but this increases sidelobes and decreases gain. The gain, on the other hand, is optimized by speeding the wave up at the expense of increased tilt.³⁰

As g increases, the beam tilt decreases: when $g = \ell$, $\psi \cong 0.7\psi_{max}$; when $g = 3\ell$, $\psi \cong 0.5\psi_{max}$; when $g = 20\ell$, $\psi \cong 0.2\psi_{max}$ —a very gradual approach to the infinite-ground-plane condition. The beamwidth approaches the unperturbed value more rapidly: when $g = \ell$, BW' $\cong 1.25$ BW.²⁹ Modifying the surface-wave velocity again has an opposite effect on beam tilt and gain.

If no beam tilting or loss in gain can be tolerated, flush mounting must be abandoned in favor of a full-size structure (pod-mounted to reduce drag, if necessary). A less drastic remedy is to

reduce the tilt angle, at a small cost in gain, by bending the antenna and ground plane into a cylindrical or spherical cap.³¹⁻³³ The curvature produces an attenuation in the surface wave, which can be enhanced by tapering the antenna along its entire length (Fig. 12-15d). If the total attenuation is such that about 50 percent of the power has leaked off before the surface wave reaches the termination, the tilt angle will be reduced to near zero no matter how short the ground plane.³⁰

12-4 SURFACE-WAVE ANTENNAS: SPECIFIC STRUCTURES

Numerical values of λ/λ_z and design details for specific structures are presented in this section. The λ/λ_z curves are displayed for several values of relative dielectric constant ϵ , ranging from 2.56 (polystyrene) to 165 (a calcium titanate ceramic). Hard, low-loss, high-temperature materials, for example, fused quartz ($\epsilon \cong 3.7$), pyroceram ($\epsilon \cong 5.6$), and alite (an aluminum oxide, very durable, $\epsilon \cong 8.25$), are of special interest.

The dielectric-loss tangent δ , which is temperature-dependent, produces a planewave attenuation

$$\alpha\lambda = \sqrt{\epsilon} \tan \delta$$

in an infinite medium, but since a large fraction of the surface wave propagates outside the medium, the surface-wave attenuation $\alpha_z\lambda$ is smaller. For $\lambda/\lambda_z=1.2$, $\alpha_z\cong0.7\alpha$; for $\lambda/\lambda_z=1.03$, $\alpha_z\cong0.1\alpha$. As long as δ is smaller than 10^{-2} , the loss will therefore be less than 0.1 dB per wavelength. Data on long Yagi-Udas³⁵ indicate that, for λ/λ_z near 1, loss in artificial dielectrics is likewise negligible, provided all joints are firmly press-fit or soldered and the metal is of high conductivity. As the corrugations or dipole elements approach resonance, λ/λ_z increases and ohmic losses rise sharply. A typical figure for loss in a 6λ -long dielectric rod or Yagi-Uda is 0.5 dB. (Since the maximum-gain curve in Fig. 12-10 is based on experiment, the effect of ohmic loss is included.) Surface-wave losses can be measured by the resonator method.³⁶

Because of low frequencies the metal elements of artificial dielectrics can be constructed of slender poles and chicken wire; they weigh far less than solid dielectrics. Large ground structures at UHF or below are therefore invariably artificial dielectrics. In the microwave range, the choice of medium depends on mechanical strength, temperature behavior, erosion resistance, and cost; ordinary dielectrics, some of which can be cheaply molded into cavities recessed in the skin, are usually preferred for flush airplane or missile installation.

Dielectric Rod^{8,17,20,21,34,37-42}

Dielectric rod is termed *polyrod* and *ferrod* when made of polystyrene and ferrite material respectively. See Fig. 12-16 a for phase velocity as a function of rod diameter. The higher the dielectric constant, the thinner the rod (for a given gain) and the lighter therefore the weight; also, however, the larger the dispersion and therefore the narrower the bandwidth.

Modes higher than the fundamental HE₁₁ cannot propagate provided $d/\lambda < 0.626/\sqrt{\epsilon}$. The first two higher modes, TE₀₁ and TM₀₁, produce a null in the end-fire direction.

Cross sections other than circular are often useful. To a good approximation,³⁴ the phase velocity depends only on the cross-section area A, and Fig. 12-16 a therefore remains valid if d is replaced by 1.13 \sqrt{A} . Sliced in half along the plane of electric symmetry (Fig. 12-4c)—which does not affect the phase velocity—a circular or rectangular rod can be placed on a ground plane (dielectric-image line, Fig. 12-17a and b); when recessed for flush mounting, this structure is called the dielectric channel guide (Fig. 12-17c). Another variant, the dielectric tube,⁴² has also been studied but appears to have no advantages over ordinary rods.

Mallach³⁸ found that for optimum design the rod diameter at the feed end of a linearly tapered dielectric rod should be $d_{max}/\lambda \cong [\pi(\epsilon-1)]^{-1/2}$, and at the termination $d_{min}/\lambda \cong [2.5\pi(\epsilon-1)]^{-1/2}$. In the range $2.5 < \epsilon < 20$, this rule corresponds to letting λ/λ_z at the feed be roughly equal to 1.1 and at the termination to 1.0. The resulting patterns are often adequate but can be improved by using the methods described in Sec. 16-3.

A rough approximation to the rod pattern, due to Zinke, 38 consists in multiplying

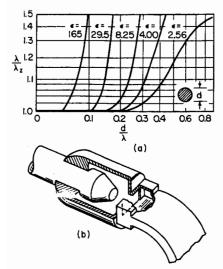


FIG. 12-16 Dielectric rod. (a) Relative phase velocity (see Refs. 37–39; in case of a noncircular cross section, replace d/λ by 1.13 \sqrt{A}/λ). (b) Conventional feed. (Courtesy of G. C. Southworth and D. Van Nostrand Company, Inc.⁴³)

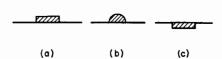


FIG. 12-17 Dielectric image lines and channel guide. (a) and (b) Image lines (identical λ/λ_z if cross section, areas are the same). (c) Channel guide.

the $\sin \xi/\xi$ pattern shown in Fig. 12-7 by the factor $\cos [(\pi d/\lambda \sin \theta)]$ (but the predicted sharp nulls do not in fact exist).

Figure 12-16b shows details of a conventional feed that has proved itself in practice. Other feeds are illustrated in Figs. 12-6 and 12-13. In the case of waveguide feeds, it has been found desirable, ¹⁷ both for snug fitting and for sidelobe suppression, to wrap dielectric tape around the feed point or, equivalently, to let the diameter of the waveguide feed be slightly smaller than that of the dielectric rod at the feed point, as shown in Fig. 12-6b. If $\epsilon > 8$, the rod can be fed over a narrow band by direct insertion in the narrow side of a waveguide, or in a cavity.⁴⁴

Dielectric Channel Guide^{28,45,46} (Fig. 12-17c)

Two modes are of interest: a vertically polarized one that is a deformation of the HE_{11} rod mode and a horizontally polarized one. The phase velocity of the vertically polarized mode is very slightly faster in Fig. 12-17c than in Fig. 12-17a or b. The mode may be slightly leaky (small attenuation in the axial direction), but this is not known with certainty. The structure can be viewed as a channel of the type shown in Fig. 12-2b, but with most of the sidewalls removed. The phase velocity is then determined as follows: we rewrite Eq. (12-5b) in the form

$$\frac{\lambda}{\lambda_z} = \sqrt{\left(\frac{\lambda}{\lambda_z'}\right)^2 - \left(\frac{\lambda}{2\omega}\right)^2}$$

where λ/λ_s' is the relative phase velocity on an infinitely wide slab-on-metal, as given in Fig. 12-19c. Removal of the sidewalls above the dielectric-air interface appears to have negligible effect on the phase velocity²⁸ and, at least as long as $\lambda/\lambda_s > 1$ (ω is not too narrow), introduces little if any leakage attenuation.

The horizontally polarized mode is the lowest-order TE mode in the channel of Fig. 12-2b (slightly perturbed by the removal of most of the sidewalls), which in turn is identical with the lowest-order TE mode on a dielectric slab-on-metal (solid curves, Fig. 12-19d).

The dielectric-filled channel also supports leaky waves, and care must be taken not to choose parameters that allow these to be excited.

Yagi-Udas 13,19,47-62

These are sometimes referred to as *ladder* arrays. Figure 12-18 shows that the phase velocity is controlled by adjusting the spacing, height, and diameter of the monopole elements. The dispersion is more pronounced than on a dielectric rod, and the best-reported bandwidth (within which the gain drops no more than 3 dB) is only \pm 10 percent; this can perhaps be improved by application of the broadband design method described in Sec. 16-3. The bandwidth of an array of Yagis is at best \pm 5 percent.

The curves in Fig. 12-18 apply to the row of monopoles shown in Fig. 12-6a and equally to a row of dipoles (element height 2h). A center boom for mounting the dipole elements has negligible effect on the phase velocity provided the total dipole span 2h includes the boom diameter. Yagi-Udas can be photoetched on a copper-clad dielectric sheet; 50,51 since the dielectric slows down the wave, the element height needed to produce a given phase velocity is less than indicated in Fig. 12-18.

Dielectric Sheets and Panels^{4,7,31-33,63-68}

Because of the imaging properties of vertically polarized waves, the lowest-order TM mode on a dielectric sheet-on-metal is identical with that on a panel of twice the sheet thickness (Fig. 12-19 a-c). This wave has no cutoff frequency; its properties are discussed in Sec. 12-2, and Fig. 12-4 shows the field configuration.

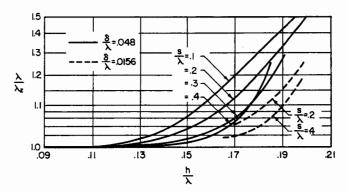


FIG. 12-18 Relative phase velocity on Yagi-Uda antenna. (After Ehrenspeck and Poehier. 13) For the meaning of parameters, see Fig. 12-6a.

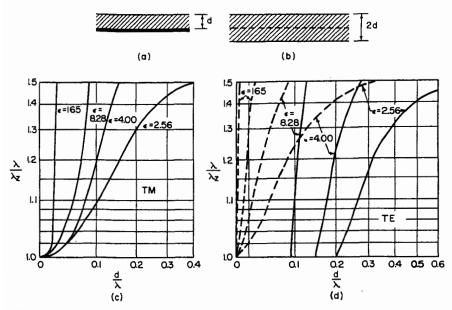


FIG. 12-19 Dielectric sheets and panels. (a) Sheet-on-metal. (b) Panel. (c) Lowest-order TM mode on sheet or panel (d) Lowest-order TE mode on sheet (solid curves) and panel (dashed curves).

The lowest-order horizontally polarized wave on a dielectric sheet-on-metal produces a null in the end-fire direction and has a cutoff (solid curves, Fig. 12-19d). On a panel, on the other hand, the lowest-order horizontally polarized wave produces a maximum in the end-fire direction and has no cutoff (dashed curves, Fig. 12-19d). (The next higher TE mode on the panel is identical with the lowest TE mode on the sheet, but because of the end-fire null it is not a useful mode).

In designing tapered sheets on metal, a flush air-dielectric interface can be maintained by contouring the depth of ground plane. Good contact between dielectric and ground plane is needed, since air spaces affect the phase velocity.⁷

Circular dielectric disks⁶⁶ and spherical caps^{32,33} are useful as omnidirectional beacon antennas. For design principles, see Sec. 12-3 (paragraphs on the effect of finite ground plane on the radiation pattern and on beam-shaping techniques). Figure 12-19c and d is still applicable, since λ/λ_z is only slightly affected by a decreasing radius of curvature. The leakage attenuation has been calculated by Elliott.³² Patterns provide good null filling to 45° off end fire and have a bandwidth of \pm 8 percent.³³

Circular (or cross) polarization can be produced if the surface-wave structure supports a TM and a TE wave with identical phase velocities. One example is the two-layer dielectric sheet, ^{7,67} illustrated in Fig. 12-20 a for the case in which the lower layer is air. Given λ/λ_z , Fig. 12-20 b prescribes the layer thickness (with $\epsilon = \epsilon_l/\epsilon_0$ as a parameter). Another, structurally superior example is the simple-layer dielectric in which longitudinal metal vanes that short out the vertically polarized mode while leaving the horizontally polarized one unperturbed are embedded (Fig. 12-20 c). The TM

wave therefore "sees" a thinner sheet than the TE wave, and for a prescribed λ / λ_x Fig. 12-20c and d gives the values (in

first approximation) of the vane height and total layer thickness. For details, see Hansen.⁶⁸

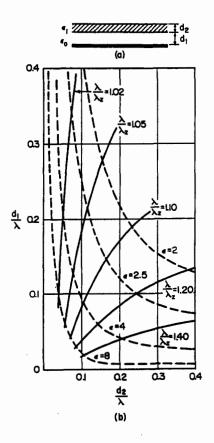


Fig. 12-20 Circular (or cross) polarization on dielectric sheets. (a) A simple double-layer structure. (b) Parameter combinations (with $\epsilon = \epsilon_1/\epsilon_0$) that allow (a) to support a circularly polarized surface wave with λ/λ_z between 1.02 and 1.40. (From Piummer and Hansen. et al. (c) Longitudinal metal vanes embedded in dielectric. (After Ref. 68.)

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Helical Antennas

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13-1 Introduction 13-2

13-2 Axial-Mode Helical Antennas 13-3
Impedance and VSWR 13-3
Uniform-Diameter Helices 13-5
Nonuniform-Diameter and Tapered
Helices 13-13

13-3 Array of Helical Antennas 13-17

13-4 Normal-Mode Helical Antennas 13-18

13-5 Other Helical Antennas 13-19

A helical antenna consists of a single conductor or multiple conductors wound into a helical shape. Although a helix can radiate in many modes, the axial mode and the normal mode are the ones of general interest. The axial mode, the most commonly used mode, provides maximum radiation along the helix axis, which occurs when the helix circumference is of the order of one wavelength. The normal mode, which yields radiation broadside to the helix axis, occurs when the helix diameter is small with respect to a wavelength. Higher-order-radiation modes are also possible; e.g., when the helix dimensions exceed those required for the axial mode, a conical or multilobed pattern will result, as illustrated in Fig. 13-1.

The basic concepts of a helix antenna were established by Kraus^{1,2} in 1947, and much of Kraus's early results was summarized by Harris.³ Generally, helical antennas are wound with a single conductor. However, a helix can be designed with bifilar,⁴ quadrifilar,^{5,6} or multifilar,⁷ windings. Radiation characteristics of bifilar helices operating in the backfire mode have been described by Patton.⁸ An advantage of a backfire helix is that it does not generally require a ground plane.

The helix-antenna parameters are defined as follows (see Fig. 13-2):

D = diameter of helix (center to center)

 $C = \text{circumference of helix} = \pi D$

S =spacing between turns (center to center)

 $\alpha = \text{pitch angle} = \tan^{-1} (S/\pi D)$

N = number of turns

L = axial length of helix = NS

d = diameter of helix conductor

 $\ell = \text{length of one turn} = \sqrt{(\pi D)^2 + S^2}$

Although helical antennas are normally constructed with a circular cross section, elliptical helical antennas have also been investigated.9

This chapter presents detailed helical-antenna design information. Measured impedance, pattern, gain, and axial-ratio characteristics are shown for a variety of

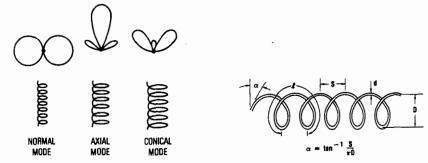


FIG. 13-1 Three radiation modes of a helical antenna.

FIG. 13-2 Helix geometry.

helical-antenna configurations. Empirical relations which express the antenna radiation performance characteristics as a function of wavelength and the helix design parameters (diameter, pitch angle, and number of turns) are derived on the basis of measured data.

13-2 AXIAL-MODE HELICAL ANTENNAS

The helical beam antenna is a very simple structure possessing a number of interesting properties including wideband impedance characteristics and circularly polarized radiation. It requires a simple feed network, and its radiation characteristics are reasonably predictable. Either right-hand or left-hand circular polarization may be gen-

erated by a helical beam antenna. A helix wound like a right-hand screw radiates or receives right-hand circular polarization, while a helix wound like a left-hand screw radiates or receives left-hand circular polarization.

Helical antennas are generally constructed with a uniform diameter and operated in conjunction with a ground plane, cavity, or helical launcher. However, as will be shown, nonuniform-diameter helical structures can be employed to widen the bandwidth of a uniform-diameter helical antenna and improve radiation performance characteristics. 11,12

A typical uniform-helix configuration is shown in Fig. 13-3. The helix is backed by a circular cavity, rather than a conventional ground plane, to reduce the

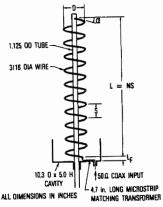


FIG. 13-3 Mechanical arrangement of a cavity-backed helix for 650 to 1100 MHz.

back radiation and enhance the forward gain. Although the helix of Fig. 13-3 was designed specifically to operate in the ultrahigh-frequency (UHF) range from about 650 to 1100 MHz, the helix and the cavity dimensions can be scaled to other frequencies of operation as well. The helix is fed by a coaxial connection at the bottom of the cavity. The helical conductor can be made from round tubing or flat strip and supported with a lightweight foam dielectric cylinder or by radial dielectric rods. The center mechanical support can be constructed from either metal or dielectric material.

Impedance and VSWR

The impedance characteristics of a helical antenna have been established by Glasser and Kraus. When the helix circumference is less than two-thirds wavelength, the terminal impedance is highly sensitive to frequency changes. However, when the circumference is of the order of one wavelength (axial mode), the terminal impedance is nearly a pure resistance and is given approximately (within \pm 20 percent) by the empirical relation $R=140~C/\lambda~\Omega$. The relatively constant terminal impedance may be explained by the rapidly attenuating character of the total outgoing wave near the input end and the total reflected wave near the open end. \(^{14}

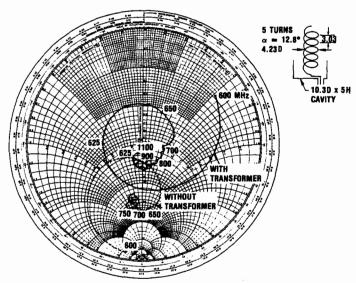


FIG. 13-4 Impedance characteristics of a five-turn helix with and without an impedance-matching transformer.

For the UHF helix configuration of Fig. 13-3, a 4.7-in- (119-mm-) long, linear-taper impedance transformer is used to match the 140- Ω helix to the 50- Ω coaxial line. The transformer is a microstripline constructed from Teflon-fiberglass printed-circuit board. The same transformer can be used for all axial-mode helices—uniform-, tapered-, or nonuniform-diameter. Another approach to attain a 50- Ω impedance for helical beam antennas has been described by Kraus. 15

Figure 13-4 depicts the impedance characteristics of a five-turn helix with and without the impedance-matching transformer, and Fig. 13-5 depicts the voltage-

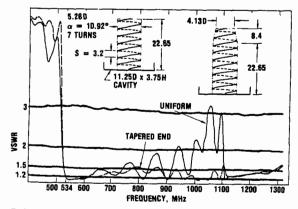


FIG. 13-5 VSWR of a seven-turn uniform helix and the same helix with two additional turns wound on a tapered diameter.

standing-wave-ratio (VSWR) response measured at the input of the matching transformer for a seven-turn uniform helix and also for the same helix with two additional turns of tapered diameter, as illustrated by the inset. By adding the two-turn end taper, a significant reduction in VSWR over a wide frequency band can be achieved (dashed curve). The reduction in VSWR is due to the suppression of the reflected currents by the tapered end section. ^{16,17} Also, it is noted that the low-frequency characteristics are essentially unchanged with the cutoff at ~ 534 MHz, corresponding to $C/\lambda \sim 0.75$, where C is the circumference of the 5.28-in- (134.1-mm-) diameter helix. The low-frequency cutoff characteristics agree well with theoretical predictions. ^{1,2} The VSWR characteristics for longer helices are generally similar to those of Fig. 13-5.

Uniform-Diameter Helices

As a first approximation, the radiation pattern of an axial-mode helix may be obtained by assuming a single traveling wave of uniform amplitude along the conductor. By the principle of pattern multiplication, the far-field pattern is the product of the pattern of one turn and the pattern of an array of N isotropic elements with spacing S, where N equals the number of turns and S is the spacing between turns. If the pattern of a single turn is approximated by $\cos \theta$, where θ is the angle measured from the axis of the helix, the total radiation pattern becomes

$$E(\theta) = A \frac{\sin{(N\psi/2)}}{\sin{(\psi/2)}} \cos{\theta}$$
 (13-1)

where A = normalization factor

$$\psi = \frac{2\pi}{\lambda} S \cos \theta - \delta \tag{13-2}$$

$$\delta = \frac{2\pi}{\lambda} \frac{\ell}{(\upsilon/c)} = \text{progressive phase between turns}$$

 ℓ = length of one turn

v =phase velocity along helical conductor

c =velocity of light in free space

Kraus² has shown that for an axial-mode helix the relative phase velocity, p = v/c, of the wave propagating along the helical conductor is in close agreement with that required to satisfy the Hansen-Woodyard condition for an end-fire array with increased directivity¹⁸; i.e.,

$$p = \frac{(\ell/\lambda)}{(S/\lambda) + (2N+1)/2N}$$
 (13-3)

Thus, for the increased-directivity condition, the quantity ψ may be written as

$$\psi = \frac{2\pi}{\lambda} S(\cos \theta - 1) - \frac{\pi}{N}$$
 (13-4)

and

$$A = \sin\left(\pi/2N\right) \tag{13-5}$$

The radiation is elliptically polarized. The ellipticity ratio or axial ratio (AR) of an N-turn helix operating in the axial mode for the increased-directivity condition is given by

$$AR = \frac{2N+1}{2N}$$
 (13-6)

If N is large, the axial ratio approaches unity and the polarization is nearly circular. In a practical situation, the observed axial ratio may be expected to deviate somewhat from the theoretical value for various reasons such as methods of construction, tolerances, instrumentation, and range errors. For a uniform helix consisting of at least a few turns, an axial ratio of the order of 1 dB is not uncommon.

To provide parametric design equations for axial-mode helices, Kraus² has suggested the following relations for the half-power beamwidth (HPBW) and gain (G) as a function of C/λ and NS/λ for constant-pitch helices with $12^{\circ} < \alpha < 15^{\circ}$, $\% < C/\lambda < \%$, and N > 3:

HPBW =
$$K_B/(C/\lambda) \sqrt{NS/\lambda}$$
 (13-7)

$$G = K_G(C/\lambda)^2(NS/\lambda)$$
 (13-8)

where K_B is the HPBW factor, K_G is the gain factor, $C = \pi D$ is the circumference, and NS is the axial length. On the basis of a number of pattern measurements on helices < 10 turns, Kraus quasi-empirically established $K_B = 52$. Also, he derived $K_G = 15$ for the directive gain (lossless antenna) based on the approximation $G = 41,250/(\text{HPBW})^2$, where HPBW is in degrees. A gain-beamwidth product $G = (\text{HPBW})^2 < 41,250$ is generally expected for most practical antennas¹⁹ because of minor-lobe radiation and beam-shape variations.

Additional data on the radiation characteristics of axial-mode helices are available in the literature. 11,20-22 The low-frequency and high-frequency limits were investigated by Maclean and Kouyoumjian²⁰ and by Maclean. 23 In a practical situation, the pattern and gain versus frequency characteristics are of interest to the antenna designer. Such data would allow the designer to optimize the helix parameters for operation over a specified bandwidth.

The discussions which follow summarize the results of an extensive study of the gain and pattern characteristics of uniform helical antennas, one to eight wavelengths long, in the UHF range from about 650 to 1100 MHz. With reference to Fig. 13-3, the helices were constructed by winding %-in-diameter copper tubing about a Styrofoam cylindrical form that was concentric with the 1.125-in-diameter metallic support tube. The helix dimensions can be scaled to other frequencies of operation with essentially the same radio-frequency performance characteristics. All gain and pattern measurements were made with respect to the phase center of the helix, which was estimated to be one-fourth of the helix length from the feed point.²⁴

Fixed-Length Helix Figures 13-6 and 13-7 show the gain and HPBW versus frequency characteristics, respectively, of a 30-in- (762-mm-) long (NS = 30 in) and 4.3-in- (109.22-mm-) diameter helix for three helix pitch angles ($\alpha = 12.5$, 13.5, and 14.5°). The helix with a smaller pitch angle (more turns per unit length) yields a higher peak gain and a lower cutoff frequency. With N = 8.6 to 10 turns, it appears that the gain-frequency slope is approximately proportional to f^3 and the HPBW-frequency slope is approximately proportional to $f^{-3/2}$, where f equals the frequency, which are in general agreement with Kraus for $C/\lambda < 1.1$ [see Eqs. (13-7) and (13-8)]. However, as will be shown later, experimental data indicate that the gain-frequency slope depends on the antenna length and is approximately proportional to f^{N} .

Figures 13-8 and 13-9 show the gain and HPBW characteristics, respectively, of

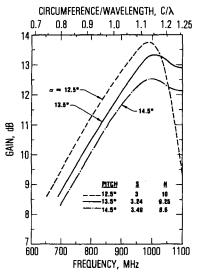


FIG. 13-6 Gain versus frequency of a fixed-length (NS = 30 in, or 762 mm) helix; $\alpha = 12.5^{\circ}$, 13.5° , and 14.5° , D = 4.3 in (109 mm).

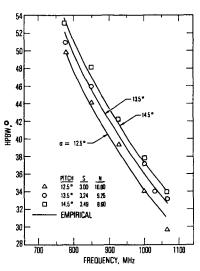


FIG. 13-7 Half-power beamwidth versus frequency of a fixed-length helix (NS=30 in, or 762 mm); $\alpha=12.5^{\circ}$, 13.5°, and 14.5°, D=4.3 in (109 mm).

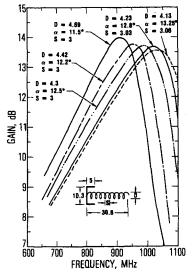


FIG. 13-8 Gain of a fixed-length (NS = 30 in, or 762 mm) helical antenna with different diameters.

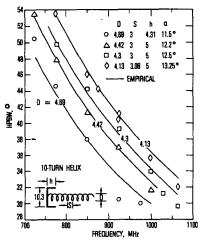
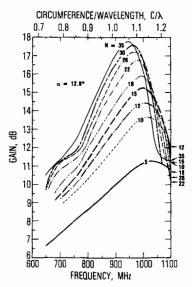


FIG. 13-9 Half-power beamwidths of a 10-turn fixed-length (NS = 30 in, or 762 mm) helix with different diameters.



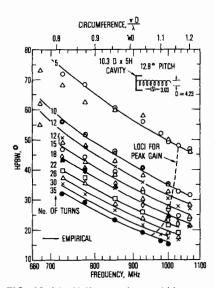


FIG. 13-10 Gain versus frequency for a 5-to 35-turn helix; $\alpha = 12.8^{\circ}$, D = 4.23 in (107.4 mm).

FIG. 13-11 Half-power beamwidth versus frequency for a 5- to 35-turn helix; $\alpha = 12.8^{\circ}$, D = 4.23 in (107.4 mm).

a 30-in-long ($N \approx 10$ turns) helix with variable diameter and pitch angle. The peak gain varies by less than 0.5 dB. In general, a slightly higher peak gain is observed for a larger-diameter helix with a smaller pitch angle, but the bandwidth is narrower than that of a smaller-diameter helix with a larger pitch angle.

The axial ratio, a measure of the purity of the circularly polarized wave, is generally less than 1.5 dB for $0.8 < C/\lambda < 1.2$. The axial ratio can be improved by tapering the last two turns of the helix, particularly at the high end of the band.^{12,17,25}

Variable-Length Hellx Figures 13-10 and 13-11 show the gain and HPBW versus frequency, respectively, of helices consisting of 5 to 35 turns with constant pitch ($\alpha = 12.8^{\circ}$, S = 3.03 in, or 76.96 mm) and constant diameter (D = 4.23 in, or 107.4 mm). These helices were designed to operate over the UHF test frequencies with the helix circumference varied from 0.75 λ to 1.25 λ . N was selected as 5, 10, 12, 15, 18, 22, 26, 30, and 35 turns. The gain is referred to a circularly polarized illuminating source. The gain curves reveal that the peak gain occurs at $C/\lambda = 1.55$ for N = 5 and at a lower value, $C/\lambda = 1.07$, for N = 35. The gain-frequency slope is not proportional to f^3 for all values of N [see Eq. (13-8)]; e.g., for N = 5 the gain varies approximately as $f^{2.5}$, and for N = 35 the gain follows approximately an f^6 slope, where f is the frequency.

Typical measured radiation patterns for N=5, 10, 18, and 35 are shown in Fig. 13-12. The axial ratio is ~ 1 dB over most of the measurement frequency range and is slightly higher at the band edges. The HPBWs are generally within $\pm 1^{\circ}$ in the two orthogonal principal planes. At frequencies a few percent above the peak gain frequency, the patterns begin to deteriorate. The beamwidth broadens rapidly, and the first sidelobes merge with the main lobe as the operating frequency approaches the upper limit.

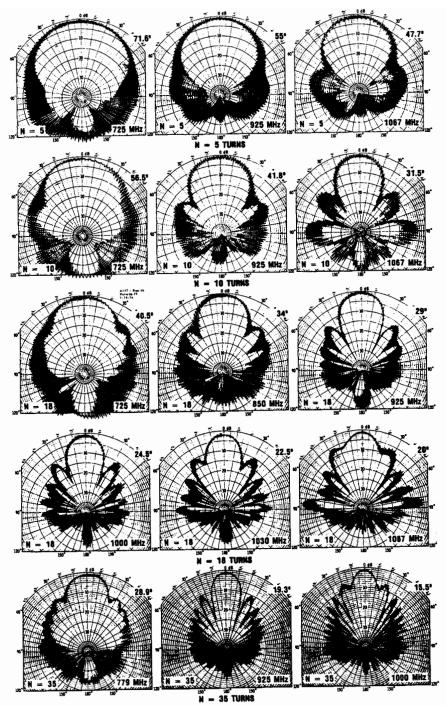


FIG. 13-12 Typical radiation patterns of a 5- to 35-turn helix; $\alpha = 12.8^{\circ}$, D = 4.23 in (107.4 mm).

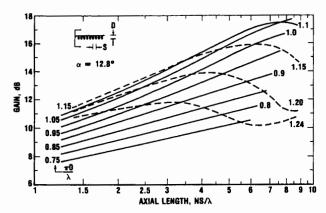


FIG. 13-13 Parametric helix-antenna gain curves as a function of axial length with circumference as a parameter.

Parametric helix characteristic curves—gain and halfpower beamwidth—for the 4.23-in- (107.4-mm-) diameter constant-pitch ($\alpha=12.8^{\circ}$) helix are shown in Figs. 13-13 and 13-14, respectively, as a function of axial length NS/λ with circumference $\pi D/\lambda$ as a parameter. Thus, for a specified length and diameter the helix gain and HPBW can be estimated.

Figure 13-15 depicts the gain-beamwidth product K = G (HPBW)² based on the measured gain data of Fig. 13-10 and the HPBW data of Fig. 13-11. The quantity K is useful for estimating the gain when the HPBW is known, and vice versa. It should be noted, however, that the gain-beamwidth product is not constant but depends on N

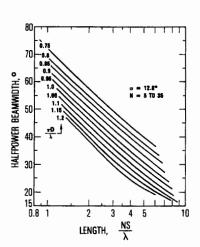


FIG. 13-14 Parametric helix-antenna halfpower-beamwidth curves as a function of axial length with circumference as a parameter.

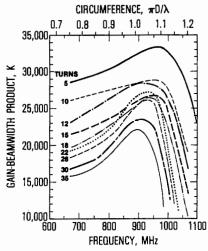


FIG. 13-15 Gain-beamwidth products of a 5- to 35-tum helix; $\alpha = 12.8^{\circ}$, D = 4.23 in (107.4 mm).

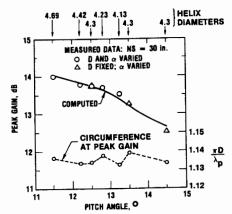


FIG. 13-16 Peak gain of a fixed-length helix (NS = 30 in, or 762 mm) as a function of a pitch angle.

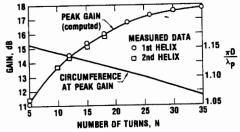
and frequency. All curves have been smoothed to within ± 5 percent of the measureddata points.

Empirical Relations On the basis of the gain data of Figs. 13-6, 13-8, and 13-10, the peak gain may be empirically expressed as11

$$G_p = 8.3 \left(\frac{\pi D}{\lambda_p}\right)^{\sqrt{N+2}-1} \left(\frac{NS}{\lambda_p}\right)^{0.8} \left[\frac{\tan 12.5^{\circ}}{\tan \alpha}\right]^{\sqrt{N}/2}$$
 (13-9)

where λ_p is the wavelength at peak gain. The computed values for the fixed-length helices (NS = constant) are within ± 0.1 dB of the measured data as depicted in Fig. 13-16. The data points indicated by the circle were obtained by varying the diameter and pitch angle while keeping the length constant with N = 10 turns, and those indicated by the triangle were obtained by varying the pitch angle while keeping the length and diameter constant ($N \approx 8.6$ to 10). The diameters of the various experimental helices are shown on the top of the figure. For these fixed-length helices, the peak gains occur at nearly the same circumference, $\pi D/\lambda \sim 1.135$.

Figure 13-17 is a plot of the peak gain versus N for a constant-pitch ($\alpha = 12.8^{\circ}$)



Peak gain of a variable-length helix FIG. 13-17 with $\alpha = 12.8^{\circ}$.

helix. The corresponding values of C/λ_p are also shown in the figure, where λ_p is the wavelength at peak gain. The peak gain is not quite proportional to the number of turns; i.e., doubling the number of turns does not yield a 3-dB increase in the peak gain. The computed values for the peak gain, using Eq. (13-9) with $\alpha = 12.8^{\circ}$ and N = 5 to 35 turns, are within \pm 0.1 dB of the measured data.

A similar empirical expression for the HPBW is as follows:26

HPBW
$$\approx \frac{K_B \left(\frac{2N}{N+5}\right)^{0.6}}{\left(\frac{\pi D}{\lambda}\right)^{\sqrt{N}/4} \left(\frac{NS}{\lambda}\right)^{0.7}} \left(\frac{\tan \alpha}{\tan 12.5^{\circ}}\right)^{\sqrt{N}/4}$$
 (13-10)

where K_B is a constant in degrees. For the helices constructed by using the arrangement of Fig. 13-3, it was found that, with $K_B \simeq 61.5^{\circ}$, Eq. (13-10) matches the measured data within \pm a few percent over the useful operating frequency range of the helix as shown in Figs. 13-7, 13-9, and 13-11. For helices that employ a different construction technique (e.g., tape helices that are wound on a dielectric support instead of using a metallic central support rod), Eq. (13-10) can still be applied, but a slightly different value of K_B must be used. The measured HPBWs for the helices investigated are generally 10 to 20 percent wider than Kraus's formula [Eq. (13-7)]. It should be mentioned that Eqs. (13-9) and (13-10) are not unique; however, these relations are useful as a design tool.

The helix bandwidth may be defined as the operating frequency range over which the gain drops by an allowable amount. The -3-dB and -2-dB bandwidths as a function of N may be obtained by using the curves of Fig. 13-18. For example, if the -3-dB or -2-dB bandwidth is desired for a given N, one determines the values of $\pi D/\lambda_h$ and $\pi D/\lambda_t$ from Fig. 13-18, where λ_h and λ_t are the free-space wavelengths corresponding to the upper frequency limit f_h and the lower frequency limit f_t respectively. The choice of a -3-dB or -2-dB bandwidth depends upon the antenna designer's application. The frequency limits f_h and f_t may be determined by using the mea-

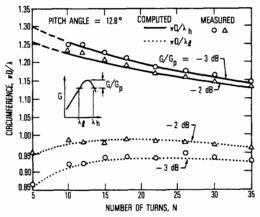


FIG. 13-18 Gain-bandwidth characteristics of a uniform helix with $\alpha = 12.8^{\circ}$.

sured gain data of Fig. 13-10. Note that the gain varies approximately as $f^{\sqrt{N}}$ for $f < f_p/1.04$ and as $f^{-3\sqrt{N}}$ for $f > 1.03 f_p$, where f_p is the frequency at peak gain. On the basis of these observations, the bandwidth frequency ratio may be empirically expressed as¹¹

$$\frac{f_h}{f_t} \approx 1.07 \left(\frac{0.91}{G/G_p}\right)^{4/(3\sqrt{N})} \tag{13-11}$$

where G_p is the peak gain from Eq. (13-9). The computed bandwidth characteristics for $G/G_p=-3$ dB and -2 dB agree reasonably well with the measured data as shown in Fig. 13-18. The bandwidth decreases as the axial length of the helix increases. This bandwidth behavior follows the same trends described by Maclean and Kouyoumjian, ²⁰ although these authors employ a sidelobe criterion rather than a gain criterion. Beyond the $G/G_p=-3$ dB point the gain drops off sharply at the high-frequency end as the upper limit for the axial mode is approached.

Nonuniform-Diameter and Tapered Helices

The tapered-diameter^{27,28} and nonuniform-diameter¹² helices represent additional types of axial-mode helical antennas. These helical configurations are capable of providing a wider bandwidth than a conventional uniform (constant-diameter) helix. A nonuniform helix consists of multiple uniform-diameter helical sections that are joined together by short tapered transitions. Some studies have been made to investigate the broadband-frequency response of nonuniform-diameter helical antennas.^{29,30} The various types of helical-antenna configurations (uniform, tapered, and nonuniform-diameter) are shown in Fig. 13-19, and the radiation performance characteristics are described in Ref. 12.

The experimental helices were wound with thin copper strips 0.468 in (11.887 mm) wide. The plane of the strip (the wide dimensions of the strip) was wound orthogonally to the helix axis similarly to a Slinky toy. Helices wound with round conductors or with metallic tapes (wound so that the plane of the tape is parallel to the helix axis) yield similar results. A constant-pitch spacing of 3.2 in (81.28 mm) was selected, and the helix was backed by an 11.25-in- (285.75-mm-) diameter × 3.75-in- (95.25-mm-) high cavity. The feed arrangement and the metallic central support tube are similar to those of Fig. 13-3. The VSWR of a nonuniform helix is ≤ 1.5:1 over the test frequency range of 650 to 1100 MHz (similar to the dashed curve of Fig. 13-5).

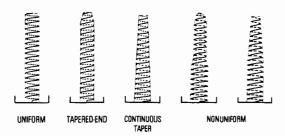


FIG. 13-19 Various axial-mode helical configurations.

Tapered-End Hellx For reference purposes, the gain and axial-ratio characteristics of an 18-turn uniformly wound helix, with D=4.59 in (116.59 mm) and $\alpha=12.5$ °, are shown in Fig. 13-20. Also shown in this figure are the gain and axial-ratio characteristics of a similar helix with the same overall length, but the diameter of the last two turns is tapered from 4.59 in to 2.98 in (75.69 mm). It can be seen that the end taper provides a marked improvement in axial-ratio characteristics, 12,16,17

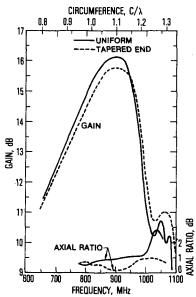


FIG. 13-20 Gain and axial-ratio characteristics of an 18-turn uniformly wound and tapered-end helix.

although the peak gain is reduced slightly. Figure 13-21 compares the radiation patterns of a uniform and a tapered-end helix measured at the same frequency. The HPBWs are approximately the same, but the axial-ratio improvement is observed over the entire pattern (on axis and off axis). Similar results have been reported by Donn.²⁵

Continuously Tapered Helix The gain and axial characteristics of a continuously tapered helix, ¹² often referred to as a conical helix, are shown in Fig. 13-22. The helix consists of 17.64 turns with a constant-pitch spacing of 3.2 in (81.28 mm) and tapers from a 5.32-in (135.13-mm) diameter at the base to a 2.98-in (75.69-mm) diameter at the top (see inset). Typical measured patterns are shown in Fig. 13-23. The peak gain is slightly lower than that of the uniform helix, but the pattern characteristics and bandwidth performance are much better.

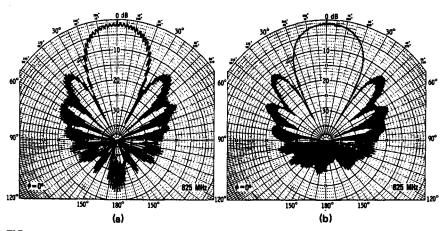


FIG. 13-21 Radiation patterns of an 18-turn (a) uniform and (b) tapered-end helix.

Nonuniform-Diameter Helix A nonuniform helix provides a unique approach for widening the bandwidth of a helical antenna with improved gain and pattern characteristics. It may be constructed with two or more uniform helix sections of different diameters or a combination of uniform and tapered sections. The dimensions of the different helical sections (diameter, number of turns, etc.) can be varied to synthesize an antenna with a specific gain-frequency response. ^{12,31}

Two nonuniform helical configurations and the corresponding gain and axialratio characteristics are illustrated in Fig. 13-24. Configuration a consists principally

of two uniform-diameter sections [5.28] and 4.13 in (134.1 and 104.9 mm)] joined together by a short tapered transition. This helix may be described as 7turn (5.28 D) + 2-turn taper (5.28 D) to 4.13 D) + 6.64-turn (4.13 D) + 2-turn end taper (4.13 D to 2.98 D). A constantpitch spacing of 3.2 in (81.28 mm) was maintained in all four helical sections. The performance of this nonuniform helix configuration was optimized over the low-frequency region. The gain is $14.7 \pm 0.4 \text{ dB from } 773 \text{ to } 900 \text{ MHz and}$ remains relatively flat (14.05 \pm 0.25 dB) from 900 to 1067 MHz. Note that the gain is constant within ± 1 dB over a frequency ratio of 1.55:1 (1100/710 MHz) as compared with 1.26:1 for a uniform helix. Table 13-1 provides a comparison of the ±1-dB bandwidth for the various axial-mode helical antennas. The axial

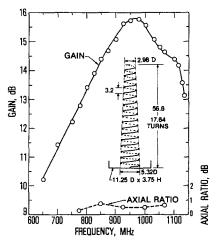


FIG. 13-22 Gain and axial-ratio characteristics of a 17.64-turn conical helix.

ratio is < 1 dB. The beam-shape and sidelobe characteristics are improved over those of a uniform helix as illustrated in the patterns of Fig. 13-25. Note that the high-frequency cutoff is limited not by the larger 5.28-in-diameter helical section ($C/\lambda = 1.55$ at 1100 MHz) but rather by the smaller 4.13-in-diameter helical section ($C/\lambda = 1.21$ at 1100 MHz). The HPBW is relatively constant, 33° \pm 3° over the 773- to 1067- MHz test frequency range. 12

Configuration b of Fig. 13-24 consists of a uniform section (5.28-in diameter) plus a tapered section from 5.28- to 2.98-in diameter. The \pm 1.1-dB gain bandwidth is wider than that of configuration a, but the gain at the high-frequency end is lower.

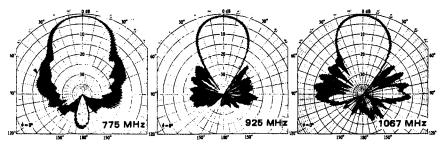


FIG. 13-23 Radiation patterns of a 17.64-turn conical helix.

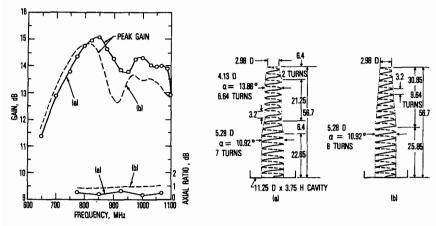


FIG. 13-24 Gain and axial-ratio characteristics of two 17.64-turn nonuniform-diameter helices.

TABLE 13-1

Type of helix	Frequency range with ±1-dB gain variation, MHz	Frequency ratio,
Uniform	770–970	1.26:1
Tapered-end	770-980	1.27:1
Continuous-taper	820-1120	1.37:1
Nonuniform	710–1100	1.55:1

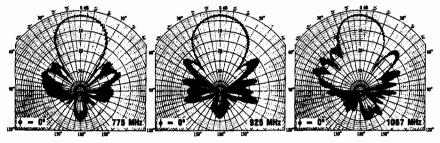


FIG. 13-25 Radiation patterns of a 17.64-turn nonuniform-diameter helix—configuration a of Fig. 13-24.

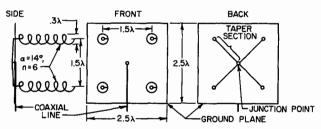


FIG. 13-26 2 x 2 array of six-turn helices.

13-3 ARRAY OF HELICAL ANTENNAS

A single axial-mode helical antenna produces moderate gain in the end-fire direction (see Fig. 13-17). When higher gain is desired, a linear or planar array of helices may be used to produce a fan-shaped beam or a pencil beam respectively. The array gain depends on the element spacing with respect to the operating wavelength and the element gain. To realize the advantage of the increased gain, the helical elements should be spaced so that the area occupied by each helix is approximately equal to its effective area. To the first-order estimate, this spacing is $\sim \sqrt{G_e/4\pi} \lambda$, where G_e is the power gain of the individual helices. As the spacing is increased to $> \sqrt{G_e/4\pi} \lambda$, the array gain approaches the asymptotic value NG_e , where N is the number of elements.³²

Some measured data on this type of array have been reported by Harris, 3,33 and the construction and the radiation characteristics of a typical 2 x 2 planar array of six-turn helices ($D=0.3\lambda$ and $\alpha=14^{\circ}$) spaced 1.5λ are shown in Figs. 13-26 and 13-27 respectively. Also, shaped-beam and steerable arrays employing axial-mode helices have been designed for spacecraft applications. 22,34,35

Generally, arrays employing highgain elements are not suitable for wideangle scanning because of grating lobes. However, when antenna gain and sidelobes (or grating lobes) are not important, such arrays can be phased to scan over a limited angular range.

For certain applications, such as FM and TV broadcasting, a moderately high-gain, azimuthally omnidirectional pattern is required. A vertical array of side-fire helices mounted concentrically on a conducting cylinder may be employed to produce a narrow-beam pattern in the elevation plane. The helix ele-

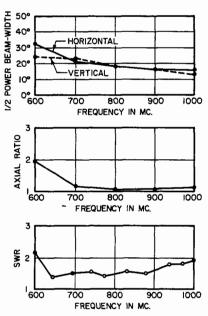


FIG. 13-27 Measured characteristics of a 2 x 2 array of six-turn helices.

ments are generally excited in the second- or higher-order modes which produce maximum radiation broadside (normal) to the helix axis and a null along the helix axis. The helix diameter and pitch are chosen so that the length of one turn is equal to an integral number of wavelengths.

If horizontal polarization is desired, the radiating element may be constructed with two oppositely wound helices (one right-handed and the other left-handed), each consisting of a few turns, placed end to end and fed in the center. Design data on this type of vertical array are available in the literature. 3,36,37

Vertical helical-array antennas designed to produce omnidirectional, circularly polarized radiation in the horizontal plane for VHF-UHF TV broadcasting (Chap. 28) have been described by DuHamel. ³⁸ In this case, the radiating elements are endfed, four-turn bifilar helices operating in various modes which are selected so that the helix circumference is about $\lambda/2$ greater than the circumference of the central support cylinder. Depending on the operating frequency, horizontal circularity of ± 0.5 dB to ± 1 dB and an axial ratio of ~ 1.5 dB have been reported.

13-4 NORMAL-MODE HELICAL ANTENNAS

When the dimensions of the helix are small compared with wavelength, the maximum radiation is in a direction normal to the helix axis. Kraus² has shown that the radiation from a short-axial-length helix can be calculated by assuming that the helix is composed of small loops of diameter D and short dipoles of length S. The far field of a short dipole has only an E_{θ} component,

$$E_{\theta} = \frac{jBe^{-jkr}}{r} \left(\frac{S}{\lambda}\right) \sin \theta \qquad (13-12)$$

and the far field of a small loop has only an E_{ϕ} component,

$$E_{\phi} = \frac{Be^{-jkr}}{2r} \left(\frac{\pi D}{\lambda}\right)^2 \sin\theta \qquad (13-13)$$

where r is the distance and B is a constant. The E_{\bullet} and E_{\bullet} components are 90° out of phase, and the far field of a small helix is, in general, elliptically polarized. The axial ratio is given by

$$AR = \frac{|E_{\theta}|}{|E_{\phi}|} = \left(\frac{2S}{\lambda}\right) / \left(\frac{\pi D}{\lambda}\right)^{2}$$
 (13-14)

When $\pi D = \sqrt{2S\lambda}$, the axial ratio becomes unity and the radiation is circularly polarized.³⁹ On the other hand, the polarization of the radiated field will be predominantly horizontal $(AR \rightarrow 0)$ when $\pi D \gg \sqrt{2S\lambda}$ or predominantly vertical $(AR \rightarrow \infty)$ when $\pi D \ll \sqrt{2S\lambda}$.

For a normal-mode helix whose dimensions are small compared with wavelength, the current distribution along the helix is approximately sinusoidal.² The terminal impedance is very sensitive to changes in frequency, and the bandwidth is narrow. Nevertheless, a normal helix has been used as an effective means for reducing the

length of thin-wire-type (whip) antennas for personal radio and mobile communications systems in the HF and VHF bands.⁴⁰⁻⁴³ Also, balanced-fed dipole antennas can be constructed by using short-axial-length normal-mode helices when a reduced dipole length is desired.⁴⁴

When a short normal-mode helix is used in conjunction with a ground plane, the polarization is predominantly vertical and the radiation pattern is similar to that of a monopole. The radiation resistance of a short resonant helix above a perfect ground is approximately given⁴⁰ by $(25.3 \ h/\lambda)^2$,

approximately given by (23.3 h/λ), where h is the axial length or height above the ground plane.

Typical feeding arrangements for a helical monopole are shown in Fig. 13-28. In the series-fed arrangement, the helix is connected directly to the coaxial input, and an impedance transformer or matching network may be required. In the shunt-fed arrangement, the helix provides a self-matching network by tapping a small portion of the helix. A feed

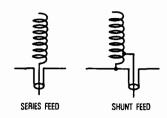


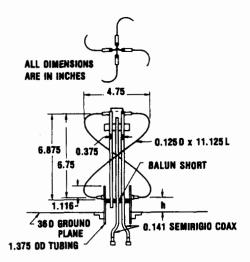
FIG. 13-28 Typical feed arrangements for a helical monopole.

arrangement which employs a bifilar helix to increase the input impedance is described in Ref. 41, and another design which utilizes a short helical monopole and top-loading wire to produce a self-resonant antenna over the 2-30-MHz frequency range without the need of a matching device is described in Ref. 43.

13-5 OTHER HELICAL ANTENNAS

Fractional-Turn Resonant Quadrifilar Helices A class of resonant quadrifilar helices, also referred to as volutes, capable of radiating circular polarization with a cardioid-shaped pattern has been described by Kilgus. $^{45-47}$ The antenna consists of two orthogonal fractional-turn (one-fourth to one turn) bifilar helices excited in phase quadrature. Each bifilar helix is balun-fed at the top, and the helical arms are wires or metallic strips of resonant length ($\ell = m\lambda/4$, m = 1, 2, 3, ...) wound on a small diameter with a large pitch angle. The ends of the helices are open-circuited at the base when m = odd and short-circuited when m = even. When properly excited, the volute produces a very broad beamwidth with relatively low backlobes and good axial-ratio characteristics over a wide angular range. Since the volute is a resonant structure, the impedance bandwidth is narrow. Typically, the VSWR is < 2:1 over a 3 to 5 percent bandwidth. Generally a wider bandwidth can be achieved with larger-diameter wires for a given helix design. This type of antenna has been designed for various applications requiring a wide beamwidth over a relatively narrow frequency range. $^{48.49}$

Because of its low-backlobe characteristics, a volute can be operated as an isolated antenna or with a ground plane. A half-turn $\lambda/2$ -volute antenna and a typical measured pattern obtained with a rotating linearly polarized source at 488 MHz are shown in Fig. 13-29. The pattern was measured with a 90° hybrid connected to the coaxial input ports of the two bifilar helices. The half-turn, half-wavelength volute is of particular interest because the input impedance of each bifilar can be matched to a 50- Ω coaxial input simply by minor adjustment of the helical-arm lengths without



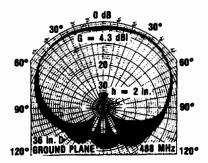


FIG. 13-29 Half-turn, half-wavelength volute antenna and measured pattern at 488 MHz.

the need of a transformer. The measured VSWR is <2:1 over ~5 percent bandwidth centered at 488 MHz.50

Short Axial-Mode Helices For certain applications requiring a wideband and broadbeam antenna with a relatively small physical size, such as reflector feeds, a short axial-mode helix (two to four turns) housed in a conical or circular cavity similar to that of Fig. 13-3 can be employed. As discussed in the subsection "Nonuniform-Diameter and Tapered Helices," the end of the helix may be slightly tapered to improve the VSWR and axial-ratio performance. A similar cavity-backed short helix designed for flush-mounting applications is described by Bystrom and Berntsen. A dual-helix feed system which utilizes two concentric helices to provide operation over two narrow-frequency bands is described by Holland.

A helical feed design for a paraboloidal reflector which utilizes a four-turn backfire bifilar helix is described in Ref. 53. This feed was designed for a spacecraft antenna

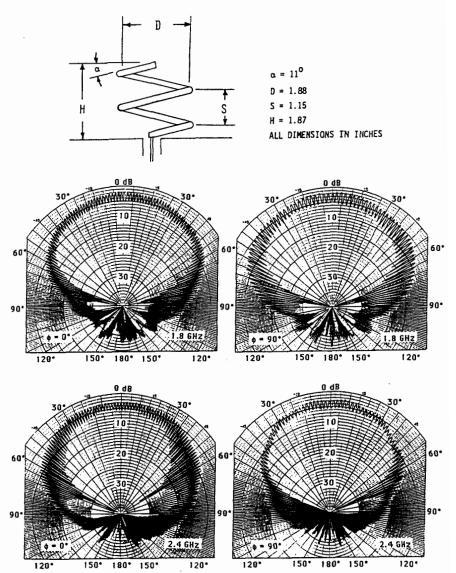


FIG. 13-30 Radiation patterns of a 1.59-turn helix on a 30- by 30-in ground plane.

operating in the 240- to 270-MHz band.* An attractive feature of the backfire bifilar-helix feed is that it does not require a cavity or ground plane, thus minimizing blockage effects and improving reflector-antenna efficiency. Based on the measured gain results reported in Ref. 53, antenna efficiency of 64 to 70 percent is achievable over a 12 percent band-

^{*}By TRW Systems Group, Redondo Beach, Calif.

width. Similar reflector feed designs employing a backfire monofilar helix have been described by Johnson and Cotton⁵⁴ and Nakano et al.⁵⁵

Short-axial-mode helices with less than three turns are useful for array applications, particularly when circular polarization is desired. Nakano et al. ⁵⁶ have demonstrated that a two-turn helix with a pitch angle as small as 4° can provide an axial ratio of less than 3 dB over a 12 percent bandwidth. A combination of low pitch and a small number of turns results in a low-profile configuration. A circular array using the two-turn helix as the radiating element is described in Ref. 57.

The performance of a short-axial-mode helix is generally limited by its axial ratio and bandwidth characteristics. The helix can be designed to operate over a larger bandwidth if a larger pitch angle is employed and with some compromise on the minimum achievable axial ratio. Figure 13-30 depicts the typical measured radiation patterns of a 1.59-turn helix with a pitch angle of 11° on a 30- by 30-in (76.2- by 76.2-cm) ground plane.† The axial ratio varies from 1 to 3 dB in the 1.8- to 2.4-GHz band, which represents a bandwidth of pearly 30 percent. The helix was constructed using 0.081-in (2.06-mm) diameter copper wire wound on a Styrofoam cylinder. Additional laboratory experiments indicated that the axial ratio characteristics of short-axial-length helices can be improved by loading the helix end with a small taper, a small loop, or a flat spiral.

As mentioned previously, when a short-axial-mode helix is used as a single widebeam element, it can be placed in a circular cavity instead of a ground plane. Limited laboratory measurements showed that there are no significant changes in axial ratio characteristics. It also should be mentioned that when a short-axial-mode helix with an imperfect axial ratio is used as the radiating element for an array, the overall axial ratio characteristics of the array can be improved by appropriately arranging the relative orientation (roll position) and adjusting the excitation phase of the individual elements within the array.⁵⁸

Helicone Antennas An axial-mode helix can be operated in conjunction with a conical horn to provide a broadband antenna with low sidelobes. 59 The axial length of the helix and the horn are approximately the same. Sidelobe levels of the order of -25 dB have been reported. Design and performance data are available in the literature. 60

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Frequency-Independent Antennas

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14-1 Basic Principles 14-2 Frequency-Independent Antennas Quasi-Frequency-Independent Antennas 14-4 14-2 Spiral Antennas 14-4 Comparison of Log-Spiral and Archimedean-Spiral Antennas 14-4 Modal Characteristics of Multiarm Spiral Antennas 14-8 Radiation Characteristics of Planar Two-Arm Strip Spiral Antennas On Reduced-Size Spiral Antennas 14-16 Planar Spiral Antennas 14-17 Conical Log-Spiral Antennas 14-29

14-3 Log-Periodic Antennas 14-32
General Characteristics 14-33
Log-Periodic Dipole Antennas 14-35
Asymmetric Log-Periodic
Structures 14-39
Symmetric Log-Periodic
Structures 14-40
Special Considerations 14-47
Arrays of Log-Periodic Elements 14-47
Dual Pologized Sinyons Antennas

Dual-Polarized Sinuous Antennas 14-53 Circularly Polarized Structures

Feeds for Reflectors and Lenses

The types of antennas described in this chapter are capable of bandwidths of operation that were believed impossible several decades ago. The frequency-independent antennas, including the log-periodic antenna, are based on rather stringent design principles. It turns out that the performance characteristics of most of these antennas are insensitive to the design ratio τ and the angles defining the antenna structure. Thus it is possible to vary these design parameters with the radius r in order to produce desired frequency-dependent performance characteristics, to satisfy physical constraints, or to simplify the design process. These latter antennas are classified as quasi-frequency-independent antennas.

Frequency-Independent Antennas

The frequency-independent antennas represent the implementation of relatively simple yet powerful ideas. The first idea¹ evolves from the observation that the impedance and pattern properties of an antenna are determined by its shape and dimensions expressed in wavelengths. If by an arbitrary scaling the antenna is transformed into a structure identical to the original one, except for a possible rotation about the vertex, its properties will be independent of frequency. The antenna then satisfies the angle condition, which means that its form can be specified entirely by angles only and not by any particular dimension. There are two classes of antennas satisfying this condition: conical antennas, made up of infinite cones of arbitrary cross section having a common vertex, and equiangular antennas, with surfaces generated by equiangular spirals having a common axis and the same defining parameter. The patterns of the spiral antennas rotate around the common axis with frequency. Since equiangular spirals are also called logarithmic spirals, the name log-spiral antenna is commonly used and will be used in the rest of this chapter.

The second idea² is that if a structure becomes equal to itself by a particular scaling $1/\tau$ of its dimensions, it will have the same properties at frequencies f and τf . The consequence is that the antenna characteristics are a periodic function, with a period of $|\log \tau|$, of the logarithm of the frequency. Antennas obtained from this principle are called log-periodic. By making τ close enough to 1, the variation of the properties over the frequency band $(f, \tau f)$, and therefore everywhere, may be small for some types of structures. In practice, even with τ not very close to 1, good frequency-independent behaviors are observed.

A third idea is that self-complementary planar conducting strip antennas have a frequency-independent input impedance. The complementary strip structure is obtained by interchanging the conducting and nonconducting planar surfaces of the specified strip antenna. The self-complementary condition requires that the complementary structure is identical to the original structure except for a rotation about a vertex point. It then follows from Babinet's principle that the product of the input impedances of the original and the complementary structures are a constant independent of frequency. Therefore, each impedance is independent of frequency, since the two impedances are identical. If for a finite structure there is little end effect (i.e., small reflections from outside the structure), then the impedances will be independent of frequency. This is a sufficient, but not necessary, condition for frequency-independent performance of log-spiral and log-periodic antennas. However, this condition was used to achieve the first successful log-periodic and sinuous antenna designs.

Log-spiral antennas have been referred to as continuously scaled structures wherein

the scaling is equivalent to a rotation of the structure and therefore a rotation of the pattern versus frequency for a fixed structure. Since the radiation patterns are rarely rotationally symmetrical for arbitrary angles of rotation, the log-spiral antennas are not frequency-independent. In fact, they are log-periodic, as shown by the following discussion. If the log-spiral curve is defined by $r = \exp(a\phi)$, then a scaling of $\tau = \exp(2\pi a)$ leaves the structure unchanged; i.e., there is no rotation of the pattern. Thus it is a log-periodic structure because the patterns are identical only for frequencies related by integral powers of τ .

To conform to the conditions stated above, equiangular as well as log-periodic structures should extend from the center of expansion O, which is also the feed point, to infinity. A practical antenna is obtained by taking a section of the ideal infinite structure contained between two spheres of center O and of radii r_1 and r_2 , respectively.

Inside the smaller sphere is the feed region, where the infinite structure, which ideally should converge to the point O, is replaced by some coupling mechanism to the feed transmission line or waveguide. The smaller sphere of radius r_1 determines the highest frequency of operation f_1 of the antenna by the condition that r_1 must be small enough, compared with the wavelength λ_1 , to make the exact shape of the coupling mechanism have little influence on the impedance or the pattern of the antenna. Ultimately, the dimension r_1 is fixed by the size of the waveguide or transmission line connected to the structure.

The outside dimension of the antenna, specified by the radius r_2 , determines the lowest frequency of operation by the following considerations. It is observed, for some structures, that the currents (or the field components near the material boundaries of the structure) decrease rapidly with distance from the center. Thus it becomes possible to cut off the structure at the distance where these currents are so small with respect to the feed-point current that they can be eliminated without changing appreciably the radiation pattern or the impedance. For a given frequency, the distance at which this happens is proportional to the corresponding wavelength. Thus the lower cutoff frequency may be decreased at will by increasing the size of the antenna.

The rapidity of decrease of the current with distance depends on the particular structure being considered. For conical antennas excited at the vertex, the field is transverse to the radial direction and decreases only as the inverse of the distance r to the center. Examples of finite sections of conical structures that have broadband properties are the discone antenna and a V dipole with conical arms. However, the conical structures are not frequency-independent because any finite portion, however large, will show end effects (reflections from the ends produce variations of the radiation patterns). The bandwidth cannot, therefore, be increased at will by increasing the size. Equiangular and some log-periodic antennas, on the other hand, exhibit a decrease of current with distance faster than 1/r. The end effect becomes negligible at a distance in wavelengths that depends on the exact shape of the structure. Thus some antennas will be more compact than others for a given lowest frequency f_2 and a given relative importance of end effect.

A property common to both types of antennas and related to the absence of end effect is that the radiation field must be substantially zero in the directions of the conductors forming the structure, as seen from the center point.

Some relations between the two types of antennas should be noted. Log-spiral antennas are special cases of log-periodic antennas with a period of log τ . This property is not destroyed if the cones on which the spirals lie are distorted or given different axes. For example, one cone may be flattened, or several equiangular spiral arms with the same vertex but different axes may form an array having the log-periodic property.

Quasi-Frequency-Independent Antennas

As mentioned earlier, the log-spiral and log-periodic design principles place stringent and unnecessary design requirements on these antennas. The most notable example is the archimedean spiral. The archimedean spiral* antenna, originated by E. M. Turner, 6 has extremely wideband characteristics which are essentially equivalent to those of the log-spiral antenna. The archimedean spiral, with constant spacing between adjacent arms, can be considered as a log-spiral for which τ varies with the radius. In many cases, the equivalent design ratio $\tau_{\rm eq}$ varies from about 0.3 to 0.9, which is an extreme range, with little change in radiation characteristics over a 10:1 frequency range.

Variations of τ and the angular design parameters with radius for log-spiral and log-periodic antennas may be incorporated with little and/or desired changes in performance characteristics. Rather abrupt changes of the design parameters with radius often may be tolerated. Unfortunately, there is little reference to this very important property of frequency-independent antennas.

Although none of the finite-size antennas considered is truly frequency-independent over the range zero to infinity, the name is justified because possibilities for increasing the bandwidth are almost unlimited. Without changing the design, but simply by adding some turns to the spirals or some sections to the log-periodic antenna, any desired bandwidth can be achieved.

Strictly speaking, none of these antennas is frequency-independent because of the dispersive characteristics of the radiated fields. The phase of the radiated field of the circularly polarized spiral antennas is delayed an extra 360° per period of frequency because of the pattern rotation. The same phenomenon is observed for linearly and circularly polarized log-periodic antennas. The early history of the development of frequency-independent antennas is given by Jordan et al.³

14-2 SPIRAL ANTENNAS

Planar and conical multiarm log-spiral and archimedean spiral antennas are discussed in the following sections. Two-arm cavity-backed planar and conical spirals are used to produce a unidirectional single-lobe pattern. Three or more arms may be used for direction-finding and homing applications^{4,5} or to obtain larger bandwidths for dual-polarization spirals or high-mode-purity (rotationally symmetric) patterns.

Comparison of Log-Spiral and Archimedean-Spiral Antennas

Figures 14-1 and 14-2 illustrate the planar log-spiral and archimedean-spiral structures. Strictly speaking, the archimedean spiral is not a frequency-independent antenna structure because the spacing between arms is specified by a constant, not an angle. However, this is a moot point because essentially frequency-independent performance is commonly achieved over 10:1 bandwidths.

The two-arm planar log-spiral strip antenna of Fig. 14-1 is defined by the angles ψ and δ . The equation for a log-spiral curve is

$$r = r_0 e^{a\phi} \tag{14-1}$$

[•]This is based on the spiral of Archimedes, which was defined in the third century B.C.

$$\psi = \tan^{-1} (1/|a|)$$

$$\tau = e^{-2\pi|a|} = OA/OB$$

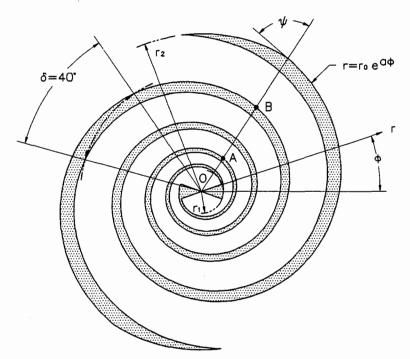


FIG. 14-1 Two-arm log-spiral antenna: outline and parameters.

The pitch angle ψ is related to the expansion coefficient a by

$$\tan \psi = \frac{r}{da/d\phi} = \frac{1}{a} \tag{14-2}$$

This angle is the complement of the angle commonly defined as the pitch angle for helical antennas. The arc length l from the origin O is finite and proportional to the radius r:

$$l = \frac{r}{\cos \psi} \tag{14-3}$$

The design ratio τ is defined to be less than 1 and is given by

$$\tau = e^{-2\pi|a|} = e^{-(2\pi/|\tan\psi|)} \tag{14-4}$$

This is the ratio OA/OB of the figure and is the ratio of the radii for one turn of the log-spiral curve. It is apparent that a scaling of the infinite structure by τ leaves it unchanged.

$$\psi(r) = \tan^{-1} (r/a)$$
$$\tau(r) = e^{-2\pi(|a/r|)}$$

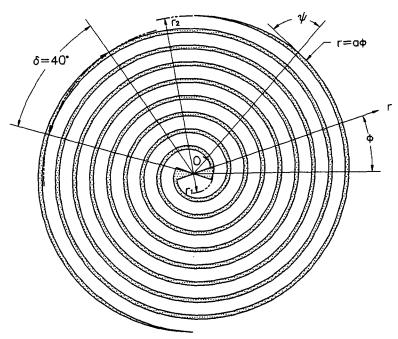


FIG. 14-2 Two-arm archimedean-spiral antenna: outline and parameters.

The relations

$$a = -\frac{\ln \tau}{2\pi} \tag{14-5}$$

and

$$\psi = \tan^{-1} \left(\frac{2\pi}{|\ln \tau|} \right) \tag{14-6}$$

follow from the preceding equations.

The other side of the strip may be defined by rotating the curve (14-1) by the angle δ to give

$$r = r_0 e^{a(y+\delta)} \tag{14-7}$$

This is equivalent to a scaling K of the spiral curve equal to

$$K = e^{a\delta} ag{14-8}$$

The width W of the spiral arm at radius r is therefore

$$W = r(1 - K)\sin\psi \tag{14-9}$$

The second arm of the log-spiral structure is obtained by rotating the first arm by 180° around the origin O. The inner and outer radii of the finite log-spiral structures are given by r_1 and r_2 , respectively. The constant r_0 in Eq. (14-1) may be determined from the initial value of ϕ , which is arbitrary, and r_1 or r_2 . The range of ϕ depends only on the ratio r_2/r_1 .

The planar log-spiral antenna may be viewed and analyzed as a strip radiator with currents flowing along the arms or as a slot radiator with electric fields between the strips flowing along the slots. The results should be the same. For $\delta = 90^{\circ}$, the planar structure is self-complementary, and Babinet's principle leads to the conclusion that the input impedance is $60\pi \Omega$ for free space (no dielectric loading) and independent of frequency.

The centerline of the archimedean-spiral strip of Fig. 14-2 may be defined by

$$r = a\phi \tag{14-10}$$

The pitch angle ψ varies with radius as

$$\tan \psi = \frac{r}{a} \tag{14-11}$$

The pitch angle approaches 90° for large r. An equivalent design ratio τ_{eq} , which varies with radius, may be defined for the archimedean spiral that has the same pitch angle ψ at radius r. Using Eq. (14-4), we have

$$\tau_{\rm eq}(r) = e^{-2\pi/|\tan w|} = e^{-2\pi|a/r|}$$
 (14-12)

Note that τ_{eq} approaches 1 for large r. The sides of a strip may be defined in terms of the rotation angle ϕ of Fig. 14-2 and the angle δ to obtain

$$r = a\left(\phi \pm \frac{\delta}{2}\right) \tag{14-13}$$

The radial width of the strip W, is a constant independent of radius and is given by

$$W_r = a\delta \tag{14-14}$$

The actual width of the strip varies slightly with radius and is given by

$$W = a\delta \sin \psi \tag{14-15}$$

The spacing S, between the centerlines of adjacent turns for one arm is given by

$$S_r = 2\pi a$$
 (14-16)

and the actual spacing is given by

$$S = S, \sin \psi = 2\pi a \sin \psi \tag{14-17}$$

The two-arm spiral is self-complementary when W/S = 1/4 or $\delta = \pi/2$. Since the strip widths and spacings are defined by constants rather than by angles, the archimedean spiral does not conform to either the frequency-independent or log-periodic principles

described in Sec. 14-1. Practically speaking, frequency-independent performance is obtained if τ is large enough in the active region (radiation region), wherein the circumference of the radiation ring is about one wavelength. Unfortunately, little information has been published on the degradation of gain and patterns versus τ .

The archimedean spirals is by far the most popular of the two types of spirals mostly because government funding of R&D programs was concentrated on the archimedean spiral. Some results indicate that loosely wound log-spirals perform as well as the tightly wound archimedean spirals. It seems that both types of spirals are insensitive to variations of their design parameters. Variations of τ and δ with radius for the log-spiral antennas may be used to satisfy input impedance or fabrication requirements.

The sense of circular polarization for spiral antennas may be determined as follows. Wrap the fingers of the right hand around the axis of the spiral with the fingers pointing in the direction in which the circumferential currents are flowing. The spiral radiates right-hand circular polarization (RHCP) in the direction to which the thumb points and left-hand circular polarization (LHCP) in the opposite direction.

Modal Characteristics of Multiarm Spiral Antennas

An approximate analysis of spiral antennas assumes that the radiation pattern is the superposition of radiation from annular rings of traveling-wave currents wherein the circumference of a ring is L wavelengths, where L is an integer greater than zero. This holds for tightly wound spirals for which $\tau > 0.25$. The free-space circumference of the rings will be less than L wavelengths according to the velocity of propagation of the currents on the spiral arms. If the ends of the spiral arms are terminated so that the reflected waves are negligible, then there are only outward-traveling waves for center-fed spirals. The particular radiation rings that influence the patterns may be inferred from a normal mode analysis of the excitation of the spiral arms and the estimated attenuation through the first active region. This qualitative analysis provides great insight into the performance of the spiral antennas and is a great aid in explaining the strange patterns that often occur.

In general, consider an N-arm conical spiral with rotational symmetry such that a rotation of $2\pi/N$ radians about the axis of the conical spiral leaves the structure unchanged. Figure 14-3 shows the coordinate system for a conical four-arm spiral. Because of the rotational symmetry, it is convenient and very useful to decompose an arbitrary excitation into the normal modes.* There are N normal modes for an N-arm structure. For any mode M, the arms are excited with equal magnitudes and with progressive phases as given by $\exp[-2\pi M/N]$, where N is the number of the arm. For perfect excitation of a single mode M, the azimuth pattern is the summation in p of terms of the form $\exp[-j(M+pN)\phi]$, where p is a nonnegative integer.

The terms correspond to radiation from rings in the spiral, where the circumference of the ring is approximately M + pN wavelengths. These rings are determined from the condition that currents in adjacent arms of the spiral are approximately in phase, taking into account the differences in path lengths to the origin and the phase of the excitation of the arms. The term p = 0 represents the desired first active region. For p > 0, the terms represent higher-order radiation rings which only distort the desired pattern and reduce

^{*}The normal modes are also called *eigenvectors*. The eigenvalues for the impedance matrix are the characteristic impedances for each arm. Cosine and sine functions also may be used to define the normal modes. However, the exponential functions are preferred for circularly polarized antennas.

the gain of the antenna. For a good spiral design, the term p=0 dominates so that the azimuth pattern varies essentially as $\exp(-jM\phi)$. This occurs when there are only outward-traveling waves on the arms and there is large attenuation through the first active region.

A general excitation of an N-arm spiral may be expressed as a summation of the N normal modes with complex amplitudes, which may be determined by a finite Fourier analysis of the excitation coefficients. Usually, only one normal mode (mode 1 or 2 for sum or difference patterns) is desired, but errors in the feed network cause the excitation of undesired modes. Thus the total azimuth pattern for a desired mode M_d is the summation of the pattern of the M_d ring plus the patterns of $M_d + pN$ rings plus the patterns of the M_e rings (the error modes) plus the patterns of the $M_e + pN$ rings for each of the error modes M_e . This seems quite complicated, but it becomes rather simple for most applications.

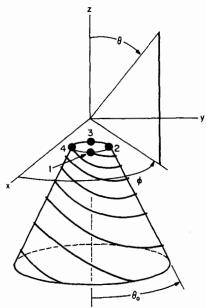


FIG. 14-3 A four-arm conical spiral and its associated coordinates.

First, we need to know the pattern characteristics of the $Q\lambda$ rings (Q an integer). For planar spirals, they may be obtained from an analysis of a planar-sheath spiral antenna with an infinite number of arms. Figure 14-4 shows the computed elevation patterns⁷ for the fundamental mode excitations of a free-space planar-sheath spiral antenna. All modal patterns except M=1 have nulls on the axis. The patterns are normalized with respect to the M=1 pattern; thus the radiation values of any two modes may be determined for any elevation angle assuming equal power inputs. The minimum beamwidth that can be achieved by varying τ and δ for mode 1 is about 70°.

For each mode, the pattern has rotational symmetry about the z axis and the field is pure circular polarization, with the sense of the circular polarization depending on how the spiral is wound about the axis. The patterns are shown only for the half space above the xy plane. The patterns for the lower half space are the mirror images of those shown, but the sense of circular polarization is opposite to that above the xy plane. For each modal pattern, the magnitude is independent of ϕ , and the phase varies as exp $(-jM\phi)$. There are an infinite number of wires in this hypothetical sheath structure and, therefore, an infinite number of normal modes. Radiation for mode M occurs in a "radiation ring" where the circumference is approximately $M\lambda$. There is radiation only from the $M\lambda$ ring for this sheath model.

These patterns are quite useful in the sense that they represent (approximately) radiation from the $M\lambda$ ring of spirals with a finite number of arms N. For example, for a two-arm planar spiral, it is desired that all the radiation occurs in the λ ring. However, because of finite attenuation through the active region (λ ring), there will be radiation from the 3λ , 5λ , . . . rings if the frequency is such that they exist on the structure. The total pattern is then the sum of the mode 1, 3, 5, . . . patterns weighted according to the

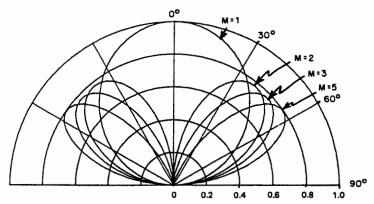


FIG. 14-4 Mode patterns for a planar-sheath log-spiral antenna.

attenuation through the rings. Frequency independence is then lost because the total pattern is not rotationally symmetric and rotates with frequency.

If the attenuation through the first active region is not large, as in the case of thin-wire or slow-wave spirals, then the waves will travel with little attenuation to the second radiation ring, which is the $(M + N)\lambda$ ring (provided the spiral is large enough), where an azimuth pattern of the type $\exp[-j(M+N)\phi]$ is radiated. The total pattern is the superposition of the $M\lambda$ and $(M+N)\lambda$ ring patterns and may be expressed as

$$E(\phi) \approx e^{-jM\phi} (1 + a_1 e^{-jN\phi})$$
 (14-18)

where a_1 is the relative complex amplitude of the p=1 radiation ring. For a two-arm spiral, N=2 and the conical-cut pattern has two maxima and two minima. For a four-arm spiral, the conical-cut pattern has four of each. The presence of a higher-order mode therefore may be easily detected by measuring "conical-cut" patterns about the boresight axis. In general, we have

$$E(\phi) = e^{-jM\phi} \left(1 + \sum_{p=1}^{\infty} a_p e^{-jpN\phi} \right)$$
 (14-19)

and the pattern is a more complex function of ϕ . However, the term p=1 usually dominates. The bandwidth over which the $(M+N)\lambda$ ring does not exist increases with N, but this requires a more complicated feed network. If the spiral is too small to have an $(M+N)\lambda$ ring and there are no resistive terminations on the arms, then the waves are reflected and will radiate in the $(N-M)\lambda$ ring (if it exists). The azimuth variation will be $\exp[j(N-M)\phi]$, and the sense of circular polarization will be reversed because the waves are traveling in the opposite direction in the ring. If the $(N-M)\lambda$ ring does not exist, the waves will flow back into the feed circuit. If the excitation of the desired mode is not perfect, then error modes will be excited, each with its higher-order radiation rings. For a two-arm spiral, the only error mode is the M=2 mode (also referred to as the M=0 mode), which is produced by unbalanced balun circuits. This results in a tilted beam and a conical-cut pattern with one maximum and one minimum. An excellent treatment of all of these modes is given by Corzine and Mosko.

Radiation Characteristics of Planar Two-Arm Strip Spiral Antennas

As inferred in the preceding subsection, it is quite important to achieve large attenuation through the first active region. For example, for a two-arm planar spiral that may radiate from the λ and 3λ rings, the ratio of the M=3 pattern to the M=1 pattern at $\theta=60^{\circ}$ for equal powers radiated is 0.68/0.44, which is 3.8 dB. If it is desired that the WOW (ratio of maximum to minimum field) of the conical pattern cut at $\theta=60^{\circ}$ is less than 3 dB, then the attenuation through the λ ring should be greater than 19.1 dB. (WOW and the ratio of radiated fields $E_{3\lambda}/E_{\lambda}$ correspond to VSWR and reflection coefficient on a transmission line.) This is not an unusual requirement, but it is difficult to achieve, as will be shown. For WOW = 6 dB, the required attenuation is 13.4 dB. This is often achieved in practice.

Approximate calculations were performed for a planar log-spiral antenna in free space. This simulates a perfectly absorbing cavity placed underneath the spiral and neglects losses due to the presence of absorbing materials in the near fields of the spiral structure. The strips are replaced by cylindrical rods with the diameters equal to one-half the strip width. This allows the use of thin-wire antenna computer programs. A method-of-moments (MOM) program with pulses for testing functions was used (an expanded version of MININEC38). This program (and others) does not give accurate results for closely spaced wires where the diameter of the wires is not much less than the spacing between wires, which is the case for self-complementary spirals. Thus it was necessary to restrict δ to less than about 70°.

The objective was to determine the attenuation through the active region (λ ring) of a two-arm planar log-spiral antenna as a function of τ , δ , and ν/c , the relative velocity (compared with free space) of propagation of currents on the spiral arms. The results may be applied to archimedean spirals that have similar values of τ and δ in the active region.* Distributed resistive loading was placed in the outer quarter turn of the spiral arms to obtain a matched termination. For a given velocity of propagation, the frequency was chosen so that the outer circumference of the spiral structure was 2.5 λ . This reduced radiation from the 3 λ ring to a negligible value, as evidenced by the computed conical pattern cuts at $\theta = 70^{\circ}$ with the WOW < 3 dB. The attenuation through the active region and loss in antenna gain were determined from the computed antenna input power and the power absorbed in the matched terminations. The current distribution was checked to make sure that reflections from the matched terminations were small.

The velocity of propagation was controlled by adding distributed-series inductance to the wire segments of the spiral arms. This slows the waves on the arms and increases the characteristic impedance of the arms. The computed value of v/c for an assumed value of inductive loading neglected the mutual coupling between spiral turns.

Babinet's principle may be used to extend the results of this study. The width of the strips to be analyzed is limited by the computer program. The complementary structure to the thin spiral strip structure is an infinite thin-slot spiral structure, which is also a thick-strip spiral structure. The complement of the finite-diameter spiral strip is an infinite ground plane with a finite-diameter spiral slot structure cut out of it. The solutions for the electromagnetic fields are identical except for an interchange of E and E. Thus the attenuation through the active region and the radiation patterns are identical for the two

^{*}The log-spiral was chosen for the study because the arm length was much smaller than that for the archimedean spiral and requires much less computer time. For example, for a 10:1 bandwidth, a log-spiral with $\tau=0.4$ has about 4 turns, whereas an archimedean spiral with τ varying from 0.92 to about 0.4 in the active region at the highest frequency has about 11 turns.

cases. The input impedances for the two cases are related by

$$Z_{\text{strip}}Z_{\text{slot}} = (60\pi)^2$$
 (14-20)

Series inductive loading of the strips is equivalent to shunt capacitive loading of the complementary slots.

Microwave spiral strips are usually etched from a thin metal sheet placed on a dielectric substrate. The presence of the substrate slows down the waves propagating along the spiral arms. The amount of slowing increases with the thickness and dielectric constant of the substrate in a complex manner. Cohn's analysis's of slot transmission lines may be used to estimate the propagation constant. In some cases, it may be desirable to slow the waves down in order to reduce the circumference (and diameter) of the first active region. This reduces the diameter of the spiral antenna for a given low-frequency cutoff. This can be accomplished by using thick and large-dielectric-constant substrates on one or both sides of the spiral strips. Alternatively, the spiral arms may be printed with zigzag, sinuous, or meander-line modulations of the spiral arms in order to increase the turn length and therefore obtain a slow wave structure. The severe penalties paid by using these techniques will become evident from the results of this study.

Figure 14-5 shows the variations of the computed minimum and maximum loss in gain and the attenuation through the λ ring (active region) versus v/c for planar two-arm log-spirals with $\tau=0.4$ and four values of δ . It is apparent that the attenuation increases rapidly as δ is increased from 5 to 65° for v/c close to 1. It might be expected that the attenuation would increase for wider strips up to the point where δ is slightly less than 180° (thin slots), since radiation from wires increases with the thickness of the wires. The invocation of Babinet's principle requires that the attenuation and gain loss are identical for δ and (180° $-\delta$). These results imply that the attenuation is maximum and the gain loss is minimum for the self-complementary condition of $\delta=90^\circ$.

As v/c is decreased from 1, the attenuation decreases and the gain loss increases

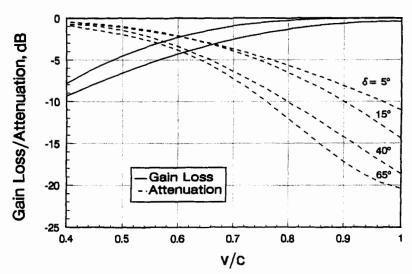


FIG. 14-5 1 λ -ring gain loss and attenuation versus v/c for $\tau = 0.4$.

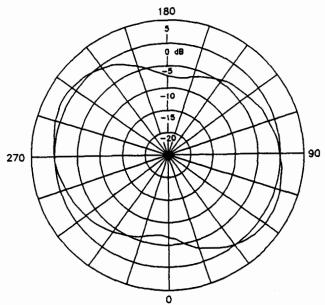


FIG. 14-6 Calculated log-spiral pattern—conical cut at $\phi=60^\circ$.

rapidly. It is seen that in order to achieve a WOW of 6 dB at a conical cut with $\theta = 60^{\circ}$, the approximate restrictions should be v/c > 0.9 and $40^{\circ} < \delta < 140^{\circ}$.

Figure 14-6 shows a computed conical cut for $\tau = 0.4$, $\delta = 65^{\circ}$, v/c = 0.65, and f = 7.2 GHz with $\theta = 60^{\circ}$ for a 2-in-diameter log-spiral. The outside circumference is 3.8 λ . The pattern has two peaks and two minima with a WOW of 8.2 dB. Figures 14-7 and 14-8 show the elevation patterns for two azimuth directions where the beamwidths are maximum and minimum, respectively. It can be seen from these patterns that the WOW at $\theta = 75^{\circ}$ is 10 dB. Use of this spiral for broadband direction-finding applications presents difficulties because the patterns rotate with frequency, and therefore, the amplitude comparisons used for direction determinations are frequency-dependent as well. The measured conical-cut and principal-plane patterns of Figs. 14-9 and 14-10 (taken with a rotating linearly polarized source) of a 2-in-diameter archimedean spiral with an absorbing cavity confirm these calculations and indicate the presence of the 3λ radiation ring with a WOW of approximately 8 dB in the 60° conical cut. The modulation of the pattern represents the axial ratio in that direction. The two principal-plane patterns in Fig. 14-10

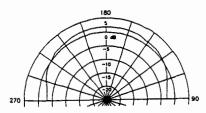


FIG. 14-7 Calculated principal-plane pattern at maximum beamwidth for a log-spiral antenna.

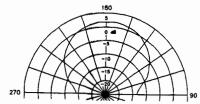


FIG. 14-8 Calculated principal-plane pattern at minimum beamwidth for a log-spiral antenna.

confirm the difference in beamwidths due to the WOW and are different from the calculated results most likely because the calculations were for a free-space spiral and did not include cavity effects. The WOW may be reduced to 3.8 dB by increasing v/c to 0.9. For frequencies less than 4 GHz where the 3λ ring does not exist on the 2-in-diameter spiral, the WOW is 2 dB or less for v/c = 0.65 and 0.9.

Figure 14-11 shows the maximum and minimum extremes of gain loss and attenuation through the λ ring versus ν/c for $\delta = 40^{\circ}$ and $\tau = 0.31, 0.4$, and 0.55. The gain loss and attenuation are relatively insensitive to τ for this range of τ . This was a surprising result because it was expected that the attenuation through the active region would increase as τ increases, since there would be a larger length of the spiral radiator in the radiation region (λ ring band). This suggests that it is not necessary to use tightly wound archimedean spirals where τ values of 0.9 to 0.95 are commonly used in the outer portion of the spiral structure. It would be expected that the resistive loss in the spiral arms could be reduced by using log-spiral structures with τ values of 0.4 to 0.5, which would greatly reduce the spiral path length to the outer portion. No published data were found to support this expectation.

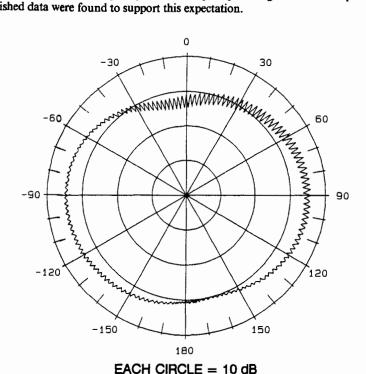


FIG. 14-9 Measured conical-cut pattern of a 2-in-diameter cavity-backed archimedean spiral.

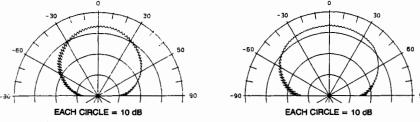


FIG. 14-10 Measured principal-plane patterns of a 2-in-diameter cavity-backed archimedean spiral.

The maximum directivity with respect to a circularly polarized isotropic source decreases from 4.5 to about 2 dB as v/c is decreased from 1 to 0.5. The beamwidth of the pattern increases as v/c is decreased because the diameter of the λ ring measured in wavelengths decreases. It is insensitive to τ and δ for the ranges studied. The maximum gain is simply the maximum directivity minus the gain loss in decibels.

Figure 14-12 shows the computed characteristic impedance Z_0 of the two-arm planar log-spiral strip antenna versus the angular arm width δ for three values of v/c. Equation (14-20) was used to calculate Z_0 for $\delta > 90^\circ$. For v/c = 1, it appears that extrapolated curves for $\delta < 90^\circ$ and $\delta > 90^\circ$ come close to the theoretical value of 60π Ω for a self-complementary ($\delta = 90^\circ$) structure. This adds credence to the accuracy of the approximations used in the computations. For v/c < 1 and $\delta < 90^\circ$, the characteristic impedance increases because of the added series inductance to the strip lines. For $\delta > 90^\circ$, the added shunt capacitance reduced the Z_0 . Thus the curves do not extrapolate to a common point at $\delta = 90^\circ$. The parameter δ allows a large range of Z_0 , but large deviations from 90° are undesirable because this reduces the attenuation through the active region, as evidenced in Figs. 14-5 and 14-11.

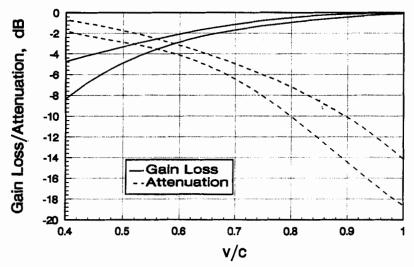


FIG. 14-11 1 λ -ring gain loss and attenuation (maximum and minimum) versus v/c for $\tau=0.31,\,0.4,\,$ and 0.55 and $\delta=0.40^{\circ}.$

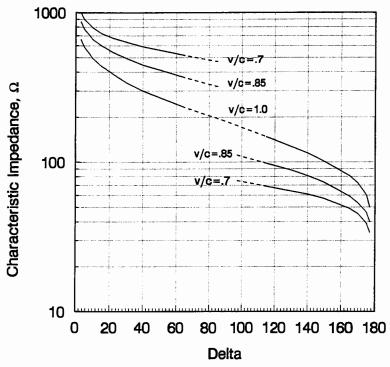


FIG. 14-12 Log-spiral input impedance versus δ for v/c= 0.7, 0.85, and 1.0 and $\tau=$ 0.4.

Figure 14-13 shows the computed current attenuation through the active region for a planar four-arm log-spiral strip antenna with $\tau=0.43$ versus v/c for two values of δ . A self-complementary structure is obtained when $\delta=45^\circ$ rather than 90° for the two-arm structure. These results were obtained using the NEC-81¹⁰ method-of-moments program, which is a PC version of the widely used NEC-2 program. These are smoothed curves and represent the average attenuation for three modes, M=1, 2, and 3, i.e., the attenuation through the λ , 2λ , and 3λ rings. The maximum deviation from the smoothed curve is about 2.0 dB for the three modes, which is surprising since the curves are drawn as straight lines. Comparing these results with those for the two-arm spiral (Fig. 14-5), it is seen that they are quite similar except for v/c < 0.8. The discrepancy may be due to the fact that the two-arm results are for power attenuations rather than current attenuation and that the characteristic impedance of the arms varies with radius.

On Reduced-Size Spiral Antennas

Systems and structural engineers are notorious for specifying difficult requirements in performance for reduced-size antennas. Over the last four decades, exceedingly large R&D efforts have been expended on reducing the size of broadband spiral antennas by factors of 2 or more. The results presented in the preceding subsection offer insight into this problem.

In order to obtain circularly polarized, rotationally symmetric patterns from spirals,

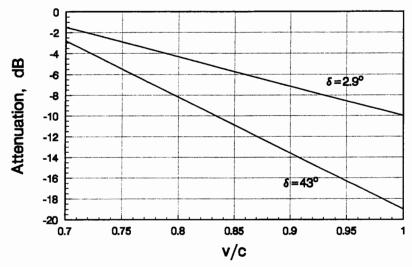


FIG. 14-13 Calculated attenuation through the active region for a four-arm log-spiral for $\tau = 0.43$. (Courtesy R. W. O'Connor, Loral Randtron Systems.)

it is necessary to establish traveling-wave currents in the active region (λ ring) and no radiation from the higher-order radiation rings. For bandwidths less than 3:1 for a twoarm spiral, the 3λ ring does not exist, so an outward traveling wave in the λ ring is achieved with matched terminations on the spiral arms. The size reduction is proportional to v/c. It is seen from Figs. 14-5 and 14-11 that the gain loss becomes excessive for small v/c. For bandwidths greater than 2.5:1 and small v/c, it is necessary to introduce attenuation after the λ ring in order to prevent radiation from the higher-order radiation rings that destroys the rotational symmetry of the patterns. The introduction of this attenuation will result in a reduction in gain for large bandwidths for the antenna. This strongly infers that significant size reductions are always accompanied by significant losses in gain.

It is also significant that after four decades of effort, no significant breakthroughs have been reported.

Planar Spiral Antennas

The spirals shown in Figs. 14-1 and 14-2 have bidirectional patterns with rotationally symmetric beams pointing normal to the plane of the structures. For most applications which require a unidirectional pattern, a cavity is placed on one side of the spiral. The frequency-independent-pattern bandwidth in this case is limited to the order of an octave for lossless cavities. Decade bandwidths may be achieved by placing absorbing materials in the cavities.

Although the geometries of the archimedean-spiral and log-spiral designs are quite different, the radiation patterns should be similar if τ , δ , and v/c are commensurate in the active region. The fact that the archimedean spiral, wherein τ_{eo} varies from about 0.9 to 0.3, is essentially frequency-independent over 10:1 bandwidths (except for radiation from higher-order rings) infers that the radiation patterns are rather insensitive to τ . In addition, the design of the cavity, absorbing materials, spiral-arm terminations, and feed techniques, including baluns, is practically the same for the two types of spirals.

Cavity-Backed Archimedean-Spiral Antennas

General characteristics The cavity-backed archimedean spiral can properly contend as one of the most proliferate radiators since its conception in early 1950.6 Its unidirectional, broad-bandwidth characteristics are attractive features, particularly when combined with its mechanical simplicity and compact size. The general features of this radiator are shown in Fig. 14-14. The cavity may be a hollow metal-based cylinder for near-octave bandwidths or absorber-loaded (at the expense of gain) for a greater-thandecade bandwidth. The balun may be infinite, printed-circuit, lumped-constant, waveguide-fed, or matrix-excited.

The archimedean-spiral trace is defined by

$$r = a\left(\phi \pm \frac{\delta}{2}\right) \tag{14-21}$$

where the coordinates are identified in Fig. 14-2. The spiral pitch angle ψ and τ_{eq} are both functions of radius and are given by Eqs. (14-11) and (14-12). The spiral arm width and the spacing between arms is defined by Eqs. (14-14) through (14-17). For an N-arm spiral, the N conductors are identical except that their starting points in ϕ are displaced by $2\pi/N$.

Archimedean-spiral design The radiation characteristics of the archimedean spiral depend on a and δ , which were defined in the subsection "Comparison of Log-Spiral and Archimedean-Spiral Antennas," and v/c. The equivalent design ratio τ_{eq} varies from a

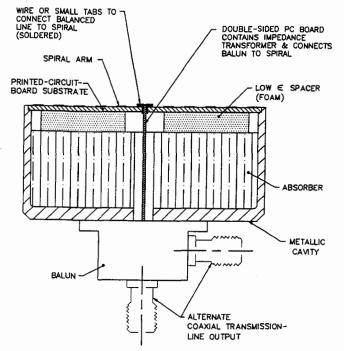


FIG. 14-14 Absorber-loaded cavity-backed two-arm archimedeanspiral antenna.

small value at the input region to a large value at the outside of the spiral, i.e., from a loosely wound to a tightly wound spiral. The question is, How loosely wound may the spiral be at the input region without deteriorating the performance at the high end of the frequency range? This involves the determination of the maximum value of a. As a increases, the number of turns decreases and tolerances on fabrication are relaxed. Computations were performed for a two-arm free-space archimedean-spiral antenna for a range of τ_{eq} at the λ ring ($r_H = \lambda/2\pi$) for the largest frequency of the desired band. See Eq. (14-12) for a definition of τ_{eq} . The expansion coefficient a may be calculated from the assumed τ_{eq} from this equation. The spiral was truncated at the 2.5 λ ring so that radiation from the 3λ ring region was small. The radius of the feed terminals was defined as $r_H/3$. The angle δ was set equal to 70° for reasons similar to those described in reference to Fig. 14-5 for the two-arm log-spiral (see the subsection "Radiation Characteristics of Planar Two-Arm Strip Spiral Antennas").

Figure 14-15 shows the computed attenuation through the λ ring and WOW for τ_{eq} varying from 0.07 to 0.4 for v/c = 1 and 0.9. The WOW shown is mostly due to the rapid expansion of the spiral. The WOW of the complete spiral will be increased by radiation from the 3λ ring which is inversely proportional to the attenuation through the active region. Using the criteria that the attenuation through the active region should be greater than 16 dB, it appears that τ_{eq} can be about 0.15 for v/c = 1 but should be about 0.4 for v/c = 0.9. This is a strange result. There has been no experimental verification of these

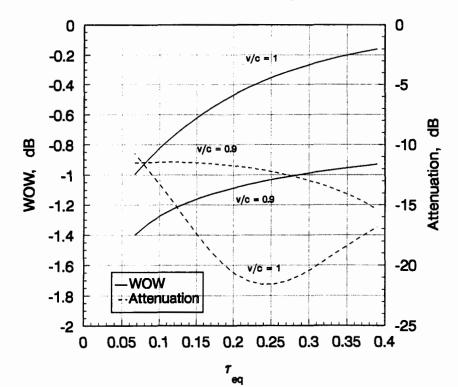


FIG. 14-15 1 λ -ring attenuation and WOW for a two-arm archimedean-spiral antenna versus τ_{eq} .

results. Thus, to be safe, we should use $\tau_{eq} = 0.4$ as a minimum. Additional computations should be made for particular designs.

As with the log-spiral, δ should be in the range of 40 to 140° to ensure adequate attenuation through the active region. The curves of Fig. 14-12 for Z_0 versus δ also hold approximately for the archimedean spiral. Z_0 is quite insensitive to $\tau_{\rm eq}$ in the feed region. If the infinite-balun feed were used, it would be desirable to choose δ so that $Z_0 = 50~\Omega$. However, this requires that δ is about 170 to 175°, which provides insufficient attenuation through the active region. For conventional balanced axial feed lines, δ should be in the range of 90 to 130°, which provides a Z_0 range of 130 to 90 Ω for v/c = 0.9. Unfortunately, it is difficult to determine v/c accurately theoretically or experimentally for given values of design parameters.

Given the frequency band of f_{low} to f_{high} , the inside and outside radii r_1 and r_2 are determined as follows. The high-frequency cutoff f_{high} being given, the radius r_1 of the feed region must be small compared with the wavelength at f_{high} ; that is, $r_1 \approx \lambda_{high}/6\pi$, for example. Larger values of r_1 will degrade the rotational symmetry of the patterns and the axial ratio. The radius r_2 for the low cutoff frequency depends on how much degradation of pattern rotational symmetry and gain is tolerable. The pattern symmetry depends mostly on τ_{eq} at the outside of the spiral. For the archimedean spiral, τ_{eq} at the outside of the spiral is usually 0.8 to 0.9, which is easily large enough to ensure excellent rotational symmetry of the patterns. The radiation region for the λ ring of a spiral extends over a radial region where the circumference varies from about 0.7λ to 1.4λ . The attenuation through the active region is essentially independent of τ_{eq} if $\tau_{eq} > 0.4$ and depends mostly on δ and v/c. The gain at the low-frequency limit depends mostly on how much power is lost in the matched termination of the spiral arms. For $r_2 = \lambda_{low}/2\pi$ at f_{low} , the loss in gain is typically about 5 dB compared with higher frequencies. The beamwidth increases to about 95°, compared with about 70° for higher frequencies. The loss in gain and increase in beamwidth are small for $r_2 = 1.5 \lambda_{low}/2\pi$, but this is a 50 percent increase in diameter. A compromise between minimum gain and spiral diameter is usually made. Alternatively, v/c could be reduced in the outer region of the spiral (by dielectric loading, for example) to increase the gain by reducing the power lost in the termination, at the expense of a hopefully smaller loss in gain due to the reduced attenuation through the active region (see Fig. 14-5).

Two-arm archimedean-spiral characteristics Cavity-backed spirals radiate a unidirectional sum mode when the adjacent-arm phase progression is $2\pi/N(\pi)$ rad in the case of a two-arm spiral). The sum mode will radiate most efficiently at a diameter of λ/π independent of the number of arms. This condition occurs as a result of the in-phase condition of currents on adjacent arms that occurs at this circumference.

Unfortunately, the cavity walls, mounting flange, and balun assembly all influence the pattern. It is also true for unloaded cavities that a portion of the image radiation from the cavity base will couple into the spiral aperture and reradiate from a higher-order radiation ring (if supported). The rest of the reflected energy will leak through the spiral structure. Both contributions from the image further modify the primary pattern. The image effects are discussed in more detail in the subsection "Absorber-Loaded-Cavity Characteristics."

Unloaded-cavity characteristics For applications where maximum gain or high average power is a primary consideration, an unloaded cavity is often used. An empirical estimation of the two-arm archimedean spiral backed by an unloaded cavity is provided by Bawer and Wolfe. 11 Figure 14-16 illustrates the impact of cavity diameter on gain and

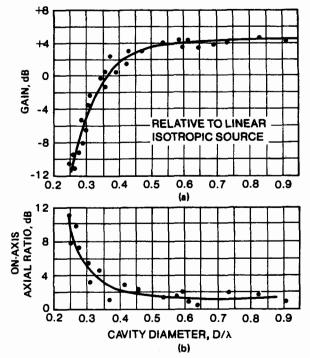


FIG. 14-16 Effect of cavity diameter on gain and axial ratio.

axial ratio. The gain curve has a knee slightly above λ/π but does not approach the asymptote of 4 dB until a cavity diameter of 0.5λ is reached. The gain is for the desired sense of circular polarization and is relative to that of a linearly polarized isotropic source. These data represent a compilation from a large number of spirals operating in the 0.2- to 18-GHz region. Figure 14-16b illustrates the cavity diameter's effect on axial ratio for the case in which the spiral outer terminals are either open or short-circuited. Deterioration of the axial ratio with diminishing diameter is not surprising, since the reflected wave from the outer terminals radiates the opposite sense of circular polarization to that radiated from the incident wave. When the spiral outer terminals are terminated with matched loads, the axial ratio for small diameters $(0.25\lambda$ to 0.4λ) can be reduced to values below 4 dB. The effect of cavity depth on directivity can be approximated by image theory to the extent that maximum directivity occurs at a depth of approximately 0.25λ . The effects of the cavity sidewalls, the balun structure, and mounting flanges can alter this approximation. The loss in gain due to power lost in the loads increases as the cavity depth decreases because the attenuation through the active region decreases.

Wang and Tripp¹² have reported the results of suspending a two-arm archimedeanspiral antenna close to a ground plane at a spacing as low as 0.05λ . Their configuration did not include metallic sidewalls (as in a cavity), and absorbers were not used, except for a narrow ring of absorber placed between the spiral and ground plane at the spiral outer radius. The absorber ring formed a termination for the spiral arms. This configuration had

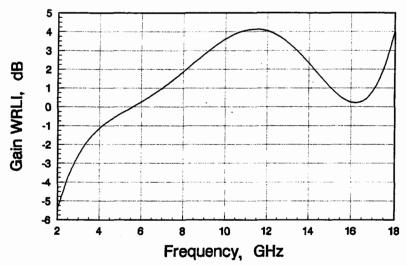
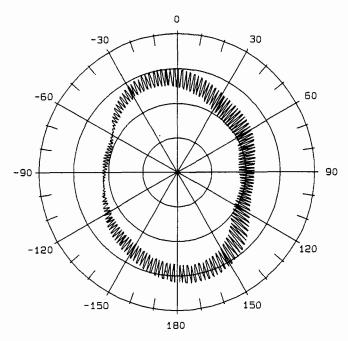


FIG. 14-17 Gain of an archimedean spiral spaced 0.15 in above a ground plane.

measured gain approaching 4 dB WRLI (with respect to linear isotropic) over bandwidths greater than an octave. Measured patterns showed a strong presence of higher-order mode radiation for $f > 3f_L$.

A similar investigation¹³ used a 2-in-diameter, etched-circuit archimedean spiral suspended 0.15 in over a ground plane. The spiral arms were terminated with absorber paint, and no absorbers were placed between the spiral and the ground plane. Gain measurements of this antenna are shown in Fig. 14-17. Patterns indicate the presence of 3λ mode radiation, since the principal-plane and conical-cut patterns show WOW on the order of 10 to 15 dB. Principal-plane and 60° conical-cut patterns measured at 10 GHz are shown in Figs. 14-18 and 14-19. It is speculated that the reflection from the ground plane couples into the spiral circuit, propagates outward toward the spiral terminations, and radiates from the 3λ ring. Furthermore, the attenuation through the 1λ ring is reduced by the closely spaced (<0.1 λ) ground plane, which accentuates the 3λ mode radiation. The high, but uniform, axial ratio values on the pattern edges indicate that some energy has leaked through the 3λ ring and is reflected from the terminations. The reflected wave from the terminations radiates from the 3λ ring (with a null on axis) in the opposite sense of circular polarization than that for the incident wave and thus causes high axial ratios at angles off axis.

Absorber-loaded-cavity characteristics Two-arm spiral unloaded-cavity radiators are limited to an octave bandwidth by the metallic cavity base and sidewalls. However, if absorbing material is interposed between the cavity base and the radiating surface, as suggested by Fig. 14-14, greater-than-decade bandwidths are achievable. Figure 14-20 depicts a typical measured pattern (with a rotating linearly polarized source) obtained with an absorber-loaded 2-in-diameter 2- to 18-GHz spiral. The quality of the patterns is excellent, and on-axis axial ratios of less than 2 dB over the full decade are achievable. Figure 14-21 shows measured gain of the 2-in-diameter archimedean spiral. Two examples of 2-in-diameter archimedean spirals are shown in Fig. 14-22. While absorber re-



EACH CIRCLE = 10 dB

FIG. 14-18 Measured conical-cut pattern at 60° on an archimedean spiral spaced 0.15 in above a ground plane at 10 GHz. (Courtesy Loral Randtron Systems.)

moves the cavity-imposed bandwidth limitation, it results in a gain loss on the order of 3 dB compared with the unloaded-cavity case. This loss depends on the proximity of the spiral arms to the absorber, the cavity depth, and the characteristics of the absorber itself. The absorber layer generally fills the lower volume of the cavity to within 10 or 20 percent of the top. For a cavity-backed spiral designed for the 2- to 18-GHz band, the cavity depth is typically 1 in, and the absorber is spaced approximately 0.15 in below the spiral arms.

It is important that the absorbing material in the cavity produces enough attenuation that the reflected wave from the base of the conducting cavity back into the spiral is small compared with the incident wave radiated into the cavity. The reflected wave has the

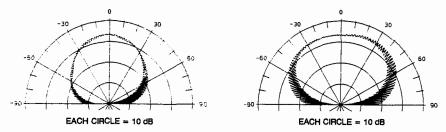


FIG. 14-19 Measured principal-plane patterns on an archimedean spiral spaced 0.15 in above a ground plane at 10 GHz. (Courtesy Loral Randtron Systems.)

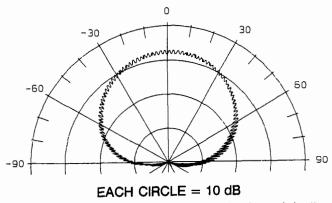


FIG. 14-20 A 2-in-diameter cavity-backed archimedean-spiral pattern at 10 GHz.

opposite sense of circular polarization than the incident wave and will couple into the spiral to produce traveling waves on the spiral that propagate to the outside terminations of the spiral arms. (Remember that exciting the spiral from the inside and outside terminals produces opposite polarizations.) If the terminations are not matched, then the reflected waves will radiate and degrade the axial ratio. If the frequency is such that higher-order radiation rings (M + pN) rings) exist on the spiral, then the outward-traveling waves resulting from the cavity reflection and the "leakage" through the first active region will add vectorially. Since the path length for the cavity reflection is larger than that for the leakage wave, the WOW will vary periodically with frequency. This strongly suggests that the terminations should be well matched and that the two-way attenuation through the cavity should be greater than 16 to 18 dB at the lowest frequency for which the first higher-order radiation ring, $(M + N)\lambda$, exists on the spiral.

The impedance seen by the spiral is the parallel combination of the impedance seen looking into free space through the radome, if any exists, and approximately the imped-

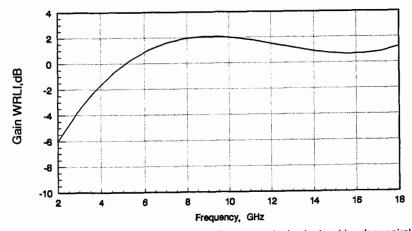


FIG. 14-21 Measured gain (WRLI) of a 2-in-diameter cavity-backed archimedean spiral.

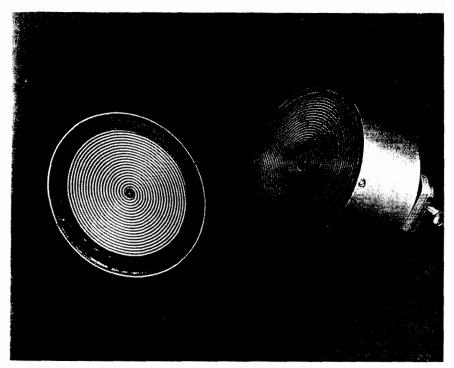


FIG. 14-22 Two 2-in-diameter complementary archimedean spirals terminated with absorber paint and a $100-\Omega$ resistor; arm width W=0.022 in. (Courtesy Loral Randtron Systems.)

ance looking into half space filled with the absorbing material (since the cavity reflections do not couple into the feed terminals). The power split is inversely proportional to the ratio of the characteristic impedances of these two media. For equal impedances, half the input power is lost in the absorbing cavity. Ideally, we would like to have an absorbing structure with a characteristic impedance much higher than that for free space. This could increase the gain by nearly 3 dB. Unfortunately, there is no known technique for accomplishing this over a wide bandwidth. Thus the objective is to try to make the characteristic impedance of the absorber nearly equal to the free-space impedance. This is accomplished by using honeycomb absorbers, corrugated structures, and tapered structures.

Balun circuits The two-arm spiral antenna is fed in a balanced-transmission-line mode (180° phase difference between arms) to obtain radiation in the axial direction. Normally, the output port of the spiral antenna is connected to an unbalanced coaxial transmission line; thus a balun, or balanced-to-unbalanced, transformation circuit is needed. Also, there is often a difference in impedances between the spiral arms (approximately 120 Ω for a printed-circuit complementary archimedean spiral) and the output coaxial line (usually 50 Ω), so the balun circuit also may incorporate an impedance-matching device. A number of balun types and their operation are described in Chap. 43. Of these circuits, only a few have practical application to spirals. For octave-bandwidth requirements, a balun described by Bawer and Wolfe¹⁴ using a hybrid microstrip-stripline

printed-circuit implementation is simple and cost-effective. This balun, based on earlier work by Roberts, ¹⁵ can provide a VSWR of less than 1.7 over a full octave for cavity-backed spirals in the 0.1- to 12-GHz region.

For extreme bandwidths, the infinite balun¹⁶ can be implemented using a small coaxial transmission line and embedding or soldering the outer conductor to one of the two spiral arms and attaching the center conductor to the other arm at the central feed point. For symmetry, a dummy cable is sometimes soldered to the other arm of the spiral in a similar configuration. Saul¹⁷ has developed a microstrip infinite balun that allows VSWR levels of less than 2:1 to 40 GHz. One of the spiral arms is fed from its outer periphery by a coaxial-cable microstrip transition. The microstrip conductor uses the spiral radiating arm, printed on the opposite side of the substrate, as its ground plane. At the center point, the microstrip center conductor is simply connected to the second arm to form the infinite balun.

The coaxial infinite balun, while simple to implement, does not have the impedance flexibility of the microstrip balun because tapering or stepping the impedance is not easy. These infinite baluns are limited to use on spirals that have wide arm dimensions (to act as a ground plane or to support the coaxial outer conductor) such as the log-spiral with a low τ and low-frequency log or archimedean spirals.

Very-wide-band baluns are required for absorber-loaded cavity-backed spiral antennas. Coaxial implementations based on the designs proposed by Marchand¹⁸ are commonly used. This balun is well balanced at its output and provides excellent overall performance for 10:1 bandwidths, provided the upper limit is less than 40 GHz. Excellent impedance transformations are easily achieved when a double-sided printed-circuit balanced transmission line is used to connect the spiral arms to the balun circuit (see Fig. 14-14). A simple linearly tapered transformation can be used for low impedance ratios, and the more sophisticated Chebyshev transformer (see Chap. 43) can be used to obtain optimal performance for large impedance ratios. VSWR levels of less than 3:1 have been achieved by Greiser and Wahl¹⁹ using the Marchand balun. They also describe an alternative printed-circuit version that operates from 0.4 to 18 GHz with a VSWR of less than 2:1 and excellent phase (±4°) and amplitude (±0.5 dB) balance.

A broadband balun widely used because of its simple construction is the tapered balun described in Chap. 43. Mode transformation is obtained by a gradual tapering in cross section from unbalanced coaxial line or stripline to a balanced two-conductor line. 20,21 Impedance transformation can be accomplished by using the above-referenced impedance tapers. The impedance of the unsymmetric transition region (unbalanced-to-balanced) transmission line has been developed by Duncan and Minerva²⁰ for coaxial transmission line and Holloway²² for unequal-width two-strip transmission line. Care must be exercised in the implementation of these baluns because the taper in the transition region can cause poor balance at the output. This results in the excitation of mode 0 (or 2), which produces a beam tilt for the radiation pattern. Absorbers are carefully placed at the transition region so as to attenuate the ++ mode much more than the desired +- mode.

Axial ratio and polarization diversity Spirals radiate one sense of polarization when excited from their central feed points and the opposite sense when excited from their terminals. Energy that radiates when fed from the central terminals must be totally absorbed by terminations at the spiral ends to avoid deterioration of the axial ratio. If the frequency is such that the 3λ ring does not exist on the spiral, then the on-axis voltage axial ratio AR is approximately

$$AR = \frac{1 + A\rho_t}{1 - A\rho_t} \tag{14-22}$$

where A is the square root of the power attenuation through the 1λ ring and ρ_t is the magnitude of the reflection coefficient at the termination. Equation (14-22) may be used to estimate A for spiral antennas by measuring the axial ratio for both an open-circuited $(\rho_t = 1)$ and a terminated case $(\rho_t = 0)$ and then solving for A. The efficiency also may be determined from the attenuation through the active region. If the 3λ ring exists, then the WOW is increased and the reflected energy from the terminations will radiate in the 3λ ring and will degrade the axial ratio only in the direction off the axis, since the 3λ ring pattern has a null on axis.

Terminating loads may be achieved by a number of methods. A variety of resistive paints (Emerson and Cumming Ecco-Sorb 268E, for example), absorbers, or resistive cards applied to a termination length of at least one-half wavelength will provide an acceptable load. A cavity sidewall lined with an absorber will act as a termination if the spiral-circuit substrate is not too thick. Another approach is to ground the spiral arms, through a carbon resistor (approximately $100~\Omega$), to the cavity. Similarly, adjacent spiral arms can be connected together through a resistor at the periphery to form a termination. Examples of spirals terminated with absorber paint and a grounding resistor are shown in Fig. 14-22.

Feed radiation, reflections, and asymmetries in the cavity and aperture also will contribute to increased axial ratio. These problems are typically linearly polarized and cause an unsymmetric axial-ratio response of principal-plane and conical-cut radiation patterns. The conical-cut pattern of Fig. 14-9 is an example of two distinct problems: the two maxima and two minima indicate 3λ ring radiation, and feed radiation (or a reflection) is evidenced by unequal axial ratios at the minima.

Dual-polarized radiation may be obtained by simultaneously feeding the spiral at both its central and peripheral terminals. However, the spiral size for a two-arm structure should not exceed a diameter of $2\lambda/\pi$ to ensure against the generation of undesired modes when feeding from the outer rim. Given the earlier-cited radiating width (approximately 0.7λ to 1.4λ), the operating bandwidth is restricted to approximately 2:1. If dual circular polarization is required over a very broad band, then a more effective approach is to use the sinuous concept (capable of at least 14:1 bandwidths) described in the subsection "Dual-Polarized Sinuous Antennas."

Multiple-arm cavity-backed spirals An N-arm spiral can excite N-1 pattern modes. The total phase progression across all spiral arms is $2\pi M(M=1,2,\ldots,N-1)$. Thus the interarm phase progressions have the value $2\pi M/N$. When M=1, the result is always a unidirectional pattern independent of N. All other pattern modes are symmetric about the boresight axis and have a null on axis. Aside from the uniqueness of the M=1 or sum-channel mode, all modes are principally differentiated by their phase progression about the normal axis (θ variant). A more complete treatment of the mode characteristics of the multiarm spiral is given in the subsection "Modal Characteristics of Multiarm Spiral Antennas."

For self-complementary multiple-arm planar spiral (and log-periodic) structures, the characteristic impedance of each arm with respect to ground is given by

$$Z_{M} = \frac{30\pi}{\sin\left(\frac{\pi M}{N}\right)} \tag{14-23}$$

where M is the mode number and N is the number of arms. This applies to thin-sheet structures for free-space conditions. Dielectric substrates will lower the impedances. The characteristic impedances are different for each mode, and compromises are necessary in

selecting a feeder impedance. For example, a reasonable compromise for a four-arm spiral operating in the M=1 and M=2 modes, for which Z_1 and Z_2 are 133.3 and 94.2 Ω , respectively, would be 112 Ω at the feed point. This value would limit the inherent mismatch to less than 1.19 for both modes. Broadband transformers are used to match to the characteristic impedance of the feed network. An indepth treatment of multiarm spiral mode characteristics, balun networks, and construction techniques is given by Corzine and Mosko.⁵

Two-Arm Log-Spiral Antennas As mentioned previously, the design of the spiral terminations, cavity (including absorber materials), and balun is essentially the same for the log-spiral as for the archimedean spiral. However, the design of the spiral arms is different for the two cases.

The design ratio τ is independent of radius for the log-spiral arms. The gain loss and attenuation through the active region are essentially independent of τ for the range of 0.3 to 0.55 for frequencies greater than $2f_L$. However, this is not the case for $f < 2f_L$.

A computer-aided study was performed to determine the variations in gain, directivity, loss in the termination, WOW, and cross-polarization with the parameters τ and r_2/λ for two-arm planar strip log-spirals with $\delta = 65^{\circ}$ and v/c = 0.92. The termination was matched with a return loss greater than 16 dB by means of distributed-series resistive loading of the last quarter turn of the spiral arms. The gain loss represents power dissipated in the terminations. An ideal absorbing cavity without walls was assumed. The results are shown in Fig. 14-23 in the form of antenna gain with respect to a linearly polarized isotropic antenna versus $2\pi r_2/\lambda$ for $\tau = 0.12$ to 0.56. For $2\pi r_2/\lambda = 1$, the outside circumference of the spiral is one wavelength (λ ring). Note that the gain drops off rapidly as τ and r_2/λ are decreased. The gain for the smaller values of τ may be increased somewhat by using resistor terminations at the outside of the spiral instead of resistive loading along the last quarter turn that protrudes into the active region at the low-frequency end. This would reduce the power dissipated in the terminations. The directivity varies from about 3.0 to

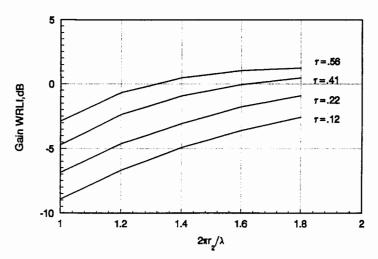


FIG. 14-23 Planar two-arm log-spiral antenna gain versus $2\pi r_2/\lambda$ for $\tau=0.12, 0.22, 0.41$, and 0.56.

4.2 dB as τ varies from 0.12 to 0.56. Surprisingly, the WOW and on-axis axial ratio were essentially independent of τ and r_2/λ for $\tau \ge 0.22$ and have values of about 0.5 and 1.5 dB, respectively. It was not possible to obtain results for $\tau > 0.6$ because of accuracy limitations of the MININEC3 computer program.

It is apparent that τ should be 0.56 or greater in the outer region of the spiral to ensure adequate gain for $f < 2f_L$, τ may be gradually reduced to about 0.3 in the inner region of the spiral in order to relax the tolerances on the construction of the spiral arms and the connection of the feed conductors. As with the archimedean spiral, δ should be in the range of 90 to 130°, which provides a Z_0 range of 130 to 90 Ω for v/c = 0.9. The value of v/cshould be 0.9 or greater to ensure adequate attenuation through the active region and modest WOW for frequencies greater than $3f_L$. The results of these studies indicate that it is not necessary to adhere to the stringent design principles for log-spiral antennas. In fact, it is probably desirable in most cases to vary τ and/or δ with the radius. An example is to use $\tau > 0.6$ in the outside region of the spiral where the gain increases with τ and smaller values of τ in the inside region where the gain is insensitive to τ . An unlimited number of variations can be used. These conjectures have not been verified experimentally. The archimedean spiral is just one example of these quasi-frequency-independent antennas. For bandwidths less than 3:1, where radiation from the 3λ ring is negligible, lower values of v/c may be used to reduce the diameter of the spiral with a modest loss in gain. The determination of r_1 and r_2 is quite similar to that for the archimedean spiral.

Four-Arm Log-Spiral Antennas Four-arm planar log-spiral antennas have been developed for homing and direction-finding systems with amazing accuracies over a wide field of view and over decade bandwidths. The reader is referred to the excellent book by Corzine and Mosko⁵ for a detailed discussion of these antenna systems. Briefly, use is made of several important design techniques. Modes 1 and 2 are used to form either rotationally symmetric sum and difference patterns or four tilted beams. The directionfinding information is obtained by comparing the relative phase and/or amplitude of the various patterns. Planar structures are used so that the phase centers for modes 1 and 2 are the same. A tapered τ log-spiral is designed such that the pattern rotation versus frequency may be compensated for by a linear (with frequency) phase delay between modes 1 and 2. A four-arm conical spiral could be used, but it is impractical for wide bandwidths because of the separation of the phase centers for modes 1 and 2. The most important design technique is that symmetric feed networks have been devised such that the boresight error is zero if similar circuits are identical, even though the circuits have errors in their scattering matrices. The feed networks are composed of quadrature hybrids, tapered-line magic-T's, phase-difference circuits, and isolated power splitters.

The end result is that boresight errors of about 1/50 of the sum-pattern beamwidth (usually about 70°) have been achieved. This is several times better than what was achieved in the sixties.

Conical Log-Spiral Antennas

Multiple-arm conical spiral antennas are employed to obtain unidirectional patterns without the use of a cavity or a reflector. Excellent computer programs^{23,24} that calculate the patterns, current distribution, and impedance were developed in the late sixties. Present-day method-of-moments programs are now preferred because of their versatility. When fed from the vertex, the phasing of the currents in the arms along a radial line on the cone is such that radiation first takes place in a backfire mode, which is essential for frequency-independent operation. Most R&D efforts have been expended on conical

log-spiral antennas, but archimedean-type conical spiral antennas with uniform spacing between arms also can be used. Half-cone angles of 25° or less are usually required to achieve a good unidirectional pattern.

Two-arm conical spirals fed in a balanced manner (mode 1) are commonly used to provide a single-lobe, unidirectional, circularly polarized pattern. Four-arm conical spirals fed in mode 2 (+, -, +, -excitation) are used to provide a circularly polarized, rotationally symmetric difference pattern. When the axis of the cone is oriented vertically, the antenna produces wideband, omnidirectional, circularly polarized coverage. Conical spiral structures with four or more arms may be excited by networks of hybrid circuits to provide sum and difference patterns or tilted beams for direction-finding and homing applications. However, the accuracy is severely limited because the phase centers of the sum and difference modes (λ and 2λ radiation rings) are displaced from each other along the z axis.

Two-Arm Conical Spirals Extensive experimental²⁵ and theoretical²⁴ results have been reported. Figure 14-24 shows a two-arm conical spiral consisting of angular strips lying on the surface of a cone and defines the various parameters that specify the spiral structure. Tapered rods can be used for the arms, and even constant-diameter rods may be used for surprisingly wide bandwidths.

Figure 14-25 shows average half-power beamwidth (HPBW) and directivity as a function of the spiral pitch angle for various cone angles as measured by Dyson and Mayes. ²⁶ The variation in HPBW to be expected over wide bandwidths is shown in Fig. 14-26. A conical-cut pattern at $\theta = 60^{\circ}$ would show a WOW that increases with the variation. Notice that the variation decreases as the pitch angle ψ increases (or τ increases).

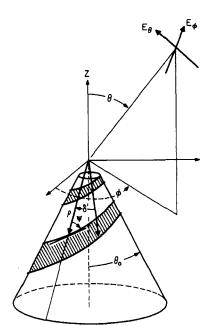


FIG. 14-24 Parameters of the conical logspiral antenna. (© 1965, IEEE.)

The variation is due to radiation from regions other than the 1λ ring, such as the 3λ ring, which produces a nonrotationally symmetric pattern. Pitch angles greater than 75° ($\tau > 0.2$) are required for small variations. However, this necessitates a tightly wound spiral with longer arms than for smaller pitch angles. The front-to-back ratio of the unidirectional pattern increases with pitch angle and decreases with increasing cone angles. For $\psi = 80^{\circ}$, the front-to-back ratio increases from 6 to 25 dB as $2\theta_0$ decreases from 45 to 15°. The axial ratio is on the order of 2 to 4 dB for θ varying from 0 to 90° for a pitch angle of 45° with a $2\theta_0 = 20^\circ$ cone. For larger pitch angles, the axial ratio approaches 0 for $\theta =$ 0 but increases rapidly for $\theta > 60^{\circ}$ (such as 4 dB or more).

The radiation mechanism of the spiral may be explained as follows. A generator excites out-of-phase traveling-wave currents at the vertex of the two-arm spiral. These currents travel in a nonradiating or transmission-line mode until they reach the active region. There is little radiation,

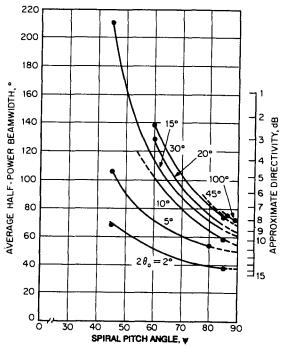


FIG. 14-25 Average half-power beamwidth and approximate directivity of conical log-spiral antennas ($\delta = 90^{\circ}$). (© 1965, IEEE.)

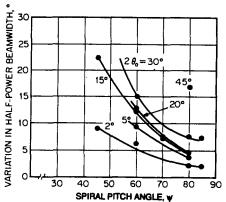


FIG. 14-26 Approximate variation in halfpower beamwidth for wideband operation. (© 1965, IEEE.)

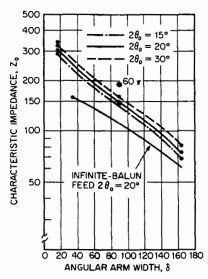


FIG. 14-27 Approximate characteristic impedance of the conical log-spiral antenna as a function of the angular arm width. (© 1965, IEEE.)

since the currents in adjacent arms are approximately out of phase. In the active region, currents in adjacent arms are nearly in phase. Calculations by Yeh and Mei²⁴ have shown that attenuation in the active region is in the range of 7 to 10 dB per wavelength along the spiral arms. Dyson and Mayes²⁶ have shown that if the cone is truncated at a point where the total attenuation in the active region is 15 dB, then radiation and impedance characteristics are essentially the same as those of the infinite structure. This point occurs when the circumference of the cone is somewhat less than 1.5 λ , depending on ψ and θ_0 . The transmission-line region may be truncated at a point where the circumference of the cone is less than 0.4\(\lambda\). Detailed information for designing spirals for specified bandwidths is given by Dyson and Mayes.26

Figure 14-27 shows the characteristic impedance of the conical spiral as a function of the angular arm width δ for several

cone angles and one with an infinite-balun feed. In the latter case, the addition of the coaxial line to the arm reduces the characteristic impedance. A voltage standing-wave ratio (VSWR) of less than 1.5:1 with respect to the Z_0 of the spiral may be obtained over the bandwidth.

Four-Arm Conical Spirals A four-arm spiral fed in mode 2 (+, -, +, -excitation) produces a difference pattern with rotational symmetry, 26 provided there is sufficient attenuation through the active region, which implies pitch angles greater than 60°. Figure 14-28 shows the computed direction and beamwidth²³ of the beams versus secant ψ . To obtain good coverage in the horizontal plane (β close to 90°), ψ must be in the range of 45 to 50° for $2\theta_0 \approx 20^\circ$.

A photograph of an omnidirectional conical spiral is shown in Fig. 14-29. The antenna is fed by a four-conductor system running up the axis of the cone, which is excited by the feed network shown in the right side of the photograph. For pitch angles of less than 60°, there is considerable end effect, so the azimuth and elevation patterns are scalloped and the axial ratio is increased. However, the patterns are satisfactory for surveillance applications. A VSWR < 2:1 may be achieved over wide bandwidths.

14-3 LOG-PERIODIC ANTENNAS

The first successful log-periodic (LP) antenna was introduced by DuHamel and Isbell² and was a self-complementary planar-sheet structure consisting of two angular strips supporting curved teeth. It produced a bidirectional pattern. Isbell²⁷ then demonstrated that a unidirectional pattern could be obtained by using a nonplanar arrangement of the two halves of the antenna. Then it was found that the self-complementary condition was not required, and a variety of sheet and wire LP designs were introduced by DuHamel and Ore.²⁸ Isbell²⁹ then introduced the LP dipole array, the most commonly used LP antenna.

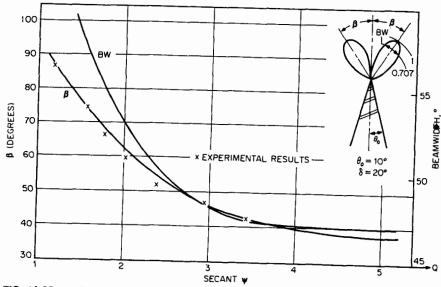


FIG. 14-28 Half-power beamwidth and beam orientation versus secant ψ for mode 2; θ_0 = 10° and δ = 20°. (© 1971, IEEE.)

Since that time, many types of LP antennas have been studied with varying degrees of success. Space does not permit a discussion of all the types or a presentation of detailed design data.

General Characteristics

The geometry of LP antenna structures is chosen so that the electrical properties must repeat periodically with the logarithm of the frequency. Although this appears to be a backward approach to the broadbandantenna problem, nevertheless, frequency independence can be obtained when the variation of the properties over one period, and therefore all periods, is small. The LP design principles are illustrated in Fig. 14-30, which shows a metal-sheet LP structure with trapezoidal teeth. The two LP elements in the H-plane array are fed against each other by a generator placed between their vertices. The four sets of teeth are defined by similar curves, the equations for which may be written in polar coordinates as $\theta = g(r)$, where g(r) is some function of r. If θ is plotted versus $\ln r$ in rectangular coordinates, that is, $\theta = f(\ln r)$, then LP principles demand that f be a peri-

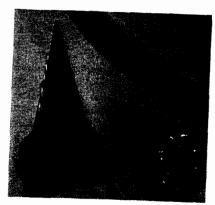


FIG. 14-29 Four-arm conical log-spirals excited in mode 2 for circularly polarized omnidirectional pattern, 2 to 12 GHz. (Courtesy of GTE Sylvania Systems Group.)

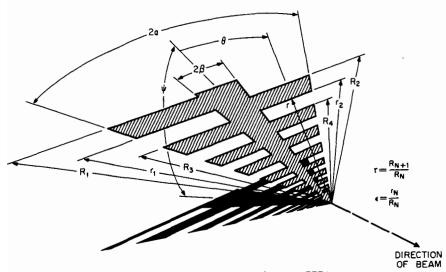


FIG. 14-30 Trapezoldal-tooth log-periodic antenna. (© 1958, IEEE.)

odic function. A more general but rather academic definition of LP structures for non-planar and three-dimensional structures is given by DuHamel. ³⁰ Let $\tau = R_{n+1}/R_n$, where R_n is the distance from the vertex to the outer edge of a tooth. Let $r_n = \epsilon R_n$. Then ϵ is a measure of the tooth width (the figure is drawn for $\epsilon = \tau$, but usually $\epsilon > \tau$). It may be seen that the logarithmic principle implies two conditions. The first is that all similar sets of dimensions, such as R_1 , R_2 , R_3 , etc., must form a geometric sequence with the same geometric ratio τ . The second is that angles are used to a considerable extent in defining the antenna. For example, the extremities of the teeth and the triangular supporting section of the teeth are defined by angles.

Now if the antenna structure of Fig. 14-30 were infinitely large and infinitely precise near the feed point, it is easily reasoned that the structure must look exactly the same to the generator every time that the frequency is changed by the factor τ . The current distribution on the structure at τf_0 is identical with that at τ_0 except that everything is moved out one step along with a 180° rotation. Thus, since the wavelength has changed by a proportionate amount, the input impedance must be the same at τf_0 and f_0 . Thus the input impedance varies periodically with the logarithm of frequency with a period of $\ln (1/\tau)$. Because of the special left-right asymmetry of the structure, the period of the radiation pattern is $2 \ln (1/\tau)$ rather than $\ln (1/\tau)$.

If the variation of the impedance and pattern is small over a period and, therefore, over all periods because of the repetitive characteristics, it is seen that the result is essentially a frequency-independent antenna. Fortunately, some finite LP structures provide frequency-independent operation above a certain low-frequency cutoff, which occurs when the longest tooth is approximately one-quarter wavelength long. Frequency-independent operation above the cutoff frequency is possible because some LP antennas display little end effect. It is found that the currents on the structure die off quite rapidly past the region where a quarter-wave tooth exists. This means that a smaller and smaller portion of the antenna is used as the frequency is increased, which is another way of saying that the effective electrical aperture (the aperture measured in wavelengths) is essentially

independent of frequency. Since it is not possible to extend the antenna to the origin because of the presence of the feed transmission line, a high-frequency cutoff occurs when the shortest tooth is less than one-quarter wavelength long.

The structure of Fig. 14-30 is horizontally polarized and has a bidirectional beam for $\psi=180^\circ$, with the beams pointing into and out of the paper. If the input impedance is plotted on a Smith chart over a frequency range of several periods, it will be found that the locus forms an approximate circle with the center lying on the zero-reactance line. The characteristic impedance of the LP structure is defined as the geometric mean of the maximum and minimum real values on the locus. The VSWR referred to this characteristic impedance is then simply equal to the ratio of the maximum impedance to the characteristic impedance.

The operation of this antenna is explained briefly as follows. The two angular strips of width 2β form a uniform biconical TEM transmission line. The generator excites a wave on this line, which in turn excites currents on the *monopoles* (trapezoidal-shaped monopoles). Most of the radiation takes place in the active region where the monopoles are about $\lambda/4$ long. Attachment of monopoles to opposite sides of a strip introduces a 180° phase shift of the currents in successive monopoles. The additional phase delay in the transmission line between monopoles is sufficient to produce backfire radiation, which is essential for frequency-independent performance.³¹ Each of the two elements produces a unidirectional pattern pointing in the direction of the element. The region before the active region is called the *transmission-line region*, where there is little radiation. The monopoles present shunt capacitive loading of the line. Near the feed point, the loading per unit length is constant, and the characteristic impedance of the antenna is determined by the amount of the loading. It is always lower than the characteristic impedance of the two angular strips, which are commonly called the *feeder*.

There is nothing sacred about adhering to the LP design principles described above. The design parameters τ , ϵ , α , β , and ψ may vary gradually or even abruptly with radius r with only modest changes in the radiation characteristics because they are rather insensitive to the design parameters. These designs are referred to as quasi-frequency-independent antennas. For example, α may be increased for the longest teeth so as to reduce the length of the antenna with only a slight reduction of gain at the low-frequency band of the antenna. The β angle could be gradually increased near the feed-point region in order to decrease the Z_0 of the feeder and therefore the Z_0 of the antenna. It is recommended that the effect of such changes should be evaluated by a method-of-moments computer program before implementing the changes.

Log-Periodic Dipole Antennas

If β approaches zero and ϵ approaches unity for the trapezoidal-tooth structure, then the antenna becomes two monopole arrays supported by thin angular strips. The strips form an angular transmission line whose characteristic impedance is independent of r. If ψ approaches zero, the antenna becomes a dipole array excited by a balanced transmission line. Rather than use tapered transmission-line strips, it is preferable to use constant-width strips or rods²⁹ with constant spacing, illustrated in Fig. 14-31. This is the most popular and most thoroughly studied LP antenna. A schematic circuit for the LP dipole array is illustrated in Fig. 14-32, wherein transpositions of the feeder between dipoles are shown. The parameter σ is defined as

$$\sigma = \frac{1 - \tau}{4} \cot \alpha \tag{14-24}$$

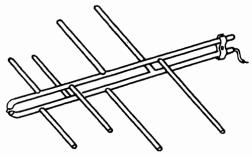


FIG. 14-31 Log-periodic dipole antenna.

and is the spacing in wavelengths between a $\lambda/2$ dipole and the adjacent shorter dipole. Once two of the three parameters α , τ , and σ are specified, the third may be determined from this formula. The ratio of the half-dipole length to the radius of the dipole is defined as h/a, and the transmission-line (feeder) characteristic impedance is Z_0 . The antenna may be considered as a cascade of cells consisting of sections of transmission line shunt-loaded at the center by the dipole impedance (taking into account the coupling between dipoles). For small α and large τ , there is essentially a traveling wave propagating away from the generator on the left. The transmission-line region of the antenna is the first portion where the dipole lengths are considerably less than a half wavelength. Because of the phase reversal between dipoles and the small spacing, the dipoles are phased to radiate in the invisible region, which means that there is little radiation. The first active region occurs when the dipoles are about one-half wavelength. Radiation occurs in the backfire direction³¹ (to the left) because of the phase reversal between dipoles. If the phase reversals are not included, radiation will occur in the end-fire direction (to the right), which illumi-

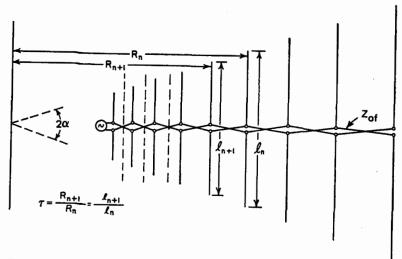


FIG. 14-32 Schematic diagram of a log-periodic antenna. The three dashed lines indicate typical locations of electric ground planes between each pair of dipoles.

nates the larger portions of the array and produces scalloped patterns and erratic impedance behavior. This is called *end effect* and has been observed many times.

The attenuation through the active region due to radiation and reflection loss is a complicated function of τ , σ , Z_{0f} , and h/a. The shunt loading (or attenuation) of the line by a resonant dipole increases with the feeder impedance, and the bandwidth over which the dipole loads the line is inversely proportional to the Q of the dipole, which increases with h/a. The attenuation increases as τ is increased, provided σ does not become very small. An attenuation of about 20 dB through the active region is desired to keep the end effects small. The energy that passes through the active region will radiate to some extent in the region where the dipole lengths are between $\lambda/2$ and $3\lambda/2$, but predominantly in the second active region, where the dipoles are $3\lambda/2$ long. The radiation direction will depend on τ and σ and usually produces frequency-dependent patterns. If the frequency is such that the longest dipole is less than $3\lambda/2$ long, then the energy will be reflected (unless there is a resistive termination on the antenna) and will radiate in the active region in the backfire direction, which produces a backlobe in the antenna pattern.

The directivity of the antenna increases with the length of the active region, which increases as τ is increased with σ held constant (α is decreased), since there are more dipoles near a length of $\lambda/2$. The length of the active region increases as Z_{0f} is decreased, since the attenuation per cell is decreased. The E- and H-plane beamwidths vary with α approximately as shown in Fig. 14-33 for a single-wire trapezoidal-tooth LP element.

Carrel³² performed the first and an extensive theoretical study of the LP dipole array wherein he assumed sinusoidal currents on the dipoles. Later, Cheong and King³³ and De Vito and Stracca^{34,35} performed theoretical studies by assuming a three-term current

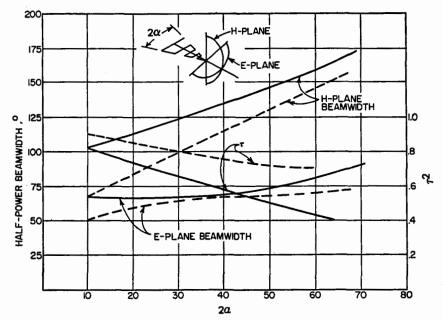


FIG. 14-33 Pattern characteristics of a wire trapezoidal-tooth element for (——) the approximate minimum value of τ and (---) a larger value of τ .

distribution, which they claimed gave much better accuracy and gains of 1 or 2 dB less than that reported by Carrel. Still later, Butson and Thomson³⁶ pointed out that Carrel had made an error in the calculation of the *E*-plane pattern. When it was corrected, they showed that the gain calculations for the two methods were nearly identical. Figure 14-34 shows directivity as a function of τ and σ for $Z_{0f}=100~\Omega$ and h/a=125, as reported by Carrel. His gain numbers have been reduced by 1.5 dB, which is an average correction for the error. Since the *E*-plane beamwidth is determined mostly by the dipole pattern and is approximately 60°, the *H*-plane beamwidth may be determined from the beamwidth formula for directivity; that is, $D=41,253/(BW_EBW_H)$. De Vito and Stracca give extensive results for impedance and gain for a wide range of Z_{0f} , τ (with σ optimal), and h/a. Increased gains may be achieved by using an *E*- or an *H*-plane array of LP monopole elements.

The characteristic impedance of the antenna may be computed from the image impedance of a cell for small dipole lengths. It is given by

$$Z_0 = Z_{0f} \left(1 + \frac{Z_{0f}}{2Z_{0a}X} \right)^{-1/2}$$
 (14-25)

where X is the ratio of the cell length to the monopole length and is

$$X = \frac{2\tau(1-\tau)}{(1+\tau)\tan\alpha} = \frac{8\tau\sigma}{1+\tau}$$
 (14-26)

and Z_{0a} is the characteristic impedance of the monopole. For small spacings, adjacent dipoles are 180° out of phase. Then the characteristic impedance of a monopole is approximately the same as that of a rod of radius a placed between electric ground planes, as illustrated by the dashed lines in Fig. 14-32.

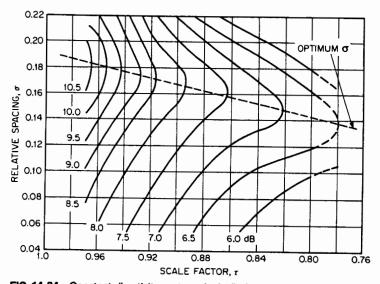


FIG. 14-34 Constant-directivity contours in decibels versus τ and σ ; $Z_{\rm or}=100$ Ω , h/a=125. Optimum σ indicates maximum directivity for a given value of τ . (After Ref. 32.)

The characteristic impedance of the monopole is then given by

$$Z_{0a} = 60 \ln (2hX/\pi a)$$
 (14-27)

Equation (14-25) may be solved for Z_0 in terms of the other parameters in order to achieve a desired Z_0 .

Asymmetric Log-Periodic Structures

Some of the useful LP elements which are asymmetrical about their centerline are shown in Fig. 14-35. They have the property that a scaling by the factor τ and a rotation of 180° about the centerline leads to an identical structure. Hence the impedance is unchanged, but the pattern is rotated 180°. It follows that the phase of the radiated field changes by 180° as the frequency is changed by τ . Each of the elements has a unidirectional beam in the direction toward which the element points. One of the elements may be fed against ground, or two or more elements may be fed against each other to form various types of frequency-independent arrays (such as circular or E-plane and/or H-plane arrays). These asymmetric structures tend to perform naturally and are much less critical to the design parameters than the symmetric structures discussed in the next subsection.

The first four elements of Fig. 14-35 consist basically of a transmission-line shunt loaded by various types of monopoles which are resonant when their length is about $\lambda/4$. The remaining elements are various types of zigzag elements and are similar to traveling-wave antennas. The active region occurs when the width of the structure is about $\lambda/2$. In order to obtain sufficient attenuation through the active region (and little end effect), α should be less than about 20° and τ greater than about 0.85. The restrictions on the shunt-loaded elements are much less severe. Two of the linear monopole elements of Fig. 14-35a placed in an H-plane array with ψ near zero form the LP dipole array that was discussed previously. The monopoles may be bent forward^{37,38} to form a more compact structure, but at the expense of increased E- and H-plane beamwidths. However, LP V-dipole antennas have been used very successfully as television receiving antennas. The antenna is truncated at the front so that the active region occurs in the $\lambda/2$ and $3\lambda/2$ dipoles for the low- and high-VHF bands, respectively, which provides for higher gain in the high band along with a more compact antenna.

The elements of Fig. 14-35c and d are wire outlines of trapezoidal and triangular sheet monopoles.²⁸ Because of the wider bandwidth of these thick monopoles compared with thin-wire monopoles, the pattern characteristics for a given τ_0 are about the same for

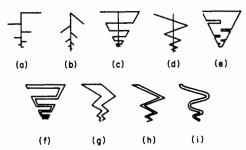


FIG. 14-35 Log-periodic elements which are invariant to a scaling by τ and a rotation of 180° about the centerline.

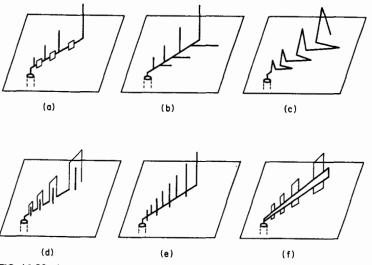
the thin-wire monopoles with $\tau = \sqrt{\tau_0}$. Thus the amount of wire is about the same, but the construction of the thin-wire structure is simpler. The zigzag elements of Fig. 14-35g and h have been studied by Kuo and Mayes³⁹ for $\alpha < 20^{\circ}$. E- and H-plane beamwidths in the range of 40 to 55° were obtained for an H-plane two-element array with $\psi = 2\alpha$. Limited studies have been reported on the sinusoidal type of LP zigzag. However, studies on periodic zigzags show that better performance is obtained with curved bends, since this reduces reflections from the bends. The reflections add up in the active region because the bends are spaced about $\lambda/2$.

For microwave applications, the LP elements are commonly printed on the opposite sides of a dielectric sheet. For the shunt-loaded elements it is preferable to use the trapezoidal-tooth sheet structure of Fig. 14-30, which allows a smaller τ than the wire monopole element. A constant-width feeder is used because the spacing between the feeder lines is constant. The tooth-width parameter ϵ should be somewhat greater than τ to prevent overlap of teeth on opposite sides of the sheet. If the teeth overlap, they tend to act like shunt transmission lines rather than radiating elements.

Symmetric Log-Periodic Structures

Many applications require a vertically polarized frequency-independent antenna over a ground plane with a height of about $\lambda/4$ at the low-frequency cutoff. One-half of a symmetric structure can be fed against a ground plane. The problem is how to obtain the extra 180° phase shift between adjacent radiating elements which comes naturally with asymmetric elements. Figure 14-36 shows several techniques for accomplishing this, but most are quite sensitive designs.

Figure 14-36a shows an LP monopole array fed by a transmission line over ground. The blocks represent 1:1 transformers with a phase reversal. This is not a sensitive design, but the cost and losses of the transformers may be prohibitive. If the transformers are not



 $\begin{tabular}{ll} \textbf{FIG. 14-36} & Log-periodic elements which are symmetric when combined with a ground-plane image. \end{tabular}$

included, backfire radiation does not occur in the active region and broadband performance is not obtained. The monopole and zigzag elements may be bent along their centerlines and fed against the ground plane, as illustrated in Fig. 14-36b and c. Half the monopole elements act like open-circuited transmission lines whose lengths must be adjusted within a few percent to obtain frequency-independent performance. Berry and Ore⁴⁰ give extensive design data. The shunt transmission lines may be replaced by series LC circuits. The shunt loading produces the extra phase delay required for backfire radiation. The bent zigzag studied by Greiser and Mayes41 achieves the extra delay by the portions of the line lying over the ground plane. This antenna design is less sensitive than the bent-monopole antenna. Another scheme studied by Greiser⁴² is the trapezoidal-type zigzag with parasite monopoles placed as shown in Fig. 14-36d. This configuration is described in more detail in the following paragraphs. Barbano⁴³ introduced parasitic monopoles between the elements of a monopole array as illustrated in Fig. 14-36e to achieve backfire radiation. The height of the parasitic element is approximately the geometric mean of the adjacent driven-element heights and must be adjusted to within 1 percent of the required height. Another technique devised by Wickersham. 44 using capacitive coupling to trapezoidal-sheet monopoles, is shown in Fig. 14-36f.

Ingerson and Mayes⁴⁵ used delay lines between elements of a monopole array to achieve backfire radiation. Since the lines were longer than $\lambda/2$ in the active region, they had to devise a method of eliminating the stop band in the region of the antenna where the lines were $\lambda/2$ long. They achieved this by adding reflections in the lines by means of changing the impedance of a portion of the line. This was called a *modulated-impedance feeder*. They also used this technique to feed an LP array of cavity-backed slots.

For these structures, τ is usually defined as the ratio of heights of adjacent vertical radiators. Hence the phase of the radiated field changes by 360° as the frequency changes by τ .

Log-Periodic Folded-Monopole, Folded-Dipole, and Folded-Slot Antennas Of the symmetrical elements shown in Fig. 14-36, perhaps the elements that exhibit the least sensitivity to design parameters are the folded-monopole array (Fig. 14-36a) and the corresponding folded-dipole array. The folded-slot array is derived from the complement of the folded-dipole array. All three of these antennas are described by Greiser. ⁴² This class of LP antennas is unusually versatile because three linearly polarized modes of radiation may be achieved: free-space dipole arrays, vertically polarized monopole arrays fed against a ground plane, and slot arrays in a ground plane.

These LP arrays are described by a few key angles and ratios. Figure 14-37 defines the parameters of the folded-slot antenna. The symmetry of the element about the centerline is evident from the figure. The principal design parameter is τ , which is used as the element-expansion ratio in the same manner as τ is used in the LP dipole array. The angles α , α_{s1} , and β are used to define the element lengths and feeder details. A complementary folded-dipole array may be defined by changing the slot portions of the figure to metal and the surrounding metal ground plane to free space. A balun or a 180° hybrid circuit may be used to feed the balanced transmission line formed at the front of the folded-dipole structure. A folded-monopole array also can be described by Fig. 14-37 by cutting the dipole version of the figure in half and feeding the half structure against a ground plane. Techniques for feeding the various arrays are shown in Fig. 14-38. These folded slots, dipoles, and monopoles are different from the conventional folded structures because they have both input and output terminals on each half of the folded structure, whereas the

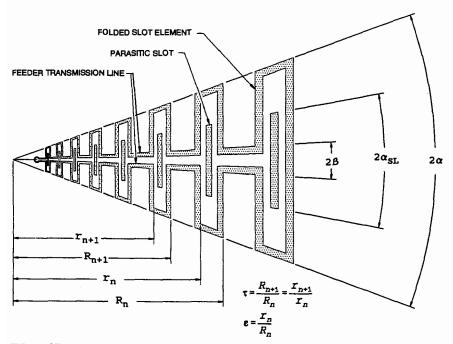


FIG. 14-37 Log-periodic folded-slot array: outline and parameters.

conventional folded structures have only one terminal, with the other one terminated by an open or short circuit. The folded structures also may be considered as a meander-line structure with parasitic loading, as described in later paragraphs.

In an investigation by Scherer, ⁴⁶ a large number of printed-circuit folded-slot and folded-monopole arrays were fabricated and tested over a frequency range of 2 to 12 GHz to determine the sensitivity of the array performance to the design parameters. Pictures of two of these arrays, which were photo-etched on a 0.020-in-thick fiberglass substrate, are shown in Fig. 14-39. For the study, τ was varied from 0.580 to 0.900 and α was varied from 20 to 35°. The angle α_1 was held constant at $\alpha/2$, β was set equal to $\alpha/3$, and ϵ was set equal to $\tau^{1/2}$. The length of the rear element of the folded-slot arrays was set at 3 in independent of τ and α . The front elements varied in length between 0.3 and 0.4 in depending on τ and α . The lengths of the folded-monopole elements were exactly one-half those of the folded-slot arrays. The arrays were centered on a ground plane that was 24 in along the array axis and 18 in wide. For the folded-slot array, an absorber-loaded cavity was placed below the array to allow radiation on only one side of the ground plane.

Radiation patterns for a folded-monopole array and a folded-slot array ($\tau = 0.85$ and $\alpha = 20^{\circ}$ for each) at a frequency of 5 GHz are shown in Fig. 14-40. The *H*-plane patterns were great circle cuts taken at the peak of the *E*-plane pattern ($\theta = 0$ and $\phi \approx 22^{\circ}$). The angle of the *E*-plane pattern peak above the ground plane is dependent on the extent of the ground plane in front of the array, τ , and frequency. However, for the tests described, the angle varied linearly from 26° at 2 GHz to 17° at 12 GHz. VSWR was typically below 2.5:1 for both the array types. Measured gain performance for both types of arrays is shown in Fig. 14-41 for $\tau = 0.850$ and $\alpha = 20^{\circ}$. As expected, the gain of the

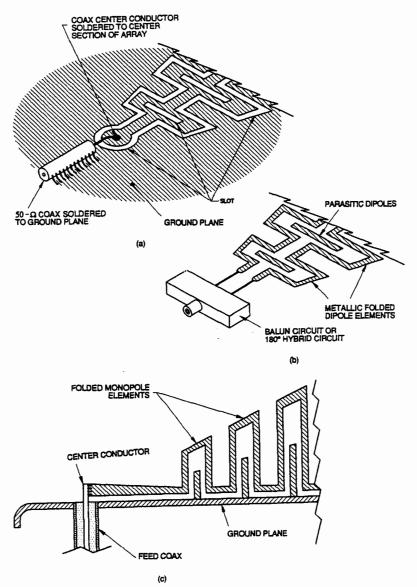


FIG. 14-38 Various feed techniques for log-periodic folded arrays. (a) Log-periodic folded-slot array feed, (b) log-periodic folded-dipole array feed, (c) log-periodic folded-monopole array feed.

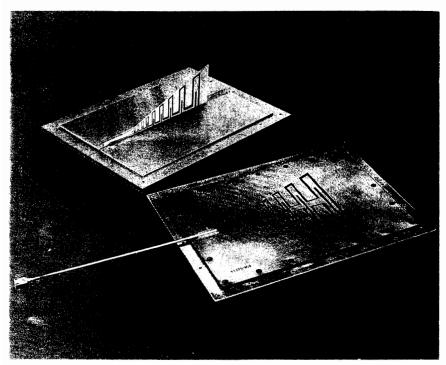


FIG. 14-39 Log-periodic folded-monopole and log-periodic folded-slot array models. (Courtesy Loral Randtron Systems.)

monopole array is about 3 dB higher than for the slot array. The slot and dipole arrays, with equivalent τ and α , will have similar gain.

The performance presented is typical for τ values between 0.75 and 0.86. Below $\tau=0.75$, dropouts in gain and pattern uniformity were experienced. Above $\tau=0.86$, the gain dropped off, most likely due to dielectric and resistive losses. Little variation in gain or beamwidth was found associated with α over the range of 20 to 35°. It was discovered that the cavity base and absorber significantly reduced the folded-slot array gain if the absorber was spaced less than 0.1λ from the elements. It appeared that fringing fields from the slots forming the elements and feeder transmission lines were coupling into the absorber. As a result, a tapered arrangement of cavity depth and absorber spacing was used. The best results were obtained when the distance from the absorber to the elements varied from 0.25 in at the front element (high-frequency element, 12 GHz) to 0.75 in at the rear element (low-frequency element, 2 GHz).

To investigate the impact of the short parasitic slot, the parasitic slot angle for the folded-slot array, shown as α_{i1} in Fig. 14-37, was varied from zero to nearly 2α . Performance characteristics were measured and found to be generally insensitive to the slot angle between values of $\alpha/3$ and 1.5α . At a slot angle of zero (no slot), the pattern backlobe and sidelobes increased, and the backfire mainbeam shape was somewhat degraded and broadened in both planes. This indicates that the presence of the short slot element has an

effect on the propagation velocity along the structure, but its length is not overly sensitive. The sensitivity of the angle α_{s1} and the overall operation of the folded-dipole array were also investigated using the method-of-moments computer program NEC-81.^{10,47} The parasitic-element insensitivity to length (or α_{s1}) was confirmed to be as measured. The elimination of the parasitic slot in the computer model also broadened the mainbeam and degraded the backlobe and sidelobes.

From both the experimental and calculated (method-of-moments) studies, an understanding of the operation of the folded-element array was developed. Like certain other LP antennas, such as the LP zigzag array, the folded-element arrays operate as a traveling-wave structure. The active region is formed where the monopoles are approximately $\lambda/4$ high and the dipoles and slots are approximately $\lambda/2$ wide. As discussed in previous paragraphs, a 180° phase shift between adjacent elements is required for backfire radiation. For asymmetric arrays, the 180° phase shift is a natural occurrence. For some symmetric arrays, the 180° phase delay is obtained with feeder transmission-line loading

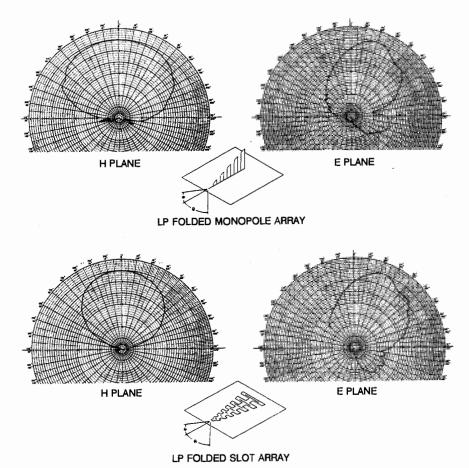


FIG. 14-40 Folded-monopole and folded-slot array E- and H-plane patterns.

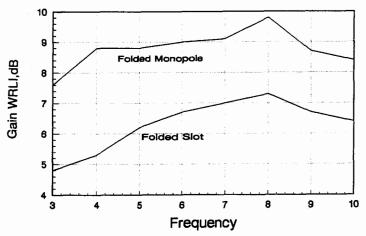


Fig. 14-41 Log-periodic folded-monopole array and log-periodic folded-slot array gain (WRLI) for $\tau=0.85$ and $\alpha=20^\circ$.

or delay line (Fig. 14-36b and c). Referring to Fig. 14-37 for the folded arrays, there is a 180° phase shift between currents on the element segments at r_n and the segments at R_n due to the meander-line reversal in direction. If the folded arrays are designed with $\epsilon = r_n/R_n = \tau^{1/2}$, then the spacing between the radiating r_n and R_n segments is log-periodic in frequency with a period of $\ln (1/\tau^{1/2})$. This implies an equivalence to asymmetric arrays where an equivalent τ for the folded arrays is $\tau^{1/2}$. An added implication is that the period of the radiation pattern should be $2 \ln (1/\tau^{1/2})$. The asymmetric array-pattern repetition period is $2 \ln (1/\tau)$ (see the subsection "General Characteristics"). These implications have been confirmed through calculations using the method-of-moments NEC-81 program. A change in frequency of τ , for example, changed the radiated-pattern phase by 360°, and a change in frequency of $\tau^{1/2}$ changed the phase by 180°.

Additional phase shift is provided by capacitive loading from the parasitic elements located at the center of each folded element. However, as described in earlier paragraphs, the parasitic-element dimensions are not critical, so the dominant phase-delay mechanisms are the phase reversal from the folded or meander-line configuration plus the phase delay through the meander line. The parasitic elements are spaced by the factor of τ (not $\tau^{1/2}$), so precise analogies to the asymmetric arrays are not possible.

A study using the computer model also was undertaken to determine the significance of ϵ equal to $\tau^{1/2}$. The results of this study, although not exhaustive, indicate that a value of $\epsilon = \tau^{1/2}$ is optimal because directivity and pattern shape degrade gradually as ϵ approaches 1.

These arrays have demonstrated unusually versatile performance characteristics which, along with their printed-circuit simplicity and fabrication ease, make them good candidates for a number of applications. Conformally mounted airborne installations and direction-finding systems requiring amplitude and phase information are good examples. Folded-slot arrays have been designed successfully to cover broad frequency bandwidths such as 2 to 20 GHz and are easily integrated into one-dimensional curvatures, such as aircraft leading and trailing edges. Similar bandwidths have been obtained with the folded-

monopole arrays for nonconformal applications where relatively high gain and low fabrication costs were required.

Special Considerations

Initial investigation of LP antennas over extreme bandwidths is greatly simplified because it is necessary only to establish that there is little end effect and then to determine performance over several periods of frequency. If there is little end effect, the impedance and pattern will be log-periodic. It is advisable to use swept frequency in order to detect anomalies, as discussed below. It is also advisable that the structure have two active regions $(\lambda/2)$ and $(\lambda/2)$ widths) so that end effects will show up in the radiation pattern.

For wire LP antennas, method-of-moments computer programs^{10,48} may be employed to calculate performance (patterns, polarization, gain, impedance, and current distribution) with good accuracy and great economy compared with experimental techniques. For more complex structures such as sheet and slot elements, experimental techniques are used.

Theoretical and experimental studies of the periodic counterparts of LP structures that involve the determination of the Brillouin $(k - \beta)$ diagram have led to considerable insight regarding operation of the antennas, ^{49,50} especially the determination of unsuccessful structures. However, the technique gives little insight into the variation of performance of an LP antenna with the α angle.

Balmain and Bantin^{51,52} performed an extensive swept-frequency study of compressed LP antennas showing the variation of patterns and gain with α and λ . For a feeder impedance of 100 Ω , which is normally used for 50- Ω antennas, anomalies consisting of very-narrow-band drops in gain were detected for τ less than a certain value that increased with α . This was caused by end effect due to decreased attenuation through the active region. Balmain and Bantin later determined that the anomalies could be greatly reduced by increasing the feeder impedance.

Asymmetries ⁵³ in LP elements due to construction errors and/or mutual coupling to adjacent elements can cause serious degradation of patterns and gain over very narrow bands. Again, swept-frequency techniques should be used to determine that this type of anomaly does not occur. A serious problem occurs with *E*-plane arrays. Because of mutual coupling, the impedance of the monopoles on one side of the feeder is affected differently from that of those on the other side. For an LP dipole element, it is believed that this sets up ++ currents on the feeder that radiate broadside to the feeder. However, the same dropout occurs with monopole elements. The best solution is to increase the angle between elements in the array. The same phenomenon occurs in pyramidal arrays.

Arrays of Log-Periodic Elements

The pattern of an array of LP elements may be considered as the simple superposition of the patterns of the individual elements if it is assumed that the presence of other elements does not affect the pattern of an element.⁵⁴ To obtain frequency-independent operation with an array, it is necessary that the locations of the elements with respect to each other be defined by angles rather than by distances. This implies that all the elements have their vertices or feed points at a common point.

LP arrays are unique in two respects. First, although the element patterns are identical in shape (if it is assumed that design parameters are identical), they point in different directions. Second, since the radiation from an element may be considered to emanate

from the phase center, the array sources lie on the surface of a sphere for a twodimensional array and on a circle for a one-dimensional array. Thus the array theory is more complex and much less amenable to synthesis procedures than that for linear arrays of isotropic elements.

Element Characteristics Figure 14-33 shows the variation of the E- and H-plane beamwidths of a single-wire trapezoidal-tooth element as a function of 2a. For a given angle α , there is a minimum value of the design ratio τ that can be used. For values of τ smaller than this minimum, the pattern breaks up considerably, and for larger values, the beamwidths will decrease. The approximate minimum value of τ that can be used is plotted in Fig. 14-33 (solid curve) as a function of the parameter 2α . The E- and H-plane beamwidths for this minimum value of τ are also shown as solid lines. The dashed curves for the E- and H-plane beamwidths correspond to the dashed curve for τ , which is somewhat larger than the minimum value. It is noticed that the E-plane and especially the H-plane beamwidths decrease as α is decreased and τ is increased. For a given lower-frequency limit, which implies that the last transverse-element length remains fixed, decreasing α and increasing τ mean that the length of the structure and the number of transverse elements, respectively, are increased. The pattern behavior for the other types of elements is similar to that shown in Fig. 14-33.

The phase center of an LP element does not lie at the vertex; rather, it lies some distance d behind the vertex. Figure 14-42 shows the distance of the phase center from the vertices d as a function of 2α for wire trapezoidal-tooth structures. For a fixed structure, the distance as measured in wavelengths is essentially independent of frequency. For values of 2α less than 60° and for values of τ above the minimum value of τ given in Fig. 14-33, the position of the phase center is essentially independent of τ . Measurements⁵⁵ indicate that d depends on τ in a complex manner for 2α greater than 60°. The phase center lies on the centerline of the half structure at a point near where a half-wave transverse element exists.

Two-Element Arrays Both the E- and H-plane arrays may be considered as arrays of two elements with the element patterns pointing in different directions. The pattern can be calculated easily once the element pattern and distance from the vertex to the phase center are known. A schematic representation of a two-element array is given in Fig. 14-43. The radial lines separated by the angle ψ represent the two elements, and d is the

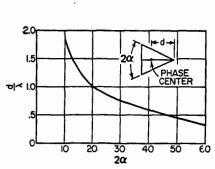


FIG. 14-42 Distance from vertex to phase center as a function of 2α .

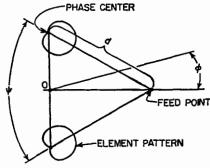


FIG. 14-43 Schematic representation of a two-element array.

distance to the phase center. The direction to a distant field point is given by ϕ . Typical element patterns are shown in the schematic. The pattern of the array is given by

$$E = \cos^{n}\left(\frac{\phi}{2} + \frac{\psi}{2}\right) \exp\left(j\beta d \sin\frac{\psi}{2}\sin\phi\right) + \cos^{n}\left(\frac{\phi}{2} - \frac{\psi}{2}\right) \exp\left(-j\beta d \sin\frac{\psi}{2}\sin\phi\right)$$
(14-28)

where $\cos^n(\phi/2)$ is an assumed functional form for the element pattern. The exponent n is related to the half-power beamwidth BW by

$$n = -0.35 / \ln \left(\cos \frac{\text{BW}}{2} \right) \tag{14-29}$$

For an *H*-plane array (like Fig. 14-30) the *H*-plane beamwidth is used and for an *E*-plane array the *E*-plane beamwidth is used to determine *n*. The beamwidths may be obtained from Fig. 14-33. Although this procedure neglects the effect of the presence of one half structure on the pattern of the other, it will give fairly accurate results, especially for values of α smaller than 60°. Figure 14-44 shows the variation of the *H*-plane beamwidth, gain, and front-to-back ratio with the angle ψ for a wire trapezoidal-tooth *H*-plane array with $2\alpha = 60^{\circ}$ and $\tau = 0.77$. The *E*-plane beamwidth is nearly independent of the angle ψ , and its value is approximately 63°. Of course, for $\psi = 180^{\circ}$, a bidirectional beam is produced. Notice that if both high gain and high front-to-back ratio are desired, a compromise value of ψ must be chosen. As is to be expected, the *H*-plane beamwidth decreases rapidly with increasing ψ because this increases the *H*-plane aperture of the antenna.

The characteristic impedance increases as the angle between the two elements increases; it will be in the range of about 100 to 300 Ω and also will depend on the type of element. Thus it may be necessary to use broadband transformers to match to the transmission-line feed.

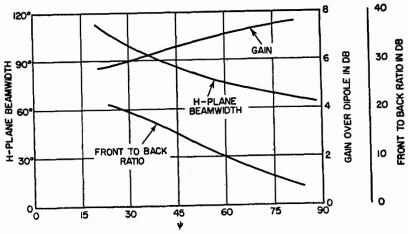


FIG. 14-44 Effect of angle ψ on pattern characteristics for an antenna with $2\alpha=60^{\circ}$ and $\tau=0.77$.

Multielement Arrays A schematic representation of an array of N elements as viewed from the top is illustrated in Fig. 14-45. The radial lines defined by δ_n represent the elements of the array. The α and τ parameters for the N elements are made identical so as to ensure identical element patterns. The xy-plane radiation pattern of the array is given by

$$E(\phi) = \sum_{n=1}^{N} A_n f(\phi - \delta_n) \exp\left\{-j[\beta d \cos(\phi - \delta_n) - \gamma_n]\right\}$$
 (14-30)

where $f(\phi)$ is the element pattern and $\beta d \cos (\phi - \delta_n)$ represents the phase advance of the phase center relative to the origin. The function f may take the same form as that used previously, that is, $f(\phi) = \cos^n(\phi/2)$. The value of the feed-point current for the nth element is given by A_n . In nearly all practical cases, $A_n = 1$ for all n. This is accomplished in practice by connecting half the elements together and feeding them against the other half. The parameter γ_n is the relative phase of the field radiated from the nth element. It may be controlled by expanding or contracting the element according to the phase-rotation principle to be described later.

The assumptions made in Eq. (14-28) are that the element patterns and input impedances are identical. Although mutual effects can make these assumptions invalid, good correlation between theory and experiment has been obtained. Cut-and-try synthesis procedures may be used with Eq. (14-30).

A basic characteristic of LP antennas is the phase-rotation phenomenon. It has been verified experimentally that if the phase of the electric field received at a distant dipole (Fig. 14-46) is measured relative to the phase of the current at the feed point of the structure, the phase of the received signal will be delayed by 180° as the structure is expanded through a period. In Fig. 14-46, the distance to an arbitrary transverse element is given by KR_n . The expansion of the structure through a period is accomplished by letting K increase from 1 to $1/\tau$. During this expansion, all lengths involved in the structure are multiplied by K. In Fig. 14-46, the phase delay in radians is plotted versus K on a logarithmic scale. The ideal phase variation is given by the solid straight line. Measurements have indicated that the actual phase variation is somewhat like the dashed line. The approximate measurements made to date indicate that the deviation of the dashed line from the

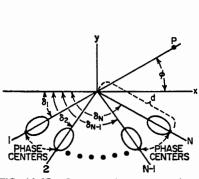


FIG. 14-45 Geometry for an array of endfire elements.

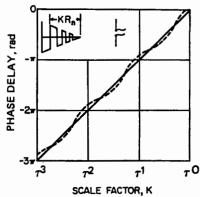


FIG. 14-46 Illustration of the phase-rotation phenomenon for log-periodic antennas.

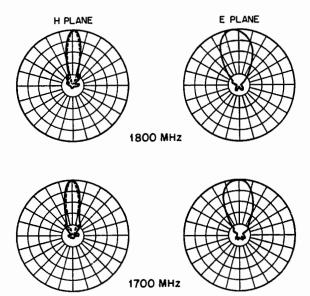


FIG. 14-47 Predicted (---) and measured (----) patterns of a six-element phased array.

straight line is not more than 15°. The relation between the phase γ_n and K_n is given by

$$K_{\mu} = \tau^{\gamma n/\pi} \tag{14-31}$$

Fortunately, the phase center and the element patterns are independent of the expansion or contraction of a logarithmically periodic element.

This phase rotation appears not only in the radiation field but also in the reflected wave on the feeder for LP antennas and LP transmission-line circuits. It produces dispersion of transmitted or received signals, and the dispersion increases as τ approaches unity.

The information given in Figs. 14-33, 14-42, and 14-46 is sufficient for predicting the pattern of an array of similar end-fire elements. The method can be extended to cover a combination of *E*- and *H*-plane arrays. The phase-rotation phenomenon is extremely important because it allows a frequency-independent method of phasing the elements of the array.

Experimental and theoretical patterns for a six-element phased H-plane array of wire trapezoidal-tooth elements are given in Fig. 14-47. The values of the design parameters for this array were $\alpha = 19^{\circ}$, $\tau = 0.94$, N = 6, $\delta_n - \delta_{n-1} \approx 17^{\circ}$ for all n, and $d/\lambda = 1.95$. The elements were phased to produce a beam-cophasal condition. The gain of the array was 14 dB over a dipole.

Although gains of up to 18 dB are feasible by using a combined E- and H-plane array, the size and complexity of the antenna become great because it is necessary to use very small α angles and τ values near unity.

An approximate design procedure for arrays is given in Ref. 54.

Arrays Over Ground Although the antennas discussed above have radiation patterns that are essentially independent of frequency, many applications demand that the anten-

nas be placed near ground. If one of these antennas is placed with its feed point above ground, it is apparent that the resulting pattern will be frequency-dependent because its electrical height above ground changes with frequency. However, the preceding array theory suggests that if LP elements are inclined with respect to ground and their feed points are at ground level, the resulting radiation pattern will be frequency-independent. The elements can be placed so that with their images they form either H- or E-plane arrays or a combined E- and H-plane array. For an equivalent H-plane array, there will, of course, be a null in the resulting pattern on the horizon. The array theory may be used to calculate the resulting pattern by adjusting the phase of the image elements. For an H-plane array the phase of the image element will be 180° different from that of the element above ground, whereas for an E-plane array the phase of the image element will be the same as that of the element.

A very important application for this type of antenna is in point-to-point communication circuits. 55 Figure 14-48 shows a two-element array above ground oriented so that these elements and their image elements form an H-plane array. Theoretically, the feed point of the antenna should be at ground level, but in practice the feed point is placed a small height above ground to protect personnel from high radiofrequency voltages. Except for very short distances, high-frequency point-to-point communication is accomplished by the reflection of the radio waves from the ionosphere. The vertical angle of arrival or departure (from the ground) depends on the distance between the points and the height of the reflecting layer. Although its value ranges from 70° down to a few degrees for various circuits, the value for a particular circuit is relatively constant because the height of the reflecting layer does not change by a great amount. However, because of changing ionospheric conditions during the sunspot cycle and from night to day, it is necessary to change the operating frequency over bandwidths of 4 or 6:1. Thus it is most desirable to have an antenna for which the vertical angle of the main lobe is independent of frequency. Some antennas, such as the dipole, rhombic, billboard, and discone, do not satisfy this requirement.

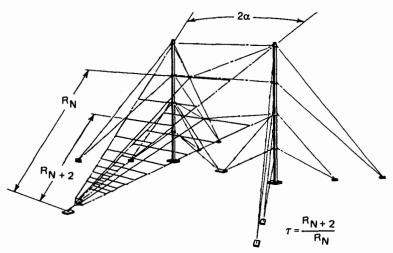


FIG. 14-48 Log-periodic high-frequency antenna with a frequency-independent elevation pattern.



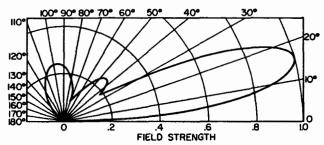


FIG. 14-49 Elevation pattern and design parameters for the typical antenna of Fig. 14-48.

The direction of the main lobe for the structure of Fig. 14-48 may be controlled by the α angle of the individual element and the angles of the elements with respect to ground. The size of the structure is determined by the lower frequency limit. Figure 14-49 shows the vertical-plane pattern for a structure with $2\alpha = 14^{\circ}$ and $\tau = 0.75$. The two half structures are oriented at angles of 32 and 48° with respect to ground. The dimensions of the antenna at the lowest frequency are given in wavelengths in the figure. The lower half structure is scaled so that its radiation leads that of the upper by 130°. This particular phasing increases the gain by 5 dB over that obtained with no difference in phasing. Although the gain for this type of antenna is only moderate (13.4 dB over a dipole), maximum use of this gain is made over the complete frequency range. The gain for this structure can be increased by 3 dB by adding two additional elements to the side to form a combined E- and H-plane array.

If vertical polarization is required rather than horizontal polarization (which is obtained for the structure above), then the two-element array can be rotated 90° about its centerline so that the plane of each of the half structures would be normal to the ground plane.

Dual-Polarized Sinuous Antennas

Many applications such as direction-finding systems or reflector feeds require a broadband antenna element that provides orthogonal senses of polarization. Simultaneous polarization capability such as vertical and horizontal or right and left circular from a common aperture with coincident phase centers is of particular interest. In the past, this requirement has been met with varying degrees of success by using elements such as crossed LP arrays of dipoles or by carefully configured and fed spiral antennas. These solutions often failed, though, because they were either too large, their phase centers moved with frequency, their E- and H-plane radiation pattern beamwidths were not the same, or their radiation characteristics were not frequency-independent.

In 1982, DuHamel⁵⁷ conceived an element called the sinuous antenna that addresses

many of these deficiencies. The sinuous concept evolved from the idea that a current distribution, circumferential in nature, could help to solve the E/H-plane pattern-uniformity problem, an interleaved structure could lead to a small frequency-independent antenna, and a self-complementary structure would lead to a frequency-independent input impedance. A multiple-arc structure with asymmetric arms is required in order to incorporate these ideas. The result is an antenna that is similar in size to the spiral element, has a beamwidth and gain approximately the same as the spiral, but provides two orthogonal senses of polarization.

The curve of Fig. 14-50 shows the basic shape of a sinuous curve which, with a rotation, may be used to define an arm of a sinuous antenna. Consistent with good LP practice, the sinuous curve is defined entirely by angles and an expansion ratio τ . As described in Fig. 14-50, the curve is a series of cells starting with cell 1 at the outer radius R_1 . R_p defines the outer radius of cell p, and α_p with τ_p define the angular width and ratio of the inside-to-outside radius for each cell. The equation for the pth cell is given by

$$\phi = (-1)^{p} \alpha_{p} \sin \left[\frac{180 \ln (r/R_{p})}{\ln \tau_{p}} \right] \qquad R_{p+1} \le r \le R_{p}$$
 (14-32)

where r and ϕ are the polar coordinates of the curve.

The radii R_p are related by

$$R_{p} = \tau_{p-1} R_{p-1} \tag{14-33}$$

The design parameters τ_p and α_p may be independent of p to form an LP structure that is a

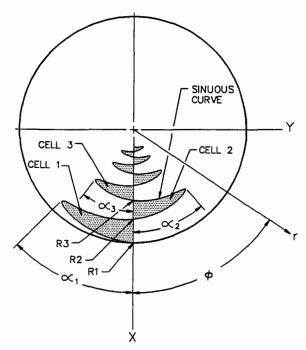


FIG. 14-50 Basic sinuous curve.

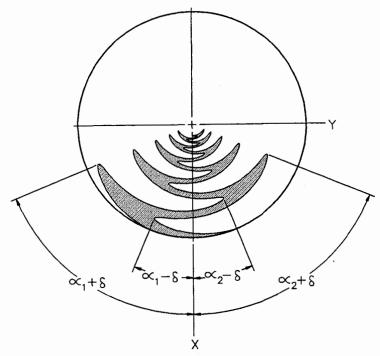


FIG. 14-51 One sinuous arm.

periodic function of the logarithm of the radius r. The parameters also may be dependent on p to form a quasi-LP or tapered-LP structure. The tapered structure has the potential of developing frequency-dependent characteristics such as pattern beamwidth and gain.

One sinuous arm is formed by rotating the curve of Eq. (14-32) by plus and minus an angle δ around the origin, as shown in Fig. 14-51. A complete aperture is developed by the angular rotation of the single arm through 360/N degree increments to form an N-arm structure, where N is greater than 1. The four-arm structures are used to develop dual-linear or dual-circular polarized apertures. Multimode, dual-polarized structures may be developed by using five or more arms, as explained in later paragraphs.

The more common four-arm structure is shown in Fig. 14-52. To form orthogonally polarized beams from this aperture, opposite arms are fed 180° out of phase at the central portion of the arms as shown. The result is two rotationally symmetric bidirectional beams, linearly polarized with respect to each pair of arms, as shown in Fig. 14-52. The two beams have their peaks in the same direction along the perpendicular to the plane of the aperture. Unidirectional beams can be developed by using an absorber-loaded cavity on one side of the aperture to absorb the radiation in that direction. The two senses of circular polarization can be developed by combining the two linearly polarized beams in plus and minus 90° phase rotation using a 3-dB 90° hybrid. The circuits used with the four-arm aperture for dual-linear and dual-circular polarization are shown in Fig. 14-53.

Design Considerations Even though the sinuous structure conforms to well-known LP design principles and the radiation characteristics are not particularly sensitive to any

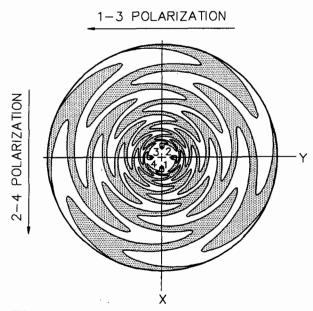


FIG. 14-52 Four-arm sinuous aperture.

one design parameter, there are limits to the values of the design parameters that ensure good performance. It is felt that the amount of interleaving between arms or the angle $\alpha + \delta$ in Fig. 14-51 should be adjusted so that $\alpha + \delta < 70^\circ$ to ensure good efficiency and gain performance without dropouts over the frequency band. It is believed that the angle δ is important in providing the capacitance necessary to tune out the sharp inductive corners of the sinuous shape. The self-complementary aperture obtained with angles $\alpha = 45^\circ$ and $\delta = 22.5^\circ$ shown in Fig. 14-52, for example, has demonstrated consistent performance in gain and pattern characteristics.

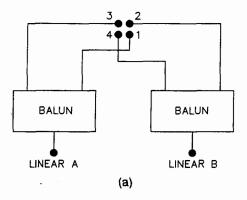
The active region of radiation for the sinuous antenna is at the radius where the product of the circumferential arm width defined by the angle $2(\alpha_p + \delta)$ and the radius r is approximately one-half wavelength. That is,

$$2r\left(\alpha_{p}+\delta\right)\approx\frac{\lambda}{2}\tag{14-34}$$

where the angles are expressed in radians. The lowest frequency is therefore limited by the antenna outer radius R_1 , or $\lambda_L = 4R_1(\alpha_1 + \delta)$. Performance drops off quickly, especially in directivity, as the frequency is lowered below that which R_1 can support. The high-frequency limit is typically bounded by the feed-point design. For good performance at the high-frequency limit, the smallest segment should be somewhat smaller than $\lambda_H/4$ to provide a good transition from the feed-point area to the active region. A good compromise is to use

$$2R_p(\alpha_p + \delta) = \frac{\lambda_H}{4}$$
 (14-35)

The overall bandwidth may be increased by increasing R_1 and/or decreasing R_p . Dual



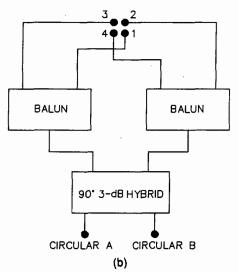


FIG. 14-53 Linear-polarization (a) and circularpolarization (b) feed networks for four-arm sinuous antennas.

circularly polarized bandwidths as high as 14:1 have been obtained, with the limitation for larger bandwidths being the feed circuitry, especially the 90° hybrid, and not the aperture.

Impedance A self-complementary sinuous structure has an impedance that is essentially real and independent of frequency within the frequency band of operation. This fact assumes that the aperture is an efficient radiator and therefore that end effects are negligible. The condition for an N-arm sinuous antenna to be self-complementary is given by

$$\delta = \frac{180}{2N} \tag{14-36}$$

Deschamps⁵⁸ has shown that when a rotationally symmetric structure such as the self-complementary sinuous antenna is fed in mode M (or -M), the impedance of each arm to ground is given by Eq. (14-23).

A self-complementary four-arm aperture fed in mode 1 with a balanced feed system will, according to Eq. (14-23), have an arm impedance of 133 Ω . Because of practical design considerations, feed methods, the loading due to surrounding dielectrics, and an absorptive cavity, the value will be somewhat lower. Also, increasing or decreasing δ from 22.5° decreases or increases the gap between the arms and therefore decreases or increases the arm impedance, respectively. Practical implementations of a complementary sinuous structure using 140- Ω balanced feed lines have resulted in VSWR values on the average of 1.7:1.

Radiation Patterns and Polarization The measured patterns for the self-complementary structure, as shown in Fig. 14-52 with $\alpha=45^{\circ}$, are similar to those measured on the spiral antenna. The 3-dB beamwidth within the operating band is typically 75° for both the principal E and H planes when α is approximately 45°. It is believed that the radiation-pattern beamwidth can be varied by adjusting the radius of the active region defined in Eq. (14-34). This is accomplished by varying the angle α . Since the beamwidth BW is inversely proportional to the active-region radius, the following relationship should hold:

$$BW \approx \frac{1}{\alpha_p + \delta}$$
 (14-37)

For a linearly polarized sinuous antenna, the radiated pattern polarization is aligned with the arms, as illustrated in Fig. 14-52. On the four-arm structure shown, the angle between the two linearly polarized beams has been measured to be 90° independent of frequency. However, measurements and calculations have shown that the vector orientation of the two polarizations wobbles with frequency plus and minus approximately 4° about a nominal orientation. It appears that the asymmetry of the arms causes the polarization wobble.

Circularly polarized sinuous antennas exhibit similar performance to linear versions. For designs fed with well-designed 90° hybrids, measured axial ratios less than 2 dB out to 75° from the beam peak are common. The excellent E- and H-plane pattern-shape uniformity out to these extreme angles accounts for the good axial-ratio performance. Good radiation attenuation in the antenna active region is confirmed by near-circular (mode-free), conical-cut patterns. By contrast, the typical spiral antenna does not radiate as efficiently in the active region, and therefore, it is possible that some energy is radiated in the next-higher 3λ mode region. The 3λ pattern, which is a difference pattern, adds and subtracts from the first-mode sum pattern because of its relative phase. The result is elliptically shaped conical-cut patterns with an amplitude WOW as high as 8 dB (see the subsection "Modal Characteristics of Multiarm Spiral Antennas" for an in-depth discussion of higher-order modes in spiral antennas). The WOW for the sinuous antenna is typically 2 dB or less. The improved pattern performance of the sinuous antenna over the spiral antenna allows for improved direction-finding performance out to extreme angles, independent of polarization and frequency.

Cavity Design In contrast to the cavity-backed spiral antenna, reflections from the cavity on a sinuous aperture produce variations of the power split between the cavity and

free space and, therefore, variations in the gain rather than the degradation of the axial ratio and variations of the WOW (see the subsection "Planar Spiral Antennas"). The reflections from the cavity are mostly coupled back to the inside feed terminals rather than to the outside terminations. Thus the impedance looking into the cavity seen by each sinuous arm is similar to a lossy-shorted transmission line. The impedance locus is a quasi-circle located about the characteristic impedance of the absorbing material in the cavity. Thus the power split to free space is maximum and minimum when the cavity impedance is maximum and minimum, respectively. Periodic variations of gain of ± 1.5 dB versus frequency may occur if the attenuation through the cavity is small. The two-way attenuation through the cavity should be about 16 dB at the lowest frequency.

Feed Circuit Sinuous antennas have been developed using a variety of circuit elements. Figure 14-53 shows the preferred arrangements for both linear and circularly polarized applications. For the balun, tapered-stripline, Phelan, ⁵⁹ and Marchand ¹⁸ circuits are all good candidates. Impedance matching and frequency requirements, combined with the antenna size limitations, are the primary considerations for this decision. For circular polarization, the typical 90° hybrid implementation has been a cascade of two 8.34-dB quadrature hybrids.

Four-Arm Implementations A common application for the sinuous antenna is a replacement for the single-sense polarization spiral in direction-finding systems that operate over a 2- to 18-GHz frequency range. A 2-in-diameter version of a dual circularly polarized element that covers this band is shown in Fig. 14-54. For this antenna, the sinuous aperture is self-complementary with $\alpha=45^\circ$. It is fed with two tapered-stripline baluns which are in turn fed by a cascaded 90° hybrid to simultaneously form left and right circularly polarized beams. The antenna radiates unidirectionally because of the absorber-loaded cavity. The loaded cavity reduces the gain of the antenna by approximately 3 dB because one-half the total radiated energy is absorbed.

The measured maximum VSWR of the antenna is less than 1.6:1 for either port over the 2- to 18-GHz band. A radiation pattern measured at 10 GHz with a rotating linear horn illuminator is shown in Fig. 14-55a and is typical of the shape and axial-ratio performance measured from 5 to 18 GHz. Below 5 GHz the beam gradually widens to a beamwidth of approximately 95° at 2 GHz owing to the electrically small aperture at these lower frequencies. The gain varies between -1 and 1 dB with respect to a linear isotrope over the 5- to 18-GHz band and drops to -6 dB at 2 GHz. Axial ratios at the beam peak and beam squint are less than 1 dB and \pm 3°, respectively, over the entire 2- to 18-GHz band. A conical-cut pattern, taken at 10 GHz at 60° off boresight with rotating linear, is shown in Fig. 14-55b and illustrates the controlled, mode-free performance available from the sinuous aperture.

Performance of a 2-in-diameter dual linearly polarized antenna is similar to the circularly polarized 2-in-diameter antenna of Fig. 14-54. Measured gain varies between 2 and 4 dB with respect to a linear isotrope. The increase in gain over the dual circularly polarized antenna is due to reduced losses without the 90° hybrid and the gain referenced to matched polarization.

Uses of the sinuous antenna include direction finders (both amplitude-type and phase interferometers), polarimeters (dual linear), feeds for reflectors, and feeds for compact ranges. For many applications, the sinuous antenna has allowed for performance and capabilities not previously available. Some applications, however, may require higher

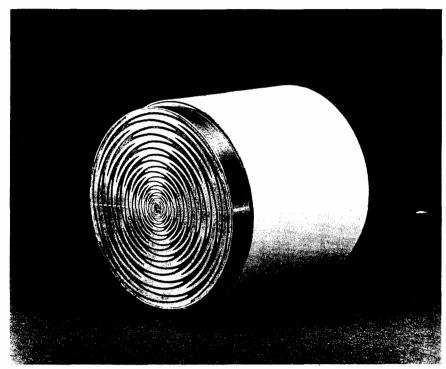


FIG. 14-54 A 2-in-diameter sinuous antenna, $\tau = 0.75$, $\alpha = 45^{\circ}$, and $\delta = 22.5^{\circ}$. (Courtesy Loral Randtron Systems.)

gain, or the planar shape of the above-described sinuous antenna may not match the requirement. For these applications, the four sinuous arms can be placed on a pyramidal or conical structure to develop a natural unidirectional beam similar to that of the conical spiral. The increased gain is available because the absorber cavity is no longer needed to absorb one of two beams—an improvement of 3 dB. Figure 14-56 shows a six-arm conical sinuous antenna. The beam, which radiates in the direction of the cone structure tip and feed point, can be adjusted by changes in the cone angle σ and τ . A smaller σ (<30°), for example, produces a front-to-back ratio greater than 10 dB. As σ is increased toward 90°, a planar structure, the backlobe increases and the absorber-loaded cavity is needed to obtain unidirectional patterns. The active region for the conical structure occurs when

$$r(\alpha_p + \delta) \sin \theta_0 \approx \frac{\lambda}{4}$$
 (14-38)

in a manner similar to the planar structures.

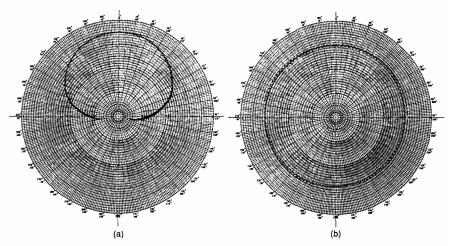


FIG. 14-55 (a) Principal-plane pattern of a 2-in-diameter sinuous antenna at 10 GHz. (b) 60° conical-cut pattern of a 2-in-diameter sinuous antenna at 10 GHz.

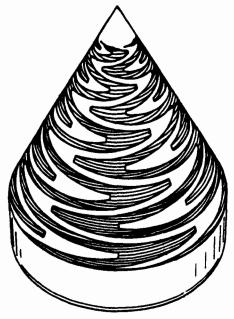


FIG. 14-56 Six-arm conical sinuous antenna.

Multimode Implementations In general, sinuous antennas may consist of N arms lying on the surface of a plane, cone, or pyramid with a rotational symmetry such that a rotation of 360/N degrees around the antenna central axis leaves the structure unchanged. The antenna may be excited in one or more normal modes to produce a variety of useful patterns. The voltage excitations for a normal mode are given by

$$V_{n,m} = A_m \exp(j360mn/N)$$
 (14-39)

where $n = 1, 2, \ldots, N$ is the arm number, $m = \pm 1, \pm 2, \ldots$ is the mode number, and A_m is the excitation amplitude of mode m and may be complex. All modal patterns are rotationally symmetric and have a null on the axis of rotation except for modes M_1 and M_{-1} . N must be greater than 2 in order to provide two patterns with orthogonal polarizations.

N must be greater than 4 to provide two rotationally symmetric difference patterns with orthogonal senses of polarization. Modes M_1 and M_2 are used to provide monopulse-type direction finding for one sense of circular polarization, and modes M_{-1} and M_{-2} are used for the other sense of circular polarization. Orthogonal senses of linear polarization may be developed by the mode combinations of $M_2 + M_{-2}$ and $M_2 - M_{-2}$ for the difference patterns and $M_1 + M_{-1}$ and $M_1 - M_{-1}$ for the sum patterns.

For direction finding and homing systems, it is often desirable to have an antenna with four orthogonal tilted beams. This can be achieved by combinations of sum and difference modes. For one sense of circular polarization, mode combinations $M_1 + M_2$, $M_1 - M_2$, $M_1 + jM_2$, and $M_1 - jM_2$ are used to provide four orthogonal tilted beams. The other sense of circular polarization is obtained by changing the signs of the preceding mode numbers. A 3-dB loss in the feed network is incurred because eight beams are formed from only four normal modes.

The feed network for a multimode sinuous antenna can be quite complex compared with the feed network of a multimode spiral antenna. This is due, of course, to implementation of the second sense of polarization. For example, the feed network for a six-arm sinuous antenna that develops sum and difference patterns of two orthogonal polarizations, that is, M_1 , M_{-1} , M_2 , and M_{-2} , is shown in Fig. 14-57. More complex networks are needed to form tilted-beam antennas. Additional descriptions of modal variations and possibilities are given in DuHamel's patent.⁵⁷

It would be quite desirable to develop zero-boresight-error networks for these sinuous antennas in a manner similar to that described by Corzine and Mosko⁵ for the four-arm spirals.

Circularly Polarized Structures

Circular polarization may be obtained by using crossed LP dipole arrays. Figure 14-58 is a front view of a practical configuration. Feeders 1 and 2 are used to excite the vertical and horizontal dipoles, respectively. The solid lines represent the dipoles in one cell and the dashed lines the dipoles in the next cell. It is desirable to make the spacing between the feeder lines as small as practicable in order to simulate planar arrays. If the two crossed arrays are identical, it is necessary to excite the two feeders with a broadband 90° phase-difference circuit or a broadband quadrature hybrid. In the latter case, both left- and right-circular polarizations are obtained simultaneously. Alternatively, one dipole array may be scaled by $\tau^{1/2}$ with respect to the other, producing a 90° phase shift of the radiated field. The two feeders may be fed in or out of phase for one sense of circular polarization or by a broadband 0 to 180° hybrid for both senses of circular polarization.

Another approach is to use two crossed-dipole arrays, one scaled by $\tau^{1/2}$, and excite

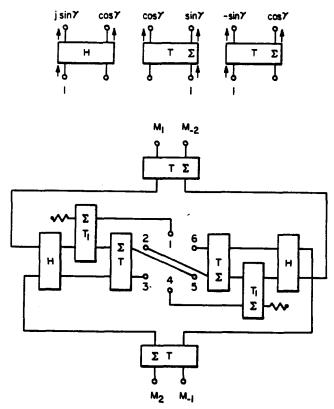


FIG. 14-57 Six-arm sinuous feed structure.

them by a single feeder, as illustrated in Fig. 14-59. It is quite surprising that this gives the 90° phasing between the two arrays. Of course, only one sense of circular polarization may be obtained.

Since the H-plane beamwidth is usually about 50 percent greater than the E-plane beamwidth, the axial ratio is low only for directions close to the axis of the array. To obtain low axial ratios over wide angles, a traveling-wave ring-type radiator is desired rather than crossed dipoles. Another approach is to use four LP elements placed on the sides of a pyramid. Because of the asymmetric-coupling problems between adjacent elements, the shunt-loaded LP

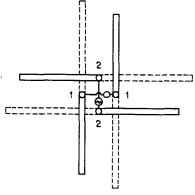


Fig. 14-58 Feeder configuration for crossed log-periodic dipole antennas.

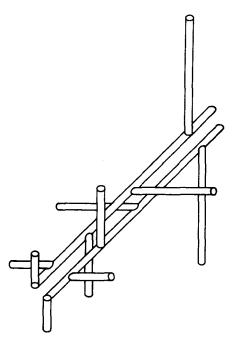


FIG. 14-59 View of circularly polarized crossed LP dipole arrays with a single feeder.

elements of Fig. 14-35 do not work unless the spacing between the tips of adjacent elements is large. In this case the ψ angle is large, and, in turn, the back radiation is large. The traveling-wave structures of Fig. 14-36 may be used because they are much less susceptible to the asymmetric coupling. However, these structures are limited to small angles, which leads to a long antenna. Some LP monopulse antennas have been used as feeds for reflectors. They consist of a circular array of six or eight elements of the type

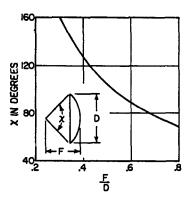


FIG. 14-60 Angle subtended by a parabolic reflector as a function of f/d.

shown in Fig. 14-36 placed on the surface of a metal cone and excited in modes 1 and $2 (\Sigma \text{ and } \Delta \text{ patterns})$ by a broadband hybrid-feed network. Again, the axial ratio is poor off boresight because of the large difference in beamwidths of the E_{θ} and E_{ϕ} polarizations.

Feeds for Reflectors and Lenses⁶¹

Many applications call for high-gain antennas that will work over extremely wide frequency ranges. Although lens- or reflector-type antennas are ideally suited, their bandwidths have been limited in the past by that of the primary feed, Ideally, the radiation

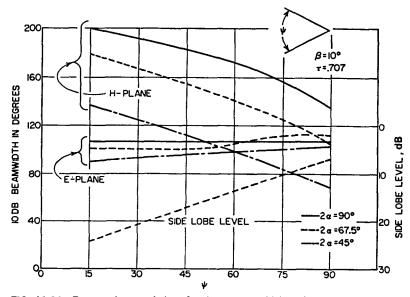


FIG. 14-61 Pattern characteristics of a sheet trapezoidal-tooth structure.

pattern and input impedance of the primary radiator should be independent of frequency; thus unidirectional LP or equiangular antennas are well suited for this application. The required design information for LP feeds is the primary pattern, phase center, and input impedance.

Figure 14-60 shows the angle subtended by a circular-parabolic reflector as observed from the focal point as a function of the f/d ratio. Figure 14-61 shows the variation of the E- and H-plane 10-dB beamwidths and the sidelobe level as a function of ψ for several different values of α for two-element sheet trapezoidal-tooth structures. The largest sidelobe nearly always occurs in the opposite direction of the beam. If a 10-dB taper is desired, it is seen that a two-element structure can be designed so as to give fairly good illumination tapers for f/d ratios from about 0.35 to 0.6.

The planar sinuous antenna is also an excellent candidate for reflector and lens applications. It possesses a constant beamwidth in the E and H planes and is especially suitable owing to its frequency-independent phase center. Reflector f/d ratios between 0.3 and 0.5 can effectively be illuminated by the sinuous antenna element in either a dual linear or a dual circularly polarized mode. See the subsection "Dual-Polarized Sinuous Antennas" for an in-depth discussion of the sinuous antenna.

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Horn Antennas

Allan W. Love

Rockwell International

15-1	General 15-2
	Types and Uses 15-2
	Effect of Horn Flare 15-3
	Obliquity Factors 15-4
15-2	Dominant-Mode Rectangular
	Horns 15-5
	Sectoral Horns 15-5
	Pyramidal Horns 15-7
	Gain 15-8
	Optimum-Gain Horns 15-11
	Impedance 15-12
15-3	Dominant-Mode Conical Horns
	15-13
	Radiation Patterns 15-13
	Gain 15-15
	Optimum-Gain Horns 15-17
	Impedance 15-17
15-4	Multimode Horns 15-18
	General 15-18
	Diagonal Horn 15-18
	Dual-Mode Conical Horn 15-19
	Multimode Pyramidal Horns
	15-25
	Gain and Impedance 15-27
	•

```
15-5 Corrugated Horns 15-28
       Hybrid Modes 15-28
       Conical Corrugated Horn
         (Small-Flare-Angle) 15-34
        Wide-Flare-Angle Scalar Horn
         15-37
        Gain 15-39
        Impedance 15-40
        Wide-Band Feed Horn 15-42
        Compact, Profiled Corrugated
         Horns 15-42
        Two-Hybrid-Mode Horns 15-43
        Rectangular Corrugated Horn
         15-45
15-6 New Topics 15-45
        Soft and Hard Boundaries for
         Horns 15-45
```

Soft Horns with Dielectric Lining

Absorber-Lined Horns 15-48

Hard Horns 15-48 Soft Horns with Elliptical Apertures 15-51

15-47

Types and Uses

The horn antenna in general is a device which effects a transition between waves propagating in a transmission line, usually a waveguide, and waves propagating in an unbounded medium such as free space. They are constructed in a variety of shapes for the purpose of controlling one or more of the fundamental properties: gain, radiation pattern, and impedance. The types most often used with rectangular and round guides are shown in Figs. 15-1 and 15-2.

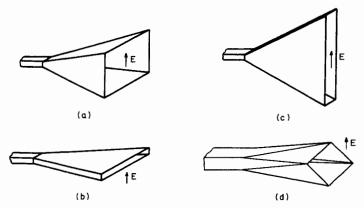


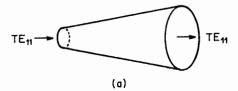
FIG. 15-1 Rectangular-waveguide horns. (a) Pyramidal. (b) Sectoral H-plane. (c) Sectoral E-plane. (d) Diagonal.

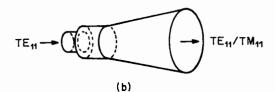
The pyramidal horn of Fig. 15-1a is most commonly used as a primary gain standard since its gain may be calculated to within 0.1 dB from its known dimensions. Independent control of the beamwidths in the two principal planes is possible by varying the rectangular-aperture dimensions.

The sectoral horns of Fig. 15-1b and c are special cases of the pyramidal horn, being flared in only one plane. They radiate fan-shaped beams, broad in the plane orthogonal to the flare. The diagonal horn of Fig. 15-1d is another special case in which the horn aperture is square but the electric field is essentially parallel to a diagonal. This horn radiates a pattern with a high degree of rotational symmetry but does suffer from a relatively high level of cross-polarization in the intercardinal planes.

The conical horn of Fig. 15-2a is, by virtue of its axial symmetry, capable of handling any polarization of the exciting dominant TE_{11} mode. It is particularly well suited for circular polarization. Despite its axial symmetry, however, the beamwidths in the principal planes are generally unequal. Like the pyramidal horn, the conical horn may be used as a primary standard since its gain is accurately calculable.

The dual-mode and corrugated (hybrid-mode) conical horns of Fig. 15-2b and c overcome the lack of axial symmetry in the radiation pattern and at the same time achieve suppression of cross-polar radiation in the intercardinal planes to a very low level. In the dual-mode horn, some of the exciting TE_{11} mode is converted to TM_{11} at





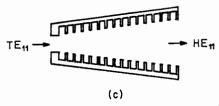


FIG. 15-2 Round-waveguide horns. (a) Conical. (b) Dual-mode conical. (c) Corrugated conical.

the step discontinuity in diameter. In the horn of Fig. 15-2c the corrugations force propagation in a hybrid mixture of TE_{11} and TM_{11} waves called the HE_{11} mode. In both cases the aperture field of the horn is modified in such a way as to produce axisymmetry in the radiation patterns.

A collection of important historical papers dealing with horn antennas will be found in Ref. 1.

Effect of Horn Flare

The radiation characteristics of horns with aperture dimensions greater than about one wavelength may be calculated with reasonable accuracy by using Huygens' principle along with the known aperture field in the horn mouth. For single dominant-mode horns, the aperture field is usually taken to be identical with the transverse electric field of that mode as it would exist in a cylindrical waveguide of the same cross section and size as the horn mouth. In a waveguide which flares to a horn, it is clear that the boundary conditions require the existence of higher-order nonevanescent modes in addition to the fundamental mode. It is customary to assume that the flare angle is small enough to permit the higher-mode field components to be neglected in comparison with those of the dominant mode.

Even when the flare angle is not particularly small, the above treatment gives surprisingly accurate results if the effect of the curvature of the dominant-mode wave-

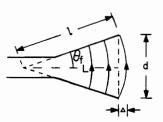


FIG. 15-3 Phase error due to wavefront curvature in the horn aperture.

front in the aperture is taken into account. In Fig. 15-3 the field lines are shown as though the dominant mode were expanding as a cylindrical wave (in a sectoral horn) or a spherical wave (in a conical horn) with a radius of curvature at the aperture equal to ℓ , the slant length of the horn. The path difference between this curved wavefront and an ideal plane wave in the aperture constitutes a phase error which requires that the planar fields of the dominant mode be

modified by the inclusion of a phase factor of approximately quadratic form, $\exp(jk\Delta x^2)$, where x is the normalized aperture coordinate. From the geometry it is easy to see that the total excursion of the path error is Δ , where

$$\Delta = \ell - L = \frac{1}{2} d \tan \frac{\theta_f}{2} = 2\ell \sin^2 \frac{\theta_f}{2}$$
 (15-1)

L and ℓ are the axial and slant lengths respectively, and θ_f is the semiflare angle.

The quadratic phase form implicitly assumes that the small-angle approximations may be applied to Eq. (15-1), giving the equivalent simplified expressions

$$\Delta = d^2/(8L)$$
 or $d^2/(8\ell)$ (15-2)

The ambiguity implied in Eq. (15-2) arises only in cases in which the quadratic phase approximation is indiscriminately applied when θ_f is not small. This can be a source of confusion and error. In this section the approximation $\Delta = d^2/(8\ell)$ will be used, ℓ being the slant length, unless otherwise noted.

The consequences of quadratic phase error are loss in gain accompanied by broadening of the radiation pattern, an increase in sidelobe levels, and obliteration of the nulls. In the rest of this section all pattern calculations are based on the above approximate model with quadratic-error correction applied as necessary.

Obliquity Factors

Radiation patterns of dominant (i.e., TE-mode) horns differ in the principal planes for two reasons. The basic transverse-field distributions and the associated obliquity factors differ in the two orthogonal directions. The obliquity factor is a pattern function multiplier which takes account of the effects of mode propagation constant and reflection at the horn aperture.

In the E plane the obliquity factor, denoted by F_{ϵ} , is given by²

$$F_{e} = \frac{1}{2} \left[1 + \frac{\lambda}{\lambda_{g}} \cos \theta + \Gamma \left(1 - \frac{\lambda}{\lambda_{g}} \cos \theta \right) \right]$$
 (15-3)

while in the H plane

$$F_h = \frac{1}{2} \left[\cos \theta + \frac{\lambda}{\lambda_g} + \Gamma \left(\cos \theta - \frac{\lambda}{\lambda_g} \right) \right]$$
 (15-4)

where λ_g is the wavelength appropriate to the guide dimension at the horn mouth and Γ is the reflection coefficient presented by the aperture discontinuity. θ is the usual far-field polar angle.

In small-aperture horns F_{ϵ} and F_h may be significantly different. Moreover, because Γ is generally an unknown complex number, they are not calculable, a fact which partially accounts for a notable lack of success in predicting the patterns of small horns.

For apertures larger than about 2λ the aperture discontinuity is small, so that $\Gamma \to 0$, while $\lambda/\lambda_g \to 1$. Under these circumstances F_e and F_h are nearly identical:

$$F_e \doteq F_h \doteq \frac{1}{2}(1 + \cos \theta) = \cos^2 \theta/2$$
 (15-5)

When the aperture is very large, the main beam is narrow and radiation is largely confined to small values of θ . For this reason $\cos \theta$ is often taken to be unity in Eq. (15-5), and the obliquity factors, both then unity, are suppressed altogether.

15-2 DOMINANT-MODE RECTANGULAR HORNS'

Sectoral Horns

The radiation patterns of sectoral horns may be calculated in the plane of the flare on the assumption that the horn is excited by the dominant TE_{10} mode in rectangular waveguide.² The results of such calculations are shown in Figs. 15-4 and 15-5 for E-and H-plane flares respectively. In each case there is a family of curves corresponding to various values of the cylindrical-wave error Δ due to the flare. The ordinate is the normalized far-zone electric field strength, and the abscissa is the reduced variable $b/\lambda \sin \theta$ or $a/\lambda \sin \theta$, where b and a are the dimensions of the horn mouth (b in the E plane, a in the H plane).

The effects of phase error due to the flare are seen in the various curves corresponding to the parameters s and t, which are normalized path errors in wavelengths,

$$s = \frac{\Delta_e}{\lambda} = \frac{b^2}{8\lambda\ell_e} \qquad t = \frac{\Delta_h}{\lambda} = \frac{a^2}{8\lambda\ell_h}$$
 (15-6)

For the same values of s and t the phase error due to the flare has a much more pronounced effect in the E plane than in the H plane. The reason is simply that the field is constant across the aperture of a sectoral horn flared in the E plane but varies sinusoidally for one flared in the H plane. The patterns also exhibit much higher minor-lobe levels for the former case.

The curves in both Fig. 15-4 and Fig. 15-5 are reasonably accurate when either a or b is at least several wavelengths. For smaller apertures it will be necessary to multiply by the appropriate obliquity factor, F_e or F_h . The approximate form given by Eq. (15-5) is reasonably accurate for aperture dimensions greater than about 1.5 λ .

Expressions for the field in the aperture of a sectoral horn, upon which radiationpattern calculations depend, are given in Sec. 10.9 of Silver.² In Sec. 10.10 it is remarked that there is disagreement between theory and experiment for E-plane sectoral horns. In part, this is due to an error in Eqs. (45a) and (45b) on pages 357 and

^{*}For 10-dB beamwidths of small horns, see also Fig. 46-13.

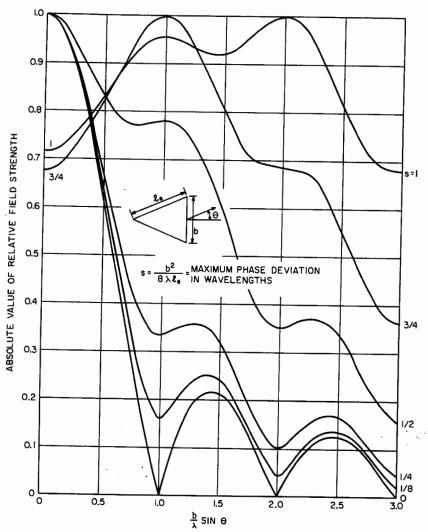


FIG. 15-4 Universal radiation patterns of horns flared in the E plane (sectoral or pyramidal).

358 of Ref. 2. This error was pointed out by Narasimhan and Rao³ and arose inadvertently through the use of a left-handed coordinate system in Fig. 10.9a on page 351. To correct the error the factors $E_{\theta} - Z_0 H_x \cos{(\Theta - \theta)}$ and $E_{\theta} \cos{\Theta} - Z_0 H_x \cos{\theta}$, which appear in the integrands of Eqs. (45a) and (45b), should be changed to read $E_{\theta} + Z_0 H_x \cos{\Theta} - \theta$ and $E_{\theta} \cos{\Theta} + Z_0 H_x \cos{\theta}$.

The aperture field method is incapable of predicting the radiation pattern in the rear sector of a horn antenna and is not accurate in the wide-angle-sidelobe region because it neglects diffraction at the aperture edges. The prediction of wide-angle and

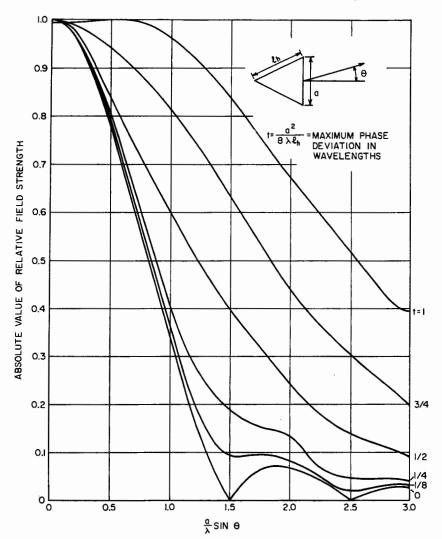


FIG. 15-5 Universal radiation patterns of horns flared in the H plane (sectoral or pyramidal).

rearward-radiated fields is now possible by using the techniques of the geometrical theory of diffraction (GTD). It is impractical to attempt such a treatment here; the interested reader should consult Refs. 4, 5, and 6.

Pyramidal Horns

The pyramidal horn of Fig. 15-1a flares in both the E and the H planes. Its radiation patterns in these planes are the same as those of the corresponding flared sectoral

horns. Thus the *E*-plane patterns of a pyramidal horn are as shown in Fig. 15-4, while its *H*-plane patterns are those of Fig. 15-5. For aperture dimensions greater than about 1λ the patterns in the two planes may be controlled independently by adjustment of the mouth dimensions.

The design of a horn for specified beamwidths in the principal planes must be done iteratively because of the need to fit the throat of the horn to a given waveguide. The patterns of Figs. 15-4 and 15-5 are first used to select possible values of a, b, ℓ_e , and ℓ_h . Only values which satisfy the condition

$$(a - a_0)^2 [(\ell_b/a)^2 - \%] = (b - b_0)^2 [(\ell_e/b)^2 - \%]$$
 (15-7)

may be retained if the horn is to be physically realizable. Here, a_0 and b_0 are the *H*-and *E*-plane waveguide dimensions respectively.

Gain

The gain of sectoral horns may be determined⁷ from the normalized gain curves of Figs. 15-6 and 15-7, provided the narrow dimension is at least one wavelength. It is seen that the gain initially increases as the aperture dimension increases, then reaches a maximum before falling off. The decrease in gain is due to increasing cylindrical-wave phase error as the aperture increases while slant length remains constant.

The points of maximum gain in each case occur approximately where

$$s = b^2/(8\lambda \ell_*) = \frac{1}{4}$$
 (15-8)

$$t = a^2/(8\lambda \ell_h) = \%$$
 (15-9)

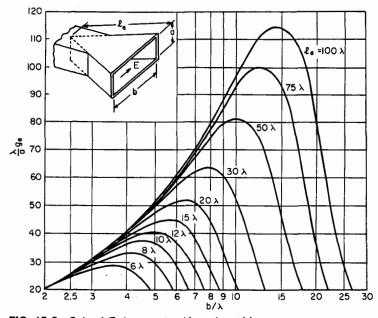


FIG. 15-6 Gain of *E*-plane sectoral horn ($a \le \lambda$).

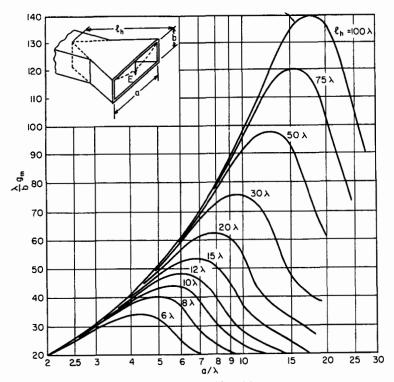


FIG. 15-7 Gain of H-plane sectoral horn ($b \le \lambda$).

for E- and H-plane sectoral horns respectively, corresponding to phase errors of 90° and 135°.

The gain of both sectoral and pyramidal horns⁷ may be determined from

$$G = G_0 R_{\epsilon} R_h \tag{15-10}$$

where the area gain G_0 is given by

$$G_0 = 32ab/(\pi\lambda^2)$$
 (15-11)

relative to a fictitious isotropic radiator. The factors R_e and R_h , both equal to or less than unity, account for the reduction in gain due to phase error caused by the flare; thus R_e is a function of s, while R_h is a function of t. Both R_e and R_h involve Fresnel integrals.

By combining Eq. (15-10) with Eq. (15-11) and converting to decibel form, the gain is

Gain (dB) =
$$10.08 + 10 \log_{10} ab/\lambda^2 - L_{\epsilon} - L_{k}$$
 (15-12)

where
$$L_e = -10 \log_{10} R_e$$
 $L_h = -10 \log_{10} R_h$ (15-13)

The factors L_e and L_h , shown graphically in Fig. 15-8 and tabulated in Table 15-1,⁸ are functions of the parameters s and t given in Eq. (15-6). For a sectoral horn either

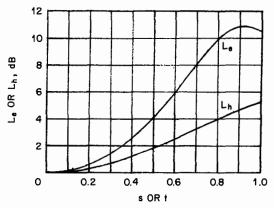


FIG. 15-8 Gain-reduction factor for *E*- and *H*-plane flares.

TABLE 15-1 Gain-Reduction Factors, $L_{\rm e}$ or $L_{\rm h}$, for Sectoral and Pyramidal Horns

16 <i>s</i> or 16 <i>t</i>	<i>L₌</i> , dB	L _{ii} , dB	16s or 16 <i>t</i>	L., dB	L _{is} , dB
1.0	0.060	0.029	14.0	10.783	4.486
1.5	0.134	0.064	15.0	10.849	4.892
2.0	0.239	0.114	16.0	10.502	5.252
2.5	0.374	0.179	18.0	9.474	5.819
3.0	0.541	0.257	20.0	8.847	6.210
3.5	0.738	0.349	22.0	8.901	6.504
4.0	0.967	0.454	24.0	9.637	6.785
4.5	1.229	0.573	26.0	10.938	7.102
5.0	1.525	0.705	28.0	12.430	7.460
5.5	1.854	0.850	30.0	13.312	7.831
6.0	2.218	1.007	32.0	13.052	8.175
6.5	2.618	1.176	34.0	12.251	8.460
7.0	3.054	1.357	36.0	11.666	8.684
7.5	3.527	1.547	38.0	11.607	8.869
8.0	4.037	1.748	40.0	12.121	9.047
9.0	5.166	2.175	42.0	13.104	9.243
10.0	6.427	2.630	44.0	14.221	9.462
11.0	7.769	3.101	46.0	14.851	9.692
12.0	9.081	3.577	48.0	14.619	9.911
13.0	10.163	4.043	50.0	13.937	10.101

Courtesy IEE; see Ref. 8.

 ℓ_e or ℓ_h will be infinite, and the corresponding loss factor $L_{h,e}$ will be zero. An alternative way of calculating the gain of a pyramidal horn is to take the product of the gains of the corresponding sectoral horns, obtained from Figs. 15-6 and 15-7, and then to multiply by the factor $\pi/32$.

In the above discussion of gain, far-field conditions are implicitly understood. It has been shown, however, that Eqs. (15-10) and (15-12) may be used at finite range (in the Fresnel zone) by a simple redefinition of terms. This is possible because the effect of finite range is simply to modify the already existing quadratic phase error in the aperture due to the flare. G_0 , R_e , and R_h are determined as before, but the parameters s and t are now taken to be

$$s = b^2/(8\lambda \ell_*')$$
 $t = a^2/(8\lambda \ell_h')$ (15-14)

in which

$$1/\ell'_{\epsilon} = 1/\ell_{\epsilon} + 1/r$$
 $1/\ell'_{h} = 1/\ell_{h} + 1/r$ (15-15)

r being the distance from the aperture to the field point.

When the a dimension in a sectoral or pyramidal horn is small $(a \le \lambda)$, the close proximity of the magnetic walls causes errors in the gain equations, (15-10) and (15-11). A more accurate equation has been derived:

$$G = R_e R_h \frac{16ab}{\lambda^2 (1 + \lambda_g/\lambda)} \exp\left[\frac{\pi a}{\lambda} \left(1 - \frac{\lambda}{\lambda_g}\right)\right]$$
 (15-16)

in which R_e and R_h are as before except that in calculating R_e the parameter s must be slightly modified. Thus

$$s = b^2 / \left(8\lambda_g \ell_e \cos^2 \frac{\theta_f}{2} \right)$$
 (15-17)

where θ_f is the semiflare angle (Fig. 15-3). There is no such corresponding modification to t, and λ_g is the guide wavelength appropriate to the dimension a, i.e.,

$$\lambda/\lambda_{r} = [1 - (\lambda/2a)^{2}]^{1/2}$$
 (15-18)

Equation (15-10), which may be called Schelkunoff's gain formula, includes the geometrical-optics field in the aperture of the horn and the effects of singly diffracted fields at the aperture edges. It does not, however, include effects due to multiple-edge diffractions or diffracted fields which are reflected from interior horn walls. These effects manifest themselves in the form of small oscillations about the monotonic curve predicted by Schelkunoff's equations, (15-10) and (15-11). The oscillations are of the order of ± 0.5 dB for pyramidal horns with a gain of about 12 dB. They decrease to about ± 0.2 dB for horns with a gain of about 18 dB, and they appear to be less than ± 0.1 dB when the gain exceeds 23 dB. $^{10.11}$

Optimum-Gain Horns

An optimum-gain horn is a pyramidal horn whose dimensions are such that it produces the maximum far-field gain for given slant lengths in the E and H planes. From what has been said above, this condition will occur when the parameters s and t are respectively about $\frac{1}{2}$ and $\frac{1}{2}$. Thus an optimum-gain horn will have aperture dimensions given approximately by

$$a = \sqrt{3\lambda \ell_h} \qquad b = \sqrt{2\lambda \ell_e} \tag{15-19}$$

The effective area of an optimum-gain horn is very close to 50 percent of its actual aperture area; its gain is

Gain (dB) =
$$8.1 + 10 \log_{10} ab/\lambda^2$$
 (15-20)

Such a horn will have full half-power beamwidths (HPBWs) and first-sidelobe levels given approximately by

$$2 \sin^{-1} (0.45\lambda/b)$$
 -9 dB E plane
 $2 \sin^{-1} (0.63\lambda/a)$ -16 dB H plane

The H-plane sidelobe is not well defined, amounting to no more than a shoulder on the main beam.

In designing a standard horn, one generally knows the desired gain, wavelength, and dimensions of the feeding waveguide. If the horn is also to be optimum, these quantities, together with the restrictions discussed above, completely determine the final dimensions of the horn. Let a_0 and b_0 be the H- and E-plane waveguide dimensions respectively. Then the following equation must be satisfied if the horn is to be physically realizable (that is, fit the feeding waveguide), be optimum, and have numerical gain G:

$$\left(\sqrt{\frac{2\ell_{\epsilon}}{\lambda}} - \frac{b_0}{\lambda}\right)^2 \left(\frac{2\ell_{\epsilon}}{\lambda} - 1\right) = \left(\sqrt{\frac{3K\lambda}{\ell_{\epsilon}}} - \frac{a_0}{\lambda}\right)^2 \left(\frac{4K\lambda}{3\ell_{\epsilon}} - 1\right)$$
 (15-21)

where $K = (G/15.75)^2$.

This equation may be easily solved by trial and error for ℓ_e . A rough approximation which can serve as a first trial is $\ell_e = \lambda \sqrt{K}$. After ℓ_e has been determined, ℓ_h is given by

$$\ell_h = K\lambda^2/\ell_e \tag{15-22}$$

Impedance

The impedance characteristics of sectoral horns depend on the mismatch between the horn mouth and free space, the length of radial guide between the horn aperture and throat, and the mismatch at the junction between the uniform guide and the throat. The input voltage standing-wave ratio (VSWR) of an E-plane horn in general varies periodically between 1.05 and 1.5 as the horn slant length is varied, with minima occurring every half-guide wavelength.^{2,12} The guide wavelength in the E-plane sectoral horn is equal to that in the rectangular waveguide.

The input impedance of an H-plane sectoral horn differs somewhat from that of the E-plane horn, in that the mismatch at the junction of the horn and rectangular waveguide is much smaller than that at the horn aperture. The result is that the input VSWR to an H-plane sectoral horn is essentially constant in magnitude and varies only in phase as the length of the horn is changed.²

A broadband match is best obtained in the E-plane sectoral horn by treating the two discontinuities separately. The mismatch at the junction of the waveguide and horn may be eliminated with a reactive window (usually inductive) at the junction. The horn aperture is frequently matched to free space by using a plastic radome of proper thickness and dielectric constant. If no radome is used, a match may be obtained by the use of small reactive discontinuities at the aperture.

The problem of obtaining a broadband match with the H-plane horn is somewhat

easier because of the small discontinuity at the horn throat. Generally, only the aperture needs to be matched, and the techniques mentioned for the *E*-plane horn may be employed.

The impedance characteristics of pyramidal horns are somewhat more complicated than those of sectoral horns. However, horns having a gain of 20 dB or more and moderate flare angles, such as optimum horns, are usually well matched by a rectangular waveguide supporting only the dominant mode. For example, an optimum horn with 28-dB gain at 3000 MHz fed by 1½- by 3-in (38- by 76-mm) waveguide has an input VSWR of about 1.03. Where the overall match must be improved, techniques similar to those described for sectoral horns may be used.

15-3 DOMINANT-MODE CONICAL HORNS

Radiation Patterns

The conical horn excited by a circular waveguide in the TE₁₁ mode is the counterpart of a pyramidal horn with TE₁₀ excitation in rectangular guide, and in many respects its behavior is quite similar. The modes in an infinite conical horn are exactly expressible in terms of a combination of spherical Hankel and Legendre functions. Rigorous application of vector diffraction theory is possible but leads to such complexity that approximate solutions must be sought. Considerable simplification can be achieved by use of asymptotic expressions for the fields, as shown in Ref. 13. One of the earliest applications of GTD to the conical horn is given in Ref. 14, in which contributions from as many as seven rays, including multiple diffractions, are summed. Better results are claimed in Ref. 15, in which the slope diffraction technique is combined with GTD. Results of such computations are in reasonably good agreement with observed patterns, but the number of test cases is very few and accuracy limits cannot, in general, be given. As a result, no reliable universal pattern curves, similar to those of Figs. 15-4 and 15-5, are available for the conical horn even today.

Experimental data on conical-horn patterns are also limited, and it still seems necessary to rely on the observations made by Bell Laboratories investigators as far back as 40 years ago. The now familiar conical-horn patterns given by King 17 in 1950 are reproduced in Fig. 15-9 for aperture diameters in the range $1.4 < d/\lambda < 4.3$. The spherical-wave phase-error parameter $s = d^2/(8\lambda\ell)$ ranges from 0.03 to 0.6. It should be noted that in King's original paper 17 the parameter was given as $d^2/(8\lambda L)$, where L is the axial horn length. To conform with the first edition of this handbook s has been recomputed in terms of slant length ℓ rather than axial length ℓ . The lengths ℓ and ℓ can differ significantly because the semiflare angle is not small except for case ℓ . This can be a source of confusion, as pointed out in Sec. 10-1. From Fig. 15-3 it is seen that the semiflare angle is given by

$$\tan \theta_f = d/(2L)$$
 or $\sin \theta_f = d/(2\ell)$ (15-23)

The horns in Fig. 15-9a and b have aperture dimensions less than optimum. The horn in c is close to optimum size, while g shows the patterns of an optimum horn in greater detail. Optimum is again used to refer to a horn whose aperture dimension is such as to yield maximum gain for a given length; in this case the diameter is denoted by d_m . Although only six different patterns are shown in Fig. 15-9, they can be used for approximate estimation of pattern shapes for a variety of horns, provided the proportions of the horn in question are such as to match (or nearly match) the phase-

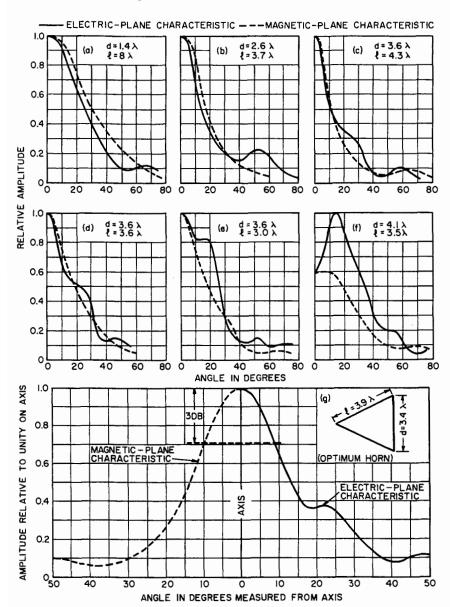


FIG. 15-9 Experimentally observed patterns of conical horns of various dimensions.

error parameter s of one of those in Fig. 15-9. As an example, consider a horn with aperture diameter $d=6\lambda$, which does not appear in the figure. If the length of this horn is $\ell=10\lambda$, then its parameter s will match that of horn d; i.e., s=0.45. As a consequence, the patterns of this horn will have nearly the same shapes as those in Fig. 15-9 d, with only a scale change in the angle θ . The new angle θ_1 is related to the θ in d by the relation $d_1/\lambda \sin \theta_1 = d/\lambda \sin \theta$, whence $\sin \theta_1 = 0.6 \sin \theta$.

It happens that for a small-diameter horn in which $d = 0.86\lambda$, the *E*- and *H*-plane patterns become nearly identical, at least down to the -12-dB level, providing the wall thickness at the aperture is less than about $\lambda/100$. In this case, the full beamwidth at -12 dB is about 132° . Such a horn is suitable as a feed for a reflector having F/D = 0.4.

Gain

The curves in Fig. 15-10 show how the gain (in decibels above isotropic) of a conical horn varies with its dimensions. Note that the parameter L/λ in this figure is the axial

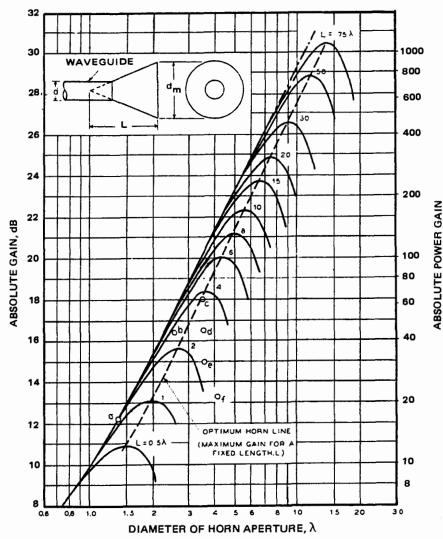


FIG. 15-10 Calculated gain of a conical horn as a function of aperture diameter with axial length as parameter. (© 1950 IEEE; see Ref. 17.)

length. Conversion to ℓ/λ has not been made in this case, since the resulting fractional values would hinder interpolation. The curves are taken from King's paper, 17 and he attributed them to the unpublished work of his Bell Laboratories coworkers M. C. Gray and S. A. Schelkunoff. They are believed to have been derived theoretically; since the nature of any approximations used is not known, it is difficult to assess the limits of accuracy associated with these curves. Numerical gain calculations based on a GTD analysis in Ref. 14 are said to be in agreement with gain values in Fig. 15-10 to within ± 0.1 dB, but the ranges of d/λ and L/λ over which this is true are not stated. A closed-form expression involving Lommel functions is derived in Ref. 13, from which a family of curves with parameter values the same as those in Fig. 15-10 is given. Comparison of the two sets of curves shows differences ranging from +0.4 to -0.8 dB. The same authors in another paper 18 give a very simple expression for the gain as a function of L/λ and d/λ . Unfortunately the expression applies only to a circular aperture with uniform illumination and quadratic phase; it most certainly does not apply to a conical horn. The points a to f in Fig. 15-10 are the measured gains of the horns depicted in Fig. 15-9, and they appear to be in reasonable agreement with values obtained by interpolation between curves.

The gain of a conical horn in terms of its aperture diameter may clearly be written as

$$G = (\pi d/\lambda)^2 R \tag{15-24}$$

or
$$Gain (dB) = 20 log_{10} (\pi d/\lambda) - L$$
 (15-25)

where R and L are factors analogous to those for sectoral horns in Sec. 15-2 that account for loss in gain due to spherical-wave phase error. Figure 15-11 shows the value of L in decibels as a function of the phase-error parameter $s = d^2/(8\lambda\ell)$, where ℓ is slant length. This curve, which appeared in the first edition of this handbook, was based on a gain expression involving Lommel functions that was derived but not published by W. C. Jakes* of Bell Laboratories.

The accuracy with which gain predictions can be made from Eq. (15-24) and Fig. 15-11 is not known with certainty, but it appears to be as good as that given by Fig. 15-10.

The case of s = 0 corresponds to a horn with no flare, i.e., to an open-ended circular-waveguide radiator. If only the TE_{11} mode is present, then the gain is given by Ref. 2 (page 341),

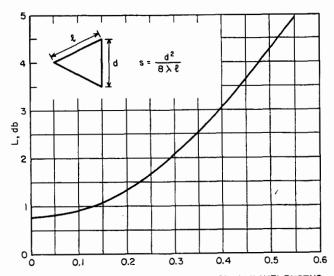
$$G = (\pi d/\lambda)^2 \frac{\left| \sqrt{\frac{\lambda}{\lambda_g}} + \sqrt{\frac{\lambda_g}{\lambda}} + \Gamma\left(\sqrt{\frac{\lambda_g}{\lambda}} - \sqrt{\frac{\lambda}{\lambda_g}}\right) \right|^2}{2(p_{11}^{\prime 2} - 1)(1 - |\Gamma|^2)}$$
(15-26)

where $p'_{11} = 1.841$ is the first root of $J'_1(p) = 0$ and Γ is the complex reflection coefficient at the aperture. For large apertures

$$G \to 0.837 (\pi d/\lambda)^2$$
 (15-27)

This shows that R = 0.837 for long horns with small flare angles; also, L = 0.773 dB, corresponding to the intercept at s = 0 in Fig. 15-11. In contrast to the sectoral-horn case, the parameter R for the conical horn is always less than unity. This is

^{*}Private communication: W. C. Jakes wrote the chapter "Horn Antennas" in the first edition of this handbook.



s, MAXIMUM APERTURE PHASE DEVIATION IN WAVELENGTHS

FIG. 15-11 Gain-correction factor for conical horns.

simply a consequence of a slight change in definition [compare Eq. (15-24) with Eq. (15-10)] such that for the conical horn the effect of amplitude taper as well as phase taper is included in R.

Optimum-Gain Horns

In Fig. 15-10 the dashed line connecting the maxima of the gain curves defines the gain and dimensions, d/λ , L/λ , of optimum conical horns. An empirical equation for this line over the range of variables shown in the figure is

Gain (dB) =
$$7.0 + 20.6 \log_{10} d/\lambda$$
 (15-28)

When the quantity $d^2/(8\lambda L)$, L being the axial length, is evaluated at the maxima in Fig. 15-10, it is found to vary from 0.56 for $L=0.5\lambda$ to 0.31 for $L=75\lambda$. The slant length ℓ can easily be determined from the known values of d and L, for example, by using Eqs. (15-23) or, more simply, $\ell=(L^2+d^2/4)^{1/2}$. If this is done and the parameter $s=d^2/(8\lambda\ell)$ is computed, it is found to vary only from about 0.30 to 0.375. Thus the dimensions of optimum conical horns can be expressed by

$$d = \sqrt{n\lambda \ell} \tag{15-29}$$

where n lies between 2.4 and 3.0.

The effective area of an optimum horn is between 52 and 56 percent of its actual aperture area.

Impedance

The remarks regarding the impedance of pyramidal horns in Sec. 15-2 also apply to conical horns if "dominant-mode round waveguide" is read for "rectangular guide."

15-4 MULTIMODE HORNS

General

The dominant single-mode horn, whether conical (TE_{11}) or pyramidal (TE_{10}) , radiates a pattern in which the E plane differs significantly from the H plane so that axial-beam symmetry does not exist in general. The reason for this is that the electric field in the horn aperture is heavily tapered in the H plane (since it must vanish on the conducting walls) but tapered very little (in the conical case) or not at all (in the pyramidal case) in the E plane. The patterns in the two planes can be made identical or nearly so by introducing appropriate additional modes into the horn structure, which then propagate to the horn aperture along with the dominant mode. The aperture field is then a superposition of the fields of the individual modes. In most practical applications of this technique only one additional mode is required; such horns are called dual-mode.

Diagonal Horn

The simplest example of a dual-mode horn is the diagonal horn, 19 in which two spatially orthogonal dominant modes, the TE_{10} and the TE_{01} , are excited with equal amplitude and phase in a square waveguide which flares to a pyramidal horn. In this case the electric field in the aperture is aligned with one of the diagonals. A simple



FIG. 15-12 Transformation from rectangular waveguide to diagonal horn.

transformation from rectangular guide to diagonal horn is shown in Fig. 15-12. Another method of excitation is the use of coaxial-fed orthogonal probe couplers in square waveguide along with a suitable power splitter.

For apertures in which $d \approx 2\lambda$ the E-, H-, and intercardinal-plane patterns will be essentially identical to well below

the -10-dB level, as is evident in the universal patterns in Fig. 15-13. True axial symmetry is not achieved, however, because the intercardinal-plane patterns differ markedly in sidelobe structure from those in the principal planes. Moreover, a significant amount of cross-polarization is manifested in the intercardinal planes, as shown by the dashed curves in Fig. 15-13.

By writing $u = (\pi d/\lambda) \sin \theta$, the principal-plane patterns of the diagonal horn are given by

$$E_{\infty} = \begin{cases} F_s \\ F_h \end{cases} \frac{\sin u/\sqrt{2}}{u/\sqrt{2}} \cdot \frac{\cos u/\sqrt{2}}{1 - 2u^2/\pi^2} \qquad E_{\text{cross}} = 0 \qquad \text{(15-30)}$$

while in the intercardinal planes

$$\frac{E_{co}}{E_{cross}} = \frac{1}{2} \left(F_e \cdot \frac{\sin u}{u} \pm F_h \cdot \frac{\cos u}{1 - 4u^2/\pi^2} \right)$$
 (15-31)

 F_e and F_h are the obliquity factors discussed in Sec. 15-1. When $d \approx 2\lambda$, it was observed that $F_e \rightarrow F_h \rightarrow 1$; this is the case for the patterns shown in Fig. 15-13.

Prime-focus feed horns have small apertures $(d = \lambda)$ for commonly used f/D ratios. The diagonal horn is at a disadvantage here because the disparity between F_{\bullet}

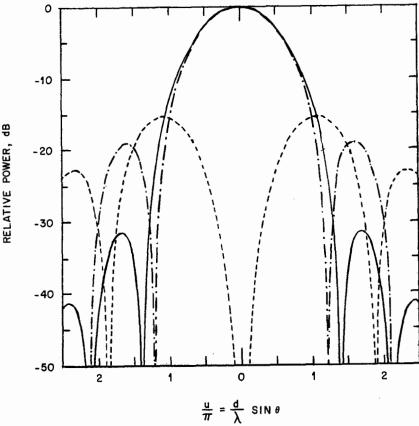


FIG. 15-13 Principal- and intercardinal-plane patterns of diagonal horn $(d \gg \lambda)$: ——, E and H planes; ———, intercardinal, copolar; ——, intercardinal, cross-polar. (*From* Microwave Journal; see Ref. 19.)

and F_h destroys the circular symmetry of the beam. It is an observed fact, however, that in the neighborhood of $d=1.23\lambda$ a diagonal horn does possess axial-beam symmetry with full widths of 40 and 73° at the -3- and -10-dB levels. Apparently, in this case the values of Γ and λ/λ_g (see Sec. 15-1) happen to be such that F_e and F_h are equal.

Important characteristics of large-aperture diagonal horns are given in Table 15-2.

Duai-Mode Conical Horn

In the case of the conical horn the addition of the higher-order TM_{11} mode to the dominant TE_{11} mode can create a radiation pattern with good axial-beam symmetry and with a low level of cross-polarization as well. When properly phased at the horn aperture, the TM_{11} mode will cancel the ϕ component of magnetic field due to the

TABLE 15-2 Ch	aracteristics of	Diagonal	Horns
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Parameter	Principal planes	45° and 135° planes	
3-dB beamwidth,	58.5 λ/d	58.0 λ/d	
10-dB beamwidth, °	$101 \lambda/d$	98 λ/d	
Angular position, first null,	81 λ/d	$70 \lambda/d$	
Angular position, first lobe,*	96 λ/d	92 λ/d	
Level of first sidelobe	31½ dB	19 dB	
Angular position, second null,*	$122 \lambda/d$	$122 \lambda/d$	
Angular position, second lobe,*	139 λ/d	$147 \lambda/d$	
Level of second sidelobe	41½ dB	24 dB	

From Microwave Journal; see Ref. 19.

 TE_{11} mode at the aperture boundary, causing H_{ϕ} as well as E_{ϕ} to vanish. This is a condition that leads to axial symmetry and low cross-polarization in the radiation pattern. In the original version, the TM_{11} mode was generated by a step change in guide radius from a to b in the horn throat, as shown in Fig. 15-14. The radius a must be

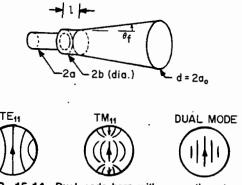


FIG. 15-14 Dual-mode horn with generating step and its approximate aperture field distribution.

large enough to support the TE_{11} mode but small enough to ensure that the TM_{11} is cut off (1.84 < ka < 3.83). The amount of TM_{11} so generated increases with the ratio b/a, but b should not be so large as to permit the TE_{12} mode to propagate (3.83 < kb < 5.33). Owing to the axial symmetry, TE_{mn} or TM_{mn} modes with m > 1 will not be excited. Figure 15-14 also indicates qualitatively the distribution of the electric field in the aperture for the two modes both individually and in combination. In the central region of the aperture the electric field of the TM_{11} mode reinforces that of the TE_{11} . Near the aperture boundary the two fields oppose one another. Thus the resulting electric field may be heavily tapered in the E as well as in the H plane.

A set of patterns in the E, H, and intercardinal planes is shown in Fig. 15-15 for

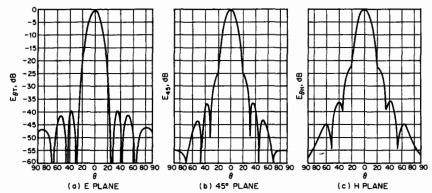


FIG. 15-15 Radiation patterns of dual-mode conical horn, $d = 4.67\lambda$. (*From* Microwave Journal; see Ref. 20.)

a horn with aperture diameter $2a_0 = 4.67\lambda$ and a small semiflare angle of 6.25° . In this horn $a = 1.02\lambda$, $b = 1.30\lambda$, and $\ell = 0.20\lambda$. The short constant-diameter section of length ℓ is used to ensure that the two modes will be in the same phase at the center of the aperture at the design frequency. This length depends upon the flare angle and the distance from the step to the aperture as well as on the launch phase of the TM₁₁ mode relative to the TE₁₁.

The TE₁₁ mode generates θ and ϕ components of E in the far field, while the TM₁₁ mode generates only the θ component. In terms of the usual variable, $u=ka_0\sin\theta$, and with the assumption that the aperture is reasonably large $(a_0 \gtrsim \lambda)$ so that the reflection coefficient Γ is approximately zero, the radiated far-field components are

coefficient
$$\Gamma$$
 is approximately zero, the radiated far-field components are
$$E_{\theta} = \left[1 + \frac{\lambda}{\lambda_g} \cos \theta - \alpha \frac{\lambda/\lambda_g' + \cos \theta}{1 - (3.83/u)^2} \right] \frac{J_1(u)}{u} \cdot \cos \phi$$

$$E_{\phi} = \left(\frac{\lambda}{\lambda_g} + \cos \theta \right) \frac{J_1'(u)}{1 - (u/1.84)^2} \cdot \sin \phi$$
(15-32)

where λ/λ_g and λ/λ_g' refer to the TE₁₁ and TM₁₁ modes, respectively, and α , the mode-content factor, is a measure of the field strengths of the two modes at the aperture center. For $\alpha=0.65$ the E- and H-plane HPBWs are equalized, and the phase centers in the two planes are coincident. Other values of α , in the neighborhood of 0.6, lead to suppression of the first sidelobe in the E plane or to suppression of the cross-polar radiation in the intercardinal planes. The presence of the TM₁₁ mode has no effect in the H plane, where this mode does not radiate. The beamwidth of a dual-mode conical horn will vary somewhat with the mode-content factor; typically HPBW = $72 \lambda/d^*$.

Mode conversion at a discontinuous step in round waveguide has been investigated theoretically and experimentally. Figure 15-16 shows the mode conversion coefficient and excitation phase of the TM_{11} mode relative to the TE_{11} mode on the guide centerline in the plane of the step at z=0. If $\phi_{\rm ex}$ represents the launch phase, $\phi_{\rm ph}$ the differential phase in the constant-diameter phasing section, and $\phi_{\rm fl}$ the differential phase of the modes in the flared section of Fig. 15-14, then the condition for reinforcement of the electric fields at the aperture center is

$$\phi_{\rm ph} + \phi_{\rm fl} - \phi_{\rm ex} = 0 \text{ or } 2m\pi$$
 (15-33)

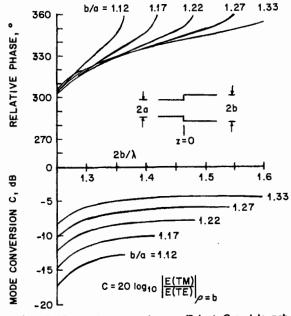


FIG. 15-16 Mode conversion coefficient C and launch phase of TM_{11} mode relative to TE_{11} at step discontinuity $(TM_{11} \text{ lags } TE_{11})$. (© 1970 IEEE; see Ref. 21.)

If λ_g and λ_g' are the guide wavelengths of the TE_{11} and the TM_{11} modes respectively, then

$$\phi_{\rm ph} = 2\pi \ell (1/\lambda_g - 1/\lambda_g') = 2\pi \ell / \lambda (\lambda/\lambda_g - \lambda/\lambda_g')$$
 (15-34)

where λ_g and λ'_g are constant and depend on the diameter 2b in the phasing section. In the flared horn the differential phase shift is closely given by

$$\phi_{fl} = 2\pi \int \left[\frac{1}{\lambda_g(z)} - \frac{1}{\lambda_g'(z)} \right] dz \qquad (15-35)$$

in which the guide wavelengths are now functions of the axial coordinate z and where integration is taken from $z = \ell$ to the z value at the aperture plane. Note that ϕ_{ph} and ϕ_{fl} are positive angles because $\lambda_g' > \lambda_g$. These equations have been computed in Ref. 20 and are shown in Fig. 15-17. In the case of ϕ_{fl} the z coordinate has been eliminated by introducing the semiflare angle θ_f .

As an example of the use of these design curves, consider the horn whose patterns are given in Fig. 15-15. With $a_0/\lambda=2.33$, $b/\lambda=0.65$, and $\theta_f=6.25^\circ$, Fig. 15-17 a gives $\phi_{\rm fl}=620^\circ$, while b with $\ell/\lambda=0.20$ gives $\phi_{\rm ph}=40^\circ$. The expected excitation phase is obtained from Fig. 15-16; $\phi_{\rm ex}=-40^\circ$. When these values are substituted into Eq. (15-33), the equation is satisfied with a small error of 20°. From the same figure the TM₁₁-mode conversion coefficient appears to be about -7.5 dB; evidently this corresponds closely to the value $\alpha=0.6$ for the mode-content factor defined in Ref. 20.

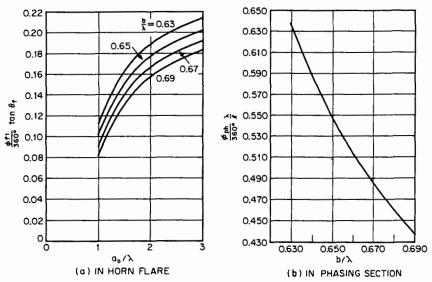


FIG. 15-17 Differential phase shifts in (a) the flared horn and (b) the phasing section. (From Microwave Journal; see Ref. 20.)

The phasing condition of Eq. (15-33) can be satisfied only at a single frequency because of the different dispersion characteristics of the two modes. Thus the dual-mode horn is frequency-sensitive (the horn of Fig. 15-15 has a useful bandwidth of only 3 to 4 percent), and the sensitivity increases with horn length. For horns that are not too long some improvement can be obtained by loading the step discontinuity with a dielectric ring.²¹

Use of a step discontinuity near the horn throat is not the only way to convert TE_{11} to TM_{11} energy in a horn. A technique described by $Satoh^{23}$ employs a thin dielectric band placed internally in contact with the horn wall. When the length of the band, its thickness, and its position are correctly determined, the resulting bandwidth of this dual-mode horn is said to be 25 percent (defined so that all sidelobes are below -20 dB and E- and H-plane beamwidths differ by no more than 5 percent).

Conversion from the TE_{11} mode to the TM_{11} and other higher modes (TE_{12} , TM_{12} , TE_{13} , ...) at a relatively large-diameter junction between round and conical waveguides has been investigated analytically by Tomiyasu.²⁴ In this case a discontin-

uous step (as in Fig. 15-14) is not needed. Using this technique, Turrin²⁵ has designed multimode horns of the type shown in Fig. 15-18; typical *E*-plane patterns are shown in Fig. 15-19 for two different aperture sizes: (a) 1.31λ and (b) 1.86λ . In this type of horn the input guide should be sized to propagate the TE_{11} mode but not the TM_{11} mode (1.84 < ka < 3.83). Conversion takes place at the plane AA' in Fig. 15-18, where the diam-

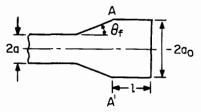


FIG. 15-18 Stepless dual-mode horn. (© 1967 IEEE; see Ref. 25.)

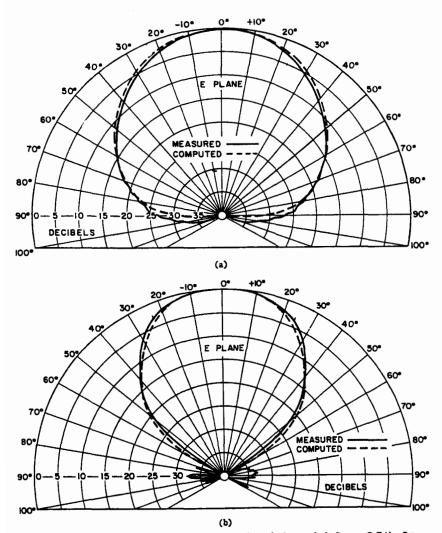


FIG. 15-19 *E*-plane patterns of stepless dual-mode horn. (a) $2a = 0.71\lambda$, $2a_0 = 1.31\lambda$, $\ell = 1.37\lambda$, $\theta_f = 30^\circ$. (b) $2a = 0.71\lambda$, $2a_0 = 1.86\lambda$, $\ell = 3.75\lambda$, $\theta_f = 28^\circ$. (© 1967 IEEE; see Ref. 25.)

eter $2a_0$ is large enough to support this mode; i.e., $ka_0 > 3.83$. The next-higher modes with the proper symmetry are the TE_{12} , which requires $ka_0 > 5.33$, and the TM_{12} , requiring $ka_0 > 7.02$. Since these modes are not wanted, the aperture diameter should be restricted so that $3.83 < ka_0 < 5.33$; i.e., $1.22 < 2a_0/\lambda < 1.70$. This condition is satisfied by the horn in Fig. 15-19 a but not b. In the latter case the aperture must contain TE_{12} as well as TE_{11} and TM_{11} modes; evidently the amount of TE_{12} is small and does not significantly affect the radiation pattern.

At the plane AA' in Fig. 15-18 the higher-order TM_{11} mode is 90° out of phase with the TE_{11} mode; hence the phasing section ℓ should have a differential length of 270° for the two modes to ensure correct phasing at the aperture; thus

$$\ell (1/\lambda_g - 1/\lambda_g') = 0.75$$
 (15-36)

where
$$\lambda/\lambda_g = \left[1 - \left(\frac{1.84}{ka_0}\right)^2\right]^{1/2}$$
 and $\lambda/\lambda_g' = \left[1 - \left(\frac{3.83}{ka_0}\right)^2\right]^{1/2}$

To ensure that the correct amount of TM_{11} relative to TE_{11} power is generated at the conical junction, the flare angle θ_f should be chosen to satisfy

$$\theta_f = 44.6 \, \lambda / 2a_0$$
 degrees (15-37)

This simple equation comes from equating two different expressions for the mode power ratio, one given in Ref. 24 and the other in Ref. 25. If Eqs. (15-36) and (15-37) are applied to the horns in Fig. 15-19, they predict $\ell = 1.42\lambda$, $\theta_f = 34^{\circ}$ for horn a and $\ell = 3.86\lambda$, $\theta_f = 24^{\circ}$ for horn b, in reasonably good agreement with the actual values. Small horns constructed in accordance with these principles appear to yield a useful bandwidth of about 12 percent.

There is conversion of TE_{11} energy to TM_{11} at the aperture of the horn in Fig. 15-14 (see subsection "Multimode Pyramidal Horns") as well as at the step. The TM_{11} mode generated at the aperture is in quadrature with the TE_{11} component, and its amplitude is not negligible unless the flare angle is very small. The existence of two physically separate sources of TM_{11} -mode generation complicates the design of these horns, and recourse to empirical adjustment of step size and phasing length is usually necessary.

Multimode Pyramidal Horns

Beam shaping in a pyramidal horn with square aperture can be accomplished in much the same way as with the conical horn. In this case the dominant mode is the TE_{10} , while the necessary higher-order mode is a hybrid mixture of TE_{12} and TM_{12} modes, as shown by Jensen. These two modes, which have the same propagation constant, thus can exist as a hybrid pair, and their relative amplitudes can be adjusted to give a purely linearly polarized aperture field. When added in the proper phase to the TE_{10} field in the aperture, the resulting distribution is tapered in the E as well as in the E plane, as in Fig. 15-20. If one assumes that dual-polarization capability is required, the input waveguide in the figure will be square with a side of dimension E such that the E the E pair cannot propagate; i.e., E and E the mode-generating step both dimensions of the guide increase to E, where E the mode-generating step both dimensions of the guide increase to E that E is large enough to support 11, 02, and 20

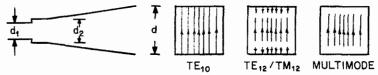


FIG. 15-20 Dual-mode pyramidal horn.

modes as well as the dominant TE_{10} (or TE_{01}). For this reason a tapered transition is needed to transform from purely dominant-mode guide (for which $\lambda < 2d_0 < \sqrt{2}\lambda$) to the input guide of side d_1 . As for the conical case, a constant-dimension phasing section of length ℓ is used to ensure correct phasing at the aperture. The frequency sensitivity is much like that of the dual-mode conical horn, and a pyramidal horn with a 3λ aperture has a useful pattern bandwidth of 3 to 4 percent.

If the aperture is large enough to make the obliquity factors essentially equal to unity $(d \approx 2\lambda)$ and the semiflare angle small enough to render spherical-wave error negligible, the patterns of a multimode horn are given by

E plane
$$E = \sin u/(u) \left(1 + \beta \sqrt{2} \frac{u^2}{\pi^2 - u^2}\right)$$
H plane
$$E = \cos u/\left[1 - \left(\frac{2u}{\pi}\right)^2\right]$$
(15-38)

where $u=(\pi d/\lambda)\sin\theta$ and β^2 represents the fractional TE₁₂/TM₁₂-mode power content relative to unity for the TE₁₀. The interesting range for β is between 0.45 and 0.55, corresponding to a power level in the TE₁₂/TM₁₂ mode between 7 and 5 dB below that in the dominant mode. The patterns shown in Fig. 15-21 were calculated from Eqs. (15-38) for $\beta=0.464$. Note that the main-beam shapes are nearly identical in the two planes down to the -20-dB level, while the first *E*-plane sidelobe level is very low, approximately -45 dB. The second sidelobe in this plane has a level of -31 dB. The *H*-plane first sidelobe has a level of -23 dB. The full HPBW in all planes is $69 \lambda/d^{\frac{\pi}{2}}$.

Flare-angle changes may also be used in a pyramidal horn to generate the hybrid TE_{12}/TM_{12} pair, as shown by $Cohn^{27}$ and illustrated in Fig. 15-22. It is assumed that only the dominant mode propagates at the throat. Conversion to TE_{12}/TM_{12} occurs at the point where the flare angle changes from θ_f to zero. Relative to unity for the TE_{10} mode, the TE_{12}/TM_{12} amplitude is

$$A = j2d\theta_f/(3\lambda_g) \tag{15-39}$$

providing θ_f is small, $\lesssim 23^{\circ}$, and where λ_g is the TE₁₀-guide wavelength corresponding to the waveguide dimension d. It is seen that the hybrid-mode phase leads that of the dominant mode by 90°. Therefore, the constant-diameter section must create a 270° differential shift to obtain correct phasing in the aperture. The length ℓ can be calculated from Eq. (15-36), but in this case

$$\lambda/\lambda_g = [1 - (\lambda/2d)^2]^{1/2}$$
 and $\lambda/\lambda_g' = [1 - 5(\lambda/2d)^2]^{1/2}$

If no phasing section is used (i.e., $\ell=0$), mode conversion still occurs and Eq. (15-39) still holds. This means that the TE_{12} and TM_{12} energy is improperly phased relative to the TE_{11} and performance is that of a simple flared horn with spherical-wave error in the aperture. This complication must be reckoned with in any design.

If it is desired to design a horn to give the patterns of Fig. 15-21, it is required that $|A| = \beta\sqrt{2}$ with $\beta = 0.464$. Thus the condition is $2d\theta_f/(3\lambda_g) = 0.656$. This becomes $\theta_f = 56\lambda_g/d$ degrees [see Eq. (15-37)]. For a small-aperture horn (e.g., $d = 2\lambda$) this condition leads to a relatively large value for θ_f , which may violate the small-angle condition used in deriving Eq. (15-39). In this case two or more separate flare changes may be used, since the A coefficients are additive, but frequency sensitivity will increase. Good pattern performance over a 30 percent band has been reported for the single-flare-change case.

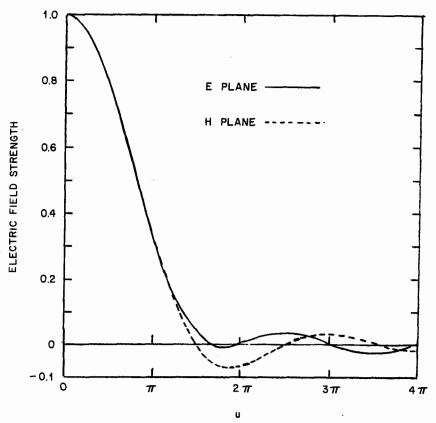


FIG. 15-21 Field-strength patterns of multimode pyramidal horn with $\beta=0.464$ (calculated).

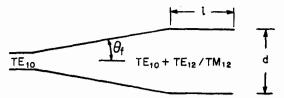


FIG. 15-22 Section through square-aperture pyramidal horn with flare-angle change.

Gain and Impedance

The gain of any of the multimode horns described here can be calculated from

$$G = \eta 4\pi A/\lambda^2$$
 (A = aperture area)
 $G = \eta k^2 a^2$ (conical horn, aperture radius a)
 $G = \eta 4\pi d^2/\lambda^2$ (pyramidal horn, square aperture, side d)

but of course it is necessary to calculate or at least estimate the value of the aperture efficiency η .

In the diagonal horn the power is split equally between the TE_{10} and TE_{01} modes, which are everywhere in phase. Each of these modes has $\eta = 8/\pi^2 = 0.811$; hence this is also the gain factor for a diagonal horn.

In horns employing higher modes the efficiency will be less than that of the dominant mode in all cases described above. This is true because the higher modes that are used for beam shaping do not radiate in the direction $\theta=0$ and hence contribute nothing to the axial gain given above. Thus, for the pyramidal horn of Fig. 15-21 the aperture efficiency for the dominant TE_{10} mode is 0.81, but this mode carries only $1/(1+\beta^2)$ of the power, namely, 82.3 percent for $\beta=0.464$. Hence the net aperture efficiency is $\eta=0.823\times0.811=0.667$. For a dual-mode conical horn the basic efficiency of the dominant TE_{11} mode is 0.837 (Sec. 15-3). Hence the net aperture efficiency for this horn can be expected to be slightly higher, about 69 percent, than for the pyramidal horn. These figures are upper limits and will be lower if the spherical-wave phase error due to horn flare is nonnegligible. In this case the gain may be estimated approximately by reference to the curve for $\kappa a=2.405$ of Fig. 15-33 in Sec. 15-5, dealing with corrugated horns. This curve is roughly applicable to a dual-mode conical horn.

Horns, both conical and pyramidal, that use flare-angle change to generate the higher modes are usually quite well matched, with VSWR typically less than 1.03. However, those using a step discontinuity at the throat may have a VSWR of 1.2 to 1.4. This may be matched out by an iris or a dielectric plug inserted in the input dominant-mode waveguide. The matching device should have axial symmetry if dual polarizations are needed.

15-5 CORRUGATED HORNS

Hybrid Modes

The desirable properties of axial-beam symmetry, low sidelobes, and cross-polarization levels can be obtained over a wide frequency range (1.6:1 or more) in a conical horn or open-ended round waveguide that supports the hybrid HE_{11} mode. This mode is again a mixture of TE_{11} and TM_{11} modes of the form $TM_{11} + \gamma TE_{11}$, where γ is a parameter called the mode-content factor. However, the inner surface of the horn or guide may no longer be a smooth metallic conductor. Instead, the surface must be anisotropic in such a way that it has different reactances, X_{ϕ} in the azimuthal direction and X_{τ} in the axial direction, with $X_{\phi} \rightarrow 0$ while $X_{\tau} \rightarrow \infty$. If these conditions are realized, the TE and TM components become locked together as a single (hybrid) mode and they propagate with a unique common velocity.

Such an anisotropic impedance can be achieved by cutting circumferential slots into the surface, as suggested by Simmons and Kay²⁸ and described by Minnett and Thomas.²⁹ Thus, in Fig. 15-23, which represents a longitudinal section through a cylindrical corrugated waveguide, E_{ϕ} will be zero on the surface of the teeth at $\rho = a$. Each slot acts as a radial transmission line that is short-circuited at $\rho = b$. If the line

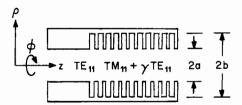


FIG. 15-23 Cylindrical corrugated waveguide with TE₁₁-mode excitation.

length, b-a, is one-quarter guide wavelength, then an open circuit appears across each gap at $\rho=a$. Providing there are several slots per wavelength, then the conditions $X_{\phi} \to 0$, $X_{z} \to \infty$ will be realized in an average sense. Looked at in another way, the open-circuit gaps ensure that no axial current can flow at $\rho=a$. Consequently, H_{ϕ} , the magnetic field which induces axial current flow, must also vanish. On average, the same boundary conditions now prevail for the azimuthal components of both E and E fields at the guide wall. This was conjectured by Simmons and Kay²⁸ and later shown by Rumsey³⁰ to be a condition on the aperture field of a horn that leads to symmetry and freedom from cross-polarization in its radiation pattern.

The properties of corrugated waveguides supporting such hybrid modes are thoroughly treated in the literature. 31,32,33,34 Nevertheless, it is not easy to abstract the fundamentals in a useful and comprehensive way. This is partly due to differences in approach and in notation on the parts of the authors and partly to the inherent complexity of the analysis. As an example of the latter, when the radiation pattern of a hybrid-mode horn is calculated by the Kirchhoff-Huygens method, the condition for symmetry and zero cross-polarization is found to be $\gamma = 1$, but when calculated by the Fourier transform technique the condition obtained is $\gamma = \beta/k$ (where $\beta/k =$ λ/λ_g). Experimentally, it is found that the aperture diameter must be fairly large to obtain the desired performance. This means that β/k must be near unity, and so, of course, the condition becomes $\gamma \rightarrow 1$, but subject to the restriction to reasonably large aperture size. The discussion that follows, rather more tutorial than is customary in a handbook, is presented as a brief eclectic summary of the more important features necessary to an understanding of the radiation characteristics of corrugated horns. Only those modes that vary azimuthally as $\cos \phi$, $\sin \phi$ are treated. These correspond to fields that vary radially as $J_m(\kappa\rho)$, $J'_m(\kappa\rho)$, where m is restricted to the value unity.

With reference to Fig. 15-23, the dominant TE_{11} mode is introduced in the smooth-wall section of round waveguide at the left. Some reflection of this mode occurs at the abrupt junction between the smooth wall and the first slot. In the corrugated section the new boundary conditions ensure that the propagating mode is the hybrid combination symbolically represented by $TM_{11} + \gamma TE_{11}$. This mode has the cylindrical components

$$E_{\rho} = e_{\rho}(\rho) \cos \phi \qquad Z_{0}H_{\rho} = h_{\rho}(\rho) \sin \phi$$

$$E_{\phi} = e_{\phi}(\rho) \sin \phi \qquad Z_{0}H_{\phi} = h_{\phi}(\rho) \cos \phi$$

$$E_{z} = e_{z}(\rho) \cos \phi \qquad Z_{0}H_{z} = h_{z}(\rho) \sin \phi$$
(15-40)

where exp $(-j\beta z)$ is understood, and

$$e_{\rho}(\rho) = -j \left[\frac{\beta}{k} J_{1}'(\kappa \rho) + \gamma \frac{J_{1}(\kappa \rho)}{\kappa \rho} \right]$$

$$e_{\phi}(\rho) = j \left[\frac{\beta}{k} \frac{J_{1}(\kappa \rho)}{\kappa \rho} + \gamma J_{1}'(\kappa \rho) \right]$$

$$e_{z}(\rho) = \frac{\kappa}{k} J_{1}(\kappa \rho)$$

$$h_{\rho}(\rho) = -j \left[\frac{J_{1}(\kappa \rho)}{\kappa \rho} + \gamma \frac{\beta}{k} J_{1}'(\kappa \rho) \right]$$

$$h_{\phi}(\rho) = -j \left[J_{1}'(\kappa \rho) + \gamma \frac{\beta}{k} \frac{J_{1}(\kappa \rho)}{\kappa \rho} \right]$$

$$h_{z}(\rho) = \gamma \frac{\kappa}{k} J_{1}(\kappa \rho)$$

$$(15-41)$$

 β and κ are the propagation constants in the z and ρ directions, respectively, and are related to the free-space wave number by

$$\beta^2 + \kappa^2 = k^2 \qquad (k = 2\pi/\lambda)$$
 (15-42)

By the use of Bessel-function recurrence formulas and a transformation to rectangular coordinates, the x and y components of field are found to be

$$E_{x} \sim (1 + \gamma k/\beta) \cdot J_{0}(\kappa \rho) - (1 - \gamma k/\beta) \cdot J_{2}(\kappa \rho) \cdot \cos 2\phi$$

$$E_{y} \sim (1 - \gamma k/\beta) \cdot J_{2}(\kappa \rho) \cdot \sin 2\phi$$
(15-43)

These will be the transverse components of field in the aperture of the open waveguide in Fig. 15-23 if it is assumed that the aperture is reasonably large so that reflection is negligible. E_x and E_y are respectively the copolar and cross-polar components, and it is clear that the cross-polarization will be zero if $\gamma = \beta/k$. Furthermore, this condition ensures that E_x tapers radially with ρ but does not vary azimuthally with ϕ . However, if $\gamma = -\beta/k$, the aperture field is a mixture of E_x and E_y with strong azimuthal variations.

To satisfy the condition $X_{\phi} = 0$, E_{ϕ} must vanish at $\rho = a$, and Eqs. (15-41) then give

$$\gamma = -\frac{\beta}{k} \cdot \frac{J_1(\kappa a)}{\kappa a J_1'(\kappa a)} = \frac{\beta}{k} \cdot \frac{J_2(\kappa a) + J_0(\kappa a)}{J_2(\kappa a) - J_0(\kappa a)}$$
(15-44)

Thus it is observed that the condition $\gamma = \beta/k$ occurs whenever $J_0(\kappa a)$ vanishes, which happens for $\kappa a = 2.405, 5.520, 8.654...$ In this case the modes are designated HE_{11} , HE_{12} , HE_{13} ..., respectively, and all these modes create purely copolar aperture fields. The condition $\gamma = -\beta/k$ is seen to occur whenever $J_2(\kappa a)$ vanishes; i.e., for $\kappa a = 0, 5.136, 8.417, \ldots$, and these modes are designated $EH_{11}, EH_{12}, EH_{13}...$

The longitudinal reactance X_z (which is infinite only at the slot resonant frequency) is given in the general case by $X_z/Z_0 = je_z/h_\phi$ evaluated at $\rho = a$. Hence, from Eqs. (15-41)

$$X_z/Z_0 = \frac{-\kappa^2 a J_1(\kappa a)}{k\kappa a J_1'(\kappa a) + \gamma \beta J_1(\kappa a)}$$
 (15-45)

Combining Eqs. (15-44) and (15-45) gives

$$\frac{1}{\gamma} - \gamma = \frac{\kappa^2 a}{\beta} \cdot Z_0 / X_z \tag{15-46}$$

and in the special case of resonant slots $(X_r = \infty)$ it follows that $\gamma = \pm 1$. This is called the *balanced* hybrid condition, and the designation HE is used for $\gamma = +1$ and EH for $\gamma = -1$. Because Eq. (15-46) is a quadratic in γ , it has two roots in the general case and the designations HE and EH are still applicable even under unbalanced conditions.

The characteristic equation for HE or EH hybrid modes is obtained from Eq. (15-45) by substituting for γ from Eq. (15-44). Solutions are shown graphically in Fig. 15-24 in the form given by Chu and Legg, ³⁵ in which the quantity κa is plotted as a function of guide circumference ka, with normalized reactance X_z/Z_0 as a parameter. The dispersion characteristics of the corrugated-waveguide modes then follow when β/k (i.e., λ/λ_g) is determined from these solutions for κa , along with the use of Eq. (15-42). β/k is shown in Fig. 15-25 as a function of ka for a number of HE and EH

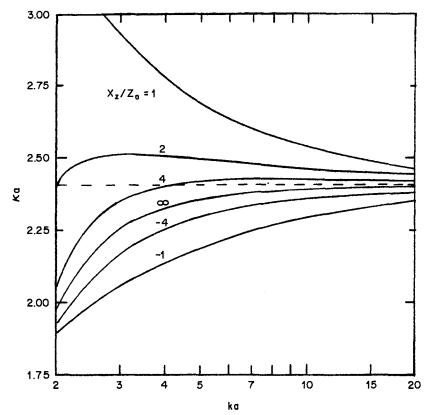


FIG. 15-24 Solutions to characteristic equation; κa versus ka with X_z/Z_0 as a parameter. (© 1982 IEEE; see Ref. 35.)

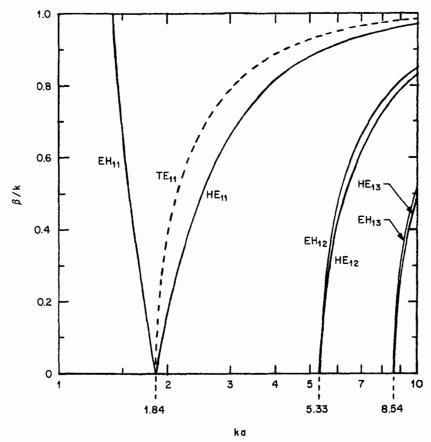


FIG. 15-25 Dispersion characteristics of balanced hybrid modes (TE₁₁ mode also shown for comparison).

modes under the condition $\gamma=\pm 1$. The dashed line, shown for comparison, is the dispersion curve for the dominant TE_{11} mode, for which κa has the constant eigenvalue 1.841. The behavior of the hybrid modes is complicated by the fact that κa is not constant even in the balanced case.

Figure 15-24 shows that the desired condition on the aperture field, namely, $\kappa a = 2.405$, is approached asymptotically when ka is large. In that case β/k approaches unity, and from Eq. (15-44) γ must approach +1. The restriction to large values of ka was pointed out by Knop³³ in the form $ka \geq 2\pi$. On the other hand, Fig. 15-24 also shows that when ka is large, κa will be close to the desired value of 2.405 even when X_r is far from resonance. This means that $J_0(\kappa a)$ will be small and that $\gamma k/\beta$ will not depart greatly from unity despite the fact that X_r changes drastically with frequency. This was noted by Dragone, ³⁶ who also verified experimentally that operation is possible over a frequency range of more than 1.5:1. The value of ka in this

case was 12 at the lowest frequency in the band, corresponding to an aperture diameter of about 4λ . Slot depth at the aperture varied from about 0.21λ to 0.31λ , and in the throat from 0.34λ to 0.51λ . Operation was limited at the high end of the band by the appearance of the unwanted EH_{II} mode.

Slot resonance $(X_z = \infty)$ occurs when slot depth is one-quarter wavelength in the radial line of radii a, b. This depth approaches one-quarter free-space wavelength when ka is large, as shown in Fig. 15-26. The tooth width t in Fig. 15-27 should be small compared with slot width w, say, t < 0.2w, in order to reduce frequency sensitivity. There should be several slots per wavelength, preferably four or more, although in wideband horns it is permissible to have only two per wavelength at the high-frequency end of the band.

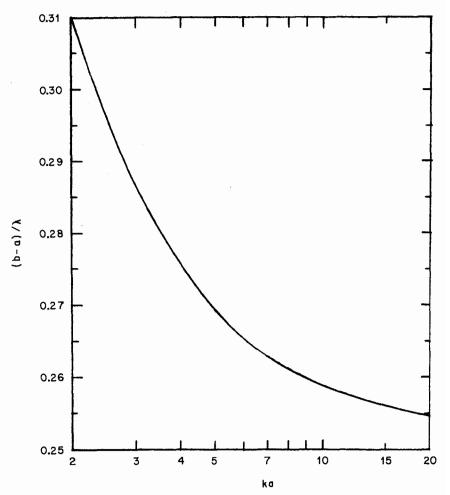


FIG. 15-26 Slot depth, b - a, at resonance. (© 1978 IEEE; see Ref. 37.)

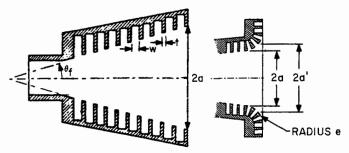


FIG. 15-27 Small-flare-angle corrugated horn at left; corrugations extended into flange at right. (© 1978 IEEE; see Ref. 37.)

Conical Corrugated Horn (Small-Flare-Angle)

Figure 15-27 shows a corrugated horn in which slot depth varies in accordance with Fig. 15-26 in order to satisfy the resonance condition at some midband frequency. The assumption of a small flare angle permits the use of the approximation that the aperture field is just that of a corrugated waveguide of diameter 2a, but with the superposition of a spherical-wave error of the kind discussed in Sec. 15-1. Thus the phase of the field in the aperture will vary quadratically with radius, and the expressions given by Eqs. (15-43) must be multiplied by $\exp(-jk\Delta r^2)$, where $r = \rho/a$ and $\Delta = a^2/(2\ell)$.

The far field of this aperture distribution can be calculated by the Fourier transform method, as in Ref. 33. If the obliquity factors of Sec. 15-1 are suppressed, the field at a distant point P having coordinates $(R, \theta, \phi)^*$ is

$$E_{x}(P) \sim (1 + \gamma k/\beta) \cdot g(u,\Delta) + (1 - \gamma k/\beta) \cdot h(u,\Delta) \cdot \cos 2\phi$$

$$E_{y}(P) \sim (1 - \gamma k/\beta) \cdot h(u,\Delta) \cdot \sin 2\phi$$
(15-47)

where $u = ka \cdot \sin \theta$ $r = \rho/a$ and

$$g(u,\Delta) = \int_0^1 J_0(\kappa ar) J_0(ur) \exp(-jk\Delta r^2) \cdot rdr$$

$$h(u,\Delta) = \int_0^1 J_2(\kappa ar) J_2(ur) \exp(-jk\Delta r^2) \cdot rdr$$
(15-48)

When $\Delta=0$, corresponding to the open waveguide of Fig. 15-23, Eqs. (15-48) are directly integrable and yield

$$g(u,0) = [(\kappa a)^2 - u^2]^{-1} \cdot [\kappa a J_1(\kappa a) J_0(u) - u J_0(\kappa a) J_1(u)] h(u,0) = [(\kappa a)^2 - u^2]^{-1} \cdot [u J_1(u) J_2(\kappa a) - \kappa a J_1(\kappa a) J_2(u)]$$
 (15-49)

These equations show that h(u,0) vanishes, while g(u,0) has its maximum in the axial direction u = 0. The function h(u,0), which determines the shape of the cross-polar pattern, has its first maximum at u = 3.65. Thus the cross-polar component E_v is zero

^{*}This far-field spherical-coordinate system is distinct from the aperture coordinate frame (ρ, ϕ, z) .

on axis and in the principal planes and has peaks in the intercardinal planes ($\phi = \pm 45^{\circ}$) situated approximately where $\theta = \sin^{-1}(0.58\lambda/a)$.

Under balanced hybrid conditions and large ka, i.e., with $\kappa a = 2.405$, and when $\Delta = 0$, Eqs. (15-47) and (15-48) simplify to

$$E_x(P) \sim \frac{J_0(u)}{1 - (u/2.405)^2}$$
 $E_y(P) = 0$ (15-50)

confirming that there is zero cross-polarization and that the copolar pattern is axially symmetric for the HE₁₁ mode. This is also true for the higher-order HE₁₂, HE₁₃, ... modes.

The balanced EH modes correspond to $J_2(\kappa a) = 0$, $\gamma = -\beta/k$, and the far field is then

$$E_x(P) \sim (1 - u^2/\kappa^2 a^2)^{-1} \cdot J_2(u) \cdot \cos 2\phi$$

$$E_y(P) \sim (1 - u^2/\kappa^2 a^2)^{-1} \cdot J_2(u) \cdot \sin 2\phi$$
(15-51)

These modes therefore radiate with a null in the axial direction ($\theta = 0$) and a state of polarization that may be linear, elliptical, or circular, depending on ϕ . They are almost invariably undesirable in antenna engineering applications.

A set of universal patterns for the small-flare horn of Fig. 15-27 is shown in Fig. 15-28 under balanced hybrid conditions and large ka. The patterns were computer-

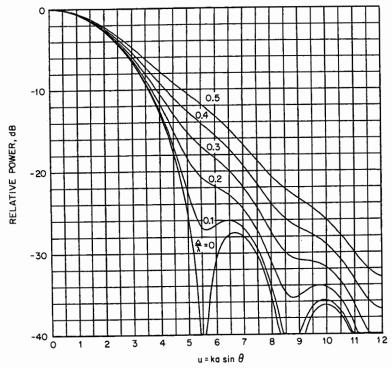


FIG. 15-28 Universal patterns for small-flare-angle corrugated horns under near-balanced conditions.

generated from the first of Eqs. (15-48) and are reasonably accurate for a half-flare angle less than about 20°. According to Thomas, 37 as ka decreases below about 12, the sidelobe level for a given Δ gradually decreases but the shape of the main lobe is virtually unaffected until ka reaches about 6. This is confirmed in Ref. 33. For ka < 6 the flange at the aperture begins to affect the pattern. The patterns become invalid for ka < 4.

When the flange affects the pattern shape (i.e., $ka \approx 6$), a remedy recommended in Ref. 37 is to extend the corrugations into the plane of the flange as indicated in Fig. 15-27. This will preserve pattern symmetry, but it increases the effective aperture size slightly. The new aperture radius is approximately a' = a + e/2, where e is the radius of the curved portion of the flange.

Universal beam-efficiency curves for conical corrugated horns are shown in Fig. 15-29 for various values of the spherical-wave parameter Δ/λ . It has been assumed that the slots are resonant, so $\kappa a = 2.405$, and that the aperture diameter exceeds about 2λ , corresponding to the balanced HE₁₁ mode of operation. Because of this restriction on

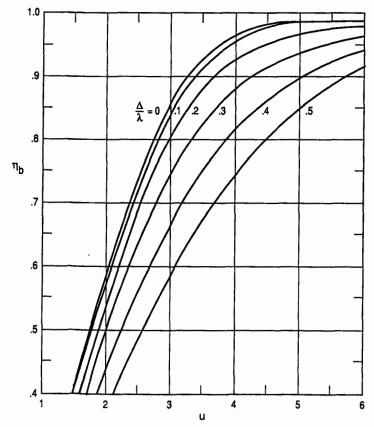


FIG. 15-29 Universal beam-efficiency curves for balanced HE₁₁ mode homs. $\eta_{\rm b}$ versus $u=ka\sin\theta$.

aperture size, they should not be used to predict spillover efficiency for prime-focus-fed symmetric reflector antennas, which commonly have F/D ratios in the range 0.3 to 0.5. They can, however, safely be used for all offset and most Cassegrain reflector systems for which F/D normally exceeds 0.6.

Wide-Flare-Angle Scalar Horn

A wide-flare horn is shown in Fig. 15-30, and it is apparent that the path error in the aperture can become quite large. In this case Eqs. (15-2) are inaccurate, and the

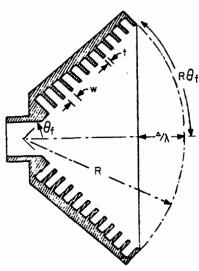


FIG. 15-30 Wide-flare scalar hom. (© 1978 IEEE; see Ref. 37.)

expressions in Eqs. (15-48) and the patterns of Fig. 15-28 are no longer applicable. Such a horn nevertheless may still exhibit axial symmetry and low crosspolarization in its radiation pattern, but pattern calculation becomes considerably more complex, involving spherical rather than cylindrical hybrid modes.32,38 Note that the slots are customarily cut perpendicularly to the horn wall, as in Fig. 15-30, rather than to the horn axis, as in Fig. 15-27. The term scalar horn was coined 28 to emphasize the fact that the far-zone field can be represented by a single scalar quantity under ideal conditions when there is no cross-polarization. Although this is equally true for the small-flare horn, the term scalar horn is usually reserved for the wide-flare case.

A set of universal patterns for scalar horns under near-balanced hybrid conditions is shown in Fig. 15-31, taken from Thomas.³⁷ It is important to note that the

abscissa is now θ/θ_f , where θ is the far-field polar angle and θ_f is the semiflare angle of the horn. Since θ/θ_f is independent of frequency, it is clear that the scalar-horn patterns are, in large measure, frequency-insensitive. This is in direct contrast to the small-flare-horn case, in which beamwidth is proportional to aperture size ka. The transition is determined by the value of Δ as defined in Fig. 15-30 by

$$\Delta = R \sin \theta_f \tan \theta_f / 2 = a \tan \theta_f / 2 \qquad (15-52)$$

For $\Delta < 0.4\lambda$ the beamwidth is controlled mainly by ka and is therefore frequency-dependent. As Δ increases beyond 0.5 λ , this dependence becomes less and less, and when Δ exceeds about 0.75 λ , the nearly frequency-independent conditions shown in Fig. 15-31 result. These patterns are applicable for values of θ_f up to about 70°. As Δ increases beyond 0.75 λ , the beam acquires a flattened top and the skirts become steeper. At $\Delta = 1.25\lambda$ there is actually a slight dip in the axial direction. Figure 15-32 shows the effect of Δ on the beamwidth of scalar horns at various power levels. A good rule of thumb is that the beam angle at the -12-dB level is very close to $0.8 \, \theta_f$, while at the -15-dB level it is very close to $0.9 \, \theta_f$ for any Δ between 0.75λ and 1.5λ .

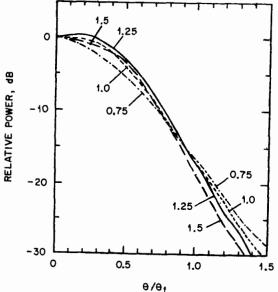


FIG. 15-31 Universal patterns for wide-flare scalar homs (θ_t < 70°) with Δ/λ as a parameter. (© 1978 IEEE; see Ref. 37.)

The spherical-wave error Δ has a marked effect on the location of the phase center of the horn, as can be seen in Fig. 15-33. When Δ is very small, the phase center is on the horn axis very close to the plane of the aperture. As Δ increases, the phase center moves along the axis toward the throat and eventually becomes fixed at the horn apex for scalar horns with $\Delta \lesssim 0.7\lambda$. The bars show the effect of a frequency

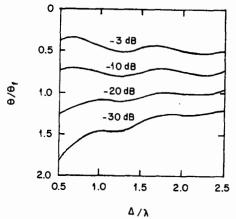


FIG. 15-32 Effect of Δ/λ on the beamwidth of scalar horns at various power levels. (© 1978 IEEE; see Ref. 37.)

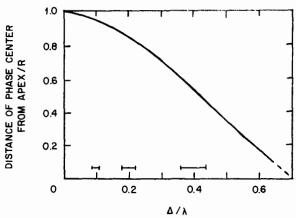


FIG. 15-33 Distance of phase center, normalized relative to slant length *R* from apex. (© 1978 IEEE; see Ref. 37.)

change of ± 10 percent. The beam efficiency of scalar horns is high. When Δ exceeds 0.75 λ , the beam efficiency at the -10-dB level is greater than 87 percent and at the -20-dB level it is greater than 98 percent. This is a valuable asset when such a horn is used as a feed in a reflector antenna since spillover loss will be small.

To design a scalar horn with a given beamwidth at some relative power level, say, -6-dB, one determines θ/θ_f from Fig. 15-31. It is apparent that $\theta/\theta_f = 0.6$ in this case and that the parameter Δ/λ may have any value between 1.0 and 1.5. If the desired beamwidth is $2\theta = 60^{\circ}$, one finds that $\theta_f = 50^{\circ}$, and from Eq. (15-52) R may lie between 2.8 λ and 4.2 λ .

Gain

The conical corrugated horn has certain advantages over the dominant-mode pyramidal horn as a gain standard. It is not subject to the small gain uncertainties¹¹ caused by *E*-plane edge diffraction, its ohmic loss is very small, and it has considerably lower sidelobe levels than the pyramidal horn. The gain of a small-flare corrugated horn has been calculated³⁵ as a function of the phase-error parameter Δ/λ by making use of the aperture field expressions given by Eqs. (15-43). Relative to a uniform circular aperture of the same diameter the gain factor is

$$\eta = \frac{\left| 2(1 + \gamma k/\beta) \int_0^1 J_0(\kappa a r) e^{-jk\Delta r^2} r dr \right|^2}{(1 + \gamma k/\beta)^2 [J_0^2(\kappa a) + J_1^2(\kappa a)] + (1 - \gamma k/\beta)^2 [J_2^2(\kappa a) - J_1(\kappa a)J_3(\kappa a)]}$$
(15-53)

This expression has been computed³⁵ as a function of Δ/λ for three values of κa , namely, 2.3, 2.405, and 2.5. The results are given in Table 15-3 and are shown graphically in Fig. 15-34. It is seen that the gain is not highly sensitive to deviations from the zero cross-polar condition, $\kappa a = 2.405$, and that this is particularly true in the vicinity of $\Delta = 0.5\lambda$. It is clear that Eq. (15-53) is based on the quadratic phase approximation and hence is valid only for small-flare angles ($\theta_f \gtrsim 20^{\circ}$).

TABLE 15-3 Calculated Gain Factor of Small-Flare Corrugated Horn, dB

Spherical-wave phase error Δ/λ	Eigenvalue parameter <i>ka</i>		
	2.3	2.405	2.5
0	-1.27	-1.60	-1.99
0.05	-1.30	-1.61	-2.01
0.10	-1.37	-1.68	-2.06
0.15	-1.50	-1.79	-2.15
0.20	-1.68	-1.95	-2.28
0.25	-1.92	-2.15	-2.45
0.30	-2.20	-2.40	-2.65
0.35	-2.54	-2.69	-2.90
0.40	-2.94	-3.04	-3.18
0.45	-3.39	-3.42	-3.50
0.50	-3.89	-3.86	-3.86
0.55	-4.45	-4.34	-4.26
0.60	-5.07	-4.86	-4.70
0.65	-5.74	-5.43	-5.18
0.70	-6.46	-6.05	-5.70
0.75	-7.22	-6.70	-6.27
0.80	-8.02	-7.39	-6.87
0.85	-8.84	-8.11	-7.50
0.90	-9.66	-8.84	-8.16
0.95	-10.46	-9.57	-8.85
1.00	-11.19	-10.28	-9.55

© 1982 IEEE; see Ref. 35.

The actual gain of the corrugated horn is, of course, $G = \eta(2\pi a/\lambda)^2$. Using the small-flare-angle approximation, $\Delta = a^2/(2\ell)$, allows the gain to be written as $G = 8\pi^2\eta\ell\Delta/\lambda^2$, which shows that for a fixed ℓ/λ the gain is maximized when the product $\eta\Delta/\lambda$ is maximized. This product is plotted in Fig. 15-35 by using the data in Table 15-3. The optimum-gain condition is thus seen to be $\Delta = 0.5\lambda$, and in this region it is clear that the gain is insensitive both to frequency and to small deviations from the condition $\kappa a = 2.405$.

Experimental measurements reported in Ref. 35 on a conical corrugated horn with an aperture diameter 2a=127 mm and $\theta_f=13.5^{\circ}$ are in excellent agreement with values calculated from Eq. (15-53). At 19.04 and 28.56 GHz the calculated values were 24.4 and 25.1 dB respectively. The corresponding measured values were 24.40 \pm 0.08 dB and 24.98 \pm 0.08 dB.

Impedance

A good match between the TE_{11} and the HE_{11} modes at the point at which the corrugations begin can be achieved by making the first slot one-half wavelength deep, then gradually reducing the slot depth until the resonant depth determined from Fig.

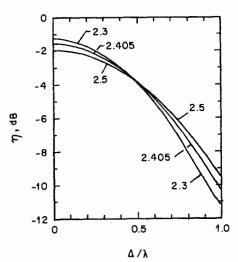


FIG. 15-34 Gain factor η versus spherical-wave error Δ/λ for conical corrugated hom with κa as a parameter. (© 1982 IEEE; see Ref. 35.)

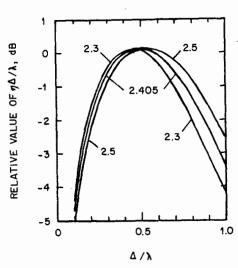


FIG. 15-35 Relative value of $\eta\Delta/\lambda$ versus Δ/λ (i.e., relative gain for fixed ℓ/λ) for a conical corrugated horn with κa as a parameter. (© 1982 IEEE; see Ref. 35.)

15-26 is reached at the band-center frequency. If the depth is tapered over a distance of a wavelength or more, the match will remain good over a wide (1.5:1) frequency range. By making the first few slots close to one-half wavelength deep, the reactance X_z will be close to zero, thus minimizing the discontinuity between the smooth conducting boundary and the corrugated wall.

To prevent generation of the unwanted EH₁₁ mode at the junction of the smooth and slotted guides the reactance X_z should not be positive ($X_z > 0$). Hence it is advisable to make the first slot one-half wavelength deep at the highest frequency in the band.

By following the above practices it should be possible to obtain a VSWR less than about 1.25 over a 1.5:1 frequency range in a scalar horn and to do considerably better in a small-flare horn over a narrower frequency range.

Wide-Band Feed Horn

The structure of a high-performance wide-band horn can be complex, as demonstrated in the design of a Calcagrain feed by Thomas, James, and Greene. They achieved essentially constant beamwidth, low cross-polarization, and low input reflection over a bandwidth ratio of 2.1:1 with a four-section horn. The first section is a smooth-walled, profiled taper from standard round waveguide to a larger-diameter second section which acts as a converter for the HE₁₁ mode. This is the most critical part of the horn because it determines return loss and strongly affects generation of unwanted EH-type modes. Ringloaded slots are employed for greater bandwidth, and dimensions are optimized independently of the conical output which constitutes the fourth section. This requires the use of an intermediate, or third, section acting as a transition device. In this section, the slot depth and pitch change gradually until resonant depth is reached. There is also a gradual change in flare angle to match that of the output section.

The flare angle and length of the output section are such that the spherical wave error Δ exceeds $\lambda/2$ at the lowest frequency in the band. This results in a fixed phase-center location and ensures nearly constant beamwidth over a 2.1:1 bandwidth ratio, such that the relative pattern level is about -17 dB at a radiation angle equal to the output semiflare angle. Over the same band, the return loss is greater than 30 dB and the cross-polarization lobes (in the intercardinal planes) are below -30 dB for output semiflare angles up to 20°. For larger flare angles, the cross-polarization gradually rises, reaching -27 dB when the angle becomes 30°, while the bandwidth ratio decreases to 1.7:1.

Compact, Profiled Corrugated Horns

The small-flare-angle horn, described earlier, tends to be quite long because Δ , the spherical wave parameter at the aperture, normally does not exceed about $\lambda/4$. Furthermore, while it retains good axial-pattern symmetry over a relatively wide frequency range, the beamwidth varies nearly inversely with frequency. Therefore, as a feed for a Cassegrain reflector antenna, it yields high efficiency only over a narrow frequency band.

The wide-flare, or scalar, horn achieves nearly constant beamwidth and good pattern symmetry over a wide frequency range (1.5:1 or more) as long as the parameter Δ exceeds about $\lambda/2$. However, it has an aperture diameter considerably larger (by 20 to 25 percent) than the small-flare horn, and this can cause excessive blocking when it is used as a prime-focus feed in a symmetric paraboloid. As a Cassegrain feed it tends to be both lengthy and builty.

These shortcomings are mitigated in the compact, profiled corrugated horn in which the flare angle is not constant. Thus the horn has an axial profile that is curved rather than displaying a simple linear taper. By using an input section with ring-loaded slots to effect conversion from the TE₁₁ to the HE₁₁ mode, followed by a specially chosen profiled section, James⁴⁰ was able to achieve satisfactory performance over a frequency range of 2.4:1 from a horn significantly smaller than the conventional scalar horn. Since the cross-polarization level is not high and beamwidth and phase-center movement are not severe, this compact horn can be recommended as a feed whenever space is at a premium at the secondary focus of a dual-reflector antenna.

Olver and Xiang⁴¹ have described the design of a horn in which the curved profile is approximated by a small number (five) of linearly tapered sections of different flare angles. In the input section the first slot is $\lambda/2$ deep; slot depths then successively decrease until a value of 0.26λ is reached, at which point the depth remains constant throughout the remaining sections. This ensures that the reflection coefficient at the input will be small. At each junction, where the flare angle changes discontinuously, a certain amount of power conversion to the HE₁₂ mode takes place. The junction positions are therefore carefully chosen to ensure that the phases of these unwanted contributions are such that the total HE₁₂ power is very small at the radiating aperture. This results in a phase-center location close to the aperture plane and a nearly constant phase pattern over the useful part of the main beam. An experimental model with aperture diameter of 5.2λ and length of 4.8λ demonstrated phase uniformity to within 15° between the -12-dB pattern levels that occur at $\theta = 15^{\circ}$. The useful bandwidth is at least 20 percent.

Two-Hybrid-Mode Horns

Additional beam shaping is possible in a corrugated horn by generating higher-order hybrid modes along with the HE_{11} . The desired higher-order modes are the HE_{12} , HE_{13} , ..., all of which have axially symmetric patterns that are free of cross-polarization under near-balanced conditions, i.e., large aperture and $\gamma \rightarrow 1$. However, the higher-order modes have different dispersion characteristics, as seen in Fig. 15-25, and this causes such horns to be quite frequency-sensitive. For this reason and also because of difficulties in generating the higher modes in the correct amplitude ratios, only the two-hybrid-mode horn has seen any practical use.

The two-mode horn utilizes only the HE_{11} and the HE_{12} modes, both of which can be generated by a step discontinuity in the throat of a corrugated horn as shown

in Fig. 15-36. The smooth-wall input guide supports only the TE_{11} mode, so that 1.84 < ka < 3.83. In the corrugated region beyond the step the radius is a_0 , and it must be large enough to support the HE_{12} as well as the HE_{11} mode but not so large as to support the HE_{13} mode. Thus, Fig. 15-25 shows that $5.33 < ka_0 < 8.54$. Thomas⁴² states that a signifi-

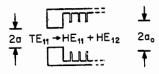


FIG. 15-36 Two-hybrid-mode generation at a step discontinuity.

cant improvement in the match near cutoff can be obtained by a gradual tapered increase in the diameter of the input guide near the step. This does result, however, in a slight reduction in the relative power of the HE_{12} mode for a given diameter a_0 in the corrugated region. The HE_{12} -mode power relative to that of the HE_{11} mode increases as the ratio a_0/a increases; unfortunately a small amount of the EH_{12} mode

is also produced. The presence of this mode is undesirable since it causes a significant increase in cross-polar radiation.

The radius a_0 in the corrugated section should be chosen so that ka_0 is close to 8.54, the cutoff for the HE_{13} mode, at the uppermost frequency in the band of interest. If the mismatch at the upper frequency is then too large, the radius a_0 must be decreased somewhat. A compromise also must be made in regard to the TE_{11} input-guide diameter. Large values of a (ka near 3.83) lead to a low VSWR and a low level of the unwanted EH_{12} mode but may not result in sufficient power in the HE_{12} mode. Values between 2.5 and 3.0 for the ratio a_0/a have provided satisfactory results.

Because the two modes have different propagation constants (Fig. 15-25), the two-hybrid-mode horn must usually incorporate a constant-diameter $(2a_0)$ phasing section before it flares to its final aperture diameter. This is to ensure that the modes are in the correct phase at the aperture and is exactly analogous to the use of a phasing section in the dual-mode conical horn of Fig. 15-14.

The pattern of a two-hybrid-mode horn having $ka_0 = 8.17$ at the aperture (there is no flare) is shown in Fig. 15-37.⁴³ In this case the length of the corrugated section (of diameter $2a_0$) is such as to antiphase the main lobes of the HE₁₁ and HE₁₂ radiation patterns; this creates the dip in the resultant pattern in the direction $\theta = 0$. The phase relationship will change with frequency, and so, of course, will the pattern shape. This horn was designed as a highly efficient feed for a radiotelescope reflector antenna having an opening angle $\theta = 63^{\circ}$ at the rim. Similar feeds described in Ref.

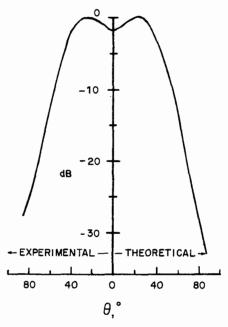


FIG. 15-37 Experimental and theoretical patterns of a two-hybrid-mode hom with ka_0 = 8.17. (Courtesy IEEE; see Ref. 43.)

42 have bandwidths of a few percent. The relative power levels in the two modes are about equal. The pattern in Fig. 15-37 obviously has desirable characteristics in earth-coverage use from a satellite in a high-altitude circular orbit.

A two-mode horn of this kind has been designed and tested⁴⁴ for use on Navstar satellites of the Global Positioning System, orbiting at an altitute of 20,200 km. It has a length of 14.7 cm and an aperture diameter of 4.29 cm, which is almost exactly twice that of an optimized single-mode horn. The gain at edge of coverage (EOC), 14.3°, is a minimum of 15.7 dB over a band of 2 GHz in the 44-GHz military communication band. This is 1.7 dB higher than the gain of the optimized single-mode horn at EOC, a considerable improvement.

Rectangular Corrugated Horn

Sectoral and pyramidal horns excited by the TE_{10} mode in a rectangular waveguide may also benefit from the use of corrugations in the electric (i.e., broad) walls of the horn. ^{45,46} The effect of the corrugations is to make the magnetic field small or zero at the electric walls, analogously to the vanishing electric field at the magnetic walls. As a result the *E*-plane beamwidth is broadened, and the sidelobes are greatly suppressed.

In a square-aperture horn with corrugations in the electric walls the E- and H-plane patterns will be very nearly identical, at least to the -20-dB level, and this can be achieved over nearly a 2:1 frequency range.⁴⁶ Such a horn, however, is restricted to a single polarization, namely, that in which E is orthogonal to the corrugated walls.

In principle, a dual or circularly polarized horn can be constructed by corrugating all four walls of a square-aperture pyramidal horn. In practice, these horns have generally been found to suffer from impedance irregularities and deviations from axial-beam symmetry when wideband (1.5:1) operation is desired. They apparently have not found the favor accorded conical corrugated horns and will not be further discussed. However, dielectric-lined rectangular and square waveguides have been shown⁴⁷ to support hybrid modes of the type HE₁₁. This offers promise that some of the drawbacks noted above for the square-aperture hybrid-mode horn may be overcome.

15-6 NEW TOPICS

Soft and Hard Boundaries for Horns

In acoustics there are surfaces that are termed either hard or soft, on the basis of whether there is intense power flow along the surface or no power flow at all close to the surface. That there is an analogous situation for electromagnetic waves has been pointed out by Kildal⁴⁸ and further discussed in Kildal⁴⁹ and Kildal, Lier, and Aas.⁵⁰ The inner surface of the corrugated horn described in Sec. 15-5 is an example of a soft surface at the slot resonant frequency. Hard surfaces also exist in electromagnetics. An example is a longitudinally corrugated surface in which the slots are filled with dielectric.

The concept of surface impedance is useful in understanding the electromagnetic case, and since resistance is zero for a perfect conductor, its surface impedance is purely reactive, that is, Z = jX. For the corrugated horn, this quantity is anisotropic; in the circumferential direction it is defined by

$$Z_{\phi} = jX_{\phi} = \frac{E_{\phi}}{H_z} \tag{15-54}$$

while in the axial direction it is given by

$$Z_z = jX_z = \frac{-E_z}{H_\phi}$$
 (15-55)

 E_{ϕ} must be zero on the conducting teeth; hence, from Eq. (15-54) it follows that $X_{\phi} = 0$. The field in the horn, however, is known to satisfy the relation for axial-pattern symmetry, that is,

$$Z_{\phi}Z_{z} = -X_{\phi}X_{z} = Z_{0}^{2} \tag{15-56}$$

which is derived from Rumsey's condition.³⁰ This can happen only if $Z_z = \infty$ or, equivalently, $X_z = \infty$, and Eq. (15-55) then shows that $H_{\phi} = 0$, as was pointed out in the introduction to Sec. 15-5.

Because both E_{ϕ} and H_{ϕ} are zero at the inner surface of the corrugated horn under balanced conditions, it follows that the axial component of the Poynting vector also must be zero, and there will be no axial power flow along the surface. The corrugated surface is therefore soft, and the horn itself is referred to as a *soft horn*. Other methods of devising soft horns will be described later.

The surface reactance conditions for a soft horn are

$$X_{\phi} = 0 \quad \text{and} \quad X_{z} = \infty \tag{15-57}$$

as indicated above. For a hard horn, the conditions were chosen by Kildal⁴⁸ to be the inverse of these (for reasons which will become apparent below), namely,

$$X_{\phi} = \infty \quad \text{and} \quad X_z = 0 \tag{15-58}$$

Since it is possible for these anisotropic reactances also to satisfy the condition (15-56), the implication is that a hard horn also may radiate an axially symmetric pattern. Equation (15-58) together with Eqs. (15-54), (15-55), and (15-40) immediately show that both e_z and h_z must vanish at the horn's hard inner surface, that is, at $\rho = a$. Inspection of the field equations in Eq. (15-41) shows that the radial-separation constant κ must then vanish, and this therefore means that the e_z and h_z field components are zero everywhere within the interior of the horn. The mode is, in fact, TEM, and since $\beta = k$ when $\kappa = 0$, it propagates with the speed of light.

It might seem that in such a degenerate mode, all field components would vanish, but reference to the field equations in Eq. (15-41) shows that this is not necessarily the case. It is found that the transverse components become

$$e_{\rho} = -e_{\phi} = h_{\rho} = h_{\phi} = -j(1+\gamma)/2$$
 (15-59)

which are nonzero and independent of ρ . The value of the mode-content factor γ is quite immaterial. If it is zero, then the mode can be said to be a degenerate form of TM_{11} ; if it is infinite, it is a degenerate form of TE_{11} . The mode also can be regarded as degenerate HE_{11} if $\gamma = 1$; if $\gamma = -1$, however, all components vanish. The components in Eq. (15-59) show that the Poynting vector is z-directed, constant, and also independent of ρ , as befits the hard surface. Furthermore, Eq. (15-43) indicates that the aperture field contains only the component E_x ; the cross-polar component E_y is zero. This is a uniform field, and in the absence of spherical wave-phase error, it will radiate with 100 percent aperture efficiency and -17.6-dB first sidelobes. By comparison, the ideal soft horn has 69 percent efficiency,

-27.5-dB first sidelobes, and a half-power beamwidth that is 28 percent larger than that of the ideal hard horn of the same aperture diameter.⁵¹ Specific examples of hard horns will be described later.

Soft Horns with Dielectric Lining

As an alternative to the corrugated horn, a smooth-wall horn can support both HE and EH hybrid modes if it is loaded internally with dielectric material. A solid dielectric cone, separated from the wall of the horn by a thin layer of lower-permittivity material (or air), allows the balanced HE₁₁ mode to radiate^{52,53} if, at the aperture (assumed to have a large diameter), the thickness of the layer is t, given by

$$t = \frac{\lambda}{4\pi\sqrt{\epsilon_1 - \epsilon_2}} \ln \frac{\sqrt{\epsilon_1} + \sqrt{\epsilon_2}}{\sqrt{\epsilon_1} - \sqrt{\epsilon_2}}$$
 (15-60)

where ϵ_1 is the permittivity of the cone and ϵ_2 is that of the layer, with $\epsilon_1 > \epsilon_2$. Spherical wave-phase error in the aperture of the horn may be corrected easily if the outer surface of the cone is made ellipsoidal instead of planar so that it acts as a lens. This surface may require a quarter-wave matching plate in order to reduce the mismatch.

A smooth-wall horn with a simple layer of dielectric on its inner wall also can support balanced, or nearly balanced, hybrid modes. ⁵⁴ An asymptotic solution which is valid for large diameters ($ka \gg 1$) shows that if the thickness of the layer t and its relative permittivity satisfy

$$\tan kt \sqrt{\epsilon - 1} = \sqrt{\epsilon} \tag{15-61}$$

then the condition given in Eq. (15-44) is realized, and hybrid modes propagate. A modification that results in a wider bandwidth for low cross-polarization also has been described. In this case, circumferential corrugations are cut in the inner surface of the dielectric liner, creating an anisotropic surface impedance. There are many of these corrugations per wavelength, and the gap width is made equal to the tooth width. A groove depth of about 0.08a gives good performance for relative permittivities greater than about $\epsilon = 6$ over a wavelength range such that 14 < ka < 18. The grooves are cut completely through the dielectric liner to the metal wall. The fields in the dielectric layer are quite small in a properly designed horn, but there is some radiation from this region that can degrade the axial symmetry of the horn's radiation pattern and lead to an increase in the cross-polarization in the intercardinal planes. This effect is greatest in horns with a small aperture diameter.

Another modification of the smooth-wall horn with a lining of dielectric on the inner wall also gives wider bandwidth for hybrid-mode operation and low cross-polar radiation. ⁵⁶ In this "strip-loaded" horn, the inner surface of the dielectric is coated with periodic circumferential bands of thin, metallized strips which provide an anisotropic surface impedance. In general, there are several bands per wavelength, and the width of the metallized strips is small compared with the total width of a band. For large ka, the thickness of the dielectric approaches

$$t = \frac{\lambda}{4\sqrt{\epsilon - 1}} \tag{15-62}$$

A small-diameter circular waveguide with a partial dielectric filling also can support hybrid modes and makes an efficient feed for a front-fed paraboloid.⁵⁷ The guide has a

diameter of 0.8λ and is fitted with a hollow plug of nylon ($\epsilon = 3$). The length of the plug is 0.75λ , and its inner diameter is 0.30λ . As a feed for a paraboloidal reflector it yields an overall aperture efficiency of 70 percent for F/D = 0.3 and 75 percent for F/D = 0.35.

Absorber Lined Horns

It has been shown that a horn with a lossy dielectric layer can support nearly balanced hybrid modes³⁴ when the horn diameter is large $(ka \gg 1)$. The thickness of the layer and the dielectric-loss tangent should be large enough to ensure that one-way transmission is attenuated by at least 10 to 15 dB. In this case, the eigenvalue κa will be close to the desired value, 2.405, and it will have a small imaginary part. As a consequence, the propagation constant also will have a small imaginary part, which means that the HE₁₁ mode will suffer a slight ohmic loss. There is then no upper limit to the frequency of hybrid-mode operation. The absorber thickness decreases as ϵ' and ϵ'' increase, and in a horn with large ka, the field radiated from the absorber annulus will be negligible. These important results were first discovered by Knop et al., ⁵⁸ who have demonstrated nearly balanced HE₁₁ mode operation in a horn reflector with an aperture diameter of 85.5 in. An absorber dielectric with $\epsilon' = 1.4$ and $\epsilon'' = 0.56$ lines the upper part of the cone and enables it to operate from 4 to 12 GHz, the upper limit in the frequency being set by the nature of the waveguide launcher at the throat of the horn. The ohmic loss is less than 0.5 dB over the band.

A conical horn lined with magnetically lossy material has been shown to exhibit hybrid-mode operation⁵⁹ but at the expense of 10 dB of ohmic loss. In a different version,⁶⁰ the loss was considerably reduced, being between 0.8 and 2.7 dB.

Hard Horns

An early embodiment of a hard horn was described in a 1979 paper by Kumar, 61 although he did not use the term *hard*. He analyzed the propagation and radiation characteristics of an open-ended round-waveguide feed with a diameter of 3.0 cm, having a lining of dielectric with a thickness of 0.3 cm and $\epsilon = 2.6$. This feed showed a measured aperture efficiency between 91 and 96 percent, with cross-polar levels below -27 dB, over the frequency range 8.0 to 10.5 GHz. The -10-dB beamwidths were nearly equal in the E and H planes and varied from 99° at 10.5 GHz to about 123° at 8.0 GHz.

A longitudinally slotted, small-flare-angle conical horn has been shown to radiate patterns with nearly equal beamwidths in all planes and with low cross-polarization. 62 The effect of the slots is to decrease the eigenvalue κa of the TE₁₁ mode (i.e., increase the cutoff wavelength) from its normal value of 1.84 in smooth-wall guide to about 1.1. The modal fields become modified in such a way as to create an approach to a uniform aperture illumination with a low level of cross-polarization, as in a hard horn.

If the eigenvalue κa could be made to vanish, the horn would be truly hard and would have no cutoff, as was discussed earlier. It has been shown that this condition can be achieved if the longitudinal slots are filled with a dielectric material. The geometry of such a horn is shown in Fig. 15-38. There must be a sufficiently large number of slots around the horn's circumference to ensure that the slot width is small enough that there can be only a constant ϕ component of electric field in the slots themselves but no z component. With dominant TE₁₁ mode excitation at the throat of the horn, the fields in the central region will retain that form with $E_z = 0$, but the eigenvalue will no longer be 1.84. The characteristic equation, obtained in Ref. 63 by making E_{ϕ} and H_z continuous across the boundary at $\rho = a$, is



FIG. 15-38 Geometry of longitudinally slotted horn with dielectric in slots.

$$\frac{J_1'(\kappa a)}{\kappa a J_1(\kappa a)} = \frac{-1}{Ka} \cdot \frac{J_1(Ka) Y_1(Kb) - J_1(Kb) Y_1(Ka)}{J_0(Ka) Y_1(Kb) - J_1(Kb) Y_0(Ka)}$$
(15-63)

where Y_0 and Y_1 are Bessel functions of the second kind and

$$\kappa^2 = k^2 - \beta^2$$
 $K^2 = k^2 \epsilon - \beta^2$
 $K^2 = k^2 (\epsilon - 1) + \kappa^2$
(15-64)

hence

In this derivation it has been assumed that the tooth width is small compared with the gap width for each of the slots. The first root of this equation is the value of κa that determines the propagation characteristics of the lowest-order mode through Eq. (15-64). Solutions obtained by Aly and Mahmoud⁶³ are shown graphically in Fig. 15-39 for values of ka equal to 5, 10, and 15 and for relative permittivities between 1 and 3.5. In all cases for which $\epsilon > 1$ it is seen that there is a value of slot depth that makes κa vanish. In this case, the surface at $\rho = a$ is truly hard as far as the fields in the central region are concerned.

When $\kappa a = 0$, Eq. (15-64) shows that

$$K = k\sqrt{\epsilon - 1} \tag{15-65}$$

Furthermore, the left side of Eq. (15-63) becomes infinite, which requires that the denominator of the right side must vanish, that is,

$$J_0(Ka)Y_1(Kb) = J_1(Kb)Y_0(Ka)$$
 (15-66)

A solution to Eq. (15-66) is easily obtained when Ka is large enough to permit use of the asymptotic forms for the Bessel functions. It is then found that

$$\cos K(b-a)=0$$

Hence $K(b-a) = \pi/2$, $3\pi/2$, etc. Using the first root for the lowest-order mode, along with Eq. (15-65), then determines the slot depth that makes $\kappa a = 0$, namely,

$$(b-a)\sqrt{\epsilon-1} = \frac{\lambda}{4} \tag{15-67}$$

Above the frequency that makes κa vanish, the eigenvalue becomes imaginary and the mode becomes a slow surface wave, which is generally undesirable. At that critical frequency the field in the central aperture is uniform and free of cross-polarization, but there is a ϕ component of the electric field in the slots. The latter will contribute little to the copolar far-field radiation pattern as long as the slot depth, b-a, is small compared with the central radius a. The slot field radiation, however, will affect the overall cross-polar

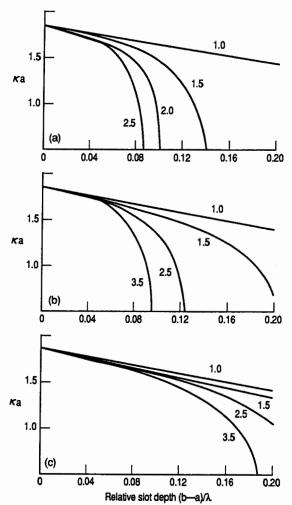


FIG. 15-39 Eigenvalue κa versus relative slot depth $(b-a)/\lambda$, with ϵ as parameter. (a) ka=15, (b) ka=10, (c) ka=5. (Courtesy IEE; see Ref. 63.)

pattern in such a way that minimum cross-polarization, which occurs in the 45° planes, will now happen at a small, nonzero value of κa .

Reference 63 shows a computed pattern for a horn of this type having a flare angle of 10° and an aperture for which ka = 12.25. The slot depth at the aperture is such that b = 1.1a, the dielectric in the slots has $\epsilon = 2.5$, and κa appears to be close to zero. The main lobe is a very close match to that expected of a uniformly illuminated aperture, that is, $J_1(u)/u$, and is identical in both the E and H planes with a first null at 18° . The first two sidelobes in the E plane are at relative levels of -17.5 and -23.5 dB, almost exactly those of the uniform aperture. In the H plane they are each about 2.5 dB lower, possibly due to

the influence of the field radiated by the slots. The horn has a bandwidth of about 13 percent for a cross-polar level of -30 dB or less. This bandwidth decreases as ϵ increases.

A strip-loaded dielectric-lined hard horn has been described⁶⁴ whose performance is very similar to that of the longitudinally slotted horn above. The metallized strips run longitudinally in this case, and the thickness of the dielectric is again given by Eq. (15-67) when ka is large. The hard horn as an element in a cluster feed for satellite reflector antennas has the potential for a considerable reduction in spillover.⁶⁵ A lining of dielectric has been shown to be capable of creating a hard boundary in square waveguide,⁶⁶ but little information is available on the radiation behavior of such a horn.

Soft Horns with Elliptical Apertures

It has been shown⁶⁷ that a radiation pattern with low sidelobes, elliptical cross section, and circular polarization at every field point can be obtained from an elliptical-aperture horn if its walls are anisotropic in such a way as to form a soft boundary. This can be achieved by the use of appropriate corrugations⁶⁸ that will generate HE₁₁-type modes. Because of the elliptical cross section in the horn, there will be two hybrid modes that are spatially orthogonal. The mode in which the transverse electric field is parallel to the minor diameter of the ellipse is called an *even mode*. Its orthogonal counterpart, having a transverse electric field parallel to the major diameter, is called an *odd mode*. It has been shown that for each even mode there exists an odd mode having the same propagation constant. Furthermore, the two modes will have identical, but non-axially-symmetric radiation patterns with orthogonal polarizations. It then follows that if the two orthogonal modes are excited in such a way as to have equal amplitudes and a 90° phase difference, the radiated field will be everywhere circularly polarized.

Although the theory of hybrid modes in an elliptical horn is complex, a satisfactory engineering design may be based on use of the data given in Sec. 15-5 for round corrugated horns to determine slot depth and pitch. It is assumed that in the principal planes of the elliptical horn (i.e., the planes containing the major and minor axes) the radiation patterns will be approximately the same as those of round horns of corresponding aperture diameters. If ka and kb are moderately large, where a and b are the major and minor aperture radii, it is permissible to use constant depth in any one slot, rather than one that varies with the angle ϕ . This greatly simplifies construction of the horn.

Unless the flare angle of the horn is small, in which case the horn becomes very long, there will be a sizeable spherical-wave error in the plane of the major aperture diameter if a is two or three times larger than b. This can have two undesirable effects: it will broaden the pattern in the major plane, and it will result in different phase-center locations in the major and minor planes. The latter is undesirable if the horn is to be used as a feed. The former seems to imply that the major diameter should be increased in order to compensate for the broadening, but this would only increase the spherical-wave error and would further aggravate the situation. A satisfactory remedy is to use a lens in the aperture to remove the phase error entirely. For best results it has been found necessary to match both surfaces of the lens. These procedures were found to provide a satisfactory design for the feed horn in an elliptically contoured offset reflector that created a circularly polarized beam with widths of 3.0 and 6.0° at the -4-dB level. The antenna was intended to provide efficient coverage of the continental United States from a satellite in geostationary orbit.

Dielectric loading may be used in lieu of corrugations to generate elliptically shaped beams with good circular polarization over a broad band. 69,70 Both elliptical- and rectangular-aperture horns have been used successfully for this purpose.

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Lens Antennas

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16-1	Basic Lens Operation 16-2	
16-2	Lens-Surface Formulas for $n > 1$ 16-3	
	Single Refracting Surface, $n > 1$ 16-3	
	Two Refracting Surfaces, $n > 1$ 16-5	
	Zoning Formulas, $n > 1$ 16-6	
	Effects of Zoning on Aperture Illumination, n	
	> 1 16-6	
	Bandwidth of Zoned Lenses, $n > 1$ 16-7	
16-3	actors Affecting Gain and Sidelobe Levels of	
	Lens Antennas 16-7	
	Spillover Loss 16-8	
	Effect of Lens Shape on Aperture	
	Illumination 16-8	
	Dissipation Loss in Lens Media 16-8	
	Reflections from Lens Surfaces 16-8	
16-4	Lens-Surface Formulas for $n < 1$ 16-9	
16-5	Metal-Plate and Waveguide Media 16-12	
	Limitations on Metal-Plate Spacing and	
	Rectangular-Waveguide Width 16-12	
	Reflection and Transmission at an	
	Interface 16-13	
	Methods of Reducing Reflection Losses 16-16	
16-6		
16-7	Rootlace-Type Lenses 16-19	

16-8 Phased-Array Lenses 16-23
 16-9 Dome Antennas 16-23
 16-10 Luneburg Lenses 16-26
 16-11 Fresnel Zone Plate Lenses 16-27

Lenses and reflectors (Chap. 17) are used as collimating elements in microwave antennas. Reflectors have a single degree of freedom (the reflector surface), have no internal loss, have low reflection loss, have no chromatic aberration, are relatively easy to support, and can be perforated to reduce weight and wind loads. Lenses have up to four degrees of freedom [inner surface, outer surface, index of refraction n, and (for constrained lenses) inner- versus outer-surface radiator positions], have no aperture blockage by the feed, have internal and surface-reflection losses, must be edge-supported, and are relatively heavy and bulky. In general, if a reflector can provide the required performance for a given application, it should be used. However, since lenses are more versatile, especially in wide-scan-angle performance, they are used in many applications that do not require the greater flexibility of a phased array.

The methods for determining radiation-pattern characteristics from an aperture (amplitude and phase) distribution, including deviations from desired distributions, are derived and discussed in Chap. 2. Lens applications are discussed in several other chapters and are only suggested in this chapter. References I to 6 contain summaries of most lens types and list a number of references. The material in Ref. 1 is the basis of this chapter, and many sections are only updated; however, the section on artificial dielectric materials is not repeated here.

Some microwave lenses are adapted directly from optics, but microwave antennas generally use only a single element since multielement designs common in optics are generally too bulky and heavy for microwave applications. However, several techniques are available at microwave frequencies that permit specialized designs which are difficult, if not impossible, to use at optical frequencies; these techniques include nonspherical lens surfaces, artificial dielectric materials, constrained and geodesic media, and variable n with position in the media.

Lenses are designed to collimate one wavefront into another by using ray tracing on the basis of the law of the optical path that all rays between wavefronts (or phase fronts) have equal optical path lengths and of the application of the Fresnel equations (Snell's law plus polarization effects) at the lens surfaces. The lenses discussed in this chapter collimate a spherical or cylindrical wavefront produced by a point or line source feed into a planar or linear wavefront; i.e., they are focused at infinity. In practice, however, complex feeds can be used since performance does not deteriorate rapidly with small off-axis feed displacement. Other lens designs have limited application at microwave frequencies.

Figure 16-1 shows two ways of achieving lens designs; in methods a and b rotational lenses are used in conjunction with a point-source feed (the term rotational means that the surfaces of the lens are obtained by revolution of a curved line about the lens axis), while in methods c and d cylindrical lenses (i.e., lenses whose surfaces are generated by moving a straight line perpendicularly to itself) are used in conjunction with a line-source feed.

At microwave frequencies, natural homogeneous dielectric media always have n > 1 (i.e., a phase velocity less than that of light in free space), which leads to the convex lens shapes of Fig. 16-1a and c. However, artificial or fabricated media may be constructed with a range of n from $n \gg 1$ to $n \ll 1$. Examples of lenses constructed with n < 1 are shown in Fig. 16-1b and d, where it is seen that a concave shape is required to focus a beam. In general, the types having n < 1 are highly dispersive

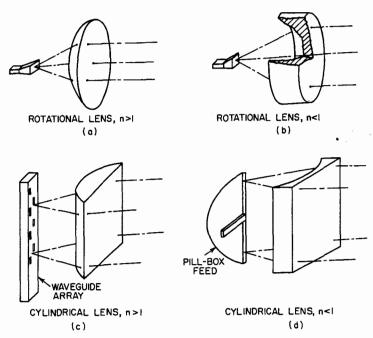


FIG. 16-1 Basic lens configurations.

(i.e., n varies rapidly with frequency), while those having n > 1 are nondispersive. Thus lenses having n < 1 are usually limited to small frequency bandwidths, while lenses having n > 1 may be designed to operate over an octave or more.

16-2 LENS-SURFACE FORMULAS FOR n > 1

Common shapes for n > 1 media lenses are shown in Fig. 16-2; all are single-degree-of-freedom, single-focal-point lenses because either they refract at only one surface or one surface is fixed during the design. The formulas given in the figure apply to both rotational and cylindrical surfaces.

Single Refracting Surface, n > 1

The lenses in Fig. 16-2a-d refract at only one surface. In lenses a to c, refraction occurs at the inner surface (adjacent to the focal point) and in lens d at the outer surface. In each case, the nonrefracting lens surface is parallel to a wavefront. The lens-surface formulas in Fig. 16-2 are derived by equating the optical-path length of a general ray to that of the central ray from an on-axis point at a distance f from the inner surface to a planar wavefront perpendicular to the axis; for example, for the lens in Fig. 16-2a, the relation is $r = f + n (r \cos \theta - f)$, which can be easily manipulated

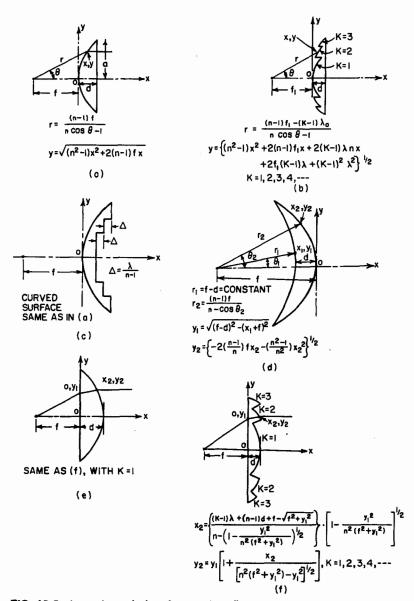


FIG. 16-2 Lens-shape designs for n > 1 media.

into the form given in Fig. 16-2a, a hyperbola. The feed is located at the focal point farthest removed from the inner surface.

A disadvantage of this type of lens is that reflections from the nonrefracting surface will converge at the focal point, since the surface is coincident with a wavefront, and cause a feed-line mismatch approximately equal to the surface-reflection coefficient. It is desirable that this surface reflection be either prevented from entering the

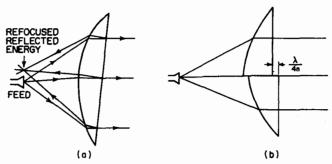


FIG. 16-3 Reduction of feed VSWR by (a) lens tilt and (b) quarter-wavelength displacement of half of the lens.

feed line or eliminated. A high feed-line voltage standing-wave ratio (VSWR) may be avoided by using a ferrite isolator, by tilting the lens slightly (as in Fig. 16-3a) so that the reflected energy will be refocused off the feed, or by displacing half of the lens a quarter wavelength (in the lens medium) along the axis with respect to the other half (as in Fig. 16-3b) so that reflections from the two lens halves are 180° out of phase and create a null at the feed center. These methods have been found to be effective in reducing the feed-line VSWR; however, they do not eliminate the other effects of surface reflection, such as loss of gain and increase in sidelobe level. Whenever these factors are important, the surface-matching techniques to be described later are recommended. Avoiding feed-line mismatch by the technique of Fig. 16-3a depends on low wavefront distortion for small off-axis feed displacements. Analysis⁷ of aberrations due to feed displacement from the focal point shows that coma is the predominant term that limits performance, that come is reduced as focal length and n are increased, and that the coma for a large-n hyperbolic lens is twice that for an equivalent-focallength paraboloidal reflector. Although this is not usually necessary for small lenses, if the technique of Fig. 16-3b is used for large-diameter lenses, the two lens halves should be designed with different focal lengths.

These lenses may be constructed with natural dielectric materials and artificial delay media. Kock⁸ developed a number of artificial delay media and constructed lenses of the type shown in Fig. 16-2a and b with these media.

Two Refracting Surfaces, n > 1

Microwave lenses that refract at both surfaces have not been used as frequently as the single-refracting-surface types because their performance is not sufficiently better to justify the more difficult design problems.

Lens designs that meet the Abbe sine condition (to eliminate coma for small offaxis feed displacements) have been developed. The planoconvex single-focal-point lenses in Fig. 16-2e and f almost satisfy the Abbe sine condition for n = 1.6 and an f/D = 1. An experimental 50-wavelength-aperture lens had good performance over a total scan angle of 20°.

A lens with two refracting surfaces has two degrees of freedom that should permit designs with two focal points. Several investigators¹⁰⁻¹² have developed bifocal design techniques that are iterative and do not lead to closed-form solutions. These lens designs are two-dimensional (cylindrical) and symmetrical about the lens axis.

One technique 10 assumes prisms at the lens edges and represents surfaces with evenorder polynomials to permit iterative ray tracing. Another technique 11 involves a lattice method wherein points on the two lens surfaces are determined by alternating between the two focal points for ray tracing. Brown 12 uses prisms at the lens edges and the lattice method for determining the surfaces. For n = 1.6 and focal points at $\pm 20^{\circ}$, the resulting lens is almost planoconvex (the almost linear surface is slightly concave), very nearly that obtained in Ref. 10. Zoning is achieved by designing separate lenses for each of the zones. Three-dimensional lenses were obtained by rotating the two-dimensional designs about the lens axis. In these lenses, astigmatism is large and limits the beam-scan angles to about 20° . Brown 12 shows experimental data for 50-wavelength-diameter lenses with n = 1.6 and focal points at $\pm 20^{\circ}$ for f/D's from 1 to 2.

Zoning Formulas, n > 1

In the case of physically large lenses, the use of continuous surfaces (as in Fig. 16-2a, d, and e) results in a massive structure that is difficult to produce without imperfections, and the long path lengths in the medium make its index of refraction highly critical. To alleviate these disadvantages, use is commonly made of discontinuous, or zoned, surfaces as in Fig. 16-2b, c, and f. Ray paths through any two adjacent zones are designed to differ from each other by exactly 360° (or a whole multiple thereof) at the design frequency so that a plane wavefront results on the outer side of the lens.

Figure 16-2b and c gives the surface-shape formulas for zoned versions of the lens of Fig. 16-2a, while Fig. 16-2f shows the zoned counterpart of Fig. 16-2e; the use of integers $K=1,2,\ldots$ gives a family of lenses that has a focal point at x=-f and produces plane wavefronts that differ from each other in phase by integral multiples of 360°. In the use of these formulas, a thickness d on the axis is chosen, and the central zone of the surface is computed for K=1. At the radius for which the lens thickness is equal to the minimum allowed by mechanical considerations, the second zone is computed for K=2. In a similar manner, additional zones are computed with K=3, etc., until the desired lens diameter is attained. If the minimum allowable thickness is d_{\min} , the maximum thickness is approximately $d_{\min} + \lambda/(n-1)$, where λ is the design wavelength.

Effects of Zoning on Aperture Illumination, n > 1

The aperture illumination of a lens is determined by a number of factors, one of which is the lens-material loss that is proportional to lens thickness. In an unzoned lens with n > 1, this loss is larger for on-axis rays where the lens has maximum thickness than for edge rays. This leads to a more nearly uniform amplitude distribution than would be estimated without considering loss. Since a zoned lens is thinner and therefore has less loss, the aperture illumination is less strongly affected.

Certain defects in the aperture illumination usually occur with zoned lenses and should be considered carefully in the lens design. For example, Fig. 16-4a shows how shadowed bands (without energy) occur in the aperture field of a refracting outer surface. Inspection of the figure reveals that there is no way in which the zonal boundary can be shaped to eliminate the shadow. These nonilluminated bands produce aperture illumination discontinuities that increase sidelobe levels and decrease gain.

A second type of defect occurs when a first refracting surface is zoned, as in Fig.

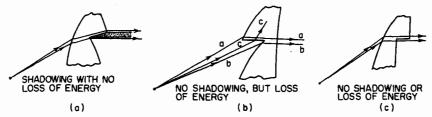


FIG. 16-4 Effects of zoning on aperture illumination, n > 1.

16-4b. In this case, the rays between rays a and b are not properly refracted by the lens and are scattered in undesired directions. Although there is no shadowing in this case, the aperture illumination is perturbed at the zone boundaries and deteriorates the expected radiation pattern.

However, zoning without shadowing or energy loss is possible if it is done on a nonrefracting surface of the lens. Figure 16-4c shows an example for the case of a plane outer surface. The surface of the step between zones must be perpendicular to the zoned surface. This type of zoning should provide the most satisfactory aperture illumination, but disturbances still exist along the zone boundaries because of phase differences between the rays just inside and outside the dielectric surface. In the special instance of a cylindrical lens in which the E vector is everywhere perpendicular to the step surfaces, this disturbance may be avoided by covering the zone boundaries with thin conducting sheets.

Bandwidth of Zoned Lenses, n > 1

The surface-shape design of an unzoned constant-n lens is independent of frequency. However, as may be seen from the formulas in Fig. 16-2, zoning introduces a frequency dependence so that a zoned lens has a limited bandwidth of satisfactory operation. Rays through adjacent zones will differ by exactly 360° only at the design frequency. If the lens has a total of N wavelength steps between the central and edge zones, the effective path-length difference between a ray through the edge zone and a ray through the central zone is $N \lambda_0$ at the design wavelength λ_0 and $N \lambda$ at any other wavelength λ , where N is 1 less than the K of the outermost zone. The phase difference, in wavelengths, of the edge zone compared with the central zone is $-N d\lambda$, where $d\lambda = \lambda - \lambda_0$. Since the total bandwidth is approximately $100 (2d\lambda/\lambda)$ percent, if a phase difference of $\pm \lambda/8$ is allowed, the bandwidth of a lens having N wavelength steps is 25/N percent. Thus a zoned lens has an approximate bandwidth of 5 percent for N = 5 if only zoning effects are present. However, since there are other sources of phase error and it is necessary to allocate the total allowable phase error among all error sources, the bandwidth may be smaller than indicated above.

16-3 FACTORS AFFECTING GAIN AND SIDELOBE LEVELS OF LENS ANTENNAS

The gain of a lens antenna is reduced by a number of factors that include the amount of feed energy not incident upon the lens (spillover loss), the effects of lens shape on

aperture illumination, dissipation loss in the lens medium, and reflection from the surfaces.

Spillover Loss

Spillover may be avoided if the feed horn is extended to the lens edges; however, this is usually not done, since lens-surface reflections are reflected by the horn walls and radiated from the lens in undesired directions, thereby increasing sidelobe levels. The horn walls can be covered with absorbing material to reduce the energy in the reflected waves, but with this technique the antenna gain is reduced since feed energy is also absorbed.

In applications in which low sidelobe levels are important, the use of a multielement (array) feed to tailor the aperture illumination and reduce spillover is recommended. Also, surface matching is recommended to permit the use of an extended horn, increase gain, and reduce sidelobe levels.

Effect of Lens Shape on Aperture Illumination

The aperture amplitude distribution is a function of the feed radiation pattern, the shape of the lens, lens-surface reflections, and lens losses. References 1 and 2 derive the relations for conversion from the power per solid angle radiated by the feed to the power per unit area in the aperture for several lens types and plot the conversion factors for several sets of lens parameters. In general, for n > 1 lenses, the conversion factor is <1; for n < 1 lenses, the factor is >1; therefore, if a given feed is used for the two lens types, the n < 1 lens will have a higher edge illumination than the n > 1 lens.

Dissipation Loss in Lens Media

The dissipative attenuation constant for a dielectric medium is approximately 27.3 (tan δ) n (dB/wavelength), where n is the index of refraction and tan δ is the loss tangent of the medium. Since the maximum thickness of a zoned n > 1 lens is approximately $\lambda/(n-1)$, the upper limit for lens attenuation is approximately 27.3 (tan δ)n/(n-1) (dB). Therefore, for most practical materials the maximum dissipation loss is several tenths of a decibel. Reference 13 contains extensive dielectric-constant and loss-tangent data for many dielectric materials over a large range of frequencies and temperatures.

Reflections from Lens Surfaces

The air-to-dielectric interface at each lens surface produces reflected and transmitted waves. The amplitude and phase of these waves are obtained by the application of Fresnel's equations and depend on n, the angle of incidence, and the polarization relative to the incidence plane (a plane through the incident ray and the surface normal). Since there are reflections at both lens surfaces, the effects of internal multiple reflections are determined by the ray path lengths between the surfaces. The thickness of a typical lens varies appreciably over its aperture so that, with the transmitted waves adding in various phases, there are a number of almost sinusoidal variations in amplitude and phase over the aperture. For most lenses, incidence angles are less than 45°

so that reflection losses can be averaged over all incident polarizations and angles to obtain an approximate lens reflection loss of $8.69(n-1)^2/(n+1)^2$ dB. For an n=1

1.6 lens, this reflection loss is less than 0.5 dB. However, sidelobe levels are seriously increased and for most lenses are limited to values about -20 dB.

These effects may be reduced by matching the lens surfaces. $^{14-16}$ For near-normal incidence angles, this can be accomplished by adding to each surface a quarter-wavelength-thick coating (in the material) with an index of refraction of $(n)^{1/2}$, where n is the lens-material index of refraction. If it is necessary to match for nonnormal incidence angles, the coating thickness and index of refraction may be modified as discussed in Ref. 1.

For many lens materials, a coating material with the correct index may not be available; in that case, surface matching may be performed by machining the lens surfaces to the configurations shown in Fig. 16-5 and discussed in detail in Refs. 1 and 14-16. The improvement

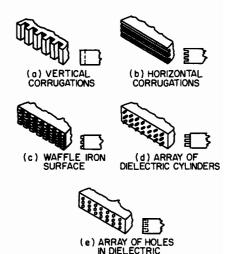


FIG. 16-5 Simulated quarter-wavelength matching transformers for lens surface.

that can be obtained in lens performance by lens-surface matching¹⁶ is shown in Fig. 16-6; however, these lenses were matched with artificial dielectrics not discussed in this chapter.

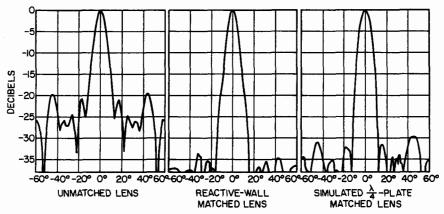


FIG. 16-6 Radiation patterns of unmatched and matched lenses.

16-4 LENS-SURFACE FORMULAS FOR n < 1

The lens formulas given in Fig. 16-2 apply for n < 1 as well as for n > 1; however, for convenience, the lens-surface formulas for n < 1 media planoconcave lenses are

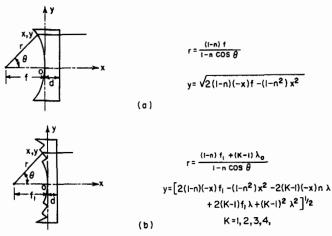


FIG. 16-7a and b Lens-shape designs for n < 1 media.

shown in Fig. 16-7 and apply to both rotational and cylindrical surfaces. These are single-refracting-surface, single-focal-point lenses since the planar outer surface is fixed during the design to lie on a wavefront. The inner surface is an ellipse with foci on the axis; the feed is located at the focus farthest removed from the inner surface. Reflections from the outer surface converge at the focal point as for n > 1 lenses and can be eliminated by techniques used for those lenses.

For the stepped inner surface in Fig. 16-7b, shadow bands at the steps cannot be avoided, as may be seen in Fig. 16-8. Although all the rays emanating from the feed

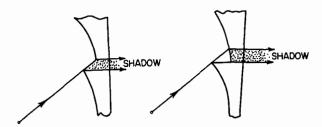


FIG. 16-8 Shadows introduced by zoned lens in Fig. 16-7b.

are collimated by the lens, the steps cause discontinuities in the aperture illumination. As in the case of n > 1 lenses, zoning can be accomplished without shadowing or energy loss only if the steps are formed in the equiphase outer surface, but the resulting meniscus-type lens shape is more difficult to manufacture and to support than the flat shape of Fig. 16-7b.

The maximum thickness of the stepped lens for n < 1 is equal to $d_{\min} + \lambda/(1 - n)$, where d_{\min} is the minimum thickness permitted in the mechanical design. The bandwidth limitation due to zoning alone is the same as for n > 1 lenses. However, the bandwidth of the actual lens is considerably less than this when the frequency

sensitivity of n is taken into account, since all known media having n < 1 exhibit a large rate of change of n with frequency. Thus, in the common case of a metal-plate zoned lens having the shape shown in Fig. 16-7b, if $\pm \lambda/8$ phase error is allowed, the bandwidth is approximately $25n_0/(1 + (N+1)/n_0)$ percent, where n_0 is the n at the design frequency and N is the number of one-wavelength steps between the central and edge zones. In the case of frequency-sensitive media, zoning increases the bandwidth of a lens over that of an equivalent unzoned lens by a factor of 2 or 3 because the ray path lengths in the dispersive medium are greatly reduced by zoning. The bandwidth of a given lens antenna may be extended considerably if the antenna application permits moving the feed position along the lens axis as a function of frequency, since defocus is the principal effect of a frequency change.

The lenses in Fig. 16-7 may be constructed with artificial dielectric, metal-plate, or waveguide media. An excellent summary of artificial dielectric media is contained in Ref. 1. Metal-plate and waveguide media are discussed in the next section. Kock¹⁷ used a number of techniques to construct metal-plate lenses with both circular and rectangular apertures. Figure 16-9 is a photograph from Ref. 8 of a stepped 96-wave-

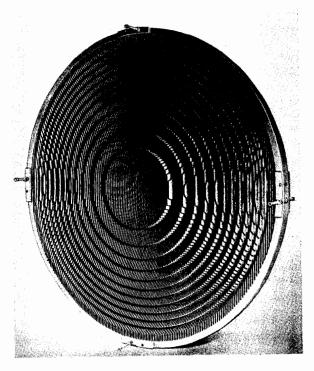


FIG. 16-9 An F/D = 0.95 zoned lens.

length-aperture, F/D = 0.96, metal-plate lens that has a useful bandwidth of about 5 percent. Most early metal-plate lenses used the designs and techniques of Kock. Additional n < 1 lenses are discussed in Sec. 16-6, "Waveguide Lenses."

16-5 METAL-PLATE AND WAVEGUIDE MEDIA

Rays incident on natural dielectric and many artificial dielectric media obey Snell's law at the surface. A metal-plate medium (composed of parallel, equally spaced plane metal sheets) constrains rays in the medium to paths parallel to the plates; therefore, Snell's law is not obeyed for incident rays in a plane normal to the plates (see Fig. 16-10), while it is obeyed for rays incident in a plane parallel to the plates (see Fig. 16-

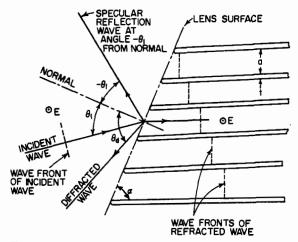


FIG. 16-10 Constrained refraction in the H plane.

11a). A waveguide medium constrains rays in the medium to paths parallel to the waveguide axis (see Fig. 16-11b); therefore, Snell's law is not obeyed for any incidence angle.

Both metal-plate and waveguide media operate in the fundamental TE mode of propagation, and since the phase velocity exceeds the velocity of light in free space, n < 1. If the cutoff wavelength is λ_c , then $n = [1 - (\lambda/\lambda_c)^2]^{1/2}$ for an operating wavelength λ . For both parallel plates spaced a apart and a waveguide of width a, $\lambda_c = 2a$. For a regular hexagon of width a between parallel sides, $\lambda_c = 1.792a$. For a circular waveguide of diameter a, $\lambda_c = 1.705a$.

When parallel plates are used, an E-field component perpendicular to the plates must be avoided, since this excites a TEM mode that propagates between the plates with the velocity of light (n = 1) and the energy would not be focused. For square, circular, and hexagonal cross-section waveguide media, n is independent of incident polarization, and these structures can be used for any polarization. A rectangular cross-section waveguide medium has different values of n for the two principal linear polarizations.

Limitations on Metal-Plate Spacing and Rectangular-Waveguide Width

A basic limitation on the choice of plate spacing a results from the fact that the medium must operate between the cutoff frequencies of the fundamental and the next

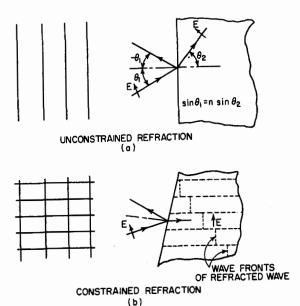


FIG. 16-11 Unconstrained (a) and constrained (b) refraction in the E plane.

higher TE modes. For air-filled structures, this requires that $0.5 < a/\lambda < 1.0$; this range of a/λ corresponds to a range in n of 0 < n < 0.866. However, a further restriction on the plate spacing must be imposed if the existence of diffracted waves due to the grating effect is to be avoided. It will be shown later how such diffracted waves cause considerable loss of transmitted power, distortion of the aperture illumination function, and consequent loss of gain and increased sidelobe levels. The presence of one diffracted wave is shown in Fig. 16-10. This occurs in the direction in which the diffracted waves from the individual plate edges combine in phase. It can only occur when the plate spacing exceeds a particular value and will be avoided if the following condition is met:

$$[\lambda \sin \alpha/(a+t)] - 1 > |\sin \theta_1| \tag{16-1}$$

where t is the wall thickness and the other symbols are defined in Fig. 16-10. This is also the condition for avoiding a diffracted wave when the incident wave is in the medium and the transmitted ray emerges at angle θ_1 . For $\alpha=90^\circ$, this is the familiar expression for avoiding grating lobes from a phased array: $s=a+t<\lambda/(1+\sin\theta_1)$. The limiting values of Eq. 16-1 are shown graphically in Fig. 16-12, where the angle θ_1 of the ray in free space is plotted versus $(a+t)/\lambda$ for different values of α from 30 to 90°. For each particular value of α , the region to the lower left of the curve gives the ranges of θ_1 and $(a+t)/\lambda$ in which diffracted waves are avoided.

Reflection and Transmission at an Interface

For the case of the E field parallel to the plane of incidence and parallel to the plates (Fig. 16-11a), the power-reflection coefficient is

$$r^2 = \sin^2(\theta_1 - \theta_2)/\sin^2(\theta_1 + \theta_2)$$
 (16-2)

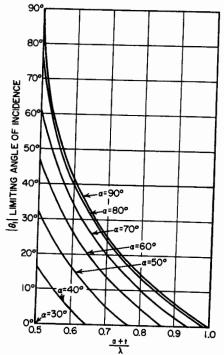


Fig. 16-12 Limiting angle of incidence for pure specular reflection versus plate spacing.

where θ_1 is the ray angle in free space and θ_2 the ray angle in the parallel-plate medium, both angles being measured from the normal to the surface. The plates are assumed to be very thin; however, thick plates are treated in Ref. 18 for $\theta_1=0$ and $\alpha=90^\circ$. Equation (16-2) also holds true for a wave incident from the metal-plate region. The reflected ray is then within the metal-plate region at an angle $-\theta_2$. It is of interest to note that Eq. (16-2) also applies for a solid dielectric with E perpendicular to the plane of incidence. Equation (16-2) and Snell's law of refraction hold for all angles of incidence [if $0.5 < (a+t)/\lambda < 1.0$], and diffracted waves do not occur. However, this is not true of parallel polarization incident on a constrained medium (Fig. 16-11b), and a solution for that case is not available.

Considerable published information is available for the case of E perpendicular to the plane of incidence and parallel to the edges of a set of very thin plates (Fig. 16-10). The basic analysis is due to Carlson and Heins, ¹⁹ while further theoretical work was done by Lengyel, ²⁰ Berz, ²¹ and Whitehead. ²² In the range of θ_1 free of diffracted waves, as given by Eq. (16-1) and Fig. 16-12, the power-reflection coefficient for a wave incident on an array of plates is

$$|r|^2 = \left[\frac{\cos(\theta_1 + \psi) - n}{\cos(\theta_1 + \psi) + n}\right] \left[\frac{\cos(\theta_1 - \psi) - n}{\cos(\theta_1 - \psi) + n}\right]$$
 (16-3)

where $\psi = 90^{\circ} - \alpha$ is the angle between the normal to the boundary and the plates. The specularly reflected wave propagates at angle $-\theta_1$. Because of reciprocity, this formula also applies to waves in the plate region incident upon the free-space boundary, where the waves between the plates are phased to produce a transmitted wave propagating at angle θ_1 from the normal. For normal incidence and $\alpha = 90^{\circ}$, Eq. (16-3) reduces to $r^2 = (1 - n)^2/(1 + n)^2$, which also applies to a solid-dielectric boundary. In the range of θ_1 where diffracted waves may exist, Eq. (16-3) is no longer valid. Formulas for this range have been derived by Lengyel, ²⁰ Berz, ²¹ and Whitehead²² and are much more complicated than Eq. (16-3).

Figure 16-13 shows the percentage of incident power transmitted into a metalplate medium for the conditions of Fig. 16-10 and $\alpha = 90^{\circ}$. To the left of the break

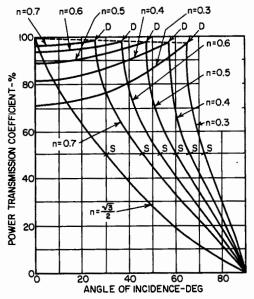


FIG. 16-13 Percentage of power transmitted into metal-plate medium, $\psi = 0$.

in each curve (points D), the nontransmitted power is reflected in the specular reflected wave, while to the right of the break the nontransmitted power is divided between the specular reflected wave and a diffracted wave. The power loss in the latter region is large and should be avoided in lens design. At points S, the angle θ_d of the diffracted wave is equal to θ_1 of the incident wave (Fig. 16-10). When $\alpha \neq 90^{\circ}$, the reflection and transmission quantities are not symmetrical about $\theta_1 = 0$.

The discontinuity effect at the boundary of the metal-plate medium also results in a phase change. Formulas giving this change have been derived by Lengyel, ²⁰ Berz, ²¹ and Whitehead. ²² Graphical plots of this phase change versus the angle of incidence are given by Berz and Whitehead and show a moderate variation with the angle of incidence. Calculations by Whitehead for a typical planoellipsoidal lens show that substantial curvature of the wavefront occurs at the aperture when the feed ele-

ment is at the focal point but that the wavefront may be made almost plane by moving the element slightly away from the focal point.

The above-described data for perpendicular polarization incident on a set of parallel plates apply equally well to an array of thin-walled square or rectangular tubes (Fig. 16-11b). However, for parallel polarization the constraint offered by the array of tubes has a large effect on its reflection characteristics. Wells²³ shows that, at the angle of incidence for which the diffracted wave first appears, a sharp peak of specular reflection also occurs.

Methods of Reducing Reflection Losses

Within the angle-of-incidence range given by Eq. (16-1) and Fig. 16-12, the reflection from the surface of a metal-plate or waveguide lens may be canceled through the introduction of an additional reflecting discontinuity. Possible structures are shown in Fig. 16-14, where in a a dielectric sheet is placed outside the lens and in b obstacles

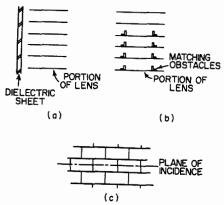


FIG. 16-14 Techniques for reducing surface reflections from metal-plate lenses.

are placed inside the lens. In both cases the magnitude and phase of the additional reflection are adjusted to cancel the reflection from the plates. The magnitude depends upon the dielectric constant and the thickness of the dielectric sheet or the shape and size of the obstacles, while the proper phase relationship is obtained through choice of the spacing of the dielectric sheet or obstacles from the plate edges. The correct design for a given lens may be obtained experimentally; however, a theoretical design may also be computed through the use of graphical and tabulated data given by Lengyel²⁰ for the magnitude and phase of the reflection coefficient of the boundary.

In a practical lens design, it is difficult to avoid the ranges of θ_1 for which diffracted waves occur. Many early designs of metal-plate lenses did not do this, and as a result considerable loss of gain resulted. One method of avoiding this condition, as may be seen from Fig. 16-12, is to reduce the plate spacing; however, this reduces n and increases the reflection loss at angles near normal incidence and reduces the bandwidth. A further possibility is to fill the regions between the plates with dielectric material or to introduce ridges in the waveguide parallel to the axis (Fig. 16-14b) in

a manner analogous to ridge waveguide. 24,25 In this way, the plate spacing may be reduced to a point at which diffraction is no longer a problem while n remains at a reasonable value.

Another method of avoiding diffracted waves in one plane is to use a staggered arrangement of waveguide channels, 23 as in Fig. 16-14c, now a proven technique in space-fed phased arrays. The spacing between scattering edges is effectively cut in half, thus doubling the frequency at which a diffracted wave first appears. This staggered arrangement also eliminates the sharp peak of specular reflection that occurs with the nonstaggered array of tubes for parallel polarization.

16-6 WAVEGUIDE LENSES

Three-dimensional unzoned waveguide lenses of the type shown in Fig. 16-7a have been designed. The inner surface is an ellipsoid of revolution about the lens axis, and the outer surface is a plane perpendicular to the axis. One such lens²⁶ has a 36-in (914-mm) diameter and a 31.2-in (792-mm) nominal focal length and is constructed of 0.68-in- (17.3-mm-) inside-diameter square waveguide to provide a nominal n = 0.5 at 10 GHz. The lens was fed with a circular-aperture-waveguide horn that produced circular polarization. The reference has a number of plots of experimental data: gain, beamwidth, n, and focal length versus frequency; gain, beamwidth, and first sidelobe level versus feed-horn diameter; radiation patterns as a function of beam-scan angle; and gain, beamwidth, and first sidelobe level versus beam-scan angle. The sidelobe level increases from -22.5 dB on axis to -11 dB at 13° beam scan and remains at about that level for beam scan to 22°. The gain decreases by 3 dB (from the on-axis value of 36 dB) at a beam-scan angle of 18°, or 7.65 beamwidths.

Another design²⁷ has a 24-in (610-mm) diameter and a 36-in (914-mm) focal length constructed of $\frac{1}{2}$ -in (4.0-mm) cell honeycomb to provide an n = 0.642 at 55 GHz. Because the honeycomb cells deviated from perfect hexagons, the performance varied with the linear-polarization orientation. The aperture efficiency was only 18.3 percent because random variations in the cell size produced large aperture phase variations.

To obtain wide-scan-angle performance, Ruze²⁸ investigated bifocal cylindrical constrained lenses in which the two focal points are equally displaced from the lens axis at P_1 and P_2 as shown in Fig. 16-15. The inner surface is found by equating optical-path lengths for the central ray and a general ray from each of the focal points. It is an ellipse, with foci at the two focal points, independent of n or lens thickness, given by

$$(x + af)^2/(af)^2 + y^2/f^2 = 1$$
 (16-4)

where $a = \cos \phi$. Imposing the two focal points uses two of the three degrees of freedom available. Ruze considered several alternatives for choosing the third condition: constant n, constant thickness, linear outer surface, third correction point, and no second-order error; for the last four, n varies with y. The deviations from a linear phase front for a general feed point were expanded into a power series and examined for each case. For the on-axis feed point there are no odd-order terms, and the second-order deviation (defocus) can be corrected by moving the feed point along the axis;

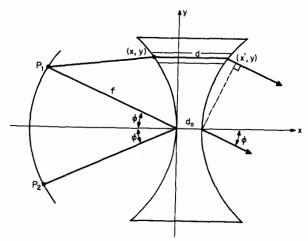


FIG. 16-15 Bifocal metal waveguide lens.

however, this correction is not needed for all cases. The feed arc is chosen as a circle through the corrected on-axis feed position and the two focal points. Several of these designs permit a beam scan of 110° for $\phi = 50^{\circ}$. Feed-arc selection for reduced phase errors is discussed in Refs. 29 and 30.

The constant-n lens has been the most popular. The thickness is given by

$$d = d_0 + (m\lambda + ax)/(n - a)$$
 (16-5)

where m is the number of wavelength steps in the outer surface. Reference 31 analyzed this type of lens with results near those of Ruze. The constant-n lens was expanded to three dimensions by Ref. 32; the inner surface is an ellipsoid of revolution about the line through the focal points, and the outer surface is an ellipsoid with unequal principal radii. The performance is well behaved for feed points between the two focal points, but performance deteriorates rapidly for feed points beyond the focal points. Performance also degrades rapidly as the feed point is moved away from the xy plane.

A constant-n lens was used in an application³³ for which the scanning feed system was most conveniently designed for a planar feed aperture. The phase errors were minimized for the on-axis feed point by a method of stepping the outer surface. A constant-n lens was also used for a satellite antenna,³⁴ but with the two correction points collapsed to a single on-axis point so that the inner surface was a segment of a sphere and the outer surface a segment of a spheroid. The effects of zoning the outer surface were computed. The radiation-pattern effects of zoning were also computed in Ref. 35.

A linear-outer-surface two-dimensional lens between parallel plates was constructed for an X-band multibeam application by milling waveguides of unequal width (to obtain variable n with y) in metal blocks. The lens had good performance, and the tolerances obtained appeared sufficient to permit this technique to be used for frequencies up to 40 GHz.

Waveguide lenses have been designed to provide a larger bandwidth by designing for equal time delay^{37,38} for all rays through the lens. The phase delay in each wave-

guide is adjusted with a phase shifter to provide a planar wavefront. These lenses have a spherical inner surface so that they satisfy the Abbe sine condition for off-axis performance. Reference 38 has both single- and dual-frequency designs which obtain bandwidths that vary from 40 to 20 percent for lens diameters from 20 to 100 wavelengths.

16-7 BOOTLACE-TYPE LENSES

Bootlace lenses can have four degrees of freedom that permit designs with four focal points to obtain wide-angle performance for either multiple simultaneous beams or a scanning beam; however, most designs fix the outer surface and have three focal points. These constrained lenses have radiators on the inner and outer surfaces connected by TEM-mode transmission lines (usually coaxial or stripline), which give the appearance of untightened bootlaces, hence the name. Typically, all rays in these lenses have equal time delays from a focal point to the corresponding linear wavefront, and therefore they are inherently broadband, limited only by component bandwidths and the performance of a fixed aperture size.

Gent³⁹ identified most of the useful properties of this type of lens, including (1) four degrees of freedom, (2) the fact that one surface may be displaced and/or rotated relative to the other (i.e., the surfaces may have independent coordinate systems), (3) the ability to add phase shifters, attenuators, and/or amplifiers in the lens transmission lines to provide outer-surface aperture illumination control and beam scan, (4) the fact that the line lengths can be stepped by multiple wavelengths, analogously to the physical stepping shown in Fig. 16-2 without creating shadowing but with reduced bandwidth, (5) the ability of radiators on the two lens surfaces to have different polarizations, and (6) the fact that the spacing between aperture radiators must be less than $\lambda/(1 + \sin \theta_{\text{max}})$ to avoid grating lobes, where θ_{max} is the maximum beam-scan angle from the aperture normal.

The Rotman-Turner⁴⁰ lens is a two-dimensional bootlace lens with a linear outer surface perpendicular to the lens axis and three focal points, one on axis and two equally displaced from the lens axis, shown in Fig. 16-16 as points G(-g, 0), $F_1(-\cos\phi, \sin\phi)$, and $F_2(-\cos\phi, -\sin\phi)$, respectively, where central rays from F_1 and F_2 subtend an angle ϕ with the axis. Desired wavefronts are displaced from the vertical by angles $0, \psi$, and $-\psi$ respectively, where $\psi = \phi$ in this design. All dimensions are normalized to the F_1 -to-origin distance. Pairs of inner- and outer-surface radiators are connected by coaxial lines with the general pair located at P(x,y) and Q(t,u) respectively. Let $w = s - s_0$ be the normalized electrical path-length difference between the general and the central line lengths. Equating the optical-path lengths for a general ray and the central ray for each focal point produces

$$y = u(1 - w) ag{16-6}$$

$$x^2 + y^2 + 2dx = w^2 + e^2u^2 - 2w$$
 (16-7)

$$x^2 + y^2 + 2gx = w^2 - 2gw ag{16-8}$$

where $d = \cos \phi$

 $e = \sin \phi$

x and y can be eliminated to obtain

$$aw^2 + bw + c = 0 ag{16-9}$$

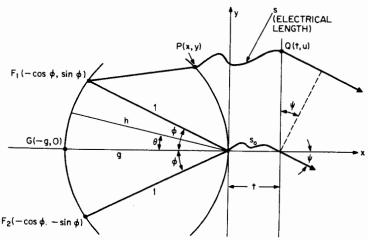


FIG. 16-16 Rotman-Turner lens nomenclature.

where
$$a = 1 - u^2 - (g - 1)^2/(g - d)^2$$

 $b = 2g(g - 1)/(g - d) - e^2u^2(g - 1)/(g - d)^2 + 2u^2 - 2g$
 $c = ge^2u^2/(g - d) - e^4u^4/(4(g - d)^2) - u^2$

w as a function of u is determined from Eq. (16-9) for fixed parameters ϕ and g. Substitution into Eqs. (16-6), (16-7), and (16-8) determines x and y. The technique of Ruze²⁸ (for the linear-outer-surface lens) for minimizing aberrations from a linear wavefront for a general feed point θ between $\pm \phi$ is used to determine $g = 1 + \phi^2/2$, for ϕ in radians. The feed path is chosen as a circle that intersects the three focal points.

Reference 40 contains computations of w, x, and y as a function of u for $\phi=30^\circ$ and computations of deviations from a linear wavefront for $0 \le \theta \le 40^\circ$ and several values of g. Also shown are lens shapes for four values of g. For $\phi=30^\circ$ and g=1.137 (the optimum value of g for $\phi=30^\circ$), the normalized path-length error is <0.00013 for $-0.55 \le u \le 0.55$ (i.e., aperture = $2u_{\rm max}=1.10$ and $g/2u_{\rm max}=1.035$). If a phase error of $\pm \lambda/8$ is allowed, an aperture of 1000 wavelengths can be used to obtain a beamwidth < 0.075° that can be scanned more than 60°, or more than 800 beamwidths.

An experimental lens at 3.0 GHz with $\phi=30^\circ$, g=1.137, $u_{\rm max}=0.6$, and $D/\lambda=18$ was constructed by using RG-9/U coaxial cables for the lens, a TEM-mode parallel-plate structure between the feed position or positions and the inner lens surface, a flared parallel-plate aperture that contained the linear outer surface, and quarter-wavelength probes into the parallel-plate regions.

The Archer lens⁴¹ is a Rotman-Turner lens with additional features: (1) The parallel-plate region between the feeds and the inner surface is filled with a dielectric material of relative dielectric constant ϵ_r to reduce all linear dimensions by a factor of $n=(\epsilon_r)^{1/2}$, thereby permitting its use in a smaller volume. (2) Stripline or microstrip lens and feed-port connecting lines are printed on an extension of the dielectric material, thereby removing connectors and probes and the associated mismatches and permitting construction to tight tolerances and wide-bandwidth operation. (3) The beam angle ψ can differ from the feed angle θ so that $\sin \psi / \sin \theta = K$ (where K=1 for

the Rotman-Turner lens)⁴²; K > 1 permits obtaining large beam-scan angles with practical feed positions, and K < 1 permits reduction of the lens size for limited scanangle applications. These features increase the lens versatility but do not increase the design degrees of freedom.

There is a nomenclature difference between the Archer and Rotman-Turner lenses. In the Archer lens, the printed-circuit lines that form the lens appear to be just connecting lines, while the dielectric region between the feed ports and the inner surface appears to be a lens and is usually referred to as such.

Archer lenses⁴¹ have been designed and constructed with materials with ϵ_r 's from 2.5 (Teflon fiberglass) to 233 (cadmium titanate). Figure 16-17 shows a 20-radiator,

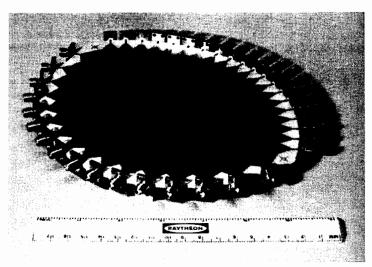


FIG. 16-17 Archer lens, $\epsilon_r = 38$.

16-beam lens constructed in microstrip on a barium tetratitanate ceramic substrate with $\epsilon_r = 38$. Most designs have a beam coverage of 120°, range from a 4-radiator, 4-beam lens to a 140-radiator, 153-beam lens, and have a typical operating frequency band of almost two octaves. Designs usually have adjacent beams overlap at the 3-dB points (with feeds at equal intervals in sine space) at the maximum operating frequency where the gain and beamwidth are consistent with that obtainable from the full aperture. At lower frequencies, the beams broaden and overlap at a higher level, and gain decreases more rapidly than the beamwidth broadening would indicate owing to beam-coupling loss. Low sidelobe patterns⁴³ are obtained by feeding several adjacent beam ports with weighted amplitudes.

Alternative designs⁴¹ are obtained by fixing the outer surface as a circle, with an arc up to 60°, that is more adaptable to conformal applications. A circular aperture eases the design problem of eliminating aperture resonances that are common in linear arrays, increases the beam coverage with reduced gain roll-off with off-axis beam scan traded against on-axis gain, and reduces the effects of outer-surface mismatch since reflections do not have a constant phase difference from radiator to radiator as with a linear array.

The linear-aperture bootlace lenses discussed above produce fan beams. Multiple pencil beams in a plane can be produced by illuminating a parabolic-cylinder reflector or cylindrical lens (see Fig. 16-1) with the linear aperture. A two-dimensional cluster of pencil beams may be formed by stacking vertical linear-aperture lenses, so that the outer surface of each lens provides a column of radiators, and by feeding the beam ports of these lenses with the output ports of a stack of horizontal lenses. The beam ports can be used separately, adjacent beam ports may be combined to provide monopulse-type outputs, and multiple beam ports may be combined after weighting to provide low sidelobe beams. Three-dimensional bootlace-type lenses are discussed in Refs. 39, 41, and 44-47.

Gent³⁹ found a special case of the two-dimensional bootlace lens that has feed points and the inner surface on a circle of radius R and the outer surface on a circle of radius 2R with equal line lengths between the inner- and outer-surface radiators and recognized that it is equivalent to the R-2R geodesic scanner. ^{48,49} It is proved in Ref. 50 that the R-2R bootlace lens is unique. Bootlace R-2R lenses have been constructed by using printed-circuit techniques on dielectric materials. The R-2R-type lens has been extended into an R-KR lens, ⁴¹ shown in Fig. 16-18, that has equal

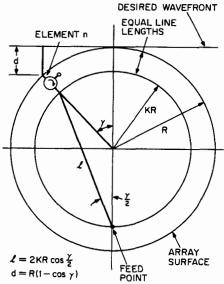


FIG. 16-18 *R-KR*-array geometric relationships.

radial line lengths between radiators on a circle of radius KR and radiators on a circle of radius R. With K=1.92, the optimum value, it is the printed-circuit version of a constant-index lens. It provides a nearly linear wavefront for an arc of approximately 120° on the circle with radius R. By adding a circulator in each of the lines to permit feed inputs, beams covering 360° can be obtained simultaneously.

16-8 PHASED-ARRAY LENSES

Phased arrays are discussed in Chap. 20; in this section space-fed phased-array lenses are discussed for comparison with other lenses.

Space-fed arrays⁵¹⁻⁵⁷ have constrained lenses that usually are constant-thickness^{51,54} with planar surfaces. Elements (or modules), usually perpendicular to the surfaces, contain inner- and outer-surface radiators, phase shifters, and in some cases other components such as phase-shifter drivers and polarization switches. The inner-surface radiator has the polarization of the feed or feeds and needs to be matched only for the incidence angles from the feed or feeds. The outer-surface radiator can have any polarization or polarizations that may be switchable, must be matched for the range of beam-scan angles used, and must withstand the environment. Most phase shifters are digital, modulo 360°, in which the number of bits is determined by the required beam-pointing accuracy and sidelobe levels. Either diode- or ferrite-type phase shifters are used, the type for a given application being determined by the operating frequency, radio-frequency power levels, required phase-state-switching speed, and switching and/or phase-state-holding power.

Beam steering and collimation (the conversion of the feed wavefront to a plane wave) are obtained by the phase shifters; the computed phase shifts required for the two functions are superimposed. The phase shift required for collimation is determined from ray tracing as for other lenses. Phase-shift commands may be computed and commanded on an element-by-element basis or by rows and columns.⁵² This collimation method reduces the number of phase-shifter bits required to obtain a given beampointing error, since the otherwise-present regularity of phase errors over the lens outer surface is destroyed.

In many pulsed-radar applications, it is possible to change the state of the phase shifters between transmit and receive; in these cases, separate transmit and receive feeds may be used. If sufficient isolation between feeds is obtained, the need for a transmit-receive switch is eliminated. In addition, separate feeds permit the lens illumination to be optimized for both transmit and receive; e.g., to obtain maximum gain on transmit and low sidelobes on receive.

For applications that require large beam-scan angles and large instantaneous-frequency bandwidth, lenses permit the total angular coverage to be divided into sectors, each with a separate feed, to obtain more nearly equal time delay for all beam positions. The feeds may be used to obtain simultaneous beams,⁵³ or one feed may be selected by a switching network.

Some applications of space-fed-array lenses are discussed in Refs. 54 to 57.

16-9 DOME ANTENNAS 58-65

The dome antenna was developed to obtain an antenna to scan a beam over a full hemisphere or more for hemispherical-coverage applications as an alternative to the three or four planar arrays usually considered.

In its simplest form, the dome antenna (Fig. 16-19) has a constrained constantthickness lens (the dome) fed by a planar array, both symmetric about the vertical axis. The technique is to illuminate an aperture (a portion of the dome) that has an appreciable area perpendicular to any of the desired beam directions to obtain antenna gain in those directions. The feed array can produce convergent or divergent rays to

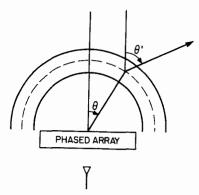


FIG. 16-19 Dome-antenna nomenclature.

illuminate the required lens area. The lens has a phase-delay gradient in the elevation plane to refract rays in the θ' direction when fed at an angle θ . $K = \theta'$ / θ is defined as the scan amplification factor.

The dome is constructed of modules normal to the surfaces which have radiators on each surface connected by transmission lines that contain the required phase delay. The phase delay could be provided by switchable phase shifters, 58 but in practice this method is too expensive, so fixed delays are used. There are a number of methods for implementing the delays; in one module configuration, 59 the lengths of two dielectric-filled circular

waveguides of different diameters in series are varied to obtain the phase delay in 20° increments. The modules may have phase delays modulo 360° (with a bandwidth penalty) and have different polarizations on the two lens surfaces. The spacing between modules must be small enough to suppress grating lobes.

Phase delays are generally equal in all modules that have the same cone angle θ . There are several design techniques for determining dome-module phase delays. Since the dome is in the near field of the feed array, rat-tracing methods may be used. For a hemispherical dome of radius R and a constant $K \neq 1$, one technique ⁵⁸ equates the path lengths for rays from the center of the feed array at angles θ and $\theta + d\theta$ and, after integrating, obtains the required phase delay, which is $(2\pi/\lambda)R[1 - \cos(\theta' - \theta)]/(K - 1)$. For these fixed phase delays, rays from the desired planar wavefront are traced through the lens to the feed array to determine the required feed-array wave-

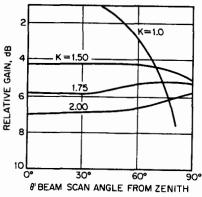


FIG. 16-20 Dome-antenna relative gain versus θ' as a function of K.

front, which in general is not planar. The gain (relative to the feed-array broadside gain without a dome) of an antenna designed in this manner is shown in Fig. 16-20 for several values of K. It is evident that beam angles greater than 90° can be obtained for K > 1 and that maximum gain occurs for beam angles $\theta' > 90$ ° for K > 2.

It is desirable to be able to design for prescribed antenna gain versus θ' profiles as, for example, 58 that shown in Fig. 16-21. For some applications, it is also helpful if the dome has an elongated shape along the axis; i.e., the dome is a cylinder generated by a noncircular arc. For these cases, the lens-module phase delays can be designed 58 by allowing a

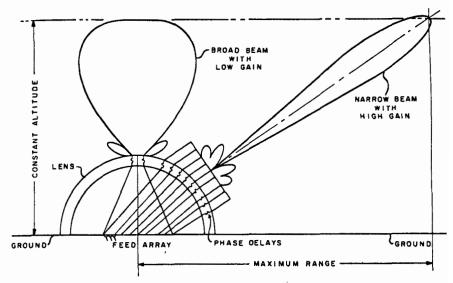


FIG. 16-21 Typical gain versus θ' profile for a dome antenna.

variable K with θ and applying the techniques used for designing a shaped-beam reflector (see Ref. 2, pages 497-500).

These techniques have been implemented⁵⁹ at C band with a 4-ft- (1.2-m-) diameter hemispherical dome composed of 3636 modules (dielectric-loaded circular waveguides with a phase-delay increment of 20°) and an F/D = 0.75, space-fed planar phased array with 805 elements. Dome loss was less than 1 dB over a 10 percent frequency band. Two gain-versus-scan-angle-profile designs were measured. One version with K < 2 with maximum gain at approximately 60° had peak sidelobes below -18 dB and average sidelobes below -25 dB. It had a 13 percent bandwidth for a zenith beam and a 6.3 percent bandwidth for a 60° beam position. The gain profile matched predictions within 0.3 dB for scan angles up to 60°. Another version with K = 2.6 with maximum gain at 110° demonstrated good performance in a limited amount of data. Another implementation, 60 also at C band, had a hemisphere on a cylinder dome 76 in (1.93 m) in diameter and 51 in (1.30 m) high that had 8511 modules, each a thin-walled metal tube that contained a serrated cruciform to provide the phase delay in increments of 20° between modules. The feed array was 47 in (1.19 m) in diameter and used 1120 elements. The gain profile had maximum gain at θ' 90°.

An alternative to a constrained lens is the use of a graded-thickness (in elevation) homogeneous dielectric material with quarter-wavelength matching layers on each surface. ^{58,65} Several techniques for designing to desired gain versus scan-angle profiles and for determining limits on attainable profiles have been analyzed. ⁶¹⁻⁶³ A two-dimensional antenna with K=1.5 that used a concave-outer-surface Archer lens for the feed has been analyzed. ⁶³ and measured; ⁶⁴ it improves the wide-scan-angle side-lobes, operates over a frequency band of more than an octave, and can provide multiple simultaneous beams.

16-10 LUNEBURG LENSES

Luneburg. Luneburg. Investigated a class of spherically symmetric, variable-index-of-refraction n lenses that image two concentric spheres on each other. The Luneburg lens is a special case of this class in which one sphere has an infinite radius and the other is the lens surface. For a unit-radius lens, the n as a function of the radius r is $n=(2-r^2)^{1/2}$. When fed at a point on the surface, it produces a plane wavefront, and by moving the feed on the surface, beam scan over all space can be obtained (if the presence of the lens support and feed-scanning mechanism is ignored). The scanning applications and many design principles of Luneburg lenses are discussed in Chap. 18.

A number of authors^{67–75} have extended Luneburg's work. References 67 to 70 derive small-feed-circle lenses in which the feed radius is smaller than the lens radius. References 70 to 74 consider variations that include conical and beam-shaping wavefronts in addition to the plane wavefront. Reference 75 considers a design to use a defocused feed.

Luneburg-lens radiation-pattern computations have been considered by most of the Luneburg-lens authors and in particular by Refs. 76 and 77. The Luneburg-lens aperture illumination is the feed pattern times $\sec \phi$, where ϕ is the feed-pattern angle. The increase in energy density near the aperture edges produces (relative to other lenses) high gain and small beamwidths and limits the sidelobe levels to -17 to -18 dB.

Early Luneburg lenses were two-dimensional (or cylindrical) slices through the center of the sphere because techniques were not available for constructing a sphere. One model⁷⁸ was a 36-in- (914-mm-) diameter lens constructed of almost parallel plates filled with polystyrene that operated in the TE_{10} mode at X band. The plate spacing was $a = \lambda/[2(\epsilon_r - 2 - r^2)^{1/2}]$, where ϵ_r is the dielectric constant of the filler material and r is the normalized radius. In addition to the aperture-edge energy increase, two-dimensional Luneburg lenses produce a saddle-shaped wavefront because of the circular aperture. This can be corrected by adding to the aperture parallel plates with a linear aperture, but this limits the beam-scan angle. Calculated and experimental radiation patterns show about -17-dB sidelobes in the E plane and a flat-top pattern in the H plane. Jones⁷⁹ constructed an air-filled, almost parallel-plate TE_{10} -mode lens. Walter⁸⁰ constructed surface-wave lenses with tapered-thickness dielectric on a ground plane, metal posts on a ground plane, and a "holey-plate" structure.

The symmetry of the Luneburg lens can be exploited by adding planar reflectors through the lens center to obtain a virtual-source antenna.⁸¹ This permits eliminating large segments of the lens to reduce weight and allows the lens to be supported more easily, but it introduces aperture blocking by the feed.

Spherical Luneburg lenses have been constructed by using several techniques. Crushed Styrofoam⁸² was used for a 24-in- (610-mm-) diameter lens. Expandable polystyrene beads, ⁸³⁻⁸⁵ expanded and solidified in heated hemispherical molds, were used for a 10-step, equal- ϵ , increment, 18-in- (457-mm-) diameter lens. Reference 86 provides performance of a 10-step Styrofoam 18-in- (457-mm-) diameter lens. Foamed glass⁸⁷ was used to fabricate a 10-step 12-in- (305-mm-) diameter lens to obtain high-power operation. Calculations⁸⁸ of the heat distribution in a Luneburg lens indicate that the feed region reaches the highest temperature under high-power operation. A ray-tracing method for checking the design of a stepped-n Luneburg lens is provided in Ref. 89.

An important use of the Luneburg lens is as a reflector, 85,90 obtained by placing a reflecting cap on the lens surface. An incoming plane wave is focused at a point on the cap and reflected; after transit through the lens the second time, it is a plane wave propagating in the opposite direction. The angular extent of the cap is chosen as a compromise between obtaining wide-angle performance and minimizing partial blockage of incoming rays by the cap.

For many applications that do not require the performance of a Luneburg lens, Refs. 91 to 95 investigate the performance of constant-n spherical lenses that are more

easily constructed than Luneburg lenses.

Another class of two-dimensional Luneburg lenses is the geodesic lens, composed of a pair of nonplanar metal plates spaced a constant distance apart with a spacing small enough so that only a TEM mode can propagate. Myers⁴⁹ proved that rays in this medium follow geodesic paths on the mean surface. Rinehart 6,97 derived the surface shape that is required for a two-dimensional Luneburg analog whose edge has a tangent normal to the aperture plane. References 98 and 99 derived surfaces with the edge tangent parallel to the aperture plane. Kunz100 generalized the analysis and described several designs. Rudduck et al. 101-103 describe small-feed-circle designs and also designs that radiate at a displaced angle from the aperture plane. Johnson 104 provides an excellent summary of geodesic lenses and distinguishes between tin-hat, helmet, and clamshell types. Reference 105 describes a feed-scanning implementation for limited beam-scan angles with a geodesic Luneburg lens. Johnson 106 shows radiation patterns of a 24-in- (610-mm-) diameter, 4.3-mm-\(\lambda \) lens with extension plates to a linear aperture that provides a total beam scan of 60°. The beamwidth is 0.5°, and sidelobes are below -25 dB for most beam positions. Johnson¹⁰⁷ demonstrates that any two-dimensional lens can have a geodesic analog.

16-11 FRESNEL ZONE PLATE LENSES

Lens antennas called *Fresnel zone plates* can be constructed in a planar form. They have the advantages of reduced weight, lower ohmic loss, and ease of construction compared with the conventional dielectric lenses shown in Fig. 16-1. A Fresnel amplitude-zone plate lens consists of alternating opaque (metal) and transparent (dielectric) rings with the radii determined by the zone number. Measured results show that the beamwidth from these lenses is comparable with that obtained from a paraboidal reflector of the same size but that the gain is about 15 dB less. ¹⁰⁸ Fresnel phase-zone plate lenses are constructed by cutting annular rings in a flat piece of dielectric or by utilizing concentric rings of different dielectric materials of the same thickness. ¹⁰⁹ Phase-zone plate lenses do not suffer the inefficiency of amplitude-zone plate lenses because the former are completely transparent.

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Reflector Antennas

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	Planar Reflectors 17-2
	Reflectors with Parabolic Arc 17-6
	Reflectors Other Than Plane or
	Parabolic 17-9
	Point-Source to Point-Source Reflectors 17-11
	Point-Source to Line-Source Reflectors 17-12
	Shaped-Beam, Singly Curved Reflectors 17-14
	Doubly Curved Reflectors 17-14
	Paraboloidal-Type Reflectors 17-17
	Shielded-Aperture Reflectors 17-22
	Passive Reflectors 17-24
	Polarization-Sensitive Reflectors 17-28
	Frequency-Sensitive Reflectors 17-30
17-2	Large-Aperture Reflector Antennas 17-31
	Introduction 17-31
	Pencil-Beam Reflector Antennas 17-31
	High-Efficiency Dual-Reflector Systems 17-39
	Wide-Angle, Multiple-Beam Reflector
	Antennas 17-41

17-1 Conventional Reflector Antennas 17-2

17-1 CONVENTIONAL REFLECTOR ANTENNAS

The reflector antennas treated in the first half of this chapter are those which have been used for decades. The very-high-gain reflectors used in earth stations, which have a more sophisticated design, are treated in the last half of the chapter. The conventional reflector designs are (1) planar, (2) parabolic-arc, (3) double-curvature, (4) paraboloid, and (5) shielded reflectors. In addition, passive reflectors used in communications and radar are described. Sec. 17-2 then considers the sophisticated large reflectors.

Planar Reflectors

Corner Reflector¹ The corner-reflector antenna is made up of two plane reflector panels and a dipole element (Fig. 17-1). This antenna is useful in obtaining gains of the order of 12 dBi. Higher gains can be obtained by using large reflectors and larger spacing of the dipole to the panel intersection. The gain also depends upon the corner angle. Figure 17-2 shows the gain as a function of dipole spacing for four values of corner angle. Figures 17-3 through 17-6 show the radiation patterns for E and H planes. One of the angles is 180°, and the data therefore include the planar reflector.

The size of reflector panels is a compromise between gain and antenna wind load. The wind load is reduced by replacing the panels by parallel rod reflectors with spacing of $\lambda/10$. The rod length should be 0.6λ . The size of the reflector panels must be increased as the dipole spacing is increased. A spacing of $\lambda/3$ requires a panel length of 0.6λ , a spacing of $\lambda/2$ requires λ , etc. The impedance of the corner reflector depends upon the spacing and upon the dipole impedance. Spacings of less than $\lambda/3$ for the 90° corner are not recommended. Larger spacings have less effect on impedance.

An increase in the corner-reflector gain² is obtained by adding a third panel which serves as a ground plane for a 0.75λ monopole feed. The long monopole gives a peak signal above the ground plane (about 45°). The panel lengths are 2λ , and the monopole spacing is about one wavelength. As in the conventional corner reflector, the gain depends upon corner angle and spacing: 90° and 0.9λ give 17 dBi, 60° and 1.2λ give 19 dBi, and 45° and 1.6λ give 21 dBi.

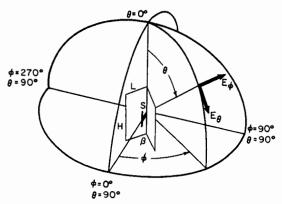


FIG. 17-1 Corner-reflector antenna and coordinate system.

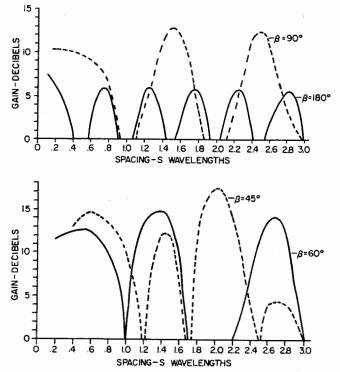


FIG. 17-2 Gain of corner reflectors.

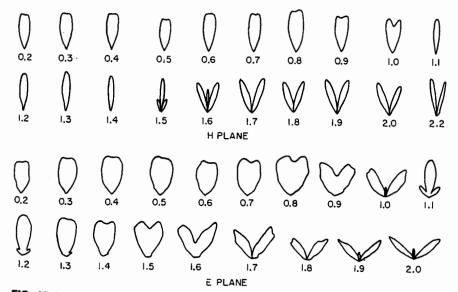


FIG. 17-3 Patterns of 60° corner, S_{λ} variable.

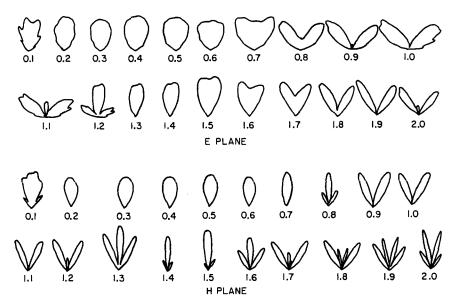


FIG. 17-4 Patterns of 90° corner, S_{λ} variable.

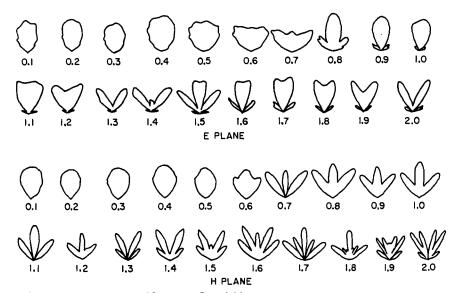


FIG. 17-5 Patterns of 120° corner, S_{λ} variable.

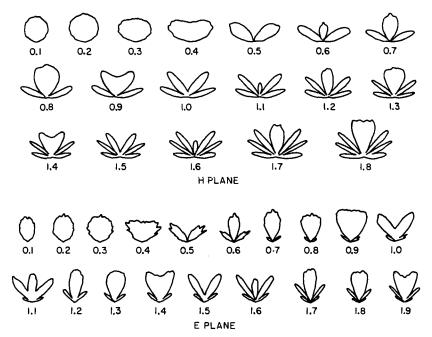


FIG. 17-6 Patterns of flat-sheet, S_{λ} variable.

An increase in corner-reflector bandwidth³ can be achieved with a broadband dipole feed. An open-sleeve dipole with the center section of coaxial line in the sleeve replaced by slab line gave almost an octave bandwidth with a voltage standing-wave ratio (VSWR) of 2.5:1. The gain was 11.5 ± 1 dBi. The match was achieved by a cut-and-try procedure.

Planar Reflectors The antennas in this subsection give good gain for limited size. Their characteristics are shown in Fig. 17-7. The size range is from $\lambda/2$ to 5λ . They appear to have a large reactive field, so good conductors and dielectrics are needed in the design.

 0.5λ by 0.5λ The skeleton-slot antenna⁴ has provided a gain of 9 dBi over the 225- to 400-MHz band. At the lowest frequency, the reflector has a side dimension of one-half wavelength. The driven element is a rectangular loop which forms the edge of a slot. The slot ends are firmly anchored to the ground plane to give a more rugged structure than that of a plane reflector with a dipole as the driven element.

 λ by λ The plantenna⁵ has a very close spacing of the dipole and reflector and employs bent edges of the reflector to give directivity of 11 dBi. This antenna operates over a 1.5:1 band and usually employs a printed-circuit dipole.

 2λ by 2λ The short backfire antenna^{6,7} is the best candidate for high gain over a restricted band. It uses a plane disk reflector of 2λ diameter and a rim at the edge of 0.25 λ . When the dipole driver is in the plane of the rim and the dipole reflector is spaced 0.6 λ from the 2λ reflector, the gain is 15 dBi. For large reflectors the edges are removed, and the gain⁸ is reduced to 12 dBi. When the dipole reflector was removed and the edge retained, the gain was reduced to 11.5 dBi. The dipole had a length of

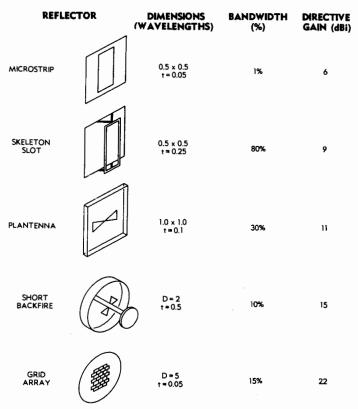


FIG. 17-7 Plane-reflector antennas. Dimension t is the depth of the antenna.

 0.4λ , and the dipole reflector was a disk with a diameter of 0.55λ . In another program, the reflector and the rim were replaced by loops of metal. Six loops were required to replace the reflector, and another six loops to replace the rim. The rim length for best performance was increased to 0.6λ .

 5λ by 5λ This reflector, with a driven element formed as a wire grid, will give gains in excess of 20 dBi. The grid is made up of rectangular building blocks which are $\lambda/2$ by λ . The element is very close to the ground plane so that only the $\lambda/2$ elements radiate; the remainder of the grid serves as the transmission line. Experimental data showed that the λ sides gave a cross-polarized pattern 20 dB below the copolarized ($\lambda/2$) patterns. The wire cross sections can be varied to control the currents on the $\lambda/2$ elements. One design showed a gain of 21 dBi and sidelobes of -22 dB.

Reflectors with Parabolic Arc

The parabolic arc can be used as a generating curve for a number of useful reflector surfaces. When moved so that the focal point travels along a straight line, the curve generates a parabolic cylinder. With a limited motion along this line, the reflector for

a pillbox is generated. When the focal point is moved along a circle enclosing the arc, an hourglass surface is generated, and for a circle which does not enclose the arc a parabolic torus is generated. Figure 17-8 shows the basic parameters of these surfaces.

Parabolic Cylinder The elements of the cylinder are all perpendicular to the plane of the parabolic arc. Because this is a singly curved surface, problems of construction and maintaining tolerances are somewhat easier than those encountered in the case of the paraboloid. The cylinder can be constructed of tubes or slats which are straightline elements of the surface, or it can use identical parabolic arcs formed of tubes or slats positioned so that the planes of the parabolic arcs are perpendicular to the elements of the cylinder.

The widest use of the cylinder is with a line-source feed, which may be formed in a number of ways. The line-source aperture is made to coincide with the focal line of the cylinder (the line made by joining the focal points of all arcs). The aperture of the line source can contain energy in phase along the length or have a linear-phase variation along the length. The first produces a cylindrical wavefront, while the linear-phase variation produces a conical wavefront. The cylindrical wave is focused into a plane wave in the direction of the axis of a parabolic arc. The conical wavefront produces a plane wave tilted from the parabolic axis by an angle equal to the half angle of the cone.

REFLECTOR		EXCITER	GAIN	USE
PARABOLIC CYLINDER		DIPOLE HORN LINE SOURCE POINT SOURCE	10-dB INCREASE	FAN BEAM PENCIL BEAM SCANNING LINE SOURCE
PILLBOX		DIPOLE HORN	15 dB	FAN BEAM PARABOLIC CYLINDER FEED
HOURGLASS		CIRCULAR ARRAY	10-dB INCREASE	VERTICAL GAIN
PARABOLIC TORUS	8	DIPOLES OR HORNS	35 dB	WIDE-ANGLE COVERAGE
ELPAR OR HYPLAR		HORN	15 dB	FAN BEAM

FIG. 17-8 Reflectors with parabolic curves.

The illumination problems of a line-source feed with the cylinder are related to those of the paraboloid. The decrease in energy in the cylindrical or conical wave is proportional to distance rather than to the square of the distance. The space-attenuation factor in decibels is one-half of that given below in Fig. 17-19. The sidelobes present a problem in the parabolic cylinder since the relative gain between the line source and the final antenna system is not sufficient to suppress the sidelobes of the source. Care must be given to the design of the aperture of the line source, particularly in control of the *E*-plane sidelobes.

The feed-blocking problem for a line source and parabolic cylinder is serious since the line source presents a large blockage. For this reason, it is usually desirable to use an offset reflector in which the line-source feed structure is removed from the path of the reflected radiation.

The parabolic cylinder can be fed by a point-source feed horn. The horn illumination function is defined by energy which falls off with the square of distance. The reflected wavefront will be a cylinder with elements perpendicular to the elements of the parabolic cylinder. In one plane the point source is focused, and in the other plane the cylinder reproduces the pattern of the feed horn. The result can be a narrow beam in azimuth and a broad-coverage beam in elevation. The best work on such an antenna¹² used a cylinder with its straight-line elements tilted from vertical. Close-in sidelobes were controlled, and the largest sidelobes (of the order of -28 dB) were removed from the main-beam region. This reflector operated at 9.3 GHz and measured 5 ft by 1 ft (1.5 m by 0.3 m), with a focal length of 1.5 ft (4.5 m). The tilt of the reflector was 12°.

Since the horn and cylinder will give a cylindrical wave and since the parabolic cylinder focuses the cylindrical wave, a second reflector can be used. Use of a point-source feed and two parabolic cylinders gives a final wavefront identical to that of a paraboloid.¹³ If the equation of the first cylinder is $y^2 = 4fx$, with f the focal length, the second cylindrical surface is given by $(x + f)^2 = 4f(z + f)$, and the final rays are all parallel to the z axis. The plane curves of intersection for the cylinders before development are given in Ref. 13.

The parabolic cylinder can also be used as the reflector in the pillbox, or cheese, antenna. The pillbox is formed by two parallel planes which cut through a parabolic cylinder perpendicular to the cylinder elements. Typically the focal line of the cylinder is positioned in the center of the aperture formed by the open ends of the parallel plates. When a feed is placed at the focal line, it blocks a significant portion of the open region. The blockage causes large sidelobes in the pattern of the pillbox. The feed backlobes are significant, and a portion of the feed's radiation is reflected back into itself to produce a standing wave. An improvement in performance is obtained when a half pillbox is used in the same fashion as the offset parabolic cylinder. The arc of the parabola extends from the vertex to the 90° point. The feed horn is pointed at the 45° point, and although the illumination is asymmetrical, good sidelobes are obtained. The maximum sidelobe of -26 dB was from the spillover past the 90° point of the parabolic arc.

Hourglass Reflector¹⁵ The hourglass reflector is generated by rotating a parabolic arc (symmetrical or offset) about a vertical axis which is on the convex side of the arc. The feed system for the hourglass reflector is a circular array. The hourglass serves to give increased gain in the vertical plane. The circular array has the characteristics of the Wullenweber system, ¹⁶ which provides scanning beams, fixed beams, and beams from a hybrid matrix system. The sidelobes in the elevation plane are controlled by

controlling the elevation pattern of the array elements. In the horizontal plane the sidelobes are controlled by tapering the energy in the array elements.

Parabolic Torus¹⁷ This reflector is formed by rotating the parabolic arc about a vertical axis positioned on the concave side of the arc. It can be formed by a symmetrical arc or by the more widely used offset arc. This reflector is fed by multiple feed horns, each of which uses portions of the reflector surface used by adjacent horns. With multiple usage of the surface, a relatively compact structure can be obtained. The torus is discussed in greater detail in Sec. 17-2. The final surfaces with a parabolic arc are the elpar and hypar surfaces with an ellipse and a hyperboloid in the second principal plane. These reflectors are discussed in the next subsection.

Reflectors Other Than Plane or Parabolic

General Surface There are a number of useful surfaces in addition to the plane and the surfaces with a parabolic arc. The coordinates of these surfaces are determined by the required phase and amplitude at points on the reflected wavefront. The phase is associated with the length of the incident and reflected ray paths, ¹⁸ and the amplitudes depend upon the density of the rays. ¹⁹ The most widespread use of general surfaces has been in shaped beams and Cassegrain antennas, but other useful surfaces are included here.

Sphere The first surface considered is the sphere (Fig. 17-9), which was shown in Ref. 18 to have the phase error $2(1 - a^2)^{1/2} + 2(da^2 - 1)$, where d is the distance from the sphere center to the feed and a is the distance from the centerline to the

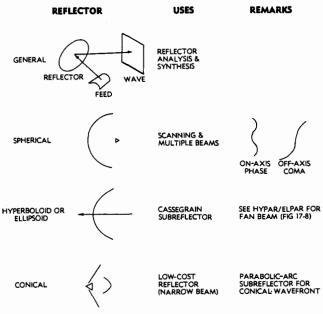


FIG. 17-9 Reflectors other than parabolic.

spherical surface. The sphere has unit radius. A practical sphere is limited in extent. If an attempt is made to scan it to one side, the phase errors do not remain the same but increase as the beam is moved off axis. That is, the value of r in the expression for phase error must increase on one side and decrease on the other. Consider a plane through the sphere containing the axis. The phase-error expression can be plotted in Fig. 17-10 for a number of values of the feed position d. The reflector edges move across the phase-error curves as the feed horn is moved off axis. The error will decrease slightly on one side and increase very rapidly on the other side. A careful analysis of the error will show that it has a strong cubic term (coma), just as the paraboloid has a strong cubic term. The sphere and the paraboloid have similar off-axis characteristics.

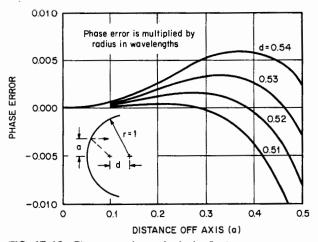


FIG. 17-10 Phase error in a spherical reflector.

If the spherical reflector can have an efficiency of the order of 10 percent, it will give patterns which do not change with the beam moved off axis.²⁰ In this instance, the sphere is fed from a large feed horn which confines its radiation to a small portion of the surface. The reflector edges which were the problem in the normal sphere are then eliminated. In effect, this solution uses a very-long-focal-length system in which the paraboloid and the sphere become very much alike.

The design of the sphere is based upon the phase-error formula. The error curve is used out to the point at which the phase error is zero. An argument can be made that some phase error beyond this point can be accepted. A tapered illumination from the feed will minimize these errors. In practical design, however, the phase error increases so fast that only a marginal improvement is achieved by considering the feed illumination. Some fine tuning can be done with illumination, but the basic design depends upon the simple use of the two points on the phase-error curves, namely, the maximum value and the edge (zero) value which defines the maximum value of the aperture radius r. A simple ratio, namely, maximum phase error divided by r, is used. Let the phase error be $\lambda/16$ and the radius be 10λ (aperture diameter of 20λ). The ratio is 160:1. The design consists of selecting a specific curve using the parameter d which gives a ratio of 160:1. Note that the p coordinate in the figure is greatly expanded compared with the p coordinate.

Point-Source to Point-Source Reflectors

For some applications, it is desirable to produce a virtual source from a given real source. For example, it may be desirable to position a real source at the vertex of a paraboloidal reflector and utilize some surface between the vertex and the focal point which images the real source into a virtual source located at the focal point. The resulting antenna system, a counterpart of the optical Cassegrain system, will then have a focused beam, since the paraboloid is energized by a source which is apparently at the focal point.

It is first obvious that the reflector surface desired must be symmetrical about the axis joining the two sources. If a cross section of the reflector is known, the complete surface can be formed by rotating this reflector arc about the axis. Figure 17-11 indicates the geometry of the two-dimensional problem. The reflected rays should

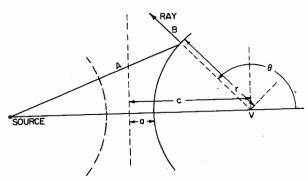


FIG. 17-11 Geometry of hyperbola reflection.

appear to originate at the point v, or, in other words, rays from the real source shall be reflected to form a spherical wavefront with its center at v. Since in the figure we require that A + B be a constant and r + B should be a constant, we find that the surface is determined by the fact that A - r is a constant. From analytic geometry, it is known that the locus of points satisfying this condition is a hyperbola. This curve can then be written as

$$r = \frac{c^2 - a^2}{a \pm c \cos \theta}$$

The quantities here are indicated in the figure. The plus-or-minus sign corresponds to two possible reflector surfaces, one concave and one convex.

Another possible reflector for translating a point source into a point source is an ellipsoid. The ellipse cross section is given by

$$r = \frac{a^2 - c^2}{a + c \cos \theta}$$

where the quantities are the same as in Fig. 17-11.

For application to the paraboloidal reflector mentioned in the first paragraph of this subsection, three surfaces, namely, the ellipsoid and the two hyperboloids, are possible. For practical application, the ellipsoid, which must be mounted at a greater distance from the reflector, is not satisfactory. Of the two hyperboloid surfaces, the

ОΓ

one which can be mounted farther from the reflector illuminates typical reflectors better than the nearer, which requires a paraboloid with large f/D ratio. When the real source is moved from one focal point of the hyperboloid system, the image source will move away from the other focal point but will, at the same time, become distorted. Any great motion of the real source produces a poor image.

Point-Source to Line-Source Reflectors

It has been mentioned that the parabolic-cylinder reflection will convert a point source into a line source. However, this property is not unique for this reflector. Other surfaces²¹ capable of accomplishing the same result have been designated as hypar and elpar surfaces. These have principal plane sections which are hyperbolas, parabolas, and ellipses. It can be seen that in the plane of the parabola rays from the feed source can be focused to be parallel, whereas in the plane of a hyperbola (or an ellipse) the rays can be reflected so that they appear to come from a virtual-source point. This does not prove that the reflected wave is a cylindrical wavefront but indicates only that the cross sections of this wave in the two principal planes correspond to those of a cylindrical wave. A general reflector can be obtained by assuming that the point source lies at the coordinate value (d, 0,0) and that the line source coincides with the z axis as in Fig. 17-12. By taking a general ray not lying in either principal

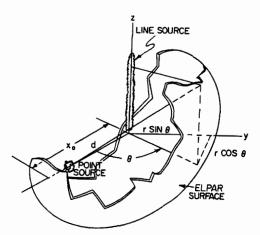


FIG. 17-12 Geometry of elpar surface.

plane and requiring that it have a constant path length between the point source and the line source, it can be shown that the reflector surface is given by the following expression:

$$\sqrt{(r\sin\theta)^2 + (r\cos\theta - d)^2 + z^2} + r = 2x_0 - d$$

$$\sqrt{(x-d)^2 + y^2 + z^2} + \sqrt{x^2 + y^2} = 2x_0 - d$$

All quantities in this expression are shown in Fig. 17-12. If one sets θ equal to a constant, it can be shown that all such sections of the reflector are parabolas, whereas setting z equal to a constant yields ellipses in those planes.

A reflector directly related to that indicated above involves cross sections which are hyperbolas rather than ellipses. The mathematics is similar. Using the quantities of Fig. 17-12, we have the expression

$$\sqrt{(r \sin \theta)^2 + (r \cos \theta - d)^2 + z^2} - r = \pm (2x_0 - d)$$

The plus-or-minus signs indicate two possible surfaces, one concave and one convex. Here it can be shown that the planes $\theta = \text{constant}$ intersect at the surface in parabolas and the planes z = constant intersect it in hyperbolas.

Conical Reflector²² The conical reflector is excellent in applications in which the complexity of a doubly curved large aperture is to be avoided. A simple feed with

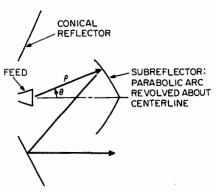


FIG. 17-13 Conical reflector.

spherical wavefront is reflected from a unique surface into a conical wave which is reflected from the conical surface as a plane wave. Figure 17-13 shows a cross section of the three elements which are the basis of this system. The elements are the small horn, the small parabolic-arc reflector, and the conical reflector, which in the figure becomes a straight line. The complete system is obtained by rotating the cross sections about the axis. It can be seen that the tilted straight line when rotated about the axis becomes a cone with the center area open. The parabolic arc when rotated produces an unusual surface with a pointed vertex like a cone. The feed structure (small aperture and

parabolic arc) blocks the center of the cone to give large sidelobes. An offset version of this system will eliminate the blocking, but the additional mechanical complexity reduces the advantage of using the simple cone.

The design of the conical reflector is based upon two angles, (1) the cone angle and (2) the angle which defines the subreflector. The cone angle is found to be 26°; the angle defining the subreflector is about 50°. The equation of the generating curve of the subreflector is $\rho = 2f/[1 + \cos(52^{\circ} - \theta)]$. The zero coordinate of this curve coincides with the phase center of the feed. Reference 22 gives detailed design data which show that the optimum configuration has a usable annular ring of aperture with width 1.25 times the radius of the parabolic-arc reflector. Experimental measurements showed a gain in excess of 40 dBi with sidelobes of -12 dB.

The conical reflector can also be used as a magnifier system in which a smaller aperture radiates a plane wave toward a conical subreflector of equal aperture. The reflected conical wavefront then is used to feed the same conical reflector of Fig. 17-13. The concept is essentially the same as that of the figure except that the initial wavefront is a plane rather than the spherical wave from the horn antenna. The magnification gives an increased directivity of the order of 2.5:1.

Shaped-Beam, Singly Curved Reflectors

This problem is essentially two-dimensional, so that ray paths can be restricted to a plane and the cylindrical-reflector surface can be obtained from its plane-curve generator. The basic concepts for the design of a singly curved reflector are simple; the desired shaped-beam pattern is obtained point by point from the primary-feed pattern. The problem presented is that of forming the reflector to make any particular segment of primary-pattern energy appear at the desired point in space. Two basic conditions must be satisfied. The first is that of the energy correspondence between primary $I(\phi)$ and secondary pattern $P(\theta)$, which can be expressed as

$$\frac{\int_{\theta_1}^{\theta} P(\theta) \ d\theta}{\int_{\theta_1}^{\theta_2} P(\theta) \ d\theta} = \frac{\int_{\phi_1}^{\phi} I(\phi) \ d\phi}{\int_{\phi_1}^{\phi_2} I(\phi) \ d\phi}$$

where ϕ and θ are the primary- and secondary-pattern angles and the subscript values correspond to the reflector limits. The second condition relates the angle of incidence to the radius vector defining the surface:

$$\frac{\rho'}{\rho} = \tan i = \tan \frac{\phi - \theta}{2}$$

The relationship between θ and ϕ obtained from the first expression can be substituted in the second expression so that a differential equation is obtained between the radius vector ρ and the feed angle ϕ ; this relationship defines the desired reflector curve.

The most difficult part of the shaped-beam problem is that of computing the desired curve from the above expressions. Quite often the first expression must be solved graphically so that the differential equation also requires a graphic solution. If the functions $P(\theta)$ and $I(\phi)$ are integrable, then the first expression can be solved for $\theta(\varphi)$ and the second expression becomes

$$\ln \frac{\rho}{\rho_1} = \int_{\sigma_1}^{\sigma} \tan \frac{\varphi - \theta(\varphi)}{2} d\varphi$$

and the integral is evaluated by numerical methods. If the pattern functions are not integrable directly, numerical methods are used. First, a plot is made of the pattern functions. Next, the four integrals in the first expression are evaluated by obtaining the corresponding areas under the curves. For the integrals with variable upper limits, many different values of the area must be found, corresponding to different values of the variable. With this information, it is possible to obtain the two curves of Fig. 17-14. These curves are used to obtain the desired value of θ for any given value of ϕ . With this known, $\tan \{[\varphi - \theta(\varphi)]/2\}$ is plotted and the integral evaluated so that $\rho(\varphi)$, the desired curve, can be obtained.

Doubly Curved Reflectors²³

The problem of beam shaping becomes somewhat more complicated when the reflector is to shape the beam in one principal plane and focus it in the other plane. Since the problem is a three-dimensional one, the possibility also exists that the feed might not produce a simple spherical wavefront but might also yield a cylindrical surface, a foot-

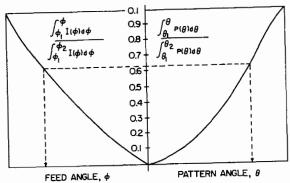


FIG. 17-14 Relationship between feed angle and pattern angle in a shaped reflector.

ball-type surface, or any one of a number of other surfaces. Fortunately, all feed systems of interest have a circular wavefront in the plane of beam shaping, so that techniques similar to that employed in the preceding subsection can be utilized to determine the surface cross section in that plane. The existing techniques consist of forming the reflector surface from the plane-curve cross section, which serves as a spine, and a series of other plane curves which are attached as ribs to the spine. Some question has arisen regarding this general technique, but it has been found to produce satisfactory experimental results for cases in which beam shaping is desired over a limited angle. This problem may be studied more carefully for application to beam shaping over wider angles.

The plane curve, identified as a spine above, has been called the central-section curve. This curve is found in a manner quite similar to that described in the preceding subsection. The design equations for the feed with spherical wavefront are obtained, using the same quantities as before:

$$\frac{\int_{\theta_1}^{\theta} P(\theta) \ d\theta}{\int_{\theta_1}^{\theta_2} P(\theta) \ d\theta} = \frac{\int_{\phi_1}^{\phi} \frac{I(\phi)}{\rho} \ d\phi}{\int_{\phi_1}^{\phi_2} \frac{I(\phi) \ d\theta}{\rho}} \qquad \frac{\rho'}{\rho} = \tan \frac{\phi - \theta}{2}$$

The major difference between these expressions and the previous ones occurs in the presence of ρ under the integral sign. The integration can be carried out as before if first ρ is assumed to be a constant over the shaped portion of the central-section curve; then follow a parabolic arc $[\rho = \sec^2(\phi/2)]$ over the region which produces the main beam. With this assumption, the procedure is identical with that of the last subsection for obtaining the function $\rho(\varphi)$. This function represents a closer approximation to the correct value than the original assumption. When it is used as the value under the integral sign and the entire procedure is repeated, a new value of $\rho(\varphi)$ that is as close to the true value as necessary in any practical case is obtained.

A discussion of the rib curves will indicate the limitations in the present techniques. To obtain the ribs, it is customary to consider an incoming bundle of rays from the secondary-pattern angle θ . For beam shaping in the vertical plane, this bundle of rays is confined to a plane making an angle θ with the horizontal plane. It is required

that the reflector surface direct these rays to the feed position. Figure 17-15 shows two parallel rays in this plane which intersect the reflector in the curve AA'. The rays

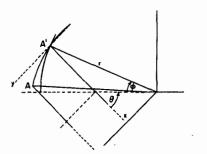


FIG. 17-15 Geometry of a three-dimensional shaped reflector.

between the points A and A' are reflected to lie on a conical surface with apex at the feed.

If we considered the transmit case and a plane sheet of rays emanating from the feed point, they would intersect the reflector in a curve AA' and the reflected rays would lie on a cylindrical surface tilted at an angle of θ with the horizontal plane. It should be apparent that although they have the same end points, the plane curves AA' are not the same for the transmit and receive cases. This can be understood since it is known that if focusing is desired, the reflector surface

in the neighborhood of the points of ray incidence must be a paraboloid. The plane curve cut by this paraboloid will be different if we consider the intersection caused by the transmit plane passing through a focal point and that caused by the receive plane inclined at an angle θ to the horizontal. It is difficult to make a choice between the two curves, although the great majority of existing efforts have chosen the receiving-plane case. A compromise solution might be the plane bisecting the angle formed by the transmitting and receiving planes. The parabolic curve for the receive case mentioned above is

$$y^2 = 4z\rho\cos^2\frac{\theta + \varphi}{2}$$

Here z is the coordinate measured from the point \mathcal{A}' away from the reflector, and y is the orthogonal coordinate. It should be noted that each of the rib curves is a parabola lying in a different plane; when the reflector surface is formed, the planes of various parabola ribs must be inclined at the corresponding angles.

All the previous expressions yield only normalized coordinates for the surface; these must be converted to usable dimensions before the reflector can be constructed. It is desirable to make the central-section curve as large as possible in order to minimize the diffraction effects on the shaped-beam pattern. In the other plane, the reflector size is chosen to produce the desired beamwidth. The feed angles associated with the reflector are chosen in a manner similar to those of the simple paraboloid. It is desirable that the aperture illumination be 10 dB down at the reflector edges.

The most advanced technique²⁴ for defining the reflector for beam shaping permits beam control in both principal planes. A two-variable generalized far-field pattern is used to define the reflector surface. The generalization is achieved by replacing the ray-to-ray correspondence by a curve of incident ray directions related to a curve of reflected ray directions.

The caution in the use of any ray relationship is that it ignores diffraction effects. Therefore the reflector defined by geometrical optics should be checked by defining the phase and amplitude across the reflector aperture and integrating for the far-field patterns.

Paraboloidal-Type Reflectors

The most useful of the high-gain reflector antennas utilizes the paraboloidal surface, which is formed by rotating the arc of a parabola about the line joining the vertex and the focal point. The geometrical relations for such a reflector can be obtained from Fig. 17-16, which represents a typical cross section through the reflector in a plane containing the axis. The major problems associated with this reflector antenna are

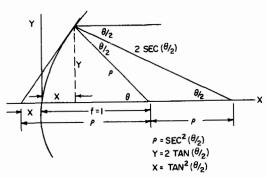


FIG. 17-16 Geometric relationships in parabola with unit focal length.

related to obtaining an efficient combination of reflector and feed. If it is assumed, for convenience, that the typical feed pattern can be described as a cosine function of the angle measured away from the peak of the beam, some general conclusions can be found. The first is that the reflector cannot intercept all energy from the feed, as might be desirable for maximum gain. A second consideration is that in attempting to intercept all this energy, the reflector size becomes large and its outer portion, which represents a considerable amount of the reflector area, receives a low-intensity field from the feed. This tends to minimize the abrupt field discontinuity at the reflector edges and so minimizes sidelobes. Since reflector size is limited from the mechanical-design standpoint, it is often desirable to minimize reflector regions of low intensity. A compromise must therefore be reached between making the reflector sufficiently large to capture the feed energy and making it too large to be useful from a mechanical standpoint.

In a typical design the reflector size is chosen to be as large as practical, and then the feed is designed for efficient illumination. Normally, the design is based on obtaining either the maximum gain from the antenna or a reduction in sidelobes at the expense of a slight decrease in gain. For maximum gain, it has been found that the energy reflected should be distributed so that the field at the reflector edges is approximately 10 dB below that of the center; for good sidelobe performance, the field at the edge should be about 20 dB down.

It has been found useful in feed design to employ a set of curves which will indicate the beamwidth of the feed necessary to produce the desired edge illumination on a particular reflector. One of the curves utilized is a normalized feed pattern (Fig. 17-17). This pattern was obtained through a comparison of many experimentally mea-

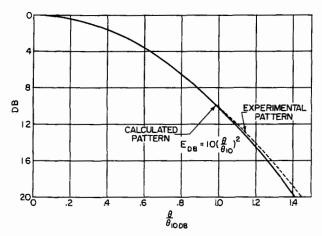


FIG. 17-17 Universal feed-horn pattern.

sured data points. It can be closely approximated over all but the lower-intensity regions of the beam by a simple quadratic function. The beamwidth at any point is proportional to the square root of the decibel reading at that point. For example, the beamwidth is doubled when the decibel reading is increased by a factor of 4. This curve is necessary because of the fact that beamwidth information is normally available only at a particular decibel value, such as 3 or 10 dB, whereas in actual application we are interested in the beamwidth at the points where rays are directed to the edges of the reflector.

To relate the reflector geometry to the pattern beamwidth, a second curve is necessary. Normally, the information available on the paraboloidal-reflector surface is its focal length and aperture dimension, so that we can immediately use the ratio of these quantities, designated by f/D. From the information of Fig. 17-16 it is possible to produce a curve relating the f/D ratio to the feed angle θ . This relationship is given graphically in Fig. 17-18.

Once the feed angle corresponding to the reflector edges has been determined, it would appear possible to utilize Fig. 17-17 directly in order to obtain a value of edge illumination. However, one additional factor must be considered, the divergence factor $(\cos^4 \theta/2)$. This function can be converted to decibels and plotted in Fig. 17-19. It is evident from the figure that the space-attenuation factor is negligible for small values of feed angle and becomes relatively large for feed angles of the order of 90°.

To understand the use of Figs. 17-17 to 17-19, a typical problem can be solved. If it is required that the edge illumination should be 20 dB in a reflector whose f/D ratio is 0.5, we first enter the curve of Fig. 17-18 and find that the total feed angle is 106°. From Fig. 17-19, the space attenuation at this angle (53° from the axis) is 1.9 dB. The desired edge illumination can then be found by noting that the feed horn should have a signal 18.1 dB down at an angle of 53° from the peak of the beam. Since the feed-horn design curves are given in terms of the 10-dB beamwidth, it is necessary to determine what 10-dB width is associated with 18.1 dB at 53°. Since, as previously stated, the beamwidth ratio is proportional to the square root of the decibel ratio, the desired width is given by $(10/18.1)^{1/2} \times 53^{\circ} = 39.5^{\circ}$, so that the total 10-dB width is equal to 79°.

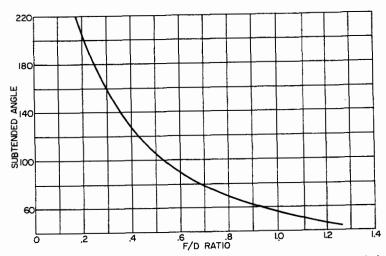


FIG. 17-18 Ratio of focal length to aperture diameter versus subtended angle at focal point.

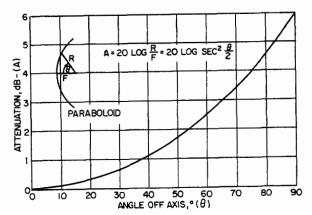


FIG. 17-19 Space attenuation versus feed angle.

Some slight improvement in accuracy might be obtained if the quadratic nature of the beamwidth were ignored and the standard pattern of Fig. 17-17 used. From this figure, it is found that the ratio in beamwidth between 10 and 18.1 dB is equal to 0.73, which corresponds to a feed whose 10-dB width is 77.5°. Because of the negligible difference between these two answers, it can be seen that for most practical applications the quadratic approximation to the standard pattern can be employed.

Interaction between Reflector and Feed From the considerations of the previous section, it is evident that the design of the reflector cannot be entirely divorced from that of the feed. An even more significant relationship arises when one considers interaction between these two elements. Because of this interaction, the feed disturbs

the radiation pattern of the reflector and the reflector affects the match of the feed. A third problem of considerable significance in smaller reflectors is the contribution of the backward radiation from the feed to the pattern formed by the reflector. This effect tends to raise the sidelobe level of the radiation pattern as the reflector aperture is decreased below an aperture of 10 wavelengths.

The effect of the horn on the radiation pattern of a large reflector can be analyzed in a very simple manner. The horn, with its associated waveguide, represents an obstacle in the radiating aperture. The final radiation pattern can be shown to consist of the pattern from the unobstructed aperture minus the pattern of the obstruction. This very simple analysis has been shown to be satisfactory and to compare very closely with measured experimental results. Since, in general, the feed design is determined from mechanical considerations and from the reasoning of the preceding subsection, a minimization in the effect of feed blocking is obtained only as the aperture size in wavelengths increases. This is due to the fact that the feed geometry depends primarily on the angular sector of the dish and so is unchanged as the reflector size in wavelengths is increased. It should be noted that the feed obstruction, that is, the feed horn plus waveguide, is normally limited to a single plane. The effect of this obstruction on sidelobe performance is then most pronounced in the plane perpendicular to the feed obstruction where the obstruction pattern is very broad. In the other plane, the obstruction pattern has a much narrower beamwidth, which approaches that of the reflector and so is relatively weak in the regions where it might contribute an increase in sidelobe level.

The above discussion of feed obstruction assumes that the dimension of this obstruction in the direction of propagation is relatively small; however, if this dimension becomes appreciable, the effect of the obstruction on the feed pattern becomes more complex, and in almost every case a further increase in sidelobe level is found. Experimentally, it has been determined that the minimum value of sidelobe level is obtained if the feed structure in the direction of propagation is streamlined. This has been accomplished by enclosing all parts of the feed structure, with the exception of the feed horn itself, in a thin cylinder whose cross section approximates an ellipse of large ratio between major and minor axes.

The effect of the reflector on the match of the feed horn can be analyzed in a simple manner if it is understood that most of the energy reflected back into the feed comes from the region in the neighborhood of the reflector vertex. Since the incident wave was divergent, a focal length large in wavelengths would tend to minimize the amount of signal reflected back to the feed. For a given reflector, an increase in the gain of the feed, which corresponds to an increase in peak signal compared with signals from other directions, will result in greater energy incident upon the reflector vertex and therefore a greater reflected wave and a greater mismatch. From these considerations it can be shown that the reflection coefficient introduced by the presence of the paraboloid is given by $\Gamma = g\lambda/4\pi f$, where g is the gain of the feed in the direction of the vertex.

It is of interest to determine the proper value of focal length for minimum mismatch if the reflector aperture and illumination are held fixed. Since for a circular aperture the feed gain is inversely proportional to the beamwidth squared, it can be replaced in the formula by the square of an angle, which except for space attenuation is directly related to the angle θ , subtended by the aperture at the focal point. Since the aperture diameter is given by $D = 2f \tan (\theta/2)$ (Fig. 17-16), we can write $\Gamma \propto [\tan (\theta/2)]/\theta^2$, which indicates a smaller value of reflection coefficient for large θ , that

is, for short focal lengths. The minimum reflection is limited by the decreased value of reflector gain realized when a short-focal-length reflector is used.

Paraboloid Edge Configuration The paraboloid shape can be circular, elliptical, or diamond-shaped or of any other configuration. The edge configuration can be used to control sidelobes in the same manner that the feed taper controls sidelobes. The sidelobes in any plane through the aperture are determined by considering the illumination function along the line where the plane intersects the aperture. Figure 17-20 shows how the illumination function is determined when the line of interest is the x axis. The value at a point x depends upon the energy along the line perpendicular to x. For a given feed illumination, the energy depends upon the length of this line.

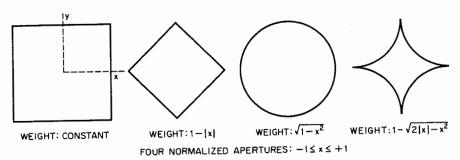


FIG. 17-20 Aperture illumination weighting.

That is, the longer the strips of energy, the greater the total energy at the point x. The diamond-shaped aperture has a taper in the line length as x increases, so that the illumination of a given feed horn is tapered by the use of a diamond configuration. The rectangular configuration gives no additional taper to the feed-horn illumination. The circle gives some taper and is the same for all planes through the aperture. It was found experimentally by the author in the late 1940s that a diamond with concave edges gave the best performance for horizontal-plane patterns. It should be noted that the sidelobes in a 45° plane will have much higher levels. The same analysis of the length of line perpendicular to the aperture line will give the illumination taper for any plane cutting the aperture.

The reason for caution in the use of the edge configuration to control sidelobes is that the spillover from the horn may be increased, which reduces the gain and gives sidelobes far removed from the main beam.

The illumination taper can also be controlled by using nonreflecting material at the edges of the aperture. The surface-impedance variation near the edges of the aperture will have a significant effect²⁵ on the far-out sidelobes. The surface-impedance approach can also be applied to the edges of the subreflectors used in Cassegrain systems.

Another illumination characteristic of interest is related to varying the illumination function in one of the principal planes while holding the taper fixed in the other plane. As expected, the increased illumination taper decreases the near-in sidelobes. However, this taper in one plane will increase sidelobe levels in the other plane. The reason for this can be traced back to the explanation of Fig. 17-20. The illumination along the aperture line is weighted by the field in a strip perpendicular to the line. The

taper in one plane (for example, the horizontal plane) tends to decrease the field at the center of the other (vertical) principal plane. A decrease in illumination in the center of the vertical line through the aperture means less illumination taper in that plane and so higher sidelobes (Fig. 17-21).

The edge configuration has played an important role in compact ranges which use paraboloids. The edges are serrated²⁶ⁿ or rolled^{26b} to reduce the intensity of edge energy (typically toroidal wave) in the quiet zone region near the paraboloid aperture. The best serrations appear to be 10 wavelengths long at the lowest frequency of operation. The best rolled edges have an elliptical cross section, and the extent of the ellipse is on the order of 10 wavelengths.

Shielded-Aperture Reflectors

In some applications it is desirable to have very low sidelobes from a pencil-beam reflector. In this instance, considerable improvement can be obtained by the use of metal shielding around the reflector aperture (Fig. 17-22). The typical sidelobes are at about 0 dBi, which for most reflectors represents a value of the order of -30 to -40 dB below the peak gain. With a shielding technique, the far-out sidelobes can be reduced to -80 dB.

The simplest approach to shielding the reflector is a cylindrical "shroud," or tunnel, of metal around the edge of a circular reflector (Fig. 17-22). If the aperture is elliptical in cross section, an elliptical cylinder can be used. The tunnel forms a waveguide of large cross section with the paraboloid at one end. The radiated energy has low levels of current on the outside edge of the tunnel and so has little radiation at wide angles from the beam. There is energy in the waveguide which leaves the feed horn to reflect from the inside of the cylinder. This energy is then reflected by the paraboloid into angles away from the axis.

An improved shielding system which eliminates the reflection of the feed-horn energy is shown in Fig. 17-23 as the *horn reflector*. The two versions employ a pyramidal horn and a circular-waveguide horn. These antennas are discussed in Sec. 30-5, "Conical and Pyramidal Cornucopias," in Chap. 30. The variation among cornucopia horns is associated with the variation in aperture illumination. In many applications, the low sidelobe capability is associated primarily with the horizontal plane

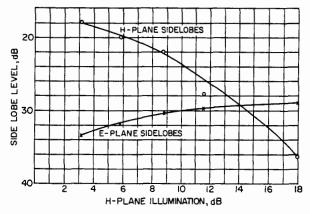


FIG. 17-21 Sidelobe level as a function of illumination.

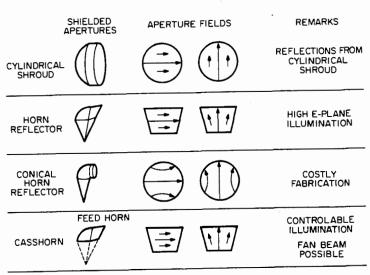


FIG. 17-22 Shielded-aperture reflectors.

where interfering sources are found. The circular aperture will give reduced lobes, and the diagonal aperture (see discussion of aperture illumination in the preceding subsection) will give the best performance. The references for experimental cornucopia design are given in Sec. 30-5.

The final shielded horn to be considered is the casshorn,²⁷ which uses a secondary reflector to replace the horn structure in the cornucopia. The secondary reflector is designed in the same manner as the Cassegrain system. In the lowest-cost version the reflector is plane.²⁸ The aperture of the casshorn can be formed in a variety of ways according to the illumination concepts discussed earlier. An elliptical aperture can be designed as easily as a trapezoid or circular aperture. The feed for the casshorn is mounted at one edge of the aperture (Fig. 17-22). The problems in the design are

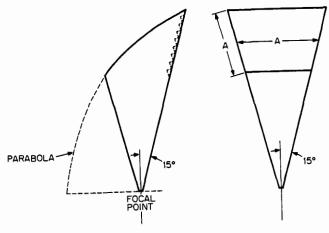


FIG. 17-23 Geometry of horn reflector.

associated with making sure that the feed pattern is not distorted by the nearby reflector surface.

A comparison of the casshorn and the cornucopia indicates that the free-space feed of the casshorn can be used to provide more illumination taper for the aperture (particularly in the E plane) than the cornucopia. However, the casshorn has not proved to be superior to the cornucopia in sidelobe performance. Greater application of shielded antennas can be expected as the number of microwave installations increases.

Passive Reflectors

There are reflector systems which do not contain a feed source. These reflectors, which are called passive, usually receive and reflect a plane wave. There are three general types of passive reflectors: (1) those used in microwave links, (2) those used as radar targets, and (3) those used in a beam waveguide.

Microwave Relay The passive reflectors^{29,30,31} used in microwave links can be classified as repeaters or periscopes. The first reflector system controls a plane wave in the

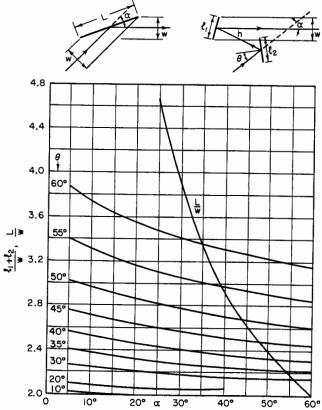


FIG. 17-24 Variation of (normalized) mirror length with α and θ for single- and double-mirror passive repeaters.

horizontal plane, and the second controls the plane wave in the vertical plane. The design information for repeater reflectors given in Fig. 17-24 shows the geometry of a single-reflector and a dual-reflector repeater system. The reflector surfaces should be within $\lambda/16$ of a plane. The extent of the plane surface should be minimized to reduce costs. The figure shows dual and single reflectors with the dimensions required for various angles of the ray paths. The path loss for the two systems can be calculated by assuming that the projected area seen by the transmitter and receiver is the same (and assuming that in the case of the two-reflector system all the transmitter energy captured by one reflector is reflected from the second reflector). If the ranges from the transmitter and receiver are given by d_t and d_D then the path loss is

$$10 \log \frac{\lambda^4 d_1^2 d_2^2}{A_T A_P A}$$

where the areas are designated for transmitter, receiver, and projected area of the repeater plane surfaces.

The periscope reflector system uses a large reflector at the top of a tower and a smaller reflector on the ground. This antenna can employ a plane reflector or a curved reflector at the top of the tower. The gain obtainable from the two type surfaces is shown in Figs. 17-25 and 17-26.

Radar Targets Radar targets are passive reflectors which have a reflected-signal distribution similar to the patterns of an antenna. A number of classical targets are given in Fig. 17-27. The basic problem in the design of radar targets is that of maximizing the target return. Mechanical tolerances of the reflector surface limit the performance. For targets of the order of 20λ in extent, a $\lambda/3$ error in the edges will give

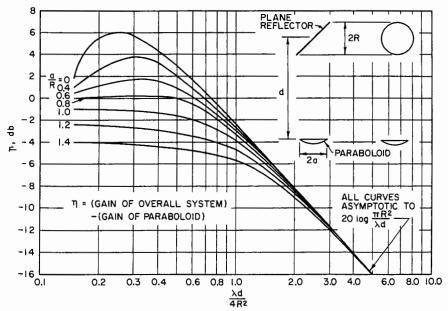


FIG. 17-25 Relative gain of a periscope antenna system employing a plane elevated reflector.

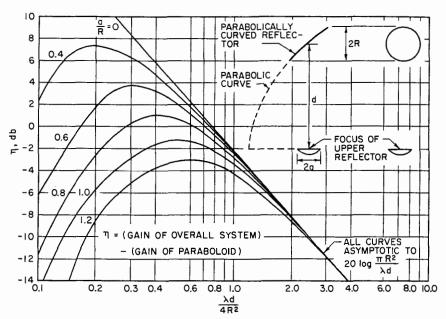


FIG. 17-26 Relative gain of a periscope antenna system employing a curved elevated reflector.

a loss of 3 dB in the returned signal compared with a perfect target. Figure 17-28 shows the loss for three different corner reflectors for angular errors of the order of 2°.

The simple corner reflector is usable over an angular sector of about 30°. For a wider-coverage angle, an array of corner reflectors can be employed, or the Luneburg lens can be used with a spherical cap reflector³³ (see Fig. 17-29). The figure shows that the maximum-coverage angle is of the order of 120°. Another lens³⁴ which gives a theoretical return from all directions has been developed. This lens was fabricated by Emerson & Cuming, Canton, Massachusetts. The index variation is given by $n^2 = (2 - r)/r$. The dielectric constant required for small r becomes very large (at quarter radius the value is 7.5). It is possible to replace the center of the lens by a metallic sphere in order to avoid the large dielectric constant. The center portion represents only a small portion of the aperture, so that an operable system could be achieved without the expense of specialized dielectrics.

For coverage in all directions of space, a combination of 20 corner reflectors (duodecahedron) has been used successfully tested.³⁵ The difficulty in obtaining reproducible lenses has made this reflector approach more satisfactory.

Beam Waveguide The final use of passive reflectors is in earth stations, where typical waveguide losses cannot be tolerated. The beam-waveguide concept uses a series of large-aperture reflectors to transmit energy with little loss. Initial work on such waveguides³⁶ used lens-type apertures. The best existing beam waveguide uses a series of paraboloids, hyperboloids, or ellipsoids. The energy is carried along the guide from one focal point to another, and at each focal point it is received from one reflector aperture and transmitted to the next reflector.

TYPE		MAXIMUM		ANGULAR RESPONSE	
	DIMENSIONS	AT	σ	θ	φ
SPHERE	φ de la	<u>a λ</u> 2	π a ²	360°	360°
CYLINDER	φ φ φ φ φ φ φ φ φ φ	b√ <u>a X</u>	<u>2παb²</u> λ	360°	SHARP
FLAT PLATE	b 100	ab	$\frac{4\pi a^2 b^2}{\lambda^2}$	SHARP	SHARP
DIHEDRAL CORNER	b o le	√2ab	8 π σ ² b ²	± 30° (TO - 10 DB ECHO LEVELS)	SHARP
TRIANGULAR TRIHEDRAL	100	$\frac{a^2}{\sqrt{3}}$	4 π a ⁴ 3λ ²	9 = 0 8 40 20 0 -50° 0 50° 0 50°	θ=0 Θ=0 Θ=0 Θ=0 Θ=0 Θ=0 Θ=0
SQUARE TRIHEDRAL	970	√3°°	12 π α ⁴ λ ²	Αθ 13 0 14 0 15 0 16 10 17 0 18 10 18 10 1	θ = 0 N 40 N 40 N 50° 0 50°
NOTES	$\begin{array}{l} A_T = & \mbox{EQUIVALENT FLAT-PLATE AREA OF TARGET} \\ \sigma = & \mbox{SCATTERING CROSS SECTION OF TARGET} \\ \hline \sigma = & 4\pi\frac{A_T^2}{\lambda^2} \\ P_R = & P_T\frac{A_R^2A_T^2}{\lambda^4\ d^4} = & P_T\frac{A_R^2\ \sigma}{4\pi\ \lambda^4\ d^4}\ (\mbox{FREE-SPACE TRANSMISSION}) \\ P_T = & \mbox{POWER EMITTED BY RADAR} \\ P_R = & \mbox{ECHO POWER COLLECTED BY RADAR} \\ d = & \mbox{DISTANCE FROM RADAR TO TARGET} \\ A_R = & \mbox{EFFECTIVE AREA OF RADAR ANTENNA} = & \frac{G\lambda^2}{4\pi}\ , \ \mbox{WHERE G = GAIN} \\ \lambda = & \mbox{WAVELENGTH IN SAME UNITS AS d, } \sqrt{A_R}\ \ \mbox{AND} \sqrt{A_T} \\ \mbox{ALL DIMENSIONS ARE ASSUMED LARGE IN WAVELENGTHS} \\ \theta = & \mbox{AND} \phi = \mbox{ARE ANGLES BETWEEN THE DIRECTION TO THE RADAR ANTENNA AND THE MAXIMUM RESPONSE AXIS OF THE TARGET} \\ \hline \end{array}$				

FIG. 17-27 Characteristics of various types of radar targets. The columns labeled A_T and σ give the maximum values of these quantities for optimum orientation of the target. G is the gain of an antenna over an isotropic radiator.

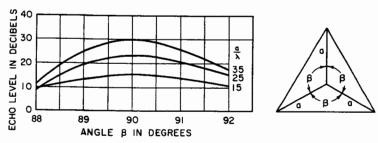


FIG. 17-28 Effect of error in all three corner angles upon a trihedral echo response. Incident radiation is parallel to the symmetric axis.

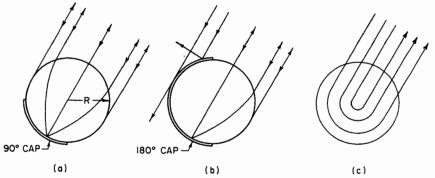


FIG. 17-29 Lens reflectors. (a) 90° cap. (b) 180° cap. (c) No cap.

Figure 17-30 shows the geometry of the most effective beam waveguide. The reflectors used are either paraboloid-paraboloid or ellipsoid-hyperboloid.^{37,38} With the configuration chosen, it is possible to eliminate rotary joints in the transmission line. There is very little loss in beam waveguides, and they can be shielded from external signals by the use of large metallic cylinders which encase the beams as they travel between reflectors.

Polarization-Sensitive Reflectors39

One or more reflectors in an antenna system can be made up of linear parallel reflectors which will reflect one polarization and transmit the orthogonal polarization. Such reflectors are called *transreflectors*. When they are aligned with the linear reflecting elements at 45° to the incoming polarization, half of the energy is passed and half is reflected. A second solid reflector will redirect the transmitted energy back through the linear elements with a phase which depends upon the spacing between the linear elements and the solid reflector. A spacing of one-eighth wavelength creates a 90° phase shift and circular polarization. A spacing of one-quarter wavelength creates a half-wave phase shift and a reflected polarization at 90° from the incident polarization. This system is called a *twist reflector*.

A transreflector can be used as a focusing device which has 360° coverage in the azimuth plane. The linear elements are aligned at 45°, so that half of the incident linear or circular polarization is passed and the remainder is scattered. The reflector

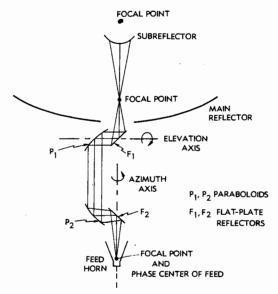


FIG. 17-30 Geometry of a beam-waveguide feed system.

appears as a dome which in the azimuth plane shows the near-side linear elements to be orthogonal to those on the far side. Therefore, the energy which passes through the near side of the dome is reflected at the far side. If the surface contour matches a sphere (helisphere) or parabolic torus, the energy which reflects from the far side is focused.

The transreflector in a planar configuration can be used to provide two-feed systems in a single reflector. That is, a horizontally polarized signal can pass through vertically polarized reflecting elements. The transreflector can be placed between a paraboloidal reflector and the horizontally polarized feed at the focus. A second, vertically polarized feed can be placed at the image of the focal point in the plane reflector. This has been termed focus splitting.

A unique use of the transreflector and twist reflector lies in providing a thin focusing system with a very low f/D ratio.* The paraboloid with focus in face has an f/D ratio of 0.25. A transreflector mounted across the face of the curved reflector will return the energy to the curved paraboloidal surface, where it is rereflected. If this surface is a twist reflector, the reflected radiation is shifted through 90° in polarization so that it now passes through the transreflector. The parallel beam of rays from the system was created by reflection at two curved surfaces (two uses of the twist-reflector surface), and therefore the surface curvature required is reduced. The f/D ratio is reduced to 0.125. A further reduction in the f/D ratio is obtained if a Cassegrain subreflector is added and the feed is placed at the vertex. The f/D ratio then is 0.08.

The transreflector or the twist reflector is made up of about 10 linear elements per wavelength. Accurate planar surfaces can be easily obtained by printed-circuit-

^{*}See J. P. Shelton, U.S. Patent 4,228,437, Oct. 14, 1980.

card techniques. Curved surfaces are best formed with the same technology, and for this reason polarization-sensitive reflectors are most often used for physically small surfaces.

Frequency-Sensitive Reflectors⁴⁰

It is possible to design a reflector which will pass signals of one frequency band and reflect signals of other frequencies. These reflectors are called *dichroic* or frequency-sensitive surfaces (FSS). Such reflectors are made up of a large array of closely spaced resonant elements. Slots or dipoles can be used. The dipoles reflect the chosen frequency band, and the slots transmit this band. When the dipoles become small compared with a wavelength of interest, there is limited reflection and most of the energy is transmitted. When the slots become small compared with the wavelength of interest, the energy is almost totally reflected. By a proper choice of dipoles or slots, the passband can be at a higher or lower frequency than the second band of frequencies.

The most important constraint in the design is the spacing between the two bands of frequencies. If there is an octave band or less, the design becomes difficult and greater losses are introduced. If two octaves separate the bands, the design restrictions are not severe. For sharper response between frequency bands, it is possible to use two or more surfaces, in a manner analogous to transmission-line filter design. The remaining serious design problem is associated with polarization. The surface should preserve the incoming polarization for any angle of incidence. Most surfaces have a different response to polarization in the plane of incidence than to orthogonal polarization.

Polarization limitations have ruled out simple patch and crossed dipole elements in the frequency-sensitive array. The two most widely used elements are the *tripole* and the *Jerusalem cross* (Fig. 17-31). These elements can be more tightly packed in an array. The support of these elements presents a practical design problem since the substrate dielectric will distort the design. Thin Mylar or Kevlar is used for the array, and foam dielectric is used for support of the reflector array.

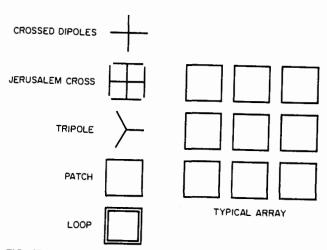


FIG. 17-31 Elements of frequency-sensitive surfaces.

17-2 LARGE-APERTURE REFLECTOR ANTENNAS

Introduction

Reflector antennas with electrically large apertures, greater than 60 wavelengths, became relatively common in the 1970s. The design of such antennas is dominated by considerations of geometrical optics, 41,42,42a which are often refined by considerations of physical optics. 43,44 There remain parameters of concern: gain, beamwidth, sidelobe level, polarization and cross-polarization, antenna noise temperature, and, if more than one beam position is needed, the variation of these parameters with scan angle. The feed design or, in the case of more complex antenna optics, the design of the feed system and subreflector intimately affect the parameters through illumination control, feed polarization properties, and spillover past the subreflector or the main reflector. Finally, the very structural design affects electrical performance through the scattering of energy from surface-panel irregularities and interpanel gaps, from subreflector and/or feed-support spars, and from the correlation of this scattering arising from the structural design and alignment procedures.

Since the birth of satellite communications, satellite-borne antennas have steadily increased in gain and complexity. 44a Higher gain derives from a need to increase EIRP in a power-limited environment. 44b Complexity may derive from several sources such as beam shaping or reconfigurability. 44c Both lead to larger reflectors. Currently, reflectors electrically as large as about 200\(\lambda\) (ACTS) and mechanically as large as 6 m (M-Sat) are being prepared for mid-90s launch. Significantly larger antennas are planned for future applications. Electrically large reflectors are usually fed by simpler antennas such as horns or arrays of horns or by folded-optics systems involving subreflectors and feeds. In many instances, the antennas are designed to produce two coaxial beams with orthogonal polarizations over near-octave bandwidths. The feed systems may then terminate in complex microwave circuits involving polarizers and orthomode transducers to separate or combine orthogonally polarized beams as well as in microwave multiplexers to separate or combine different frequencies.

Electrically large reflector antennas have their principal applications in radar (Chaps. 32 and 34), where their high gain and narrow beamwidths enhance radar range and angular resolution; in radio astronomy (Chap. 41) and other deep-space applications, where the same parameters enhance sensitivity and resolution of stellar radio sources; and in microwave communications (Chaps. 30 and 36), where high gain, low noise, and sidelobe control enhance effective radiated power relative to isotropic (EIRP), receive sensitivity, and isolation from interference. For reflector antennas of diameter greater than 60 wavelengths, gains range from 40 dBi to about 70 dBi, half-power beamwidths (HPBWs) from about 1.5° to about 0.05°, and average wide-angle sidelobe levels down to -20 dBi (almost 90 dB below the peak of the main beam); dual-polarized radiation-pattern orthogonality provides isolations greater than 33 dB over the HPBWs. Of course, these properties depend upon the feed system as well as the reflectors.

Pencil-Beam Reflector Antennas

Front-Fed Paraboloidal-Reflector Systems The paraboloidal-reflector antenna and its design are described in Sec. 17-1. Since the design is geometry-controlled and since the larger electrical apertures considered here make geometrical-optics considerations even more valid, the choices of f/D ratio, edge taper, etc., remain the same. However, the simple front-fed reflector has disadvantages due to the blocking of the

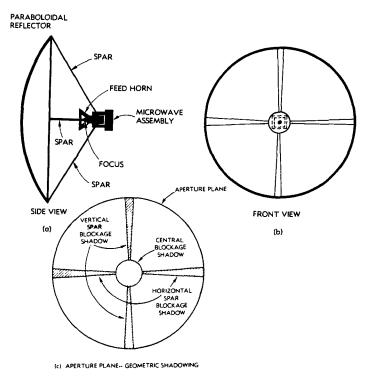


FIG. 17-32 Front-fed paraboloidal-reflector antenna.

aperture by the feed system and by the feed supports. 45,46 Figure 17-32 shows two views of a front-fed paraboloidal-reflector antenna with feed supports extending from the reflector edge. It is seen that the feed supports intercept radiation reflected from the paraboloid. (Supports which are not on the edge intercept energy from the feed before it reaches the reflector.) In a geometrical-optics sense, the feed supports cast a shadow upon the aperture plane, shown in the third view. This shadow, called aperture blockage, reduces gain and affects near-in sidelobes, raising some and lowering others. In addition, the blocked radiation is scattered by the feed supports and can significantly increase wide-angle sidelobes. In general, the front-fed design with a simple feed horn has less blockage than the folded-optics designs. Additionally, the feed subtends a wider angle at the main reflector than a feed illuminating a subreflector does, and therefore the feed is a simpler, lower-gain design. However, if the feed system is complex and the microwave package abutting it is large and heavy [containing polarizers, orthomode transducers (OMTs), low-noise amplifiers (LNAs), etc.], the blocking advantage is negated somewhat. Further, the focal point is an awkward location for such electronic gear, both structurally, because the weight is not desirable at the end of a large-moment arm, and from the point of view of equipment servicing. Finally, in electrically large reflectors, in which reflector size must be minimized, the folded-optics system can be made more efficient. The front-fed reflector has an efficiency of 55 to 60 percent. Folded-optics designs can employ shaped subreflectors to increase efficiency.

Folded Optics Pencil-beam reflectors may be illuminated by feed systems in which the path of energy from the feed (which terminates the guided-wave-waveguide assembly) is reflected by one or more subreflectors. Figure 17-33 portrays the geometry of the Cassegrain reflector system, whence it is seen that the incoming-ray trajectories are folded back in the direction of the vertex of the paraboloid P by reflection from the hyperboloidal subreflector P. The focusing properties of the system derive from the colocation of one focus of the hyperboloid P with that of the paraboloid at P at incoming plane wave from the direction of the paraboloid axis is reflected from the paraboloid and from the hyperboloid and focuses at P, the other focus of the hyperboloid P. A feed with its phase center at P will then receive the incident energy.

Figure 17-34 portrays the geometry of the gregorian reflector system. Here the subreflector is an ellipsoid E with its near focus colocated at F_1 with the focus of the

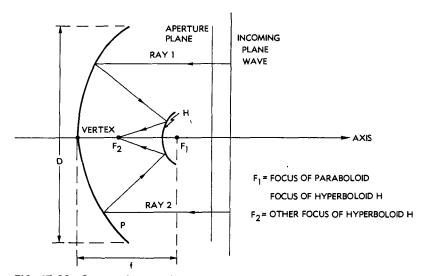
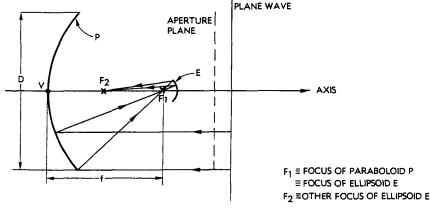


FIG. 17-33 Cassegrain geometry.



INCOMING

FIG. 17-34 Gregorian geometry.

paraboloid, the ellipsoid lying on the side away from the paraboloid vertex. The phase center of the feed should then lie at F_2 , the other focus of the ellipsoid. Another configuration is shown in Fig. 17-35. Here the subreflector is paraboloidal, with its focus colocated at F with the focus of the paraboloidal main reflector. The result of the reflection of the rays representing the incoming plane wave is a collimated cylinder of rays parallel to the axis. This creates the possibility of another, smaller aperture plane parallel to XX'. A feed system associated with this aperture would have a plane wavefront, or the parallel rays could be associated with an appropriate beam-waveguide system.

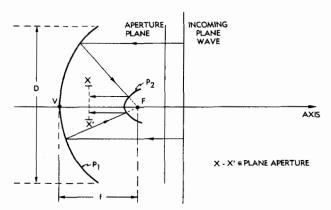


FIG. 17-35 Planar-feed field geometry.

An immediate advantage of all three folded systems is that the feed system is now located nearer the vertex of the main reflector and, in fact, can usually be reached from access provisions at the vertex. More subtly, introduction of the additional reflection at the subreflector provides an additional degree of design freedom. Aperture distribution can be controlled to increase efficiency and decrease blockage by shaping the subreflector and the main reflector so that the surfaces deviate from the hyperboloid, ellipsoid, and paraboloid.

The Cassegrain system is more compact than the gregorian system for the same focal length. There have been claims that gregorian systems provide improved wide-angle sidelobes in apertures of the order of 200 wavelengths. However, because of blockage of the feed system, subreflector, and supports, the sidelobes of these folded antennas are not especially low. By careful design and construction, the sidelobe envelope can be made to conform to international and Federal Communications Commission (FCC) requirements. For example, INTELSAT old Standard A antennas, which have gain in excess of 57 dBi (generally 60 dBi), require sidelobe envelopes to be less than $(29-25 \log \theta)$ dBi, from 1° to 48°, and less than -10 dBi beyond 48°. (θ is the pattern angle measured in a band of \pm 1° about the geostationary arc.)

One of the design principles used in minimizing subreflector and feed blockage is to make them equal, as shown in Fig. 17-36. The subreflector blocks incoming rays, and the feed blocks rays that would hit the main reflector and be reflected to the subreflector. For the case shown, the shadows of the feed and subreflector intersect on P, the paraboloid main reflector, presenting the ideal case.

It has been found that keeping the subreflector diameter small (10 percent of the diameter of the main reflector) will keep the central-blockage sidelobes from exceed-

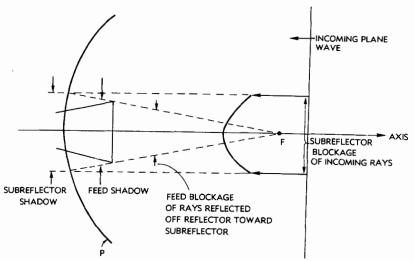


FIG. 17-36 Blockage by feed and subreflector.

ing the specifications given above. If this is not done, the sidelobes are high in the 1° to 10° region. The subreflector support spars tend to create sidelobe problems in a region of 5° to 20° in the plane perpendicular to the spars. It has been found useful to use a spar quadruped with all spars at 45° to the plane of concern. However, the best way to reduce sidelobes is to eliminate the blockage by the use of offset reflectors.

Sidelobes in Electrically Large Antennas Sidelobes in a folded-optics system arise from a number of sources. These include (1) radiation-pattern sidelobes from the aperture illumination, (2) spillover and edge diffraction from the subreflector illuminated by the feed system, (3) spillover and edge diffraction from the main reflector illuminated from the subreflector, (4) central blockage (subreflector and feed system), (5) spar (subreflector support) blockage and scattering, (6) deviation of reflector surfaces from the desired contours, and (7) effects of gaps between panels.

Control of aperture illumination amplitude and phase to reduce sidelobes dates back to the earliest days of antenna theory and practice, and many references can be found in any basic antenna text. More recent techniques are discussed in two review articles. 462,465 One approach that has become quite important is the use of offset geometry, yielding an unblocked aperture which eliminates sidelobes arising from central blockage, spar blockage, and spar scattering. This will be discussed in greater detail below.

Departure of the aperture illumination in amplitude and phase from that desired can arise from feed-aperture phase errors⁴⁵ and defocusing. ⁴⁶ These will cause the radiation (diffraction) pattern to depart from the design values but are correctible by careful feed design and positioning. Spillover and edge-diffraction effects can be avoided by illumination of the subreflector with a more deeply tapered feed pattern to about 20 dB down at the edge. For the shaped subreflector, it is possible to obtain sharp illumination taper at the main-reflector edge. ^{47,48} Spillover and edge diffraction of feed radiation will give increased sidelobes in the 10° to 20° region of the pencilbeam axis.

Minimizing the central blocking and optimizing the illumination are not compatible, since the first requires smaller feed systems and the second requires larger

feed systems. Equalizing the subreflector and horn blockage as discussed in the preceding subsection is the best approach. Then if the subreflector diameter can be kept to less than 10 percent of the main-reflector diameter, shaping is possible and the blockage lobes will meet the sidelobe criterion of the preceding subsection. Central blockage casts a wide beam inversely proportional to the diameter of the central blockage and thus typically 10 times the beamwidth and 20 dB down from the main beam. It is out of phase with the main beam and thus subtracts a fraction of 1 dB from the main beam, adds 2 to 3 dB to the first sidelobe, subtracts from the second sidelobe, etc. Spar blockage and scattering 45,49 are not circularly symmetrical and depend upon spar shape and spar-reflector-subreflector geometry. If the spars are not mounted at the dish edges, shadows are cast on the main reflector to reduce efficiency and blockage of the reflected energy is still present. Spar scattering effects are strongest in the forward hemisphere at an angle of 180° $-\xi$, where ξ is the angle between the spar axis and the aperture plane. 45 The sidelobes are strongest in the forward direction in the plane containing the spar and the beam axis. This typically occurs in the region at 5° to 15° off the main-beam axis. Spar design can minimize but not eliminate this effect. Streamlining the spar cross section is useful for the polarization perpendicular to the spar. Orienting the spars in a quadruped at 45° to the horizontal is effective for earth stations in keeping spar-induced sidelobes out of the region of the geostationary arc. Figure 17-37 shows the effects of central blockage, spar blockage, and forward (subreflector) spillover on a radiation pattern.

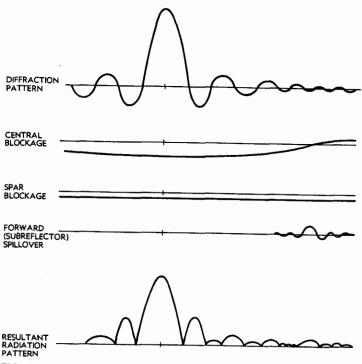


FIG. 17-37 Blockage effects on sidelobe structure.

The remaining two sources of sidelobe energy derive from the manner in which electrically large antennas are fabricated, assembled, and installed. Most electrically large reflectors are constructed of segments (panels) assembled onto a backup structure or with the backup structure as an integral part of the panels. The subreflectors are generally single units.

The rms errors associated with fabricating a single panel or a subreflector can be controlled with care to 0.1 mm (4 mils) for a reflector or panel up to 3 m across; however, fabrication techniques commonly used permit rms errors of 0.25 to 1.27 mm (10 to 15 mils) for panels of this size. Assembly and installation errors are each of the same order, provided careful checkout procedures are used. A rule of thumb for communication and radar reflectors in the 8- to 30-m class is that the ratio of rms error to reflector diameter is 2 to 5 times 10⁻⁵. Some electrically large antennas have been built to better tolerances for radio astronomy, but they usually require special protection from the environment. The pattern effects of the errors depend upon their statistical nature. 45,50,51,52,53

It has been shown⁵⁴ that when error correlation intervals are small, the results obtained by Ruze^{50,51} for axial gain apply (see Fig. 17-38 and Chap. 2). However, because panel-fabrication error contributions tend to be of the same order or smaller than assembly and installation error contributions, the large correlation errors of the assembly can dominate. Therefore, one cannot reasonably assume small correlation intervals in most large antennas. Bao⁵⁴ has shown that the effect of these large correlation intervals is to reduce the gain loss and that the sidelobes are significantly lower than predicted under Ruze's assumptions regarding correlation. In a similar fashion, the distortions due to wind and gravity have long correlation intervals and

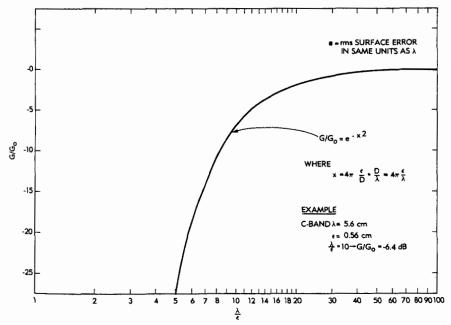
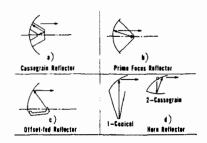
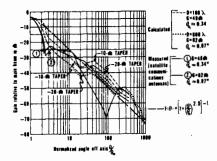


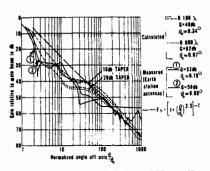
FIG. 17-38 Normalized loss due to finite surface error.



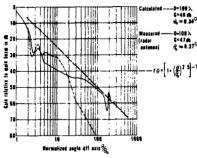
BASIC CONFIGURATIONS OF ANTENNAS



CASSEGRAIN-FED REFLECTOR RADIATION OIAGRAMS



PRIME-FOCUS-FED PARABOLIC REFLECTOR



OFFSET-FED PARABOLIC REFLECTOR

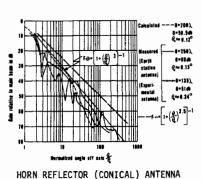
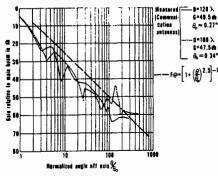


FIG. 17-39 Practical sidelobe-level envelope.



HORN REFLECTOR (CASSEGRAIN) ANTENNA

hence less effect than predicted by the small-correlation-interval theory. The large correlation intervals increase the sidelobes in the region near the main beam, while the small correlation intervals (random errors) contribute significantly to wide-angle sidelobes. A recent review paper by Corkish^{54a} on the effects of reflector surface distortions on sidelobe levels covers the various approaches to this subject in some detail and provides a wealth of references.

An excellent treatment on very large earth station antenna sidelobes was given by Korvin and Kreutel, 46 who presented results of both theoretical and measured studies for apertures ranging from 100 to 600 wavelengths. Figure 17-39 presents some of these results.

As real-time control techniques and data processing have become more capable in the past decade, the possibility of correcting for distortions has become a reality. Real-time adaptive optics for optical telescopes was demonstrated in 1989, mainly to remove distortion due to the atmosphere. Adaptive phased-array feeds can be used in a similar manner to compensate for deterioration of scanning. See Schell's multiplate antenna, See while invented for other purposes, embodies all the necessary characteristics for adaptive removal of both atmospheric and surface distortions. The advent of modern control electronics and drive mechanisms should make the multiplate antenna a candidate approach for large-aperture reflectors.

The increased interest in large, spacecraft-borne antennas and in sidelobe control has given rise to increased interest in and use of offset configurations, especially for multibeam and scanning applications. ^{54e,54f} The conventional pencil-beam Cassegrain and gregorian configurations have been studied to provide design techniques for the offset cases. ^{54e,54i} A technique for increasing antenna efficiency by extending the subreflector in an offset Cassegrain antenna has been analyzed. ⁵⁴ⁱ When offset Cassegrain or gregorian reflector systems are used in beam-scanning or multibeam applications, feeds must be moved or located in the positions that provide optimal beam performance. This turns out to be a hyperboloid for the offset Cassegrain ^{54k,54i} and an ellipsoid for the offset gregorian. ^{54m}

High-Efficiency Dual-Reflector Systems

Electrically large pencil-beam antennas are costly. Cost is almost a linear function of aperture area (reflector surface). The higher the efficiency, the smaller the aperture required to collect incoming waves or to provide gain for a transmitted wave. Antenna efficiency is the product of a number of factors, each of which represents the degree with which the energy is protected against diversion from the desired direction or polarization by a particular mechanism. The factors include effects of (1) aperture illumination (η_i) , (2) spillover around the main reflector and subreflector (η_{sl}, η_{s2}) , (3) blockage (η_b) , (4) reflector-surface deviations (η_r) , (5) polarization purity (η_p) , and (6) losses in waveguide and feed (η_0) . These efficiency factors are defined in Table 17-1.

TABLE 17-1

```
\eta_i = \frac{1}{A} | \int F dA |^2 / \int |F|^2 dA \ (F \text{ is illumination over aperture } A.)
```

 η_{s1} = power on main reflector/(power from subreflector - scattered power)

 η_{s2} = power on subreflector/power from feed system

 η_b = power blocked/total power from main reflector

 $\eta_r = \exp\left[-\left(4\pi\epsilon/\lambda\right)^2\right]$ ($\epsilon = \text{rms error}$. This is worst-case approximation.)

 η_0 = power radiated by feed/power input to feed system

 η_p = aperture power of desired polarization/total aperture power

Spillover, blockage, and surface tolerance effects have been discussed earlier in terms of sidelobe control. Improvement in efficiency and reduction of sidelobe effects go hand in hand for these factors. Polarization purity is controlled by feed-system polarization properties, by curvature of the reflector, by symmetry, by scattering properties of the blockage elements, and, for circular polarization, by internal reflections in the waveguide and feed system.

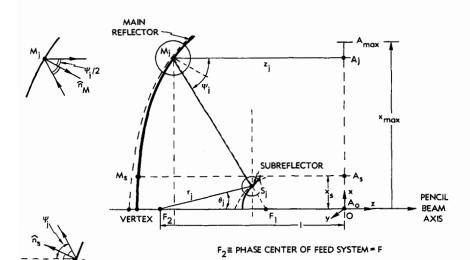
Control of aperture illumination ^{55,56,57} is a major factor in improving efficiency. Techniques for controlling illumination can also minimize the effects of central blockage, as will be seen. If maximum gain is desired, the object is to shape the subreflector and the main reflector so that the aperture illumination is as nearly uniform as possible, with minimum spillover and with minimum energy blocked.

Three basic conditions are used to shape the two reflectors: (1) Path length from phase center of feed to aperture plane is constant for all paths. For the *j*th ray, as shown in Fig. 17-40, $(\overline{F_2S_j} + \overline{S_jM_j} + \overline{M_jA_j}) = \text{path length from feed point to aperture plane} = r_j + z_j + (r_j \cos \theta_j - l + z_j)/\cos \theta_j = \text{constant.}$ (2) Aperture illumination is constant. It can be shown 56.57 that this requirement leads to

$$x_j^2/x_{\text{max}}^2 = \left(\int_0^{\theta_j} E_f^2 \sin\theta d\theta\right) / \left(\int_0^{\theta_{\text{max}}} E_f^2 \sin\theta d\theta\right)$$

where $E_f = E_f(\theta)$ is the circularly symmetric pattern of the feed horn. (3) Snell's law must apply. This leads to the expressions

$$\frac{1}{r}\frac{dr}{d\theta} = \tan\left(\frac{\theta + \psi}{2}\right) \qquad -\frac{dz}{dx} = \tan\frac{\psi}{2}$$



Ms, As = PROJECTION OF OUTER EDGE OF SUBREFLECTOR ON MAIN REFLECTOR AND APERTURE PLANE

(Amox-Ao) = APERTURE RADIUS=D/2

FIG. 17-40 Shaping of main reflector and subreflectors.

These three conditions (four equations) can be solved on a computer to yield the two surfaces desired. But the general nature of the solution can be deduced from the physical problem. It is desirable to make the aperture illumination more uniform when it is too high in the center. If the slope of the subreflector near the center were altered to reflect central rays from the feed away from the center of the main reflector, this would have the desired effect. The dotted curve in front of the subreflector represents such a distortion. The main reflector must now be reshaped to maintain the focused beam. This results in the dotted curve behind the main reflector.

If this process is exaggerated near the middle of the subreflector, a hole would result in the illumination of the main reflector. The energy here is normally blocked by the subreflector so that there is no basic change in the radiation pattern near the main beam. There will be a reduction in the energy scattered by the subreflector and, therefore, lower scattered sidelobes at wider angles. It has been indicated 57a that one can optimize the shaping of dual-reflector systems for $G/T_{antenna}$, rather than G alone. Since $T_{antenna}$ has a major component arising from sidelobes intercepting the earth, this entails sidelobe control as well as gain optimization.

At the edge of the subreflector the surface can be shaped to direct energy inward and so give a shorter and deeper illumination taper at the edge of the main reflector to reduce spillover. The shaping of the subreflector edges can compensate for deeper tapering of the energy incident upon this surface. Therefore a system with less spillover past the subreflector and with underillumination of the main reflector can use the shaping of the subreflector edges to compensate for the underillumination. Thus, it is seen that reflector and subreflector shaping not only can improve the aperture illumination but can also reduce spillover past both reflectors.

It has been found that the simple geometrical-optics analysis of shaping is not sufficiently accurate. ⁵⁸ Improved performance can be obtained by considering diffraction effects at the subreflector. ⁴⁸ The system improvement has been limited in bandwidth, and a third approach ⁴⁸ modifies geometrical-optics design to give good performance over a wider bandwidth.

With the growing popularity of offset configurations, shaping theory has been applied to improve the efficiency of offset-fed dual reflectors. The geometric-optics approach developed by Galindo⁵⁵ has been particularized for the Cassegrain and gregorian configurations^{58a-58c} and extended to show that the geometric-optics-based design produces very similar results when geometric-optics-based predictions are compared with those of physical optics and the geometric theory of diffraction in the aperture.^{58d}

Wide-Angle, Multiple-Beam Reflector Antennas

Many applications in radar, astronomy, and communications require the use of more than one beam from a single reflector. The problem first arose in radar systems, and the solutions considered were based upon counterparts from optics. ^{59,60,61,62,63,64,65,66,67} Microwave-optics problems were similar for systems with multiple beams or with single beams and multiple-beam positions. The solutions employed simple front-fed paraboloids, folded-reflector systems, and spherical and toroidal reflectors.

Wide-Angle Characteristics of Large Paraboloidal Reflectors When the feed of a paraboloidal reflector is displaced from the focal point and off the axis of the system, the main beam of the radiation pattern moves in the opposite direction. Crude ray tracing, as shown in Fig. 17-41, demonstrates that rays from F_1 , the transversely

and

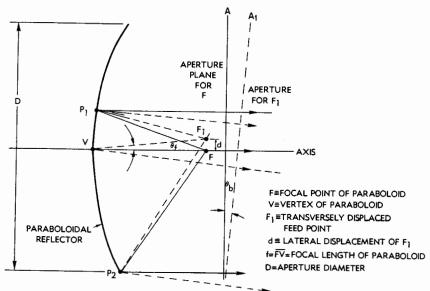


FIG. 17-41 Paraboloid with transverse displacement of feed.

displaced feed above the axis, reflect in a downward direction. More precise ray tracing to the aperture plane A would show that for small feed displacements the ray paths are almost constant to a new aperture A_1 tilted with respect to A. If the feed at F_1 is displaced through an angle θ_f , then the main beam is tilted at an angle θ_b in the opposite direction. For practical values of antenna parameters, θ_b is less than θ_f . The ratio of these angles is called the beam-deviation factor (BDF). For a shallow reflector and for small displacements, Lo⁶⁸ has shown that

$$\frac{\sin \theta_b}{\tan \theta_f} \approx \left[\frac{1 + k(D/4f)^2}{1 + (D/4f)^2} \right] \equiv (BDF)_0$$

$$BDF \approx (BDF)_0 \left[1 + \frac{1}{3} \left(\frac{d}{f} \right)^2 \left[\frac{1}{2} (BDF)_0^2 + 1 \right] \right]$$

Here k can vary from 0.3 to 0.7 as a function of the feed pattern and edge taper. Increased taper emphasizes the flatter central portion of the reflector to imply a longer

beam-deviation factor increasing rapidly to 0.9 as the f/D ratio goes from 0.25 to 0.5. As the feed horn is moved off axis, the beam is scanned with a decrease in gain of the beam and with an increase in sidelobes. These changes are depicted in Fig. 17-42. There is a reduction in gain, ΔG . The first sidelobe nearest the system axis (coma lobe) is increased, and the opposite sidelobe is decreased. Figure 18-16 in Chap. 18 shows this process for a paraboloidal reflector of f/D ratio of 0.5- and 20-dB edge illumination.

effective f/D ratio. The f/D ratio is the most important factor for BDF, with the

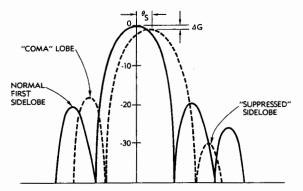


FIG. 17-42 Radiation patterns for focused and laterally defocused feeds.

It has been shown⁶⁹ that simple lateral displacement creates not only coma and astigmatism^{70,71} but also curvature of the field and higher-order aberrations. These manifest themselves by filling in the nulls in the pattern and by a broadening of the main beam.

Ruze⁶⁹ provides computed graphs of HPBW, gain loss, beam-deviation factor, and level of coma lobes for a range of f/D ratios and aperture illuminations. Loss of gain ΔG can be predicted by the equation

$$26.75 \left[\Delta G(\mathrm{dB})\right]^2 - 4.75 \left[\Delta G(\mathrm{dB})\right]^4 \approx \theta_s \left(\frac{D}{f}\right)^2 / \left[1 + 0.02 \left(\frac{D}{f}\right)^2\right]$$

Physical-optics considerations are used by Rusch and Ludwig⁷² to determine maximum scan-gain contours. These tend to be flat and close to the transverse plane through the focus. They initially curve toward the vertex and for wider-scan angle bend away from the vertex.

An equally important factor is the demonstration⁷² that maximum gain depends upon the feed axis remaining parallel to the reflector axis rather than pointing the feed to the vertex. Gain loss and gain optimization are not a closed subject.⁷³ Data taken from six authors in the time period 1947–1973 are compared and shown to have significant differences which are attributed to differences in illumination.

As noted in the introduction to Sec. 17-2, recent increases in satellite-borne antenna requirements can be satisfied by large-aperture antennas. This evolution 44a started with simple dipole-like antennas in the mid-60s, through earth-coverage horns to broad spot beams and now to 1.6° spot beams at Ku band and reconfigurable multibeam C-band antennas employing 3.2-m-diameter reflectors for transmit, with a triple stack of switchable beam-forming networks controlling the excitation of 147 horns dually polarized to produce 6 beams, on INTELSAT VI.44c Spot-beam beamwidths down to 0.3° at K/Ka bands are used in hopping beams on the ACTS, 44b scheduled for launch in 1993. Antenna dimensions in excess of 6 m are being employed at L band on the M-Sat satellites to be launched in 1994 to provide mobile satellite services.

Wide-Angle Scanning of Electrically Large Folded-Feed Reflectors

Cassegrain and gregorian antennas derive from the front-fed paraboloid through considerations of geometrical optics. Therefore, scanning of the reflectors can be related

to scanning of front-fed reflectors. The concept of the equivalent paraboloid ^{65,66} provides the desired link. If, in a Cassegrain antenna system (Fig. 17-43) with F the focal point for the actual feed, the subreflector subtends an angle $2\phi_f$ and the paraboloid subtends an angle $2\phi_r$, then one can define a magnification m in terms of focal lengths:

$$m = \frac{f'}{f} = \frac{\tan{(\phi_r/2)}}{\tan{(\phi'_r/2)}} = \frac{e+1}{e-1}$$

where e is the eccentricity of the hyperboloid subreflector and f' is the focal length of the equivalent paraboloid. It subtends the angle $2\phi_f'$ at F' and intercepts the same marginal rays as the main reflector (has the same axis and diameter D). Since e > 1, f' > f and F'/D > f/D. As noted earlier, the beam deviation factor, coma aberration, and gain loss are strong functions of f/D, the larger f/D being preferred. Therefore, the longer effective f/D ratio of the Cassegrain reflector offers potential for enhanced scanning performance. For the gregorian system, f'/f = -(e+1)(e-1), so that one may choose f' > f. This system also therefore offers potential for scanning.

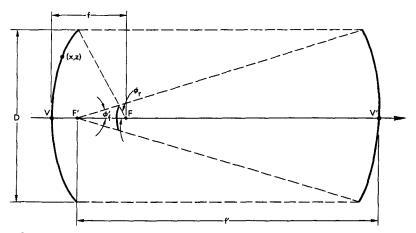


FIG. 17-43 Geometry of the equivalent paraboloid.

The design of scanning systems (Chap. 18) sometimes employs the Abbe sine condition to minimize aberrations for small scan angles; this is for the ray incident at the general point (x, z) in Fig. 17-43, $x/\sin \phi' = \text{constant}$. Neither the front-fed paraboloid, nor the Cassegrain system, nor the gregorian system satisfies the Abbe sine condition. However, the latter two systems show better results for this criterion than the simple paraboloid. The best dual-reflector system for scanning is the Schwarzschild.⁶⁷ Studies^{66,74,75} indicate that for electrically large antennas the Schwarzschild system is promising. Other dual-reflector systems with promise include the two-point correction, ^{73,76,77} the spheroboloidal-gregorian dual-reflector system, ^{73,77} the offset bifocal dual-reflector system ^{77a} easily providing $\pm 9^{\circ}$ (earth coverage) scan from space and for up to 60° scan, and the ellipse-derived-shaped single reflector. ^{77b}

Spherical and Toroidal Wide-Angle, Multiple-Beam Reflectors The spherical reflector offers symmetry which can be used for scanning systems. The design problem lies in designing a feed system which will effectively illuminate the aperture with the proper phase characteristics. Ashmead and Pippard⁶⁰ and Li²⁰ have provided useful information on point-source feeds. The data depend upon the sphere radius R, the aperture in wavelengths D/λ , and the allowable maximum phase error Δ/λ .

$$(D/R)_{\text{max}}^4 = k(\Delta/\lambda)/(R/\lambda)$$

Ashmead and Pippard found a value of k=250, and Li found a value of 235.2. These data show that point-source feeds require a small D/R value which is not practical. However, when efficiency is not the most significant parameter, as in receive-only earth stations, the spherical reflector has been used.

Improvement of the spherical-reflector scanning system requires correction of the phase error of Fig. 17-10. Analysis of the focal-region field (receiving antenna) by geometrical ^{78,79} and physical optics ⁸⁰ shows a calculable phase progression along the line between the focal point and the reflector. Each small region along this axis is illuminated by concentric zones on the spherical reflector (Fig. 17-44). Line-source feeds with an element for each zone ^{81,82} have been effectively used to correct the spherical aberration represented by the phase of each zone in the 1000-ft (305-m) reflector at Arecibo, Puerto Rico. These feeds are bandwidth-limited and mechanically limited.

The alternative to correction along a line between the feed and the reflector is to correct in the transverse focal region. 83,84,85,86 Efforts at transverse correction 87,88,89 resulted in one promising design 87 shown in Fig. 17-45. The shape of the gregorian

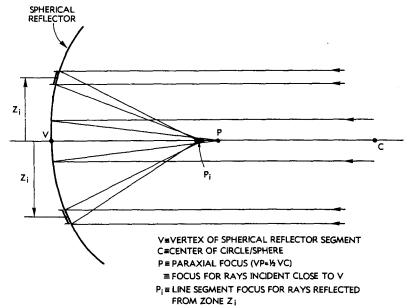


FIG. 17-44 Axial line focusing for a spherical reflector.

subreflector, G(u, v), using the notation of Holt and Bouche, is given by the coordinates u and v:

$$u = c - [(c^2 - 2c + 2p)(2c^2 - 1)]/[4(pc^2 - c) + 2]$$

$$v = \pm s(2cu - 1)/(2c^2 - 1)$$

where $c = \cos \theta$, $s = \sin \theta$.

A further advance in aberration correction has been obtained using a dual-reflector quasi-gregorian feed system, 89a i.e., secondary and tertiary subreflectors. The system has been analyzed and verified with scale-model tests.

The toroidal-reflector family also provides scan by symmetry, but the symmetry is limited to a single plane. The generalized geometry for toroidal reflectors is shown in Fig. 17-46. M is a conic section with axis along the z coordinate, and z' is the axis of rotation lying in the xz plane at an angle of α to the z axis. When M is rotated about z', the toroidal surface is swept out. If M is a parabola of focal length f ($f \leq \overline{OV}/2$) and R is the radius of the circular arc ($R = \overline{OV}$) and α is 90°, the torus reflector of Kelleher and Hibbs⁹⁰ is obtained. Replacing the parabola with an appropriate ellipse gives the Peeler-Archer torus. ⁹¹ For $\alpha \neq 90^\circ$, the axis of the conic section moves on the surface of a cone. ⁹² For $\alpha = 90^\circ$, the cone degenerates into a plane. This case will be termed the rectangular torus. Such a reflector has been used for very large radar reflectors with an organ-pipe-scanner feed system (Chap. 18). It also has been proposed for satellite communications earth station and terrestrial multibeam wide-angle applications, ^{92a} with numerical computations verified by measurements for a 15° scan angle scale-model design.

For earth stations in temperate latitudes which are scanning the geostationary arc, $\alpha = 95.5^{\circ}$ can be shown to give an optimum torus design. Studies of the aperture fields, far-field patterns, and efficiency led to the choice of a parabolic section with a focal length to radius f/R of 0.487 and feed location H, given by x,y,z coordinates as

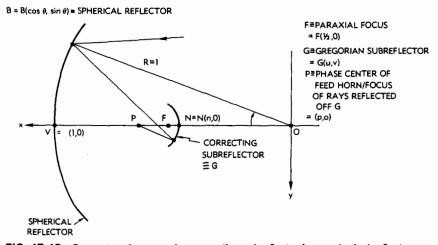


FIG. 17-45 Geometry of a gregorian correcting subreflector for a spherical reflector.

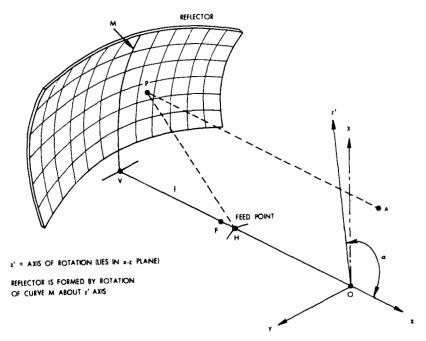


FIG. 17-46 Torus-antenna geometry.

0.001 R, 0.0, -0.5 R. Some of these considerations⁹³ are shown in Figs. 17-47 and 17-48. On the basis of these design parameters, a scale model and a full-scale antenna were fabricated and shown to give excellent performance⁹⁴ as part of the unattended earth terminal (UET). Test results verified the design process using the finite-element approach embodied in the GAP (General Antenna Program) computer program.⁹⁵ Both the scale model and the final torus antenna used a corrugated scalar horn^{96,97,98} as a feed because this horn has a well-defined, frequency-invariant phase center near the throat. The horn has very symmetric patterns with low sidelobes that appear to match well the focal-region fields of large reflector antennas.⁹⁹ The implementation of the corrugated horn used in the UET is shown in Fig. 17-49. The 30- by 55-ft (9.1-m by 16.8-m) UET torus antenna operating in the 6- and 4-GHz fixed-satellite bands is shown in Fig. 17-50.

Finally, it should be noted that the aberration present in the conical-torus antenna system can be removed by an aberration-correcting subreflector, 100-102 designed by using the GAP95 to define the surface. The geometry for the torus with subreflector is shown in Fig. 17-51, the scale-model subreflector is shown in Fig. 17-52, and the performance is given in Fig. 17-53. The subreflector has a hyperbola arc in the vertical plane of symmetry (as in the Cassegrain) and a somewhat elliptical arc in the other plane (gregorian). It is called *cassegorian*. Gain performance follows frequency squared beyond 60 dBi, whereas comparable uncorrected torus performance shows aberration losses above 53 dBi. Measured efficiency for an assumed circularly

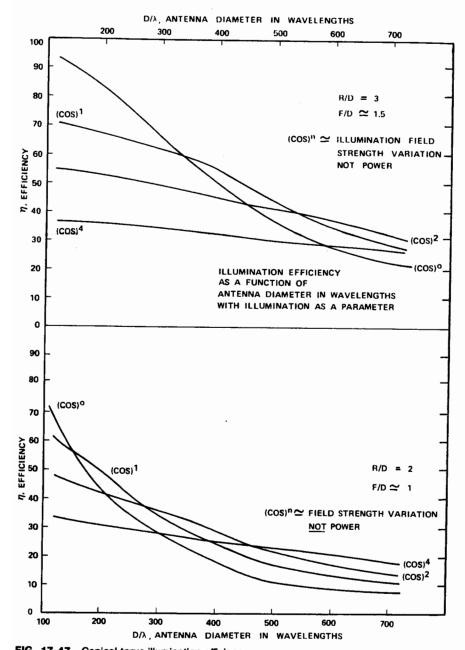
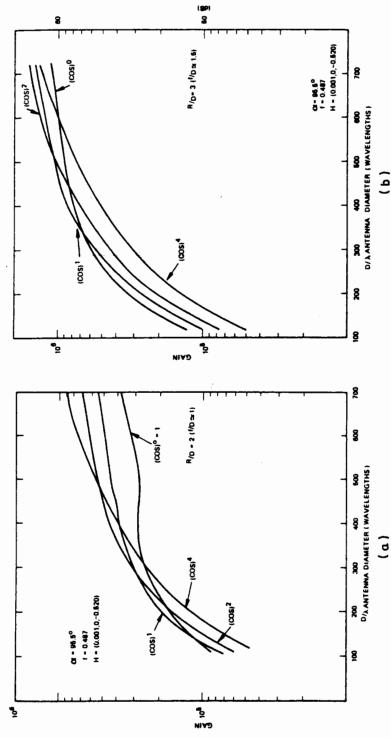


FIG. 17-47 Conical-torus illumination efficiency.



L FIG. 17-48 Gain for a torus antenna. (a) R/D = 2, f/D = 1. (b) R/D = 3, f/D = 1.5.



FIG. 17-49 Corrugated feed horn.

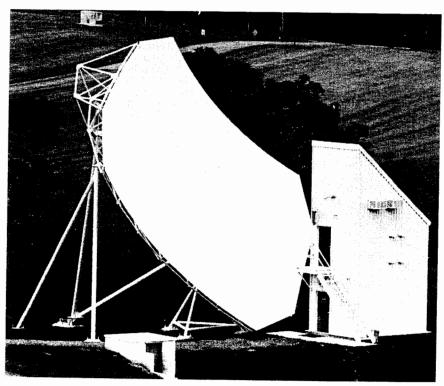


FIG. 17-50 Multibeam torus antenna (MBTA).

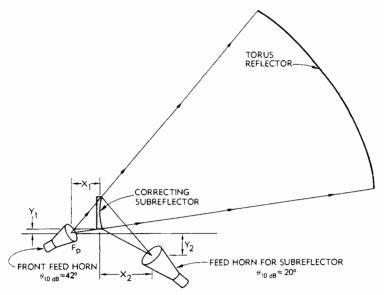


FIG. 17-51 Front-fed and subreflector configurations.

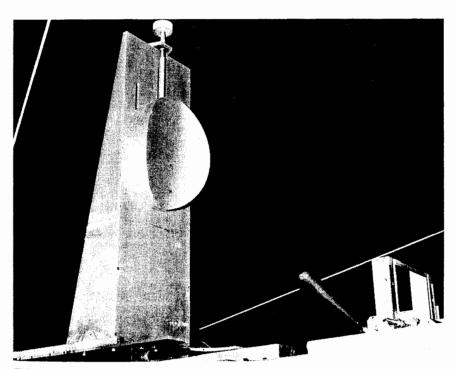


FIG. 17-52 Aberration-correcting subreflector for a torus reflector.

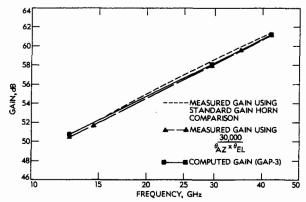


FIG. 17-53 Comparison of measured and calculated gain versus frequency.

illuminated aperture exceeded 70 percent at 12.4 GHz and approached 74 percent at 42 GHz.

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Electromechanical Scanning Antennas

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18-4 Parallel-Plate Scanners 18-11

Schmidt Lens 18-13

Surface-of-Revolution Scanners 18-11 Double-Layer Pillbox 18-12 Concentric-Lens Scanner 18-13

18-1 Basic Scanning Principles 18-2 Schwarzschild System 18-14 General Types of Scanners 18-2 Zeiss-Cardioid System 18-14 18-2 Luneburg-Type Lenses 18-2 18-5 Scanning with Reflectors Spherical Luneburg Lens 18-2 Single-Refractive-Index Lens 18-3 Paraboloidal Reflector 18-15 Reflector Tilt 18-16 Double-Refractive-Index Lens Spherical Reflector 18-17 Two-Dimensional Luneburg Lens 18-4 Corrected Spherical Reflector 18-18 Torus Reflector 18-18 Virtual-Source Luneburg Lens 18-5 Parabolic-Torus Reflector 18-19 Small-Feed-Circle Luneburg 18-6 Feed-Motion Systems 18-20 Lens 18-6 Lewis Scanner 18-21 Parallel-Plate Luneburg Lens 18-6 Robinson Scanner 18-21 Surface-Wave Luneburg Lens Virtual-Source Scanner 18-21 Geodesic Analog of Luneburg Tilting-Plane Scanner 18-21 Lens 18-6 18-3 Lens Scanners 18-7 Prism Scanner 18-22 Dielectric Lens 18-7 Foster Scanner 18-22 Wide-Angle Dielectric Lenses 18-8 NRL Organ-Pipe Scanner 18-23 Metal-Plate Lenses 18-9 Sector Organ Pipe 18-24 Metal-Plate Lenses with Two-Point RCA Organ Pipe 18-24 Tape Scanner 18-24 Correction 18-10

Helical-Slot Scanner 18-25

Ring Switch 18-26

18-1 BASIC SCANNING PRINCIPLES

The material covered in this chapter is limited to lens or reflector systems capable of producing a scanning beam without a motion of the lens or reflector or a motion of the entire antenna assembly. It therefore excludes the simple scanning obtained from mount rotation or the conical scanning from feed rotation. These scanner types have been included in earlier literature.¹

General Types of Scanners

The simplest type of scanner consists of a focusing objective and a point-source feed. The focusing objective can be the conventional paraboloid or the lens with hyperboloid-plane surfaces. The scanning action is then as depicted in Fig. 18-1. When the

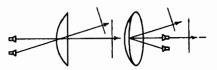


FIG. 18-1 Scanning with focusing objectives.

point source is at the focal point of either objective, a plane wave which propagates along the system axis is produced. When the point source is moved off axis, the wave propagates in a direction at some angle to the axis. The motion of the source moves the antenna beam.

Another entirely different method of scanning keeps both the source and the

objective fixed and adjusts the phase in the path between the source and the objective. This type of phase adjustment was first done in the Foster scanner (Sec. 18-6). At the present time, it is best done by phased-array techniques (Chap. 20). A variation of the phasing between the objective and the feed source is obtained when a large number of fixed feeds are used and phase correction is achieved in the feed complex. This approach can be accomplished with the Butler matrix or with bit phase shifters. Both techniques are *phased arrays*.

The material in this chapter is limited to wide-angle focusing objectives and the feed-motion systems used with such objectives. The best-known focusing device is the Luneburg lens, which is treated first. Among other devices are other lenses, pillbox scanners, and reflector scanners. The chapter concludes with a discussion of feed mechanisms for rapid motion of the source.

18-2 LUNEBURG'-TYPE LENSES

Spherical Luneburg Lens

The best-known symmetrical scanning system is a lens described by Luneburg² and investigated further by others.³⁻⁷ In its complete form, the lens is a sphere with the property that energy from a feed source at any point on the spherical surface is propagated through the sphere and focused into parallel rays emerging from the other side of the sphere. Perfect focusing is obtained for all feed positions on the surface.

This lens is formed as a nonhomogeneous medium in which the index of refrac-

^{*}For years this name has been misspelled because of an error in publishing Luneburg's notes of Ref. 2.

tion *n* varies with lens radius *r* according to the expression $n^2 = 2 - r^2$ for a unitradius sphere. A central cross section of the sphere is shown in Fig. 18-2, together

with typical ray paths through the lens. The ray paths are sections of ellipses which are given in polar (r,θ) coordinates by the expression $r^2 = \sin^2 \alpha/[1 - \cos \alpha \cos (2\theta - \alpha)]$, where α is the feed angle defining a particular ray. Because the lens is a symmetrical structure, certain relationships between angles in the system are evident from Fig. 18-2. The most important is the equiangular relationship between the following: the angle formed between the ray and the radius vector at the point where the ray leaves the lens; the polar angle defined by the radius vec-

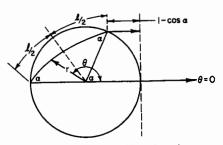


FIG. 18-2 Geometry of Luneburg-lens cross section.

tor to the point at which the ray leaves the lens; and the feed angle, i.e., the angle measured at the source point between the central ray and the general ray. Another point of interest is the fact that the radius vector normal to the ray path bisects the ray path within the lens. Further geometrical information obtained from Fig. 18-2 shows that the path length of a ray within the lens can be obtained as a function of the feed angle. For maximum feed angle of 90°, the ray travels along the lens periphery for a distance of $\pi/2$. A general path length within the lens can be determined from the fact that the optical path length equals $\pi/2 + \cos \alpha$. From the path-length variation it is possible to give an expression for the variation in phase across the semicircular output arc of the lens cross section as $1 - \cos \alpha$, where α is the polar angle.

Another significant property of the Luneburg lens is the fact that the rays emerging from the feedhorn do not appear in a uniform manner across the aperture, but instead tend to spread out in the center and approach a theoretically infinite concentration at the edges. Because of this fact, the analytical aperture illumination is obtained from the original feed pattern multiplied by the factor $sec \alpha$.

Single-Refractive-Index Lens

An approximation to the Luneburg lens can be obtained by the use of a constant-refractive-index material for the sphere. This design sets the path length of the central ray equal to the path length of the ray at 30° from the axis. (Other angles can be chosen by the designer.) For a sphere of unit radius, the equation is $2n = 2n \cos \theta + 1 - \cos 2\theta$. This expression is solved for refractive index:

$$n = \frac{1}{2} \left[\frac{1 - \cos 2\theta}{1 - \cos \theta} \right] = 1.87$$

With this value of refractive index, the phase error normalized to the sphere radius is

$$\Delta(\theta) = 1 - \cos 2\theta - 3.74(1 - \cos \theta).$$

The phase error gives a reduction in gain and an increase in sidelobes. For a radius of 10 wavelengths, the maximum phase error becomes one-tenth wavelength, an accept-

able value. Higher values of radius give greater error. Besides the phase error, the lens has a surface reflection not found in the Luneburg.

Double-Refractive-Index Lens

A variation of the spherical lens uses two indices of refraction to give more flexibility. A two-shell lens⁸ was used to collect rays from across the entire aperture, whereas the lens described above used about 90 percent of the aperture dimension. This two-shell design requires indices of 3.6 in the outer shell and 2.75 in the inner shell. It has a much greater reflection coefficient at the lens surface. The design of the constant-index-lens shells is straightforward, and the designer can employ whatever compromise is needed between the use of the entire aperture and the increase in refractive index required.

Two-Dimensional Luneburg Lens

Many interesting variations of the Luneburg lens have been analyzed. The simplest to consider is one in which only a plane section of the lens is utilized. The ray paths through this section are, of course, identical with those of Fig. 18-2. However, the emerging wavefront is not a plane but a saddle-shaped surface. This surface is the envelope of the Huygens wavelets, with centers on the semicircular aperture. In rectangular coordinates, this surface is given by the parametric expression

$$x = \beta$$

$$y = \frac{\sqrt{1 - \alpha^2}}{\alpha} (1 - \beta - \alpha)$$

$$z = \left[(1 - \alpha^2)^2 - (\beta - \alpha)^2 - \frac{1 - \alpha^2}{\alpha^2} (1 - \beta - 2\alpha)^2 \right]^{1/2}$$

Because of this distorted wavefront, certain limitations exist in the radiation pattern. This pattern has been carefully analyzed in Ref. 9, in which it is shown that a sidelobe level of 17 to 18 dB exists for all normal feed-horn illuminations. This problem can be circumvented by introducing a linear aperture, as shown in Fig. 18-3. A cylindrical wavefront is produced by this system, so the pattern expected is similar to that

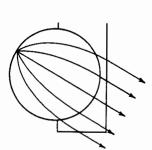


FIG. 18-3 Luneburg lens with a linear aperture.

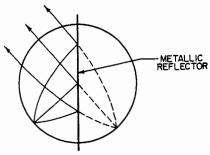


FIG. 18-4 Ray paths in a virtual-source Luneburg lens.

obtained from an ordinary line source. It should be pointed out that the introduction of the linear aperture destroys the symmetry of the lens and so limits the system to narrower angles of scan. Experimental models using the linear aperture have been shown to have sidelobes of 25 dB.

Virtual-Source Luneburg Lens

Another variation of the Luneburg lens involves the addition of plane metallic reflectors passing through the center of the lens. ¹⁰ The addition of such reflectors produces virtual sources whose positions depend on the orientation of the real feed source and the metallic reflector. Figure 18-4 shows a lens cross section with a single reflector in place. From a consideration of the ray paths, it is evident that a perfect virtual image of the real source is formed. It should be noted from the figure that not all the energy from the real source which passes through the lens will strike the reflector. Therefore, this antenna will produce two focused beams, one from the real source and one from the virtual source.

Small-Feed-Circle Luneburg Lens

Another variation of the spherical Luneburg lens has produced a system with a smaller radius of the feed circle and a limited angle of scan. Three general expressions are available.

The first expression was obtained by Eaton in Ref. 3. He considered a sphere of unit radius, with refractive index equal to unity on the surface and with a feed position at any distance, less than or equal to unity, from the center of the sphere. If the radius of the feed circle is denoted by a, then the variation in index is given by the following expression:

$$n^{2} = \frac{2a - r^{2}}{a^{2}} \qquad \text{for } 0 \le r \le a$$

$$n^{2} = \frac{2 - r}{r} \qquad \text{for } a \le r \le 1$$

From the expression it can be seen that if the feed-circle radius is one-half of the radius of the sphere, the index at the center is 2, the index at the feed circle is 1.7, and at the edge of the lens the index is unity. The variation in index can be shown to be continuous with discontinuous slope at the point a.

The second expression for a small-feed-circle Luneburg lens was derived by J. Brown. He indicated that the problem could be attacked by assuming a certain variation in index between the feed circle and the outer surface and then computing the variation within the feed circle which would yield the desired focusing properties. He considered the problem of bringing all rays incident upon the lens surface into the feed point and displayed two solutions to this problem. The first solution involved choosing a refractive index which was constant in the outer region. In terms of the variables used above, the refractive index was chosen as 1/a. With this constant value of refractive index, the index variation in the inner region was found by a numerical-integration process. For a feed-circle radius of one-half of the lens radius, the results showed that the index had a maximum value of 2.34 at the lens center and decreased monotonically

to the value of 2 at the feed circle. The index in the outer region had the constant value of 2.

A third small-feed-circle Luneburg lens was obtained by Gutman.⁷ He selected an index variation given by the expression $n^2 = (1 + a^2 - r^2)/a^2$ and then showed that with the feed at a distance a from the lens center the outgoing rays would be parallel. It is obvious from this expression that the index and its slope are continuous functions of the radius. For a feed-circle radius equal to one-half of the lens radius, the index varies from 2.24 at the lens center to 2 at the feed-circle radius and to unity at the surface.

Parallel-Plate Luneburg Lens

The Luneburg can be used in parallel-plate form with either the TEM^{11,16} or the TE^{9,16} mode. The formulas are:

TE₁₀: plate spacing
$$s = \frac{\lambda}{2\sqrt{n^2 - 2 + r^2}}$$

TEM: $\tanh \left[\frac{2\pi}{\lambda} (s - t) \sqrt{1 - r^2} \right]$

$$- \frac{1}{n^2} \sqrt{\frac{n^2 - 2 + r^2}{1 - r^2}} \tan \left(\frac{2\pi t}{\lambda} \sqrt{n^2 - 2 + r^2} \right)$$

where t is dielective thickness and λ is free-space wavelength.

Surface-Wave Luneburg Lens

The Luneburg lens can be configured by using a TM or TE mode in a surface wave (see Chap. 12 for a discussion of surface-wave media). A number of surface-wave lenses¹² have been described. Their performance has been limited only by the difficulty of controlling the pattern in the plane perpendicular to the lens surface. The lens configuration is similar to that of the TEM lens with the top cover removed. Reference 12 gives design and experimental data.

Geodesic Analog of Luneburg Lens

Another variation of the Luneburg lens is obtained by using the relationship between geodesics on a surface and ray propagation in a plane variable-index medium. The relationship can be understood by considering Fig. 18-5, which shows geodesics on a surface and the corresponding rays in a plane. A given element of geodesic-arc length on the surface corresponds to an element of optical-path length in the plane. Since the required index variation in the plane is known, it is possible, by relating arc-length elements, to determine the required surface containing the geodesics. ¹³ It can be shown that this surface is a surface of revolution whose generating curve is given in rectangular coordinates by the expression

$$Z = \sqrt{P^2 + \frac{R^2}{4} + P} - \frac{1}{3} \ln \left(\frac{\sqrt{3}}{2} \sqrt{1 + P} + \frac{\sqrt{1 + 3P}}{2} \right)$$

where Z = coordinate along axis of revolution

$$P^2 = 1 - R^2$$

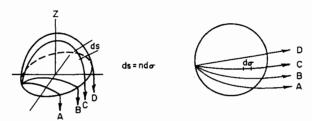


FIG. 18-5 Rays on a surface and in the corresponding variable-index region.

$$R^2 = X^2 + Y^2$$

A major problem arises in constructing the geodesic analog of the Luneburg lens. From a consideration of Fig. 18-5, it can be seen that the rays leave the dome-shaped surface along a cylindrical surface and are not focused in a plane, as required in the original lens. To correct for this fact, that the analog surface has a vertical tangent at its periphery, a toroidal bend is introduced. This bend produces some defocusing of the family of rays.

To avoid the defocusing introduced by the toroidal bend, Warren¹⁴ developed an analog of the Luneburg lens whose surface had horizontal tangents at the periphery. The surface is obtained by a method of approximation, which amounts to a construction as a series of conical sections, the slope of each cone being chosen to focus the ray at a particular feed angle. Warren developed another analog in which a toroidal bend was introduced in the feed region so that the feed horn could be mounted and rotated under the dome of the lens.

Further work on the geodesic Luneburg lens is given in Refs. 15 and 16. The latter reference presents an excellent discussion of these antennas.

18-3 LENS SCANNERS

Dielectric Lens

The simplest type of scanning lens is that which uses a constant index of refraction, a hyperboloid as the initial surface, and a plane as the secondary surface.¹⁷ The design of this lens is based upon placing the source at the focal point of the hyperboloid. Rays from the feed are bent at the initial surface to be parallel to the system axis. The lens cross section, shown in Fig. 18-6, is a hyperbola whose eccentricity is equal to the refractive index of the dielectric material. In the notation of the figure, the focal length of the system is f = c + a, and the index is n = c/a. For a given focal length f and index n, one can solve for c and a so that the hyperbola in rectangular coordinates is

$$x^2 - y^2 (n^2 - 1) = \frac{f^2}{(n+1)^2}$$

Since the lens is designed only for on-axis focusing, exceptional scanning qualities are not expected.

Another dielectric lens which has been used for scanning involves a symmetrical element with identical initial and secondary surfaces. ¹⁸ A feature of this lens is that

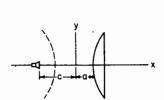


FIG. 18-6 Geometry of a dielectric lens.

FIG. 18-7 Symmetrical dielectric lens.

two scanning feeds can be used simultaneously, one on either side of the lens. The two beams can cover sectors 180° apart in space.

The design of this lens is based on the assumption that the lens can be closely approximated by a prism between the points where a ray enters and leaves the surface. The coordinates of the lens surface can be found from the following expression, all the parameters of which are given in Fig. 18-7:

$$x = \frac{[f(1 - \sec \varphi) + 2a(n - 1)](2 \cos^2 \alpha \sin \omega - \sin \beta)}{(n - \cos \alpha) \sin \beta + (n \sec \alpha - \sec \varphi)(2 \cos^2 \alpha \sin \omega - \sin \beta)}$$
$$y = (f - x) \tan \varphi$$

The three angles β , φ , and α are known in terms of the ω parameter:

$$\beta = 2\omega - \cos^{-1}\left(\frac{\cos\omega}{n}\right)$$

$$\varphi = \omega - \cos^{-1}\left(n\cos r_1\right)$$

$$\alpha = \cos^{-1}\left(\frac{\cos\omega}{n}\right) - \omega$$

The surface is found by selecting values of the parameter ω , computing the three angles, and substituting their values into the expression for x and y.

Wide-Angle Dielectric Lenses

The Abbe sine condition has been used in designing the dielectric lens for scanning. This condition applies to a symmetrical optical system with its source on axis. It concerns a matching of the ray from the source (spherical wave) with its corresponding ray (in a plane wave) emerging from the system. The reflections and refractions within the system are ignored, and the condition asks that the intersection of corresponding rays lie on the spherical wavefront. In a cross section containing the axis, an initial ray at an angle α meets a final ray at a distance d from the axis on a circle defined by $d = r \sin \alpha$, where r is the radius of the circle.

The greatest amount of work using this condition was done by Friedlander.¹⁸ He found that he could closely approximate the circle of intersection between initial rays and final rays by using a relatively simple lens. Instead of using two curved surfaces, his lens had a plane face for the initial surface and a curved face for the final surface.

With a refractive index of 1.6 and f/D = 1, he found a deviation from the sine condition of the order of 0.33 percent of the focal length. An experimental lens of 50 λ aperture gave satisfactory patterns over a 20° total scan angle.

A lens system which gives promise of wide-angle focusing is one that uses two curved surfaces to obtain perfect focusing (at two focal points) of waves from two conjugate directions. ^{19,20,21} The two most useful design methods are the algebraic curve and the lattice. The first assumes that the two-dimensional-lens faces are algebraic curves and then determines the coefficients of the algebraic expressions by selected ray tracing. The second is a step-by-step procedure, adapted to computer use, in which points on the two lens surfaces are found by considering alternately the two focal points. Some effort has been made toward designing a three-dimensional lens by using a two-dimensional design to form the lens faces as surfaces of revolution, but the resulting lens has serious astigmatism.

Metal-Plate Lenses

The simple metal-plate lens described in Chap. 16 has been used successfully as a scanning antenna. This lens design provides perfect focusing for a single position of the feed; wide-angle performance is obtained by choosing a long focal length. Some problems which arise at off-axis feed positions are related to the basic nature of the metal-plate lens. Since the lens is a periodic structure, diffraction lobes²² which increase with an increase in scan angle appear; these lobes are present in addition to the normal coma lobes. To prevent them from becoming objectionable, the angle which the incident rays make with the lens surface must be limited; this limitation in turn limits the feed displacement and the angle of scan.

Metal-plate lenses can be designed for improved performance by using the Abbe sine condition. One such lens design uses square-waveguide elements which constrain the incident energy to travel through the lens in a direction parallel to the lens axis. Such a design simplifies considerably the analysis of the system, since the refraction follows a much simpler expression than that given by Snell's law. One lens design offered²³ not only satisfied the Abbe sine condition but also, by proper choice of the waveguide medium, yielded a system which would operate over a broader band than that possible with the normal metal-plate lens.

One of the earlier metal-plate scanning lenses was constructed between parallel plates with the general form shown in Fig. 18-8.²⁴ In this lens, the initial surface was

curved, and the index of refraction was varied in the dimension. The design of the system then employed three basic variables: (1) the lens surface, (2) phase delay between input and output of a given lens channel, and (3) constraint of energy entering at a given point to leave at a desired point.

The lens surface is given by the circle $(x - \frac{1}{2})^2 + y^2 = (\frac{1}{2})^2$, the coordinates of which are shown in Fig. 18-8.

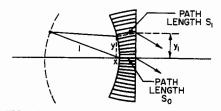


FIG. 18-8 Lens using path-length correction.

The phase delay for a particular channel is found in terms of the delay in the central channel and the coordinate z. The required expression is $s_1 - s_0 = 1 - \sqrt{1 - x}$. The final variable, the distance from the axis to a general emerging ray, is given by the expression $y_1 = \sqrt{x}$.

Experimental results on this lens showed that it maintained a constant beamwidth of 2.2° over a total scan angle of 40°; no information is available on the sidelobe level. In taking these data, the feed horn was confined to a circle of unit radius.

Metal-Plate Lenses with Two-Point Correction

A decided improvement in scanning has been achieved when the Abbe sine condition of optics is ignored and, instead, the lens is designed to provide perfect focusing at two

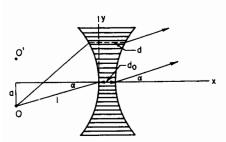


FIG. 18-9 Two-point-correction lens.

points.²⁵ Figure 18-9 indicates the geometry of such a design in a two-dimensional lens. This design employs a constrained lens of constant refractive index. The lens surfaces are chosen so that plane waves arriving from the directions $+\alpha$ and $-\alpha$ are exactly focused at the points 0 and 0' respectively. By using the design geometry of the figure, the first lens surface is an ellipse $(x/a + 1)^2 + y^2 = 1$, and the second lens surface is obtained by determining the lens thickness at any point. An expression involving the lens

thickness as a function of the lens constants and the coordinate x is given as $ax = (n - a)(d - d_0)$, where n is the refractive index and the other parameters are given in the figure.

A second two-dimensional lens utilized a variable index but a plane outer surface. In this case, the inner surface was identical with that of the lens in the preceding paragraph, and the variation in the refractive index was given by the expression $(n - n_0)d_0 = nx - m\lambda$. The term $m\lambda$ has been introduced into this expression to obtain wavelength steps in the lens. This is necessary to minimize the range over which the refractive index must vary. Since waveguide techniques are utilized, the refractive index is limited to values between 0.5 and 0.9.

A three-dimensional lens which produces perfect focusing at two points can be obtained. The inner lens surface is an ellipsoid, given by the expression

$$\left(\frac{x}{a}+1\right)^2+y^2+\left(\frac{z}{a}\right)^2=1$$

Here the symbols are those of Fig. 18-9, and the coordinate z is measured normal to the xy plane. Once the inner surface is found, the outer surface is obtained from an expression involving the lens thickness:

$$ax = (n - a)(d - d_0)$$

An important improvement in the performance of a constrained lens with two-point correction has been obtained by Peeler. His design utilized the basic lens together with steps which were arranged to minimize the phase errors in the on-axis position. He thus had corrections at three points and an overall reduction in phase errors at all scan positions. Computations on the final design showed phase errors of less than one-tenth wavelength over the aperture throughout the scanning of a ½° beam through 20°.

18-4 PARALLEL-PLATE SCANNERS

Surface-of-Revolution Scanners

The scanner considered here is a parallel-plate region whose mean surface is a surface of revolution. This surface is intended to satisfy the following conditions. ¹³

- 1 It contains a circle (the feed circle).
- 2 It contains a straight-line segment (the aperture which can become the focal line of a parabolic cylinder).
- 3 All geodesics joining a fixed point of the feed circle to points of the aperture meet the aperture at a constant angle (optical requirement).
- 4 All geodesics normal to the feed circle pass through a fixed point (the center of illumination) of the aperture (illumination requirement).

At the present time, no such surface has been found. If requirement 4 is eliminated, a solution which is known as the R-and-2R scanner²⁴ is possible. The action of this scanner can be understood by considering the mean surface laid out in Fig. 18-10. Here the source is placed on the feed circle of radius R. Energy passes across this mean surface to the opposite side of the circle, where it encounters the output region with boundaries which include a circle of radius 2R and the linear aperture. From simple geometry, the path length of a ray in the initial region is given by $2R \cos \alpha$, where α is the feed angle. The ray path in the output region is given by $2R(1 - \cos \alpha)$, so it is evident that all path lengths from the source to the aperture are equal. For another position on the feed circle, because of the symmetry in the final structure, all rays meet the aperture at a constant angle so that perfect focusing is available. For

feed positions other than that of Fig. 18-10, the central ray does not pass through the center of the aperture, so that the utility of the scanner is limited. As the feed horn scans, the maximum intensity appears at various positions in the aperture, and during the greater part of the scan the energy lies at either end of the aperture.

A lens of the type described above was constructed by introducing an imaging reflector in the initial parallel-plate region and rolling the plates into a cone with the feed arc formed into a complete

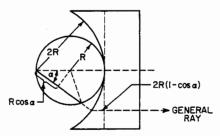


FIG. 18-10 Geometry of the general ray in the *R*-and-2*R* scanner.

circle on the base of the cone. The on-center radiation pattern had a beamwidth of 0.6° and a sidelobe level of 16 dB. This two-dimensional lens has a three-dimensional counterpart which has scan limited by astigmatism. Rays in the plane of scan have perfect focusing, but rays in the other principal plane are not perfectly focused.

The majority of the other surface-of-revolution scanners are an outgrowth of the work of Myers.²⁷ The surface considered has been either a cone or a cylinder. Since both of these are developable surfaces, it is possible to analyze the ray paths with simple geometry. The general problem is indicated in Fig. 18-11, which shows a devel-

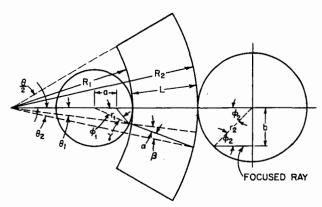


FIG. 18-11 Geometry of the conical surface-of-revolution scanner.

oped cone having a sectoral angle designated as θ . From a consideration of arc lengths on the circular top and bottom planes, one has that

$$2\theta R_2 = 2\pi r_2 \qquad 2\theta R_1 = 2\pi r_1$$

and therefore,

$$\frac{r_2}{R_2} = \frac{r_1}{R_1}$$

Further investigation of the arc lengths along the discontinuities in the conical surface shows that $R_1\theta_1 = r_1\varphi_1$ and $R_2\theta_2 = r_2\varphi_2$. It can therefore be seen that $\theta_2/\varphi_2 = \theta_1/\varphi_1$. Because geodesics on the surface form equal angles with the normal to a surface discontinuity, one can write that $\alpha = \gamma$ and $\beta = \varphi_2$.

For a cone in which r_1 and r_2 are nearly equal, $\alpha \approx \beta$, and some consideration can be given to the maximum distance b at which a ray can be normal to the aperture. It can be shown that $b = r_2 \sin \alpha$. Since r_2 is a constant, the maximum value of b occurs for large $\sin \alpha$ or large values of the feed-circle radius a. If a is set at its maximum value of r_1 , a simple lens design can be evolved: for a length L of the cone, if a ray crossing the aperture at b is in phase with the central ray, then the length L must be $r_2 \cos \varphi_2$. This design is exact only when the disk radii r_1 and r_2 are equal, i.e., when the cone becomes a cylinder.

Double-Layer Pillbox

Rotman²⁸ has investigated several experimental models of the cylindrical scanners indicated in Fig. 18-12. The half-cylinder unit shown on the left possesses the general characteristics required in the surface-of-revolution scanner. The model on the right represents an improvement in symmetry obtained by eliminating the requirement for a linear aperture and permitting the energy to radiate from the circular aperture.

Rotman divided the double-layer pillbox antennas by size in wavelengths: (1) small, $<10\lambda$, with no correction needed; (2) medium, to 20λ , using parallel-plate contours; and (3) large, to 40λ , using plate contours and multiple feeds. Rotman's early

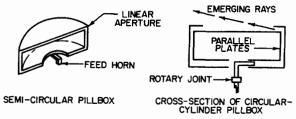


FIG. 18-12 Cylindrical surface-of-revolution scanner.

work was followed²⁹ by correcting in parallel-plate structures through using the bootlace principle of Sec. 16-10 in Chap. 16.

Concentric-Lens Scanner

The concentric-lens scanner is related to the scanners described immediately above. It is made up of a cylinder or half cylinder whose height is very small compared with its diameter. This scanner contains a lens whose surfaces are concentric with the cylinder surface; this lens can be mounted in either the upper or the lower pillbox region.

Rotman studied a concentric-lens system in which the lens was mounted in the lower (feed-horn) region, as shown in Fig. 18-13. Kales and Chait at the Naval Research Laboratory studied a scanner in which the lens was mounted in the upper (output) region. They found that if the radius of the cylinder was R and the lens radii were R_1 and R_2 , then a useful lens was obtained by using the relation $1/R = 1/R_1 - 1/R_2$.

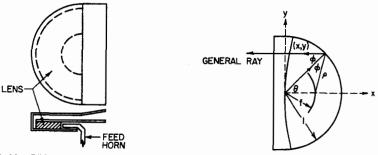


FIG. 18-13 Pilibox-concentric-lens sys- FIG. 18-14 Geometry of the Schmidt lens. tem.

Schmidt Lens

This system consists of a spherical reflector, together with a nearly plane correcting lens, which passes through the center of the sphere. A derivation of the design of this system is contained in Ref. 30. The result is that the lens cross section in Fig. 18-14 can be defined in parametric form by the following expression:

$$x = \frac{2\cos\theta - f\cos 2\theta - c\cos\psi}{1 - n\cos\psi}$$

$$y = 2 \sin \theta - f \sin 2\theta - \frac{c \sin \phi - n \sin \psi (2 \cos \theta - f \cos 2\theta)}{1 - n \cos \psi}$$

where
$$\psi = \theta - \phi$$

 $c = 2 - f$
 $\sin \phi = (f \sin \theta) / \sqrt{1 + f^2 - 2f \cos \theta}$

Several experimental models of the Schmidt system have been built in parallelplate media. Some of these have involved a single layer of parallel plates with a circular reflector, while others have employed a double layer and a toroidal-bend reflector. Excellent scanning performance has been obtained on all models which have utilized a dielectric lens. Metal-plate lenses have been less satisfactory.

Schwarzschild System

This system employs multiple mirrors rather than a lens and a mirror. It is a two-mirror device based on a general optical method developed by Schwarzschild. Such a system, in optical terminology, has no spherical aberration or coma. The only experimental system using this principle was built in the form of a triple-layer parallel-plate region. The feed horn moved on a 90° arc of a circle in the first layer. Energy from the feed was reflected at the first toroidal-bend reflector, passed through the middle layer, was reflected from the second bend, and left the parallel plates through a linear aperture in the third layer.

The surfaces of the first and second reflectors were calculated, respectively, from the equations

$$x_1 = 0.5y^2 - 0.03125y^4 - 0.22y^6$$

$$x_2 = 0.75y^2 - 5.96025y^4 + 40.53y^6$$

where the coordinate x is parallel to the direction of the optical axis.

Zeiss-Cardioid System

This system is similar to the Schwarzschild in that it employs two reflectors. The major difference is that it uses simple reflecting surfaces and yields perfect focusing for the feed on the axis. The mirrors used are a circle and a cardioid. The design of this system can be understood by considering Fig. 18-15. If the position of the feed

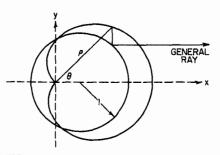


FIG. 18-15 Geometry of the Zeiss-cardioid reflector system.

horn is taken as the origin, then the reflecting surfaces have the following equations:

Reflector 1:
$$\rho = 1 + \cos \theta$$
Reflector 2: $(x - \frac{1}{2})^2 + y^2 = 1$

An X-band model of this reflector system with an aperture of 36 in (914.4 mm) had a half-power beamwidth (HPBW) of 3.3°, using a wavelength of 32 mm. This antenna, investigated by W. Rotman at the Air Force Cambridge Research Center, proved capable of scan-

ning through a total angle greater than 15 beamwidths with a loss in gain of less than 1 dB.

18-5 SCANNING WITH REFLECTORS

The simplest type of focusing objective is the reflector. This is a lightweight component, relatively easy to construct, and so has found wide application in the scanning field. The majority of the reflectors have been paraboloids; others of interest are a section of spherical surface, a torus, and a parabolic torus. These will be considered in turn in the discussion which follows.

Paraboloidal Reflector

The paraboloidal reflector has been used as a scanner in many forms, of which the simplest is the symmetrical one with the vertex of the paraboloid at the center of the reflecting surface (circular aperture). Other reflectors were formed of offset sections of the paraboloid surface which did not include the vertex point or which included this point at some off-center position. The aperture of these offset reflector types does not fit any simple plane curve, although they could normally be approximated by an ellipse. Since there are so many different offset reflectors, it is impossible to describe the scanning performance of each.

The parameters available in the circular-aperture reflector are the aperture width, the aperture illumination, and the focal length. An analysis of the pattern of the circular aperture with feed displaced from the focal point showed minimum variation of pattern shape with moderate changes of the aperture width in wavelength.³¹ For the aperture widths of interest, it is necessary only to consider the illumination and the focal length; Ref. 31 shows data for two illuminations and four focal lengths.

Most of the data of Ref. 31 were taken with the feed horn moved off axis in the H plane; a check of the characteristics of the feed horn moved off in the E plane showed agreement within experimental error. The implication is that the variation in scanning characteristics is a scalar problem independent of polarization. A check on the variation in the cross-polarized component over the angle of scan showed that it was relatively constant over the angle of scan and dropped in intensity at the edges of the scan sector.

The data for all four reflectors showed a decrease in gain and an increase in sidelobe level as the beam was scanned away from the axis. The sidelobe on the axial side of the pattern increased rapidly, while that on the other side of the pattern was merged into a main beam. Figure 18-16 shows a typical pattern variation over the angle of scan. Some difference was noted in the pattern characteristics with a change in aperture illumination. With 10-dB illumination, the sidelobe level increased more rapidly than with 20-dB illumination. Scanning characteristics improved with an increase in focal length; best results were obtained with the longest focal length, which corresponded to an f/D ratio of 0.75.

A study was made of the orientation of the feed during scanning. The two possibilities considered involved pointing the feed toward the vertex of the reflector and pointing it so that its axis was parallel to the axis of the reflector. Only minor differences in the patterns were found with changes in feed orientation, so that it was impossible to the axis of the reflector.

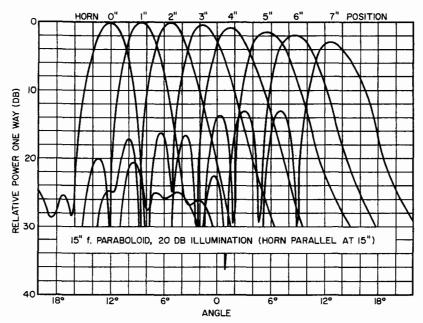


FIG. 18-16 Patterns from the paraboloid with feed displaced from the axis.

sible to say that one or the other orientation was superior. It was found that best scanning results were obtained when the feed was moved along a line perpendicular to the reflector axis.

Most deductions concerning scanning performance are based on radiation patterns taken in the plane of scan. Patterns taken in the other principal plane showed that the beam varied only slightly with feed positions and that for the larger scan angles the first sidelobe was merged into the main beam.

One very interesting effect arises from the study of the scanning performance of the paraboloid. It is found that if the feed horn is moved through a certain angle away from the axis, then the radiated beam is displaced through a smaller angle from the axis. The ratio between the angle which a radiated beam makes with the axis and the angle which the feed displacement from the axis subtends at the vertex is called the beam factor. It was found that the beam factor was dependent upon the focal length, the aperture distribution, and the position off axis. Of these three parameters, the focal length was the most significant. For moderate displacements from the axis, the beam factor showed only slight variation with feed position. Figure 18-17 shows a plot of the beam factor obtained from the experimental data.

Reflector Tilt

The paraboloidal reflector can achieve twice the angle of scan for a given beam degradation if the reflector is moved and the feed held fixed. In effect, one half of the scan comes from moving the feed off axis, and the other half comes from the motion of the focusing objective. The motion of the reflector can be very effective in millimeter antennas, in which reflectors are small.

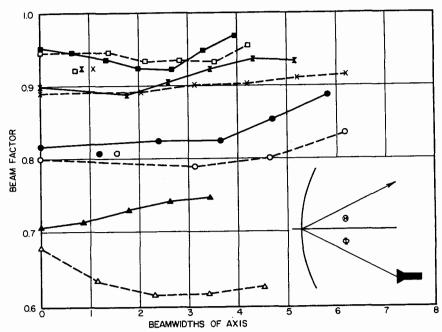


FIG. 18-17 Beam factor as a function of focal length and edge illumination in a 30-in (762-mm) paraboloid: ———— 20-dB illumination; ———— 10-dB illumination. $\Delta=7.5$ -in (190-mm) focal length, O=10.6-in (269-mm) focal length, C=10.6-in (381-mm) focal length, C=10.6-in (571.5-mm) focal length.

Another type of reflector scanning uses a plane reflector³² as indicated in Fig. 18-18. Here the paraboloidal reflector is linearly polarized so that it will reflect horizontal polarization and transmit vertical polarization. The plane reflector is a twist reflector which twists the incident polarization.

Spherical Reflector

The spherical reflector is not a replacement for the paraboloid when wide-angle scanning is needed. For long focal lengths, the two reflectors have similar performance. For short focal lengths and a restricted use of the spherical aperture, the spherical reflector gives excellent performance. However, this performance comes with the drawback of very poor aperture efficiency caused by the use of only one-tenth of the available aperture.³³

A direct comparison of the spherical reflector and the paraboloid reflector was made in Ref. 31 for values of focal length ranging from 0.25 to 0.75. The reflectors were illuminated with edge values of 10 dB and 20 dB. The sphere showed a performance similar to the paraboloid except for higher sidelobes. A simple analysis of the wavefronts from the two surfaces shows that both have third-order phase errors, and so both have the asymmetry in sidelobes sometimes called coma lobes.

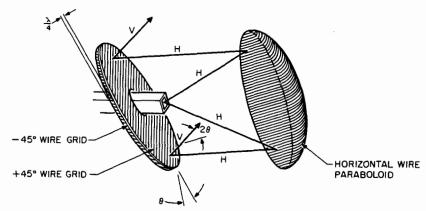


FIG. 18-18 Scanning with a plane reflector.

Corrected Spherical Reflector

There is a wide variety of approaches to correcting the spherical reflector so as to increase aperture efficiency. A correcting lens or reflector can be added to the system. The most noteworthy is the Mangin mirror technique. Here the lens is in contact with the reflector. The lens surface nearest the feed is a sphere whose radius can be varied to optimize performance. Computer programs permit a wide variety of designs. Correction of the aberration by a reflector³⁴ has been defined, but most of the effort has been devoted to corrected feed systems. The feed configuration of end-fire line sources^{35,36,37} has been studied for many years, and the Arecibo antenna in Puerto Rico uses such a source.³⁸ The alternative configuration of feeds consists of broadside sources.^{39,40,41} With phased-array techniques, the broadside feed array can be made effective for multiple scanning beams.

Torus Reflector42

Another reflector which has been suggested for scanning applications is the torus, obtained by rotating an arc of a circle completely about an axis which lies in the plane of the circle. For it to be useful, the reflecting surface must be made up of rods at 45° to the axis of revolution. A feed horn which yields polarization parallel to the reflecting elements is placed within the torus surface. The energy focused by the reflector appears at the opposite surface of the torus with a polarization normal to the reflecting elements so that it passes through the torus surface and forms a radiated pattern in space. Because of the symmetry of this reflector, the feed horn can be moved on a circle of constant radius to yield a scanning of the focused beam.

The parameters available in the design of this reflector are the radius of the feed circle, the distance from the axis of revolution to the vertex of the circular arc, and the axial extent of the surface. With one choice of parameters, the torus degenerates into a section of a spherical surface. Other variations upon the basic design would include the substitution of any plane curve for the circular arc. In this way, beam shaping in the plane normal to the plane of scan can be achieved.

The basic limitation on the torus scanner is similar to that of the spherical reflector: perfect focusing cannot be achieved. However, if the radiation characteristics obtained are satisfactory, then this scanner offers a lightweight, compact structure capable of sweeping a beam through 360° in azimuth.

Parabolic-Torus Reflector43

One variation of the torus scanner, which has been investigated in some detail, is that obtained by replacing the circular arc with a parabolic arc and by limiting the rotation

of the parabolic arc about the axis of revolution to an angle of less than 180° so that the reflector does not require the polarization properties of the previous torus. The parameters available in the design of this system are the focal length of the parabola, the distance from the axis of revolution to the vertex of the parabola (torus radius), the angle of revolution, and the axial length.

A study was made of the wavefront produced by the parabolic torus when illuminated by a point-source feed. A satisfactory reflector was the half torus. which used a parabolic arc, one of whose end points was the parabola vertex. With a ratio of focal length to radius of about 0.45, a minimum deviation from a plane wave was obtained. The patterns measured with this reflector are shown in Fig. 18-19. It is evident that reasonable sidelobe levels can be obtained in the plane of scan and that good sidelobe levels can be obtained in the other plane. However, one important characteristic of this type of reflector is the higher sidelobes which appear in the planes at 45° to the principal planes. Data obtained on this reflector show lobes as high as 13 dB in these planes. For applications in which these

lobes are not objectionable, this reflector is superior to the paraboloid and sphere.

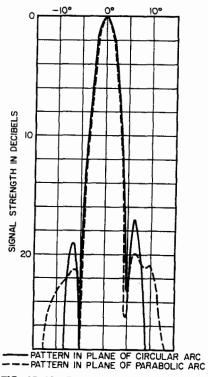


FIG. 18-19 Patterns from parabolic torus.

Another parabolic-torus reflector was the full torus, which had a circular aperture similar to the paraboloids previously described. This reflector showed radiation characteristics unlike that of the half torus; the sidelobes were merged into the main beam to produce a tent-shaped structure. The maximum sidelobes were in the principal planes. An optimization of the torus reflector produced an elliptical torus, described in Ref. 44.

18-6 FEED-MOTION SYSTEMS

The scanning systems described here are used together with one of the focusing objectives of the earlier sections. These scanners satisfy the general requirements of moving a point source rapidly over a curve or a surface in space. The great majority of the feed-motion systems produce a beam moving through a plane in space so that the feed path is a plane curve. If a scan over a volumetric region is desired, it can be obtained by a combination of several scans, each confined to a different plane.

There are two general methods of scanning over a plane, namely, oscillating scan and sawtooth scan. In the first, the beam sweeps across a plane and then returns by the same route; this can be accomplished simply by mechanical oscillation of the feed horn. In the sawtooth scan the beam sweeps across the plane of scan and then steps back instantaneously to its initial point. This normally requires a more complex feed system, but it is more efficient since the beam equally covers all positions in the plane of scan.

If we ignore the simple feed-horn oscillation, all existing feed-motion systems are based on mechanical rotary motion. These systems can be placed in three categories, namely, the virtual-source scanner, the organ-pipe scanner, and the moving of a linear or curved waveguide element. In practical application, the virtual-source scanner utilizes a source produced by a reflection or a refraction at some optical component between a real source and the focusing objective. In most of these scanners, the feed horn, a real source, is rotated continuously in front of an imaging reflector, which forms the virtual source. However, it is possible to obtain the same effect by holding the feed horn fixed and rotating a refractive prism. In either case, the apparent feed-source motion is approximately sawtooth in nature.

The most widely used feed-motion system (shipboard air search radar) is the organpipe scanner. A rotary motion of a small feed horn is converted to motion along the desired feed path through the simple process of connecting, with waveguide channels, points on the feed circle to points on the desired feed path. A variation in this system occurs when the feed horn is held fixed and a section of the waveguide channel is rotated to accomplish the same purpose. The remaining type of feed-motion system employs a moving portion of a waveguide wall, cylinder, or channel.

Lewis Scanner⁴⁵

One of the earliest virtual-source scanners was the Lewis scanner, which employed a parallel-plate region. The action of this scanner is evident from Fig. 18-20, in which

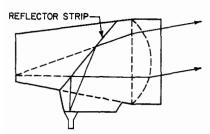


FIG. 18-20 Lewis scanner.

rays from the real source strike a reflector strip at 45° to the antenna aperture and so produce a virtual source which feeds the lens. The straight-line feed path is formed into a circle by rolling the parallel-plate region into a cylinder. A rotation of the feed about the base of the cylinder produces a virtual source which appears to be moving along a straight line. Some dead time occurs when the feed horn is opposite the position on the cylinder where the two ends of the

feed path are joined. The amount of dead time depends on the length of the feed path and the size of the feed horn; normally, it represents about 20 percent of the scanning time.

Robinson Scanner⁴⁵

The Robinson scanner is a virtual-source system made up in parallel plates in a manner similar to that of the Lewis scanner. The major differences are the absence of the focusing lens and the use of a more complex imaging reflector. This scanner uses a developable surface which, in planar form, is an isosceles trapezoid. When the surface is developed, the smaller base is bent to lie above the larger base, and then the two ends of the base are brought together to form a circle (Fig. 18-21). Since the surface was developed from a plane, ray paths can be found from a consideration of the rays in a plane. Rays emanating from a horn moving on the feed circle leave the aperture in the same manner as those rays which might come from a feed moving along the smaller base of the trapezoid. The rotary horn motion then produces an apparent linear motion of a virtual source.

The dead time found in this feed-motion system occurs when the feed is opposite the end points of the smaller trapezoid base; the system's value depends on the feed-horn size and the circumference of the feed circle and so is similar to that of the Lewis scanner.

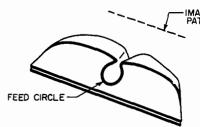


FIG. 18-21 Robinson scanner.

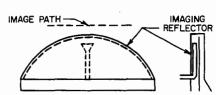


FIG. 18-22 Virtual-source scanner.

Virtuai-Source Scanner

In this system, the feed horn rotates in the lower level of a two-layer parallel-plate region. 46 Energy from the feed is reflected into the upper layer by a parabolic cylinder placed at the junction between the upper and the lower layers (Fig. 18-22). The reflected rays appear to come from a virtual source which moves along an approximately linear path while the feed horn moves through an arc of 120°.

The center of the feed-horn circle corresponds to the focal point of the parabolic cylinder; its radius is about 80 percent of the focal length. Since this feed is used for only 120° of rotation, a complete system would require three feed horns and a suitable switching mechanism. The dead time for this system will then depend on the amount of the rotation cycle required to switch from one feed to the next.

Tilting-Plane Scanner

A variation of the virtual-source scanner is obtained when the feed horn is held fixed as it directs the energy into a plane reflector. The reflected rays appear to come from

a virtual source behind the reflector. The position of this virtual source depends on the orientation of the plane. Consider an initial position with the plane vertical and the

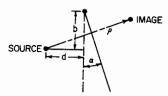


FIG. 18-23 Tilting-plane scanner.

source in a horizontal plane a distance d from the reflector. If the plane is tilted about a horizontal line at a distance from the horizontal plane (Fig. 18-23), then the equation of the virtual-source path is given by $\rho = 2(d\cos\alpha + b\sin\alpha)$.

Prism Scanner

In its simplest form, the prism scanner would employ an element placed between the feed and the objective. Figure 18-24 shows two possible

prisms: (1) the circular element, in which scanning is obtained by simple rotation; and (2) the triangular element, in which scanning is achieved by an oscillation of the triangle.

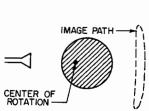
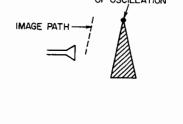


FIG. 18-24 Prism scanners.



The design problems associated with this type of scanner are concentrated in obtaining a good virtual source and minimizing the curvature of the path followed by the virtual source during the scan cycle. From the nature of the problem, most of the design work is experimental.

Foster Scanner

A scanner related to the prism scanners was invented by Foster.⁴⁷ It can be understood by considering Fig. 18-25, which shows a cross section and the complete antenna. At any cross section, the phase is varied by rotating the inner cone. The phase variation is a minimum when the input and aperture are aligned and is a maximum when the energy travels counterclockwise for almost 180°, then through the center region, and

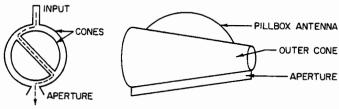


FIG. 18-25 Foster scanner.

finally clockwise for almost 180°. The maximum phase occurs immediately before the input lines up with the aperture (minimum position). This means that the system rapidly switches from maximum condition to minimum condition. Now when the cross section is moved along the cone, the amount of phase shift varies with the cone diameter. Therefore, rays at the smaller end of the cone are shifted in phase less than those at the larger end of the cone. The differential phase shift causes a tilt in the beam from the aperture as the inner cone is rotated. The development work after Foster was directed at implementing a simple configuration. In one instance the line-source input was placed on the rotating cone so that energy traveled only in the clockwise region of Fig. 18-25. The best Foster scanner⁴⁸ used a choke barrier within the conical structure and eliminated an earlier problem associated with directing the energy in the clockwise direction between the cones.

NRL Organ-Pipe Scanner⁴⁹

The action of this scanner can best be understood by considering Fig. 18-26. It can be seen that energy is introduced into certain waveguide channels at the feed circle. It

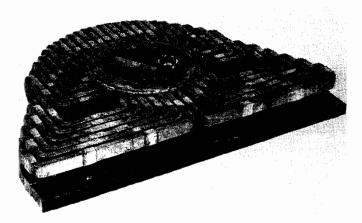


FIG. 18-26 NRL organ-pipe scanner.

propagates through these waveguides, which are all of equal length to the aperture of the system. A rotation of the feed horn produces a change in the channels which are fed and so produces a motion of the radiated energy across the scanner aperture.

The problems associated with this scanner are centered in the transition region between the feed horn and the waveguide channels. By proper choice of dimensions here, the transition loss can be held to less than 0.25 dB at 9.3 GHz. The voltage standing-wave ratio (VSWR) is minimized by maintaining the intersection between channels to a value less than ¼ in (0.397 mm). It was found that the VSWR varied with feed rotation, depending on the number of channels which were fed at any one time; best results were obtained by using a horn which energized 2½ waveguide channels.

A variation in this basic structure would permit the scanner aperture which did not lie along a straight line but fitted any curve. Another variation would involve a change in the spacing between the channel outputs; such a change would produce a nonuniform scanning with a constant rotation of the feed horn. The waveguide can be replaced by a coaxial line to give simpler packaging but increased transmission-line losses.

Sector Organ Pipe

If a circular feed path is desired, the radius of the feed circle can be minimized by introducing a sector of an organ pipe. In this system, channels on the feed circle follow radial lines to the desired scan circle. For constant feed rotation, several horns and a waveguide switch are required.

RCA Organ Pipe50

A variation of the organ-pipe principle is obtained when the feed horn is fixed and a section of the waveguide channels is rotated. One of the possible channel-rotation sys-

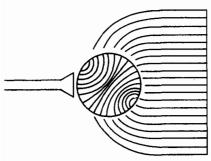


FIG. 18-27 RCA organ-pipe scanner.

tems is shown in Fig. 18-27. From a consideration of the figure, it is seen that with rotation of the cylindrical-channel region the radiated energy is moved along the scanner aperture.

Tape Scanner⁵¹

The simplest type of moving-waveguide-wall scanner involves the physical motion of slots in one face of a waveguide. One system considered is shown in Fig. 18-28. Here energy in a linear length of waveguide is radiated through two slots which

move along the waveguide lengths. To couple out all energy within the guide it is necessary to move an effective waveguide short circuit in synchronism with the slots.

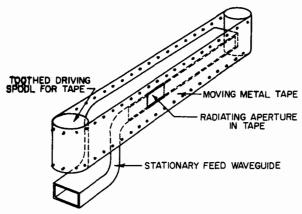


FIG. 18-28 Tape scanner.

This is done by gearing to the tape drive a rotary phase shifter which is terminated in a short circuit.

The major problem associated with this system is that of obtaining a tape which will fit tightly against the fixed waveguide section and yet will be flexible enough to pass around the rotor. One additional problem relates to the means of providing radio-frequency chokes around the periphery of the open-sided waveguide. Successful choke designs were obtained and good results were found by using metal plate in place of the tape.

Helical-Slot Scanner

Another type of moving-slot scanner utilizes a similar waveguide system with one waveguide wall removed. The slot radiator is formed between the waveguide opening

and a helical opening on a circular cylinder (Fig. 18-29). As the cylinder is rotated, the effective radiating aperture moves along a straight line corresponding to the position of the opening in the waveguide.



FIG. 18-29 Helical-slot scanner.

The major difficulty encountered in the design of the scanner was traced to the prob-

lem of the radio-frequency chokes. Any chokes parallel to the waveguide opening were inefficient at the position of the radiating slot because of the lack of necessary cover plate. Various remedies were attempted to improve this situation, including the use of both rectangular and circular waveguide. It was found impossible to obtain satisfactory radiation patterns because of the choke problem. It appeared that the rectangular waveguide was superior to the circular one, since the field within this guide held the same polarization whereas in the circular waveguide polarization varied with the motion of the slot.

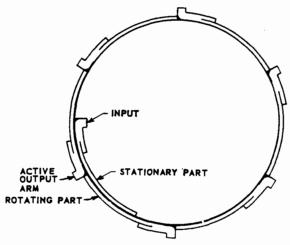


FIG. 18-30 Ring-switch scanner.

Ring Switch

The ring switch is made up of a circular section of waveguide with a fixed input and a number of moving outputs. Figure 18-30 shows a typical configuration. The waveguide between the input and the output is divided so that one portion is moving and the other portion is fixed. Choke arrangements sometimes are required to create radio-frequency continuity between the moving and the fixed portion. If the guide can be split on the center of the two broad faces, chokes may not be necessary. But such a guide might be difficult to match at the input and output ports. Several of these split-guide switches are described in Refs. 52 through 56. A ring switch designed for use with a multiple-reflector antenna (Ref. 57) is the best design available. This scanning switch uses a coupling cavity between the two waveguides, each of which is split along the centerline of the broad face; chokes normally are not necessary.

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Frequency-Scan Antennas

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19-1	Introduction 19-2
19-2	Theory of Operation 19-2
	Scan Bands 19-6
	Grating Lobes 19-6
19-3	Scan Bands and Multiple Beams 19-7
19-4	Monopulse in the Frequency-Scan Plane 19-1
	Parallel-Fed Monopulse Array 19-10
	Tandem-Fed Monopulse Array 19-11
	Dummy-Snake Monopulse Technique 19-1
19-5	Practical Frequency-Scan Antennas 19-13
19-6	Design Considerations 19-15
	Sinuous Feed 19-15
	Bends 19-15
	Couplers 19-16
	Linear Array 19-22
19-7	Millimeter-Wave Application 19-26

A frequency-scan antenna may be defined as any antenna in which the direction of the radiated beam is controlled by changing the operating frequency. The antenna itself is completely passive and is by far the least costly antenna for inertialess beam scan. Simplicity, low cost, and high reliability are the virtues of frequency scan. For these reasons, frequency-scan radars far outnumber all other radars that have inertialess beam scannning. The U.S. Navy S-band AN/SPS-26 frequency-scan radar shown in Fig. 19-1 dates back to the mid-1950s. The AN/SPS-32 ultrahigh-frequency (UHF) frequency-scan radar and the AN/SPS-33 S-band 3-D track radar, which uses phase scan in azimuth and frequency scan in elevation, date back to 1960. In addition to these radars, the U.S. Navy AN/SPS-52 (Fig. 19-2) and AN/SPS-48 (Fig. 19-3) radars, both at S band, the Marine Corps AN/TPS-32 S-band radar, and the U.S. Army X-band mortar-locating radar, the AN/TPQ-36 radar, all utilize frequency scan.

Since 1950 much work has been done in the development of frequency-scan antennas. Most of this work has been government-sponsored, and information about it is contained in government and company reports and technical memoranda and thus is not readily available to the general public. At the present time probably the most extensive discussion on frequency-scan antennas was presented by N. A. Begovich¹; an extensive bibliography is included. Begovich et al.² and Strumwasser et al.³ are examples of patents resulting from work done in the 1950s. Other examples of early work are Dion,⁴ Spradley,⁵ Bystrom et al.,⁶ Shelton,⁷ and Ishimaru and Tuan.⁸

It is virtually impossible to come even close to an all-inclusive list of significant contributors to or references on frequency-scan antennas. For reasons of convenience and ease of access, a larger than is probably justified portion of the contents of this chapter is taken from the work done at Hughes Aircraft Company. However, it is felt that the basic concepts, designs, and practical implementation are representative of those of the industry as a whole.

19-2 THEORY OF OPERATION

The frequency-scan principle is very simple, in that it is based on the fact that the phase delay through a length of transmission line changes with frequency. For TEM lines the phase shift is directly proportional to frequency and line length. For dispersive transmission lines, it is proportional to the wave number $k_g = 2\pi/\lambda_g$ and line length. As stated before, most frequency-scan antennas fall in the category of traveling-wave antennas (see Chap. 9). For radiating elements fed serially along a transmission line, there will be a phase delay between elements. This interelement phase delay is linearly progressive and is a function of frequency. Hence, the beam will scan with frequency. A general schematic diagram of a series-fed frequency-scan antenna is shown in Fig. 9-4.

To form a beam in the direction θ_m from broadside, the following relationship must be satisfied:

$$kd\sin\theta_m = k_g s - 2m\pi \tag{19-1}$$

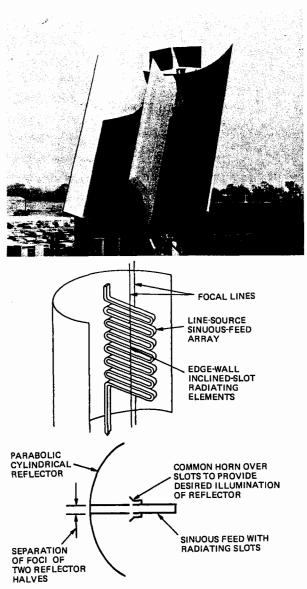


FIG. 19-1 Photograph and schematic diagram of the AN/ SPS-26 frequency-scan antenna.

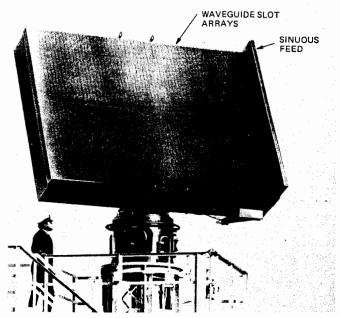


FIG. 19-2 AN/SPS-52 radar antenna.

where θ_m = angle from broadside of the beam maximum

 $k = 2\pi/\lambda$, the free-space wave number

 $k_{\rm g} = 2\pi/\lambda_{\rm g}$, the wave number for the feed line

d = distance between radiating elements

s =length of feed line between elements

m = integer (or odd half integer if the phase of the element couplers is alternately 0° and 180°)

$$\sin \theta_m = \frac{1}{kd} (k_g s - 2m\pi) \tag{19-2}$$

Let λ_{gm} be defined as the feed-line wavelength at the frequency where s is m guide wavelengths long (which also defines the corresponding wave number k_{gm} as $k_{gm}s = 2m\pi$). At these frequencies, the right side of Eq. (19-2) becomes zero and the beam is at broadside ($\theta_m = 0$). With this definition, Eq. (19-2) becomes

$$\sin \theta_m = \frac{s\lambda}{d} \left(\frac{1}{\lambda_g} - \frac{1}{\lambda_{gm}} \right)$$
 (19-3)

which is the usual form of the frequency-scan equation. The interelement phase delay $k_g s$ increases monotonically with frequency and cycles through multiples of 2π rad. This is the beam-controlling phase shift that causes a beam to scan.

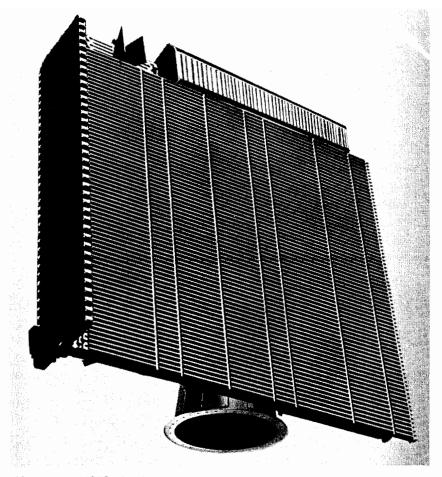


FIG. 19-3 AN/SPS-48 radar antenna.

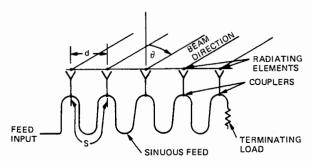


FIG. 19-4 General schematic diagram of a series-fed frequency-scan antenna.

Scan Bands

An *m*th beam can be identified with its broadside frequency corresponding to the broadside condition $k_{gm}s = 2m\pi$. By changing the frequency about its broadside frequency by an amount corresponding to one 2π interelement phase cycle, the *m*th beam will scan all space, which, depending on the element spacing, may include some invisible space as well as visible space. This frequency band is called the *m*th *scan band*. As the frequency is increased, a beam will scan from end fire toward the input end of the array, through broadside, to end fire toward the terminating load end of the array; this will be followed by another beam and another beam, etc.

Grating Lobes

As stated before, if the frequency band is great enough, there will be many beams at different frequencies, all pointing in the same direction in visible space. Similarly, if the interelement spacing d is great enough, there will be many beams in different directions in visible space, all at the same frequency. If one of these beams is the desired beam, all others are called extraneous beams, or grating lobes.

Grating lobes are caused by the fact that for widely spaced elements, as the spatial angle is changed, there will be several directions in which the radiation from all the elements will add in phase. In other words, as the spatial angle is changed monotonically, the spatial phase delay from element to element will cycle through several multiples of 2π with corresponding grating lobes, just as when frequency changes, $k_g s$ cycles through multiples of 2π with corresponding scan bands. To differentiate between the origin of multiples of 2π the subscript n will be used for grating lobes instead of m, which was used for scan bands. From Eq. (19-1), let θ_n be the direction of the nth lobe and θ_{n+1} the direction of the adjacent grating lobes which are at the same frequency (same k, same k_g). Then

$$\sin \theta_n - \sin \theta_{n+1} = \frac{\lambda}{d} \tag{19-4}$$

The beam spacing expressed in sin θ is λ/d . This is shown in the diagram of Fig. 19-5.

For only one beam to be in visible space at the same frequency requires $|\sin \theta_n| \le 1$ to ensure that θ_n is in visible space and $|\sin \theta_{n+1}| > 1$ to ensure that θ_{n+1} is not in visible space. The limit in element spacing for only one beam at a time to be in

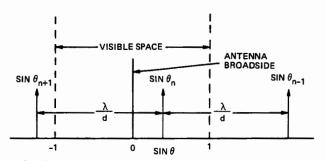


FIG. 19-5 Diagram of beam separation in $\sin \theta$.

visible space is that θ_n and θ_{n+1} are at least π rad apart ($\theta_n = \pi/2$ and $\theta_{n+1} = -\pi/2$). This leads from Eq. (19-4) to the well-known result $d \le \lambda/2$ for grating-lobe suppression over all visible space.

In practice, it is usually not necessary to scan the beam a full 180° in any plane. Owing to aperture-impedance mismatch to free space for wide-angle scan and to a further decrease in gain due to projected aperture loss, planar antennas are seldom designed to scan more than a total of 120° in one plane. Many applications require only a limited amount of scan—up to 10° or so. In these limited-scan cases, it is desirable for economic reasons to space the elements as far apart as possible without excessive performance degradation.

From the diagram of Fig. 19-5 it can be seen that as beam n (the desired beam in visible space) is scanned to the right, the grating lobe θ_{n+1} will approach visible space from the left. When the grating lobe θ_{n+1} just reaches visible space ($\theta_{n+1} = -\pi/2$), Eq. (19-4) becomes $\sin \theta_n + 1 = \lambda/d$, and if θ_{n+1} is to be kept out of visible space, $\lambda/d > 1 + \sin \theta$. The diagram of Fig. 19-5 is symmetrical in that the beam spacing is λ/d to the right or to the left, so that if the beam θ_n is scanned to the left, beam θ_{n-1} will approach visible space from the right and reach visible space for the same angle off broadside $(-\theta_n)$ of the desired beam as for scanning to the right (θ_n) . This leads to the well-known condition that

$$\frac{d}{\lambda} < \frac{1}{1 + |\sin \theta_n|} \tag{19-5}$$

for no grating lobes in visible space when the desired beam is scanned over a maximum scan range of $\pm \theta_n$ from broadside.

Since the beams are of finite width, even if the above criterion were satisfied, a portion of a grating lobe could appear in visible space although the beam peak is not in visible space. For low-sidelobe designs, this would not be desirable. Also, the aperture-impedance match to free space generally deteriorates rapidly when a grating lobe approaches free space (see Chap. 20). Therefore, it has become a rule of thumb to design the antenna so that the grating lobe is out of visible space by at least a null beamwidth (θ_{BW}) when the main beam is scanned to the maximum value. Equation (19-5) could be modified to

$$\frac{d}{\lambda} < \frac{\lambda}{1 + \sin \theta_{\rm BW} + |\sin \theta_{\rm n}|} \tag{19-6}$$

19-3 SCAN BANDS AND MULTIPLE BEAMS

The greatest disadvantage of simple frequency scan is that the entire available bandwidth is used to steer the beam and that each direction in space is associated with a definite frequency. This allows a jammer to concentrate its energy over a narrow frequency band. The simple frequency scan also limits the instantaneous bandwidth of the system. The jammer problem could, in principle, be somewhat alleviated by employing more than one scan band, so that each direction in space would have as many frequencies as scan bands. This can be done by extending the tunable bandwidth of the system to include other scan bands or by lengthening the interelement feed-line

lengths sufficiently so that there are multiple scan bands in the same nominal frequency band. These methods are not practical because extending the tunable bandwidth enough to cover several scan bands requires broadband components such as very-wide-bandwidth transmitters, receivers, and antenna components such as couplers and slot radiators.

By increasing the feed-line length s, the instantaneous bandwidth is severely restricted because the beam-scan rate with frequency is increased to a point at which not all the antenna beams corresponding to the different frequency components in a short pulse will point in the same direction. That is, the antenna beam pattern is "smeared out" in angular space, thereby broadening the effective beamwidth of the antenna and reducing its gain and angular resolution. The antenna is a narrow bandpass filter in that the frequency spectrum of the pulse radiated toward a target is modified from the spectrum entering the antenna. The spectrum is narrowed by the weighting applied to the various frequency components by their corresponding frequency-scanned beams. The frequency component corresponding to the beam scanned in the direction of the target is most heavily weighted, and each of the other frequency components is reduced (in the direction of the target) by the amount by which its antenna pattern is scanned off from the direction of the target.

On receive, the spectrum of the reflected pulse from the target is further modified in the antenna by the same transformation. There is a loss in gain, and consequently in radar range, because of the smearing out of the antenna pattern or, alternatively, because of the loss in power contained in the spectral components filtered out by the antenna. The power in the filtered-out frequency components is either reflected back into space or absorbed in the various terminating loads in the antenna. The modifying of the frequency spectrum results in the pulse being smeared out in time; thus range accuracy and range resolution are reduced. These and transient effects are discussed by Bailin, P Enenstein, 10 and Begovich. 1

A more practical method for achieving greater frequency agility, due to E. C. DuFort and R. F. Hyneman,* combines the features of scan bands with the features of grating lobes so that any of several grating lobes can be selected as the desired beam while suppressing all others. This method uses a multiple-beam-forming network in conjunction with multiple interleaved arrays. This scheme has been practically implemented for two beams in the Hughes AN/SPS-33 shipborne radar antenna. The number of beams is equal to the number of interleaved arrays. Figure 19-6a shows an example of four interleaved arrays. The theory of this technique is described in the following paragraphs.

Suppose that there are q interleaved arrays, so that the spacing between radiating elements in the composite array is d but the spacing between elements fed by any one of the interleaved feed lines is qd. In the example of Figure 19-6a, q=4. The spacing d is chosen so that the composite array does not have extraneous beams. However, each of the individual arrays with elements spaced qd will have q beams or grating lobes in the visible region of space corresponding to q values of n in Eq. (19-4). Now the entire composite array can be considered as a q-element array with the component arrays as the elements. In the example, q=4. It is a four-element array of component arrays. The elements of the component arrays are marked by 1s for the first array, 2s for the second array, etc. The antenna pattern of the whole composite

^{*}Private communication (1960) with E. C. DuFort. Both DuFort and Hyneman are with the Hughes Aircraft Company, Ground Systems Group, Fullerton, Calif.

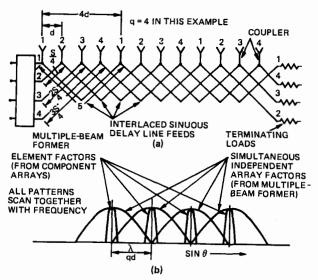


FIG. 19-6 Multiple beams and interleaved scan bands.

array is a product of the *element factor*, which is the pattern of a single-component array (each with q beams) and an array factor which is a pattern of q point sources spaced d apart.

Refer to Fig. 19-6b. This array factor (the broad pattern) picks out the desired beam while suppressing all the others. The maximum of the array factor coincides with that of the desired beam and has nulls at the peaks of all the other beams. This can be seen by applying Eq. (19-1) first to the element factor and then to the array factor. For the element factor which has element spacing qd, Eq. (19-1) becomes

or
$$kqd \sin \theta_m = k_g s - m2\pi$$

$$kd \sin \theta_m = k_g \frac{s}{q} - \frac{m}{q} 2\pi$$

and for the array factor which has element spacing d, Eq. (19-1) becomes

$$kd\sin\theta_m = k_g s' - m'2\pi \tag{19-8}$$

For the element factor and the array factor to frequency-scan together, it is required that s', the incremental line length between linear arrays, be equal to s/q, and this also makes m' = m/q. Now the array factor whose element spacing is d has only one beam in visible space, while the element factor has q beams or grating lobes corresponding to q values of n in Eq. (19-4). By superposing the proper linear progressive phase to the array factor, the array factor could be superposed exactly on any one of the grating lobes corresponding to a particular value of n in Eq. (19-4). This would pick out that beam and suppress all others. If an additional linear phase of $[2\pi(q-1)]/q$ over the array aperture were provided, the array factor would then pick out the beam corresponding to n+1, etc., up to n=q.

An orthogonal beam-forming network such as a Butler matrix will supply all the proper phase gradients simultaneously. That is, each beam port of the multiple beam former will pick out its corresponding beam, and the frequency range to scan that beam over all space may be called the *corresponding scan band*. To do this requires that the array factor beams be separated by the same amount as the grating lobes (which is λ/qd in $\sin\theta$ space) and also that there be nulls at the peaks of all the other grating lobes. This condition is automatically satisfied by an orthogonal beam-forming network (see Chap. 20). An optical-type multiple-beam former (multiple-beam reflector or lens) would not satisfy the beam-spacing criterion for all frequencies because the beam spacing would be independent of frequency.

In the preceding paragraph the frequency range to scan a beam over all space was referred to as a scan band corresponding to that beam. It should be noted that these scan bands overlap or are interleaved, so that the total frequency range to make full use of all the scan bands is only (1 + 1/q) times as great as for the simple single-scan-band case first discussed. This requirement contrasts with the q times as much bandwidth required for multiple scan bands using frequency extension. Also, the instantaneous bandwidth is decreased at most by a factor of q/(q + 1) as compared with 1/q for multiple scan bands using a longer interelement feedline of length qs.

Because of the factor s/q and m/q in Eq. (19-7), the term fractional scan bands has been suggested. However, the term overlapped or interleaved scan bands is probably more descriptive because it is related to the interleaved or overlapped array structure and, also, if a scan-band diagram of $\sin \theta$ versus frequency were plotted, the scan bands would be seen to overlap.

19-4 MONOPULSE IN THE FREQUENCY-SCAN PLANE

For greater angular accuracy in tracking radars, monopulse antennas have long been employed. However, they have not been used extensively in frequency-scan antennas, probably because subpulse beam switching is easily implemented and is adequate for most applications. In subpulse beam switching, a single pulse is divided into two parts different in frequency by a small amount so that the two beams corresponding to the two frequencies overlap. Amplitude comparison between the two beams is used for improved angular accuracy. Although in principle monopulse can be implemented in the frequency-scan plane, there is an inherent physical asymmetry in end-fed traveling-wave arrays, which include the simplest series-fed frequency-scan antennas. The practical implications of the asymmetry of series-fed arrays will be discussed later. Some representative monopulse schemes are described in the following paragraphs.

Parallel-Fed Monopulse Array

Figure 19-7 shows a parallel-fed frequency-scan array fed by a conventional monopulse feed. While schematically this is quite simple and straightforward, it has the disadvantages of complexity and cost. Also, the feed-line attenuation varies from element to element owing to the different lengths of delay line. This circumstance must, of course, be taken into account in the design of the feed network to achieve the desired aperture distributions for the sum and difference modes. However, because of its

inherently greater symmetry, this configuration may be the preferred design for applications in which an extremely high degree of monopulse tracking accuracy is required.

Tandem-Fed Monopulse Array

Figure 19-8 depicts a tandem-sinuous-feed technique for monopulse in the frequencyscan plane. This technique can generate two beams as in a Blass network with two frequency-scan sinuous delay lines in tandem as shown. The beam squint between the monopulse beams can be achieved by employing a progressive phase shift in the lines

between the tandem feeds or by making the interelement delay line length Sslightly different for the two sinuous feeds. Alternatively, one feed may be designed for the monopulse sum and the other for the monopulse difference. As a whole, the two feeds do not couple owing to the orthogonality of even and odd distributions corresponding to the sum and difference modes. The end feeding destroys the physical symmetry that is inherent in center feeding. Symmetry is desirable for the monopulse difference operation to achieve a purely odd difference distribution with the resulting deep, distinct null in the difference pattern.

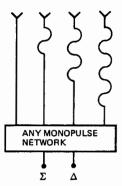


FIG. 19-7 Parallel-fed frequency-scan monopulse antenna.

Dummy-Snake Monopulse Technique

To illustrate some of the severe problems due to the symmetry of serially fed antennas for monopulse operation, a dummy-snake monopulse technique will be described.

With reference to Fig. 19-9, the array halves will be arbitrarily designated as first half and second half. The array halves must, of course, have the same feed design

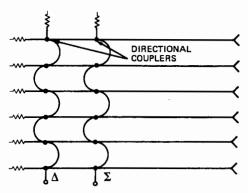


FIG. 19-8 Tandem-fed frequency-scan monopulse antenna.

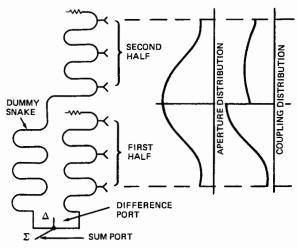


FIG. 19-9 Dummy-snake frequency-scan monopulse antenna.

so that they frequency-scan synchronously. In addition, for monopulse application they must accurately phase-track as the frequency is changed. To accomplish this, a dummy snake must be added to the second half as shown in the figure. The dummy snake must have the same phase delay as the antenna feed.

There are certain practical difficulties in using this method. First, the dummy snake must have the identical phase versus frequency characteristics of the feed in the first half. A sinuous feed loaded by radiating elements does not have exactly the same phase versus frequency characteristics as an unloaded line, and care must be exercised to design the dummy snake properly so that it will accurately phase-track the feed of the first array. A more difficult problem lies in the design of the aperture distributions of the two halves. It is apparent that the coupling distributions of the two halves must be radically different, especially for tapered-aperture distributions.

For the first half, the coupling of the first element must be very low because here the *aperture* distribution is lowest and the power in the feed line is highest, and the coupling must be nearly unity at the end of the first half because here the aperture distribution is highest and the power in the feed line is lowest. For the second half, the first element requires the highest power at the point where the power in the feed line is also highest. For a tapered-aperture distribution the conductance distribution in the second half is more nearly uniform because of the natural taper due to the attenuation caused by radiation and ohmic loss.

The general nature of the aperture and coupling distributions is shown in Fig. 19-9. Because of the widely differing conductance distributions of the two halves, it is difficult to maintain the desired symmetry of the aperture distribution of the halves for good monopulse operation. The efficiency of the two halves may also be difficult to match. Because of the difficult to keep equal over a broad frequency range. It would require a very high range of coupling values, i.e., a very low value at the input end of the first half and a very high value at the output of the first half. Another disadvantage is that independent sum and difference aperture distributions are not possible. That

is, if the sum distribution is optimized for low sidelobes, the difference patterns will have a step discontinuity at the center, resulting in a high sidelobe difference pattern.

19-5 PRACTICAL FREQUENCY-SCAN ANTENNAS

Frequency-scan antennas, like other antenna systems, can take many forms. In the frequency-scan plane, the feeding structure uses sinuous delay lines, but for pencil beams, beam collimation in the orthogonal plane can use linear arrays, reflectors, lenses, multiple-beam structures, etc. Figure 19-1 shows the AN/SPS-26 radar antenna, which is a waveguide sinuous-feed slot array feeding a parabolic cylindrical reflector. Figure 19-2 shows the AN/SPS-52 radar antenna, which is a waveguide sinuous feed feeding an array of traveling-wave slot arrays (a schematic diagram is given later in Fig. 19-12). Antennas that frequency-scan in one plane with multiple simultaneous beams in the other plane can be implemented by using stacks of planar multiple-beam antennas with multiple sinuous feeds. The multiple-beam structure can be a stack of multiple-beam lenses such as parallel-plate dielectric or geodesic lenses, constrained lenses, or any multiple-beam-forming network.

The AN/SPS-33 radar antenna is a good example of a practical phase-frequency-scan antenna with dual scan bands. A schematic diagram of the antenna is shown in Fig. 19-10.

The feed in the phase-scan plane is a folded pillbox¹¹ with monopulse capability. A folded pillbox is a two-layer parallel-plate power divider operating in the TEM

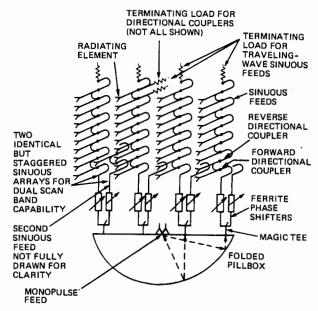


FIG. 19-10 Schematic diagram of a phase-frequency-scan antenna with dual scan bands.

mode, with a monopulse feed in the feed layer of the pillbox and the exit or aperture in the other layer of the pillbox. The two layers are separated by a common plate septum and joined by a 180° E-plane bend that has a parabolic contour in the plane of the plates. This feed has a very low loss (typically, a few tenths of a decibel for a 1° aperture) and can handle 2 MW peak and 4 kW average without pressurization at S band.

With simple open-ended waveguide or cavity-type feeds the aperture illumination for sidelobe levels below -30 dB is easily achieved over more than a 10 percent bandwidth. The output of the pillbox has a stepped transformer in parallel plate to effect an impedance match from the parallel-plate region of the pillbox to an array of waveguides in the H plane. Each of these output waveguides is power-split 1 to 2 by an H-plane folded magic (hydrid) T. Each of the outputs from a magic T feeds a high-power ferrite phase shifter, which, in turn, feeds two interleaved sinuous feeds that feed the open-ended-waveguide radiating elements via directional couplers. The two interleaved sinuous feeds provide the two-scan-band capability.

The desired scan band can be chosen by the relative phasing between adjacent ferrite phase shifters. If adjacent phase shifters are in phase (except for the linear progressive phase for phase-scanning the beam), one scan band is picked out, and if the adjacent phase shifters are alternately phased 0° and 180°, the other scan band is picked out. It should be noted that the interleaved sinuous feeds are not physically interleaved but are displaced in the plane orthogonal to the frequency-scan plane. For a large array of sinuous feeds, this lateral displacement is inconsequential. In fact, it is an advantage because the resultant array element lattice becomes triangular, which reduces the number of radiating elements required for the same volume of beam coverage compared with a rectangular lattice. ^{13,14}

Figure 19-11 is an isometric drawing of a section of the sinuous feed. The sinuous

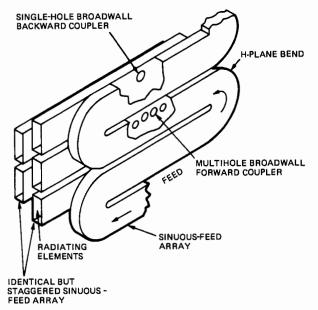


FIG. 19-11 Staggered sinuous feeds for dual scan bands.

feed is a waveguide of reduced height feeding open-ended-waveguide radiating elements with directional couplers in the broad walls of the waveguides. Both forward and reverse couplers are required. The forward couplers are multihole couplers, and the backward couplers are single Bethe hole couplers with a capacitive button on the wall opposite the hole to improve directivity. The coupling coefficients are controlled by the hole sizes. In each straight section of waveguide between the coupling holes and the radiating apertures, there is an array of capacitive buttons which correct a small amount of phase that is a function of the coupling coefficient. These designs gave essentially constant coupling in amplitude and phase over greater than a 10 percent frequency range at S band.

The monopulse feed to the folded pillbox is a multimode single-aperture feed which is fed by the two waveguide outputs of a folded H-plane magic T. The common multimode aperture is dielectrically loaded with a solid dielectric plug. The dielectric plug fulfills the dual purpose of providing one of the parameters for controlling the relative mode amplitudes and phases of the multimode aperture and of serving as a pressure seal. The pillbox itself is not pressurized. The pillbox illumination from the feed is such as to result in better than -32-dB sum-pattern sidelobes in the phase-scan plane of the antenna and -20-dB sidelobes for the difference patterns.

19-6 DESIGN CONSIDERATIONS

To illustrate some of the problems associated with frequency-scan-antenna design, an antenna of the design generally depicted in Fig. 19-12 will be discussed. This is a two-dimensional planar pencil-beam antenna that is designed to frequency-scan primarily in one plane, say, the elevation plane, with mechanical rotation for azimuth coverage. Such a design basically comprises a sinuous delay line with numerous 180° bends, couplers from the sinuous feed to branch lines, and linear arrays that collimate the beam in the plane orthogonally to the sinuous feed. Each of these parts and their effect on antenna performance are discussed in turn.

Sinuous Feed

The sinuous delay line must produce a large amount of interelement phase delay with a minimum of ohmic loss and be able to handle high power. For frequencies at and above S band, a rectangular waveguide operating in the dominant TE₁₀ mode is the usual choice. At lower frequencies, in which the waveguide is too large and cumbersome, a large coaxial line operating in the TEM mode is used for high-power application. For low-power application, stripline or microstrip might be appropriate. The frequency-scan antenna for the AN/SPS-32 long-range search radar, operating in the 200-MHz band, uses 3%-in dielectric bead-supported coaxial line for the delay line to achieve minimum loss and high-power capability. For purposes of discussion, the waveguide sinuous feed will be used.

Bends

For compactness and a low voltage standing-wave ratio (VSWR), waveguide sinuous feeds wrapped in the E plane with 180° E-plane bends are most often used, and 180° E-plane circular bends with small inductive irises or posts having a VSWR less than

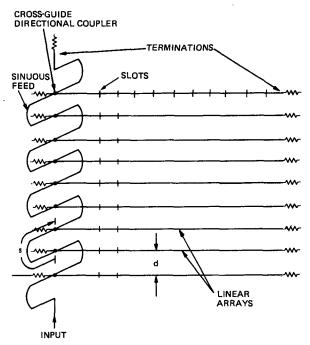


FIG. 19-12 Frequency-scanning sinuous feed feeding an array of traveling-wave linear arrays.

1.03 over a 10 percent frequency band are commercially available in most standard waveguide bands. As will be discussed later, at the frequency in which the beam is at broadside the bend VSWR should be less than 1.02:1 to produce an input VSWR on the order of 1.5:1 in a typical feed design. For the lower frequencies in which coaxial line is used, the 180° bends are made up of two well-matched 90° bends that are spaced $\lambda/4$ apart at the broadside frequency so that their reflections cancel.

Couplers

There are a number of choices for couplers from the sinuous delay line to the branch lines. The couplers can be nondirective three-port reactive couplers such as pure series or pure shunt couplers, nondirective matched couplers, or directional four-port couplers. Nondirective couplers are simple and inexpensive to fabricate. Two typical designs of nondirective waveguide shunt couplers are shown in Figs. 19-13 and 19-14. Figure 19-13 shows resonant inclined slots in the narrow dimension of the sinuous-feed waveguide which couple to the branch waveguides. The degree of coupling is controlled by the angle of slot inclination. Figure 19-14 shows nonresonant longitudinal slots in the narrow wall of the sinuous-feed waveguide which couple to the branch waveguides. An inductive iris or post is used to resonate the coupler. The degree of coupling is controlled by the length of the nonresonant slot. Figure 19-15 shows offset shunt slots in the bends of the sinuous feed.

The slot serves the dual purpose of coupler and radiating element. The degree of

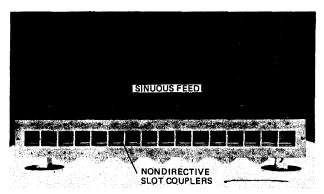


FIG. 19-13 Waveguide sinuous feed with reactive nondirective inclined-slot couplers to branch guides.

coupling is determined by the lateral offset of the slot from the centerline of the bend. Simple series or shunt couplers are inexpensive to fabricate, but they have very poor performance at or very near broadside frequencies. At broadside frequencies, the couplers are an integral number of half-guide wavelengths apart so that for shunt couplers the admittances are all in parallel and for series couplers the impedances are all in series. As a result, there is a high input VSWR, and the antenna power aperture distribution is equal to the admittance or impedance distribution, which for efficient arrays is quite asymmetrical. The smaller the power dissipated in the terminating load of the feed, the greater the asymmetry. This asymmetrical distribution has a large odd component which does not contribute to antenna gain but causes increased side-lobes and null filling.

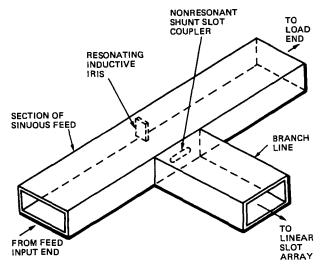


FIG. 19-14 Section of waveguide sinuous feed with nondirective, nonresonant shunt-slot couplers to branch guides.

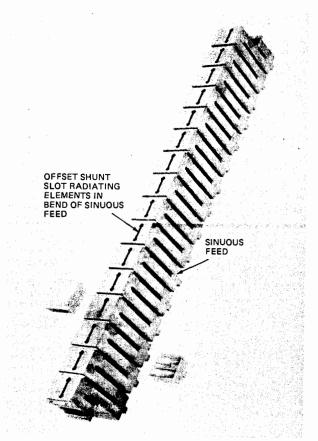


FIG. 19-15 Waveguide sinuous feed with offset shunt-slot radiators.

The curve of input VSWR versus frequency has a sharp peak at resonance and is generally low elsewhere, with only small minor lobes. It has an obvious analogy to an antenna pattern in which the independent variable is spatial angle instead of frequency. For tapered antenna distributions, the main beam broadens and the sidelobes decrease with the degree of tapering. Likewise, for tapered coupling distributions, the VSWR resonance curve broadens and the VSWR sidelobes decrease with the degree of tapering. Also, the larger the aperture distribution, the narrower the antenna beam, and the longer the feed line, the narrower the resonance curve.

Because of these resonance effects, the sinuous-feed bends and couplers must have extremely low reflections; otherwise operation at or near resonance is precluded. However, in many radar applications, beam scan through broadside is required, and the VSWR must be kept to a tolerable low level, on the order of 1.5:1 or less.

To allow operation at broadside frequencies, Kurtz and Gustafson¹⁵ investigated the possibility of impedance-matching nondirective couplers as seen from the feed end of the coupler. This technique resulted in considerable success. The coupler used was

a shunt coupler of the design shown in Fig. 19-14. The admittance in the main line at a resonant coupler is 1 + g, where g is the coupler conductance which is small compared to 1. It is clearly seen on a Smith chart that going toward the generator slightly under λ_g , the unit conductance circle is intercepted with a small capacitive susceptance approximately equal in magnitude to the coupler conductance g. This small capacitive susceptance is canceled by a thin inductive post near the wall opposite the coupler. The λ_g spacing is far enough from the coupling aperture that the coupler conductance is not affected. By this matching technique an intolerably high VSWR at the resonant frequenty was reduced to less than 1.4:1.

Without matched couplers, an antenna pattern taken slightly off the resonant frequency when reflections are still quite high produces a reflected lobe that interferes with the main antenna beam to cause severe pattern degradation. The reflected lobe occurs at an angle symmetrically opposite from broadside with respect to the main beam. Since the frequency is close to the resonant frequency, the reflection beam and the main beam overlap so as to interfere with each other, causing an asymmetrical pattern with a split-beam appearance. After the couplers have been matched, this effect virtually disappears.

For extremely low (-30-dB or lower) sidelobe designs, directional couplers with the isolated ports of the couplers terminated in well-matched loads are preferred because spurious reflections in the sinuous feed, regardless of their origin, will be absorbed in the terminating loads of the couplers and will not radiate into space to degrade the antenna pattern. A directional coupler is a four-port junction that is inherently matched in all ports. Figure 19-16 shows a typical directional coupler in a section of a sinuous feed. The first-order reflected power in the sinuous feed will split; some of it will go into the terminating load of the directional coupler, and the rest will continue back down the feed line with part of that going into the terminating load of the preceding directional coupler, etc., so that in general very little reflected power gets back to the feed input to affect the input VSWR appreciably. Because of the directivity of the directional coupler none of this first-order reflection is radiated. Also, broadband directional-coupler designs with a wide range of coupling values are readily available. As an example, the design of a waveguide sinuous feed using cross-slot-cross-guide couplers is discussed. An isometric view of a waveguide sinuous feed using

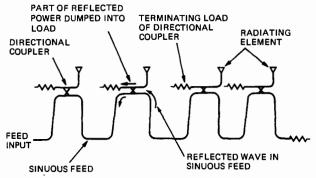


FIG. 19-16 Schematic diagram of a sinuous feed using directional couplers.

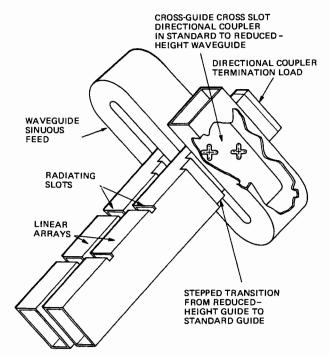


FIG. 19-17 Waveguide sinuous feed with cross-slot-cross-guide directional couplers feeding waveguide slot arrays.

cross-slot-cross-guide directional couplers is shown in Fig. 19-17. Figure 19-18 gives the coupling coefficient versus cross-slot parameters.

Couplers, in general, introduce phase shift in the main line past the coupler and in the coupled branch lines. Figure 19-19 gives phase shift past the coupler and phase shift in the branch lines as a function of coupling coefficient for a cross-slot-crossguide directional coupler. The coupling is from standard WR-384 S-band waveguide to a reduced-height guide of the same width. This design was shown in Fig. 19-17. In this coupler, the phase shifts in the main and the coupled arms are phase delays that vary monotonically with the degree of coupling. Both phase shifts can be compensated for by shortening the interelement line length S in the sinuous feed accordingly. The phase correction in the sinuous feed has an additional benefit in that it breaks up the exact periodicity in the locations of the 180° bends in the sinuous feed and thereby improves the VSWR of the sinuous feed at and near the broadside frequency. To see the effect of bend mismatch on the input VSWR, calculations were made for a 60element sinuous feed using cross-slot-cross-guide directional couplers designed for a -30-dB-sidelobe ($\overline{n} = 4$) Taylor distribution for various VSWR values of an individual bend. Coupler phase compensation was included in the calculations. The results showed that to achieve an input VSWR less than 1.5:1 at the resonant frequency required a bend VSWR of less than 1.02:1. This is easily achieved with standard waveguide bend designs. For frequencies off resonance the bend VSWR can be as high as 1.3:1 and still maintain a feed input VSWR of less than 1.5:1.

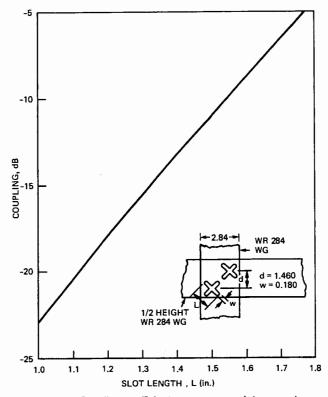


FIG. 19-18 Coupling coefficient versus cross-slot parameters.

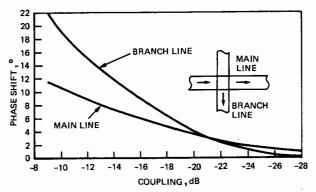


FIG. 19-19 Phase shifts of cross-slot-cross-guide directional couplers.

Linear Array

To collimate the beam in the plane orthogonal to the plane of the sinuous feed, waveguide linear slot arrays were used. The rod-excited, polarization-pure slot elements used noninclined transverse slots in the narrow wall of the waveguide. Ordinarily these slots do not radiate because they are parallel to the radio-frequency current in the wall of the waveguide. The slots are excited by thin rods or wires inside the waveguide as shown in Fig. 19-20. Metallic irises have also been used to excite waveguide slots that otherwise do not radiate. If, Is Iris techniques for narrow-wall slots were investigated but were not used in this application because of the high cost of fabrication and because of the high power arcing at the irises. The rod-excited design was tested to 40-kW peak and 1-kW average power in WR-284 S-band waveguide without pressurization.

For highly efficient very-low-sidelobe designs, this technique has a decided advantage over the more conventional inclined slot because it introduces no cross-polarization. For inclined slots there is a cross-polarized component proportional to the tangent of the inclination angle. This results in cross-polarization lobes in the antenna pattern. Since most two-dimensional slot arrays are designed so that the cross-polarization of adjacent elements and the cross-polarization of adjacent arrays cancel on the principal planes, the cross-polarization lobes occur in the off-principal planes. These relatively high cross-polarization lobes defeat the objective of very-low-sidelobe designs. Also, the more efficient the array, the larger the cross-polarization. The reason for this is that for lower power dissipation in the terminating load (and thus higher efficiency), higher conductance values are required, 4.19 which means greater slot inclination and hence greater cross-polarization.

To suppress this cross-polarization, closely spaced metallic strips or baffles that are perpendicular to the electric field of the principal polarization are used. The spacing between the baffles is much less than a half wavelength, so the baffles form waveguide regions that are below cutoff to the cross-polarization. The AN/SPS-52 radar antenna shown in Fig. 19-2 uses the cross-polarization-suppressing baffles shown in Fig. 19-21. These baffles add considerable weight and cost to the antenna. For these reasons, the polarization-pure transverse rod-excited slots in the narrow wall of the waveguide are used to design a -40-dB-sidelobe array.

Refer to Fig. 19-20. The degree of coupling of the rod-excited transverse slot is controlled by the distances of the ends of the rods from the inside corner of the wave-

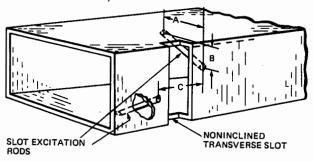


FIG. 19-20 Rod-excited transverse slot in narrow wall of waveguide.

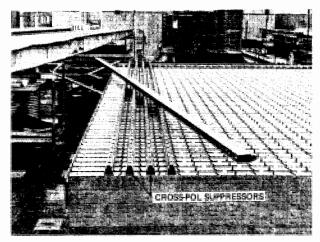


FIG. 19-21 Inclined-slot arrays with cross-polarization-suppressing baffles.

guide adjacent to the slot as shown in the figure. The rods couple the slot to the electromagnetic wave in the waveguide. The rods are tilted so that they have a component of electric field from the TE_{10} mode in the waveguide that is parallel to the rods but in opposite directions for the upper and lower rods. Thus the rods act like a two-wire transmission line feeding the slot.

The coupling to the slot increases with an increase in the dimension A or B, or both. The slot coupling is also affected by the spacing C between the two rods. The coupling decreases with an increase in C. This dimension C is held constant at a convenient value of about $\lambda_g/8$ with the slot centered so that reflections from the wires tend to cancel. For convenience and ease of data taking, the dimension A is held constant, leaving B the only variable. With A held constant at 1.45 in (36.83 mm), a wide range of coupling can be achieved. For arrays with a large number of elements, the maximum coupling value can be kept under 0.1 with 5 percent of the power dissipated into the terminating load.

Figure 19-22 gives the slot-coupling coefficient versus the B dimension of Fig. 19-20. There are two curves, the dotted curve showing initial values and the solid curve the final values after an iterative design procedure to be explained later. The slot structure including the rods is made resonant at the design frequency by adjusting the overall length of the slots—in this case, the amount of slot cut back into the broad wall. This resonant (zero-phase-shift) condition depends on the slot coupling. Figure 19-23 gives slot coupling and slot cutback versus slot position in the array.

The design of a two-dimensional antenna aperture composed of an array of linear traveling-wave arrays is, in general, quite complex. The aperture must be impedance-matched to free space over a wide frequency band and over a wide range of scan angles. Aperture matching of phased arrays has received a great deal of attention both analytically and experimentally since the early 1960s. (See Chap. 20 of this handbook for detailed discussions and references.) Two-dimensional traveling-wave slot arrays are particularly difficult to analyze for the following reasons: (1) The feeding network,

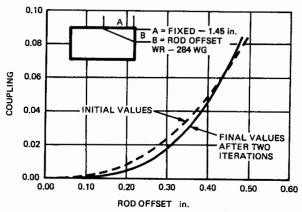


FIG. 19-22 Slot coupling versus rod offset for rod-excited transverse slot in narrow wall.

the element couplers, and the radiating elements cannot be treated separately because they often share a common physical and functional structure. For waveguide slot arrays, the waveguide with its slots is the feed network, and the slots serve the dual function of coupler and radiating element. (2) Owing to the serial feeding, there is a cumulative effect, in that errors in preceding elements affect the performance of succeeding elements. This has a great effect on aperture distribution and results in the loss of power into the terminating loads.

As with all phased-array apertures, for good impedance match to space mutual coupling between elements must be taken into account. There is mutual coupling between the elements exterior to the slots and also coupling interior to the waveguide. There is also strong mutual coupling between linear arrays that is a function of the scan angle, which, of course, for frequency scan is also a function of frequency. This

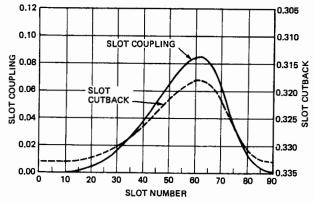


FIG. 19-23 Slot cutback and slot coupling versus slot number for -50-dB Taylor $\overline{N}=8$ aperture distribution.

mutual coupling affects the coupling coefficients of each slot so that the aperture distribution and power lost in the terminating loads can be drastically different from the intended design if the mutual-coupling effects are not properly taken into account. This has been dramatically verified by taking a linear slot array that has very good performance by itself and arraying two such arrays, three such arrays, etc. It has been found that the measured aperture distributions, radiation patterns, and power lost in the termination, in general, vary widely from each other. It has been found that after five or more linear arrays have been arrayed, the aperture distribution and percent power into the loads become nearly constant. This has led to the conclusion that at least five linear arrays are required to approximate the environment of a large array.

Because of these problems and the difficulty of a priori prediction of performance for extremely-low-sidelobe designs, a semiempirical iterative design procedure was developed at Hughes Aircraft Company, Ground Systems Group, Fullerton, California. An outline of this procedure is given by an example of a -40-dB-sidelobe-level design that meets all MIL specification requirements and is fabricated by using production personnel and production methods. The rod-excited, polarization-pure slot array was used.

The design goal:

41-dB gain
-40-dB sidelobes
2° × 1° beamwidth
15 percent bandwidth at S band

Design parameters:

Taylor -50-dB $\overline{n} = 8$ aperture distribution 90 slots in linear arrays 98 linear arrays 15- by 20-ft overall aperture

Design Procedure

- 1 Design a linear array by standard techniques such as that due to V. T. Norwood. 19
 In this example, slot data have been scaled from a previous design at a slightly different frequency band using standard WR284 S-band waveguide. The new design used thin-wall WR284 waveguide. Even approximately good slot data can be used as a starting point.
- 2 Fabricate a minimum of five linear arrays to make a small array, using any convenient feed which allows the required radio-frequency measurements.
- 3 Using a near-field probe facility,²⁰ measure the amplitude and phase along the slots of each linear array over the desired frequency range and over the desired scan angles. Measure the input power and the power into the terminating load. If the basic design concept is reasonably sound, data measured over frequency ranges and scan angles should not be widely different. Array spacing and radome

thickness and spacing from the slot aperture can be used to minimize the sensitivity to frequency and scan angle. From the measured input power, aperture distribution, and power into the load, the *actual* slot coupling and phase data of each slot in the very nearly actual environment, including all mutual-coupling effects, can be determined. Various weighted averages over frequency and scan angle can be constructed, depending on the system-performance weighting. For example, the best performance at the scan angle corresponding to the horizon scan may be more heavily weighted.

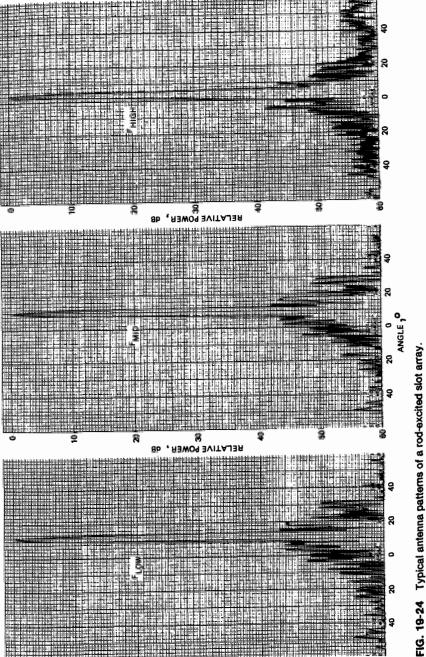
- 4 These new coupling data take into account all mutual-coupling effects in the actual array environment and encompass the entire range of coupling values required. A new and more accurate curve of coupling coefficient and phase versus the B dimension can be constructed for various frequencies and scan angles. By using these new data, a new set of at least five linear arrays is constructed and tested with the near-field setup, and another set of slot data is collected.
- 5 The process is repeated until the desired result is obtained. It has been found that two iterations are sufficient to converge to the optimum design. In this example, —40-dB-maximum sidelobes with 5 percent or less power dissipated in the terminating loads were actually achieved over a 12 percent frequency range in several production antennas. Figure 19-24 presents typical patterns over the frequency range. All the design goals were met with two iterations.

This near-field technique can also be used in the design of modifications to the antenna that might greatly alter the slot coupling. Modification to the aperture for fragmentation protection is an example.

19-7 MILLIMETER-WAVE APPLICATION

Electronic beam scanning using phase shifters for millimeter waves has not been practical because of the extreme difficulty in fabricating the phase shifters. In principle, ferrite phase shifters are feasible for millimeter waves, but the small size and the extremely high tolerance requirements make them impractical. However, because of their simplicity, frequency-scan antennas are practical for millimeter-wave application.

Frequency-scanning waveguide slot arrays at 60 GHz have been developed at Hughes Aircraft Company. These arrays use slot design data scaled from the X-band frequency range. Figure 19-25 shows an edge-wall inclined-slot array with cross-polarization-suppressing cavities to give longitudinal polarization. Figure 19-26 shows a broad-wall offset slot array for transverse polarization. Borowick, Bayka, Stern, and Babbit of the U.S. Army Electronics Research and Development Command, Fort Monmouth, New Jersey, have developed a frequency-scan linear array in dielectric waveguide operating in the HE₁₁ mode at 35 GHz. Slots cut in the dielectric waveguide perturb the guided wave to cause radiation, and the slots become the radiating elements. Since this design does not allow phase reversal, the slots are spaced one guide wavelength apart at the frequency corresponding to the broadside scan angle. However, because of the high-dielectric-constant material used in the dielectric waveguide, the guide wavelength is less than a free-space half wavelength, and there are



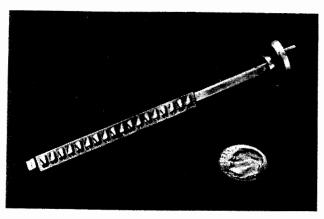


FIG. 19-25 60-GHz frequency-scan narrow-wall inclined-slot array for longitudinal polarization with cross-polarization-suppressing cavities.

no grating lobes even with the λ_g spacing. Figure 19-27 shows the geometry of the dielectric-waveguide slot array. Dielectric waveguides using metallic strips instead of slots have also been used as frequency-scanning arrays.^{22,23}

Both the metallic-waveguide slot arrays and the dielectric-waveguide slot and metal-strip arrays are very simple in structure, are easily fabricated, and perform very well. For greater scan versus frequency, the metal-waveguide slot array can be put in the form of a sinuous feed. This may be somewhat more difficult with the dielectric array because of the problem at the bends. However, this may not be necessary for many applications because the scan versus frequency is enhanced by the square root of the dielectric constant.

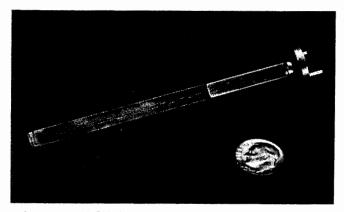


FIG. 19-26 60-GHz frequency-scan broad-wall offset slot array for transverse polarization.

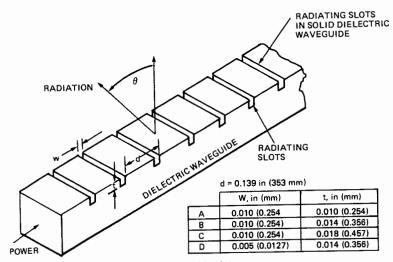


FIG. 19-27 35-GHz dielectric-waveguide slot array.

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Phased Arrays

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20-1	Introduction 20-2 Basic Concept of Phased Arrays 20-2 Advantages of Phased Arrays 20-2 Overview of the Chapter 20-2
20-2	Theory of Phased Arrays 20-3 Radiation Pattern of Linear Arrays 20-3 Element Spacing to Avoid Grating Lobes 20-6
	Amplitude Tapers for Sidelobe Control 20-6 Array-Pattern Directivity of Linear Arrays 20-12
	Radiation Pattern of Planar Arrays 20-15 Element Spacing and Lattice of Planar Arrays 20-17
	Amplitude Taper for Planar Arrays 20-21 Array Directivity and Gain of Planar Arrays 20-22
20-3	Active-Element Pattern 20-26 Design Criteria for Radiators 20-28
20-4	Development Procedure for Radiators 20-30 Selection of Phase Shifters for Phased Arrays 20-31 Selection Criteria 20-31
	Ferrite Phase Shifters 20-32 Semiconductor-Diode Phase Shifters 20-36 Performance Characteristics 20-44
20-5	Feed-Network Design for Phased Arrays Optical Space Feeds 20-49 Constrained Feeds 20-51
20-6	Bandwidth of Phased Arrays 20-60 Phase-Shifter Effects 20-60 Feed Effects 20-62

20-1 INTRODUCTION

In this chapter, the theoretical and practical considerations involved in the design of phased-array antennas are given. The intent is to provide the antenna designer with an overview of the basic design concepts of phased arrays and the means to determine the proper antenna parameters for a given radar application.

Basic Concept of Phased Arrays

Basically, the phased-array antenna is composed of a group of individual radiators which are distributed and oriented in a linear or two-dimensional spatial configuration. The amplitude and phase excitations of each radiator can be individually controlled to form a radiated beam of any desired shape (directive pencil-beam or fan-beam shape) in space. The position of the beam in space is controlled electronically by adjusting the phase of the excitation signals at the individual radiators. Hence, beam scanning is accomplished with the antenna aperture remaining fixed in space without the involvement of mechanical motion in the scanning process; in other words, this is inertialess scanning.

Advantages of Phased Arrays

The capability of rapid and accurate beam scanning in microseconds permits the radar to perform multiple functions either interlaced in time or simultaneously. An electronically steered array radar is able to track a large number of targets and illuminate some of these targets with radio-frequency (RF) energy and guide missiles toward them. It can perform complete hemispherical search with automatic target selection and hand over to tracking. It may even act as a communication system, directing highgain beams toward distant receivers and transmitters. Complete flexibility is possible. Search and track rates may be adjusted to best meet the particular situation within the limitations set by the total use of time. The antenna beamwidth may be changed electronically by means of phase spoiling to search certain areas more rapidly but with less gain. Frequency agility can be achieved through changing the frequency of transmission at will from pulse to pulse or, with coding, within a pulse. Very high powers may be generated from a multiplicity of generators distributed across the aperture. Electronically controlled phase-array antennas can give radars the flexibility needed to perform all the various functions in a way best suited to the specific task at hand. The functions can be programmed rapidly and accurately with digital beam-steering computers.

Overview of the Chapter

The first part of this chapter describes the theory of phased-array antennas, with emphasis on the basic relationships between the array performance, the excitation coefficients (amplitude and phase) of each radiator, and the physical parameters of the antenna (see Sec. 20-2). These relationships are the design formulas which an antenna designer can use to determine the required array parameters that satisfy a given set of radar system requirements. After determining the array parameters such as the number of required radiators, the spacing between the radiators, and the size

of the radiating aperture, the next step in the design would be the selection of the type of radiator, phase shifter, and beam-forming feed network to implement physically the required excitations at the radiating aperture. A detailed discussion of the various types of radiators, phase shifters, and feed networks that are commonly used is given in Secs. 20-3, 20-4, and 20-5 respectively. Corresponding to the various types of phase shifters and feed networks, the frequency-bandwidth characteristics of the phased-array antenna are described in Sec. 20-6.

20-2 THEORY OF PHASED ARRAYS

We shall begin the discussion of array theory with the simplest configuration possible: an array of isotropic radiators (radiating elements) equally spaced along a line (linear in a geometric sense). It will be seen that the more complex array theory can be framed as an extension of this simple case. For example, two-dimensional arrays are often constructed of interconnected linear arrays. From the linear-array discussion, we will then proceed to the theory of two-dimensional arrays. The theory of arrays of isotropic radiators will then be extended and modified to apply to arrays of real radiators.

To simplify and condense the material to be presented, the following assumptions will be adhered to in this discussion:

1 For practical radar purposes, targets of interest will lie in the far-field region of the antenna, commonly defined by ranges R, satisfying

$$R \ge \frac{2L^2}{\lambda}$$

where L is the largest dimension of the antenna and λ is the operating wavelength. In this region, the antenna pattern is insensitive to range except for a scale factor of $1/R^2$ in power. This scale factor is usually ignored.

- 2 The reciprocity theorem¹ will be used extensively to justify analysis of array far fields from either the transmitting or the receiving viewpoint as convenience dictates and usually without explicit mention. By virtue of this theorem, the pattern will be the same in either case if no nonreciprocal devices are used. When such devices are used, one can usually perform pattern analyses which neglect their presence.
- 3 For simplicity, interest will be restricted to the responses of arrays to continuouswave (CW) signals.

Radiation Pattern of Linear Arrays

The theory of linear arrays is described in detail by Silver, ¹ Schelkunoff, ² and Allen. ³ Let us consider the elementary array of Fig. 20-1, consisting of N isotropic radiators, equally spaced at a distance d apart. On receive, if a plane wave is incident upon the array from a direction making an angle θ with the array normal, the current in the nth element will be of the form

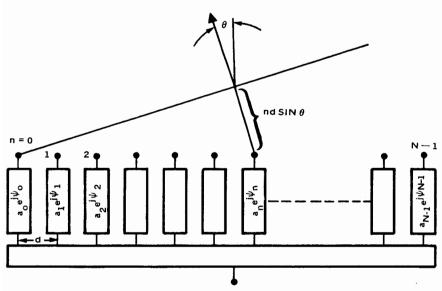


FIG. 20-1 Basic linear-array configuration.

$$i_n' = Ae^{jnkd\sin\theta} \tag{20-1}$$

where A is a complex constant related to the instantaneous amplitude and phase of the plane wave and k is the wave number:

$$k = \frac{2\pi f}{c} = \frac{2\pi}{\lambda}$$

where f =operating frequency

c = velocity of light

Equation (20-1) shows that the current in the *n*th element leads that in the (n + 1)th element by a phase shift given by $\Delta \psi = kd \sin \theta$. This phase shift corresponds to the difference in time of arrival τ of the plane wavefront of $\tau = d/c \sin \theta$. If we place a control element behind each radiator, as indicated in Fig. 20-2, with a transfer coefficient for the *n*th element given by

$$\frac{i_n''}{i_n'} = a_n e^{j\psi_n}$$

where a_n and ψ_n are the *real* current gain and phase shift of the control element respectively, the summing network produces an output

$$E_a(\theta) = \sum_{n=0}^{N-1} a_n e^{j(\psi_n + nkd \sin \theta)}$$
 (20-2)

where we now neglect the constant A of Eq. (20-1). This relationship gives the response of the array of Fig. 20-2 to a signal arriving from a direction θ in terms of the set of a_n 's and ψ_n 's. The set of coefficient a_n is usually called the array-amplitude

taper, while the ψ_n 's are called the *phase taper*. The expression of Eq. (20-2) is called the *array factor*. To combine the received signals from all the radiators in phase to produce a maximum response in the scan direction of θ_0 , the ψ_n 's must have the form

$$\psi_n = -nkd \sin \theta_0 \tag{20-3}$$

This expression shows that the required phase taper across the array aperture is a linear taper (constant phase differential between adjacent radiators). On transmit, when the phases of the control elements such as phase shifters are set to the phase taper of Eq. (20-3), the signals radiated from all the radiators will add up in phase to produce a main beam in the direction of θ_0 . Hence, the array factor of Eq. (20-2) is the same for both transmit and receive. Substituting Eq. (20-3) into Eq. (20-2), we have for the array factor

$$E_a(\theta) = \sum_{n=0}^{N-1} a_n e^{jnkd(\sin \theta - \sin \theta_0)}$$
 (20-4)

For the special case of a uniformly illuminated array, $a_n = 1$ for all n, the array factor for an N-element array becomes

$$E_a(\theta) = \frac{\sin\left[N\pi\frac{d}{\lambda}(\sin\theta - \sin\theta_0)\right]}{N\sin\left[\pi\frac{d}{\lambda}(\sin\theta - \sin\theta_0)\right]}$$
(20-5)

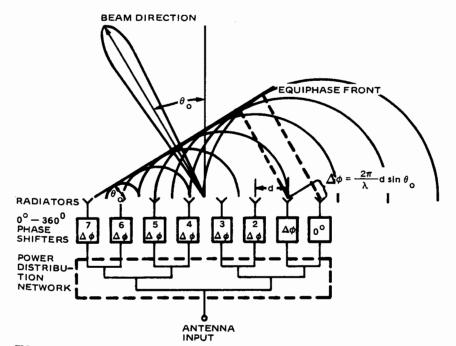


FIG. 20-2 Beam-steering concept using phase shifters at each radiating element.

Element Spacing to Avoid Grating Lobes

The array factor of Eq. (20-4) can also be expressed in terms of the variable $\nu = \sin \theta$ as follows:

$$E_a(\nu) = \sum_{n=0}^{N-1} a_n e^{jnkd(\nu-n)}$$
 (20-6)

where the beam-point direction ν_0 is related to the differential phase $\Delta \psi$ by $\Delta \psi = -k d\nu_0$. It is obvious that $E_a(\nu)$ and $E_a(\theta)$ are related by a one-to-one mapping in the region $|\nu| \leq 1$, which is often referred to as the visible space corresponding to the real angles of θ . It is also apparent that $E_a(\nu)$ is a periodic function of ν of period

$$\frac{2\pi}{kd} = \frac{1}{d/\lambda} = \frac{\lambda}{d}$$

and that Eq. (20-6) is in the form of a Fourier-series representation, which is readily analyzable and easy to visualize. The maxima of $E_a(\nu)$ occur whenever the argument of Eq. (20-6) is a multiple of 2π ; i.e., $kd(\nu - \nu_0) = 2i\pi$, where $i = 0, \pm 1, \pm 2, \ldots$, or

$$\nu_i - \nu_0 = \frac{i}{d/\lambda}$$

When $\nu_i = \nu_0$ or i = 0, this maximum is generally referred to as the *principal lobe* or main beam, and the other maxima are known as the *grating lobes* from the corresponding phenomena with optical gratings. In the design of phased arrays, it is imperative that the grating lobes be eliminated within the visible space since these lobes reduce the power in the main beam and thus reduce the antenna gain. This means that the element spacing d must be chosen to avoid the grating lobes over the range of ν from -1 to +1. When the main beam is scanned to ν_0 , the closest grating lobe to the visible space is located at $\nu_i = \nu_0 - 1 d/\lambda$ (see Fig. 20-3). This grating lobe will just appear in visible space (at end-fire direction of the array) when $\nu_0 - 1 d/\lambda = -1$, or

$$\frac{d}{\lambda} = \frac{1}{1 + \sin |\theta_0|}$$

Thus, the element-spacing criterion stated in terms of the desired maximum scan angle θ_{0max} is

$$\frac{d}{\lambda} < \frac{1}{1 + \sin |\theta_{0max}|} \tag{20-7}$$

If the equality sign is used in Eq. (20-7), we might actually incur rather than avoid the grating lobe. For narrow beams, however, the error committed by applying Eq. (20-7) is frequently small enough (particularly when the actual patterns of the real elements instead of the isotropic radiators are included) to justify using it rather than the more cumbersome exact formula which accounts for the finite width of the grating lobe. In actual practice, the value of d/λ is reduced by a few percent to assure that the grating lobe is positioned beyond end fire. Figure 20-4 presents a plot of Eq. (20-7).

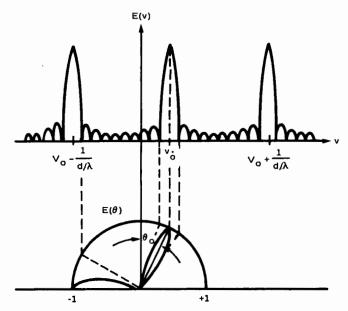


FIG. 20-3 Grating-lobe location as a function of beam scan and element spacing.

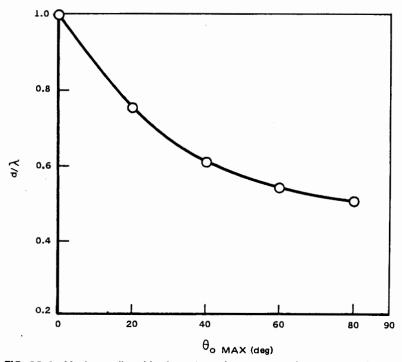


FIG. 20-4 Maximum allowable element spacing versus maximum scan angle.

Amplitude Tapers for Sidelobe Control

The far-field-pattern properties of most frequent concern to the array designer are the array sidelobe level, array gain, and beamwidth. All these properties depend upon the amplitude taper applied to the excitation coefficients a_n 's of Eq. (20-4). In general, a stronger amplitude taper across the array aperture has the effect of reducing the sidelobes at the expense of increased beamwidth and reduced aperture efficiency (antenna gain). There are four principal classes of amplitude tapers which will be outlined and compared: (1) powers of cosine on a pedestal, (2) Taylor distributions, (3) the modified $\sin \pi u/\pi u$ of Taylor distribution, and (4) Dolph-Chebyshev distribution.

The powers-of-cosine distributions are the class of tapers that resemble closely those provided by an optical feed system such as the primary illumination pattern of a feed horn illuminating a parabolic-reflector antenna. The continuous taper is of the form

$$a(x) = h + (1 - h) \cos^m \frac{\pi x}{L}$$
 (20-8)

where x = distance measured from center of array aperture

L = total length of aperture

h = normalized pedestal height

The most frequently used distributions of this class are the cosine (m = 1) and the cosine-squared (m = 2). The lowest first sidelobes achievable with the cosine are -23 dB when h = 0. This yields an illumination efficiency of 0.81 and a half-power beamwidth (HPBW) coefficient of 69°.

The cosine-squared taper reduces the peak sidelobe level of -32 dB when h=0. In general, the gain decreases and the beamwidth increases with increasing n. After the highest lobe, the sidelobes decay monotonically. The first sidelobe level, aperture efficiency, and HPBW for varous cosine tapers with h=0 are shown in Table 20-1.

The Taylor distribution provides a certain number of equal sidelobes symmetrically located on both sides of the main beam with the amplitudes of the remaining sidelobes decreasing monotonically. For a given design sidelobe level, the Taylor distribution provides a narrower beamwidth than that of the cosine distributions. The Taylor amplitude distribution is of the form

$$A(x,A,\overline{n}) = \frac{1}{2\pi} \left\{ F(0,A,\overline{n}) + 2 \sum_{n=1}^{\overline{n}-1} F(n,A,\overline{n}) \cos \frac{n\pi x}{L} \right\}$$

$$F(n,A,n) = \frac{\left[(n-1)! \right]^2 \prod_{m=1}^{\overline{n}-1} \left(1 - \frac{n^2}{\sigma^2 [A^2 + (m-\frac{1}{2})^2]} \right)}{(\overline{n}-1+n)! (\overline{n}-1-n)!}$$
(20-9)

where x = distance from center of aperture

L = total length of aperture

 $A = 1/\pi \operatorname{arc} \cosh R$

R = design sidelobe voltage ratio

$$\sigma = \frac{\overline{n}}{\sqrt{A^2 + (\overline{n} - \frac{1}{2})^2}}$$

 \tilde{n} = number of equiamplitude sidelobes adjacent to main beam on one side

m	First sidelobe level, dB	Aperture efficiency	Half-power beamwidth, °	Main-beam null width, °
0	13.2	1	50.4 λ/L	57.3 λ/L
1	23.0	0.810	$68.76\lambda/L$	85.95λ/ <i>L</i>
2	32.0	0.667	$83.08\lambda/L$	$114.6 \lambda/L$
3	40.0	0.575	$95.12\lambda/L$	$143.2 \lambda/L$
4	48	0.515	$110.59\lambda /L$	$171.9 \lambda/L$

TABLE 20-1 Pattern Characteristics for (cos) Distributions

Corresponding to this amplitude distribution, the beamwidth of a one-wavelength source is given by

$$\beta = \sigma \beta_0 \tag{20-10}$$

where

$$\beta_0 = \frac{2}{\pi} \sqrt{(\operatorname{arc cosh} R)^2 - \left(\operatorname{arc cosh} \frac{R}{\sqrt{2}}\right)^2}$$

For an array with aperture length L, the beamwidth is given by

Beamwidth =
$$\sigma \beta_0 \frac{\lambda}{L}$$
 rad (20-11)

Beamwidth as a function of the design sidelobe level for various values of \overline{n} is given in Table 20-2.

The modified $\sin \pi u/\pi u$ taper of Taylor distribution produces monotonically decreasing sidelobes. The radiation pattern has a main lobe of adjustable amplitude and a sidelobe structure similar to that of the radiation from a uniformly illuminated source. The amplitude distribution is of the form

$$a(x) = \frac{1}{2\pi} J_0 \left[j\pi\beta \sqrt{1 - \left(\frac{2x}{L}\right)^2} \right]$$
 (20-12)

where x = distance measured from center of aperture

L = total length of aperture

 $J_0 = \text{zero-order Bessel function of first kind}$

 β = parameter fixing ratio R of main-beam amplitude to amplitude of first sidelobe by $R = 4.60333 \sinh \pi \beta / \pi \beta$

The array pattern corresponding to the above amplitude distribution is given by

$$E_a(u) = \frac{\sin \pi \sqrt{u^2 - \beta^2}}{\sqrt{u^2 - \beta^2}}$$
 (20-13)

where

$$u = (L/\lambda) \sin \theta$$

The beamwidth and aperture efficiency as a function of the design sidelobe ratio are shown in Table 20-3. Typical amplitude distributions corresponding to radiation patterns of 10-, 20-, and 30-dB sidelobe levels are shown in Fig. 20-5.

The taper of Dolph-Chebyshev distribution^{6,7,8} is optimum in the sense that it

TABLE 20-2 Design Sidelobe Level and Beamwidth for Taylor Distributions

Design	R	1808					Values of the parameter	of the p	aramete	e.		
level, dB	(sidelobe voltage ratio)	(degrees)	A²	$\bar{n}=2$	$\bar{n}=3$	_ = 4	$\bar{n}=5$	$\bar{n}=6$	$\bar{n} = 7$	<u>n</u> = 8	$\bar{n} = 9$	$\ddot{n} = 10$
15	5.62341	45.93	0.58950	1.18689	1.14712	1.11631	1.09528	1.08043	1.06969	1.06112	1.05453	1.04921
91	6.30957	47.01	0.64798	1.17486	1.14225	1.11378	1.09375	1.07491	1.06876	1.06058	1.05411	1.04887
17	7.07946	48.07	1.6267	1.13723	1.11115	1.11115	1.09216	1.07835	1.06800	1.06001	1.06367	1.04852
18	7.94328	49.12	0.77266	1.15036	1.13206	1.10843	1.09050	1.07724	1.06721	1.05942	1.05328	1.04815
19	8.91251	50.15	0.83891	1.13796	1.12676	1.10563	1.08879	1.07609	1.06639	1.05880	1.05273	1.04777
20	10.00000	51.17	0.90777	1.12549	1.12133	1.10273	1.08701	1.07490	1.06554	1.05816	1.05223	1.04738
21	11.2202	52.17	0.97927	:	1.11577	1.09974	1.08518	1.07367	1.06465	1.05750	1.06172	1.04697
22	12.5893	53.16	1.05341	:	1.11009	1.09668	1.08329	1.07240	1.06374	1.05682	1.05119	1.04654
23	14.1254	54.13	1.13020	:	1.10430	1.09352	1.08135	1.07108	1.06280	1.05611	1.05064	1.04610
24	15.8489	55.09	1.20965	:	1.09840	1.00029	1.07934	1.06973	1.06183	1.05538	1.05007	1.04565
25	17.7828	56.04	1.29177	:	1.09241	1.08598	1.07728	1.06834	1.06083	1.05463	1.04948	1.04518
26	19.9526	26.97	1.37654	:	1.08632	1.08360	1.07517	1.06690	1.05980	1.05385	1.04888	1.04669
27	22.3872	57.88	1.46395	:	1.08015	1.08014	1.07300	1.06543	1.05874	1.05305	1.04826	1.04420
28	25.1189	58.78	1.55406	:	:	1.07661	1.07078	1.06392	1.05765	1.05223	1.04762	1.04368
29	28.1838	29.67	1.64683	:	:	1.07300	1.06851	1.06237	1.05653	1.05139	1.04696	1.04316
30	31.6228	60.55	1.74229	:	:	1.06934	1.06619	1.06079	1.05538	1.05052	1.04628	1.04262
31	35.4813	61.42	1.84044	:	:	1.06561	1.06382	1.05916	1.05421	1.04963	1.04559	1.04206
32	39.8107	62.28	1.94126	:	:	1.06182	1.06140	1.05751	1.05300	1.04872	1.04488	1.04149
33	44.6684	63.12	2.04472	:	:	:	1.05893	1.05581	1.05177	1.04779	1.04415	1.04091
34	50.1187	63.96	2.15092	:	:	:	1.05642	1.05408	1.05051	0.04684	1.04341	1.04031
35	56.2341	64.78	2.25976	:	:	. :	1.05386	1.05231	1.04923	1.04587	1.04264	1.03970
36	63.0957	65.60	2.37129	:	:	:	1.05126	1.05051	1.04792	1.04487	1.04186	1.03907
37	70.7946	66.40	2.48551	:	:	:	:	1.04868	1.04658	1.04385	1.04107	1.03843
38	79.4328	61.19	2.60241	:	:	:	:	1.04681	1.04521	1.04282	1.04025	1.03777
39	89.1251	86.79	2.72201	:	:	:	:	1.04491	1.04382	1.04176	1.03942	0.03711
40	100.000	92.89	2.84428	:	:	:	:	1.04298	1.04241	1.04068	1.03808 1.03643	1.03643

TABLE 20-3 Design Sidelobe Level, Beamwidth, and Aperture Efficiency for Modified $\sin \pi u/\pi u$ Distributions

Sidelobe ratio, dB	R (sidelobe voltage ratio)	8	B ²	180 <i>β/π</i> , beamwidth of a one- wavelength source, °	β/β_0 , ratio of beamwidth to ideal ģeamwidth	aperture efficiency
	00000	_i0812825	-0.660684	33.307	1.1626	0.3452
0 4	17878	-i 0 686524	-0.471315	40.000	1.1597	0.7110
n <u>s</u>	3 16 288	-i 0 459645	-0.211274	46.620	1.1559	0.9635
0 4	5 62341	0 355769	0.126572	52.884	1.1514	0.9931
13 20	10.00000	0.738600	0.545530	58.659	1.1464	0.9330
	17 7878	1 02292	1.046365	63.938	1.1410	0.8626
5 6	21,7020	1 27616	1.628584	68.775	1.1358	0.8014
30 36	56 2341	1 51363	2.291076	73.232	1.1305	0.7509
č 4	100.000	1.74148	3.032753	77.378	1.1254	0.7090

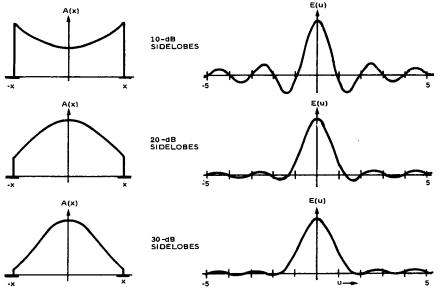


FIG. 20-5 Amplitude distributions and array patterns for three representative sidelobe levels.

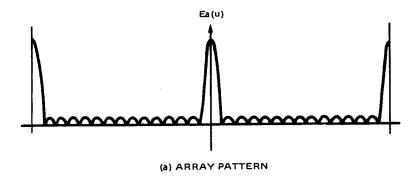
yields the narrowest beamwidth for a given sidelobe ratio, and vice versa. It is not optimum in the terms of aperture efficiency for a given sidelobe level. A special property of this taper is that it yields an array function with equal-amplitude sidelobes, as shown in Fig. 20-6. This fact and its effect on the amplitude taper lead to some secondary considerations regarding the use of this taper. Since the sidelobes do not decay, the percentage of power in the main beam varies with the number of elements N in the array for a given sidelobe level. Hansen⁹ has shown that for this reason, in order to maintain high efficiency, large Dolph-tapered arrays must use low-sidelobe tapers.

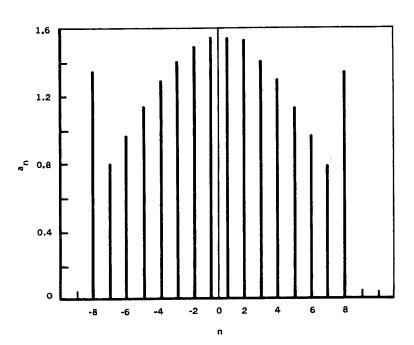
An amplitude taper which produces the array pattern of Fig. 20-6a is shown in Fig. 20-6b. The peaked-edge excitation currents are typical of a large array and high-sidelobe design (a 30-dB-sidelobe taper would have edge excitation currents approximately the same as neighboring elements). Such peak distributions are prone to error effects that arise in edge elements of arrays using real radiators. Hence, this distribution is not commonly employed in practice.

Array-Pattern Directivity of Linear Arrays

Array directivity is defined as the ratio of power density per unit solid angle at the peak of the main beam to the average power radiated per unit solid angle over all space. From this definition, it follows that the directivity of the main beam at angle θ_0 is given by

$$D(\theta_0) = \frac{|E(\theta_0)|^2}{\frac{1}{4\pi} \int_{\|\theta\| \text{ space }} |E(\theta)|^2 d\Omega}$$
 (20-14)





(b) ILLUMINATION COEFFICIENTS

FIG. 20-6 Illumination coefficients and array pattern for 20-dB Dolph taper applied to a 16-element array.

where $d\Omega = \cos\theta \ d\theta \ d\phi$. For a linear array of isotropic radiators arranged as shown in Fig. 20-7, $E(\theta)$ is independent of ϕ . Therefore, $\int |E|^2 d\Omega = 2\pi \int |E|^2 \cos\theta \ d\theta$. Using $\nu = \sin\theta$ and $d\nu = \cos\theta \ d\theta$, we have

$$D(\nu_0) = \frac{2|E(\nu_0)|^2}{\int_{-1}^{+1} |E(\nu)|^2 d\nu}$$
 (20-15)

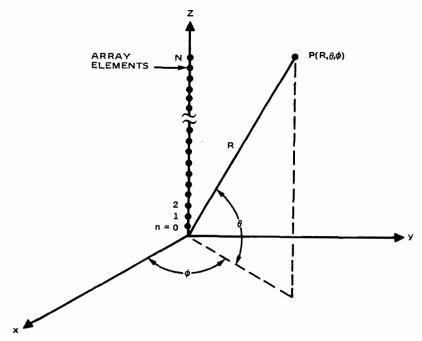


FIG. 20-7 N-element linear-array geometry.

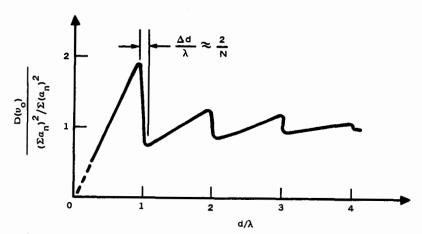


FIG. 20-8 Variation of directivity $D(v_0)$ of a linear array of isotropic radiators with element spacing d/λ . (After Ref. 3.)

Using Eq. (20-6) and integrating yield

$$D(v_0) = \frac{\left|\sum_{n=0}^{N-1} a_n\right|^2}{\sum_{n=0}^{N-1} \sum_{m=0}^{N-1} a_m a_n \frac{\sin 2\pi (d/\lambda)(n-m)}{2\pi (d/\lambda)(n-m)}}$$
(20-16)

The denominator of Eq. (20-16) prevents a simple analysis of the directivity. Only when $2d/\lambda$ is an integral number is the result simplified:

$$D(\nu_0) = \frac{\left(\sum_{n=0}^{N-1} a_n\right)^2}{\sum_{n=0}^{N-1} (a_n)^2}$$

However, a detailed analysis of Eq. (20-16) shows that the directivity varies with element spacing approximately as indicated in Fig. 20-8 for beam shapes that concentrate most of the power in the main lobe. ¹⁰ For spacings less than λ , for which only one principal lobe exists in visible space when the main beam is at broadside, we can write the simple result

$$D(\nu_0 = 0) \approx \frac{2d}{\lambda} \frac{\left(\sum_{n=0}^{N-1} a_n\right)^2}{\sum_{n=0}^{N-1} (a_n)^2}$$
 (20-17)

Letting

$$\frac{\left(\sum_{n=0}^{N-1} a_n\right)^2}{\sum_{n=0}^{N-1} (a_n)^2} = \eta N$$
 (20-18)

where η is defined as the aperture efficiency, we can write

$$D(\nu_0 = 0) \approx \frac{2\eta Nd}{\lambda}$$
 (20-19)

For a given N and d/λ , η alone determines the directivity. The value of η is determined by the amplitude taper applied across the aperture. The maximum value of η is unity, corresponding to a uniformly illuminated array. The values of η for various amplitude tapers of the modified sin u/u distributions are shown in Table 20-3.

Radiation Pattern of Planar Arrays

To provide beam scanning in two angular dimensions, a planar array of radiating elements must be used. In a spherical coordinate system, the beam position is defined by the two coordinates θ and ϕ as shown in Fig. 20-9. Also shown in Fig. 20-9 is the layout of the element lattice in the planar array. For a rectangular lattice, the *mnth*

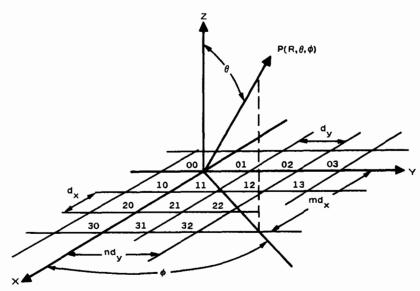


FIG. 20-9 Element geometry of a two-dimensional array.

element is located at $x_m = md_x$ and $y_n = nd_y$. For a triangular lattice, the element grid can be thought of as a rectangular grid in which every other element has been omitted. In this case, only every other value of mn contains an element. The element locations can be defined by requiring that the (m + n) be even.

The array factor of a two-dimensional array may be calculated by summing the vector contribution of each element in the array at each point in space. The array factor can be written in terms of the directional cosines, $\cos \alpha_x$ and $\cos \alpha_y$, of the spherical coordinate system as follows:

$$E_d(\cos \alpha_x, \cos \alpha_y) = \sum_m \sum_n i_{mn} e^{jk(md_x \cos \alpha_x + nd_y \cos \alpha_y)}$$
 (20-20)

where

$$\cos \alpha_x = \sin \theta \cos \phi$$
 (20-21)
 $\cos \alpha_y = \sin \theta \sin \phi$

For a uniformly illuminated $(i_{mn} = 1)$ rectangular array, we have

$$E_a(\cos \alpha_x, \cos \alpha_y) = \sum_{m=-(M-1)/2}^{(M-1)/2} e^{jkmd_x \cos \alpha_x} \sum_{n=-(N-1)/2}^{(N-1)/2} e^{jknd_y \cos \alpha_y}$$
 (20-22)

Each sum can be evaluated, producing a result analogous to Eq. (20-5) for a uniformly illuminated linear array:

$$E_{a}(\cos \alpha_{x}, \cos \alpha_{y}) = \left[\frac{\sin \left(\pi M \frac{d_{x}}{\lambda} \cos \alpha_{x} \right)}{M \sin \left(\pi \frac{d_{x}}{\lambda} \cos \alpha_{x} \right)} \right] \left[\frac{\sin \left(\pi N \frac{d_{y}}{\lambda} \cos \alpha_{y} \right)}{N \sin \left(\pi \frac{d_{y}}{\lambda} \cos \alpha_{y} \right)} \right]$$
(20-23)

Beam scanning with planar arrays is accomplished by linear phasing along both array coordinates. To scan the beam to the angular position corresponding to the directional cosines $\cos \alpha_{x0}$ and $\cos \alpha_{y0}$, a linear phase taper is introduced at each element so that the excitation at the *mn*th element is given by

$$i_{mn} = a_{mn}e^{j(kmd_x \cos a_{x0} + knd_y \cos a_{y0})}$$
 (20-24)

where $kd_x \cos \alpha_{x0}$ = element-to-element phase shift in the x direction

 $kd_y \cos \alpha_{y0} =$ element-to-element phase shift in the y direction

This form of steering phase indicates that the phase of the *mn*th element is the sum of a row phase $mkd_x \cos \alpha_{x0}$ and a column phase $nkd_y \cos \alpha_{y0}$.

The array factor of a rectangular planar array of M by N elements is then given by

$$E_a(\cos \alpha_x, \cos \alpha_y) = \sum_{m} \sum_{a} a_{mn} e^{jk[md_x(\cos \alpha_x - \cos \alpha_{x0}) + nd_y(\cos \alpha_y - \cos \alpha_{y0})]}$$
 (20-25)

Element Spacing and Lattice of Planar Arrays

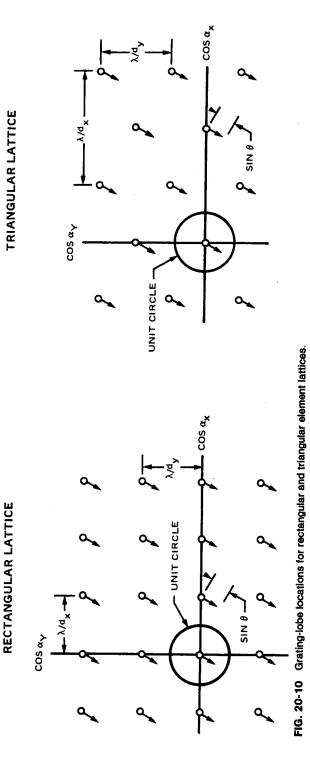
As in the case of the linear array, the array factor of the planar array [Eq. (25)] has an infinite number of grating lobes in the directional cosine space. For example, the maxima of E_a occur whenever the argument of Eq. (20-25) is a multiple of 2π . Since there is a one-to-one correspondence between the directional cosine space (cos α_x and $\cos \alpha_{\nu}$ space) and the visible space (θ and ϕ space within the boundary defined by \cos^2 $\alpha_x + \cos^2 \alpha_y = 1$), the number of grating lobes that can be projected from the directional cosine space into the visible space depends upon the parameters d_x/λ and d_y/λ λ. To avoid the formation of grating lobes in the visible space, the element spacings $d_{\rm v}/\lambda$ and $d_{\rm v}/\lambda$ must be chosen so that there is only one maximum from Eq. (20-25), namely, the main beam, in the visible space (real space). In the planar array, the element lattice and spacing can be chosen to shape the grating-lobe contour (location pattern of grating lobes) to fit the required scanning volume so that the total required number of elements in the planar array is minimized. To accomplish this optimization, it is more convenient to plot the position of the grating lobes when the main beam is phased for broadside and observe the motion of these lobes as the beam is scanned. Figure 20-10 shows the grating-lobe locations for both rectangular and triangular spacings. For a rectangular lattice, the grating lobes are located at

$$\cos \alpha_x - \cos \alpha_{x0} = \pm \frac{\lambda}{d_x} \cdot p$$

$$p, q = 0, 1, 2, \dots$$

$$\cos \alpha_y - \cos \alpha_{y0} = \pm \frac{\lambda}{d_y} \cdot q$$
(20-26)

The grating-lobe pattern of Fig. 20-10 must be mapped onto the surface of the unit sphere, as shown in Fig. 20-11, to give a true spatial distribution; therefore, only the portion of the pattern of Fig. 20-10 inside a unit circle centered at $\cos \alpha_x = \cos \alpha_y = 0$ lies in visible space. The lobe at p = q = 0 is the main beam. For a conical scan volume, the triangular grid is more efficient for the suppression of grating lobes than a rectangular grid, so that for a given aperture size fewer elements are required. If the triangular lattice contains elements at md_x and nd_y , where m + n is even, then the grating lobes are located at



20-18

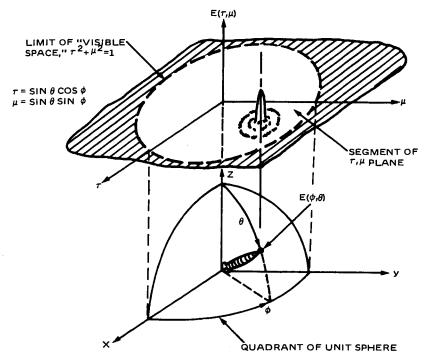


FIG. 20-11 Construction of array factor $E(\phi,\theta)$ by projection of array function $E(\tau,\mu)$ onto unit sphere.

$$\cos \alpha_x - \cos \alpha_{x0} = \pm \frac{\lambda}{2d_x} \cdot p$$

$$p, q = 0, 1, 2, \dots$$

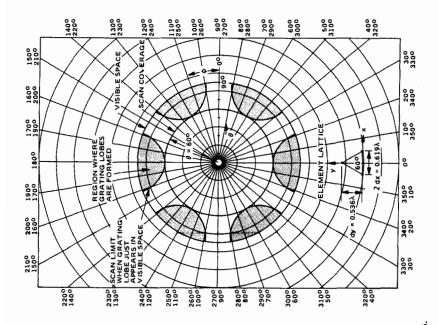
$$\cos \alpha_y - \cos \alpha_{y0} = \pm \frac{\lambda}{2d_y} \cdot q$$
(20-27)

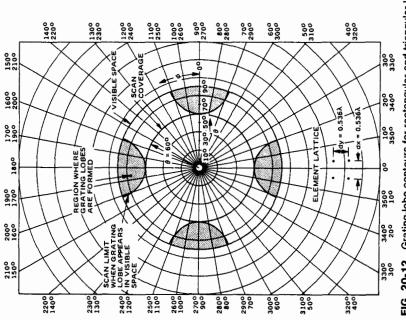
where p + q is even.

As the array is scanned away from broadside, each grating lobe (in directional cosine space) will move a distance equal to the sine of the angle of scan and in a direction determined by the plane of scan. To ensure that no grating lobes enter visible space (real space), the element spacing must be chosen so that for the maximum scan angle θ_m the movement of a grating lobe by $\sin \theta_m$ does not bring the grating lobe into visible space. If a scan angle of 60° from broadside is required for every plane of scan, no grating lobe may exist within a circle of radius $1 + \sin \theta_m = 1.866$. The square lattice that meets this requirement has

$$\frac{\lambda}{d_x} = \frac{\lambda}{d_y} = 1.866 \quad \text{or} \quad d_x = d_y = 0.536\lambda$$

Here, the area per element is





Grating-lobe contours for rectangular and triangular lattices. FIG. 20-12

$$d_x \cdot d_y = (0.536\lambda)^2 = 0.287\lambda^2$$

For an equilateral-triangular lattice, the requirement is satisfied by

$$\frac{\lambda}{d_y} = \frac{\lambda}{\sqrt{3}d_x} = 1.866 \quad \text{or} \quad d_y = 0.536\lambda, d_x = 0.309\lambda$$

If we recall that elements are located only at every other value of *mn*, the area per element is

$$2d_x d_y = 2(0.536\lambda)(0.309\lambda) = 0.332\lambda^2$$

For the same amount of grating-lobe suppression, the saving in the number of elements for the triangular versus the rectangular lattice is approximately 14 percent. The grating-lobe-contour plots illustrating the above example are shown in Fig. 20-12.

Amplitude Taper for Planar Arrays

If markedly different patterns are desired in the two orthogonal planes ($\cos \alpha_x$ and $\cos \alpha_y$ planes), it is often advantageous to use rectangularly shaped arrays with sides parallel to the specified planes and separable illumination; that is, $a_{mn} = a_{mn}a_{mn}$, so that

$$E_{a}(\cos \alpha_{x}, \cos \alpha_{y})$$

$$= \sum_{m} \sum_{n} a_{mn} e^{jk[md_{x}(\cos \alpha_{x} - \cos \alpha_{x0}) + nd_{y}(\cos \alpha_{y} - \cos \alpha_{y0})]}$$

$$= \sum_{m} a_{m} e^{jkmd_{x}(\cos \alpha_{x} - \cos \alpha_{x0})} \sum_{n} a_{n} e^{jknd_{y}(\cos \alpha_{y} - \cos \alpha_{y0})}$$

$$= E_{a}(\cos \alpha_{y}) \cdot E_{a}(\cos \alpha_{y})$$
(20-28)

where E_{a1} and E_{a2} are synthesized by linear-array techniques. In this case, the amplitude distributions described in the subsection "Amplitude Tapers for Sidelobe Control" can be applied along each orthogonal axis of the planar array to achieve the desired sidelobe control. One special feature of this separable illumination is that the sidelobe levels along the $\cos \alpha_x$ plane are those of $E_{a1}(\cos \alpha_x)$ alone, since E_{a2} is a maximum. Away from both the $\cos \alpha_x$ and the $\cos \alpha_y$ axes (diagonal planes), the sidelobes are lower as a result of the product of E_{a1} and E_{a2} , both less than their maxima. For example, the array factor for a uniformly illuminated rectangular aperture was given by Eq. (20-23). The array factor yields first sidelobes of about -13.2 dB below the main beam along the two orthogonal axes. Off the axes, the sidelobes are lower. In particular, along the 45° diagonals, the first sidelobes are twice as low in decibels, -26.4 dB.

Consequently, for a given peak sidelobe level, the taper efficiency ($\eta = \eta_1 \eta_2$) is lower for a separable illumination than that which can be realized by nonseparable means, although the average sidelobe level should be comparable to tapers of like values of η .

If a circularly symmetric pattern is desired, an array shape approximating a circle is preferred. Here, the array symmetry refers to only the symmetry of the beam shape and near-in-sidelobe structure. The element grid will still govern the grating-lobe location. In most cases, the amplitude distributions for circular arrays are non-separable. The two common distributions are $(1 - r^2)^p$ distributions¹ and circular

Taylor distributions. ^{12,13} The sidelobe level, beamwidth, and aperture efficiency for the above two types of distributions are given in Tables 20-4 and 20-5 respectively.

For the special case of a uniformly illuminated circular array, corresponding to p = 0 in the $(1 - r^2)^P$ distribution, the array pattern is given by

$$E_a(\theta) \approx \frac{J_1(ka\sin\theta)}{ka\sin\theta}$$

where $J_1(x)$ is the first-order Bessel function. The function has an HPBW coefficient of 58.5°, defined by

Beamwidth =
$$58.5 \frac{\lambda}{2a}$$

where a is the radius of the circular aperture. The first sidelobes are approximately -17.5 dB.

Array Directivity and Gain of Planar Arrays

The directivity of a planar array is defined as in Eq. (20-14) with appropriate notation changes to include both spatial angles:

$$D(\theta_0, \phi_0) = \frac{|E_a(\theta_0, \phi_0)|^2}{\frac{1}{4\pi} \int_{\text{all space}} |E_a(\theta, \phi)|^2 d\Omega}$$
 (20-29)

where $d\Omega = \sin \theta d\theta d\phi$.

For a large array, the array factor of a discrete array closely approximates that of a continuous array near the main lobe. Thus, if the array factor is such that almost all the power is in the main beam and the first few sidelobes and there is no grating lobe in the visible space, the directivity expression for a continuous aperture [Ref. 1, Eq. (19), page 177] may be used:

TABLE 20-4 Design Sidelobe, Beamwidth, and Aperture Efficiency of $(1 - r^2)^P$ Distributions for a Circular Aperture

P	First-sidelobe dB below peak intensity	Half-power width	Position of first zero	Aperture efficiency
0	17.6	$1.02 \frac{\lambda}{D}$	$\sin^{-1}\frac{1.22\lambda}{D}$	1.00
I	24.6	$1.27 \frac{\lambda}{D}$	$\sin^{-1}\frac{1.63\lambda}{D}$	0.75
2	30.6	$1.47 \frac{\lambda}{D}$	$\sin^{-1}\frac{2.03\lambda}{D}$	0.56
3	35.8	$1.65 \frac{\lambda}{D}$	$\sin^{-1}\frac{2.42\lambda}{D}$	0.44
4	40.6	$1.81 \frac{\lambda}{D}$	$\sin^{-1}\frac{2.79\lambda}{D}$	0.36

TABLE 20-5 Design Sidelobe and Beamwidth of Circular Taylor Distributions

Design	u			,		Valu	Values of the parameter σ	parame	eter σ		
sidelobe level, dB	(sidelobe voltage ratio)	beamwidth, $eta_{ m o},$	A ²	$\bar{n} = 3$	$\overline{n} = 4$	<u>n</u> = 5	$\bar{n}=6$	$\bar{n} = 7$	$\bar{n} = 8$	<u>n</u> = 9	$\bar{n} = 10$
15	5.62341	45.93	0.58950	1.2382	1.1836	1.1485	1.1244	1.1069	1.0937	1.0833	1.0751
16	6.30957	47.01	0.64798	1.2330	1.1809	1.1469	1.1233	1.1061	1.0931	1.0829	1.0747
17	7.07946	48.07	0.70901	1.2276	1.1781	1.1452	1.1222	1.1053	1.0925	1.0825	1.0743
18	7.94328	49.12	0.77266	1.2220	1.1752	1.1434	1.1210	1.1045	1.0919	1.0820	1.0740
19	8.91251	50.15	0.83891	1.2163	1.1723	1.1416	1.1198	1.1037	1.0913	1.0815	1.0736
20	10.00000	51.17	0.90777	1.2104	1.1692	1.1398	1.1186	1.1028	1.0906	1.0810	1.0732
21	11.2202	52.17	0.97927	1.2044	1.1660	1.1379	1.1173	1.1019	1.0899	1.0805	1.0728
22	12.5893	53.16	1.05341	1.1983	1.1628	1.1359	1.1160	1.1009	1.0892	1.0799	1.0723
23	14.1254	54.13	1.13020	1.1920	1.1594	1.1338	1.1146	1.1000	1.0885	1.0793	1.0719
24	15.8489	55.09	1.20965	1.1857	1.1560	1.1317	1.1132	1.0990	1.0878	1.0788	1.0714
25	17.7828	56.04	1.29177	1.1792	1.1525	1.1296	1.1118	1.0979	1.0870	1.0782	1.0709
26	19.9526	56.97	1.37654	1.1726	1.1489	1.1274	1.1103	1.0969	1.0862	1.0775	1.0704
27	22.3872	57.88	1.46395	1.1660	1.1452	1.1251	1.1087	1.0958	1.0854	1.0769	1.0699
28	25.1189	58.78	1.55406	1.1592	1.1415	1.1228	1.1072	1.0946	1.0845	1.0762	1.0694
29	28.1838	29.67	1.64683	1.1524	1.1377	1.1204	1.1056	1.0935	1.0836	1.0756	1.0688
30	31.6228	60.55	1.74229	1.1455	1.1338	1.1180	1.1039	1.0923	1.0827	1.0749	1.0683
31	35.8107	61.42	1.84044	1.1385	1.1298	1.1155	1.1022	1.0911	1.0818	1.0742	1.0677
32	39.8107	62.28	1.94126	1.1315	1.1258	1.1129	1.1005	1.0898	1.0809	1.0734	1.0671
33	44.6684	63.12	2.04473	1.1244	1.1217	1.1103	1.0987	1.0885	1.0799	1.0727	1.0665
34	50.1187	63.96	2.15092	:	1.1176	1.1077	1.0969	1.0872	1.0790	1.0719	1.0659
35	56.2341	64.78	2.25976	:	1.1134	1.1050	1.0951	1.0859	1.0779	1.0711	1.0653
36	63.0957	65.60	2.37129	:	1.1091	1.1023	1.0932	1.0846	1.0769	1.0703	1.0647
37	70.7946	66.40	2.48551	:	1.1048	1.0995	1.0913	1.0832	1.0759	1.0695	1.0640
38	79.4328	67.19	2.60241	:	1.1005	1.0967	1.0894	1.0818	1.0748	1.0687	1.0633
39	89.1251	86.79	2.72201	:	1.0961	1.0938	1.0874	1.0803	1.0737	1.0678	1.0627
40	100.0000	92.89	2.84428		1.0916	1.0910	1.0854	1.0789	1.0726	1.0670	1.0620

$$D(\theta_0,\phi_0) = \frac{4\pi}{\lambda^2} \cos \theta_0 \frac{\left| \int \int i(x,y) dx dy \right|^2}{\int \int |i(x,y)|^2 dx dy}$$
 (20-30)

where the integrals are understood to extend over the entire aperture of the antenna. For a uniformly illuminated array, i(x,y) = 1, the directivity is given by

$$D(\theta_0,\phi_0) = \frac{4\pi A}{\lambda^2} \cos \theta_0 \qquad (20-31)$$

For all tapered illuminations, the directivity would be less than that of a uniformly illuminated array. Making use of the Schwartz inequality, 12

$$\left| \int fg \, dx dy \right|^2 \le \int f^2 \, dx dy \cdot \int g^2 \, dx dy$$

where f and g are any two functions; by taking f = i(x,y) and g = 1, we find

$$\left| \int_A i(x,y) \ dxdy \right|^2 \le A \int |i(x,y)|^2 \ dxdy$$

Therefore,

$$\frac{\left|\int\int i(x,y)\ dxdy\right|^2}{\int\int |i(x,y)|^2\ dxdy} = \eta A \qquad 0 \le \eta \le 1$$
 (20-32)

where A is the physical area of the array and η is, as in the case of linear arrays, the taper efficiency or illumination efficiency; η is unity for uniform illumination and is tabulated for other tapered illuminations as shown in Table 20-5.

Substituting Eq. (20-32) into Eq. (20-30), we have

$$D(\theta_0, \phi_0) = \frac{4\pi A}{\lambda^2} \eta \cos \theta_0$$
 (20-33)

For a large array of discrete elements, the directivity can be expressed in terms of the actual taper coefficients by noting that

$$\int \int i(x,y) \ dxdy \approx \sum_{m} \sum_{n} i_{mn} \ dxdy$$

for $i_{mn} = i(md_x, nd_y)$. By a similar equivalence in the denominator of Eq. (32), it follows that

$$\frac{\left|\int\int i(x,y) \ d_x d_y\right|^2}{\left|\int\int |i(x,y)|^2 \ d_x d_y\right|} \approx \frac{\left|\sum\sum i_{mn} \ d_x d_y\right|^2}{\sum\sum |i_{mn}|^2 \ d_x d_y} \approx \eta N \ d_x d_y = \eta A$$

where N is the total number of elements in the array. Thus, for a large array

$$D(\theta_0,\phi_0) = 4\pi\eta N \frac{d_x d_y}{\lambda^2} \cos \theta_0$$
 (20-34)

The directivity expressions as shown in Eqs. (20-33) and (20-34) are for an array aperture which is impedance-matched for all beam-scan angles; i.e., the aperture is transparent for a plane-wave incidence at any scan angle θ_0 without reflections. However, in practice, the aperture is mismatched at some scan angles. Therefore, the array gain of the antenna is given by

$$G(\theta_0,\phi_0) = \frac{4\pi A}{\lambda^2} \eta \cos \theta_0 [1 - |\Gamma(\theta_0,\phi_0)|^2]$$
 (20-35)

where $|\Gamma(\theta_0,\phi_0)|$ is the amplitude of the array aperture reflection coefficient at the scan angle θ_0,ϕ_0 .

In general, the antenna beam-forming network behind the array aperture has ohmic losses such as the losses in the phase shifters, power combiners, etc. Hence, the net antenna gain is given by

$$G(\theta_0,\phi_0) = \frac{4\pi A}{\lambda^2} \eta \cos \theta_0 (1 - |\Gamma(\theta_0,\phi_0)|^2) - \text{all other ohmic losses} \qquad \textbf{(20-36)}$$

20-3 RADIATOR DESIGN FOR PHASED ARRAYS

The discussion on array theory in Sec. 20-2 is based on radiators with isotropic patterns. In practice, however, the radiation patterns of real radiators are nonisotropic, and the impedance of the radiators varies as a function of scan caused by the mutual coupling between the radiators. In fact, the pattern of an element in the environment of an array is markedly different from the pattern of an isolated element in amplitude, phase, and, perhaps, polarization as well.

One of the functions performed by the antenna is to provide a good match between the radar transmitter and free space. This means that the radiation impedance (driving-point impedance) looking into the radiators in the array environment must be matched to their generator impedances. If the antenna aperture is not matched to free space, power will be reflected back toward the generator, resulting in a loss in radiated power. In addition, a mismatch produces standing waves on the feed line to the antenna. The voltage at the peaks of these standing waves is $(1 + |\Gamma|)$ times greater than the voltage of a matched line, where Γ is the voltage reflection coefficient of the radiation impedance. This corresponds to an increased power level that is $(1 + |\Gamma|)^2$ times as great as the actual incident power. Therefore, while the antenna is radiating less power, individual components must be designed to handle more peak power. In a scanning array, the impedance of a radiating element varies as the array is scanned, and the matching problem is considerably more complicated. In some instances, spurious lobes may appear in the array pattern as a consequence of the mismatch. Furthermore, there are conditions in which an antenna that is well matched at broadside may have some angle of scan at which most of the power is reflected.

To illustrate this mutual-coupling effect on the radiation impedance, the couplings from several elements to a typical central element, element 00, is shown in Fig. 20-13. $C_{mn,pq}$ is the mutual-coupling coefficient relating the voltage (amplitude and phase) induced in the mnth element to the voltage excitation at the pqth element. The coupled signals add vectorially to produce a wave traveling toward the generator of

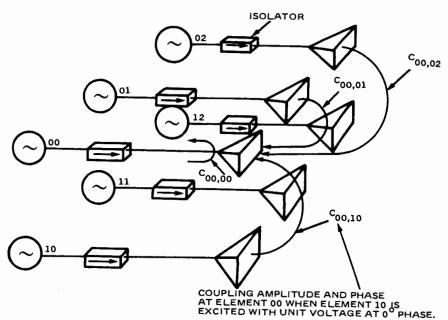


FIG. 20-13 Coupled signals to a central element from neighboring elements.

element 00, which appears to be a reflection from the radiator of element 00. As the phases of the neighboring elements are varied to scan the beam, the vector sum of the coupled signals changes and causes an apparent change in the impedance of element 00. For some scan angles the coupled voltages will tend to add in phase, causing a large reflection and possibly the loss of the main beam. Large reflections often occur at scan angles just prior to the emergence of a grating lobe into real space, but in some instances such reflections may occur at smaller scan angles.

The mutual-coupling effects described above have been studied in detail for dipole and open-ended waveguide radiators. 14,15,16,17,18,19

Active-Element Pattern

For an array with independently driven elements as shown in Fig. 20-13, the far-field array pattern at any angle (θ,ϕ) is obtained by vector addition of the contributions from all the elements at that angle with each single element driven one at a time while others are terminated in their generator impedances. The far-field array pattern is given by

$$E(\theta,\phi) = \sum_{m} \sum_{n} i_{mn} E_{e,mn}(\theta,\phi) e^{jk[md_x(\sin\theta\cos\phi-\sin\theta\cos\phi)+nd_y(\sin\theta\sin\phi-\sin\theta\cos\phi)]}$$

(20-37)

where $E_{e,mn}(\theta,\phi)$ = active-element pattern obtained when *only* the *mn*th element is driven, with all other elements terminated in their usual generator impedance

i_{mn} = current in amperes that would be flowing in the mnth feed line if all other elements were passively terminated in their usual generator impedance (i.e., the current in the mnth feed line due solely to the mnth-element generator, not including that coupled into the mnth element from any other generators)

The utility of these definitions arises from the fact that both computationally and experimentally one driven element in a passively terminated array is easier to cope with than all elements simultaneously driven. Furthermore, the active-element pattern has the significance of describing the array gain as a function of beam-scan angle.

Since $E_{e,mn}(\theta,\phi)$ is actually the pattern of the entire array when the excitation of the array is that due to the mutual couplings from the mnth element to all the neighboring elements, it is a function not only of the particular radiator configuration but also of the relative location of the driven radiator with respect to the other elements of the array. In general, the expressions of the active-element pattern, $E_{e,mn}(\theta,\phi)$, for any radiator type are quite complicated. Nevertheless, all the active-element patterns as defined in Eq. (20-37) could be individually measured or perhaps numerically calculated. Fortunately, this individual-element-pattern measurement is not usually necessary if the array is regularly spaced. For an infinite array of regularly spaced elements, every element in the array sees exactly the same environment and all the elements have the same active-element pattern. The radiation impedance of an element measured in waveguide simulators²⁰ corresponds to the element impedance in an infinite array. This infinite-array model can predict with good accuracy the array impedance and impedance variations with scan for a finite array. Even arrays of modest proportions (less than 1000 elements) have been in reasonable agreement with the results predicted for an infinite array.21 The reason for this is that, in practice, the mutual coupling between the radiators decays as $1/x^2$, where x is the distance between the radiators. Hence, the effect of mutual coupling is quite localized in cases of practical interest. All the elements with the exception of the edge elements in the array behave as though they are in an infinite-array environment. For larger arrays, the effect of edge elements on array performance is negligible. Therefore, the array factor of Eq. (20-37) can be written as

$$E(\theta,\phi) = E_e(\theta,\phi) \sum_{m} \sum_{n} i_{mn} e^{jk[md_x(\sin\theta\cos\phi - \sin\theta\cos\phi) + nd_y(\sin\theta\sin\phi - \sin\theta\cos\phi)]}$$

$$= E_e(\theta,\phi) \cdot E_o(\theta,\phi) \qquad (20-38)$$

Equation (20-38) states that the radiation pattern of an array is the product of the element pattern and the array factor. The array factor is determined by the geometric placement of the elements and their relative phasing on the assumption that the elements are isotropic and that there is no mutual coupling. Its peak value is independent of the scan angle. The active-element pattern is the actual radiation pattern of an element in the array taken in the presence of all other elements and taking into account all mutual-coupling effects and mismatches. It follows from this definition that as the array is being scanned, the peak of the radiation pattern $E(\theta,\phi)_{\text{max}}$ will trace out the element pattern. The active-element pattern may also be obtained experimentally by exciting one central element in a small test array and terminating all the other elements in matched loads. The number of terminated elements used in practice is the same as the number used for providing the central element with a large-array environment. For example, in using dipole radiators above a ground plane, an element in the center of a 7-by-7 array may be taken as typical of an element in a large array.

For an array of open-ended waveguides, a 9-by-9 array should suffice. If there is any position of scanning where a main beam does not form or where a large loss in gain occurs, it will show up as a null in the active-element pattern.

As shown in Eq. (20-35), the gain of a perfectly matched array will vary as the projected aperture area, as given by

$$G(\theta_0,\phi_0) = \frac{4\pi A}{\lambda^2} \eta \cos \theta_0$$
 (20-39)

where the term $|\Gamma(\theta_0,\phi_0)|$ is equal to zero. If we assume that each of the N elements in the array shares the gain equally and $\eta = 1$, the gain of a single element is

$$G_{\epsilon}(\theta,\phi) = \frac{4\pi A}{N\lambda^2} \cos \theta_0$$
 (20-40)

Therefore, the ideal active-element pattern for a perfectly matched array is a cosine pattern.

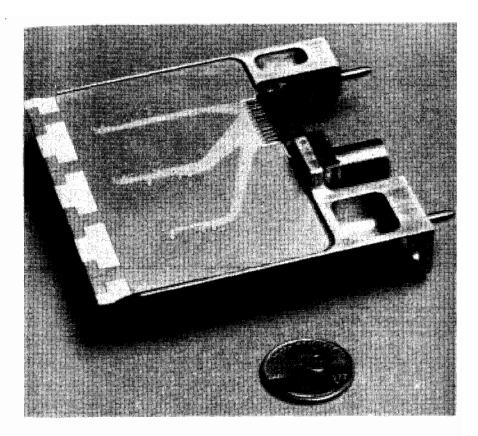
Design Criteria for Radiators

The most commonly used radiators for phased arrays are dipoles, slots, open-ended waveguides (or small horns), spirals, and microstrip disk or patch elements. The selection of a radiator for a particular application must be based upon the following considerations:

- 1 The required area of the element is small enough to fit within the allowable element spacing and lattice without the formation of grating lobes. In general, this limits the element to an area of a little more than $\lambda^2/4$.
- 2 The active-element pattern of the element provides the appropriate aperture matching over the required scan coverage.
- 3 The polarization and power-handling capability (both peak and average power) meet the radar system requirements.
- 4 The physical construction of the radiator must be able to withstand environmental requirements such as thermal, shock, and vibration requirements.
- 5 The radiator must also be inexpensive, reliable, and repeatable from unit to unit since many hundreds or thousands of radiators are required in a large phasedarray antenna.

Since the impedance and the pattern of a radiator in an array are determined predominantly by the array geometry and environment, the radiator may be chosen to best suit the feed system and the physical requirements of the antenna. For example, if the radiator is fed from a stripline or microstrip phase shifter, a stripline or microstrip dipole would be a logical choice for the radiator. An example illustrating the combination of a microstrip dipole and phase shifter is shown in Fig. 20-14. If the radiator is fed from a waveguide phase shifter, an open-ended waveguide would be most convenient. An example of this type is shown in Fig. 20-15. At the lower frequencies, where coaxial components are prevalent, dipoles have been favored for the radiating element. At the higher frequencies, open-ended waveguides and slots are frequently used.

For circular polarization, an open-ended circular waveguide or spiral may be



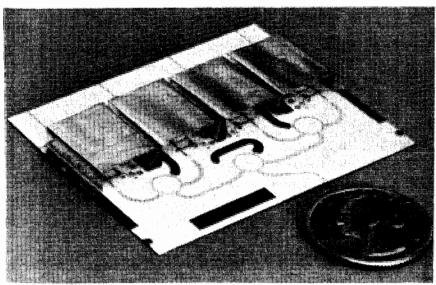


FIG. 20-14 Integrated subarray module containing four dipole radiators, four micromin diode phase shifters, and a power divider.

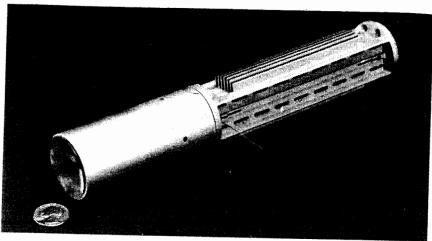


FIG. 20-15 Waveguide radiator and phase-shifter combination.

used. If polarization diversity is required, either crossed dipoles or circular waveguides may be used. With suitable feed networks, both are capable of providing vertical and horizontal polarization independently and may be combined to provide any desired polarization. An example of a dual-polarized circular-waveguide radiator is shown in Fig. 20-16.

Development Procedure for Radiators

After selecting the proper type of radiator on the basis of the criteria as stated above, the next step is to optimize the performance by following the procedure outlined below:

Select an element configuration and spacing that do not support a surface wave which generates grating lobes.

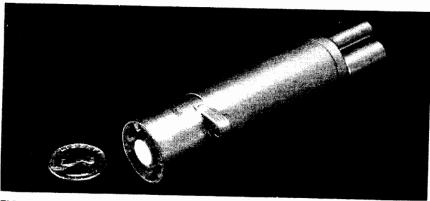


FIG. 20-16 Dual-polarized circular-waveguide radiator.

- 2 Formulate an analytical model of the radiating element in the array aperture, and optimize the performance by varying the design parameters of the radiator such as the spacing between the radiators, the aperture size, or the distance of the radiator above ground. The radiation impedance can be calculated by using modal expansion methods. ^{22,23,24} Furthermore, the aperture matching of the radiator can sometimes be improved by using inductive iris in the opening (aperture) of the waveguide radiator ²² or by using dielectric sheets in front of the radiating aperture. ²³
- 3 Using the analytical results from Step 2, fabricate waveguide simulators²⁰ to measure the radiation impedance at discrete scan angles. The design parameters of the element may have to be modified in order to optimize element performance. This measurement also verifies the calculated results of Step 2.
- 4 Fabricate a small test array and measure the active-element pattern of the central element over the required frequency band. The active-element pattern describes the variation in array gain as a function of beam-scan angle. Large aperture mismatches at any scan angle or scan plane will show up as dips in the active-element pattern.
- 5 The active-element-pattern measurement of Step 4 in conjunction with the impedance measurement of Step 3 establishes the performance characteristics of the final radiator design.

20-4 SELECTION OF PHASE SHIFTERS FOR PHASED ARRAYS

Selection Criteria

Over the past two decades considerable effort has gone into the development of phase shifters for phased-array applications. Only a cursory overview of the results of this work is given in this section. A more expansive description of phase-shifter theory and practice is covered in the literature. 25,26,27,28,29,30

There are currently two types of electronic phase shifters suitable for practical phased arrays: the ferrite phase shifter and the semiconductor-diode phase shifter. Selection of the type of phase shifter to use in a particular application depends strongly on the operating frequency and the RF power per phase shifter. Above S band, waveguide ferrite phase shifters have less loss than diode phase shifters. In situations in which RF powers are low and size and weight constraints dictate a micromin design, diode phase shifters are preferred. Other factors which have a bearing on the selection, if a phased array with a phase shifter per radiating element is assumed, are listed below.

- 1 Insertion Loss Insertion loss should be as low as possible. It results in a reduction of generated power on transmit and of lower signal-to-noise ratio on receive. It also produces phase-shifter-heating problems.
- 2 Switching Time The time to switch should be as short as possible. A long switching time increases minimum radar range when nonreciprocal phase shifters are

used and when a burst of pulses is transmitted in different directions. Times on the order of microseconds are adequate for most applications.

- 3 Drive Power Drive power should be as small as possible. A large amount of drive power generates heat and also may require power supplies that are too large for a mobile system. Large drive power may also require expensive driver-circuit components. Diode phase shifters require holding power as well as switching power. Ferrite phase shifters can be latched; that is, they do not consume drive power except when switching.
- Phase Error Phase error should be as small as possible. It should not reduce antenna gain substantially or raise sidelobes in the radiation pattern. One cause of phase error is the size of the least significant bit of a digital phase shifter. Other phase errors are due to manufacturing tolerances in the phase shifter and driver.
- Transmitted Power: Peak, Average The required power per phase shifter depends upon the maximum radar range and data rate of the system design. Typical values are from 1 to 100 kW peak and 1 to 500 W average. Power levels above 10 to 15 kW peak generally require a ferrite device.
- **Physical Size** The phase shifter should fit within a $\lambda/2$ -by- $\lambda/2$ cross section so that it can be packaged behind each element; otherwise an expensive fan-out feed is required.
- 7 Weight Phase-shifter weight should be minimized in mobile, and especially in airborne or spacecraft, installations.
- Cost and Manufacturing Ease For arrays with thousands of elements the unit 8 cost must be low. Manufacturing tolerances must be as large as possible, consistent with allowable system phase and amplitude errors.

Figure 20-17 compares ferrite and diode phase shifters as a function of operating frequency and insertion loss. In general, ferrite devices have higher power capacity with less loss above S band. Diode phase shifters predominate at the lower microwave frequencies.

Ferrite Phase Shifter

Construction of ferrite phase shifters falls into two general categories: those phase shifters enclosed by a waveguide structure and those built by using a microstrip configuration. While the construction of the microstrip ferrite phase shifter is extremely simple, the performance of the waveguide ferrite phase shifter is far superior, and this phase shifter is generally used for most applications.

Ferrite phase shifters use ferrimagnetic materials that include families of both ferrite and garnets which are basically ceramic materials with magnetic properties.

Ferrite phase shifters can be either nonreciprocal or reciprocal. The toroidal phase shifter is the best example of the nonreciprocal type, and the Reggia-Spencer and Faraday rotator phase shifters are the best representatives of reciprocal ferrite

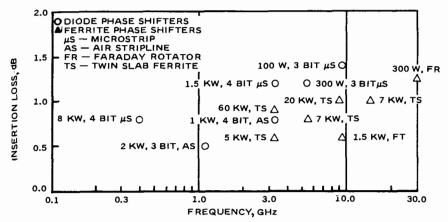


FIG. 20-17 Insertion loss of Hughes Aircraft Company diode and ferrite phase shifters at various frequency bands.

phase shifters. When nonreciprocal phase shifters are employed in a system that uses a single antenna for both transmitting and receiving, the device must be switched between these two modes of operation. This is accomplished by rapidly switching the phase shifter to the receiving state with a driving pulse w. se polarity is opposite that used in the transmitting state.

Toroidal Phase Shifter This nonreciprocal phase shifter uses a toroid geometry which consists of a ferrimagnetic toroid located within a section of waveguide as shown in Fig. 20-18. This phase shifter is sometimes referred to as a twin-slab device since phase shift is provided by the vertical toroid branches (parallel to the E field), while the horizontal branches are used to complete the magnetic circuit. The toroid is threaded with a drive wire, which in turn is connected to a driving amplifier that can supply either a positive or a negative current pulse. When the wire is pulsed with a current of sufficient amplitude, a magnetic field that drives the toroid material into saturation is produced. When the pulse is released, the material becomes latched at one of the two remanent-induction points, $+\beta_r$ or $-\beta_r$, depending on the polarity of the pulse.

The two remanent states of magnetization due to the positive and negative pulses correspond to a different electrical length, the difference being the differential phase shift. The electrical length for a forward-traveling wave latched to one state is the same as that for a backward-traveling wave latched to the opposite state. A complete digital phase shifter (Fig. 20-19) contains several lengths of ferrites adjusted to give differential phase shifts of 180°, 90°, 45°, etc., depending on the number of bits required.

This basic construction can be extended to an analog latching phase shifter by using the same toroid cross section as for the digital latching device and replacing the various toroid bits with a single toroid capable of producing at least 360° of phase

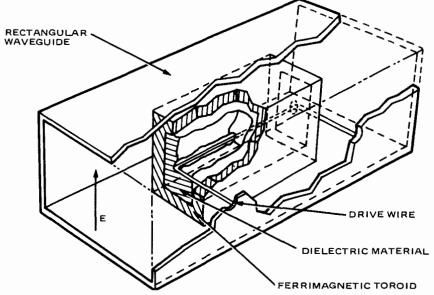


FIG. 20-18 Ferrite toroidal phase shifter.

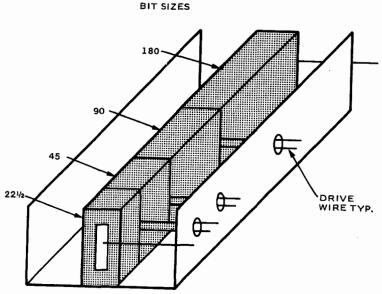


FIG. 20-19 Digital ferrite phase shifter using toroids.

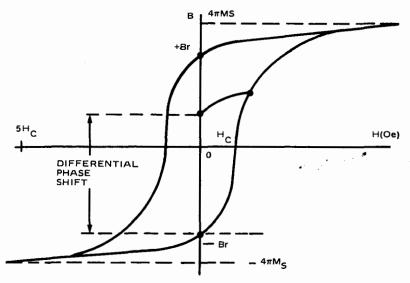


FIG. 20-20 Toroid *B-H* magnetic hysteresis loop illustrating the characteristics of drive.

shift. Phase shift is obtained by first pulsing the drive wire with a *clear* pulse (to set the induction at $-\beta$, and eliminate hysteresis errors), followed by a *set* pulse of opposite polarity. The set pulse raises the level of magnetization, and, when released, the magnetization falls back to the H=0 line, as shown in Fig. 20-20. Since the amount of partial remanent magnetization depends on the amplitude of the set pulse and since phase shift depends on magnetization, an analog phase-shifting device is achieved.

Because the device always operates at partial remanent-magnetization levels, it can be readily adapted to a flux-drive technique. Flux driving tends to minimize the temperature sensitivity of a phase shifter that would normally be dependent on the temperature sensitivity of the material. It is particularly useful for applications requiring high average power or wide ambient-temperature variations.

Reggia-Spencer Phase Shifter The Reggia-Spencer reciprocal phase shifter, shown in Fig. 20-21, consists of a bar of ferrimagnetic material located axially within a section of waveguide. A solenoid is wound around the waveguide, and when energized with a current, it produces a longitudinal magnetic field. The magnetic field causes a variation in the permeability of the material, which in turn produces a variation in the propagation constant of the RF energy. This results in an RF phase shifter whose phase shift can be controlled by a driving current.

When compared with latching ferrite phase shifters, the Reggia-Spencer device has disadvantages in terms of switching time and switching power. Switching time is increased by the large inductance of the solenoid and by the shorted-turn effect of the waveguide within the solenoid. Switching time is further increased since a saturation

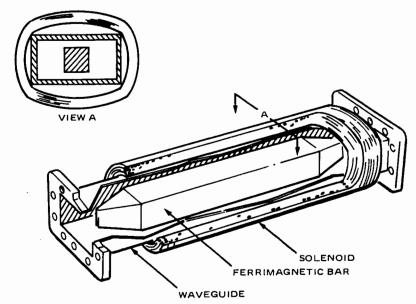


FIG. 20-21 Typical Reggia-Spencer phase-shifter configuration.

pulse must be applied to the phase-shifter solenoid before the next value of phase-shift-setting current is applied to eliminate hysteresis errors.

Because the device is nonlatching, holding currents must be employed, resulting in a relatively high drive-power requirement. As an example, at a switching rate of 500 Hz, the input drive power for an S-band Reggia-Spencer phase shifter is 21 W, whereas the input drive power for an S-band toroidal digital latching phase shifter is only 2.2 W.

Faraday Rotator Phase Shifter This reciprocal phase shifter uses a Faraday rotator section in conjunction with quarter-wave plates at each end. The device employs a small, square waveguide completely filled with ferrite. The metal walls are plated directly on the ferrite bar. An axial coil is wound around the waveguide. The magnetic circuit is completed externally to the thin waveguide wall with ferrimagnetic yokes (Fig. 20-22). The total magnetic circuit has only the small gap of the plated waveguide wall; thus the device is latching, since high remanent magnetization is produced when the magnetizing pulse is reduced to zero.

From a microwave RF viewpoint the device consists of a phase-shift section with a nonreciprocal quarter-wave plate at each end. The nonreciprocal quarter-wave plate converts energy in a rectangular waveguide to either right- or left-hand circularly polarized energy in a quadratically symmetric waveguide, depending on the direction of propagation. The insertion phase of the energy is changed by a variable axial magnetic field supplied by the coil around the waveguide.

Semiconductor-Diode Phase Shifters

Digital diode phase shifters use a diode junction of the pin type as the control element in a microwave circuit. The pin diode can have high breakdown voltage and can be

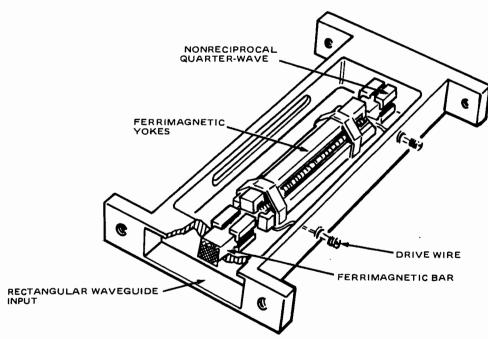


FIG. 20-22 Reciprocal Faraday rotator phase shifter.

designed to have relatively constant parameters in either of two states, forward or reverse bias. It is therefore used in high-power digital phase shifters and is switched between forward and reverse bias. Switching times for diode phase shifters vary from a few microseconds with high-voltage diodes to tens of nanoseconds with low-voltage diodes.

Physically, the pin diode consists of a region of high-resistivity (intrinsic) silicon semiconductor material situated between thin, heavily doped, low-resistivity p^+ and n^+ regions, as shown in Fig. 20-23. The intrinsic region, which may have a volume resistivity of 200 to 3000 Ω -cm, behaves as a slightly lossy dielectric at microwave frequencies, and the heavily doped regions behave as good conductors. In either the unbiased or the reverse-biased state the diode equivalent circuit is a fixed capacitance in series with a small resistance, which varies somewhat with bias. The resistance increases with decreasing reverse bias and rises to a maximum value at a forward-bias voltage equal approximately to the barrier potential of the semiconductor, which is about 0.5 V for silicon (Fig. 20-24). The peak-resistance value is approximately equal to one-half of the reactance of the reverse-biased diode. At larger forward biases a plasma floods the intrinsic region, producing low resistance.

With the addition of external reactive tuning elements, as shown in Fig. 20-25, switching action between forward and reverse bias results; that is, the impedance presented between the network terminals varies between large and small values. The tuning elements can be arranged to give either an open or a closed switch in either bias state. A capacitor in series with the diode gives a *forward-mode* switch or an RF short circuit in forward bias. A *reverse-mode* switch, producing an RF short circuit in reverse bias, is obtained by adding an inductance in series with the diode.

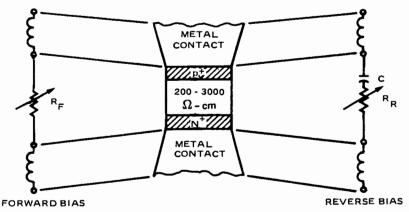


FIG. 20-23 Electrical equivalent circuit of a pin diode.

The performance of a phase shifter is specified in terms of loss, power-handling ability, bandwidth, and switching time. These parameters can be related directly to the basic diode switch.

For all circuits the loss of a diode switch varies directly as the operating frequency and inversely as the diode cutoff frequency f_c , which is defined as

$$f_c = \frac{1}{2\pi C \sqrt{R_R R_F}}$$
 (20-41)

where C is the microwave capacitance in reverse bias and R_R and R_F are the reverse and forward series resistances at the chosen bias levels. The variation of loss within a given band is not severe, but this relation indicates that the diode loss increases for the higher-frequency bands. Typical cutoff frequencies for high-voltage pin diodes range from 250 to 700 GHz.

The diode cutoff frequency is also a function of peak-power level because of high-level limiting in reverse bias, causing an increase in R_R . This occurs when the forward excursion of an applied RF voltage swings into the region of high resistance near zero bias. This effect is illustrated in Fig. 20-26. Under small RF signals the average resistance per cycle is small; thus no limiting occurs. With large signals the average RF series resistance increases because of the positive cycle of the RF voltage swinging into the high-series-resistance region near zero bias, and the switch loss will rise. The pin diode does not switch into the conducting or forward-biased state at microwave frequencies because the time required to create a plasma in the intrinsic region is of the order of the diode switching time, which is approximately 1 μ s.

The maximum peak power that a diode can handle, without consideration being given to junction heating, is limited by the diode breakdown voltage. A generally safe procedure is to limit the sum of the RF voltage amplitude and bias level to a value less than the direct-current breakdown voltage. For some pin diodes, the sum of the two voltages can exceed the direct-current voltage rating without producing breakdown. This occurs when the direct-current breakdown is determined by a diode surface effect, which is slow to produce breakdown as compared with the length of an RF cycle. The operating RF voltage rating of a particular pin diode is a function of

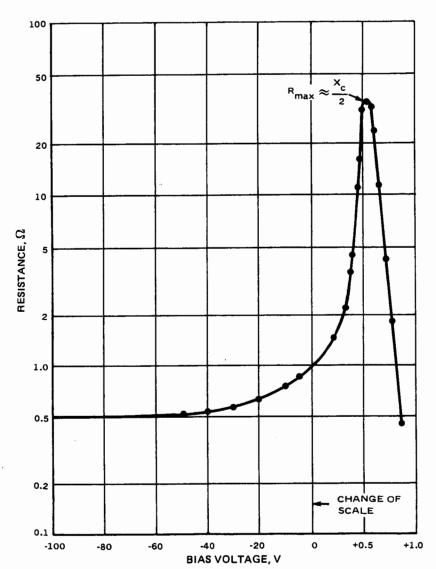


FIG. 20-24 Series resistance versus bias voltage for Microwave Associates silicon pin diode Type MA 4573 at 3.2 GHz; capacitance at -100 V bias = 0.75 pF.

diode construction, temperature of the device, pulse length, and operating frequency and generally must be determined experimentally.

The average-power rating of pin diodes is primarily determined by the temperature rise of the junction, which in turn depends on the diode heat sink and power dissipated.

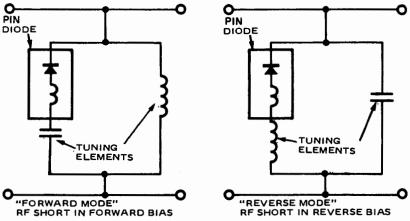


FIG. 20-25 Basic diode switching circuits.

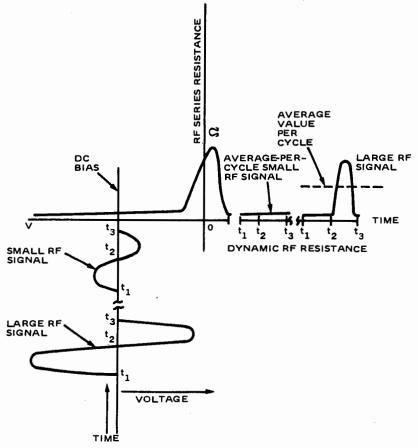


FIG. 20-26 High-level limiting in reverse-biased pin diodes.

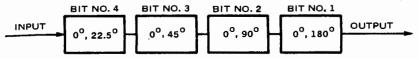


FIG. 20-27 Schematic of transmission 4-bit phase shifter.

Diode Phase-Shifter Circuits A schematic diagram of a general 4-bit phase shifter which gives 16 steps in increments of 22.5° is shown in Fig. 20-27. Any of the phase bits in the figure may take on three basic circuit forms (shown below):

- 1 Switched-line phase bit (Fig. 20-28)
- 2 Hybrid-coupled phase bit (Fig. 20-29)
- 3 Loaded-line phase bit (Fig. 20-31)

In the loaded-line-circuit form a phase bit may consist of a number of identical sections. The choice of circuit form of the phase bit depends on factors such as the number of diodes required, power level, insertion loss, and fabrication ease, which relates to cost. A comparison of these three circuit forms with regard to their loss and peakpower capacity is given in Table 20-6. For comparison purposes a minimum-loss condition has been assumed for all circuit forms. This implies equal loss in each bit state.

Table 20-7 compares the diode loss and number of diodes required for 4-bit-transmission phase shifters. The loss of the entire phase-shifter package will be greater than these values since the circuit loss must be added.

Switched-Line Phase Bit The switched-line phase shifter is shown in Fig. 20-28. This circuit consists basically of two single-pole, double-throw switches and two line lengths for each bit. The minimum number of diodes per bit is four. The line lengths are arbitrary; hence the circuit can be used for either a 0° to 360° phase shifter or a time delayer. The isolation per switch in the off branch must be greater than about 20 dB to avoid phase errors and sharp loss peaks,³¹ which are due to a resonance effect occurring between the off diodes for critical line lengths of multiples of approximately $\lambda/2$.

TABLE 20-6 Comparison of Diode Phase-Bit Types for Peak Power and Diode Loss

	Loaded line			
	Stub- mounted	Mounted in main line	Hybrid- coupled	Switched ilne
Peak-power capacity*	$\frac{V_d^2}{8Z_0\sin^2\!\!\frac{\phi}{2}}$	$\frac{V_d^2}{8Z_0}$	$\frac{V_d^2}{4Z_0\sin^2\!\!\frac{\phi}{2}}$	$\frac{V_d^2}{2Z_0}$
Loss, dB	Je 2	$17.4 \frac{f}{f_c} \tan \frac{\phi}{2}$ (per section)	Je 2	$17.4 \frac{f}{f_c}$ (per bit)

^{*} V_d = peak radio-frequency voltage rating of diode; ϕ = phase shift.

TABLE 20-7 Theoretical Diode Loss and Number of Diodes Required for 4-Bit Transmission Phase Shifters of Different Types

	Loaded line*	Hybrid-coupled	Switched Ilne
Total diode insertion loss	$52\frac{f}{f_c}$	$40\frac{f}{f_c}$	$69\frac{f}{f_c}$
Number of diodes	30	8	16

^{*}Fifteen sections of 22.5" phase shift each are assumed.

Hybrid-Coupled Bit The hybrid-coupled-bit phase shifter (Fig. 20-29) has a 3-dB hybrid junction with balanced phase bits connected to the coupled arms. Alternatively, a circulator with a single phase bit could be used if a nonreciprocal phase shifter is desired. The breakdown voltage required of the diodes depends on the bit size in which the diode is used, if equal power incident on all cascaded bits is assumed. The requirement is highest for the 180° bit but is reduced by a factor of $\sqrt{\sin(\phi/2)}$ for smaller bits. Insertion loss is also a function of bit size. If the loss of the 180° bit is L_0 , the loss of the smaller bits is $L_0 \sin(\phi/2)$. The hybrid-coupled-bit phase shifter has the least loss of the three types and uses the smallest number of diodes.

An analysis for the hybrid-coupled 180° phase bit shows that the peak-power capacity and optimum impedance level for equal loss in both switch states are given by

$$P = \frac{1}{4} \frac{V_d^2}{Z_0} = \frac{1}{4} \frac{V_d^2}{X_c} \sqrt{\frac{R_R}{R_F}}$$
 (20-42)

$$Z_0 = X_c \sqrt{\frac{R_F}{R_R}}$$
 (20-43)

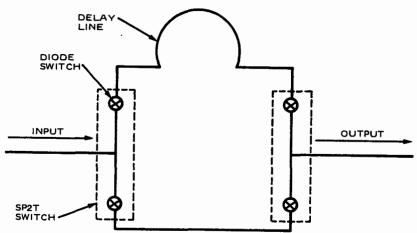


FIG. 20-28 Switched-line phase bit.

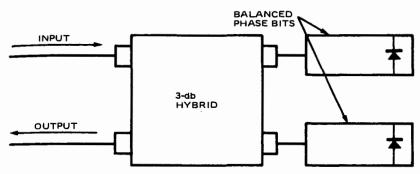


FIG. 20-29 Hybrid-coupled phase bit.

This shows that to obtain high-power capacity, high capacitance, and high breakdown voltage pin diodes operating at low impedance levels should be used.

The shorter bits can be obtained from the 180° bit by using the transformedswitch method.³² This approach maintains equal loss in the two states of the bit and also gives less loss and greater peak power as the phase-step size is decreased. The transformed-switch method can also be designed to give either a constant or a linear phase-frequency characteristic. The transformed-switch technique in concept uses an ideal transformer placed an eighth wavelength in front of the 180° bit (Fig. 20-30). The impedance-transformation ratio of the transformer is varied to produce the various phase-bit sizes.

Loaded-Line Phase Bit The loaded-line circuit uses switched loading susceptances spaced a quarter wavelength along a transmission line (Fig. 20-31). Adjacent loading susceptances are equal and are switched into either a capacitive or an inductive state. Impedance-matched transmission for both states is maintained by correctly choosing the impedance level of the transmission-line section between diodes.

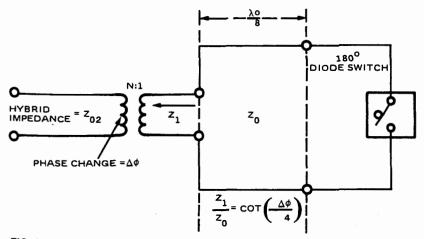


FIG. 20-30 Transformed-switch circuit.

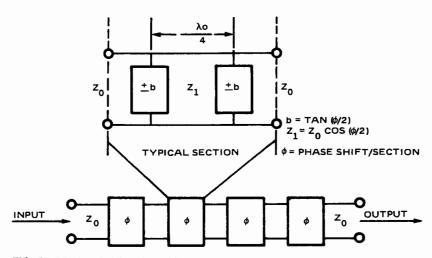


FIG. 20-31 Loaded-line phase bit.

The diodes can be either directly mounted or stub-mounted across the main line.33 In the directly mounted configuration no peak-power advantage is achieved by using many small phase steps. Power in this circuit is limited by the breakdown voltage of the diode and the level to which the characteristic impedance of the line can be reduced, as indicated in Table 20-6. In the stub-mounted configuration the diode switches are mounted in shunt stubs which are in shunt with the main line. The peakpower capacity for the configuration, as shown in Table 20-6, is a function of the voltage rating of the diode and phase-step size. For equal insertion loss in each state of the phase step, the peak-power capacity for the loaded-line phase shifter is one-half of that of the hybrid-coupled-bit design. The insertion loss of n small steps cascaded to give 180° phase shift is $\pi/2$ times as great as the loss of the 180° hybrid-coupledbit circuit. To achieve high-power capacity the loaded-line phase-shifter circuit uses many diodes and small phase increments. In applications in which maximum peakpower capacity is not a primary goal, the number of diodes can be greatly reduced. The phase-shifter design then reduces to a filter problem, and the number of diodes required becomes a function of the maximum voltage standing-wave ratio (VSWR) permitted in the phase-shifter passband.

Performance Characteristics

Ferrite Phase Shifter Table 20-8 compares the performance of two types of toroidal analog latching phase shifters. The low-power unit uses air cooling and is rated at 10 kW peak and 100 W average. The high-power unit uses liquid cooling and has a power capacity of 100 kW peak and 400 W average. Insertion losses for these types of units are generally under 1 dB at operating frequencies at X band and below.

Figure 20-32 shows an early high-power S-band Reggia-Spencer phase shifter. This unit used cold-plate liquid cooling and was rated at 50-kW peak and 150-W average power. Figure 20-33 shows a direct liquid-cooling technique³⁴ using a Teflon encapsulating jacket around the Reggia-Spencer phase-shifter ferrite bar. Table 20-9 lists the characteristics of these devices at S and C bands.

TABLE 20-8	Performance	Characteristics	of a Low- and a
High-Power To	roidal Analog	Latching Phase	Shifter*

	Low power	High power	
Frequency	5.4–5.9 GHz	5.4-5.9 GHz	
Maximum phase shift	360°	360°	
Phase-shift increments	5 % *	22.5*	
Peak power	10 kW	100 kW	
Average power	100 W	400 W	
Type of cooling	Natural convection	Liquid-cooled cold	
Insertion loss	0.7 dB	0.9 dB	
VSWR	1.20 max	1.25 max	
Switching time	10 μs	10 μs	
Switching energy	800 μJ	950 µJ	

^{*}Courtesy of Hughes Aircraft Company.

Table 20-10 shows the typical performance of Faraday rotator phase shifters. One is an S-band liquid-cooled 110-kW-peak device,³⁵ and the other is an air-cooled X-band unit. The insertion losses for the two units are 1.0 and 0.9 dB respectively.

Semiconductor-Diode Phase Shifters Figure 20-34 shows a typical air-stripline-diode-phase-shifter module. The unit consists of a 4-bit phase shifter, a power divider, and an additional subarray steering bit, all integrated in a common package. The 4-bit phase shifter uses hybrid-coupled circuits for the three larger bits and a loaded-line circuit for the small bit. The unit is rated at 1 kW peak, 40 W average.

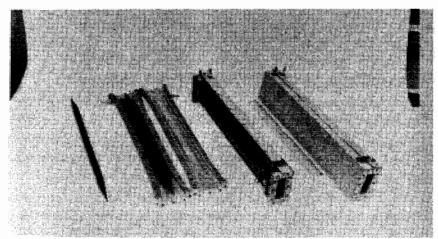


FIG. 20-32 An S-Band Reggia-Spencer phase shifter, the first large-scale application of ferrite phase shifters used in the AN/SPS-33 phase-frequency electronic-scanning radar system. The unit had an insertion loss of 1.6 dB and was rated at 50-kW peak and 150-W average power.

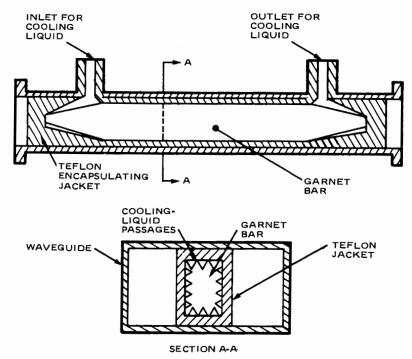


FIG. 20-33 Direct dielectric liquid-cooling technique used for high-average-power handling. (After Ref. 34.)

TABLE 20-9 Typical Parameters of S- and C-Band High-Power Reggia-Spencer Phase Shifters*

	S Band	C Band
Frequency	2.95-3.25 GHz	5.275-5.725 GH ₂
Maximum phase shift	360°	360°
Phase-shift increments	Analog	Analog
Peak power	60 kW	110 kW
Average power	600 W	600 W
Type of cooling	Direct dielectric liquid	Direct dielectric
Insertion loss	1.0 dB	0.9 dB
VSWR	1.20 max	1.25 max
Switching time	700 μs	125 μs
Switching power at 300-Hz switching rate	19 W	16 W

^{*}Courtesy of Hughes Aircraft Company.

TABLE 20-10	Typical	Performance	of	Faraday
Rotator Phase S	nifters			

	S band, high power	X band, low power	
Phase shift	360°	360°	
Bandwidth	3 percent	10 percent	
Peak power	110 kW	1.5 kW	
Average power	1500 W	15 W	
Type of cooling	Liquid	Air	
Insertion loss	1.0 dB	0.9 dB	

^{*}After Ref. 35.

Figure 20-35 shows a low-power 5-bit integrated-circuit phase shifter using a microstrip construction. Switched lines are used for the 3 large bits, and series-coupled loaded-line circuits are used for the 2 smaller bits. The main advantage of this type of unit is size: 1 by 2 in (25.4 by 50.8 mm). The average insertion loss is 1.8 dB.

Figure 20-36 shows a 4-bit C-band loaded-line phase shifter. A total of 30 diodes mounted in shunt stubs are used. The unit has a peak power capacity of 15 kW and

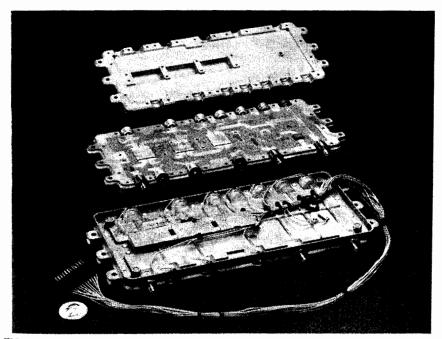


FIG. 20-34 Air-stripline-diode-phase-shifter module. The unit incorporates a 4-bit phase shifter, a power divider, and an additional loaded-line bit in one package. A total of 10 pin diodes are used.

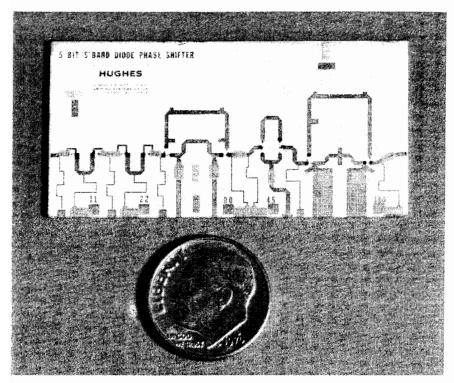


FIG. 20-35 Five-bit micromin phase shifter fabricated with thick film printing on a 1- by 2-in (25.4- by 50.8-mm) alumina substrate. The 3 long bits are frequency-compensated switched-line circuits, and the 2 short bits use series-coupled loaded-line circuits. A total of 16 pin diodes are used in the device.

200 W average. This phase shifter operates over a 15 percent bandwidh with an average insertion loss of 1.3 dB.

Figure 20-37 shows an ultrahigh-frequency phase shifter using a microstrip construction on a low-dielectric-constant substrate. The unit uses hybrid-coupled circuits for the 90° and 180° bits. Loaded-line circuits are employed for the 22° and 45° bits. The unit operates at a peak power of 8 kW, 240 W average, with an insertion loss of 0.7 dB.

20-5 FEED-NETWORK DESIGN FOR PHASED ARRAYS

This section presents a survey of the various methods of feeding the array elements to form the required beam patterns in space. For simplicity, linear-array configurations will be used as illustrations. Extrapolation to a planar array can be accomplished either with a single technique or by using a combination of two different techniques, for example, one technique for rows and the other for columns. In general, most of the beam-forming feeds for phased arrays can be categorized into two basic groups,

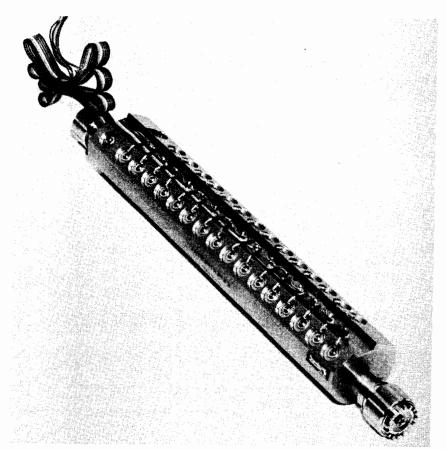


FIG. 20-36 Four-bit C-band coaxial loaded-line phase shifter. The unit uses 30 diodes mounted in shunt stubs along the main transmission line. The power capacity is 15 kW peak, 200 W average. (Courtesy of J. F. White, M/A-COM, Inc.)

(1) optical space feeds and (2) constrained feeds. A description of the various types of feeds in each of these groups is given below.

Optical Space Feeds

Illumination of the array elements in an optically space-fed antenna is accomplished by optically distributing the source signal (transmitter) through space, illuminating an array of pickup horns (elements) which are connected to the radiating elements. The advantage of an optical beam-forming feed over the constrained-feed system is simplicity. Disadvantages are a lack of amplitude-tapering control and an excessive volume of physical space required to accommodate the feed system. Two basic types of optical space feeds, the transmission type and the reflection type, are shown in Fig. 20-38.

In the transmission type, the array elements are the radiating elements of a feed-

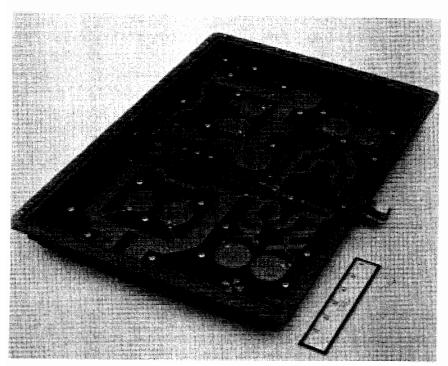


FIG. 20-37 UHF diode phase shifter with cover removed. A microstrip circuit on a %-in-(3.18-mm-) thick low-dielectric-constant board is used. A total of eight diodes are used in the circuit.

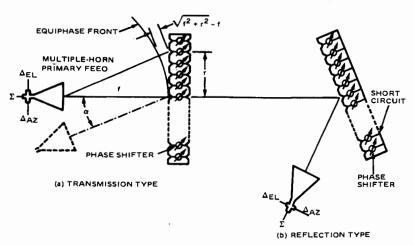


FIG. 20-38 Optical space feeds.

through lens as shown in Fig. 20-38a. These radiating elements are coupled to the pickup elements of the feed-through lens by phase shifters. Both surfaces of the lens require matching to optimize performance. The pickup surface is illuminated by a primary feed placed at a focal distance f behind the lens. The radiation pattern of the primary feed must be optimized to provide an efficient aperture illumination with little spillover loss. If desired, separate transmit and receive feeds may be used, with the feeds separated by an angle α as shown in Fig. 20-38a. The antenna is then rephased between transmitting and receiving so that in both cases the beam points in the same direction. The phasing of the antenna must include a correction for the spherical phase front of the feed. The required phase correction is given by

$$\phi_c = \frac{2\pi}{\lambda} \left(\sqrt{f^2 + r^2} - f \right) = \frac{\pi}{\lambda} \frac{r^2}{f} \left[1 - \frac{1}{4} \left(\frac{r}{f} \right)^2 + \cdots \right]$$

With a sufficiently large focal length, the spherical phase front may be approximated by that of two crossed cylinders, permitting the correction to be applied simply with row and column steering commands. The correction of the spherical phase front can be accomplished by the phase shifters. Space problems may be encountered in assembling an actual system, especially at higher frequencies, since all control circuits must be brought out at the side of the aperture. Multiple beams may be generated by adding additional primary feed horns. All the multiple beams will be scanned simultaneously by equal amounts in $\sin \theta$ space. Monopulse sum-and-difference patterns may be generated by taking the sum and difference of two adjacent multiple beams with a magic T or by using multimode feed horns.

In the reflection type, the phased-array aperture is used as a reflector as shown in Fig. 20-38b. The same radiating element collects and reradiates the signal after it has been reflected from the short circuits terminating the phase shifters. The phase of the reflected signal is determined by the phase-shifter setting. The phase shifter must be reciprocal so that there is a net controllable phase shift after the signal passes through the device in both directions. This requirement rules out nonreciprocal phase shifters. Ample space for phase-shifter control circuits exists behind the reflector. To avoid aperture blocking, the primary feed may be offset as shown. As in the case of a transmission lens, transmit and receive feeds may be separated and the phases separately computed for the two functions. Multiple beams are again possible with additional feeds.

To achieve more precise control in amplitude tapering, a multiple-beam feed array, instead of a single feed horn, must be used to illuminate the feed-through lens. One approach is shown in Fig. 20-39, in which the output of a multiple-beam Butler matrix is used to feed the radiating elements of a feed array. 36,37,38 Each input terminal of the multiple-beam Butler matrix controls effectively the amplitude illumination of a portion of the feed-through lens (radiating aperture). Hence, the amplitude tapering across the array aperture can be controlled by adjusting the signal levels at the inputs of the multiple-beam Butler matrix. The feed system also provides wide instantaneous bandwidth (\sim 10 percent) by using time-delay phase shifters at the inputs to the multiple-beam matrix.

Constrained Feeds

The various types of constrained feeds can be classified into two groups: the series feeds and the parallel feeds. In each group, the feeds can be designed to provide either

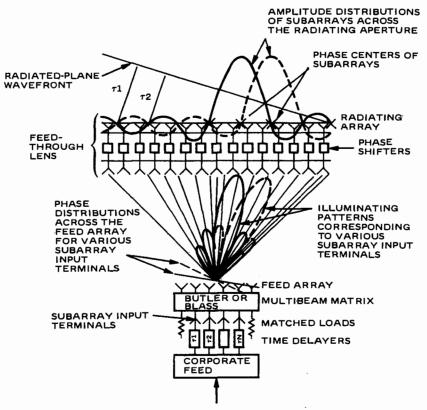


FIG. 20-39 Wide instantaneous-bandwidth feed system using completely overlapped subarrays.

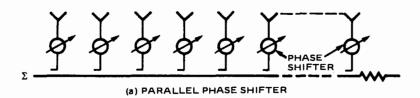


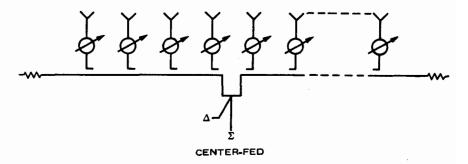


FIG. 20-40 End-fed series feeds.

a single pencil beam or monopulse sum-and-difference beams. A description of the various types of feeds in each group follows.

Series Feeds Figure 20-40 illustrates several types of series feeds. In all cases the path length to each radiating element must be computed as a function of frequency and taken into account when setting the phase shifter. Figure 20-40 a and b illustrates two examples of end-fed serial feed systems in which the elements are arranged serially along the main line. They consist of a main transmission line from which energy is tapped (in the case of transmission) through loosely coupled junctions to feed the radiating elements. To steer the beam, phase shifters are added in either the branch lines feeding the radiating elements, as shown in Fig. 20-40a, or in the main line, as shown in Fig. 20-40b. The amplitude taper is established by properly designing the couplers at the junctions. For example, if all the junction couplers are identical, the amplitude-taper envelope will be approximately exponential.

Mechanical simplicity is, perhaps, the greatest advantage of these two configurations over others to be discussed. They are easy to assemble and to construct. The configurations are easily adapted to construction in waveguides, using cross-guide directional couplers as junctions. They are potentially capable of handling full waveguide power at the input (within the limitations of the phase shifters). However, they suffer losses associated with the corresponding length of waveguide plus that of the



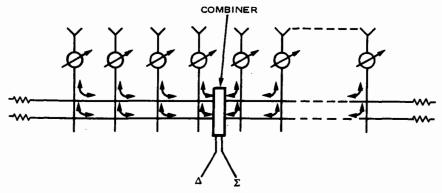


FIG. 20-41 Center-fed series feeds with monopulse sum-and-difference beams.

phase shifters. Perhaps the most severe limitation of this feed system is its dependence of pointing angle on frequency.

The configuration of Fig. 20-40a places lower power-handling demands on the phase shifters and also results in a lower system loss for a given phase-shifter loss. On the other hand, the configuration of Fig. 20-40b has an advantage in that all phase shifters will have identical phase shifts for a given pointing angle—a property which results in simplified array control. However, the total system loss of Fig. 20-40b is higher than that of Fig. 20-40a.

Monopulse sum-and-difference beams can be formed by feeding the array in the middle instead of from the end (see Fig. 20-41 a). This approach, however, would not be able to provide good sum-and-difference patterns simultaneously. For example, if the couplers in the feed are designed to provide low sidelobes for the sum pattern, the resultant pattern for the difference beam would have high sidelobes. At the cost of some additional complexity this sidelobe problem can be solved by the method shown in Fig. 20-41. Two separate center-fed feed lines are used and combined in a network to give sum-and-difference-pattern outputs.³⁹ Independent control of the two amplitude distributions is possible. For efficient operation the two feed lines require distributions that are orthogonal to each other; that is, the peak of the pattern of one feed line coincides with the null from the other. The aperture distributions are respectively even and odd.

The bandwidth of a series feed can be increased by making the path lengths from the input to each output of the branch lines all equal as shown in Fig. 20-42. However, if the bandwidth is already limited by the phase shifters and the couplers, very little benefit can be derived from this approach at the cost of a considerable increase in size and weight. The network of Fig. 20-42 simplifies the beam-steering computation since the correction for path-length differences is no longer necessary.

Parallel Feeds The frequency dependence associated with series feeds can be reduced by the use of parallel feeds at a cost of a slightly more complex mechanical structure. The frequency dependence (change in beam-pointing angle with frequency)

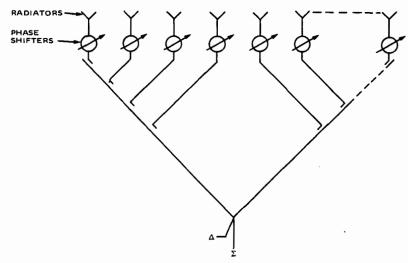
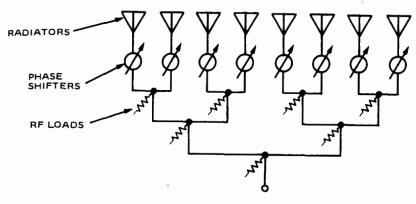


FIG. 20-42 Equal-path-length feed.



(a) CORPORATE FEED

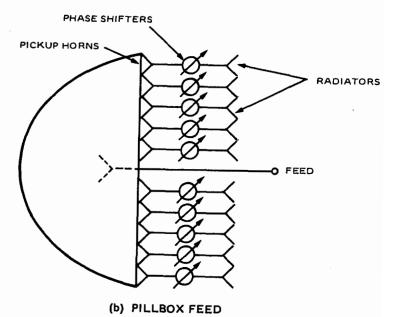


FIG. 20-43 Constrained parallel feeds. (After Ref. 40.)

of parallel-feed configurations depends mainly on the frequency characteristics of the phase shifters and the couplers at the junctions of the feed, if the line lengths from the transmitter to the radiators are all made equal. Thus, if variable time-delay phase shifters were used in place of the constant-phase type of phase shifters at each radiating element, the beam-pointing angle would be essentially independent of frequency. The frequency dependence of a parallel feed using constant-phase-type phase shifters is discussed in Sec. 20-6.

The most common technique for realizing parallel feeds is the matched-corporate-feed structure of Fig. 20-43a. In this configuration, the corporate feed is assem-

bled from matched hybrids (four-port junction devices with the isolated port terminated into matched loads). The out-of-phase components of mismatch reflections from the aperture and of other unbalanced reflections are absorbed in the terminations. The in-phase and balanced components are returned to the input, and power reflected from the aperture is not reradiated. When nonreciprocal phase shifters (the two-way path length through the phase shifter is a constant independent of the phase-shifter setting) are used in place of reciprocal phase shifters at each radiating element, the couplers at the junctions of the corporate feed can be reactive T's (three-port devices) instead of matched hybrids. In this case, however, the reflections from the aperture will add up in phase at the input to the feed. Therefore, a high-power isolator must be used to protect the transmitter and/or a high-power limiter be used to protect the receiver.

In addition to the transmission-line parallel feed, an optical pillbox feed can be used to illuminate an array of pickup elements to feed a linear array as shown in Fig. 20-43b. The array of pickup elements can be matched to the pillbox so that no reflections occur; hence, all the energy is collected by the pickups, and the loss incurred is only the normal RF loss. By the use of a folded pillbox, 40 the feed can be made not to interfere with the pickup structure. If the back surface of the pillbox is made spherical instead of parabolic, the feed can provide many multiple simultaneous beams with the use of multiple feed horns. The cost of substituting the pillbox for a corporate feed is an exchange of a certain amount of freedom in the choice of amplitude tapers and packaging configurations for a simpler mechanical structure.

A method of achieving sum-and-difference monopulse beams for a parallel feed is shown in Fig. 20-44. The signals from a pair of radiating elements, which are located symmetrically opposite from the centerline of the array, are combined in a magic T (matched hybrid) to form their sum-and-difference signals. The sum signals from all the pairs across the array aperture are then combined in a power-combiner network to form a sum beam. The desired amplitude distribution for the sum beam can be achieved by proper weighting of the signals in the power-combiner network. The difference signals from all the pairs are combined in a separate power-combiner network to form a difference beam. Amplitude weighting in the two combiner networks can be made differently to obtain low sidelobes for both the sum and the difference beams. For example, the low-sidelobe amplitude distribution for a sum beam is in the form of a Taylor distribution, whereas a Bayliss distribution is used for low-sidelobe difference beams. ⁴¹ By using this method, independent control of both the sum and the difference beams is achieved.

Multiple-Beam Feeds Another class of constrained feeds for phased arrays consists of the multiple-beam-forming feed networks. These feeds can generate multiple simultaneous beams covering a large sector of space. For the same beam-pointing direction, each beam has essentially the gain of a single-beam array of the same size and illumination except for a possible increase in RF circuit losses over a single-beam array. A separate beam terminal is provided for each beam of the multiple-beam-forming feed network.

Various types of multiple-beam-forming networks can also be classified into two groups: (1) the serial type and (2) the parallel type. One example of a serial multiple-beam-forming feed is shown in Fig. 20-45. This beam-forming network, known as the Blass matrix, ⁴² is based on the serial feed of Fig. 20-40b. To generate multiple beams, several feed lines are coupled to the branch lines by using directional couplers. Each feed line generates one beam in space. If a transmitter is connected to any of the beam

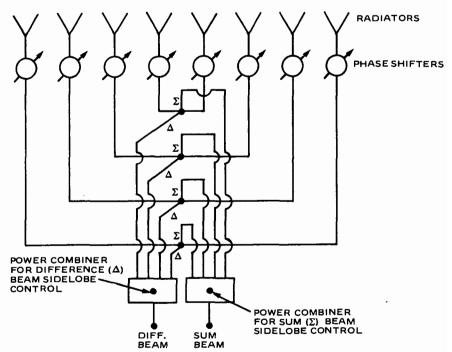


FIG. 20-44 Constrained monopulse feed with independently controllable sum-and-difference-beam sidelobes.

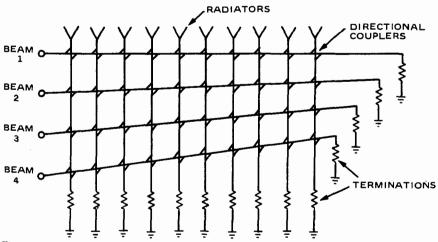


FIG. 20-45 Series-fed simultaneous beam-forming matrix. (After Ref. 42.)

terminals (feed lines), each coupler leaks off a fraction of the input signal in the feed line toward the radiating element connected to that junction in the same manner as the array of Fig. 20-40b. In fact, if it were not for the additional feed lines in front of a given feed line (toward the array aperture), there would ideally be no difference in operation between this configuration and that of Fig. 20-40. However, a portion of the signal coupled toward the radiating element is subsequently coupled into the feed lines in front of the driven feed line. Hence, this cross-coupling effect between the feed lines must be taken into account in the design of this feed network to provide the required amplitude distribution. When the beams corresponding to the feed lines are spaced a beamwidth or more apart, this cross-coupling effect is minimized, the pattern generated by each effect is minimized, and the pattern generated by each feed line is not significantly degraded by the additional feeds. Furthermore, the signals leaked into the other feed line sums very nearly to zero, and very little power is wasted in the terminations.

The phase shift between the radiating elements is governed by the *tilt* of the feed lines. This configuration is particularly adaptable to rectangular waveguides using cross-guide directional couplers. Such a waveguide feed is capable of high-power operation with fairly low RF loss.

A wide-bandwidth version of the Blass matrix is shown in Fig. 20-46. The branch

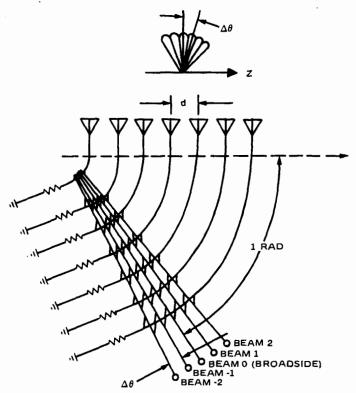


FIG. 20-46 Time-delayed multiple-beam matrix. (After Ref. 42.)

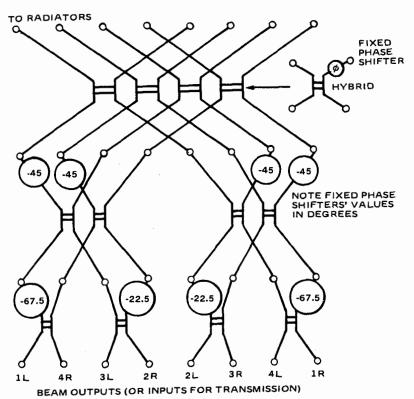


Fig. 20-47 Multiple-beam Butler-matrix feed. (After Ref. 43.)

lines to the radiating elements are circumferences of circles of radii nd. The feed line for the broadside beam is placed at an angle of 1 rad from a line parallel to the antenna face. Additional feed lines are spaced angularly by multiples of $\Delta\theta$, so that the signal travels a different distance $nd\Delta\theta$ to reach the nth radiating element. If the transmission lines have a constant velocity of propagation ν , the beam-pointing angle of the nth beam ψ_m is given by the solution of $\sin \psi_m = c/v(m\Delta\theta)$. When v = c, this feed network becomes a true time-delay feed and the bandwidth is limited only by the directional couplers.

An example of a parallel-fed multiple-beam-forming feed is shown in Fig. 20-47. This feed configuration is commonly known as the Butler-matrix feed. ^{43,44} The feed network uses directional couplers that have a 90° phase-shift property (e.g., branch-line couplers) and fixed phase shifters as indicated in Fig. 20-47.

A signal injected at any of the beam input terminals excites all the radiating elements equally in amplitude with phase differentials of odd multiples of $180^{\circ}/N$, where N is the total number of radiating elements or beam terminals. The array patterns of the beams generated are of the form $\sin Nx/\sin x$ since the amplitude taper is uniform. Specifically, they are

$$E_{m}(\nu) = \frac{\sin\frac{N}{2}\left[kd - (2m+1)\frac{\pi}{N}\right]}{\sin\frac{1}{2}\left[kd - (2m+1)\frac{\pi}{N}\right]}$$
 (20-44)

with N main beams completely covering one period of ν . The beams specified by Eq. (20-44) cross over at a relative amplitude of $2/\pi$ (\approx 4 dB), and the peaks of the beams are located at the nulls of the other beams. Since these beams are orthogonal to each other, there is no cross-coupling loss between beams.

The construction of the parallel multiple-beam configuration is not as straightforward as the construction of the serial type because of the large number of transmission-line crossovers required. If the formation of a large number of beams is desired, the parallel configuration is preferred since it uses fewer couplers for a given number of elements. If N is the total number of radiating elements and B is the number of beams required, the serial configuration requires NB couplers, while the parallel configuration requires essentially $N/2 \log_2 N$ couplers regardless of the number of beams required as long as the total number of beams does not exceed N.

20-6 BANDWIDTH OF PHASED ARRAYS

The bandwidth of a phased-array antenna depends upon the types of components, such as radiators, phase shifters, and feed networks, comprising the array. In practice, most radiators for phased arrays are matched over a broad band of frequencies. Therefore, the radiator design is not a primary factor in the determination of bandwidth. The limitations on bandwidth are determined by the frequency characteristics of the phase shifters and feed networks. As, In general, the effects due to the phase shifters and feed networks are additive, so that if the phase shifter causes the beam to scan by an amount equal to $\Delta\theta_p$ and the feed causes the beam to scan by $\Delta\theta_f$, then the total beam scan is given by $\Delta\theta_p + \Delta\theta_f$. To establish the bandwidth capability of a phased array, these two effects must be examined. A detailed evaluation of the bandwidth limitations of phased arrays is discussed by Frank.

Phase-Shifter Effects

To evaluate the effects caused by the phase shifter alone, a corporate feed (equal-line-length parallel feed) is used to illuminate all the radiating elements (see Fig. 20-48). This corporate feed exhibits no feed effects since a signal at the input illuminates all the radiating elements with the same phase regardless of frequency. The bandwidth in this case is completely determined by the type of phase shifter used in the array. In this discussion, we will consider the effects of two basic types of phase shifters: (1) time-delay phase shifters and (2) constant-phase-type phase shifters. A detailed description of these two types of phase shifters is given in Sec. 20-4.

When time-delay phase shifters are used at each radiating element, the signals received by the elements from an incident wavefront at an angle θ_0 are appropriately time-delayed so that they all arrive at the output terminal of the corporate feed at the same time. For example, the amount of time delay at the first element of the array shown in Fig. 20-48 is equal to the additional time required for the wavefront to travel

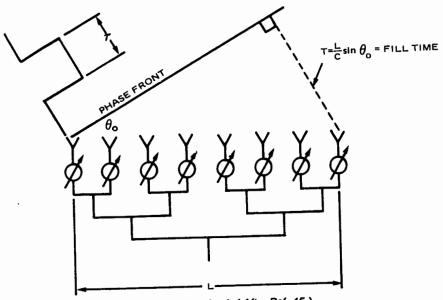


FIG. 20-48 Equal-line-length corporate feed. (After Ref. 45.)

to the last element after arriving at the first element. This time delay T, known as aperture-fill time, is given by

$$T = \frac{L}{c}\sin\theta_0$$

where L = total length of array aperture

c = velocity of light

 θ_0 = angle of incidence of wavefront from array normal

In this case, the phase distribution across the array aperture produced by the time-delay feed matches that of the incident wavefront independently of frequency. Consequently, the beam position remains stationary with frequency change, and the array has infinite bandwidth. When the angle of incidence of the incoming wavefront changes, the amounts of time delays at each element must be changed accordingly to maintain the bandwidth. This time-delayed feed network is commonly known as a time-delayed beam-steering feed. The above discussion is valid for either a CW or a pulsed incidence signal. For the pulsed incidence signal, the time-delay feed preserves the shape of the pulse without any distortion. Various methods of time-delay beam steering are described in Ref. 46.

When constant-phase-type phase shifters (phase shifters whose phase shift is independent of frequency) are used at each element, the output phase distribution of the feed matches that of the incident phase front only at one frequency f_0 and for a particular incidence angle θ_0 . At a different frequency f_1 , the output phase distribution of the feed network remains fixed; hence the array is phased to receive at a difference incidence angle θ_1 . The amount of beam squint with frequency is given by the following relationship:

$$f_1 \sin \theta_1 = f_0 \sin \theta_0 \tag{20-45}$$

For a small change in frequency, Eq. (20-45) shows that the change in scan angle is given by

$$\Delta\theta_0 = -\left(\frac{\Delta f}{f}\right) \tan \theta_0 \tag{20-46}$$

The above expression shows that the amount of beam squint depends upon the original scan angle as well as on the percent frequency change. At broadside ($\theta_0 = 0$), there is no scanning regardless of the amount of change in frequency, and the array has infinite bandwidth. When the beam scans away from broadside, the amount of beam squint with frequency increases with scan angle. Therefore, the bandwidth of an array must be specified in terms of the desired maximum scan angle. For most practical applications, the desired maximum scan angle is $\pm 60^{\circ}$ from array broadside. If we assume that the maximum allowable beam squint is ± 1 quarter beamwidth away from the desired direction, corresponding to a one-way gain loss of 0.7 dB, the bandwidth of the array is given by

Feed Effects

When a feed other than an equal-length parallel feed is used, phase errors due to the feed alone are produced across the array aperture. An example is the end-fed series feed shown in Fig. 20-49. The total phase shift across the length of the feed is $\Phi = (2\pi/\lambda)L$ rad with free-space propagation assumed. When the frequency is changed, the change in phase across the array aperture will be

$$\Delta \Phi = \frac{2\pi L}{c} \Delta f$$

This linear change in phase across the aperture scans the beam just as phase shifters would. To observe just how far the beam is scanned, let us examine the way in which an aperture is scanned with phase. For a given scan angle θ_0 , the required phase across the array is

$$\psi = \frac{2\pi L}{\lambda} \sin \theta_0$$

The required change in ψ for a change in scan angle is

$$\frac{d\psi}{d\theta} = \frac{2\pi L}{\lambda} \cos \theta$$

or

$$\Delta \psi = \frac{2\pi L}{\lambda} \cos \theta_0 \Delta \theta_0 = \frac{2\pi Lf}{c} \cos \theta_0 \Delta \theta_0$$

when the change in phase across the array is induced by the feed, $\Delta \psi = \Delta \Phi$, or

$$\frac{2\pi L}{c}\Delta f = \frac{2\pi Lf}{c}\cos\theta_0\Delta\theta_0$$

Hence the amount of beam scan for a change in frequency is given by

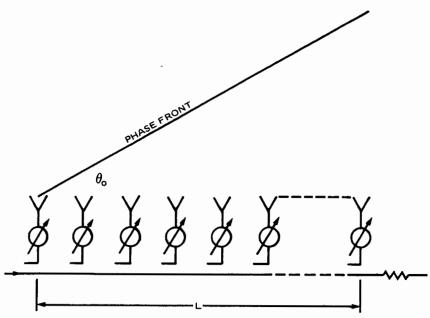


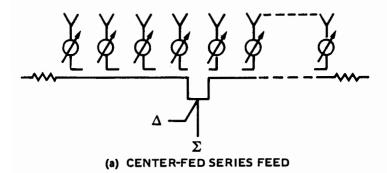
FIG. 20-49 End-fed series feed. (Atter Ref. 45.)

$$\Delta\theta_0 = \left(\frac{\Delta f}{f}\right) \frac{1}{\cos\theta_0} \tag{20-48}$$

For beams scanned in the direction of the feed load, the phase change between the radiating elements due to the feed line is partially offset by the required phase change to maintain the beam position at a given scan angle θ_0 . In fact, for an end-fire beam toward the load, the required phase change with frequency to maintain the beam at end fire is exactly the same as that due to the feed line. Hence, the bandwidth of a series feed at the end-fire-beam position toward the load is infinite. However, this end-fire-beam position is not practical to implement because of the drastic reduction in the gain of the radiating elements. Furthermore, in most applications the array is required to scan in both directions from broadside. For beams scanned in the direction of the feed input, the phase changes in space and the feed line become additive instead of canceling each other. As a result, the beam scans rapidly with frequency. For a 60° scan angle, the scanning caused by the feed alone is slightly greater than that caused by the aperture. Therefore, the bandwidth of the series feed is essentially half of that of the equal-line-length parallel feed.

In waveguide, the signal propagates more slowly; this is equivalent to having a longer feed line. This causes the feed to scan more rapidly, and the series-feed performance degrades accordingly. The slowing in waveguide is proportional to λ/λ_g , and the array scans by

$$\Delta\theta \cong \frac{\lambda_f}{\lambda} \left(\frac{\Delta f}{f} \right) \frac{1}{\cos \theta_0}$$
 rad (20-49)



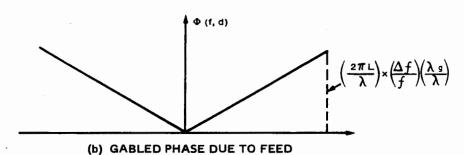


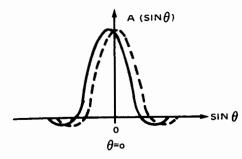
FIG. 20-50 Center-fed series array. (After Ref. 45.)

For $\pm 60^{\circ}$ scanning from broadside, the bandwidth of a series feed under the same conditions as that of a parallel feed is given by

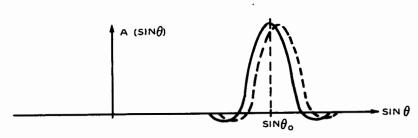
Bandwidth (percent) =
$$\frac{1}{\left(1 + \frac{\lambda_g}{\lambda}\right)}$$
 beamwidth (*) (20-50)

A center-fed series array⁴⁷ as shown in Fig. 20-50a may be thought of as two end-fed series arrays. At band center the phase shifters are set so that all the elements radiate in phase. As the frequency is changed, each half scans in the opposite direction because of the gabled phase slope as shown in Fig. 20-50b. For the broadside-beam case, this results in a broadening of the beam with no change in direction. If the two beams were to move far enough apart (Fig. 20-51), the beams would split. However, by restricting the bandwidth to reasonable values, the result is a loss in gain caused by the beam broadening.

When the array is scanned away from broadside, aperture scanning due to the phase shifter (constant phase with frequency) is also introduced, and it is superimposed on the feed scanning. As shown in Fig. 20-51, for one-half of the array (solid curve) aperture scanning and feed scanning tend to cancel each other, while for the other half (dashed curve) they tend to reinforce each other. The performance of the center-fed array is worse than that of the parallel-fed array at broadside but quite



(a) FEED EFFECTS AT BROADSIDE



(b) APERTURE AND FEED EFFECTS

FIG. 20-51 Aperture scanning superimposed on feed scanning. (After Ref. 45.)

comparable at large scan angles. At a scan angle of 60°, the center-fed array will have approximately ¼ dB more loss than the parallel-fed array. For simplicity, the same bandwidth formula [Eq. (20-47)] can be used for both feeds.

The discussion above has assumed that the center feed used nondispersive transmission with free-space propagation. If waveguide is used, the performance of the center-fed array degrades and the bandwidth is given by

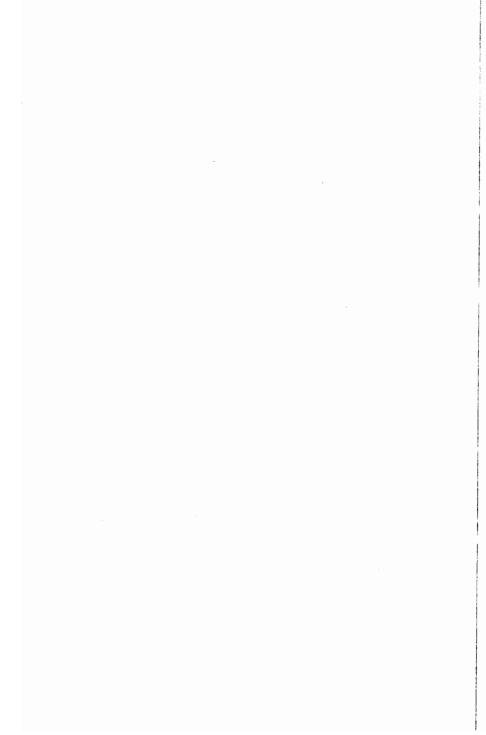
Bandwidth (percent) =
$$\left(\frac{\lambda}{\lambda_s}\right)$$
 beamwidth (degrees) (20-51)

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Conformal and Low-Profile Arrays

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21-1 Introduction 21-2

21-2 Fundamental Principles 21-3
 Properties of Isolated Elements on Finite
 Planes and Cylinders 21-3
 Pattern-Coverage Limitations for Conformal
 Arrays 21-4

Hemispherical Coverage with Fuselage-Mounted Arrays 21-6

21-3 Cylindrical Arrays 21-9

Synthesis of Omnidirectional Coverage 21-9 Element Patterns for Arrays on

Cylinders 21-10

Technology of Arrays Conformal to Cylinders 21-12

Low-Profile Arrays on Cylinders 21-13

Feed Systems and Commutators for

Cylindrical Arrays 21-15

Pattern Synthesis for Cylindrical Sector Arrays

21-4 Elements and Arrays on Conic and Generalized Surfaces 21-18 A number of applications require antenna arrays conforming to a nonplanar surface. Primary among these are requirements for scanning antennas on aircraft or missiles, where aerodynamic drag is reduced for a conformal flush-mounted geometry, and for arrays that conform to surfaces that provide some coverage advantage, for example, to a hemispherical surface for hemispherical-pattern coverage or to a cylinder for 360° coverage in the azimuth plane.

Conformal arrays can be grouped into two broad categories that have very different design goals and present significantly different technological challenges. Arrays in the first category are small with respect to the radius of curvature of the conformed body, as depicted in Fig. 21-1 a. These proportions are representative of flush-mounted and low-profile aircraft arrays at superhigh-frequency (SHF) frequencies and above. Such arrays are relatively flat and behave nearly like planar arrays. The technological problems in this case are to design an array to scan over very wide angles (for example, zenith to horizon) or to make the array so thin that it can conform to the outer surface of the aircraft without requiring large holes in the fuselage.

The second category of conformal arrays, depicted in Fig. 21-1b, is the type more commonly regarded as conformal and is comparable or large with respect to the radius of curvature of the mounting body. Such arrays include cylindrical arrays developed to provide radiation from spinning missiles and for 360° coverage of ground-based radars. Conical and spherical arrays have also been developed for ground, airborne, and missile applications.

Among the special features that make it difficult to design arrays that are large or highly curved in this sense are usually listed^{1,2} the following: (1) Array elements point in different directions, and so it is often necessary to switch off those elements that radiate primarily away from the desired direction of radiation. (2) Conformal-array synthesis is very difficult because one cannot factor an element pattern out of the total radiation pattern. (3) Mutual coupling can be severe and difficult to analyze because of the extreme asymmetry of structures like cones and because of multiple coupling paths between elements (for example, the clockwise and counterclockwise

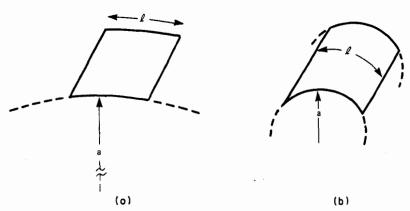


FIG. 21-1 Conformal-array apertures. (a) Aperture dimensions much less than local radius of curvature. (b) Aperture dimensions comparable with local radius of curvature.

paths between elements on a cylinder). (4) Cross-polarization effects arise because of the different pointing directions for elements on curved surfaces, which cause the polarization vector projections to be nonaligned. (5) Even for a cylindrical array there is a need to use different collimating phase shifts in the azimuth plane for an array scanned in elevation because steering in azimuth and elevation planes is not separate. Another phenonemon related to mutual coupling is the evidence of ripples on the element patterns of cylindrical arrays.

21-2 FUNDAMENTAL PRINCIPLES

Properties of Isolated Elements on Finite Planes and Cylinders

As indicated in Chap. 8, radiating elements behave differently according to the structure on which they are mounted. Examples of elementary slot antennas radiating from circular cylinders show significant pattern changes at angles near or below the horizon for a slot located at the top of the cylinder.

Figure 21-2 shows the radiated power pattern in the upper hemisphere ($\theta \le 90^{\circ}$) for an infinitesimal slot in a cylinder of radius a. Using the results of Pathak and

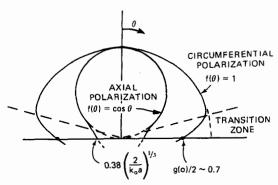


FIG. 21-2 Approximate pattern of slot on cylinder of radius a.

Kouyoumjian,³ one can express the radiation pattern of elementary slots on cylinders in terms of three distinct regions, depending upon whether the point of observation is in the upper hemisphere (called the *illuminated region*), in the lower hemisphere (called the *shadow region*), or in the vicinity of the horizon (called the *transition region*). The angular extent of the transition region is of the order of $(k_0a)^{-1/3}$ on each side of the shadow boundary. Figure 21-2 illustrates that within the illuminated region the circumferentially polarized radiation is nearly constant for an infinitesimal element but that the axially polarized radiation has a $\cos \theta$ element pattern. Moreover, within the transition region these patterns are modified so that the circumferentially polarized component drops to a value of about 0.7 in field strength, or -3.2 dB as compared with its value of zenith, while for axial polarization the horizon radiation is not zero but approximately

 $0.4 \left(\frac{2}{k_0 a}\right)^{1/3}$

Thus, for a thin slot with circumferential polarization the horizon gain is independent of the size of the cylinder, but for an axially polarized slot the horizon gain varies directly as a function of $(k_0a)^{-1/3}$. For cylinders of radius approaching 50λ , the horizon power is thus approximately 23 dB below zenith gain.

Pattern-Coverage Limitations for Conformal Arrays

In addition to the diffraction effects observed in the preceding subsection, purely geometrical effects play a major part in determining the pattern characteristics of conformal arrays. Figure 21-3 shows a conical array of slots from several angles and illustrates the polarization distortion that occurs for an array near the point of a cone. This

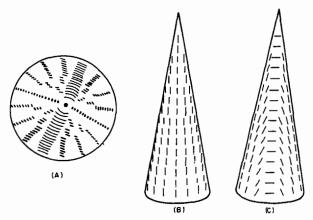


FIG. 21-3 Conical array. (a) View from axial direction. (b) Side view. (c) Side view rotated 90° from b. (After Kummer.1)

figure, due to Kummer, shows three views of a conical array with radiators located along the generatrices and oriented to give linear polarization in the axial direction. Clearly this array would radiate different polarization for each chosen angle of radiation.

Figure 21-3 also shows that for nearly any given radiation angle, especially for angles away from the tip of the cone, only a relatively small number of radiators have element patterns that point in the required direction. It is therefore usually necessary to devise a sophisticated network to switch an illuminated sector to the proper location on the conformal array for efficient radiation. Many such networks have been devised for cylindrical arrays, but the problem is more severe for cones, spheres, and more general surfaces.

Figure 21-4a shows the radiation pattern of several cylindrical arrays compared as a function of the angle subtended by the array. As pointed out by Hessel,⁴ for an array of $k_0a = 86$ with 0.65λ separation between elements, doubling the number of excited elements in the array (from 60° arc to 120° arc) increases the array gain by only about 1 dB because the edge elements do not radiate efficiently toward the beam peak. The large sidelobes near $\phi = 100$ ° are associated with grating lobes of the elements grouped at the array ends.

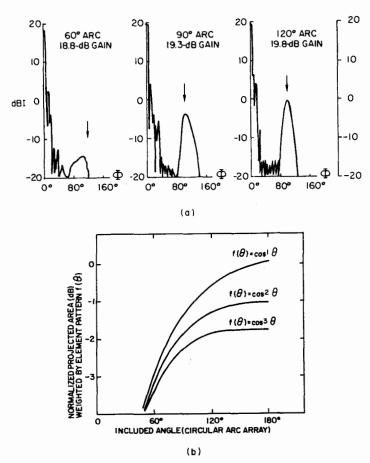


FIG. 21-4 Radiation characteristics of arc arrays. (a) Maximum-gain E-plane patterns for arc array of $k_{0a} = 86$, $b/\lambda = 0.65$. (After Hessel.⁴) (b) Normalized projected area weighted by element patterns.

These results are not equally limiting, for closer element spacing can relieve the grating-lobe problem and can broaden the element patterns, as will be described in Sec. 21-3, but Fig. 21-4b shows that the gain restrictions are fundamental limitations. Consider the projected area of a cylindrical array weighted by the element-pattern radiation in the main-beam direction. In this simple case the optimum $\cos \theta$ and more realistic $\cos^2 \theta$ and $\cos^3 \theta$ element power patterns are assumed, and it is also assumed that the element spacing approaches zero (the continuous-aperture case). The peak forward radiation, normalized to the projected area, is the integral of the $\cos^n \theta$ functions to the maximum θ value and can be considered roughly proportional to gain. Figure 21-4b shows that there is little advantage to exciting much more than a 90° sector of the cylinder.

A second fundamental result obtainable from the same very simplified analysis is that, for a four-faced square array with a perimeter equal to the circular-array circumference, the average gain over a 90°-scan sector, normalized again to the cyl-

inder projected area, is approximately -1.5 dB for a $\cos \theta$ element pattern, -1.9 dB for a $\cos^2 \theta$ element pattern, and -2.3 dB for $\cos^3 \theta$ element patterns. Figure 21-4b shows that these are essentially the same as the gain of a 90°-arc circular array with the same element pattern. A similar result is quoted by Hessel.⁴

The above results are derived for uniformally illuminated arrays. When arrays have severe illumination tapers, as, for example, low-sidelobe arrays, it is possible to occupy larger circular arcs without reduced efficiency because of the low edge illumination.

Hemispherical Coverage with Fuselage-Mounted Arrays

One of the major applications for vehicle arrays is for aircraft-to-satellite communications, for which the antenna system is often required to provide coverage throughout the entire hemisphere, usually with circular polarization and including substantial gain at the horizon. Figure 21-5 shows several options for fully electronically steered arrays, two of which are conformal, while the third is a low-profile four-faced array.

The use of a single array (Fig. 21-5a) is very appealing provided that gain-contour requirements can be met. Unfortunately, this means that the array must scan from zenith to horizon in all planes. The following illustrates some of the gain limitations for an array scanned from zenith to the horizon.

In an infinite two-dimensional array with no grating lobes, the pattern directivity for a perfectly matched aperture varies like $\cos \theta$. If the array mismatch is not corrected as a function of scan angle, the gain will vary according to the expression

$$(1-|\Gamma|^2)\cos\theta$$

For finite arrays the beamwidth in the plane of scan varies much like $\sec \theta$ except near end fire. The elevation beamwidth for an array scanned to 90° (horizon) can be obtained from well-known directivity values⁵ and is given approximately by the equation below for column and two-dimensional arrays:

$$\delta = \sqrt{\frac{4\pi}{C} \left(\frac{\lambda}{L_1}\right)}$$

Here L_1 is the length of the array in the end-fire direction, and C is the constant which varies between 3.5 and 7, depending upon phase velocity and the array distribution. If one assumes an azimuth beamwidth of approximately λ/L_2 , when L_2 is the array dimension perpendicular to the plane of scan, the directive gain at end fire is approximately

$$D = \sqrt{4\pi C} \left(\frac{L_2}{\lambda}\right) \sqrt{\frac{L_1}{\lambda}}$$

Since the directivity is multiplied by 4 for the array over a perfect ground plane (and the beamwidth is halved), the ratio of directive gain at end fire to directive gain at broadside (with perfectly conducting ground) is

$$\frac{D}{D_0} = \sqrt{\frac{C}{\pi}} \sqrt{\frac{\lambda}{L_1}}$$

This equation shows that for any given broadside directive gain D_0 it is advantageous to reduce L_1 (the array projection in the end-fire direction) as much as possible, for this minimizes scan loss. It also indicates that larger arrays undergo increased scan loss. For example, a square array with 20-dB gain at broadside should

exhibit a directivity degradation of 1 dB at end fire, but for a 30-dB square array a 4.5-dB falloff is expected.

Unfortunately this decrease in directivity is only one of the factors tending to make scanning to end fire inefficient. Other major factors are diffraction and scattering due to the vehicle on which the array is mounted (see Sec. 21-1), element-pattern narrowing, and array mismatch due to mutual coupling.

Other options for hemispherical coverage shown in Fig. 21-5 include the use of multiple conformal arrays (Fig. 21-5b), one on each side of the vehicle to provide good coverage except in conical regions near the vehicle nose and tail, or a four-faced array (Fig. 21-5c), perhaps with adequate coverage throughout the hemisphere with a relatively streamlined geometry. Multiple planar arrays have been used for ground-based-radar coverage, and Knittel⁶ gives optimum tilt angles and array orientations for that case.

Figure 21-6 shows contours of constant projected area for any of the configurations of Fig. 21-5, using the coordinate relationships below, for a planar array tilted an angle δ from the vertical:

$$\Theta = \cos^{-1} \left[v \cos \delta + c \sin \delta \right]$$

$$\Phi = \tan^{-1} \left[\frac{u}{-v \sin \delta + c \cos \delta} \right]$$

where $u = \sin \theta \cos \phi$, $v = \sin \theta \sin \phi$, and $c = \cos \theta$ is the array projection factor. In general, the array projected area does not equate directly to relative gain because of array mismatch, element-pat-

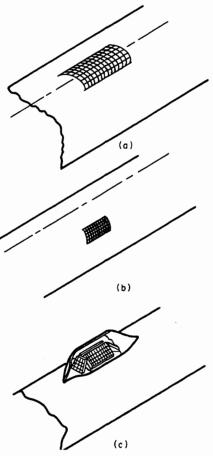
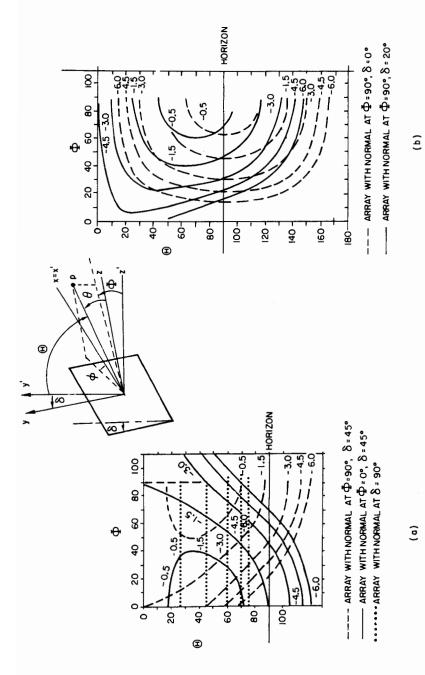


FIG. 21-5 Conformal and low-profile arrays for hemispherical coverage. (a) Large array on top of fuselage. (b) Array conformal to side of fuselage. (c) Fourfaced "tent array."

tern variations, and polarization effects, but it does provide a useful upper bound. This optimum-gain contour, normalized to peak, is given by

$$\frac{P}{P_0} = 10 \log c$$



with array normals at $\Phi=0^\circ$ and 90° and array with normal at zenith ($\delta=90^\circ$). (b) Arrays with FIG. 21-6 Coverage diagrams for a variety of tilted planar-array faces. (a) Arrays tilted to $\delta=45^\circ$ normal at $\Phi = 90^{\circ}$ and at $\delta = 0^{\circ} 20^{\circ}$

Figure 21-6a shows three contour plots of this ratio, two for arrays mounted at $\delta=45^\circ$ and one with $\delta=90^\circ$. The dotted line is the gain contour for an array with its boresight at zenith ($\delta=90^\circ$) and corresponds approximately to Fig. 21-5a. The solid curve corresponds to an array located as in Fig. 21-5b or a side face of the fourfaced array of Fig. 21-5c mounted with $\delta=45^\circ$, $\Phi=0^\circ$. The dashed curve is for an array with its boresight in the $\Phi=90^\circ$ plane and corresponds to the end face of Fig. 21-5c. Combining the solid and dashed curves, as is done for the four-faced array, indicates that an array with these four faces would cover the upper hemisphere with only a 3-dB projected area falloff near $(\Theta, \Phi)=(90^\circ, 45^\circ)$, while the array with $\delta=90^\circ$ would have less gain for all $\Theta>60^\circ$ and thus has its lowest gain over the large area near the horizon.

A more streamlined four-faced array is obtained by reducing the front and rear faces to about one-half of the size of the side faces. In this case it is convenient to mount these arrays with their boresight direction closer to the horizon because the larger side faces provide sufficient gain at the higher elevation angles in the $\Phi=90^{\circ}$ or 180° planes. Figure 21-6 shows two gain contours for full-size arrays with $\delta=20^{\circ}$ (solid) and $\delta=0^{\circ}$ (dashed) for a front-face $\Phi=90^{\circ}$. By evaluating the coverage contours in conjunction with those of the solid curve from Fig. 21-6a (side face), one can compare the available coverage for a four-faced array with a variety of array sizes and elevation angles. If the front and rear faces are selected to be smaller than the side faces, the corresponding number of decibels (for example 3 dB for one-half of the area) must be subtracted from the values on the contour lines.

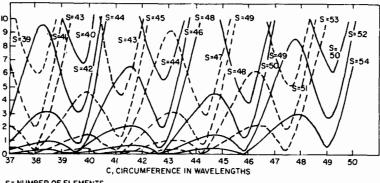
As an example, one can show that, with half-area front and rear faces and using $\delta = 20^{\circ}$ for these end faces, the array system can scan throughout the hemisphere with a minimum projected area of approximately -4.5 dB with respect to the maximum.

Figure 21-6 can also be used with $\cos^2 \theta$ element patterns by doubling all the decibel ratios given in the figures or with any other assumed element patterns that are independent of Φ by making the appropriate scale change.

21-3 CYLINDRICAL ARRAYS

Synthesis of Omnidirectional Coverage

Several applications, including missile communication, require quality omnidirectional pattern coverage in the equatorial plane from an antenna system mounted on a cylindrical metal body of large diameter. Studies^{7,8,9} have shown that an array of slots equally spaced around the vehicle circumference can produce patterns with very low ripple. Croswell and Knop⁸ have obtained extensive numerical data by using realistic element patterns for slots on a perfectly conducting plane. Figure 21-7a gives data from an array computation⁸ showing a ripple level for a cylinder with circumference C between 37 and 50 wavelengths for various numbers of slots S. The calculations show, for example, that for an array on a 39.5 λ cylinder the choice of anywhere between 48 and 54 elements gives a ripple level below ± 0.05 dB, or D = 0.1 in the figure. The selection of 54 elements leads to broader-band performance, however, as indicated by the low ripple level over a range of C near the 39.5 λ design point. In this case, the interelement spacing is approximately 0.73 λ . Spacings that approach λ lead to high ripple levels that are, in general, unacceptable for omnidirectional-coverage



S = NUMBER OF ELEMENTS

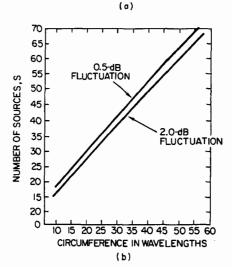


FIG. 21-7 (a) Pattern-fluctuation dependence on number of elements S and cylinder circumference C. (After Croswell and Knop.8) (b) Number of sources as a function of circumference and wavelengths for 0.5- and 2.0-dB fluctuation. (After Croswell and Cockrell.9)

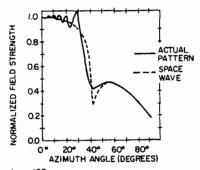
applications. Figure 21-7b gives the number of required sources as a function of the circumference in wavelengths for 0.5- and 2.0-dB fluctuation.9

Several approaches for implementation of omnidirectional missile antennas include the use of wraparound arrays as developed from the broadband Collings radiator, 10 employing plated-through holes, or from the basic microstrip elements 11 described in greater detail in Chap. 7. In either case, considerations like the above dictate the requisite number of feed points.

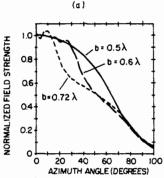
Element Patterns for Arrays on Cylinders

When the array size approaches the vehicle radius of curvature, the behavior of the array element pattern becomes very different from either the isolated element pattern

or the element pattern in a planar array. This property is well documented in the case of circular and cylindrical arrays, which have been the subject of more detailed studies than other conformal arrays. It has long been known that by using the symmetry properties of the array one can avoid the solution of N simultaneous integral equations for an N-element circular array and, instead, superimpose the solution of N independent integral equations, one for each of the solutions with periodicity $2\pi/N$. This method has been used by Tillman¹² and Mack¹³ for dipole and monopole arrays and by Borgiotti¹⁴ for waveguide arrays with active elements covering a sector on an infinite cylinder. The results of these and other theoretical studies have revealed the existence of potentially severe ripples in cylindrical-array element patterns, as shown in Fig. 21-8a. Sureau and Hessel¹⁵ have used asymptotic methods to show that the radiated pattern can be considered the superposition of a space-wave contribution and several creeping waves which propagate around the cylinder and radiate away from the cyl-



 $k_{0}\sigma$ = 185 b = 0.6 λ = element spacing (circumferential plane) d = 0.8 λ = element spacing (axial plane) aperture size 0.32 λ x 0.75 λ , circumferential polarization



koo = 120 b = ELEMENT SPACING (CIRCUMFERENTIAL PLANE) d = 0.72 XELEMENT SPACING (AXIAL PLANE)

FIG. 21-8 Circumferential element patterns.
(a) Waveguide array on cylinder. (After Sureau and Hessel. 16) (b) Dipole array in cylinder. (After Herper et al. 16)

(b)

inder in the forward direction. The space-wave and actual patterns are shown in the figure for radiation at two different angles θ measured from the cylinder axis. The ripple amplitude decreases with cylinder radius and increases with frequency. Recent work by Herper et al., ¹⁶ indicated in Fig. 21-8b, has shown that smoother element patterns can be obtained by limiting element spacing to $\lambda/2$. The improvement is attributed to the fact that the interference of the fast creeping-wave grating lobe ¹⁶ with the direct ray decreases as the azimuth spacing is reduced and disappears at 0.5 λ . This work strongly suggests that low-sidelobe circular arrays are feasible with proper concern for element design.

Technology of Arrays Conformal to Cylinders

Early experimental and theoretical studies concerned arrays built with dipole or waveguide² elements, with the array extending completely around the cylinder. Switching was accomplished by a variety of networks that were contained inside the cylinder, some of which are described in a following subsection. Figure 21-9 shows a circular array of waveguide horns developed by the Naval Electronics Laboratory Center¹⁷ and used in a study of fundamental radiating properties as well as a comparison of several kinds of switching networks. Other studies dealing with full cylindrical or ring arrays are described in a number of survey and basic reference articles.¹⁸⁻²⁰

More recently there has been substantial interest in developing microstrip conformal arrays so thin that they can be attached to the vehicle surface. Described in greater detail in Chap. 7, these array systems vary from the one- or two-dimensional receive-only arrays that have array, phase shifters, and power-divider network on one side of a thin circuit board to the use of multiple-layer construction with each of these functional pieces on a separate board. Figure 21-10 shows an eight-element circularly



FIG. 21-9 Ring array. (After Boyns et al. 17)



FIG. 21-10 Conformal microstrip array. (After Sanford.21)

polarized receive array developed for aircraft tests with the ATS-6 satellite. This L-band array was 0.36 cm thick and was scanned in one plane by means of 3-bit switched-line diode phase shifters. The array axial ratio was less than 2 dB over the scan sector.²¹

Low-Profile Arrays on Cylinders

The great difficulty in obtaining hemispherical coverage with a single fixed conformal array has stimulated interest in low-profile alternatives for SHF satellite-communication-aircraft antennas.

The low-profile array subsystem in Fig. 21-11 developed by the Hazeltine Corporation provides hemispherical coverage for an airborne satellite-communication terminal, the SESAST (small SHF-EHF satellite-communication terminal), by a combination of mechanical rotation in azimuth and electronic scanning in elevation. The array provides full duplex operation over the SHF terminal bands of 7.25 to 7.75 GHz (receive) and 7.90 to 8.40 GHz (transmit). It consists of 21 rows which are individually phased to steer the beam in elevation. Each row comprises 32 slots, providing a narrow azimuth beam. The design incorporates a dielectric sheet above the aperture for wide-angle impedance matching and delay progression along the aperture to steer the quiescent beam to 60° above the horizon. This feature minimizes scan losses at the scan extremes (0° and 90°). The array has independent ferrite phase shifters for receive and transmit and a low-loss radial power divider to provide the 21-way power split.

Arrays mounted above a cylindrical surface are subject to pattern deterioration owing to multipath scattering from the surface. Detailed pattern calculations for a

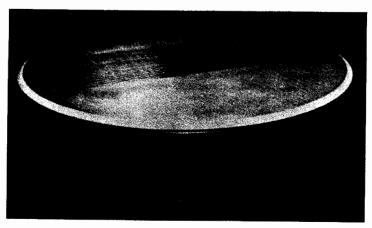


FIG. 21-11 Low-profile array. (Courtesy of Hazeltine Corporation.)

four-faced array (Fig. 21-5c) have been carried out by using geometrical optics²² following the work of Kouyoumjian and Pathak.²³ Figure 21-12 shows the computed gain for both polarizations by using a small array mounted at 45° from the top of a large cylinder. The indicated pattern ripples are the result of a specular multipath from the cylinder surface, and the figure shows that in this particular instance these ripples do not materially alter the elevation-plane coverage of the array.

One last category of low-profile array that deserves some brief mention consists

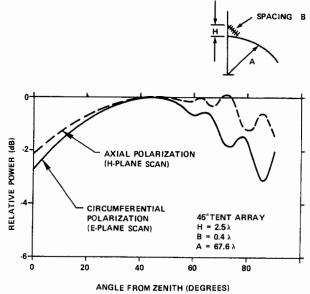


FIG. 21-12 Multipath effects on a tilted four-faced array.

of the use of an array plus some heavy dielectric or corrugated surface to enhance lowangle radiation. Such an antenna provides coverage over most of the hemisphere, operating as a conventional array for angles near the zenith and coupling into a surfacewave mode in the dielectric or corrugated surface to achieve strong radiation near end fire. Although successful in laboratory studies, ²⁴⁻²⁸ these techniques appear to offer solutions for gain up to about 20 dB and with relatively narrow bandwidth (tunable bandwidth up to about 6 percent²⁸).

Feed Systems and Commutators for Cylindrical Arrays

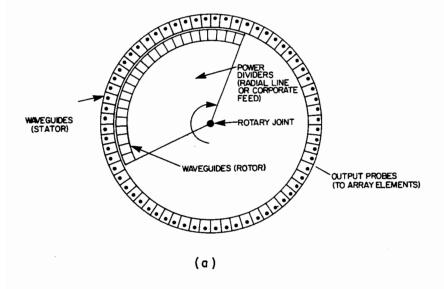
When the array extends completely around the cylindrical surface, it is necessary to devise a feed network to rotate the illuminated spot continuously through multiples of 360°. As noted by Provencher, Hill, 29 and Holley et al., 30 a number of mechanical and electrical networks have been devised to accomplish that task. Mechanical commutators such as the waveguide commutator of Fig. 21-13a are appropriate for systems with continuous scanning over multiple 360° increments. Such commutators are often seen as viable low-cost solutions for a number of applications, and they can provide scanned patterns relatively free of modulation effects if care is taken to assure that the rotating (rotor) feed elements have spacings different from those of the stationary (stator) pickup elements. This design procedure can assure that a minimum of elements is misaligned at any one time and so reduces radiation modulation. Power distribution within the rotor is achieved by using coaxial or waveguide corporate networks or radial power dividers.

A number of investigators have considered switching networks for commuting an amplitude and phase distribution around a circular array. Giannini³¹ describes a technique that uses a bank of switches to bring a given illumination taper to one sector of the array (usually a 90° to 120° arc) and a set of switches to provide fine beam steering between those characteristic positions determined by the sector-switching network. The circuit for a 32-element array is shown in Fig 21-13b; it requires 8 phase shifters and 12 transfer switches (double-pole, double-throw) and achieves sector selection by using 8 single-pole, four-throw switches. This network excites an 8-element quadrant of the array that can be moved in increments of 1 element to provide coarse beam steering. Fine steering is provided by the phase controls.

Several lens-fed circular arrays have been implemented by using R-2R Luneburg and geodesic lenses.³⁰ The R-2R lens (Fig. 21-13c) described by Boyns et al.¹⁷ forms as many beams as there are elements in the array but, like all lens systems, does not admit to fine steering (selecting angles with a separation less than the angular separation between radiating elements on the cylinder) unless additional phase controls are added to each element.

As pointed out by Holley et al.,³⁰ lens systems can be adapted for fine steering by using an amplitude illumination with a movable phase center. The net result of a progressive phase tilt at the input of the Butler matrix is to synthesize intermediate beams from a composite of the available lens beams and so to provide high-quality fine steering of the lens-radiated pattern.

There have been a number of developments in the area of multimode electronic commutators for circular arrays. These systems derive from techniques similar to that first used by Honey and Jones³² for a direction-finding-antenna application in which several modes of a biconical antenna were combined to produce a directional pattern with full 360° azimuthal rotation. Recent efforts by Bogner³³ and Irzinski³⁴ specifi-



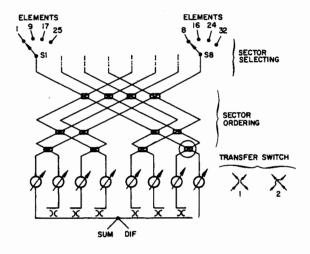
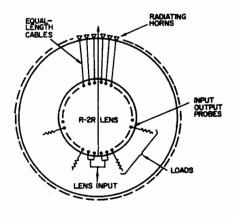
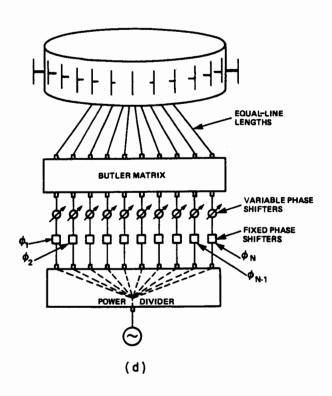


FIG. 21-13 Circular-array feed systems. (a) Commutator (waveguide). (b) Switch network. (After Glannini.³¹) (c) R-2R lens. (After Boyns et al.¹⁷) (d) Matrix scanning system. (After Sheleg.³⁶)

(b)



(c)



cally address the use of such commutators, which must be combined with phase shifters and switches at each element of the array. The phase shifters provide collimating and fine steering, and the switches are used to truncate the illumination so that only a finite sector of the array is used at any time, a procedure that is required for sidelobe control.

Several more sophisticated types of electronic switches for circular arrays are based on a concept, originally proposed by Shelton³⁵ and developed by Sheleg,³⁶ that uses a matrix-fed circular array with fixed phase shifters to excite current modes around the array and variable phase shifters to provide continuous scanning of the radiated beam over 360°. The geometry is shown in Fig. 21-13d. A more recent extension of this technique proposed by Skahil and White³⁷ excites only that part of the circular array that contributes to formation of the desired radiation pattern. The array is divided into a given number of equal sectors, and each sector is excited by a Butler matrix and phase shifters. With either of these circuits, sidelobe levels can be lowered by weighing the input excitations to the Butler matrix. The technique of Skahil and White was demonstrated by using an 8×8 Butler matrix, eight phase shifters, and eight single-pole, four-throw switches to feed four 8-element sectors of a 32-element array. The design sidelobes were -24 dB, and measured data showed sidelobes below -22 dB.

Pattern Synthesis for Cylindrical Sector Arrays

Among the difficulties with circular sector array synthesis are that the elements of the array have element-pattern maxima at different angles according to their location and that the elements do not lie in a plane. This situation is depicted in Fig. 21-14a and precludes use of all the standard synthesis methods. One can, however, control near sidelobes by projecting the array element locations and element patterns onto a plane tangent to the cylinder, as shown in Fig. 21-14a. In this process one needs to account for the nonuniform spacing that results from the projection, but the element patterns tend to account for this nonuniformity.

Figure 21-14a depicts a circular sector array with elements located equally spaced around the circumferencial sector with angular separation $\Delta \phi$. Projected onto the array tangential plane, the element locations of an array are

$$y_n = a \sin \phi_n$$

= $a \sin (n\Delta\phi)$

The projection tends to make the points y_n closer together near the ends of the array, but to first-order the element pattern tends to make up for that effect. For relatively large ϕ_n , the projected spacing between elements varies approximately like $\cos \phi_n$, and so the density of elements has a $1/\cos \phi_n$ dependence. If the array element patterns vary like $\cos \phi_n$, then to first-order the projected array weighting will be correct without altering the weights from those of a linear array with omnidirectional element patterns. If the element pattern is very different from a cosine, that fact must be included in the chosen weights.

Figure 21-14 shows several patterns synthesized by projecting a -40-dB Taylor pattern with $n_{\text{bar}} = 8$ onto cylinders with various radii and 36 elements. Element spacings were restricted to 0.5λ to avoid the grating-lobe sidelobes of Fig. 21-14a. The patterns relative to the local cylinder normal at ϕ_n in the ϕ plane have the form

$$f_n(\phi) = \cos\left(\phi - \phi_n\right)$$

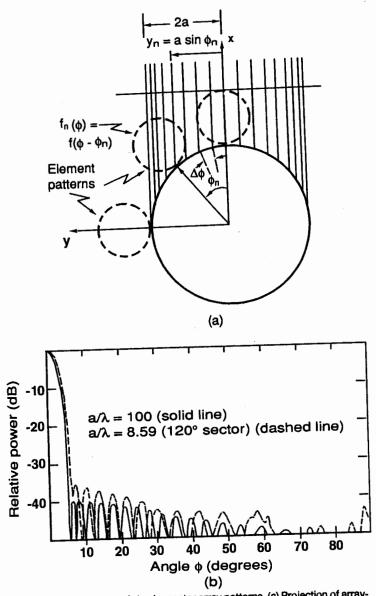


FIG. 21-14 Synthesis of circular sector array patterns. (a) Projection of array-element locations. (b) Synthesized patterns with Taylor $n_{\rm bar}=8$, -40-dB side-lobe pattern. $a/\lambda=100$ (solid), $a/\lambda=8.59$ (dashed).

The two curves show a nearly perfect Taylor pattern at radius $a = 100\lambda$ (solid) and a dashed pattern at $a = 8.59\lambda$ corresponding to an array that occupies a 120° sector of the cylinder. Significant changes in these patterns are beam broadening that results from shortening the array length and an increased sidelobe level near the main beam, with the first sidelobe starting to merge with the main beam for small cylinders. Even for this small cylinder and the array wrapped over a 120° sector, the pattern is still not severely distorted.

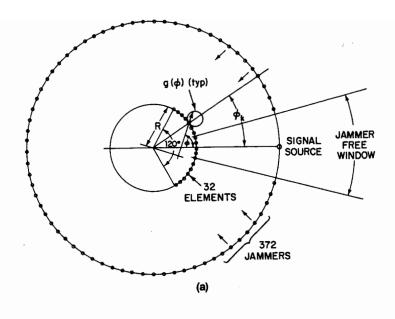
A synthesis method first suggested by Sureau and Keeping³⁸ and further developed by Dufort³⁹ and Olen and Compton⁴⁰ is readily applicable to conformal arrays on generalized surfaces. The technique uses adaptive optimization algorithms to form the array pattern in the presence of closely spaced sources of interference that are tailored or iterated⁴⁰ to achieve the desired pattern. Figure 21-15 shows results from Sureau and Keeping³⁸ for a circular sector array of 32 identical elements disposed over a 120° sector of a cylinder and displaced 0.55λ between elements. The geometry shown in Fig. 21-15a shows the 32 excited elements of a 96-element circular array. A total of 372 sources of interference were uniformly distributed outside the main-beam window to control sidelobes. The measured element pattern was used in the calculations. Figure 21-15b shows that increasing the window width produces a set of patterns with progressively lower sidelobes but decreasing aperture efficiency. Sureau and Keeping also investigated varying the interference weights to control sidelobe decay and the use of asymmetric weights for monopulse pattern control.

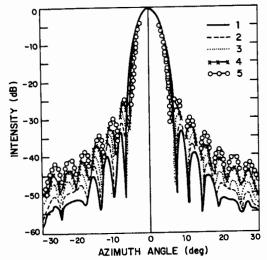
21-4 ELEMENTS AND ARRAYS ON CONIC AND GENERALIZED SURFACES

The dramatic illustration chosen by Kummer¹ (Fig. 21-3) points out the difficulty of synthesis on conical and more generalized surfaces that arise because such structures project differently into different angular regions. For example, a planar array projects as a plane independent of aspect angle, but a cone or a sphere looks very different as the aspect angle is changed. Figure 21-3 also points out the severe polarization distortion resulting from scanned conical arrays.

Nevertheless, cones and spheres are important surfaces for conformal-array development because of their obvious application to missile and certain hemispheric scanning structures. The experimental studies of Munger et al.⁴¹ provide some data on the characteristics of several conical arrays, and theoretical studies by Balzano and Dowling⁴² give rigorous expressions for element patterns in conical arrays. Golden et al.⁴³ evaluated mutual-coupling coefficients for waveguide slot elements on sharp cones, and Thiele and Donn⁴⁴ have performed analytical studies of relatively small cones excited by loop elements using a wire-grid model.

There have been several important studies of antennas on spheres. However, the dome antenna⁴⁵ is by far the most important application of a spherical array to date. This structure, shown in Fig. 21-16a, uses the vertical projection of a spherical dome to achieve increased gain at low angles of elevation. The passive spherical lens is made up of fixed phase shifters and a conventional planar phased array (Fig. 21-16b) which steers an illuminated spot to various portions of the lens. Fixed phase delays in the lens are computed so as to convert the array scan direction θ , into a factor K times that angle and so to obtain scan in excess of the planar-array scan angle. The array phase-shifter settings are determined to form the nonlinear phase progression required to scan the searchlight-type beam to various spots on the lens. Although the radiated

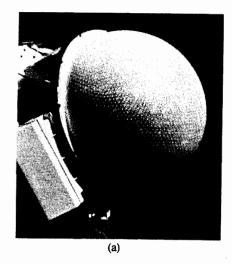




\[\]	PATTERN	WINDOW WIDTH (deg)	BEAMWIDTH 3 dB (deg)	PEAK SL (dB)	APERTURE EFFICIENCY (dB)
H	1	13.06	5.1	-33.0	-0.924
1	2	12.16	5.0	-30.5	-0.787
	3	11.25	4.76	-28.0	-0.644
Ī	4	10.34	4.20	-26.5	-0.508
	5	9.42	4.36	-23.5	-0.377

FIG. 21-15 Synthesis of circular sector array patterns using the method of Sureau and Keeping.³⁸ (a) Geometry showing array, jammer locations, and jammer free window. (b) Computed patterns and characteristics for various width jammer free windows. (After Sureau and Keeping.³⁸)

(b)



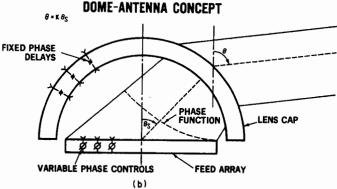


FIG. 21-16 Hemispherical dome array. (a) Dome array. (b) Domeanterina concept. (Courtesy of Sperry Corporation.)

beamwidth varies with scan angle, the dome can achieve scanning over sectors larger than a hemisphere and, in fact, has achieved scan to $\pm 120^{\circ}$ from zenith. Steyskal⁴⁶ gives equations for the gain limits of a given circular cylindrical dome based upon allowable scan angles for the feed array and shows that the ratio of the average gain to the broadside feed-array gain is bounded by a parameter that depends upon the feed-scan limit.

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Adaptive Antennas

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22-2	Fundamental Characteristics 22-2
22-3	Antenna 22-3
	Weights 22-4
22-5	Resolution 22-7
22-6	Degrees of Freedom 22-12
22-7	Weight-Determining Algorithms 22-14
	Power-Inversion Algorithm 22-15
	Maximization of Signal-to-Noise Ratio 22-1
	Transient Characteristics 22-18
	Sample Matrix Inversion 22-19
	Contract

22-8 Multiple-Beam Antenna versus Phased Array 22-20 Bandwidth 22-20 Channel Matching 22-21

22-1 Introduction 22-2

22-1 INTRODUCTION

Adaptive antennas were first used in an intrinsic form as radar antennas with sidelobe-canceling characteristics. The sidelobe-canceler antenna consists of a conventional radar antenna whose output is coupled with that of much-lower-gain auxiliary antennas. The gain of the auxiliary antennas is slightly greater than the gain of the maximum sidelobe of the radar antenna. Adding the weighted signals received by the auxiliary antenna to those received by the radar antenna permitted suppression of interfering sources located in directions other than the main beam of the radar antenna. This early use of adaptive antennas evolved to adapted array and multiple-beam antennas.

This chapter presents a description of the major components of an adaptive antenna and develops general relationships and rules governing its performance. A fundamental definition of resolution is developed, enabling one to determine the minimum tolerable angular separation between desired and interfacing signals. This resolution leads naturally to the definition of degrees of freedom and to a conceptual method of determining the potential and actual degrees of freedom available to a given adaptive antenna. It is shown that often an adaptive antenna with N degrees of freedom can suppress more than N-1 sources.

The algorithm governing the adaptation process can be based on one of three classical methods. Two methods, named for the inventors, use a feedback weight-control system. The first method requires prior knowledge of the actual or potential location of the desired sources and is commonly referred to as the power-inversion or Applebaum-Howells algorithm. The second weight-determining method using feedback control is called the Widrow algorithm and requires a known characteristic of the desired signal in order to maximize the signal-to-noise ratio of signals received from a single desired source. The third, or sample-matrix-inversion (SMI), algorithm is a completely computational process that uses the signals received at the N ports of an adaptive antenna and the desired-source angular locations to suppress interfering signals in the computed output. This SMI algorithm does not use feedback to correct for implementation inaccuracies.

Finally, some general remarks about transient effects and the comparative performance of planar-array and multiple-beam antennas are presented.

22-2 FUNDAMENTAL CHARACTERISTICS

Adaptive antennas are used primarily for receiving signals from desired sources and suppressing incident signals from undesired or interference sources. The basic configuration shown in Fig. 22-1 consists of an antenna with N(N > 1) ports, N complex weights, a signal-summing network, and a weight-determining algorithm. The N ports of the antenna can be the output terminals (ports) of the elements of an array antenna, or the ports of a multiple-beam antenna (MBA), or a mixture of these. A complex weight, in general, attenuates the amplitude and changes the phase of the signals passing through it and is usually assumed to have a frequency-independent transfer function. The summing network is often a corporate-tree arrangement of four-port T's. Each T sums the in-phase components of the signals at the two input ports in one

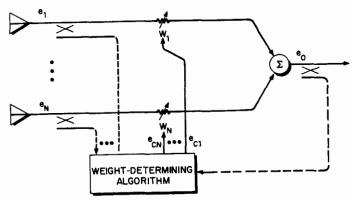


FIG. 22-1 Fundamental adaptive nulling circuit.

output port and has a matched load at the other output port to dissipate those components of the input signal that are 180° out of phase. The weight-determining algorithm (or simply the algorithm) makes use of a priori or measured information, or both, and specifies the complex weight W_n applied to the signal received at the nth port as

$$W_N = ge_{cn} \tag{22-1}$$

As shown in Fig. 22-1, the algorithm uses information derived solely from the output signal e_0 (as in a weight-dither algorithm), or solely from the input signals e_n (as in the matrix-inversion algorithm), or from both e_0 and e_n as in the Applebaum-Howells and Widrow algorithms. An intrinsic algorithm need not use either e_0 or the e_n ; hence these inputs to the weight-determining algorithms are indicated by dashed lines in Fig. 22-1. Note that these inputs are indicated as being "loosely" coupled, as opposed to being connected directly, to the e_n and e_0 signal ports.

Clearly the antenna (array, MBA, or hybrid) is that essential component of an adaptive-antenna system which is uniquely related to the disciplines of antenna design. The weight and summing circuits can operate at the antenna operating frequency f_0 or at an intermediate frequency (IF) or be part of a digital signal processor. Although the design and development of the antenna, the weights, and the summing network are important, the weight-determining algorithm almost always determines the uniqueness of an adaptive antenna. Consequently, this chapter will only briefly describe the antenna, the weights, and the summing network. Considerably more attention will be given to the fundamental limitations (i.e., degrees of freedom and resolution) of all classes of adaptive antennas and to a conceptual description of the classical weight-determining algorithms.

22-3 ANTENNA

Although adaptive-antenna systems use antennas of various types and configurations, it is possible to separate these into three basic classes: phased arrays, multiple-beam antennas, and a mixture of these two. Each configuration has several ports where

received signals e_n appear in response to sources located in the antenna's field of view (FOV). Phased arrays characteristically have many identical elements, each of which has a port where the output signal can be represented by

$$e_n = \sum_{m=1}^{M} I_m F_n(\theta_m, \phi_m) e^{jH_n(\theta_m, \phi_m)}$$
 (22-2)

where $I_m = \frac{\lambda^2 P_m G_m}{(4\pi R_m)^2}$

 P_m = power radiated by mth source

 G_m = gain of antenna used by mth source

 R_m = distance between mth source and adaptive antenna

 λ = operating wavelength

The amplitude and phase that relate I_m to a signal at the antenna port are given by F_n and H_n respectively. The angular location of the *m*th source is given by the coordinate pair θ_m, ϕ_m measured in a suitable spherical coordinate system.

It is important to note that in most if not all phased-array adaptive antennas the F_n are identical, whereas H_n is generally different for all elements of the array. For signals at the output ports of an MBA, the H_n are nearly equal and the F_n differ. It will be shown later that this fundamental difference between a phased array and an MBA results in the inherently larger bandwidth of the latter.

Phased arrays are either filled or thinned. Filled arrays do not have significant grating lobes or high sidelobes within the FOV of an array element of the array, whereas thinned arrays characteristically have either grating lobes or high sidelobes (~10 dB) in the FOV of the array element. Grating-lobe characteristics are extremely important because even when interference and desired sources are separated by a large angle (i.e., compared with the array half-power beamwidth, or HPBW), the desired source is suppressed by approximately the same amount as the interference source when an interference source is located on a grating lobe.

Although there is not a suitable formal definition of thinned or filled arrays, it is convenient to consider the thinned array as having an interelement spacing S greater than S_T , where

$$S_T = \frac{\lambda}{\sin\left(\theta_e/2\right)} \tag{22-3}$$

and θ_e is the HPBW of an element of the array. Unfortunately, Eq. (22-3) cannot be used in all cases, but it does serve as a conceptual definition.

Hybrid-antenna systems usually consist of an array antenna with each element of the array configured as an MBA. The directive gain of the MBA permits thinning of the array without forming harmful grating lobes while retaining the capability of scanning the instantaneous FOV over a larger FOV. Chapters 3, 16, 17, 20, 21, and 35 discuss some applicable antennas in greater detail.

22-4 WEIGHTS

Just as the excitation of phased arrays (see Chap. 3) determines the antenna radiation pattern, weighting of signals received at the ports of an adaptive antenna determines

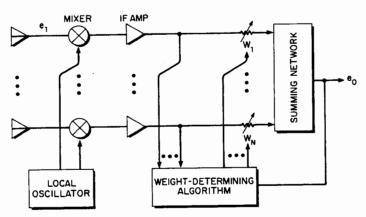


FIG. 22-2 IF adaptive nulling circuit.

the antenna's directional response to incident signals. Since the discussion of adaptive antennas presented here assumes a receiving as opposed to a transmitting antenna system, it is necessary to introduce and use the concept of weighting and combining receiving signals instead of "exciting" the array or MBA to produce a radiation pattern. However, it is often much clearer to represent the antenna's angular discrimination of received signals in the form of "radiation" patterns. The reader is cautioned to ignore the literal meaning of radiation patterns and think of the F_n and related functions as receiving-antenna patterns.

Weights attenuate and alter the phase of received signals. They are designed to be either frequency-independent or adaptively varied as a function of frequency. Some adaptive antennas operate entirely at the received frequency and use radio-frequency (RF) weights as indicated in Fig. 22-1. Still others have a mixer-amplifier at each antenna port, and the weights operate at a lower IF, as indicated in Fig. 22-2. The latter customarily uses lossy weights consisting of attenuators and hybrid power dividers as indicated in Fig. 22-3. The use of lossy weights in this way does not degrade system performance since the mixer-IF amplifier establishes the local signal-to-noise (S/N) ratio such that subsequent losses in the weights and combining, or summing, network attenuate both signal and noise without altering the S/N. For RF weighting, the weight circuit is usually a corporate configuration of "lossless" variable power dividers and a single phase shifter at each antenna port, such as shown in Fig. 22-4. Four-port variable power-dividing junctions (Fig. 22-4) are customarily used in weight and summing networks to prevent the resonant effect encountered with the use of three-port junctions. This effect is produced by small but significant reflected waves between input and output ports. Dissipative loads at the fourth port of a four-port junction (Fig. 22-4b) absorb reflected waves that do not couple to the input port; reflected waves at the input do, however, degrade the input match of the circuit. Although this effect is not uniquely associated with adaptive antennas, it is an important and significant consideration in the design of all adaptive-antenna systems.

All antenna systems have a frequency-dependent response to incident signals. Whenever frequency-independent weights are used, suppression of undesired signals will vary with frequency. This inherent performance characteristic cannot be succinctly and accurately described because it is scenario-dependent. However, it can be

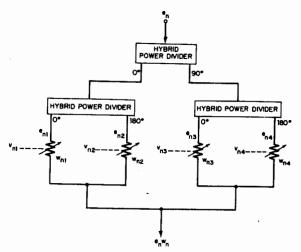


FIG. 22-3 Typical IF weight circuit.

shown³ that, for frequency-independent weights, the cancellation C (i.e., suppression of an interfering signal) of an adaptive-array antenna is limited as

$$C \le 20 \log \left[K \left(\frac{2\pi}{c} \right) DW \sin \theta_m \right]$$
 dB (22-4)

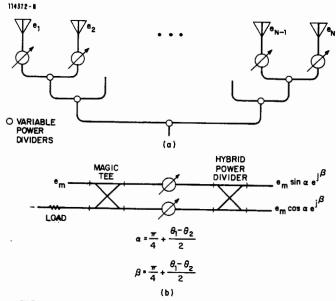


FIG. 22-4 (a) RF weight circuit. (b) Variable power-divider circuit.

where $2\theta_m = \text{maximum}$ angle subtended by FOV

D = maximum dimension of antenna aperture

W = nulling bandwidth

c =velocity of light in free space

The constant K is a function of the array configuration and the particular scenario of interfering and desired sources; it ranges between ~ 5 and ~ 15 . It is important to note that C varies as the square of W and the square of the maximum-scan angle θ_m and that Eq. (22-4) takes only antenna-related dispersive effects into account; it assumes frequency-independent weights and identical antenna-array elements. When the antenna array uses time-delay circuits, which in effect reduces θ_m , C increases accordingly.

One form of frequency-dependent weight consists of a delay line with two or more taps. The received e_n is delivered to the output of each tap, weighted, and summed with the output of all N taps (Fig. 22-5). The weights are frequency-independent, and the delay between successive taps³ depends on W, D, θ_m , λ , and the distribution of interfering sources. Observing that the maximum delay τ_{max} occurring between elements located at opposite edges of an array aperture is given by

$$\tau_{\max} = (D/c)\sin\theta_{m} \tag{22-5}$$

The number of taps N, should exceed

$$N_{r} > \tau_{\text{max}} W = (WD/c) \sin \theta_{m}$$
 (22-6)

Although the use of frequency-dependent weights will increase with the development of the associated technology, adaptive antennas using frequency-independent weights are currently most popular. Hence the discussions in this chapter are limited accordingly; the weight shown in Fig. 22-5 is introduced primarily because of its potential importance to broadband operation of large phased arrays.

22-5 RESOLUTION

Since the primary purpose of an adaptive antenna is to suppress interfering sources while maintaining adequate response to desired sources, the system designer needs to know the minimum tolerable angular separation between desired and interfering

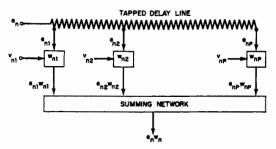


FIG. 22-5 Frequency-dependent adaptive weights.

sources. In other words, the inherent ability of the antenna to resolve desired and undesired sources is fundamental to the system design. Clearly, the antenna's resolving power increases with its aperture size D. Quantitative resolving characteristics of adaptive antennas will be discussed in this section.

The signals e_n received at the ports of the antennas (Fig. 22-1) are "multiplied" by a weight W and summed to produce the output signal e_0 . That is,

$$e_0 = \sum_{n=1}^{N} W_n e_n \tag{22-7}$$

Adaptive antennas select the W_n so as to place *nulls* in the radiation pattern in the direction of interfering sources. By using matrix notation and representing the weights as the vector

$$W = [W_1, W_2, \dots W_N]$$
 (22-8)

it can be shown⁴ that the optimum set of weights W₀ is given by

$$W_0 = M^{-1}V (22-9)$$

where V is called the steering vector and represents the quiescent weights which establish the antenna receiving pattern in the absence of interfering sources.

In Eq. (22-9), M is the covariance matrix of the e_n received signals. That is,

$$M = \begin{bmatrix} \overline{e_1 e_1^*} & \dots & \overline{e_1 e_N^*} \\ \vdots & & & \\ \vdots & & & \\ \vdots & & \overline{e_N e_N^*} \end{bmatrix}$$
 (22-10)

where the overbar indicates averaging over the correlation interval and the asterisk indicates the complex conjugate. Clearly all adaptive antennas strive to determine or estimate M or M^{-1} which enables W_0 to be determined from Eq. (22-9) or an equivalent algorithm. This optimum produces that spatial discrimination, available with the associated antennas, which maximizes the ratio of the desired signal power to the interfering plus internally generated noise power. Now the covariance matrix M and its inverse M^{-1} are key to the determination of the fundamental properties of an adaptive antenna. For example, M^{-1} can be written in the form

$$M^{-1} = \sum_{n=1}^{N} \frac{\mathbf{u}_n \mathbf{u}_n^{\dagger}}{\lambda_n} \tag{22-11}$$

where † indicates the complex-conjugate transpose, \mathbf{u}_n is the *n*th eigenvector of M with eigenvalue λ_n , and the N eigenvalues of M represent the antenna output power $e_0e_0^*$ obtained when $\mathbf{W} = \mathbf{u}_n$. Hence, if a single source is in the antenna's FOV, one eigenvalue (i.e., λ_1) will be much larger than all other eigenvalues. If two sources are in the FOV, at least one and maybe two eigenvalues will be larger than the others. Since the \mathbf{u}_n ($n = 1, 2, \ldots, N$) are an orthogonal set forming the basis of M^{-1} , two equal eigenvalues will result when two sources of equal intensity are located at spatially orthogonal positions in the FOV. In other words, if source S_1 is located in a null of the radiation pattern resulting when $\mathbf{W} = \mathbf{u}_2$, two equal-value eigenvalues will result.

The resolution of an adaptive antenna can be determined by first placing two sources, S_1 and S_2 , with intensity P at the same point in the antenna's FOV. The resulting covariance matrix will have only one large eigenvalue, λ_1 , indicating that a single degree of freedom of the array is used, and setting $\mathbf{W} = \mathbf{u}_1$ will maximize the power delivered to the output port of the adaptive antenna. Conversely, setting \mathbf{W} so that $\mathbf{W} \cdot \mathbf{u}_1 = 0$ will reduce the output power to zero.

Now as the angular separation between two sources increases from zero, λ_1 decreases, and a second significant eigenvalue, λ_2 , increases. When S_1 and S_2 are separated by an angle α_0 , $\lambda_1 = \lambda_2$ and two of the N degrees of freedom are required to establish a radiation pattern which maximizes the output power. A detailed analysis of this process indicates that when S_1 and S_2 are at the same location $\lambda_1 = 2P$ and when they are separated at an angle α_0 , $\lambda_1 = \lambda_2 = P$. The angular resolution α_0 is approximately equal to the HPBW measured in the plane R containing the two sources and the adaptive antenna. The HPBW is calculated from the known antenna aperture dimension in the plane R and an assumed uniform excitation of all elements of a phased array or excitation of a single port of an MBA.

The results presented in the preceding paragraph can also be derived mathe-

matically by substituting Eq. (22-11) into Eq. (22-9) to obtain

$$W_0 = \sum_{n=1}^{N} \frac{\mathbf{u}_n \mathbf{u}_n^{\dagger}}{\lambda_n} \cdot \mathbf{V}$$
 (22-12)

where the \mathbf{u}_n span the weight space. The radiation pattern produced by the N eigenvectors forms a complete orthogonal set whose appropriately weighted combination will form any radiation pattern that the adaptive antenna is capable of forming. (The concept of a radiation pattern is introduced to clarify the pattern synthesis implied. When receiving signals, the receiving pattern is identical to the radiation pattern for $W_n = I_n^*$, where I_n is the excitation coefficient of the *n*th port of the adaptive antenna.) Note that when λ_1 is the only large eigenvalue (i.e., S_1 and S_2 are at the same location), W_0 does not include \mathbf{u}_1 and the output of the adaptive antenna will not contain energy received from S_1 and S_2 ; only weak signals or noise determines the value of the other eigenvalues, W_0 and the antenna receiving pattern. It follows that since $W_1 = \mathbf{u}_1$ maximizes the signal from S_1 and S_2 , the resulting receiving pattern, obtained by using W_1 for the weights, must be identical to the radiation pattern that maximizes the adaptive antenna's directivity in the direction of the location of S_1 and S_2 .

As described in the foregoing, separating the sources gives rise to two large eigenvalues equal to P when the angular separation equals α_0 . From Eq. (22-12), when $\lambda_1 = \lambda_2 = P$ and all other $\lambda_n \ll P$,

$$\mathbf{W}_0 \cdot \mathbf{u}_1 = \mathbf{W}_0 \cdot \mathbf{u}_2 = 0 \tag{22-13}$$

minimizes the output power and suppresses the interference from S_1 and S_2 . However, if S_2 is a source of desired signals and its radiated power $\ll P$, the angular separation between S_1 and S_2 must be equal to or greater than α_0 if the receiving pattern is to have a null in the direction of the interfacing source and maximize the signal received from the desired source.

Since any adaptive antenna must have internal noise sources, all λ_n of M must be greater than zero; consequently, \mathbf{W}_0 given by Eq. (22-12) is always finite. It is, however, customary to normalize \mathbf{W}_0 so that their magnitude varies between 0 and 1 and their phase varies between 0° and 360°.

Nulling resolution is strongly dependent on the quiescent pattern's phase and amplitude variation with observation angle. As described in the foregoing, inherent nulling resolution is about a half-power beamwidth (HPBW) if the quiescent pattern has constant amplitude and phase as a function of the observation angle. This can be reduced to about 0.3 HPBW if 10-dB suppression of the desired signal is tolerable. Resolution can be further increased to less than 0.15 HPBW if the phase or the amplitude of the quiescent radiation pattern varies with observation angle. For example, Fig. 22-6 indicates the amplitude of the quiescent and adapted radiation patterns for two cases. In one case, the phase and amplitude of the quiescent pattern are constant; in the second case, the phase varies 90° per HPBW. Note that the width of the null, measured at the half-power level, is reduced to about one-half that achieved with uniform phase and amplitude. Introduction of phase variation produces a tolerable variation in the amplitude of the quiescent radiation pattern.

This improvement in nulling resolution can be explained by noting that for a single interfering source, the steady-state adapted radiation pattern, produced by any power inversion algorithm (virtually all are of this type), can be represented by the combination of two radiation patterns. Specifically, the narrowest highest-gain beam that the antenna can produce in the direction of the interference is subtracted from the quiescent radiation pattern. This will produce a null in the direction of the interferer. As the observation point is moved from the direction of the null, the field increases due to a difference in both the amplitude and phase of the quiescent and the high-gain "beams."

At the edge of the coverage area (or quiescent beam), radiation-pattern amplitude decreases with increasing angular separation between the coverage area and the observation point (Fig. 22-7). If an interferer is located near the edge of the coverage area, the null

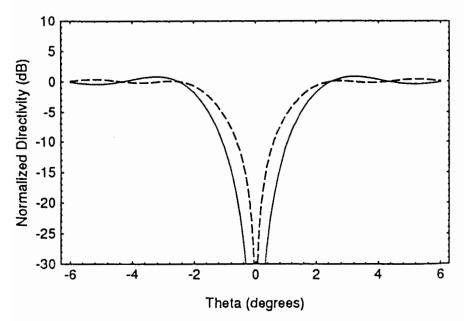


FIG. 22-6 Adapted patterns: solid curve for uniform quiescent pattern and dashed curve for 90° per HPBW phase taper.

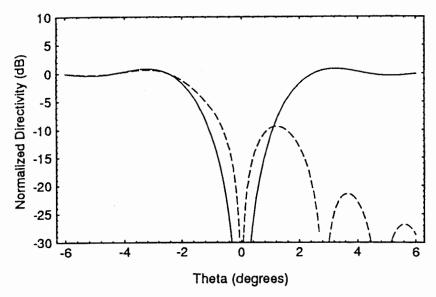


FIG. 22-7 Adapted patterns: solid curve for uniform quiescent pattern and dashed curve for interferer at edge of coverage.

width is reduced to about one-half the value obtained if the jammer were within the coverage area and the quiescent pattern's phase and amplitude were uniform. For this case, nulling resolution is increased due to the relative change of the radiation patterns of a high-gain beam pointing toward the interference and the quiescent radiation pattern at the edge of coverage.

The foregoing clearly indicates the relationship between nulling resolution and quiescent radiation pattern. These cases are presented to indicate fundamental properties and provide a method of estimating the probable nulling resolution that can be obtained with respect to the antenna's minimum HPBW.

Nulling resolution can approach % HPBW by introducing phase or amplitude variation in the quiescent radiation pattern. Note that all interfering sources located in the immediate vicinity of a single null are suppressed and only one degree of freedom is consumed, regardless of the number of interferers located in the null. It follows that an adaptive antenna can suppress more than one interferer with a single degree of freedom.

In summary, the resolution α_0 of any adaptive antenna in a given direction θ_0,ϕ_0 is approximately equal to the minimum HPBW of the radiation pattern which can be generated by the antenna and has maximum directivity in the direction θ_0,ϕ_0 . The HPBW is determined in the plane containing the resolution angle α_0 . It follows that larger-aperture antennas have higher resolution. Further, when an interfering source and a desired source have angular separation α_0 or larger, an adaptive antenna with resolution α_0 can suppress the interfering source without altering its receiving pattern or directivity (i.e., with respect to the interference-free values) in the direction of the desired source. Nulling resolution can approach % HPBW by introducing phase or amplitude variation in the quiescent radiation pattern. Note that all interference sources

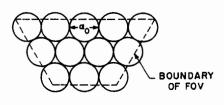
in the immediate vicinity of a single null (i.e., within $\frac{1}{2}$ HPBW) are suppressed. It is also true that only one degree of freedom is consumed regardless of the number of interferers located in the immediate vicinity of the null. It follows that an adaptive antenna can suppress more than one interferer with a single degree of freedom, or N interferers with N nulls.

22-6 DEGREES OF FREEDOM

Clearly any adaptive antenna with N ports and N weights has N degrees of freedom (DOF). However, the number of DOF required to satisfy a given scenario is not easily determined. Often is is understood mistakenly that an N-port antenna can suppress only N-1 interfering sources. Nothing could be further from the truth. It is in fact difficult, and sometimes impossible, to find that set of N interference sources that can disable an adaptive antenna with N DOF.

In particular, consider an adaptive antenna with but two degrees of freedom and the ability to suppress an interfering source P_J , 30 dB with respect to the desired signal. Assume that the interference-free signal-to-noise power ratio (S/N), at the output of the adaptive antenna, is 13 dB in the absence of adaptive nulling and that it decreases to -10 dB in the presence of signals from the interference source. Spatial discrimination of the adaptive-antenna pattern will increase the S/N to slightly less than 13 dB. The addition of four additional interfering sources, each with effective radiated power ERP = P_J at the same location, will reduce S/N to 10 dB.

The set of N eigenvectors into which the covariance matrix can be decomposed is uniquely only for a given set of signals e_n . Determining the strength and loction of N sources which will capture the N eigenvalues of the covariance matrix M (or the N DOF of an N-port adaptive antenna) is in general difficult and often impossible.



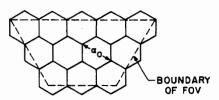


FIG. 22-8 Resolution cells and DOF.

However, an intelligent method for locating the interfering sources may result in disabling an N-port adaptive antenna with only slightly more than N interference sources. Consequently, it is helpful to derive some rule of thumb which enables the antenna designer to determine how many DOF are potentially available for suppressing sources in a specified FOV. The following guidelines are based on the foregoing and on a conceptual, as opposed to a rigorous, mathematical derivation.

Although an N-port adaptive antenna has NDOF, the antenna aperture may not be large enough to use all N degrees of freedom in the specified FOV. By using the foregoing definition of α_0 , it is conceptually acceptable to assume that an N-port adaptive antenna

with a circular aperture has N circular resolution cells, each of which subtends an angle α_0 measured at the antenna aperture. The composite of all N (N=12) resolution cells "covers" the antenna FOV as indicated in Fig. 22-8a, where α_0 is the angular diameter of each cell. As for the small but finite area at the intersection of three adjacent cells, one might consider hexagonal cells with diagonals equal to α_0 ; however, this carries the concept far beyond its intended accuracy.

If the FOV is larger than that indicated in Fig. 22-8, increasing N accordingly would still guarantee one DOF for each resolution cell within the FOV. Conversely, if the FOV is smaller than the composite area formed by the N resolution cells, either the antenna aperture size must be increased or some of the antenna ports can be eliminated without affecting the adaptive-antenna performance over the FOV.

For those adaptive antennas designed to serve a circular FOV with a circular aperture, the foregoing concept can be placed in mathematical form. That is, the number N_c of equal-diameter nonoverlapping circles that can be inscribed in a larger circle is maximum when the centers of the "smaller" circles are on a hexagonal grid and is given by

$$N_c = 1 + \sum_{m=1}^{M-1} 6m$$
 (22-14)

Setting the diameter of the smaller circles equal to α_0 gives

$$M = \text{odd integer of } [\gamma_0/\alpha_0]$$
 (22-15)

where γ_0 is the angular diameter of the larger circle defining the FOV. By recalling that α_0 is the HPBW when the antenna weights are chosen to produce maximum directivity, α_0 can be approximated as

$$\alpha_0 \approx \frac{60\lambda}{D}$$
 (22-16)

where D is the antenna aperture diameter. Substituting Eq. (22-16) into Eq. (22-15) gives

$$M = \text{odd integer of } [(D/\lambda)(\gamma_0/60)]$$
 (22-17)

Then $D/\lambda = 60M/\gamma_0$. For example, if M = 5, $N_c = 19$, the antenna D/λ must be greater than $300/\gamma_0$ if 19 degrees of freedom are required. If the antenna has more than 19 ports, only 19 will be useful in forming nulls within the FOV. If there are fewer than 19 ports, say, 10, and the antenna aperture is not thinned, the adaptive antenna still has 19 degrees of freedom, 9 of which are not available to the adaptive algorithm; however, they can be used to shape the quiescent (interference-free) receiving pattern. In particular, an adaptive antenna with a 19-beam MBA, 9 of whose ports are short-circuited, will have 19 DOF within the FOV defined by γ_0 if its aperture diameter $D = 300(\lambda/\gamma_0)$. Notice, however, that signals originating from 9 "short-circuited" resolution cells couple to the adaptive antenna only through the sidelobes of the receiving pattern associated with the 10 ports that are not short-circuited.

22-7 WEIGHT-DETERMINING ALGORITHMS

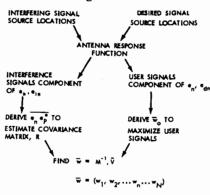
To achieve the desired antenna performance, an algorithm for choosing W_0 must be formulated. The algorithms must take the form of hardware or software, and they range from the very simple and straightforward to the complicated and sophisticated. The algorithms all have the same common goal: they must derive the desired W_0 . It is helpful to separate these algorithms into two general classes, those with and those without feedback. Specifically, the latter, or feed-forward, systems determine the desired W_0 from a given set of input data and install the weights with some small but finite error. They are not further corrected by examining the output signals, as is done in an algorithm which uses feedback. Truly adaptive algorithms adjust the weights by observing the output or some other metric related to system performance.

The algorithm for deriving weights is undoubtedly the central issue in determining the value and performance of any adaptive-antenna system. Consider first the simplest algorithm and then the more sophisticated methods for deriving W_0 . Most adaptive algorithms operate when the interfering-signal power is much larger than the desired-signal power, when both are measured in the nulling band W. This assumes that the interfering signal occupies a bandwidth W which is much larger than the instantaneous bandwidth of the desired signal.

All algorithms depend on two basic and distinct components, namely, the inverse of the covariance matrix of the received signals e_n and the steering vector V. First, recall that the voltages e_n at each antenna terminal are produced by thermal noise, interfering sources, and desired sources in the FOV; that is, $e_n = e_{\text{noise}} + e_{ln} + e_{dn}$. The goal of any algorithm is to choose weights so that the total power received from the interference sources is minimized and the output voltage e_0 is dominated by the desired signals. Since e_{noise} , e_{ln} , and e_{dn} are not correlated with one another, the covariance matrix M, formed by determining the time average value of $e_n e_q^*$, equals the sum of the covariance matrices of the thermal noise, interfering-signal sources, and desired sources; that is, $M = M_N + M_I + M_D$. In most adaptive-antenna applications, the interfering signals dominate M [i.e., $M_I \gg (M_N + M_D)$], and a good estimate of M_I can be obtained from the voltages e_n . In the absence of interfering signals (i.e., $M_I = 0$), the weights are chosen to maximize the signals received from the

desired sources. Choosing the desired weights W_0 in accordance with Eq. (22-9) will maximize the desired signal-to-total-noise-power ratio [i.e., $P_D/(P_I + P_N)$] at the output of the adaptive antenna. This maximization will occur for all user signals if W_0 is chosen appropriately.

Consider a common scenario to illustrate this basic algorithm. Assume that all signal-source locations and the relative intensity of each desired-signal-source ERP are known. Let us further assume that the antenna response to a signal source located anywhere in the FOV can be calculated. Following the



NOTE •in + •dn • •n

FIG. 22-9 Basic algorithm.

flow chart given in Fig. 22-9, the desired-signal and interference-signal components of e_n can be calculated from the foregoing information. The interference covariance matrix M_I and its inverse can be calculated from e_{in} . The covariance matrix M_D can be used to calculate V, which will maximize the power received from each desired-signal source. Choosing the weights W_0 equal to the product $M^{-1}V$ will minimize the difference between the actual and the desired antenna directive gain in the direction of the desired-signal sources while suppressing the interfering signals. It is conceptually helpful⁶ to assume that, in the absence of interfering signals, the desired signals are maximized when $W_0 = V$. Introduction of interfering signals causes the adaptive antenna to form a radiation pattern that is a least-mean-square fit to the quiescent receiving pattern, with nulls in the direction of the interfering sources.

All adaptive nulling algorithms, in their steady state, attempt to choose $W_0 = M^{-1}V$. Consequently, specific performances among various algorithms are manifested in their transient behavior, their choice of V, their hardware and/or software implementation, and the degree to which they are sensitive to errors.

Power-Inversion Algorithm

Assume that the locations of the interference signals are unknown and that their ERP is much greater than the ERP of the desired signals; that is $M_I \gg (M_D + M_N)$. Further, assume that V is selected to provide the desired antenna directive gain in the known direction of each desired-signal source. Since e_{in} is unknown, M_I cannot be calculated. However, direct measurement of the e_n or $e_n e_n^*$ would enable M or M^{-1} to be estimated; this estimate becomes more accurate as the interfering signals become much stronger than the desired signals. By choosing the nulling bandwidth appropriately, one can usually guarantee that troublesome interference will result in $M_I \gg M_d$ and that the algorithm will be very effective in choosing W_0 . Conversely, an inappropriate choice of nulling bandwidth, effective noise level, etc., will result in an undesirable reduction in the desired signals if it (they) and the interference signal (signals) have approximately the same amplitude (i.e., $|e_{in}| \sim |e_{in}|$).

This algorithm is often referred to as the power inversion or Applebaum-Howells algorithm. It is one of the best-known analog algorithms. A schematic representation of the fundamental circuit is shown in Fig. 22-10. The antenna-element, or beam-port, output signals e'_n are indicated for an N element (beam) array (multiple-beam) antenna. A mixer followed by a preamplifier (and perhaps by appropriate filtering) establishes e_n over the nulling band W. For the purpose of the present discussion, assume that e_n is a frequency-translated, band-limited representation of e'_n and consider the "loop" that is connected to antenna terminal 1. The signals e_n are weighted by W_n and summed to give an output signal e_0 ; that is,

$$e_0 = \sum_{n=1}^{N} W_n e_n \tag{22-18}$$

Thus far everything is exactly as described in the foregoing. However, in this circuit the complex weights W_n are proportional to the complex control voltages e_{cn} . As in any analog adaptive algorithm, the derivation of e_{cn} is of interest. Note that the signal e_1 is mixed with e_0 . The output of the mixer is filtered and amplified, giving a complex voltage proportional to correlation of e_1 with e_0 . The correlator's output is subtracted from a beam-steering voltage V_1 to give e_{c1} . For the moment, assume that

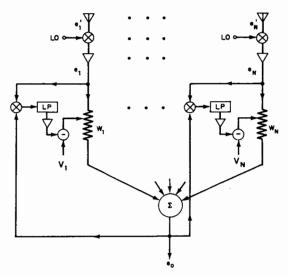


FIG. 22-10 Applebaum-Howells circuit.

 $W_1 = V_1$. If e_0 is correlated with e_1 , the low-pass filter integrates the output of the correlator to produce $e_{c1} \neq 0$, which changes the weight W_1 so as to reduce the correlation between e_0 and e_1 , decreasing the output of the correlator. Similar responses in the other loops reduce e_0 to a minimum. Combined noise in the circuit and in e_1 prevents e_0 from vanishing. Hence we see that any signal (in e_1) above the effective noise level will be sensed by the loop and weighted to reduce e_0 ; the combined effect of all N loops is to reduce e_0 below the effective noise level of the correlators. Furthermore, in the absence of signals (interfering or desired) greater than the front-end noise level, the weights will be determined by the noise. However, if the V_n are not zero, they will determine the weights, and the antenna receiving pattern will assume its quiescent shape.

The quiescent weights are determined a priori from known or expected locations, etc. It can be shown that when $M_I \gg M_N > M_D$, $M \sim M_I$, and the steady-state weights assume the optimum values given by Eq. (22-9). The transient performance and convergence to stable steady-state weights that equal W_0 are of paramount concern and will be discussed later.

In summary, the Applebaum-Howells⁷ circuit establishes W_0 when the desired-signal locations and antenna receiving pattern are known and used to determine V. It is also necessary to choose the nulling bandwidth W so that the level of the desired-signal received power S is approximately equal to or less than the front-end noise power in the band W (i.e., $M_S \leq M_N$). This circuit senses the locations of all interfering sources and reduces their received signals below the front-end noise level. If the interfering and desired sources are located near one another, the desired signal may also be reduced, but the ratio e_{ln}/e_{dn} will not be increased; it will probably be decreased.

Maximization of Signal-to-Noise Ratio

When there is a single desired-signal source present in an environment of one or many interfering sources, the definition of S/N is clear. This is not true when more than one desired source is present; however, the Applebaum-Howells circuit, discussed in the preceding subsections, allows for optimum adaptation when several desired sources and several interfering sources exist simultaneously. When there is only a single user and its location is known, the Applebaum-Howells circuit will maximize S/N if the quiescent weights V are chosen to form a single receiving pattern with maximum directivity in the direction of this desired source. By comparison, the circuit shown in Fig. 22-11 will form and steer a high-directivity beam in an unknown desired-signalsource direction while simultaneously placing a null on all interfering sources. This is accomplished without knowledge of the location of either the desired or the interfering sources. However, it is necessary to derive a reference signal that is a suitable replica of the expected desired signal. This can lead to the dilemma that if the desired signal must be known prior to adaptation, there is no need to send it to the receiver. However, the desired signal might have a deterministic component (i.e., a pseudo-noise sequence or a frequency-hopped "carrier") and a random component (i.e., that modulation on the carrier that contains unknown information). The former would be used to permit the adaptation circuit to recognize a desired signal and maximize the associated S/N.

The circuit shown in Fig. 22-11 is identical to the Applebaum-Howells circuit (Fig. 22-10) discussed in the preceding subsection except for the output portion and the absence of steering weights. A reference signal e_{REF} is subtracted from e'_0 to generate an error signal with which the e_n are correlated and the W_n determined. Some sort of

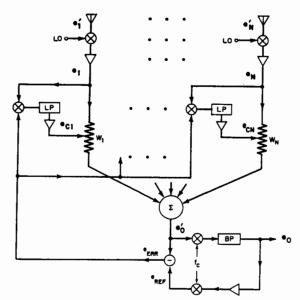


FIG. 22-11 Widrow algorithm.

spread-spectrum modulation is assumed so that a reference signal can be obtained by despreading e'_0 and bandpass-filtering it in order to increase the S/I of e_{REF} compared with the S/I of e'_0 . Amplifying the demodulated e'_0 (i.e., to obtain e_0) and modulating it with the known spread-spectrum modulation sequence results in a reference signal e_{REF} .

To understand the operation of this circuit, assume that the interfering component of e_0' is much larger than the desired-signal component. Consequently, the error signal is dominated by the interference signal, and the correlators drive the weights to reduce e_0 by placing nulls in the direction of the interfering source. Reduction of the interfering source will not, in general, reduce the desired signal. Because the reference signal is principally an amplified replica of the desired signal, the correlators drive the weights to *increase* the desired signal in order to reduce the error signal $e_{\rm ERR}$. This adjustment of the weights is identical to steering a receiving pattern with maximum directivity toward the desired source while simultaneously placing nulls in the direction of the interfering source.

This circuit (Fig. 22-11) is commonly referred to as the Widrow circuit after its inventor. It is often recommended for use in time-division—multiple-access (TDMA) communication systems employing pseudo-noise modulation as spread-spectrum protection against interfering sources. The Widrow circuit is limited to multiple-interference-source scenarios with a single desired source because the beam will be acquired only by a desired signal that is in synchronism with the spread-spectrum modulation.

It is interesting to note that if there is one desired source in the FOV, the Apple-baum-Howells and Widrow circuits produce the same steady weights if the V are chosen to steer the beam in the direction of the desired source. That is, the Widrow circuit contains a closed-loop determination of the V, whereas the Applebaum-Howells circuit requires that V be an externally generated open-loop constraint. Consequently, the former is applicable for scenarios with a single desired source, whereas the latter is applicable for any scenario for which a prescribed quiescent receiving pattern is essential, such as satellite-communication-system-spacecraft antennas that must have an earth-coverage or multiple-area-coverage receiving pattern to serve multiple users simultaneously.

Transient Characteristics

All analog and essentially all computational nulling algorithms require a finite time to respond to the onset of an interfering signal. These transient effects and a computational algorithm which eliminates them will be discussed in this subsection.

It can be shown⁴ that for a single interfering source the time constant of the nth cancellation loop (Fig. 22-10 or Fig. 22-11) is inversely proportional to the product of the loop gain and the power P_n received at the nth port. Hence, increasing the loop gain decreases the time to adapt; however, the loop gain must be low enough to prevent unstable operation. Therefore, setting the loop gain in accordance with the strongest expected interference-signal source prevents loop instability and determines the shortest possible time required for the antenna system to complete its adaptation function. If two interfering sources, one strong and one weak, are present, the stronger source is at first reduced rapidly to a level somewhat higher than its steady-state level. Then at a much slower rate its signal strength is reduced until both interfering signals are reduced to their steady-state level at the *same* time. Consequently, it is important to set the loop gain so that the weakest expected interfering-signal strength will result in

a tolerable loop time constant. If the spread in strength of all troublesome interference sources is sufficiently large, it may not be possible to choose a suitable loop gain. This situation is often referred to as an excessive spread in the eigenvalues of the covariance matrix M.

Sample Matrix Inversion

Although the circuits shown in Figs. 22-10 and 22-11 indicate the use of analog devices, it is not uncommon to use digital devices between the output of the correlator and the control terminal of the weights. Within the scope of this report, these changes do not modify the preceding discussions. However, consider a processor which converts the antenna terminal voltages e_n to a digital representation and completes the adaptation process entirely within a computational processor. For example, the processor indicated in Fig. 22-12 (LPF = low-pass filter) first demodulates the spread-spectrum modulation of the received signals and establishes an IF bandwidth that retains the necessary power differences between interfering and desired signals. The signals are amplified, to establish the system thermal noise level, and divided into two identical channels except for a relative phase of 90°. The signals are then converted to baseband and divided into a narrow signal band and a wider nulling band. All signals are then converted to a digital representation; the wideband signals are used to compute the covariance matrix M, its inverse M^{-1} , and the optimum weights. The narrowband

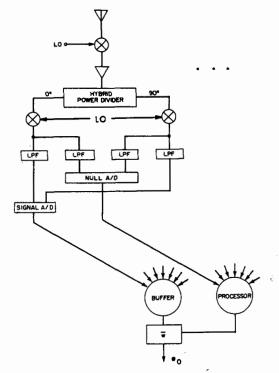


FIG. 22-12 Sample matrix inversion.

signals are stored in a buffer while the weights are being computed. As the narrow-band signals leave the buffer, they are then weighted, summed, and filtered to yield a digital representation of the desired signals. Notice that this processor eliminates the transient performance of the weights and has the linearity characteristics of a digital computer. However, the signals must undergo a delay while the weights are computed, and there is not a feedback loop as with the Applebaum-Howells and Widrow algorithms. As with all feed-forward systems, implementation must have accuracy commensurate with the desired signal suppression. In other words, the covariance matrix M must be estimated from the measured "samples" of the received signals. The performance of this algorithm is determined by the accuracy with which M is estimated, the rate at which the computations can be made, and the speed and accuracy of the analog-to-digital converters.

22-8 MULTIPLE-BEAM ANTENNA VERSUS PHASED ARRAY

Historically, adaptive antennas have used either an array antenna or an MBA. It is often important to be aware of the fundamental differences of these devices and how they affect the adaptive-antenna-system performance. In this section, the inherent bandwidth is discussed as an aid in choosing one antenna instead of the other.

Bandwidth

Classically and historically, phased-array antennas are focused to receive signals from a given direction by adjusting an array of phase shifters. Specifically, the differential time delay τ_n associated with signals arriving at the ports of the array elements is corrected by inserting a variable delay τ_n in the range $0 < \tau_n < \tau - p\lambda/c$, where p is an integer. Consequently, the array is perfectly "focused" at the design frequency f_0 and becomes defocused as the operating frequency f varies from f_0 .

For a signal source located near the boresight direction of the array, p is small, and the array antenna does not become appreciably defocused even for a large bandwidth $\Delta f = |f_0 - f|$. A rule of thumb relating Δf to antenna aperture D and θ , the angle between the signal-source direction and a normal to the plane of a planar-antenna array, can be derived as follows. The maximum differential path delay S_{max} is given by

$$S_{\text{max}} = (D/\lambda) \sin \theta \tag{22-19}$$

The phase shifter inserts a delay S_1 less than λ , and the error ϵ in differential path delay is given by

$$\varepsilon = \text{integer}[(D/\lambda) \sin \theta] \cdot \frac{\Delta f}{2f_0}$$
 (22-20)

For (D/λ) sin $\theta \gg 1$, the integer-value operation can be removed without seriously affecting the results. Solving Eq. (22-20) for the fractional bandwidth yields

$$\frac{\Delta f}{f_0} = \frac{2\varepsilon\lambda}{D\sin\theta}$$
 (22-21)

If one assumes that ε must be less than 0.1 (i.e., a path-length error = $\lambda/10$), $\theta = 10^{\circ}$, and D = 120 λ , Eq. (22-21) indicates a 1 percent frequency bandwidth. Calculated results³ indicate that for $\varepsilon = 0.1$ the interference signal will be suppressed ~ 20 dB; doubling or halving Δf changes the signal suppression to 14 dB or 26 dB respectively. That is, signal suppression varies approximately as Δf^2 .

Most MBAs use a lens or a paraboloid which focuses received signals by introducing differential path delays (as opposed to phase shifting) and translating a feed located in the focal region of the lens or paraboloid. Consequently, the system remains focused over a very wide frequency band. However, the sidelobes and receiving pattern shape change with frequency and tend to alter the amplitude instead of the phase of the received signals. Studies have indicated that this effect of varying frequency does not degrade the associated adaptive-antenna performance as much as that of an "equivalent" planar array because each beam of the MBA performs like a phased array with its receiving beam in the boresight direction. Since the sidelobes of an MBA do not dominate the determination of the weight applied to a beam port, an MBA with an aperture $D = 120\lambda$ can suppress interfering signals more than 20 dB for $\Delta f/f \sim 5$ percent.

In some applications, an array antenna is preferred to an MBA. By using the foregoing, the operating bandwidth can be estimated. If the expected $\Delta f/f_0$ meets or exceeds system requirements, the phased array may be the best choice. If the estimated $\Delta f/f_0$ is less than required, an MBA may be the best choice.

Channel Matching

Adaptive antennas suppress interfering signals in accordance with the qualitative relationship³ given in Sec. 22-3 and the similarity among the transfer functions L_n of each of the N channels. In large-aperture (D) antennas operating over a large bandwidth W, such that DW/C > 1, the natural dispersion of array antennas may limit the cancellation ratio C (see Sec. 22-3). C can also be limited by channel mismatch

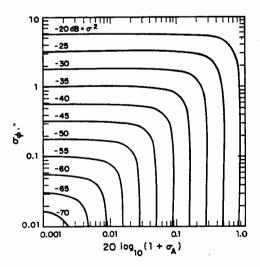


FIG. 22-13 Estimated cancellation.

 $\Delta L_{mn} = L_n - L_m \neq 0$ when frequency-independent weights are used. The use of frequency-dependent weights (Fig. 22-5) improves C in the presence of both antenna dispersion and channel mismatch. Rigorous simulation is usually required to determine the expected value of C. However, as a guide to the tolerable rms variation of ΔL_{mn} , it is useful to refer to Fig. 22-13, where the required rms amplitude and phase variation of L_n of a two-channel system are given as a function of the cancellation ratio C. The reader is cautioned to apply these results only to obtain a qualitative estimate of the expected performance of adaptive antennas with more than a few elements or beam ports.

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Methods of Polarization Synthesis

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Consultant

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23-1	General Discussion 23-2
	Typical Applications 23-3
	Polarization Synthesis 23-4
	Transmission between Two Elliptically
	Polarized Antennas 23-7
	Orthogonality 23-9
	Reflection 23-10
	Measurement Problems 23-10
23-2	Frequency Reuse by Polarization Decoupling 23-1
23-3	
23-4	Dual-Mode Horn Radiators 23-16
	Symmetrical Case 23-16
	Asymmetrical Case 23-20
	Methods of Obtaining Quadrature 23-20
	Dual-Mode Generation 23-23
23-5	Transmission- and Reflection-Type Polarizers 23-2
23-6	Radar Precipitation-Clutter Suppression 23-28

Cancellation Ratio 23-28

The plane of polarization, or simply the polarization, of a radio wave is defined by the direction in which the electric vector is aligned during the passage of at least one full cycle. In the general case, both the magnitude and the pointing of the electric vector will vary during each cycle, and the electric vector will map out an ellipse in the plane normal to the direction of propagation at the point of observation. In this general case

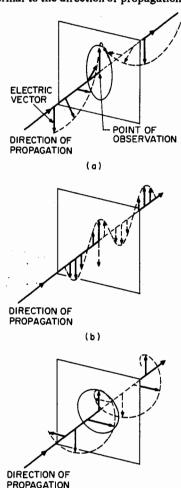


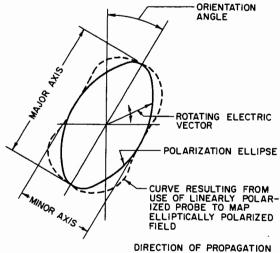
FIG. 23-1 Diagrammatic illustration of waves of various polarization. (a) Elliptical polarization. (b) Linear polarization. (c) Circular polarization (right-hand).

(c)

(shown in Fig. 23-1a), the polarization of the wave is said to be elliptical. The minor-to-major-axis ratio of the ellipse is called the *ellipticity* and will be expressed in this chapter in decibels. (Although the axis ratio is less than unity, when expressing ellipticity in decibels, the minus sign is frequently omitted for convenience. The term axial ratio is also in common use. It is the reciprocal of ellipticity.) The direction in which the major axis lies is called the *polarization orientation* and in this chapter will be measured from the vertical (Fig. 23-2).

The two special cases of ellipticity of particular interest are (1) an ellipticity of ∞ dB (minor-to-major-axis zero), which is linear polarization, and (2) an ellipticity of 0 dB (minor-tomajor-axis ratio unity), which is circular polarization. A linearly polarized wave is therefore defined as a transverse electromagnetic wave whose electric field vector (at a point in a homogeneous isotropic medium) at all times lies along a fixed line. A circularly polarized wave is similarly defined as a transverse electromagnetic wave for which the electric and/or magnetic field vector at a point describes a circle. In attempting to produce a linearly polarized wave, elliptical polarization is thought of as imperfect linear polarization, while in attempting to produce a circularly polarized wave, elliptical polarization is thought of as imperfect circular polarization.

Confusion occasionally results in the use of mental pictures similar to Figs. 23-1 and 23-2 when one overlooks the fact that although the electric vector



NORMAL TO PAGE
FIG. 23-2 Polarization ellipse.

makes one complete revolution (Fig. 23-2) per cycle, it does not rotate at a uniform rate except in the special case of a circularly polarized wave. In this special case, rotation occurs at the rate of ω rad/s.

Figure 23-1 c shows a circularly polarized wave having a right-hand sense. It is also possible, of course, to have left-hand circularly polarized waves. The definition of right-hand circular polarization as standardized by the Institute of Electrical and Electronics Engineers and as used in this chapter is as follows: for an observer looking in the direction of propagation, the rotation of the electric field vector in a stationary transverse plane is clockwise for right-hand polarization. Similarly, the rotation is counterclockwise for left-hand polarization.

One simple way of determining experimentally the sense of rotation of a circularly polarized wave is to make use of two helical beam antennas of opposite sense. A right-hand helical antenna transmits or receives right-hand polarization, while a left-hand helical antenna transmits or receives left-hand polarization. If a circularly polarized wave is received first on a right-hand helical antenna and then on a left-hand helical antenna, the antenna which receives the greater amount of signal will have a sense which corresponds to the sense of the received wave. In the case of an elliptically polarized wave, the sense will be taken to be the same as that of the predominant circular component.

Not all workers in the field use the same definition of sense. The work of different authors should be compared with this precaution in mind.

Typical Applications

Although there is reasonably general agreement on the above definitions, the use of the words circular polarization does not always have quite the same meaning to different workers in the field. The difference lies in the permissible departure (for the application at hand) from precise polarization circularity before the circularly polar-

TABLE 23-1 Two Sample Applications of Circularly Polarized Antennas and Some Typical Characteristics

·	Response to linear polarization of arbitrary orientation	Precipitation-clutter suppression in radar service (values based on search radar)
Ideal ellipticity*	0 dB	0 dB
Satisfactory ellipticity*	−3 dB	-0.5 dB
Unsatisfactory ellipticity*	-10 dB	-1.5 dB
Azimuth beamwidth	Omnidirectional	1-5*
Elevation beamwidth	20*	20*
Bandwidth	Greater than 50 percent	5-15 percent
Standing-wave ratio	5	1.15
Power rating	Milliwatt level	>100 kW, <10 MW

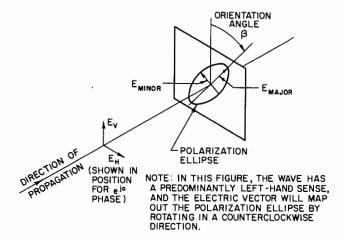
^{*}Over all or almost all of the radiation pattern.

ized antenna becomes unsatisfactory. The application of a circularly polarized antenna often falls in one of two categories. The first category is the use of a circularly polarized antenna to provide response to a linearly polarized wave of arbitrary orientation. The second category is the use of a circularly polarized antenna for suppression of precipitation clutter in radar service.² Table 23-1 shows typical characteristics for each of the applications.

Orthogonal circularly polarized antenna pairs are also in use for frequency-reuse applications with communications satellites.³ Channel isolation in excess of 20 dB is readily attainable. Reference 4 describes a practical polarization-ellipticity field measurement technique. Further discussion is in Sec. 23-2.

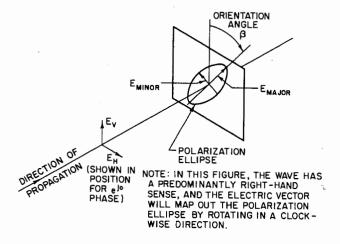
Poiarization Synthesis

Any wave of arbitrary polarization can be synthesized from two waves orthogonally polarized to each other. For example, a circularly polarized wave will be produced by the coexistence of a vertically and a horizontally polarized wave, each having the same amplitude and with a 90° phase difference between them. If they have other than the same amplitude and/or other than a 90° relationship, the resulting wave will be elliptically polarized. If, for example, the amplitude of the vertically polarized wave is zero, the resulting wave is linearly polarized and has a horizontal orientation. Further, if the two waves have equal amplitude but 0° phase difference, the resulting wave is linearly polarized with 45° orientation. There are two possible combinations of vertically and horizontally polarized waves that can produce a wave of some specific ellipticity. One of the combinations will produce a predominantly left-hand wave, and the other combination will produce a predominantly right-hand wave. Figures 23-3 and 23-4 show the two cases. Separate illustrations are provided to emphasize the need for care in specifying the coordinate system in this work and the need for consistency in adhering to the selected coordinate system while performing and interpreting any theoretical or experimental work.



$$\begin{split} & E_{V} = \frac{1}{2} \left[E_{MAJOR} \left(1 + e^{j2\beta} \right) + E_{MINOR} \left(1 - e^{j2\beta} \right) \right] \\ & E_{H} = \frac{e^{j\frac{\pi}{2}}}{2} \left[E_{MAJOR} \left(1 - e^{j2\beta} \right) + E_{MINOR} \left(1 + e^{j2\beta} \right) \right] \end{split}$$

FIG. 23-3 Linear-component synthesis of an elliptically polarized wave having a predominantly left-hand sense.



$$\begin{split} & E_{V} = \frac{1}{2} \left[E_{\text{MAJOR}} \left(\left(\right. \right) + e^{j2\beta} \right) - E_{\text{MINOR}} \left(\left. \right| - e^{j2\beta} \right) \right] \\ & E_{H} = \frac{e^{j\frac{\pi}{2}}}{2} \left[E_{\text{MAJOR}} \left(\left. \right| - e^{j2\beta} \right) - E_{\text{MINOR}} \left(\left. \right| + e^{j2\beta} \right) \right] \end{split}$$

FIG. 23-4 Linear-component synthesis of an elliptically polarized wave having a predominantly right-hand sense.

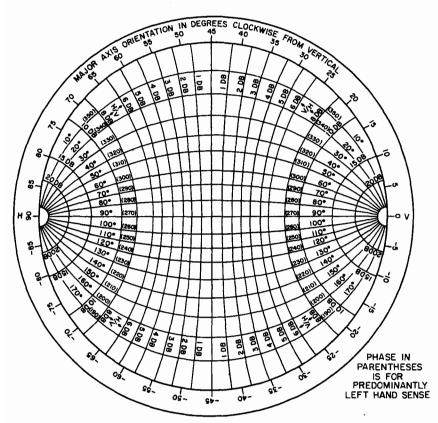


FIG. 23-5 Polarization chart.

It is often of interest to know only the ratio of the magnitudes of the vertically and horizontally polarized waves forming an elliptically polarized wave and the phase angle between them. Such information can be obtained graphically with the aid of Fig. 23-5. In this chart, the phase angle shown is the relative phase of the vertical element when the relative phase of the horizontal element is zero.

Example Given an ellipticity of 3.0 dB and an orientation of $\beta = 37^{\circ}$, find the ratio of the magnitudes of the vertically and horizontally polarized waves and the phase angle between them. Draw a line from the center of the chart to the periphery at the 37° point. Lay off a distance from the chart center to the V/H = 3.0-dB line measured on the horizontal diameter. Read V/H = 0.8 dB and a phase angle of 71° for predominantly right-hand sense or 289° for predominantly left-hand sense.

It is also possible to synthesize any elliptically polarized wave from two circularly polarized waves having opposite senses. For example, a linearly polarized wave will be produced by the coexistence of a right-hand and left-hand circularly polarized wave of the same amplitude. The orientation of the resulting linearly polarized wave will be determined by the phase difference between the two circularly polarized waves. Figure 23-6 provides the formulas for calculating the values.

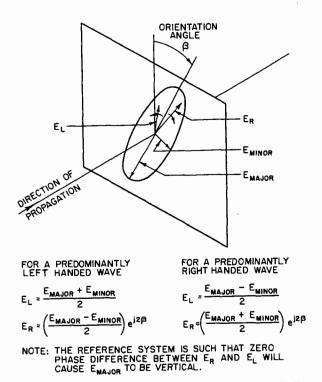


FIG. 23-6 Circular-component synthesis of an elliptically polarized wave.

Transmission between Two Elliptically Polarized Antennas

In order that a receiving antenna may extract the maximum amount of energy from a passing radio wave, it must have a polarization identical with that of the passing wave. For example, a vertically polarized receiving antenna should normally be used to receive a signal from a vertically polarized transmitting antenna. (The discussion assumes no polarization distortion in the transmission path.) Similarly, a right-hand circularly polarized antenna should be used for the reception of waves from a right-hand circularly polarized transmitting antenna. In general, maximum transmission will result between two elliptically polarized antennas when:

- 1 Their axis ratios $E_{\text{minor}}/E_{\text{major}}$ are the same.
- 2 Their predominant senses are the same.
- 3 Their ellipse orientations are translated by a minus sign; that is, $\beta_{\text{trans}} = -\beta_{\text{rec}}$.

Note that Condition 3 will result in parallel-ellipse major axes in space and implies that only in three special cases will identical antennas at each end of the circuit with the same orientation yield maximum transmission. These three cases are:

TABLE 23-2 Transmission Efficiency with Various Polarizations at the Transmitting and Receiving Antennas

Antenna 1	Antenna 2	P/P _{mex}
Vertical, e.g.: $E_R = 1$ $E_L = 1e^{j0}$ $\beta = 0$	Vertical, e.g.: $E_R = 1$ $E_L = 1e^{j0}$ $\beta = 0$	1
Vertical, e.g.: $E_R = 1$ $E_L = 1e^{f0}$ $\beta = 0$	Horizontal, e.g.: $E_R = 1$ $E_L = 1e^{f\pi}$ $\beta = 90^{\circ}$	0
Vertical, e.g.: $E_R = 1$ $E_L = 1e^{j0}$ $\beta = 0$	Circular (right), e.g.: $E_R = 1$ $E_L = 0$	1/4
Circular (right), e.g.: $E_R = 1$ $E_L = 0$	Circular (left), e.g.: $E_R = 0$ $E_L = 1$	0
Circular (left), e.g.: $E_R = 0$ $E_L = 1$	Circular (left), e.g.: $E_R = 0$ $E_L = 1$	1

- 1 $\beta = 0^{\circ} \text{ or } 180^{\circ}.$
- 2 $\beta = \pm 90^{\circ}$.
- 3 $E_{\text{minor}}/E_{\text{major}} = 1$, so that β has no significance.

Identical antennas can always be made to yield maximum transmission, however, if they are rotated so as to cause the major axes of their waves to be parallel in space.

When two arbitrarily polarized antennas are used, the normalized output power from the receiving-antenna terminals will be

$$\frac{P}{P_{\text{max}}} = \frac{|(E_{R1}E_{R2} + E_{L1}E_{L2})|^2}{(|E_{R1}|^2 + |E_{L1}|^2)(|E_{R2}|^2 + |E_{L2}|^2)}$$
(23-1)

All four variables in Eq. (23-1) are vector quantities. Similar expressions in terms of linear components, or axial ratios, may be found in References 5 and 6.

The values of E_R and E_L may be obtained with the aid of Fig. 23-6. Table 23-2 shows some typical combinations of interest.

Figure 23-7 shows a graphical means developed by Ludwig to display the maximum and minimum values of loss due to mismatched polarization between two antennas of arbitrary polarization. As an example of the use of the graph, if a predominantly right-hand polarized (RCP) transmitting antenna has an axial ratio of 8 dB and a predominantly left-hand polarized (LCP) receiving antenna has an axial ratio of 4 dB, draw two straight lines which intersect at the point P shown on the graph. This point is near the minimum-loss curve of 4 dB and the maximum-loss curve of 16 dB, and therefore the loss will vary (approximately) between 4 and 16 dB as one or

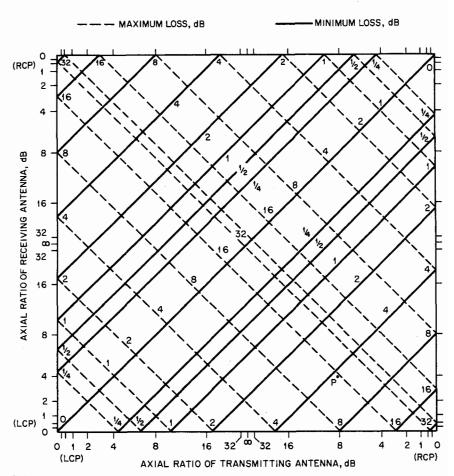


FIG. 23-7 Polarization loss between two elliptically polarized antennas.

the other antenna is rotated about its axis.* Further use of the graph to determine true gain with respect to a perfectly polarized antenna is described in Ref. 7.

Orthogonality

For any arbitrarily polarized antenna, there can be another antenna polarized so that it will not respond to the wave emanating from the first antenna. The polarizations of the two are said to be orthogonal. Using the convention of Fig. 23-6, two polarization ellipses will be orthogonal if they satisfy the relation

^{*}Portions of this paragraph and Fig. 23-7 are reprinted with permission from publishers of Microwave Journal.

$$-E_{R1}E_{R2}=E_{L1}E_{L2} (23-2)$$

Figure 23-5 can be used to determine the orthogonal-polarization ellipse to a given ellipse by performing an inversion through the center of the chart and reading the phase-shift scale associated with the opposite predominant sense.

Reflection

When a vertically polarized wave is reflected from a smooth surface, there is no change in its character.* When a horizontally polarized wave is reflected from a smooth surface, because of the coordinate-system reversal in space when one looks in the reversed direction of propagation, there is a 180° phase change. When a circularly polarized wave is reflected from a smooth surface, its horizontal component is altered by 180°; hence the sense of the wave is reversed. For an elliptically polarized wave, reflection is equivalent to altering the differential phase shift (e.g., the phase difference between the horizontally and vertically polarized linear components) by 180°. The new polarization ellipse may be determined with the aid of Fig. 23-5 by inverting the original (before reflection) ellipticity across the horizontal diameter and reading the phase-shift scale corresponding to the opposite predominant sense.

Circularly polarized antennas are unique in being entirely unable to "see" their own images in any symmetrical reflecting surface, since the reflected wave has its sense reversed and is, therefore, orthogonal to the polarization of the antenna from which it originated.

Measurement Problems

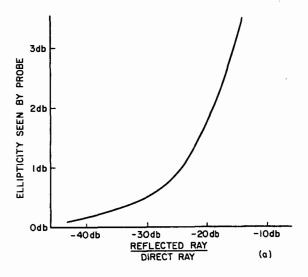
The measurement of circularly polarized antennas is generally similar to that of other antenna types, except that it is often necessary to measure the state of polarization (degree of polarization ellipticity, or axial ratio) as well as the other more customary parameters. An experimentally convenient technique is to employ a linearly polarized antenna, arranged to rotate about its boresight axis, to probe the field. The resulting data will define the ellipticity but not its right-hand or left-hand sense, which must be separately determined.

Attention is called here to the unusual degree of sensitivity of polarization measurement to small distorting influences of secondary paths in a measuring setup. Figure 23-8 illustrates the conditions.

23-2 FREQUENCY REUSE BY POLARIZATION DECOUPLING

The expanded number of communications satellites in use has made it necessary to use the same frequency to communicate with closely spaced areas on the earth. Commonly called *frequency reuse*, this method requires a decoupling mechanism between

^{*}Strictly speaking, this statement is correct only if the smooth surface is the interface between a normal propagation medium and one having an impedance of infinity. However, we are here interested only in the relative difference between the vertical and horizontal cases, so this detail will be overlooked.



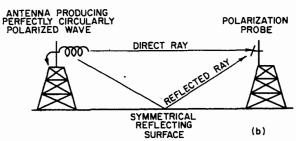


FIG. 23-8 Influence of the reflected wave on the measurement of a circularly polarized wave.

overlapping beams. Although careful shaping of the beams has been used in some cases, the use of orthogonal polarizations is more common. However, this puts stringent requirements on the amount of cross-polarization that can be present on any individual beam. Since the most common type of antenna used for satellite communications is a reflector antenna, the polarization properties of reflectors have been studied in great detail.⁸⁻¹²

Offset reflectors, which essentially eliminate aperture blockage, in particular have received a considerable amount of attention. Methods of computing the interbeam isolation and thus the frequency-reuse performance have been developed. To a symmetrical paraboloid, it has been shown that a physically circular feed with equal E- and H-plane amplitude and phase patterns will produce no cross-polarization; however, in an offset configuration, cross polarization will be present because of the asymmetry. Chu and Turrin have computed the maximum cross-polarization as a function of the offset angle θ_c and half of the reflector subtended angle θ_0 for linear polarization with a circular symmetric feed providing a 10-dB taper at the aperture edges. Their results, presented in Figs. 23-9 and 23-10, show that the amount of cross-

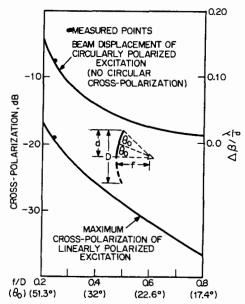


FIG. 23-9 Cross-polarization and beam displacement versus f/D ratio ($\theta_c = \theta_c$). (© 1973, IEEE.)

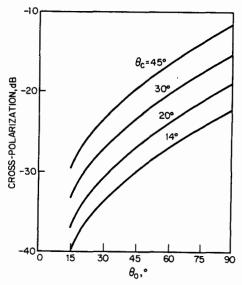


FIG. 23-10 Maximum cross-polarization of linearly polarized excitation. (© 1973, IEEE.)

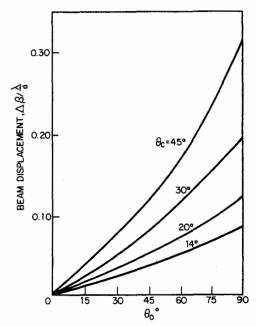


FIG. 23-11 Beam displacement of circularly polarized excitation (no circular cross-polarization). (© 1973, IEEE.)

polarization decreases with increasing f/D and increases with increasing offset angle. In addition, they have shown that if the feed is perfectly circularly polarized, no cross-polarized energy will be found in the far-field pattern, although the position of the beam will be displaced from the axial direction because of a phase shift across the aperture. Figure 23-11 presents their results as a function of θ_0 with θ_c as a parameter.

The reduction of cross-polarized energy in offset configurations can be accomplished by careful feed design. The complex focal fields for an incoming plane wave can be calculated and a feed horn designed to match the focal plane by using multimode or hybrid modes (see Chap. 15). Alternatively, a polarizing grid can be used in front of the feed horn to reduce the cross-polarization. ¹⁵ In general, this grid will not consist of parallel wires but will be aligned to match the polarization of the primary field incident on the reflector surface.

Additional details on the subject of frequency reuse are found in Chaps. 17, 35, 36, and 45.

23-3 COMBINATIONS OF ANTENNAS

Circular polarization can be achieved by a combination of electric and magnetic antennas provided that the fields produced by these antennas are equal in magnitude and in time-phase quadrature. A simple case of this combination is a horizontal loop

and a vertical dipole. ¹⁶ The time-phase-quadrature relationship is a fundamental relationship between the fields of a loop and a dipole when their currents are in phase. If the loop and dipole are oriented as in Fig. 23-12, the fields in the plane of the loop are given by

$$E_L = jCJ_1(ka)e^{j(\omega t - kr)}$$
 (23-3)

$$E_D = C_1 e^{i(\omega t - kr)} \tag{23-4}$$

where C and $C_1 = constants$

 $k = 2\pi/\lambda$

 λ = free-space wavelength

a = radius of loop

r =distance from center of loop

 J_1 = Bessel function of the first order

provided that the currents in the loop and dipole are in phase. Thus, if

$$CJ_1(ka) = C_1$$
 (23-5)

the resulting field of the combination will be circularly polarized. Equation (23-5) will be true if the loop diameter is less than about 0.6 wavelength and the dipole length is less than a half wavelength. In this particular combination it should be noted that the resulting radiation pattern is circularly polarized at all points since the individual pattern of the loop and dipole are essentially the same. However, in practice this is difficult to obtain, except over narrow bandwidths, because of the different impedance characteristics of the loop and dipole.

A second combination is that shown in Fig. 23-13, consisting of two vertical one-half-wavelength-long cylinders in which vertical slots are cut. ¹⁶ Feeding the two vertical cylinders will give a vertically polarized omnidirectional pattern in the plane normal to the axis of the cylinders, while feeding the two slots will give a horizontally polarized pattern in the same plane. If the power to both feeding arrangements is adjusted to be equal and the phase adjusted by controlling the length of the feed lines

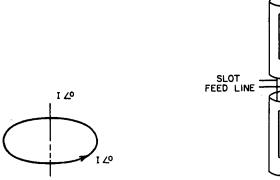


Fig. 23-12 Horizontal loop and vertical dipole.

FIG. 23-13 Slotted-cylinder circularly polarized antenna.

CYLINDER

FEED LINE

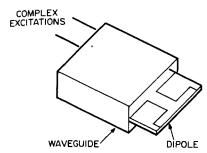


FIG. 23-14 Slot-dipole element.

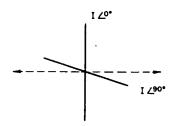


FIG. 23-15 Crossed dipoles—current in phase quadrature.

so that the two are in time-phase quadrature, the resulting pattern will be circularly polarized.

A combination of a slot and a dipole has been developed for a more directional antenna, e.g., as an element for a phased array.¹⁷ The configuration, which is shown schematically in Fig. 23-14, uses a waveguide as the slot and a printed dipole as the complementary element. Since the waveguide and dipole radiation patterns track over a wide range of angles, this combined element can be used to generate any arbitrary polarization by controlling the complex excitations of the individual elements. Some overall degradation in the polarization performance will result from the difference in phase centers between the two individual elements.

The normal radiation (broadside) mode of a helix can also be considered as a combination of electric and magnetic antennas (dipoles and loops) producing circular polarization. This type of antenna has been discussed in Chap. 13.

A pair of crossed slots in the broad wall of a rectangular waveguide in which the field configurations in the waveguide are such that one slot is in time-phase quadrature with the other can also be considered as a combination of electric and magnetic antennas producing circular polarization. This combination will be discussed in greater detail below.

Two or more similar antennas when properly oriented in either time phase or space phase or a combination of both may be used to give a circularly polarized radia-

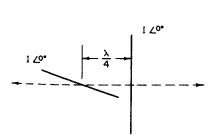


FIG. 23-16 Crossed dipoles—current in phase— $\lambda/4$ separation.

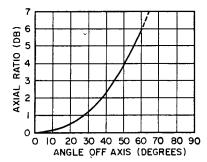


FIG. 23-17 Deviation of circularity as a function of off-axis angle for a pair of crossed dipoles.

tion field. A simple case is a pair of crossed half-wavelength dipoles. In Fig. 23-15, circular polarization is obtained by having the equal currents in the dipoles in phase quadrature. Radiation is right circularly polarized in one direction and left circularly polarized in the opposite direction. If the pair of crossed dipoles is fed in phase and separated in space by a quarter wavelength as shown in Fig. 23-16, circular polarization is again produced; however, the sense is the same in both directions. In both of these combinations the resulting field is circularly polarized only on axis. The deviation in circularity as a function of the off-axis angle is plotted in Fig. 23-17.

Another case of a simple combination of similar antennas to produce circular polarization is a pair of narrow slots at right angles and located at the proper point in the broad wall of a rectangular waveguide. ¹⁸ This may be explained by noting that the equations for the transverse and longitudinal magnetic fields of the dominant (TE_{10}) mode in rectangular waveguide (Fig. 23-18) are

$$H_x = H_0 \quad \sqrt{1 - \left(\frac{\lambda}{2a}\right)^2} \sin \frac{\pi x}{a}$$
 (23-6)

$$H_z = -jH_0 \frac{\lambda}{2a} \cos \frac{\pi x}{a} \tag{23-7}$$

From these two equations it may be seen that the fields are in phase quadrature and there are two values of x at which $|H_x| = |H_x|$. These values of x are given by

$$x = -\frac{a}{\pi} \cot^{-1} \left[\pm \sqrt{\left(\frac{2a}{\lambda}\right)^2 - 1} \right]$$
 (23-8)

Two crossed slots at either of these points will then radiate circularly polarized energy. Figure 23-19 is a plot of x versus λ over the wavelength range between the cutoff of the TE₁₀ and TE₂₀ modes. The orientation of the slots is arbitrary, and they may be made resonant and thus radiate a large amount of power (Chap. 8). The theoretical axial ratio for x = a/4 is shown in Fig. 23-20, which gives circular polarization at a frequency for which $\lambda = 2a/\sqrt{2}$.

23-4 DUAL-MODE HORN RADIATORS

A conventional waveguide horn may be used for the radiation and beaming of circularly polarized waves provided that it is fed with waveguide capable of propagating vertically and horizontally polarized waves simultaneously. The horn may be either symmetrical or asymmetrical, that is, square (round) or rectangular (elliptical). Figure 23-21 illustrates two types.

Symmetricai Case

A circularly polarized field will be obtained on the peak of the radiation pattern when the horn is fed through the square waveguide with equal-amplitude vertically and horizontally polarized modes arranged to be in quadrature. The radiated field will not, in general, be circularly polarized at other points on the radiation pattern because the vertically and horizontally polarized radiation patterns will have different bandwidths.

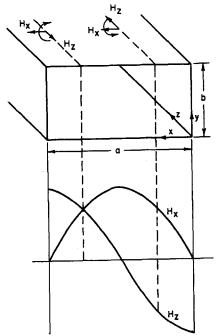


FIG. 23-18 Field configuration, TE₁₀ mode.

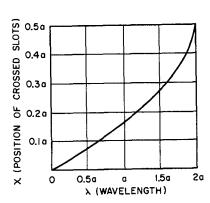


Fig. 23-19 Position of crossed slots for circular polarization versus wavelength.

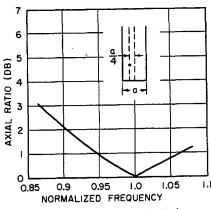
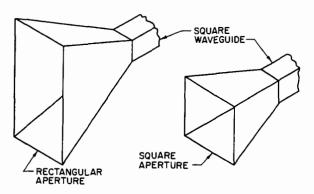


FIG. 23-20 Theoretical axial ratio for x = a/4.



ASYMMETRICAL HORN

SYMMETRICAL HORN

FIG. 23-21 Examples of symmetrical and asymmetrical dual-mode horns.

There are several methods useful in compensating for the two different beamwidths. Figure 23-22 shows two methods applied to the *azimuth plane* only of the horn. In actual practice, it is necessary to apply one of these methods (usually method B) to the elevation plane as well as to the azimuth plane.

When designing a circularly polarized horn for some specific radiation-pattern width, the standard design methods (such as those in Chap. 6 and Ref. 19) are appli-

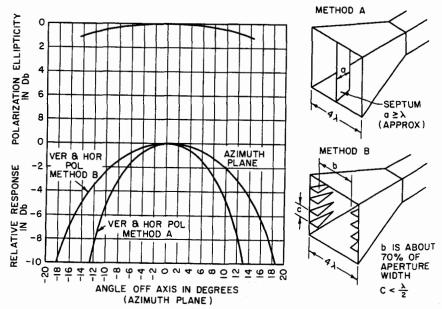


FIG. 23-22 Two methods of compensating dual-mode homs for improved circularity.

cable, bearing in mind, of course, that an *E*-plane dimension for one polarization is an *H*-plane dimension for the other and also bearing in mind the effects of any compensating scheme.

When the horn is designed along conventional pyramidal or sectoral lines, phase tracking for the vertically and horizontally polarized fields is usually not a problem; that is, the radiation centers of phase for the two polarizations are sufficiently close so that differential phase-shift variations over the radiation pattern usually do not exceed about 10 to 15° within the tenth-power points on the beam.

Horns are sometimes constructed with a wide flange around the aperture for mechanical reasons. On small horns especially, the flange width should be no larger than necessary to avoid degradation of phase tracking.

Simple conical horns have beamwidths more alike for the two principal polarizations than do pyramidal horns. Controlled excitation of TM₁₁ modes can further refine beamwidth matching. However, such structures are not as conveniently connected to square or rectangular waveguide as pyramidal horns.²⁰

Corrugated conical horns offer excellent radiation-pattern amplitude and phase tracking for the two principal polarizations over bandwidths of half an octave³ or more.

Measurements reported in the literature²¹ show that cross-polarization components suppressed 30 dB or more from 8 to 11 GHz over all angles within approximately ±45° of boresight. The conical-horn geometry is shown in Fig. 23-23. These structures tend to be larger for a given beamwidth than those of Fig. 23-22 and may limit the closeness of adjacent secondary-beam pointing when they are used as juxtaposed feeds.

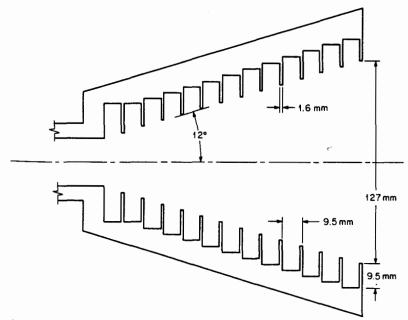


FIG. 23-23 Section through conical corrugated horn---9-GHz nominal design frequency.

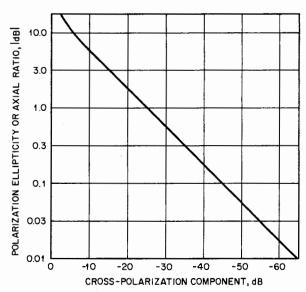


FIG. 23-24 Relationship between polarization ellipticity or axial ratio and cross-polarization component.

Figure 23-24 shows the relationship between polarization ellipticity and crosspolarization component.

Asymmetrical Case

The preceding discussion is also applicable to asymmetrical horns, except that circularly polarized fields on the peak of the radiation pattern will not be obtained unless allowance is made for the difference in phase velocity of the vertically and horizontally polarized waves within the asymmetrical-horn flare. This differential phase shift may attain quite large values. For example, a measured differential phase shift of about 220° has been observed at 2800 MHz in a horn having a flare length of about 14 in (356 mm), a width of 2.84 in (72.1 mm), and a height of 7.8 in (198 mm).

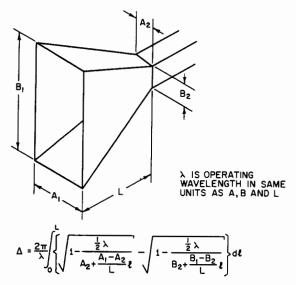
The magnitude of differential phase shift can be computed to an accuracy of perhaps 10 percent by evaluating the integral

Differential phase shift =
$$\int_{0}^{L} [\beta(\ell) - \beta(\ell)] d\ell$$
 (23-9)

in which L is the flared length of the horn and $\beta(\ell)$ is based simply on the appropriate width of the flare and the operating wavelength. Figure 23-25 shows the information in detail. Note that the differential phase shift may vary fairly rapidly with frequency. In the example mentioned above, the differential phase shift increased by about 15° for every 100-MHz decrease in frequency between 2900 and 2700 MHz.

Method of Obtaining Quadrature

Quadrature phase relationship between two orthogonally polarized modes in round or square waveguide may be achieved by any of the following techniques:



Δ IS DIFFERENTIAL PHASE SHIFT IN RADIANS

FIG. 23-25 Method of determining differential phase shift in a sectoral horn.

- 1 Rectangular or elliptical cross section
- 2 Ridge guide
- 3 Dielectric slab
- 4 Multiple-lumped-element loading
- 5 Turnstile junction

The choice of method must be based on the application, keeping such things in mind as ease of design, bandwidth, power-handling capacity, ease of adjustment, and ease of fabrication. Table 23-3 shows the trend of these characteristics in order.

TABLE 23-3 Preference Trends for Methods for Obtaining Phase Quadrature

Method	Ease of design	Band- width	Power- handling capacity	Ease of adjustment	Ease of fabrication (small quantity)
Rectangular or elliptical cross-section guide	1	5	1	5	4
Ridge guide	4	3	2	2	3
Dielectric slab	5	2	5	3	1
Multiple-lumped-element loading	2	1	3	1	2
Turnstile junction	3	4	4	4	5

The first three methods listed above are based on causing the phase velocity of the vertically and horizontally polarized modes to differ within the same section of guide. This section of guide will then be of different phase length for the two polarizations. Selection of the appropriate length to furnish the requisite differential phase shift is the last step in the design process.

For example, a rectangular section of waveguide carrying TE_{01} and TE_{10} modes and having internal dimensions a and b will produce differential phase shift at the rate of

$$\frac{2\pi}{\lambda} \left[\sqrt{1 - \left(\frac{\lambda}{2a}\right)^2} - \sqrt{1 - \left(\frac{\lambda}{2b}\right)^2} \right]$$
 rad/unit length

The values for a, b, and λ must be in the same units, of course. If such a section is to be connected to a square waveguide, it will be necessary to employ a suitable intermediate transformer section. Quarter-wavelength sections having an impedance equal to the geometric mean of the input and output impedances are satisfactory. Note that the differential phase shift (which can be computed with the aid of the above formula) of the transformer will contribute to the total.

Ridge guide can be handled in the same manner as the above rectangular guide. In the ridge case, however, the quantities 2a and 2b in the above expression should be replaced with λ_{CUTOFF} for TE₀₁ and λ_{CUTOFF} for TE₁₀ respectively.

Dielectric-slab loading in a square guide will also produce a difference in phase velocity for the two modes of interest. Figure 23-26 provides the pertinent information for a typical case. Just as above, it is necessary to provide means for obtaining an impedance match at each end of the phasing section. It is not sufficient as a rule to have the phasing section as a whole appear matched; it is important to have each end matched by itself. If this precaution is not observed, it will be very difficult to predict total phase shift as well as the change in phase shift with a change in geometry. In short, adjustment, or tailoring, is difficult. Power-handling capacity will be somewhat lower also.

Lumped-element loading in a square guide has also been used successfully. The use of probe pairs is particularly convenient. Pair doublets and pair triplets are the most convenient, with the latter providing greater bandwidth and greater power-handling capacity for a given differential phase shift. Figure 23-27 shows design data for

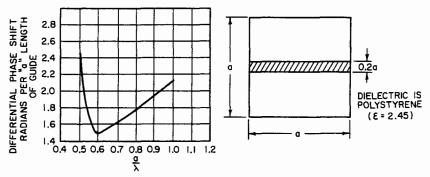


FIG. 23-26 Differential phase shift in a partially loaded square waveguide.

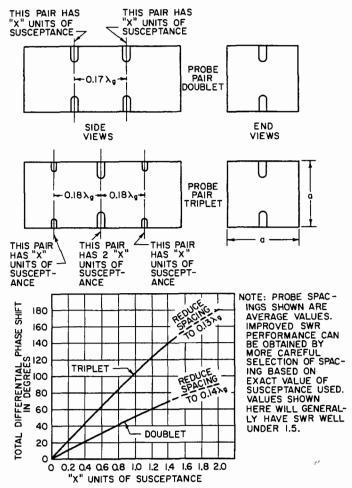


FIG. 23-27 Probe phase-shifter design.

the doublet and triplet cases. The length of the probe necessary for a given value of susceptance is shown in Fig. 23-28.

Circularly polarized waves can be generated directly in a waveguide junction known as a turnstile junction (not to be confused with a turnstile antenna). The general geometry is illustrated in Fig. 23-29.

Dual-Mode Generation

The generation of two orthogonally polarized modes in a section of square or round guide can be accomplished in several ways, of which the two most common are:

- 1 Coaxial cable probes at right angles
- 2 Conventional rectangular waveguide inclined at 45°

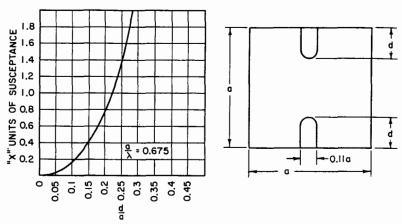


FIG. 23-28 Susceptance as a function of probe penetration.

The second case is especially convenient because the ratio of magnitudes of the vertically and horizontally polarized waves can be altered merely by altering the inclination of the rectangular guide.

In generating and guiding dual modes in square or round guide, care should be employed to keep the geometry symmetrical about each of the two principal longitudinal planes. Any asymmetry will tend to excite the TM_{11} or TE_{11} modes. For square or round guide, these two modes will usually not be very far from cutoff. For example, in square guide, with dimensions a high and a wide, cutoff for the TE_{01} and TE_{10} modes occurs at $\lambda = 2a$. The cutoff for TM_{11} and TE_{11} modes occurs at $\lambda = 2\sqrt{2a}$, or only about 41 percent above cutoff for the dominant modes.

In all the discussion above concerning phase shift, it has been assumed that there is an impedance match for each of the generated dual modes. The existence of mis-

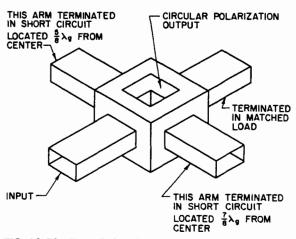


FIG. 23-29 Turnstile junction.

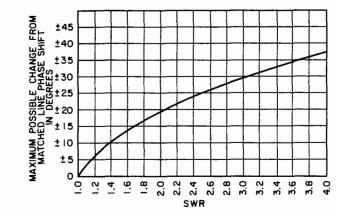


FIG. 23-30 Possible phase variation with standing-wave ratio.

match may produce an unexpected alteration in the phase shift. For example, if there is a perfect match for both the vertically and the horizontally polarized modes and the differential phase shift noted, the appearance of a mismatch in one of the modes may produce a change in differential phase shift as shown in Fig. 23-30. If the same magnitude of mismatch appears in both modes, the change may be as large as twice that of Fig. 23-29.

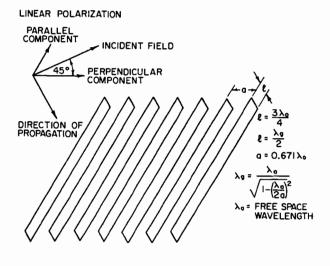
23-5 TRANSMISSION- AND REFLECTION-TYPE POLARIZERS

A transmission polarizer is an anisotropic propagation medium whose anisotropy is adjusted to achieve time (i.e., phase) quadrature for two waves whose (linear) polarization vectors are mutually orthogonal. Such polarizers operate independently of the nature of the source of the waves, are often relatively bulky and awkward to adjust, can be very inexpensive to manufacture, and can have very high power-handling capability.

The simplest type of polarizer is a parallel-metal-plate structure (Fig. 23-31). In this structure, the incident linearly polarized energy is inclined 45° to the metal-plate edges, so that there are two equal field components, one parallel to the plates and one perpendicular to the plates. The component perpendicular to the plates passes through the structure relatively undisturbed, while the component parallel to the plates experiences a phase shift relative to free-space propagation. If the spacing and length of the plates are adjusted so that the field parallel to the plates advances $\lambda/4$ with respect to the field perpendicular to the plates, the two fields at the exit of the plates result in a circularly polarized wave. This structure is commonly referred to as a quarter-wave plate.

Any anisotropic dielectric can be used as a transmission-type polarizer, provided only that positioning and properties result in two equal-amplitude, quadrature-phased linearly polarized waves at the exit port.

There are several ways to produce such anisotropy: (1) parallel metal plates, 22,23



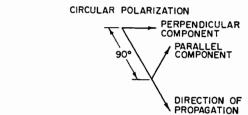


FIG. 23-31 Parallel-plate polarizer.

(2) parallel dielectric plates²⁴ (Fig. 23-32), and (3) a lattice structure composed of strips or rods.^{25,26} The first two methods are the heaviest, while the last two are the least frequency-sensitive. An unfortunate complication in design and adjustment of the simplest configurations is caused by imperfect impedance matching at the entrance and exit ports; in general, it is different for the two principal polarizations.

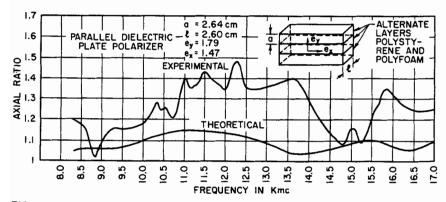


FIG. 23-32 Parallel-dielectric-plate polarizer.

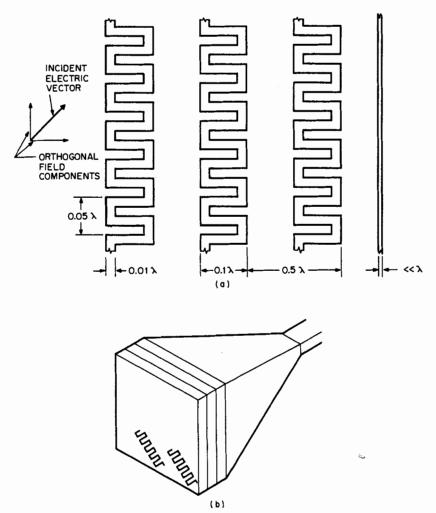


FIG. 23-33 Typical meander-line dimensions and radome applications. (a) Typical nominal dimensions of conductors on a layer (not to scale). (b) Four-layer polarizer-radome on a horn, illustrating orientation angle of typical conductors (not to scale).

Unwanted amplitude and phase effects result, including the result of a nonunity standing-wave ratio (SWR) inside the polarizer.

A variation of Method 3 above is the meander-line polarizer.^{27,28,29,30} Figure 23-33a shows a typical meandering configuration of a thin metal conductor supported on a dielectric sheet. In general, a greater number of layers of such sheets yields greater bandwidths, just as in multiple discontinuities used for broadband transmission-line transformers.

Kotlarenko²⁷ reports bandwidths of 1.7 to 1 for axial ratios of less than 3 dB for incidence angles ranging over 30° when using a six-layer design. A five-layer design

used at normal incidence yielded axial ratios under 3 dB for bandwidth exceeding an octave.

Epis³⁰ reports axial ratios under 3 dB over bandwidths of 1.75 to 1 by using a four-layer meander-line structure as a horn radome and a bandwidth exceeding 2.5 to 1 with axial ratios below 1.8 dB with six layers.

Reflection-type polarizers are essentially half-length transmission-type polarizers mounted on a conducting sheet. The simplest type of reflection-type polarizer is a series of closely spaced metal vanes, one-eighth wavelength high, on a conducting sheet. The incident energy is polarized at 45° to the vanes, so that the component parallel to the vanes is reflected by edges of the vanes and the component perpendicular to the vanes is reflected by the conducting sheet, thus delaying it 90° with respect to the parallel component and producing circular polarization. In general, any of the anisotropic propagating systems described above may be halved longitudinally and, with proper design, mounted above a conducting sheet to form a reflection polarizer.

Circular polarization may also be obtained via reflection from a conventional lossless dielectric when the dielectric constant e exceeds 5.8 and the incidence angle θ satisfies the condition $\sin^2 \theta = 2/(e+1)^{.31}$

23-6 RADAR PRECIPITATION-CLUTTER SUPPRESSION

Precipitation clutter is the name given to the radar echo from such targets as rain, snow, etc. It is not unusual for a radar to be rendered useless because precipitation clutter is sufficiently strong and extensive to hide the presence of a desired target (such as an aircraft). Because raindrops are substantially spherical (or at least much more so than an aircraft), they qualify as symmetrical reflectors. As mentioned in Sec. 23-1, a circularly polarized antenna is unable to see its own image in a symmetrical reflector. Therefore, if the radar antenna is circularly polarized, the echo from a symmetrical target such as a spherical raindrop will be circularly polarized with the wrong sense to be accepted by the antenna and will not be received. The echo from a composite target such as an aircraft will have scrambled polarization and will usually contain a polarization component to which the circularly polarized radar antenna can respond.

In other words, if the radar antenna is perfectly circularly polarized and the clutter is caused by spherical raindrops, the clutter cancellation will be perfect, enabling the presence of an otherwise-hidden composite target to be detected. When the radar antenna is elliptically polarized, the cancellation of an echo from symmetrical targets will not be complete; also, if the antenna is circularly polarized and the target is not symmetrical, cancellation will not be complete.

Cancellation Ratio

Cancellation ratio (CR) is defined at the ratio of radar power received from a symmetrical target when using a precipitation-clutter-suppression technique to the power received from the same target when not using the suppression technique. Cancellation ratio is not the same as cross-polarization ratio. Figure 23-34 shows cancellation ratio as a function of the polarization ellipticity of the antenna illuminating the symmetrical target.

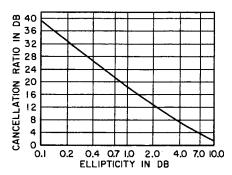


FIG. 23-34 Cancellation ratio as a function of polarization ellipticity.

Cancellation ratio, expressed in decibels, is related to the antenna polarization ellipticity by

$$CR_{dB} = 20 \log \left[\frac{1 - E^2}{1 + E^2} \right]$$
 (23-10)

Note that the polarization ellipticity E is the ratio of minor to major axis (field quantities) and that the bracketed fraction is a voltage ratio. It is often convenient to measure ellipticity in relative power quantities when using a rotating linearly polarized polarization probe. The relative powers corresponding to the major and minor polarization axes are P_{max} and P_{min} respectively. In this case

$$CR_{dB} = 20 \log \left[\frac{P_{max} - P_{min}}{P_{max} + P_{min}} \right]$$
 (23-11)

The fact that the bracketed fraction contains power quantities notwithstanding, the bracketed fraction is a voltage ratio.

Cancellation of Various Targets

Table 23-4 shows the extent of cancellation of various targets when the antenna is perfectly circularly polarized.

TABLE 23-4 Cancellation of Various Targets for Circular Polarization

Target	relative to return using linear polarization		
Sphere	Complete cancellation		
Disk facing radar	Complete cancellation		
Large sheet facing radar	Complete cancellation		
Wire grating facing radar (wires parallel to linear polarization for that case)	6-dB cancellation		
Double-bounce corner reflector	Zero cancellation		
Triple-bounce corner reflector	Complete cancellation		

Integrated Cancellation Ratio

A suitable figure of merit for a circularly polarized monostatic radar antenna is the integrated cancellation ratio (ICR). The ICR is defined as the ratio of radar power received by a radar utilizing the nominally circularly polarized antenna (common for transmission and reception) to the radar power received by the same radar utilizing a linearly polarized (but otherwise identical to the above) antenna (again, common for transmission and reception) when the antenna, in both instances, is completely surrounded by a large number of randomly distributed small symmetrical targets.

The ICR places proper emphasis on the necessity for having the radar beam circularly polarized all over and not just on its peak. The rain cloud causing the clutter does not exist only on the beam peak; therefore, the complete beam must be circularly polarized if the most effective cancellation is to be obtained.

When calculating the ICR from antenna radiation-pattern measurements, recall that the backscatter from individual raindrops will have random phase and that the receiving antenna will sum their energy rather than their fields. If one-way measurements are made with constant signal-generator output and invariant receiver gain and the combined polarization and antenna gain data recorded in relative power units as P_{max} and P_{min} , the ICR may be calculated from

$$ICR_{d\beta} = 10 \log_{10} \left\{ \frac{\sum_{\theta=0}^{360} \sum_{\phi=-90}^{90} (P_{\max,\theta,\phi} - P_{\min,\theta,\phi})^{2} |\sin \phi| \Delta \phi \Delta \theta}{\sum_{\theta=0}^{50} \sum_{\phi=-90}^{90} (P_{\max,\theta,\phi} + P_{\min,\theta,\phi})^{2} |\sin \phi| \Delta \phi \Delta \theta} \right\}$$
 (23-12)

 $P_{\max,\theta,\phi}$ denotes the relative power received in the rotating linearly polarized receiver as it lines up with the polarization-ellipse major axis, and $P_{\min,\theta,\phi}$ similarly for the minor axis. The subscripts θ,ϕ denote that there is a separate pair of such measurements for each $\Delta\theta\Delta\phi$ solid-angle sample over the full range of θ and ϕ . This process will automatically include the effect of antenna polarization and gain parameters.

Measurements should cover the full spherical-coordinate system surrounding the antenna, with sample points spaced closely enough so that data are truly representative of antenna performance. If different angular increments are used on different parts of the pattern, the correspondingly correct entries for $\Delta\theta$ and $\Delta\phi$ must be made in Eq. (23-12).

With careful design, ICRs of 30 or 35 dB can be obtained with large reflectortype antennas. For operation over a 5 or 10 percent band, because of the nonideal shape of raindrops an ICR of 20 dB is usually considered adequate. It is fairly safe to assume that the ICR is the limit of performance that can be expected with a given antenna; usually the actual cancellation of the precipitation clutter will be somewhat poorer because of the nonideal shape of the water particles.

The use of circular polarization results in some diminution in the radar power received from an aircraft target also. The diminution can vary over wide limits, depending on aircraft type, aspect ratio, wavelength, etc., and by its nature it can only be described statistically. However, diminution values well under 10 dB are often observed. Additionally, dense precipitation usually does not completely surround a radar at all ranges but tends to occur in patches. The net improvement in apparent signal-to-noise ratio (that is, the desired aircraft-target signal to precipitation-clutter noise) obtained by using circular polarization for precipitation-clutter suppression is worthwhile, with net improvement in the 10- to 20-dB area being readily achievable.

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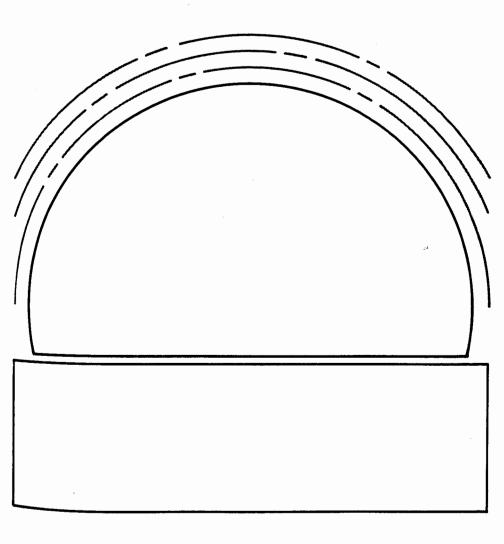
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Applications



Low-Frequency Antennas

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24-2	Basic Configurations 24-4
	Transmitting Antennas 24-4
	Receiving Antennas 24-5
24-3	Characteristics 24-5
24-4	Practical Design Considerations 24-8
	Vertical Radiators 24-8
	Top-Loaded Monopoles 24-8
	T and Inverted-L Antennas 24-8
	Triatic Antennas 24-11
	Trideco Antennas 24-12
	Valley-Span Antennas 24-12
	Multiantenna Arrays 24-13
	Antenna-Design Voltage
	24-13
	Antenna Insulation 24-14
	Conductors 24-16
	Downleads 24-18
	Structural Cables 24-19
	Special Problems of Insulated
	Towers 24-19

Grounded Tower Top-Loaded

Monopoles 24-20

24-1 General Application 24-4

Tuning-Inductor (Helix) Loss
24-23
Conductor Losses 24-24
Bridge Strand 24-25
Antenna Insulators 24-25
24-7 Design of Low-Frequency Ground
Systems 24-25
24-8 Scale-Model Measurements 24-28
Model Techniques 24-28
E- and H-Field Distribution
24-29
Potential-Gradient Evaluation
24-31
Electrolytic-Tank Model 24-31
Typical VLF-LF Antenna
Systems 24-33

24-5 Antenna and Tuning-Network
 Design Parameters 24-20
 Tuning Low-Frequency
 Antennas 24-21
 Variometers 24-22

 24-6 Radiation-System Loss Budget 24-23
 Ground Losses 24-23

The low-frequency (LF) portion of the radio-frequency (RF) spectrum is allocated to a number of special services to which the low attenuation rate and relatively stable propagation characteristics at low frequencies are of particular importance. Aeronautical and maritime navigational and communication services extend from approximately 10 to 500 kHz. Pulsed hyperbolic navigation systems operating near 100 kHz provide medium-range navigational aids. A phase-stable hyperbolic navigation system (Omega) transmitting within the 10.2- to 13.6-kHz region provides global navigation coverage. Other allocations include radio-location and maritime communications systems and LF fixed public broadcast. These services are of particular importance in the polar regions, which are subject to frequent and severe ionospheric disturbances.

Numerous strategic communication systems are currently operating within the region below 100 kHz, including a number of very-low-frequency (VLF) facilities capable of radiating hundreds of kilowatts within the 14.5- to 30-kHz band. These systems provide highly reliable service to airborne, surface, and subsurface transport.

VLF-LF transmitting systems involve large and expensive radiation systems and require extensive real estate and support facilities. Despite these drawbacks, activity within this portion of the spectrum is increasing, and many new systems have become operational within the past two decades.

24-2 BASIC CONFIGURATIONS

Transmitting Antennas

Early radiators for low-frequency transmitting application generally consisted of flattop T or inverted-L arrangements using multiwire panels supported between two masts. As the operating frequency of interest moved further into the VLF region and available transmitter power increased, additional top loading was required. Additional masts and support catenaries were provided to suspend larger top-hat panels. These triatic configurations were employed on the majority of VLF radiators, although a variation termed the umbrella type was also successful. The top hat of the umbrella antennas consisted of several multiple-wire panels supported by a central mast and a number of peripheral masts. The top-hat panels were suspended by insulators, and the support masts were grounded. In some cases, the center support mast was insulated from ground at its base to reduce its effect on antenna performance.

Many examples of these configurations are still in use, although the T and inverted-L variations are used primarily for relatively low-power applications within the upper portion of the low-frequency band.

Base-insulated, freestanding, or guyed towers have come into general use as radiators for public broadcast service in the medium-frequency (MF) band (535 to 1605 kHz). At these frequencies, tower heights of one-sixth to five-eighths wavelength are practicable. In some cases, various top-loading arrangements were added to the guyed towers in an attempt to improve their performance. These experiments were quite successful.¹

^{*10} to 300 kHz in this instance.

The most widely used variation of the base-insulated antennas for use at low frequencies is the top-loaded monopole. In this antenna, top loading is provided by additional "active" radial guys attached to the top of the tower and broken up by insulators at some point down from the top. In some cases, the top-loading radials also function as support guys.

Receiving Antennas

LF antennas designed for general receiving applications have very little requirement for efficiency. The receiving system is generally atmospheric-noise-limited, and air or ferrite loops, whips, or active probes are usually adequate. The design of low-frequency receiving antennas is not included within the scope of this chapter.

24-3 CHARACTERISTICS

Wavelengths within the low-frequency band range from 1 to 30 km. The physical size of low-frequency radiators is generally limited by structural or economic consider-

ations to a small fraction of a wavelength. These antennas therefore fall into the electrically small category and are subject to certain fundamental limitations, clearly defined by Wheeler.² These limitations become increasingly apparent at very low frequencies and are a primary consideration in the design of practical VLF-LF radiation systems.

Since the low-frequency antenna is very small in terms of wavelength, its

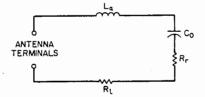


FIG. 24-1 Equivalent-circuit low-frequency antennas.

equivalent electrical circuit may be quite accurately represented by using lumped constants of inductance, capacitance, and resistance, as shown by Fig. 24-1,

where L_a = antenna inductance

 C_0 = antenna capacitance

 $R_r =$ antenna radiation resistance

 R_{ℓ} = radiation-system loss resistance

The antenna radiation resistance R_r , accounts for the radiation of useful power. It is a function of the effective height H_r of the antenna:

$$R_r = 160\pi^2 (H_e/\lambda)^2 \qquad \Omega$$

The antenna effective height is equivalent to the average height of the electrical charge on the antenna. The effective height of an electrically short, thin monopole of uniform cross section is approximately equal to one-half of its physical height. For other, more practical antenna systems, the value of effective height is not simply related to the physical dimensions of the antenna structure. It is difficult to compute accurately the electrical height of complex multiple-panel antenna systems requiring numerous support masts and guy systems.

Recently developed method-of-moment computer codes such as NEC,3 MIN-

INEC,⁴ and other programs greatly facilitate the design and performance analysis of VLF-LF antennas. These programs provide rapid evaluation of candidate antenna configurations and thereby reduce the need for numerous time-consuming scale-model measurements.

One computer-aided method for analyzing a VLF-LF antenna involves performing computations at two frequencies within the antenna's operating band (the highest and lowest frequencies may be used). Most programs will provide the current and impedance at the input frequencies. The effective height can be determined from the input resistances. The static capacitance and self-resonant frequency can be found by assuming the antenna to be represented by a series *RLC* circuit. Once the effective height, static capacitance, and resonant frequency values are known, other important characteristics can be calculated.

Many programs give the charge distribution on the antenna wires and the groundlevel magnetic field intensity from which gradients and ground losses may be estimated. NEC has provisions for computing the ground losses directly.

Static moment methods are useful for finding the antenna effective height, static capacitance, and potential distribution in the vicinity of an antenna. They are also effective in predicting the potential distribution among guy break-up insulators and the voltage distribution on low-frequency insulator strings.⁵

The designer should exercise a certain skepticism when evaluating the computer output because the results can be inaccurate or misleading. For example, NEC has been found to give slightly low static capacitance values⁶ and to generate fictitious circulating currents in electrically small loops. It is advisable to compare answers from several programs which use slightly different computational techniques in order to evaluate and develop confidence in the results.

VLF-LF transmitting antennas are physically large and very expensive. It is prudent to verify the computer results with scale-model measurements (Sec. 24-8) and, if possible, by scaling the known performance of a similar existing antenna before committing the design to construction.

Radiation-system losses are often expressed in terms of equivalent resistance. The total loss resistance R_{ℓ} is the sum of all individual circuit losses:

$$R_{\ell} = R_{g} + R_{t} + R_{c} + R_{d} + R_{\text{misc}}$$

where $R_g = \text{ground loss}$

 $R_t = \text{tuning loss}$

 $R_c = \text{conductor loss}$

 R_d = equivalent-series dielectric loss

 $R_{\text{misc}} = \text{loss in structural-support system}$

The principal loss in most systems occurs in the ground system and in the tuningnetwork inductors. Other losses occur in antenna conductors, insulators, and miscellaneous items of the structural-support system. In some locations, antenna icing, snow cover, and frozen soil may also contribute to antenna losses.

Antenna efficiency η is determined by the relative values of radiation resistance and antenna circuit loss. It is expressed by

$$\eta = R_r/(R_r + R_\ell)$$

To achieve a given efficiency, there is a maximum value of radiation-system loss resistance R_{ℓ} that can be allowed. The individual-circuit losses, particularly those con-

tributed by the tuning network and the ground system, can often be allocated during the detailed-design phase so as to minimize overall cost.

The lossless, or intrinsic, antenna bandwidth (to 3-dB points) is derived from the ratio f/Q, where Q is equal to the circuit reactance-to-resistance ratio. Therefore,

BW (intrinsic) =
$$1.10245 \times 10^{-7} C_0 H_e^2 f^4$$

where H_{ϵ} = effective height, m

 C_0 = static capacitance, μf

f =operating frequency, kHz

The intrinsic bandwidth is useful as a convenient means of antenna comparison.

The bandwidth of the radiation system (antenna, ground system, and tuning network) is inversely proportional to antenna efficiency:

BW (radiation system) = BW (intrinsic)/
$$\eta$$

This expression defines the bandwidth of the radiation system. It neglects, however, the reflected resistance of the transmitter output amplifier R, which can increase the overall bandwidth substantially, depending upon the particular amplifier design and coefficient of antenna coupling. In practice, the actual operating bandwidth of a typical transmitting system driven from a vacuum-tube amplifier is 40 to 80 percent greater than that of the radiation system alone. This may not be the case when the power is generated by a solid-state amplifier of high efficiency.

The operational bandwidth of the transmitting system driven by a high-efficiency solid-state transmitter can be extended if the proper matching techniques are used. This generally requires that an additional T network be used to present the transmitter with a parallel RLC load. The operational bandwidth will then be determined primarily by the capability of the transmitter to deliver power into a highly reactive load.

VLF antennas are normally operated at a frequency below self-resonance, and the principal tuning component is a high-Q inductor, usually referred to as the helix. It is possible to increase the operating bandwidth of the radiation system appreciably by dynamically varying the effective inductance of the helix in a manner to accommodate the bandwidth requirements of data transmission. This method of synchronous tuning is accomplished with a magnetic-core saturable reactor shunted across a portion of the helix.

The inductance of the reactor is a function of the relative permeability of its magnetic core. The relative permeability is changed by regulating the amplitude of a bias current flowing through a separate winding on the magnetic core. A control signal derived from the data stream is processed and used to regulate the bias current and to synchronize the antenna tuning in accordance with the instantaneous requirements of the modulation system.

The magnetic core material must have a smoothly curved saturation characteristic throughout the data-keying intervals to minimize production of RF harmonic frequencies. Several properly designed and controlled reactors are now in use which provide a nearly constant resistive transmitter loading at all times. Attempts to employ square loop material in a magnetic switching mode have not been successful because of the radiation of high-level harmonics during the keying transitions when the bias switch is neither fully opened nor fully closed.

24-4 PRACTICAL DESIGN CONSIDERATIONS

The first task in the design of a low-frequency radiation system is the selection of the basic antenna configuration most suitable for the application. There are, at present, few choices capable of effective performance within the 10- to 300-kHz frequency range. The most common types are identified and illustrated by Fig. 24-2. Except for the conventional base-insulated monopole, they are all structural variations of a short, top-loaded current element. The principal radiated field is vertically polarized and essentially omnidirectional. The ultimate performance of each configuration is closely related to its effective height and volume. Therefore, antenna selection depends primarily on the frequency, power-radiating capability, and bandwidth requirement of the proposed system.

Verticai Radiators

The conventional base-insulated tower of Fig. 24-2a may be adequate for low-power application within the upper portion of the low-frequency spectrum. The theoretical radiation resistance for simple vertical antennas of this type, if linear and sinusoidal current distribution is assumed and metal-structure towers, guy wires, etc., are ignored, is shown by Figs. 24-3 and 24-4.

The input reactance is represented by the equation

$$X_a = -Z_0 \cot (2\pi \ell/\lambda)$$
 Ω

which, for the case of a vertical cylindrical radiator of height h and radius ($a \ll h$), is usually evaluated by letting $\ell = h$ and

$$Z_0 = 60[\ln{(2h/a)} - 1]$$
 Ω

If the tower is very short, greater accuracy is obtained by using8

$$Z_0 = 60[\ln{(h/a)} - 1]$$
 Ω

Top-Loaded Monopoles

The base-insulated tower (Fig. 24-2b) in which top loading is provided by active radials or sections of the upper support guys is likely to be more cost-effective for low frequencies than the simple vertical radiator or the T or inverted-L types discussed later. A comprehensive parametric study of this antenna was completed by the Naval Electronics Laboratory in 1966. The study report contains numerous design curves that permit accurate evaluation of the performance of top-loaded monopoles of various configurations. The data were acquired by scale-model measurement. The top-loading radials were held taut with little sag. A reduction of approximately 4 percent should be applied to the effective height derived from the curves to account for the dead-load sag of a practical antenna.

T and inverted-L Antennas

These antennas (Figs. 24-2c and d) require two masts from which to support the insulated top section, but they do not normally require base or guy insulators. The prac-

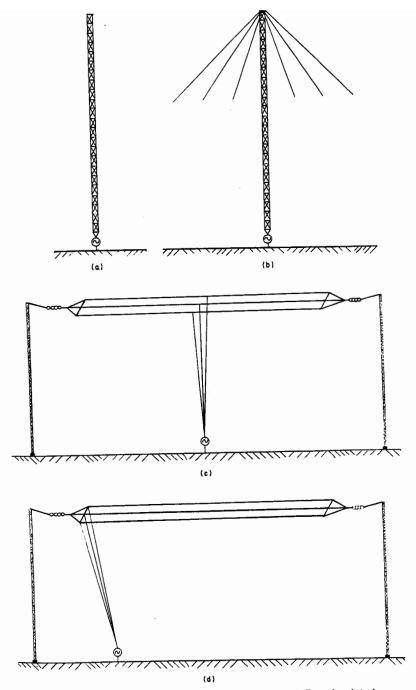


FIG. 24-2 Common types of low-frequency antennas. (a) Base-insulated monopole. (b) Top-loaded monopole. (c) T antenna. (d) Inverted-L antenna.

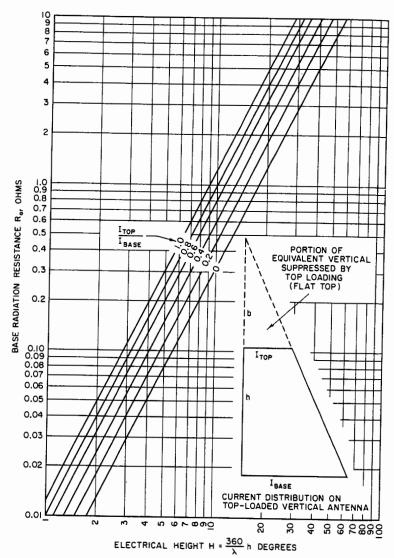


FIG. 24-3 Theoretical radiation resistance of vertical antenna for assumed linear current distribution. (After Ref. 7.)

ticable area of the top-loading top section is somewhat limited unless additional end or side masts are supplied.

This configuration and that of the triatic antenna described below may be useful if the available site area is restricted in one dimension.

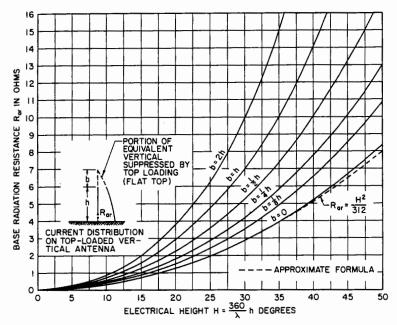


FIG. 24-4 Theoretical radiation resistance of vertical antenna for assumed sine-wave current distribution. (After Ref. 1.)

Triatic Antennas

The triatic-antenna configuration, illustrated by Fig. 24-5, consists of a relatively long antenna panel made up from parallel conductors. In addition to the masts at each end, the antenna panel is further supported at intermediate points from cross catenaries (triatics) and additional pairs of masts. The triatic antenna may be fed at any point along its length, but the design of the ground system is simplified if the downlead feed is near the midpoint.

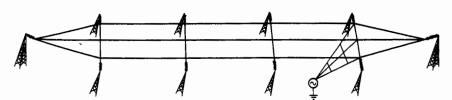


FIG. 24-5 Triatic-antenna configuration.

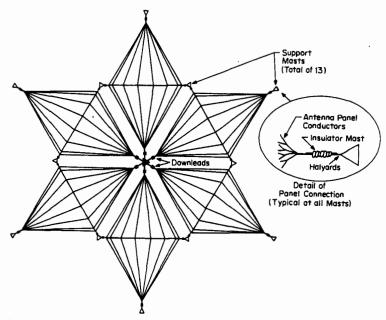


FIG. 24-6 Trideco-antenna configuration (plan view). Note: individual downleads are provided at each panel inner apex.

Trideco Antennas

The structural arrangement of a trideco antenna consists of one or more rhombic or triangular-shaped multiple-wire panels suspended from three or more masts. The individual downlead of each panel terminates at a common feed point (Fig. 24-6). This configuration has proved to be very effective for high-power applications, since it affords greater flexibility in the selection of both electrical-design and structural-design parameters. It is possible to design the top-hat panels so they can be individually lowered for maintenance without appreciably reducing antenna performance. This capability greatly simplifies antenna maintenance, thereby increasing system reliability and availability.

Valley-Span Antennas

These antennas have limited application. They are essentially T or inverted-L spans supported from natural geological formations such as those provided by a deep valley or mountainous ridges. The spans are interconnected and fed through a downlead extending to the valley floor. Typical examples of this type of antenna are in operation in Norway, Hawaii, and Washington State.

There are very few locations in the world where valley-spanning antennas can be effectively utilized. While the initial cost of such an antenna may be considerably less than that of a mast-supported system, the cost of ground-system maintenance and control of vegetation and erosion will generally be much greater.

The efficiency of existing valley-span antennas ranges from approximately 7 to 20 percent. Several factors contribute to their low efficiency. The topography of the typical valley site tends to reduce the effective antenna height and frequently limits the practicable area of the ground system. Soil cover may also be shallow and of poor effective conductivity.

Multiantenna Arrays

Two or more closely grouped, individually fed LF-VLF antennas can be integrated into a composite transmitting system to achieve a measure of structural survivability and operational redundancy. At least one such facility, consisting of eight top-loaded monopoles fed by separate transmitters, has been in operation for several years in Europe. Assuming the individual antennas to be identical and correctly tuned, the approximate first-order characteristics of the multiantenna array (A) can be expressed as

$$A_{He} = H_e$$

$$A_{C0} = nC_0k$$

$$A_{Fr} = F_r$$

$$A_{IBW} = nIBW$$

$$A_{Pr} = n^2P_r$$

where n = number of individual antennas making up the array

 H_e = effective height of the single isolated antenna

 C_0 = static capacity of the single isolated antenna

k =constant to correct for field fringing and other minor variables

 F_r = self-resonant frequency of a single isolated antenna

IBW = intrinsic bandwidth of the single isolated antenna

 P_r = voltage-limited power-radiation capability of the single isolated antenna

Two major operational and design problems associated with the multiantenna concept are the critical tuning requirements resulting from the interantenna mutual coupling and the difficulty of providing cost-effective control of the ground losses resulting from the complex *H*-field distribution of the array.

Antenna-Design Voltage

The power-radiating capability of low-frequency antennas is proportional to the square of the antenna voltage ($P_{\rm rad} \propto V^2$) and in most instances is limited by the allowable insulator voltage and the effective area of the antenna conductors. It appears that about 250 kV rms (rms values are commonly applied in VLF-LF antenna design) is the maximum operating voltage to which low-frequency antennas can presently be designed and put into service. This voltage level is not appreciably higher than that developed on VLF antennas 50 years earlier.

The voltage limitation is principally due to the physical limitation of available conductors and insulators. The potential surface gradient of the conductor can be controlled by providing adequate conductor surface. Insulator working voltages can be extended by the use of multiple-insulator assemblies. However, the structural design

loads resulting from the increased weight and wind load of the insulators and antenna panels become increasingly difficult to accommodate. The problem is particularly severe in the case of insulated and top-loaded monopoles. The top-loading radials are generally insulated near the midpoint of their spans, at which point the insulator weight results in greatly increased sag or cable tension. The same is true of support-guy insulators, which must be capable of withstanding high tensile loads. The resulting insulator weight, distributed at several points along the guy, increases guy sag and reduces guy efficiency. The cumulative effect of insulator weight, increased cable diameters, wind load, and heavier towers is regenerative and eventually reaches a practical or economic limitation.

Triatic, trideco, and similar top-loaded antennas are somewhat less vulnerable to these problems because of their structural arrangement. The mast-support guys do not require insulators. The top-hat panel insulators can be attached relatively close to the supporting masts, where their weight is more easily supported.

Antenna Insulation

Virtually all insulators used on high-power LF-VLF antennas employ porcelain as the primary dielectric material. The dependability and long service life of porcelain as an insulating material are well established. Fiberglass-reinforced plastic insulators have been under development for several years and have shown some promise in experimental service. More recently, oil-filled tubular porcelain insulators reinforced internally with a fiberglass band have performed well as the primary insulators on top-loaded monopole antennas. They offer a considerable saving in both weight and cost.

The selection of the type of insulators to be used on the antenna depends to a large extent on structural considerations and the location of the insulator in the system. Three basic types are available: the strain, or "stick," type, in which the porcelain body is subjected to tensile loads; the fail-safe, or compression, type, in which the porcelain is supported in a frame or yoke arrangement that places the porcelain under compression; and a third type which is a variation of the "stick" type in which the working loads are taken by a high-strength fiberglass band located within the oil-filled interior of the tubular porcelain body. These insulators are illustrated in Fig. 24-7.

The voltage-handling capability of the insulators must be adequate to ensure operating reliability at design power under extreme environmental conditions. The published 60-Hz voltage rating of the insulators must be derated to allow for rain and condensation, surface contamination, overvoltage transients from atmospheric disturbances, and deterioration from service aging. A derating factor of 2:1 has been commonly applied; that is, a wet flashover rating twice the normal operating voltage is required. This factor has not always been adequate, primarily because of the difficulty of testing the insulator at its projected operating frequency rather than at 60 Hz and in an environment similar to that to be encountered in service. If the normal antenna working voltage exceeds about 150 kV rms, insulator assemblies should be tested at radio frequency to confirm their continuous wet-withstand capability at a voltage at least 50 percent above the working voltage. An insulator test facility capable of subjecting insulators to test voltages up to approximately 350 kV at VLF and LF frequencies is located at Forrestport, New York. 10

Individual compression-type insulators are not available for operating voltages exceeding about 50 kV. Therefore, these insulators must often be connected in series to obtain the required voltage-withstand capability. Insulation "efficiency" decreases rapidly as insulators are added in series. Voltage-grading rings or cages are useful in

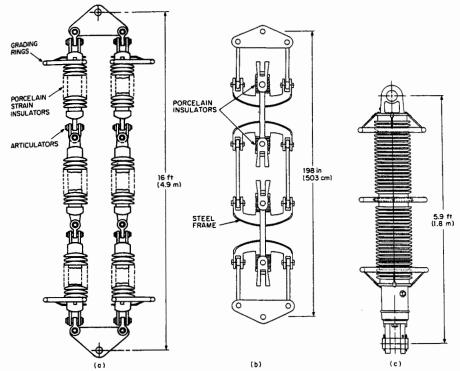


FIG. 24-7 Three types of insulators suitable for use in low-frequency antennas. (a) Strain type. (b) Fail-safe type. (c) Fiberglass-core type.

this respect since they improve voltage distribution across the insulator string. These devices increase the insulator weight and wind-load area and must be carefully designed to avoid fatigue vibration and early structural failure.

Structural design codes generally require structural guys to employ compression fail-safe insulators, although the fiberglass-reinforced, oil-filled porcelain insulators may, in some cases, be acceptable on dual-guyed towers. This requirement may also apply to panel-support insulators, in which insulator failure may jeopardize the entire antenna structure. The active nonstructural radials of top-loaded monopoles may employ strain insulators provided the tower and primary antenna guy system are properly designed.

Individual strain insulators are capable of withstanding voltages up to several hundred kilovolts. However, the tensile strength of porcelain is relatively low, and individual insulators may have to be operated in parallel combinations of two or more series units in order to develop the necessary voltage and strength characteristics. The resulting insulator and hardware weight may be difficult to accommodate.

It may appear that the selection of insulators at this point in the design is premature. However, insulator selection has a considerable impact on the final antenna configuration and performance, since it affects the dead-load shape of the antenna spans, number and placement of guys, wind-load area, and connecting hardware. The usual practice is to conduct the initial design trades on typical insulator components, using the manufacturer's estimated weights. Later, during the detailed-design phase, as various factors are optimized, specific insulators and actual weights are used.

Conductors

An equally critical selection is the choice of conductors and structural cables to be used in constructing the antenna. Conductors are required for antenna panels or spans, current jumpers, and structural cables for halyards and guys. Low-frequency-antenna panels involve long spans. The conductors must have low RF resistance, adequate tensile strength, and minimum weight. The conductor diameter and total conductor area must be sufficient to limit the surface potential to preclude corona.

The conductors are large and consist of multilayer cables stranded from aluminum or aluminum-covered steel wires. Figure 24-8 illustrates the construction of three types of conductors currently manufactured for electric power transmission and distribution systems. The ready availability of these conductors is an important consideration to the designer.

The conductor which has generally proved to be most suitable for antenna spans and panels is stranded from aluminum-clad, steel-core wires and is designated as AW (Fig. 24-8a). This conductor is listed by the manufacturer in diameters up to approximately 1½ in. It may be procured in diameters up to 1.46 in when arrangements are made for special stranding.

The size of the individual wires of the strand ranges from AWG No. 10 to AWG No. 4, depending upon the overall conductor diameter. The thickness of the outer layer of aluminum is 10 percent of the wire radius. This thickness may be less than the skin depth at the operating frequency, and RF losses are thereby increased. In applications such as downleads which are carrying a large current, it may be necessary to produce aluminum-clad wire cable with the outer strands of solid-aluminum wire (Fig. 24-8b). This type of conductor is designated AWAC, i.e., aluminum wire, aluminum-clad steel-wire core.

AWAC is not entirely satisfactory from a structural standpoint for applications in which the tensile load is high because of differences in the elasticity of the aluminum and aluminum-clad steel wires. This often results in the "basketing" of the outer wires when they are being handled or when pretension loads are relaxed.

A third type of composite conductor (Fig. 24-8c) is also in general use in power-transmission service. This conductor is made up in various combinations of aluminum and aluminized or galvanized steel wires and is designated ACSR, i.e., aluminum conductor, steel-reinforced. ACSR having steel wires exposed to the surface of the cable is not a suitable conductor for low-frequency conductors because of its relatively poor RF conductivity and the tendency of the aluminum wires to basket when tensile loads are released.

Conductors stranded of solid-aluminum wires are available and should be considered whenever high strength is not a factor. They are useful for current jumpers and for connections at feed-line terminal points.

When extreme flexibility and fatigue resistance are required in a jumper, stainless-steel wire rope should be considered. It should be fabricated from a nonmagnetic stainless alloy (Series 300), which will provide maximum skin depth and effective conductor area. Current jumpers are generally short, and their loss is usually insignificant.

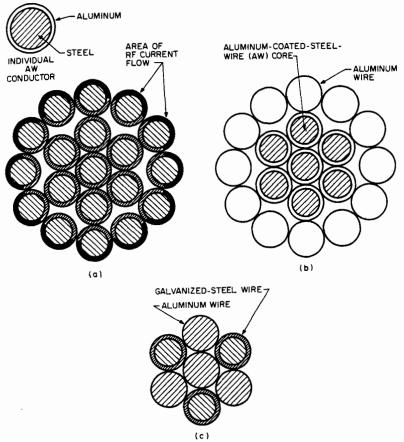


FIG. 24-8 Cross section of composite-cable conductors. (a) Concentric-lay stranded aluminum-clad steel conductor. (b) Aluminum-wire, aluminum-clad (AWAC) wire core. (c) Aluminum-conductor, steel-reinforced (ACSR).

Other specialized conductor materials have been used in high-power low-frequency antennas. Calsum bronze cables are in use at the U.S. Navy VLF station at Cutler, Maine, and hollow-core copper cable at the original VLF station at Annapolis. Future use of these specialized conductors is extremely unlikely, considering the present availability of aluminum-covered steel and the cost of procuring relatively short production runs of special cables.

Selection of Conductor Diameter The diameter of the conductors making up the antenna spans, panels, or downleads must be adequate to avoid corona as well as to develop the necessary tensile strength. The minimum conductor diameter required at the antenna design voltage should be established during the preliminary design since conductor weight and wind load are important factors in the structural design.

Generally, a conductor size adequate to handle the working loads typical of very long spans will be of sufficient diameter to limit the surface potential gradient to a safe value, provided the antenna panels are made up of an adequate number of conductors.

Experience has confirmed that limiting the surface gradient of the antenna conductors to about 0.7 kV/mm will ensure corona-free operation under normal and extreme environmental conditions.

The usual expression for computing the surface gradient of an isolated conductor above ground is not applicable to a multiconductor transmitting-antenna panel. A method developed by Wheeler¹¹ (also discussed in Chap. 6) provides a solution based on the average current flowing from the wires toward the ground per unit of wire surface area. By using this method, the average voltage gradient on the conductor surface is found by

$$E_a [kV/mm] = \frac{3\lambda^2}{2\pi H_e A_a} \sqrt{10P [watts]} \times 10^{-6}$$

where E_a is the voltage gradient, kV/mm, and A_a is the total wire surface area, m².

When the antenna span or panels are made up of a number of conductors, the gradient at the outer wires is higher than that at the inner wires. The surface gradient of the wires of a multiwire panel can be partially equalized by varying their spacing with respect to each other, the more closely spaced wires being placed at the panel sides. The gradient on the outer wires can also be equalized by increasing their relative diameter.

The largest Alumoweld stranded conductor currently available from suppliers has a nominal diameter of 1.46 in. This conductor is comprised of 61 No. 6 wires. In some applications this diameter may not be adequate to limit the surface gradient of top-loading radials to an acceptable value. A practical solution is to increase the effective diameter of the outer portion of the radials by caging two or three conductors. The wire-to-wire spacing should be optimized to minimize the additional structural loading on the tower. The surface gradient of the conductors of a two-wire cage decreases rapidly as the wire-to-wire spacing is increased to several wire diameters and then more slowly as the spacing approaches about 10 wire diameters. The chosen spacing should be no greater than necessary to ensure a safe gradient so as to minimize spreader-hardware weight and projected wind area.

Downleads

Base-insulated monopoles are generally fed at the base, and the antenna current is carried by the structural members of the tower. Virtually all low-frequency-antenna towers are fabricated of steel. The steel is usually galvanized except when a low-alloy steel is used. In any case, the thickness of the zinc is much less than a skin depth, and supplementary current buses must be provided up the tower to reduce losses.

It is recommended that triatics and similar wire-panel antennas be fed by one or more downleads terminating on a common feed point. A number of early low-frequency antennas used a system of multiple tuning, i.e., several downleads connected at various points to the antenna panel and separately tuned. Only one of the downleads was fed; the others terminated to the ground system. Multiple downleads substantially

increase antenna cost and complicate tuning procedures. Their use has not proved to be effective in reducing antenna-system

losses.

It is advantageous to use a multiwire cage (Fig. 24-9) for the antenna downlead. The total antenna current flows in the downlead, and it is more practical to control the downlead loss and potential gradient by using a multiwire cage than to use a single conductor of large diameter.

In addition, the effective diameter of a multiwire cage is much greater than that of its individual conductors. As a result, the downlead inductance is

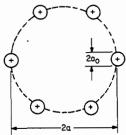


Fig. 24-9 Multiwire cage for antenna downlead.

reduced, thereby increasing the self-resonant frequency of the antenna. The large effective diameter of the multiwire cage also reduces the potential gradient at the surface of the conductors. This is particularly important along the lower portion of the downlead where it approaches the earth and grounded structures.

The effective radius of a multiwire cage is given by 13

$$a_{\rm eff} = a(na_0/a)^{1/n}$$

Where a_{eff} = effective radius of cage, m

n = number of cage wires

a = cage radius, m

 a_0 = individual wire radius, m

and, for practical purposes, the average potential gradient E_a on the individual cage wires is found by

$$E_a [V/m] = V/na_0 \ln (2h/a_{eff})$$

where h = elevation of cage above ground, m

V = voltage on cage

Structural Cables

Non-current-carrying cables used for guys, halyards, and support cables are usually fabricated from bridge strand, which is available up to approximately 4 in in diameter. The strand is made up of a number of counterwound layers of galvanized high-strength steel wires. When flexibility is important, as in passing over winches and shives, wire rope fabricated from bundles of fine steel-wire strands over a hemp core is preferable to bridge strand.

Special Problems of Insulated Towers

Antennas requiring base-insulated towers can be advantageously employed in lowand medium-power applications, particularly within the upper portion of the low-frequency band and almost exclusively within the medium-frequency broadcast band. They may not be cost-effective, however, in applications in which the antenna operating voltage is high. In addition to expensive guy and base insulators, such towers require a high-voltage obstruction-lighting isolation transformer with a voltage-with-stand rating equal to that of the base insulator, a special provision for elevator power if an elevator is desired, and some provision for boarding the tower above the level of the base insulator.

In some locations, the heavy rainfall accompanying typhoons or hurricanes may flood the porcelains of base insulators and isolation transformers, causing flashover and operational interruptions. Isolated sections of tower guys may accumulate a high-potential static charge, triggering flashover of all insulators of the guy. These problems can be overcome, but the cost may not compare favorably with an alternative configuration using uninsulated masts and guys.

Grounded Tower Top-Loaded Monopoles

Three top-loaded monopoles having grounded masts and uninsulated support guys are in service at three stations of the Omega Navigation System. These antennas operate between 10.2 and 13.6 kHz at voltage levels in excess of 200 kV. The active radials are jumpered together and insulated at their attachment to the top of the mast. One of the radials is extended to a pull-off tower and entrance bushing and serves as the feed line. The remaining radials are insulated at their outer ends in the normal manner. The uninsulated support mast and guy system reduces the antenna effective height somewhat. This can be restored by a modest increase in antenna height.

This antenna configuration may be employed in applications in which the environmental conditions are unusually severe and structurally adequate guy insulators are not available. The cost savings in base and guy insulators, attachment hardware, and obstruction-lighting isolation transformer may defray the cost of additional mast height.

24-5 ANTENNA AND TUNING-NETWORK DESIGN PARAMETERS

The potential performance of a low-frequency antenna can be predicted from three basic parameters: effective height, antenna capacity, and self-resonant frequency. These values can be computed from the principal dimensions of the proposed antenna configuration or acquired by direct measurement on a scaled antenna model (Sec. 24-8). If the proposed antenna is similar to an existing system the properties of which are known, the design parameters may be appropriately scaled.

The principal performance characteristics of the antenna are related as follows. The power-radiating capability of the antenna for a chosen level of top-hat voltage V_i is equal to

$$P_{\rm rad} = 6.95 \times 10^{-10} V_{\rm c} [\rm kV \ rms] C_0 [\mu f] H_{\rm c}^2 f^4 [\rm kHz]$$
 kW

The voltage at the antenna base or feed point V_b establishes the working-voltage requirement for the base insulator, downlead terminal, and entrance bushing:

$$V_b [kV] = V_t [kV] \{1 - (f[kHz]/f, [kHz])^2\}$$

where f =operating frequency

 f_t = antenna self-resonant frequency

The antenna-base current required to radiate a specified power is given by $I_b = (P/R_r)^{1/2}$, where P is expressed in watts, the antenna radiation resistance R_r in ohms, and the antenna-base current I_b in amperes. The antenna-base current largely determines the current rating of the helix conductor.

The power input to the radiation system required to radiate a given power is

$$P[\text{watts}] = I_{\text{base}}^2(R_r + R_\ell)$$

where $R_r =$ antenna radiation resistance

 R_{l} = antenna loss resistance, Ω

The antenna inductance L_a is expressed by

$$L_a [\mu H] = 1/4\pi^2 f_r^2 [kHz] C_0 [\mu f]$$

Since the total circuit inductance required to resonate the antenna at a given operating frequency f (below self-resonance) is $1/4\pi^2 f$ [Hz]² C_0 [μf], the effective tuning inductance required at the antenna feed point is

$$L_{\text{tune}} [\mu H] = 1/4\pi^2 f^2 [\text{Hz}] C_0 [\mu f] - L_a [\mu H]$$

If the antenna is to be designed for operation over a band of frequencies, the operating conditions at the lowest frequency will be the most severe and will establish the principal design requirements of the system. As the operating frequency is increased, the bandwidth will be improved and the current and voltage levels will be appreciably reduced.

Tuning Low-Frequency Antennas

Low-frequency antennas are generally designed to be operated well below their self-resonant frequency. The antenna impedance will then be capacitive, and the antenna may be tuned with a series inductor. A schematic drawing illustrating the arrangement of a typical tuning and matching network is given in Fig. 24-10. At frequencies above self-resonance the antenna impedance is inductive, and a series capacitor must be used. Capacitors of the size and rating required for series-tuning, high-power VLF antennas are not readily available. In addition, an inductor is inherently more reliable than a capacitor and less subject to failure from lightning or overvoltage transients. Therefore, in order to avoid the necessity of matching into an inductive reactance, the self-resonant frequency should be designed to be at least 10 percent and preferably 15 percent above the highest anticipated operating frequency. This objective may be difficult or impossible to achieve with very large antennas. In such cases, the downlead inductance should be minimized or alternative feed arrangements considered.

The helix is usually designed as a single-layer inductor. In this form, it is less difficult to install and to provide with means for taps. The voltage difference across such an inductor is quite evenly distributed. As a result, the turn-to-turn voltage is minimized and can be accommodated by means of normal turn-to-turn spacing (generally about two wire diameters). The helix is most conveniently fed at the bottom. Maximum voltage exists at the top, where it may be connected to a high-voltage exit bushing extending to the downlead.

Variometers

Low-frequency antenna-tuning circuits generally require one or more variable inductors termed variometers. Variometers consist of two concentric coaxial (partially spherical) coils connected in series. The smaller coil can be rotated about the common axis by means of a motor-driven shaft. The coefficient of coupling of the inner and outer coils is relatively high. Rotation of the inner coil through one-half revolution results in smooth variation of the effective inductance. A total inductance variation of about 8:1 can be achieved with large transmitting units.

Variometer performance can be estimated by computing the inductance, mutual inductance, and coefficient of coupling between the concentric inductors. Judgment is required in the selection of the effective radius and length of the coils, since the physical requirements of the variometer frame require the inductors to be incomplete spherical coils with few turns of varying pitch.

Inductance of helix (solenoid):

$$L = \pi \mu_0 a^2 n^2 / b + 0.9 \ a$$

Mutual inductance of two concentric coaxial helices if inner coil is slightly smaller than outer coil:

$$L_{12} = L_2(a_1^2n_1)/(a_2^2n_2)$$

Coefficient of coupling of two concentric spherical coils:

$$K_{12} = (a_1/a_2)^{3/2}$$

where a = coil radius, m

 $b = n \times \text{pitch of winding, axial length, m}$

n = number of turns

 $\mu_0 = 1.257 \times 10^{-6} = \text{magnetivity of free space}$, H/m

subscript 1 = inner coil subscript 2 = outer coil subscript 12 = mutual

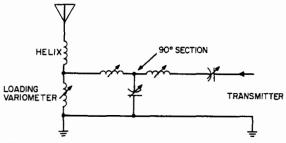


FIG. 24-10 Typical tuning circuit for use with a low-frequency antenna operating below self-resonant frequency.

24-6 RADIATION-SYSTEM LOSS BUDGET

The radiation resistance of a low-frequency radiator is relatively small; consequently, its efficiency is critically dependent upon antenna-system losses. It is useful to prepare a loss budget in which identifiable loss items are individually evaluated. The major losses are likely to occur in the ground system and tuning network. Among other losses are those in the antenna conductors and support guys and in the insulator dielectric. The sum total of all radiation-system losses must not exceed a maximum allowable value if the antenna efficiency goal is to be achieved.

Ground Losses

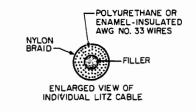
It is possible to some extent to allocate certain losses so as to minimize the overall cost of the radiation system. For example, if the site topography or soil geology makes installation of the ground system difficult and unusually expensive, it may be more economical to accept somewhat higher ground losses, provided the loss in the tuning network can be reduced accordingly. Calculation of ground loss is discussed in Sec. 24-7.

Tuning-Inductor (Helix) Loss

The principal loss in the tuning network will usually be in the main tuning inductor used to tune the antenna. It is possible to design a VLF inductor having a computed Q of several thousand, but the necessity of providing for taps and connectors makes it very difficult to achieve a practical value exceeding approximately 2500. Values of 1500 to 2000 are typical. The helix Q is primarily related to its overall size. Other factors include the conductor area and material, the inductor form factor, and the volume and material of the shield.

The most effective helix conductor is a composite cable stranded of Litz wire as illustrated in Fig. 24-11. The Litz-wire strands are made up of numerous insulated copper wires approximately a skin depth in diameter. The Litz Strands are bundled together into larger groups and jacketed over a central jute core. The wire and wire bundles are transposed within the jacket so as to distribute the current density uniformly among the individual wires

The number of individually insu-



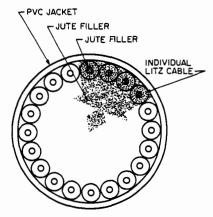


FIG. 24-11 Cross section of a large Litz conductor used in low-frequency inductor.

lated wires making up the cable is determined from the maximum value of the antenna current on the basis of 1000 circular mils per ampere. If the current requirement exceeds about 1500 A, the resulting cable diameter (typically 3½ in) becomes difficult to handle. In this case, two or three parallel cables of smaller diameter may be used. An excellent summary of the design of Litz inductors is given by Watt in Chap. 2.5 of VLF Radio Engineering. 14

Copper tubing of appropriate size may also be used for low-frequency inductors in applications in which the additional losses may be tolerated and the power level permits the use of tubing of a reasonable diameter (6 in or less). Large-tubing inductors must be assembled from sections bolted or brazed together during installation.

The helix-room shield may be fabricated from brazed or welded copper or aluminum sheets having a thickness of two to three skin depths at the lowest operating frequency. A square or rectangular helix room is usually more practical than one of cylindrical form.

The additional losses contributed by the shield will be small if the size of the helix building provides an inductor-to-shield separation of approximately one coil diameter. 15 The separation at the floor and ceiling may be somewhat less. It is advisable to limit the surface gradient of the Litz cable to a maximum of 0.5 kV/mm (rms).

Conductor Losses

Antenna current flows in downlead conductors, top-hat panels, or top-loading radials and, to a lesser extent, in guy cables and tower members. To compute the losses in these items, it is necessary to evaluate the RF resistance of each at the frequency of operation.

Concentric Lay-Stranded Aluminum-Clad Steel Conductors (AW) This type of conductor is suitable for antenna panels and long spans. The individual wire size of the conductor depends upon the diameter of the finished cable and ranges from AWG No. 10 through AWG No. 4. The thickness of the aluminum cladding over the steel core is 10 percent of the finished wire radius, or approximately 0.25 mm for the largest-diameter wire (AWG No. 4). For frequencies below about 100 kHz, this thickness is less than a skin depth. The current penetration into the steel-wire core will be negligible owing to its relative permeability. Therefore, essentially all the current is forced to flow in the aluminum surface. This is illustrated by Fig. 24-8. Since the number and size of the individual wires are selected so as to provide a tightly grouped outer layer, the current will flow only in the outer half surface of each exposed wire.

For example, a nominal 1-in cable may consist of four layers of AWG No. 7 wire with 18 wires in the outer layer. The total effective cross-sectional area of the current-carrying aluminum is

$$A = (r_1 + r_2)(r_1 - r_2)\pi N \times 10^{-6}/2$$

where r_1 = radius of individual wire, mm

 $r_2 = 0.9 r_1$ (Thickness of aluminum on steel wire is 10 percent of wire radius.)

N = number of wires in outer wrap (lay), or 18.04×10^{-6} m² in this example. The resistance per meter length is

$$R_{rf} = 1/\sigma A$$

where
$$A = \text{area, m}^2$$

 $\sigma = \text{conductivity of aluminum } (3.5 \times 10^7 \text{ S/m})$

Aluminum Wire, Aluminum-Clad Wire Core (AWAC) In some applications, downlead cages for example, the loss in aluminum-clad steel wires may exceed the allowable loss budget. It is possible to procure cable similar to AW in which the outer lay consists of solid-aluminum wires. RF loss in this cable will be equivalent to that of all-aluminum strand.

 $R_{rf} = 1.6 \text{ m}\Omega/\text{m}$ at 15 kHz

Since the wire diameter will be very much greater than a skin depth, the resistance can be expressed as

$$R_{ac} = 1/\sigma\pi \ d\delta$$

Where $\sigma = \text{conductivity}, S/m$

d =wire diameter, m

 $\delta = \text{skin depth}$, m, at frequency of interest: $\delta = 1/2\pi (f\sigma\mu_r \times 10^{-7})^{1/2}$

 μ_r = relative permeability of conductor material

Bridge Strand

Guy cables are generally made up from bridge strand. The individual steel wires of bridge strand are protected from corrosion by a thin layer of zinc. The zinc is too thin to be a factor in lowering the resistance of the cable. If a value of 200 for relative permeability and $5 \times 10^6 \, \text{S/m}$ for conductivity of the steel is assumed, the skin depth for bridge strand at 15 kHz is approximately equal to 0.13 mm. The RF resistance calculation is straightforward, taking into account skin depth and exposed-surface area.

Antenna insulators

Low-frequency insulators employ porcelain dielectric, and the loss factor at operating frequency is relatively low. The insulator loss for the antenna system is estimated from the applied working voltage, dielectric power factor, and number of insulators in the system. The dielectric loss of the insulator can also be estimated by determining the porcelain heat rise during acceptance testing.

24-7 DESIGN OF LOW-FREQUENCY GROUND SYSTEMS

The radiation resistance of electrically small antennas is very small, and if an antenna is to have a useful efficiency, system losses must be carefully controlled. The principal circuit losses occur in the tuning network and the ground system. Tuning losses can be minimized by using high-Q components. Ground losses within the site area can be reduced by providing a low-reactance, low-resistance ground system. This may consist

of a radial network of wires buried a half meter or so below the surface and extending in all directions to some distance beyond the antenna.

Ground losses result from ground-return currents flowing through the lossy soil and from E-field displacement current in the soil or vegetation above the level of the ground wires. Generally, the E-field losses are not significant and may be neglected except in locations where the soil may freeze to a substantial depth or acquire a deep snow cover. E-field loss can be evaluated by methods outlined by Watt (Secs. 2.4.37 and 2.4.38).¹⁴

The radiation-system ground loss is derived by separately computing the *E*-field and *H*-field losses of small sectors within the radian circle (a circle having a radius of $\lambda/2\pi$) and summing them to get the total loss. The loss within the radian distance is attributed to ground-system loss; that beyond the radian circle is considered to be propagation loss. Since it is rarely practical to extend the ground system to the radian distance, ground losses can be further separated into *wired-area* and *unwired-area* losses.

Early VLF-LF ground systems varied widely in concept, depending upon the antenna configuration and whether single or multiple tuning was employed. In most cases, the ground wires were buried, although several designs returned earth currents from dispersed ground terminals on overhead conductor systems. Present practice is to design the ground system around a single-point feed by using an essentially radial configuration.

There are many ways in which ground-loss computations can be carried out. Since ground-conductivity values may vary considerably over the radian-circle area, a method that allows individual computation of relatively small areas is desirable. The appropriate conductivity values can then be applied. For example, the radian circle can be divided into 36 ten-degree sectors centered at the feed point, each sector being further divided into 50 or more segments. The loss is computed for each sector; when summed, these losses give the total loss.

Once the magnitude and orientation of the normalized * H field within the antenna region have been determined, the H-field losses are calculated in the following manner. The longitudinal loss within the wired area is found from the product of the square of the normalized longitudinal component of the H field, the resistance of a 1-m^2 area, and the area. The longitudinal loss is computed for each segment of the sector with the exception of the last few segments, which are treated as termination losses. The total loss for each sector is the sum of all its segments.

The unit resistance is the resistance component of the parallel impedance of the ground wires and the earth to a current flowing parallel to the ground wires. Losses due to the wire resistance (usually small) are covered by this method. The earth impedance, the wire impedance, and the parallel impedance are computed from Watt.¹⁴

The transverse loss in the wired portion is equal to the product of the square of the normalized transverse component of the H field, the earth resistance of 1 m^2 , and the area (Watt, ¹⁴ Sec. 2.4.10). The transverse loss for a sector is the sum of the segment losses for all wired segments.

The termination loss occurs in the last few segments of the wired area, where the transition from the wired to the unwired area occurs. The number of segments is cho-

^{*}The H field is generally normalized for an antenna current of 1 A so as to make the loss resistance equal to the power loss in watts.

sen to represent the end portion of the radial wires with a length equal to the skin depth of the earth. The resistance of a single wire of this length to ground is computed from Sunde 16 (Sec. 3.36). A computed or empirically derived mutual-resistance factor is employed to obtain the effective resistance of a single wire in proximity to adjacent wires. The resistance of the terminating ground rods, if used, is then computed from Sunde (Sec. 3.30). The termination resistance for the wire-ground-rod combination is then computed, using an estimated factor for the mutual resistance, and paralleling the two components. This figure is adjusted to a resistance per square meter and multiplied by the square of the longitudinal component of the normalized H field and by the area to provide the termination loss.

The *unwired losses* apply to the unwired area extending from the ground-system boundary to the radian circle. Losses are computed for each segment as the product of the *H* field squared, the earth resistance (Watt, ¹⁴ Sec. 2.4.10), and the area. The segment losses are summed to provide the total sector loss.

Calculations of ground-system resistance, if done manually, are laborious and time-consuming. As a result, it may be difficult to determine the most cost-effective configuration. The computations described above should be programmed for a computer, thereby enabling various ground-system configurations to be quickly evaluated.

Practical ground systems are centered in the exit bushing or downlead terminal. The surrounding area is generally covered with a dense copper ground mat, lightly covered with earth and extending out to a distance of 50 to 100 m. The mesh area is enclosed by a rugged copper cable (secured by ground rods at corners and intermediate points), to which the ground radials are connected. All connections are brazed by hand or welded by using an exothermic process. The ground radials terminate to ground rods driven, if possible, to a depth of a few meters. The ground radials may be interconnected at various radii with circumferential buses to reduce transverse losses within the wired area. All support masts, foundation-reinforcing steel, and guy systems are connected to a number of ground-system radials. Guy-anchor foundations outside the ground-system area are grounded to multiple ground rods. There are some situations where it may be preferable to elevate the wires of all or some portion of the ground system. This may be the case in arctic regions where deeply frozen soil or permafrost is present or where the site area does not have sufficient earth cover to allow burial of the wires.

The ground system should be installed only after tower erection has been completed to avoid damage from heavy machinery. The ground system may be installed with a wire plow or placed manually, buried to a depth of approximately ½ m.

Soil-conductivity values generally available from published Federal Communications Commission (FCC) conductivity maps may not be suitable for use in VLF-LF ground-system design, since the skin depth in the earth at the frequency for which they are applicable is relatively shallow. The depth of penetration in average soil for frequencies within the VLF-LF region may extend to 50 m. Soils to this depth are usually composed of several layers having appreciably different values of conductivity. As a result, the effective conductivity may not be that of the surface layer but depend upon the conductivity and thickness of the individual layers at the frequency of interest.

A conductivity map of North America showing effective earth-conductivity values for a 10-kHz propagating wave has been prepared. The work was extended at a later date to include the preparation of a worldwide map showing effective conductivity values of the earth at frequencies of 10 to 30 kHz. The data presented in these

reports are of a general nature. Specific conductivity values must be obtained at the proposed antenna location for use in the design of the ground system.

Ground conductivity can be determined within the antenna-site area from data acquired by the use of a four-terminal array. 19,20 Soil-conductivity values may vary greatly when the soil is frozen. 18 Sufficient measurement radials are required to establish the soil characteristics within the immediate antenna region and to establish an average value to apply to calculations beyond the wired area. The conductivity values can be entered onto the site map and tabulated into a data file for use with a computer.

24-8 SCALE-MODEL MEASUREMENTS

Scale-model measurements provide direct confirmation of the effective height, static capacity, and self-resonant frequency of a proposed antenna configuration from which the performance of the full-size antenna can be accurately predicted. Modeling is most useful as a supplement to the design of VLF-LF antennas having extensive top loading and numerous support masts.

The E-field and H-field distribution of a simple monopole can be accurately predicted from theory, and the corresponding ground-system design is thereby simplified. This is not the case for a complex top-loaded antenna in which the field beneath the antenna is influenced by overhead-conductor currents and field distortion resulting from grounded masts and guys.

To evaluate ground losses within this high-current area, a knowledge of the *H*-field magnitude and orientation is necessary. These data can be acquired by probing the conductive ground plane upon which the model is erected with a small shielded loop.

Model Techniques

VLF-LF antennas operate over an image plane provided by the earth. To avoid excessive ground losses and to provide an effective image plane for the model, a large, flat, highly conductive surface is required. This can be simulated by using metal-wire mesh 1 cm or so per square, preferably galvanized after weaving. The area of ground plane required depends upon the model scale factor and antenna size. A scale factor of 100 is convenient for low-frequency antennas. The ground plane should extend beyond the antenna in all directions to accommodate *E*-field fringing and to approximate a semi-infinite surface.

It is advisable to elevate the ground plane to a height that will permit measurements to be taken from below. This will provide a degree of instrument shielding and avoid unnecessary disturbance of the antenna field.

The antenna model should be scaled as accurately as possible. Frame towers can be simulated with tubing of equivalent electrical diameter. Multiple-wire cages can be simulated with tubing or solid wire having an equivalent radius. Particular care should be taken to avoid stray shunt capacity at the antenna feed point, as this may reduce measurement accuracy.

A reference antenna with which to refer measurements of effective height should

be provided. This can be a slender monopole located on its own ground plane some distance away.

A source antenna is necessary to provide an essentially plane radiation field of uniform intensity over the model ground plane for measurement of effective height. This may be provided by a nearby broadcast station if its frequency and field intensity are satisfactory or by a transmitting antenna set up several wavelengths distant. The measurement frequency should be scaled up approximately by the antenna model factor but need not correspond exactly to the design frequency. The general arrangement of an antenna range for scale-model measurements is shown in Fig. 24-12.

The effective height of the model antenna is derived from measurement of its open-circuit voltage. To reduce instrument loading, the voltage measurement should be taken directly at the antenna terminal by using a field-effect-transistor (FET) emitter follower or a similar very-high-impedance probe. The voltage at the reference antenna should be measured in a similar manner when each model reading is taken.

The effective height H_{ϵ} of the antenna is determined by

$$H_{\epsilon} = K \frac{V_{\infty} \text{ test model}}{V_{\infty} \text{ reference model}} \times \text{ scale factor}$$

where K is the range-calibration factor, which is determined by relating the opencircuit voltage of a reference monopole to the intensity of the incident field and its electrical height (the electrical height of a short, thin monopole is one-half of its physical height).

The antenna static capacitance C_0 is here defined as the apparent capacitance measured at the antenna terminal as the frequency approaches zero. In practice, the measurement can be taken at a frequency not greater than a few percent of the frequency of self-resonance without introducing a significant error. An accurate measurement can be taken by using a Q meter, work coil, and standard variable capacitor. The measurement value is multiplied by the scale factor to derive the full-size value.

The antenna self-resonant frequency is determined by noting the frequency at which the antenna terminal reactance is zero or at which the terminal current and voltage are in phase. The equivalent resonant frequency of the full-size antenna is equal to the model resonant frequency divided by the scale factor.

E- and H-Field Distribution

To obtain the E- and H-field distribution about the antenna, it is necessary to drive the model antenna with sufficient base current to permit measurements to be taken out to a distance well beyond the top-loaded panels.

The H-field probe can consist of a well-balanced shielded loop as small as possible ($<5 \times 10^{-4} \lambda$ diameter at the measurement frequency). The H-field magnitude, normalized to the antenna-base current, and H-field orientation with respect to a chosen reference point should be measured along the surface of the ground plane. Current direction is found by rotating the loop to the null position which corresponds to 90° from current maximum.

E-field distribution (normalized to base-current amperes) can be taken with a short E-field probe calibrated at the measurement frequency.

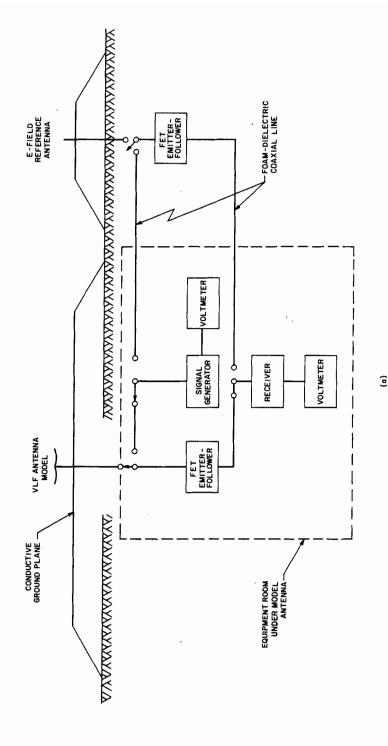


FIG. 24-12 Antenna range for scale-model measurements. (a) Sectional schematic. (b) Plain view.

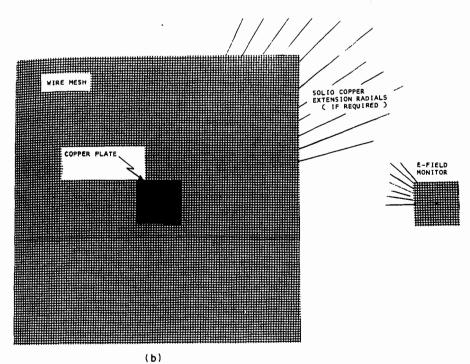


FIG. 24-12 (Continued.)

Potential-Gradient Evaluation

The scale model can also be used to identify areas of the antenna structure in which the potential gradient is higher than average. This condition may be due to panel-conductor configuration or conductor proximity to grounded structural members. The scale model is raised to a high alternating-current potential and observed or photographed after dark by using an appropriate time exposure. Successive photographs are taken as the voltage is increased in increments to the corona level. The test voltage may be provided by a variable high-voltage transformer or by a high-potential test set. Test voltages up to approximately 35 kV rms may be required.

These tests may reveal "hot spots" that will require additional grading. Scaling the corona on-set voltage to actual operating conditions, however, is not practical.

Electrolytic-Tank Model

Similitude modeling can also be conducted on a scale model immersed in an electrolytic tank. This technique has been found to be most useful in confirming the proper position of insulators in the support guys of insulated towers.

A scaled model (1:1000 is a convenient scale factor for large antennas) is erected

 TABLE 24-1
 Characteristics of Typical VLF-LF Antenna Systems

Example	Location	Nominal operating frequency, kHz	Effective height, m	Static capacity, μF	Self-resonant frequency, kHz	Radiated power
Monopole, 800 ft (244 m) Top-loaded monopole, base- insulated tower, 366 m	Annapolis, Md. Trelew, Argentina	51 10.2–13.6 (Omeoa)	104	0.0031	270.0	20 kW at 51 kHz 10 kW at 10.2 kHz
Hybrid top-loaded monopole, grounded tower, 427 m	St-Denis, Réunion	10.2–13.6 (Omega)	163	0.0348	77.17	10 kW at 10.2 kHz
Valley span, six 1920-m spans	Haiku, Hawaii	10.2–13.6 (Omega)	691	0.047	39.0	10 kW at 10.2 kHz
Valley span, 10 spans, average length 2200 m	Jim Creek, Wash.	15-27	114	0.078	34.0	15 kW at 24.8 kHz
Array of two top-loaded monopoles, base-insulated, 457 m	Lualualci, Hawaii	15.5–30	192	0.0399	37.5	460 kW at 23.4 kHz
Top-loaded monopole, base- insulated, 366 m	Hawes, Calif.	27–60	228	0.01448	72.5	50 kW at 27 kHz
Top-loaded monopole, base- insulated tower, 213 m	Aberdeen, Md.	179	152	0.00636	153.0	40 kW at 179 kHz
Hybrid trideco-triatic, 266- m base-insulated tower, eleven 183-m grounded	Annapolis, Md.	15.5–28	148	0.053	33.5	266 kW at 21.4 kHz
Array of two multiple-panel tridecos	Cutler, Me.	15.5–30	152	0.225	38.2	1 MW at 17.8 kHz
Single-multiple-panel trideco	North West Cape, Australia	15.5–30	192	0.1626	34.19	1 MW at 22.3 kHz

over a conductive sheet which forms the base for the antenna and guy system. Insulators can be simulated by small glass beads. The antenna is immersed to the bottom of the electrolytic tank and alternating-current-measurement voltages applied between the antenna-base insulator and the ground plane. The measurement voltage must be sufficient to enable accurate measurement. A convenient measurement frequency is 1 kHz. Ordinary tap water is usually a satisfactory electrolyte.

The voltage, relative to ground, on each side of each insulator is measured by using a probe that is insulated except at the tip. The number and location of the guy insulators can be varied as necessary to ensure that all units are working at their rated

Since the model simulates a static condition, this technique is applicable only to electrically small antennas.

24-9 TYPICAL VLF-LF ANTENNA SYSTEMS

The principal characteristics of a number of current VLF-LF antenna systems are summarized in Table 24-1. The table includes examples of monopoles, top-loaded monopoles, multiple-panel triatics, valley-spans, tridecos, and several hybrid variations. The frequency range represented extends from 10 to 179 kHz; input power, from 100 kW to 2 MW. A megawatt VLF antenna is illustrated in Fig. 24-13.

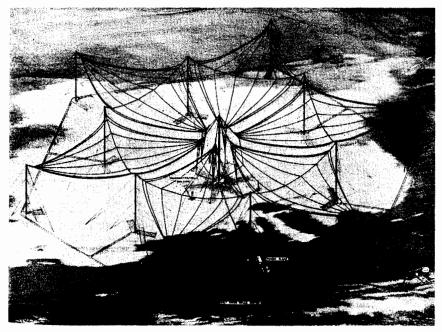


FIG. 24-13 U.S. Navy megawatt VLF antenna located at North West Cape, Australia.

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Medium-Frequency Broadcast Antennas

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25-1 Introduction 25-2
General 25-2
Scope of Design Data 25-2
Characteristics of Radiators 25-2
Ground Currents 25-3
Choice of Plane of
Polarization 25-3
Performance Required of MediumFrequency Broadcast
Antennas 25-4
25-2 Characteristics of Vertical
Radiators 25-5
Assumptions Employed in
Calculating Radiator

Characteristics 25-5

Radiator 25-5

Field Produced by Vertical

Radiation Resistance 25-5

Operating Base Resistance 25-6

General Formulas for Calculating Radiating Characteristics 25-7 Effects of Finite Cross Section 25-Shunt-Fed Radiators 25-8 Top-Loaded Radiators 25-8 Sectionalized Radiators 25-9 25-3 Ground Systems 25-11 General Requirements 25-11 Nature of Ground Currents 25-12 Effect of Ground-System Losses on Antenna Performance 25-12 Effect of Local Soil Conductivity on Ground-System Requirements 25-12 Ground Systems for Multielement Arrays 25-12

Vertical-Radiation

Characteristic 25-7

25-4 Directional Antennas 25-13 Purpose of Directional-Antenna Systems 25-13 Permissible Values of Radiation 25-13 Computation of Pattern Shape 25-Computation of Pattern Size 25-Base Operating Impedance of Radiators 25-21 Effective Field 25-21 Choice of Orientation and Spacing in Directional-Antenna Design 25-22 Choice of Tower Height 25-23 Effect of Finite Radiator Cross Section on Directional Antennas 25-23 25-5 Circuits for Supplying Power to

Directional and Nondirectional

General 25-23 Transmission-Line Requirements 25-24

25-6 Adjusting Directional-Antenna
Arrays 25-24
General Requirements 25-24
Sampling System 25-24
Initial Adjustment 25-24
Proof of Performance 25-25

25-7 Miscellaneous Problems 25-25
Guy-Wire Insulation 25-25
Circuits across Base Insulators 25-25
Simultaneous Use of Towers at
Two or More Frequencies 25-26
Selection of Transmitter Sites 25-

26
Effect of Signal Scattering and
Reradiation by Nearby
Objects 25-26
Protection against Static Discharges
and Lightning 25-26

25-1 INTRODUCTION

Antennas 25-23

Generai

Medium-frequency broadcast transmitting antennas are generally vertical radiators ranging in height from one-sixth to five-eighths wavelength, depending upon the operating characteristics desired and economic considerations. The physical heights vary from about 46 m (150 ft) to 274 m (900 ft) above ground, making the use of towers as radiators practical. The towers may be guyed or self-supporting; they are usually insulated from ground at the base, although grounded shunt-excited radiators are occasionally employed.

Scope of Design Data

The design formulas and data in this chapter are applicable primarily to broadcast service (535- to 1705-kHz band). However, the basic design principles are valid for transmitting antennas for other services in the medium-frequency band (300 to 3000 kHz).

Characteristics of Radiators

Maximum radiation is produced in the horizontal plane, increasing with radiator height up to a height of about five-eighths wavelength. The radiated field from a single tower is uniform in the horizontal plane, generally decreases with angle above the

horizon, and is zero toward the zenith. Radiators taller than one-half wavelength have an upper lobe of radiation at high vertical angles. For radiators with height in excess of about 0.72 wavelength, this upper lobe has more radiated field than the horizontal plane, with a reduction in horizontal radiation with increasing height. For a height of one wavelength, negligible energy is radiated in the horizontal plane. Radiators taller than five-eighths wavelength may be utilized by sectionalizing the tower approximately each half wavelength (Franklin type) and supplying the current to each section with the same relative phase. Figure 25-1 shows vertical radiation patterns for several commonly employed antenna heights, both for constant power and for constant radiated field in the horizontal plane.

Ground Currents

Current return takes place through the ground plane surrounding the antenna. High earth-current densities are encountered and require metallic ground systems to minimize losses.

Choice of Plane of Polarization

Vertical polarization is almost universally employed because of superior groundwave propagation characteristics. Ground-wave attenuation is much greater for horizontal than for vertical polarization, and ionospheric propagation of horizontally polarized

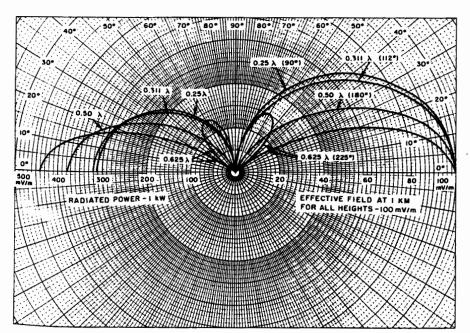


FIG. 25-1 Vertical radiation patterns for different heights of vertical antennas (FCC AM Technical Standards).

signals is more seriously influenced by geomagnetic latitude and direction of transmission. Horizontally polarized antennas have been employed in medium-frequency service in just a few instances where distant nighttime sky-wave coverage was the only objective.

Performance Required of Medium-Frequency Broadcast Antennas

The performance required is determined by class of station and channel assignment. In North America three types of broadcast channels are established: clear, regional, and local. Class I stations, operating on clear channels, are assigned to provide ground-wave service during daytime and both ground-wave and sky-wave service at night. All other classes of station are assigned to render ground-wave service only. Class II stations are secondary stations operating on clear channels and employing directional antennas, when necessary, to protect the service areas of Class I stations. Class III stations are assigned to regional channels and employ directional antennas, when required, for mutual protection. Class IV stations are assigned to local channels; both directional and nondirectional antennas are authorized.

The station classes recognized by the Region 2 Hemispherical Agreement (North, Central, and South American countries) are Classes A, B, and C. A Class I station corresponds to Class A, Classes II and III correspond to Class B, and Class IV corresponds to Class C.

Minimum required antenna performance and power limitations for each class of broadcast station in the United States are established by the Federal Communications Commission (FCC) AM Technical Standards (Table 25-1).

Class I stations are assigned to provide both ground-wave and sky-wave service at night. The vertical radiation pattern for night operation of a Class I station should be designed to provide maximum sky-wave signal beyond the ground-wave service area and minimum sky-wave signal within the ground-wave service area (antifading antennas).¹

TABLE 25-1 Antenna Performance and Power Limitations

Class of station	Required minimum effective field for 1-kW power (unattenuated field), mV/m		Minimum and
	At 1 km*	At 1 mi	maximum power, kW
I	362	225	10 -50
II	282	175	0.25 - 50
III	282	175	0.25-50
IV	241	150	0.25-1.0

^{*1} mV/m at 1 km = 1 V/m at 1 m.

25-2 CHARACTERISTICS OF VERTICAL RADIATORS

Assumptions Employed in Calculating Radiator Characteristics

The characteristics of tower antennas are ordinarily computed by assuming sinusoidal current distribution in a thin conductor over a perfectly conducting plane earth, with the wavelength along the radiator equal to the wavelength in free space. The effect of

the earth plane is represented by an image of the antenna as shown in Fig. 25-2. These assumptions provide sufficiently accurate results for most purposes, but in the determination of base operating resistance and reactance the finite cross section of the tower must be taken into account. Also, the finite cross section modifies the vertical radiation patterns slightly. Generally, this effect is of significance only in antifading antennas for clear-channel stations and in certain directional-antenna systems (discussed in Sec. 25-4). Except as noted, all formulas and data in this chapter are based on the assumptions stated above.

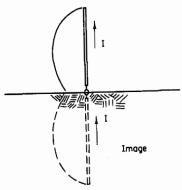


FIG. 25-2 Current distribution and image for a vertical antenna over a perfectly conducting plane.

Field Produced by Vertical Radiator

The field in the horizontal plane is a function of the current flowing and the electrical height. For uniform current in a vertical radiator over a perfectly conducting plane earth, the radiated field is 1.048 V/m (unattenuated field at 1 m) per degree-ampere. For other current distributions, the radiation is proportional to the maximum current and the *form factor K* of the antenna. For sinusoidal current distribution, the radiated field (unattenuated field, volts per meter, at 1 m) is

$$E_r = 60 I_0 (1 - \cos G)$$
 (25-1)

where I_0 = loop current, A $(1 - \cos G) = K$, form factor for sinusoidal current distribution in a vertical radiator G = electrical height of radiator above ground

Radiation Resistance

The loop current I_0 is related to the radiated power P_r by the loop radiation resistance $R_r = P_r/I_0^2$. Figure 25-3 shows the radiated field for a power of 1 kW and the radiation resistance as a function of antenna height G. The radiation resistance may be calculated from

$$R_r = 15 \left[4 \cos^2 G \operatorname{Cin} (2G) - \cos 2G \operatorname{Cin} (4G) - \sin 2G \left[2 \operatorname{Si} (2G) - \operatorname{Si} (4G) \right] \right] \Omega$$
 (25-2)

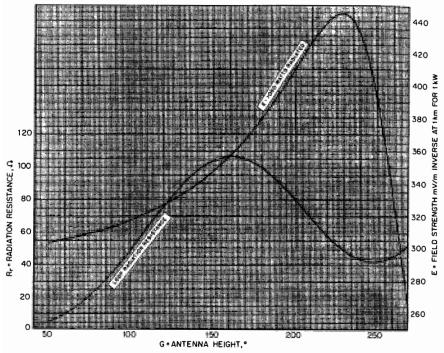


FIG. 25-3 Radiated field and radiation resistance as a function of antenna height G.

where Cin
$$(x) = \int_0^x \frac{1 - \cos x}{x} dx$$
 (cosine integral)

$$= \ln x + C - \text{Ci }(x)$$
Ci $(x) = -\int_x^\infty \frac{\cos x}{x} dx$ (cosine integral)

$$C = 0.5772 \cdots \text{ (Euler's constant)}$$
Si $(x) = \int_0^x \frac{\sin x}{x} dx$ (sine integral)

Operating Base Resistance

For sinusoidal current distribution, the base radiation resistance is related to the loop radiation resistance by $R_{\text{r(base)}} = [R_{\text{r(loop)}}]/\sin^2 G$. However, the actual base resistance of a practical tower radiator may vary widely from this value because of the finite cross section of the tower and other effects.^{2,3} Numerical electromagnetic analysis (otherwise known as moment-method modeling) is useful for estimating base impedances while taking such effects into account.

vertical-Radiation Characteristic

The relative field pattern in a vertical plane through the radiator is known as the vertical-radiation characteristic. It is defined as having unit value in the horizontal plane $(\theta = 0^{\circ})$.* Based on the assumptions stated above, the vertical-radiation characteristic is

$$f(\theta) = \frac{\cos(G\sin\theta) - \cos G}{(1 - \cos G)\cos\theta}$$
 (25-3)

General Formulas for Calculating Radiating Characteristics

The form factor and vertical-radiation characteristic establish the radiated field in the horizontal and vertical planes. For any current distribution, they may be determined from

$$Kf(\theta) = 1.048 \int_0^G I(z) \cos \theta \cos (z \sin \theta) dz$$
 V/m at 1 m (25-4)

where z = height of current element dz, electrical degrees

I(z) = current at z, A

 θ = elevation angle

G = antenna height

The radiation resistance ist

$$R_r = 60 \int_0^{\pi/2} [Kf(\theta)]^2 \cos \theta \ d\theta \qquad \Omega^{\ddagger}$$
 (25-5)

Effects of Finite Cross Section

Current Distribution The effect of finite tower cross section on the current distribution and vertical-radiation characteristic may be taken into account by assuming a current distribution of the following form suggested by Schelkunoff:²

$$I(z) = I_0 \sin \left[\gamma (G - z) \right] + jkI_0 \left(\cos \gamma z - \cos \gamma G \right)$$
 (25-6)

where $I_0 = \text{maximum in-phase current}$, A

z =height of current element

 $\gamma = \lambda_0/\lambda$, ratio of wavelength in free space to wavelength along tower

G = height of tower, electrical degrees

 $k \approx 50/(Z_0 - 45)$, for antenna heights near $\lambda/2$

 $Z_0 = 60 \left[\ln \left(2G/a_{eq} \right) - 1 \right]$, characteristic impedance of tower (25-7)

 $a_{\rm eq} = \sqrt{naa_0}$, equivalent tower radius

n = number of tower legs

a = cage radius (distance from tower center to tower leg)

 a_0 = tower-leg radius

^{*}The symbol θ is used in this chapter to denote angle above the horizontal plane.

[†]An alternative method of calculation is given by Carter.4

[‡]Note that the radiated power is equal to f^2R_r . For $E = Kf(\theta)$, mV/m at 1 km, P (watts) = $1/60 \int_0^{\pi/2} E^2 \cos \theta \ d\theta$.

When the cross section is vanishingly small, Z_0 is very large, $k \to 0$, and the current distribution approaches the simple sinusoidal.

For short towers, this current distribution is very nearly the simple sinusoidal; for a quarter-wave tower, the two are identical except for the reduced wavelength. For towers higher than a quarter wavelength, the departure becomes significant.

Vertical-Radiation Characteristic and Form Factor Applying Eq. (25-4) to the Schelkunoff current distribution, the form factor K_2 and the vertical-radiation characteristic $f_2(\theta)$ become

$$K_{2}f_{2}(\theta) = \frac{\gamma \cos \theta}{\gamma^{2} - \sin^{2} \theta} \left[\cos \left(G \sin \theta \right) - \cos \gamma G \right]$$

$$+ jk \cos \theta \left[\frac{\gamma \sin \gamma G \cos \left(G \sin \theta \right)}{\gamma^{2} - \sin^{2} \theta} \right]$$

$$- \frac{\sin \theta \cos \gamma G \sin \left(G \sin \theta \right)}{\gamma^{2} - \sin^{2} \theta}$$

$$- \frac{\cos \gamma G \sin \left(G \sin \theta \right)}{\sin \theta}$$

$$\left[\frac{\cos \gamma G \sin \left(G \sin \theta \right)}{\sin \theta} \right]$$
(25-8)

The variations of the vertical-radiation characteristic, based on the sinusoidal and Schelkunoff assumptions, are relatively small and would have only minor practical effects in nondirectional radiators or in directional-antenna systems employing identical towers. However, for directional-antenna systems employing tall towers of different heights, the variations in amplitude and phase of the vertical-radiation characteristics must be taken into account [see Sec. 25-4, Eq. (25-45)].

Shunt-Fed Radiators

Energy may be supplied to a grounded tower by shunt excitation, using a slant-wire feed as shown in Fig. 25-4. The dimensions h/λ and d/λ shown in the figure determine the impedance at the end of the slant wire.^{5,6}

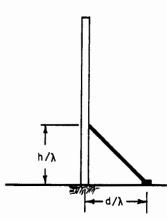


FIG. 25-4 Shunt-fed element.

The current in the slant wires and between the tap point and ground modify the vertical radiation pattern of the shunt-fed tower and result in a slight nonuniformity in radiation in the horizontal plane. Notwithstanding this, the radiation field from a shunt-fed tower is essentially the same as that from a series-fed tower of the same height.

Shunt feeding of a grounded-base tower also may be accomplished by means of a driven wire cage. The cage would generally consist of three to six wires spaced from the tower structure symmetrically on insulators, connected to the tower at the top or at some other appropriate level, and driven at ground level.^{6a}

Top-Loaded Radiators

The radiating characteristics may be modified by altering the current distribution. Top loading is

generally accomplished on guyed towers by connecting a portion of the top guy wires directly to the tower instead of having it connected through an insulator. Another method of top loading that is sometimes employed is a capacity "hat" mounted on the tower top. These methods of top loading have essentially the same effect (within limits) as increasing the tower height (Fig. 25-5).

A capacity disk of radius r at the tower top is equivalent (within practical limits) to an electrical length of

$$B = \frac{rZ_0}{15\pi} \tag{25-9}$$

 Z_0 is defined in Eq. (25-7).

The vertical-radiation characteristic for the top-loaded antenna is given by^{7,8,9}

$$f(\theta) = \frac{\cos B \cos (A \sin \theta) - \sin \theta \sin B \sin (A \sin \theta) - \cos G}{\cos \theta (\cos B - \cos G)}$$
 (25-10)

where A = electrical height of vertical portion of antenna

B =equivalent electrical height of top loading

G = A + B

Sectionalized Radiators

Effects of Sectionalization Antenna heights above five-eighths wavelength may be employed to obtain increased effective field by dividing the tower with insulators into sections of approximately one-half wavelength. The currents in each section are maintained in phase.

For heights less than one wavelength, the tower may be sectionalized in either of the arrangements shown in Fig. 25-6. The vertical-radiation characteristic for the two

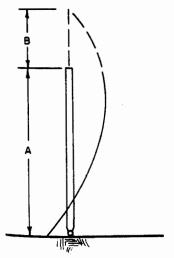


FIG. 25-5 Top-loaded element.

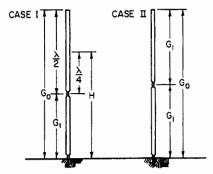


FIG. 25-6 Two methods of sectionalizing vertical radiators.

arrangements, based on simple sinusoidal current distribution, is

Case I:
$$f(\theta) = \frac{2 \cos(90 \sin \theta) \cos(H \sin \theta) + \cos(G_1 \sin \theta) - \cos G_1}{\cos \theta (3 - \cos G_1)}$$
 (25-11)

Case II:
$$f(\theta) = \frac{\cos(G_1 \sin \theta) [\cos(G_1 \sin \theta) - \cos G_1]}{\cos \theta (1 - \cos G_1)}$$
 (25-12)

If top loading is employed on a sectionalized antenna (Fig. 25-7), the vertical-radiation characteristic is expressed as^{8,9}

$$f(\theta) = \frac{\sin \Delta \left[\cos B \cos (A \sin \theta) - \cos G\right] + \sin B \left[\cos D \cos (C \sin \theta) - \sin \theta \sin D \sin (C \sin \theta) - \cos \Delta \cos (A \sin \theta)\right]}{\cos \theta \left[\sin \Delta \left(\cos B - \cos G\right) + \sin B \left(\cos D - \cos \Delta\right)\right]}$$
 (25-13)

where A = height of lower section

B = equivalent top loading of lower section

C =height of entire antenna

D =equivalent top loading of top section

G = A + B

H = C + D

 $\Delta = H - A$

Effects of Finite Cross Section of Sectionalized Radiators The actual current distribution on sectionalized towers varies from simple sinusoidal in the manner discussed above. In this case, the upper section of the tower is a half-wavelength (or very nearly so), and the base termination is adjusted to provide the same current dis-

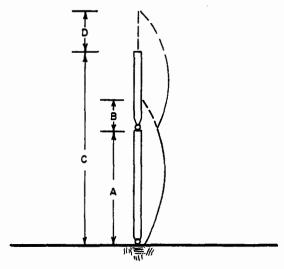


FIG. 25-7 Top-loaded sectionalized vertical radiator.

tribution on the lower section as on the upper section. For these conditions, the currents are (see Fig. 25-6, Case I)

$$I_1(z)$$
 (top section) = $I_0 \sin \left[\gamma(G_0 - z) \right]$
+ $jkI_0 \left\{ 1 + \cos \left[\gamma(G_1 - z) \right] \right\}$ (25-14a)
 $I_2(z)$ (bottom section) = $I_0 \sin \left[\gamma(G_1 - z) \right]$
+ $jkI_0 \left\{ 1 + \cos \left[\gamma(G_1 - z) \right] \right\}$ (25-14b)

where $\gamma = \lambda_0/\lambda$, ratio of wavelength in free space to wavelength along tower

 I_0 = maximum in-phase current

 G_0 = overall height of tower (both sections)

z =height of current element

 $k \approx 50/(Z_0 - 45)$ for antenna heights near $\lambda/2$

See Eq. (25-7) for Z_0 .

The form factor and the vertical-radiation characteristic are given by

$$K_{0}f_{0}(\theta) = \frac{\gamma \cos \theta}{\gamma^{2} - \sin^{2} \theta} \left[\cos \left(G_{0} \sin \theta \right) - \cos \gamma G_{1} \right.$$

$$\left. - 2 \cos \gamma \pi \cos \left(G_{1} \sin \theta \right) \right]$$

$$+ jk \cos \theta \left\{ \frac{\sin \left(G_{0} \sin \theta \right)}{\sin \theta} \right.$$

$$\left. + \frac{\gamma}{\gamma^{2} - \sin^{2}} \left[\sin \gamma G_{1} - 2 \sin \gamma \pi \cos \left(G_{1} \sin \theta \right) \right. \right.$$

$$\left. + \frac{\sin \theta \sin \left(G_{0} \sin \theta \right)}{\gamma} \right] \right\}$$

25-3 GROUND SYSTEMS

General Requirements

The ground system for a medium-frequency antenna usually consists of 120 buried copper wires, equally spaced, extending radially outward from the tower base to a minimum distance of one-quarter wavelength. In addition, an exposed copper-mesh ground screen may be used around the base of the tower when high base voltages are encountered. Ground-system wires may be supported above the earth rather than buried. This has not become common practice, however, because buried wires are much less susceptible to damage.

Wire size has a negligible effect on the effectiveness of the ground system and is chosen for mechanical strength; AWG No. 10 or larger is adequate. A depth of 4 to 6 in (102 to 152 mm) is generally adequate, although the wires may be buried to a depth of several feet if desired in order to permit cultivation of the soil. When such deep burial is required, the wires should descend to the required depth on a smooth, gentle incline from the tower base, reaching the ultimate depth some distance from the tower. If this precaution is observed, the deep burial will have relatively little effect on the effectiveness of the ground system for typical soil conditions.

Nature of Ground Currents

Ground currents are conduction currents returning directly to the base of the antenna. The total earth current flowing through a cylinder of radius x concentric with the antenna is known as the zone current. It is a function of tower height and is given by

$$I_{zone} = I_0 \left[\sin r_2 - \cos G \sin x + j \left(\cos r_2 - \cos G \cos x \right) \right]$$
 (25-16)

where $I_0 = loop$ antenna current

G = electrical height of antenna

 $r_2 = \sqrt{x^2 + G^2}$

Effect of Ground-System Losses on Antenna Performance

Ground-system losses dissipate a portion of the input power and reduce the field radiated from the antenna. These losses are equivalent to the power dissipated in a resistor in series with the antenna impedance. O Computed values of radiated field based on an assumed series loss resistance of 2 Ω give results for typical installations in good agreement with actual measured effective field intensities. FCC rules require that the assumed series loss resistance for each element of a directional-antenna system shall be 1 Ω .

Effect of Local Soil Conductivity on Ground-System Requirements

A less elaborate ground system may be effective in soil of high local conductivity, 11,12 although adequate local conductivity data are rarely available.

For a seawater site (conductivity, approximately 4.6 S/m*), the salt water provides an adequate ground system; a submerged copper ground screen is employed to make contact with the salt water.

Ground Systems for Multielement Arrays

Individual ground systems are required for each tower of a multielement array. If the individual systems would overlap, the adjoining systems are usually terminated in a common bus. Figure 25-8 shows a typical multielement ground system.

In certain cases, it might be possible to minimize land requirements by departing from the typical approach, taking into account the characteristics of the ground currents in the vicinity of the array. Recent theoretical studies have shown that the ground currents of directional antennas vary in both magnitude and direction from those which would be associated with single radiators considered individually. The magnitudes of the ground currents depend upon the directional-antenna parameters, and the directions of the ground currents vary over the individual radio-frequency cycle. This leads to the conclusion that the ground system for a directional antenna could be modified from the conventional nondirectional ground system in two ways: (1) the ground wires could be concentrated in the regions of higher current density, and (2) the paths of the ground wires could

^{*}Siemens/meter or mho/meter.

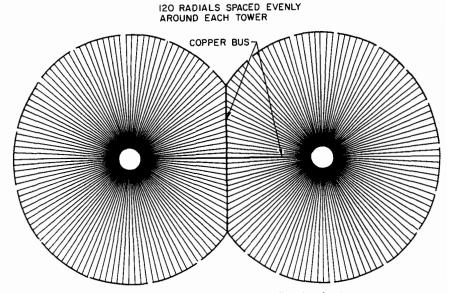


FIG. 25-8 A typical ground system for a two-element directional antenna.

be chosen to favor the direction of maximum current flow at the peak of the radio-frequency cycle.¹³

25-4 DIRECTIONAL ANTENNAS

Purpose of Directional-Antenna Systems

A directional antenna employs two or more radiators to produce radiation patterns in the horizontal and vertical planes different from those produced by a single radiator. Directional antennas are used principally to reduce the radiated signal toward other stations on the same or adjacent channels in order to avoid interference, although the resulting concentration of radiated signal in other directions may be utilized to improve service to specific areas.

Permissible Values of Radiation

Methods of computing interference and establishing maximum permissible values of radiation to avoid interference are described in detail in the FCC Rules and Regulations, Volume III, Part 73.8 For interference from ground-wave signals, radiation in the horizontal plane only is considered. For interference from sky-wave signals, radiation throughout a specified range of vertical angles must be considered. Suppression of radiation is required over sufficient arc to subtend the protected station's service area.

Computation of Pattern Shape

Fundamental Considerations: Two-Element Systems The principles underlying the computation of shape of radiation patterns from two-element arrays are fundamental and may be extended to the computations of shape of patterns from multielement arrays.

The field strength at any point from two radiators receiving radio-frequency energy from a common source is the vector sum of the fields from each of the two radiators. At large distances, the antenna system may be considered to be a point source of radiation. Referring to Fig. 25-9 and considering tower 1 to be reference or zero phase, the theoretical radiated field from the array at the angle ϕ , θ is

$$E_{th}(\theta) = E_1 f_1(\theta) / 0 + E_2 f_2(\theta) / \alpha_2$$
 (25-17)

where α_2 , the difference in phase angle between the two fields, is the sum of the *time-phase-angle* difference A_2 and the apparent space-phase-angle difference:

$$\alpha_2 = s \cos \phi \cos \theta + A_2 \tag{25-18}$$

where E_1 = field radiated by element 1

 E_2 = field radiated by element 2

 $f_1(\theta)$ = vertical-radiation characteristic of element 1

 $f_2(\theta)$ = vertical-radiation characteristic of element 2

s = spacing of element 2 from element 1

 ϕ = angle between element line and azimuth of calculation

For towers of equal height with $F_2 = E_2/E_1$, Eq. (25-17) simplifies to

$$E_{th}(\theta) = E_1 f(\theta) \sqrt{2F_2} \left[\frac{1 + F_2^2}{2F_2} + \cos(s\cos\phi\cos\theta + A_2) \right]^{1/2}$$
 (25-19)

The magnitude of E_{th} is a minimum when

$$\cos(s\cos\phi\cos\theta + A_2) = -1$$
 (25-20)

This occurs when $(s\cos\phi\cos\theta + A_2) = 180^{\circ} \pm 360^{\circ}$; if $F_2 = 1$, $E_{\rm th}$ will be zero. For $F_2 = 1$, Eq. (25-19) simplifies to

$$E_{th}(\theta) = 2E_1 \cos\left(\frac{s}{2}\cos\phi\cos\theta + \frac{A_2}{2}\right)$$
 (25-21)

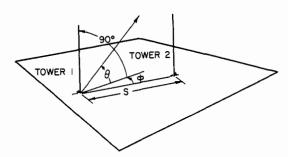


FIG. 25-9 Two-element array.

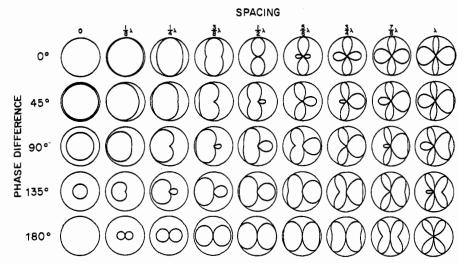


FIG. 25-10 Two-element horizontal plane patterns.

Combinations of equations of the two-element form are widely used in establishing and computing patterns for multielement arrays. Figure 25-10 shows horizontal plane patterns for two-element arrays for a variety of spacings and phasings. ¹⁴ The patterns shown are for equal fields in the two radiators ($F_2 = 1$); the effect of unequal fields is to "fill" the nulls of the pattern. For a given spacing, the angular position of the minimum is changed only by changing the phase angle. The value of $E_{\rm th}(\theta)$ is unchanged by substituting the inverse for F_2 , $F_2 = 1/F_2$.

Two or More Elements: General Equations The pattern shape of directional arrays of two or more elements may be computed by an extension of Eq. (25-17):

$$E_{th}(\theta) = E_1 \sum_{i=1}^{n} F_i f_i(\theta) / \underline{\alpha_i}$$
 (25-22)

where E_1 = field radiated by element 1

 F_i = field ratio of *i*th element, $F_i = E_i/E_1$

 $f_i(\theta)$ = vertical-radiation characteristic of *i*th element

 $\alpha_i = s_i \cos \phi_i \cos \theta + A_i$

 s_i = spacing of *i*th element relative to a reference point (usually element 1)

 ϕ_i = angle between orientation of *i*th element and azimuth of calculation

 θ = vertical angle

 A_i = phase angle of the *i*th element

Three or More Elements: Simplified Formulas for Special Cases The following are formulas for many commonly used array configurations which, through the combination of element pairs, provide a convenient means for establishing the angular position and depth of the minima.

For these examples:

 r_i = assumed field ratio for two-element pair

 a_i = phase angle for two-element pair

 F_i = resulting field ratio for *i*th element in array

 A_i = resulting phase angle for *i*th element in array

Elements are assumed to be of equal height.

FIG. 25-11 Linear array of three elements.

$$E_{th}(\theta) = E_1 f(\theta) \sqrt{4r_2 r_3} \left\{ \left[\frac{1 + r_2^2}{2r_2} + \cos(s \cos \phi \cos \theta + a_2) \right] \right.$$

$$\left. \left[\frac{1 + r_3^2}{2r_3} + \cos(s \cos \phi \cos \theta + a_3) \right] \right\}^{1/2}$$

$$F_2 / A_2 = r_2 / a_2 + r_3 / a_3$$

$$F_3 / A_3 = r_2 r_3 / a_2 + a_3$$
(25-23)

FIG. 25-12 Linear array of four elements.

$$E_{th}(\theta) = E_1 f(\theta) \sqrt{8r_2 r_3 r_4} \left\{ \left[\frac{1 + r_2^2}{2r_2} + \cos\left(s \cos \phi \cos \theta + a_2\right) \right] \right.$$

$$\left. \left[\frac{1 + r_3^2}{2r_3} + \cos\left(s \cos \phi \cos \theta + a_3\right) \right] \right.$$

$$\left. \left[\frac{1 + r_4^2}{2r_4} + \cos\left(s \cos \phi \cos \theta + a_4\right) \right] \right\}^{1/2}$$

$$F_2 / A_2 = r_2 / a_2 + r_3 / a_3 + r_4 / a_4$$

$$F_3 / A_3 = r_2 r_3 / a_2 + a_3 + r_2 r_4 / a_2 + a_4 + r_3 r_4 / a_3 + a_4$$

$$F_4 / A_4 = r_2 r_3 r_4 / a_2 + a_3 + a_4$$

FIG. 25-13 Linear array of five elements.

$$E_{th}(\theta) = E_1 f(\theta) \sqrt{16r_2r_3r_4r_5} \left\{ \left[\frac{1+r_2^2}{2r_2} + \cos(s\cos\phi\cos\theta + a_2) \right] \right.$$

$$\left. \left[\frac{1+r_3^2}{2r_3} + \cos(s\cos\phi\cos\theta + a_3) \right] \right.$$

$$\left. \left[\frac{1+r_4^2}{2r_4} + \cos(s\cos\phi\cos\theta + a_4) \right] \right.$$

$$\left. \left[\frac{1+r_5^2}{2r_5} + \cos(s\cos\phi\cos\theta + a_5) \right] \right\}^{1/2}$$

$$F_2 / A_2 = r_2 / a_2 + r_3 / a_3 + r_4 / a_4 + r_5 / a_5$$

$$F_3 / A_3 = r_2 r_3 / a_2 + a_3 + r_2 r_4 / a_2 + a_4 + r_2 r_5 / a_2 + a_5$$

$$+ r_3 r_4 / a_3 + a_4 + r_3 r_5 / a_3 + a_5 + r_4 r_5 / a_4 + a_5$$

$$F_4 / A_4 = r_2 r_3 r_4 a_2 + a_3 + a_4 + r_2 r_3 r_5 / a_2 + a_3 + a_4 + a_5$$

$$F_5 / A_5 = r_2 r_3 r_4 r_5 / a_2 + a_3 + a_4 + a_5$$

$$F_5 / A_5 = r_2 r_3 r_4 r_5 / a_2 + a_3 + a_4 + a_5$$

FIG. 25-14 Parallelogram array of four elements.

$$E_{th}(\theta) = E_1 f(\theta) \sqrt{4F_2 F_3} \left\{ \left[\frac{1 + F_2^2}{2F_2} + \cos(s_{12} \cos \phi \cos \theta + A_2) \right] \left[\frac{1 + F_3^2}{2F_3} + \cos(s_{13} \cos [\phi - \phi_c] \cos \theta + A_3 \right] \right\}^{1/2}$$
(25-26)

provided $F_4/\underline{A_4} = F_2F_3/\underline{A_2} + \underline{A_3}$. In these formulas, the field is the product of several two-element-array expressions and will be zero whenever any of the component expressions is zero. For $r_n \neq 1$, the position of the minima may be shifted slightly; however, this shift is usually small.

Formulas (25-23) through (25-26) are valid only for computing patterns in the vertical planes for towers of equal height.

Computation of Pattern Size

General Formulas (25-17) through (25-26) establish the shape of radiation patterns. To determine the magnitude of the radiation, the reference field E_1 must be evaluated.

Total Resistance The current I_1 in the reference element is related to the total radiated power P_r , by the *total resistance* R_r of the array:

$$R_{\rm rl} = \frac{P_r}{I_1^2} \quad \Omega$$
 (25-27)

where the subscript 1 indicates that the total resistance is referred to the current in element 1. The radiated field is directly proportional to the current, and

$$E_1 = E_0 \left(\frac{R_{r1}}{R_{r1}}\right)^{1/2}$$
 mV/m at 1 km (25-28)

where E_0 is the effective field of the reference element, operating independently and without loss, and R_{r1} is the radiation resistance. The total resistance is calculated from the operating resistances of each element of the array, as discussed in the following subsection.

Mutual Impedance: Definition for Antenna Case The mutual impedance between two antennas is defined in the usual manner:

$$Z_{12} = Z_{21} = V_1/I_2 = V_2/I_1$$

The mutual impedance is a complex quantity:

$$Z_{12}/\sigma_{12} = R_{12} + jX_{12} = \sqrt{R_{12}^2 + X_{12}^2}/\tan^{-1}X_{12}/R_{12}$$

The mutual impedance is a function of the spacing between the antennas and the height of the elements. The general equations for mutual resistance and reactance between two antennas of unequal height have been derived by Cox.¹⁵

Operating Resistance of Radiators in a Directional-Antenna System The operating resistance of a radiator in a directional array is the sum of the radiation resistance R_n an assumed loss resistance R_a (see Sec. 25-3), and the coupled resistance R_c .

$$R_0 = R_c + R_a + R_c \tag{25-29}$$

The coupled resistance of element 1 is

$$R_{c1} = M_{12}Z_{12}\cos(\mu_{12} + \sigma_{12}) + M_{13}Z_{13}\cos(\mu_{13} + \sigma_{13}) + \cdots + M_{1n}Z_{1n}\cos(\mu_{1n} + \sigma_{1n})$$
 (25-30)

The coupled reactance is

$$X_{c1} = M_{12}Z_{12}\sin(\mu_{12} + \sigma_{12}) + M_{13}Z_{13}\sin(\mu_{13} + \sigma_{13}) + \cdots + M_{1n}Z_{1n}\sin(\mu_{1n} + \sigma_{1n})$$
 (25-31)

where M_{1n} = current ratio between tower n and tower 1

 Z_{1n} = mutual impedance between tower n and tower 1

 μ_{1n} = phase angle of current between tower n and tower 1

 σ_{1n} = phase angle of Z_{1n}

Note that M_{12} is the *current* ratio of tower 2 referred to tower 1. For unequal height towers, the loop-current ratio and the *field* ratio are related by the ratio of the form factors. For loop-current reference,

$$\frac{M_{12}}{F_{12}} = (1 - \cos G_1)/(1 - \cos G_2)$$
 (25-32)

Computation of Total Resistance: Formulas The total resistance R_{t1} is

$$R_{t1} = R_{01} + M_{12}^2 R_{02} + M_{13}^2 R_{03} + \cdots M_{1n}^2 R_{0n}$$
 (25-33)

Determination of Reference Field by Mechanical Integration (Hemispherical Integration) The value of E_1 may be established by integration of the power flow from the antenna system over the hemisphere. The resulting hemispherical root-mean-square (rms) value is then compared with an isotropic reference, in which the power flow is uniform in all directions over the hemisphere:

$$E_1 = 245\sqrt{P}$$
 mV/m at 1 km (25-34)

where P = power, kW. The hemispherical rms value of relative field strength e_h is determined by integration over the hemisphere. The integration may be approximated by the trapezoid method:

$$e_h = \sqrt{\frac{\pi\Delta}{180} \frac{[e_{\text{rms}}(\theta = 0)]^2}{2} + \sum_{n=1}^{N} \{[e_{\text{rms}}(\theta)]^2 \cos \theta\}}$$
 (25-35)

where Δ = interval in degrees of vertical angle θ for equally spaced calculations

 θ = vertical angle (0 = horizontal)

 $N = 90/\Delta - 1$

$$e_{\rm rms}(\theta) = \sqrt{\sum_{i=1}^{k} \sum_{j=1}^{k} F_i f_i(\theta) F_j f_j(\theta) \cos \mu_{ij} J_0(S_{ij} \cos \theta)}$$
 (25-36)

 $^{^{\}circ}$ In the discussion which follows, lowercase e is used to denote relative fields. Actual electric field strengths are indicated by capital E.

[†]Other numerical approximations, such as Simpson's or Gauss's, may provide some improvement in accuracy.

where k = number of elements

F = field ratio

 $f(\theta)$ = vertical-radiation characteristic

 μ_{ij} = phase-angle difference between the *i*th and *j*th elements

 S_{ij} = spacing between *i*th and *j*th elements, rad

 $J_0(s)$ = zeroth-order Bessel function

The no-loss value of E_1 is then calculated from

$$E_{01} = \frac{E_i \sqrt{P}}{e_h}$$
 mV/m at 1 km (25-37)

Power Losses If the individual currents are known (i.e., the operating resistances are known), the total power lost in an array by dissipation in the antenna system (ground system, element-coupling system, etc.) can be calculated from

$$P_{\ell} = \frac{\sum_{i=1}^{k} R_{ai} I_{oi}^{2}}{1000} \quad \text{kW}$$
 (25-38)

where k = number of elements

 R_{ai} = assumed loss resistance of *i*th element

 $I_{\alpha} = \text{loop current of } i \text{th element (base current if } i \text{th-element height is less than } \lambda/4)$

The reference field E_1 is directly proportional to the current in the reference tower.

If, on the other hand, the individual operating resistances are not known, as would be the case when e_h is determined by hemispherical integration, the losses may be calculated and the reference field E_1 with loss determined by reference to the root-sum-square (rss) currents of the elements in the array. The rss currents are related to the rss fields by the form factor K [see Eq. (25-1)] of the individual elements. If all the elements in the array are of the same height, the two are directly proportional. To determine the losses for this condition, first determine the horizontal-plane no-loss rss of the fields from the elements of the array:

$$E_{\text{rss}} \text{ (no loss)} = \frac{245\sqrt{P}}{e_h} \sqrt{\sum_{i=1}^{k} F_i^2}$$
 (25-39)

Next, determine the no-loss current rss of the array by using the following:

$$I_{\text{rss}} \text{ (no loss)} = \frac{4.08\sqrt{P}}{e_h} \sqrt{\sum_{i=1}^{k} \left(\frac{F_i}{K_i}\right)^2}$$
 (25-40)

where K_i = form factor of element i.

For towers of different heights, the form factor K_i must be applied for each height of tower in determining I_{rss} . The reference field E_i with loss may be determined from

$$E_{l} (loss) = E_{l} (no loss) \left(\frac{P}{P + I_{rss}^{2} (no loss) \frac{R_{a}}{1000}} \right)$$
 (25-41)

Base Operating Impedance of Radiators

General The base operating impedance of a tower in a directional-antenna array is usually different from the computed operating loop impedance. The base operating resistance and reactance may be estimated as follows:

Estimate the base self-resistance (R_{base}) and reactance (X_{base}) of the tower. Then assume the base mutual impedance to be $Z_{m(base)} = Z_m(R_{base}/R_r)$, ¹⁶ and substitute these values in Eqs. (25-30) and (25-31).

Base operating impedances also may be determined by moment-method modeling. By the same process, the voltage and current drive conditions are determined.¹⁷

Parasitic (Zero-Resistance) Elements A radiating element operating at zero resistance and not supplied with power by connections from the distribution circuits is said to be parasitic. This condition obtains when the negative coupled resistance is equal to the sum of the radiation resistance and loss resistance. A parasitic element properly tuned will operate in phase-and-field-ratio relationships approximating those computed.

Arrays have been designed to use parasitic elements where major lobe gain is the primary objective. Field ratios and phases for parasitic elements cannot be independently controlled, making them undesirable for arrays which must be adjusted to produce deep nulls in radiation at specific azimuths. Where parasitic or near-parasitic elements are encountered in such arrays, specialized feeder-system design to either feed or accept small amounts of power to or from them must be employed to allow for an acceptable range of adjustment.

Negative-Resistance Elements A negative-resistance element receives more power by coupling to the other elements than is required to obtain the desired field from the element. The excess power is sometimes dissipated in a resistor but is usually returned to the positive-resistance elements through the power-distributing circuits.

Effective Field

Definition The rms value of the radiation pattern in the horizontal plane ($\theta = 0$, in unattenuated field at 1 km) is referred to as the *effective field*. The effective field of a directional antenna is modified from that for a single radiator by directivity at vertical angles and higher ground and circuit losses.

Calculation of Directional-Antenna Effective Field The rms field of a directional-antenna pattern at any vertical angle may be calculated from

$$E_{\rm eff} = E_1 e_{\rm rms}(\theta)$$
 mV/m at 1 km (25-42)

where E_1 is the reference field and $e_{rms}(\theta)$ is as defined in Eq. (25-36).

FCC Standard Radiation In the United States the FCC Rules and Regulations require that the radiation from a medium-wave directional-antenna system be depicted by a standard pattern. The standard radiation pattern is an envelope around the theoretical radiation pattern. It is intended to provide a tolerance within which the actual operating pattern can be maintained. The standard radiation values are cal-

culated from

$$E_{\text{std}}(\theta) = 1.05\sqrt{[E_{\text{th}}(\theta)]^2 + [Qg(\theta)]^2}$$
 mV/m at 1 km (25-43)

where $E_{th}(\theta)$ = theoretical radiation [Eqs. (25-17) through (25-26)]

Q = (10.0) or $(10\sqrt{P})$ or $(0.025E_{rss})$, whichever is largest

P = power, kW

 $f_s(\theta)$ = vertical-radiation characteristic of shortest element in array

 $g(\theta) = f_s(\theta)$ if shortest element is shorter than $\lambda/2$

$$g(\theta) = \frac{\sqrt{[f_s(\theta)]^2 + 0.0625}}{1.030776}$$
 if shortest element is taller than $\lambda/2$

$$E_{rss} = E_1 \sqrt{\sum_{i=1}^{n} F_i^2}$$
, horizontal plane pattern root sum square

n = total number of elements

 F_i = field ratio of *i*th element

 E_{I} = reference field

FCC rules include a provision to modify or augment the standard pattern to accommodate actual operating patterns when radiation is in excess of the standard radiation pattern. Radiation is augmented over a specified azimuthal span and is calculated from

$$E_{\text{aug}}(\theta) = \sqrt{\left[E_{\text{std}}(\theta)\right]^2 + A\left[g(\theta)\cos\left(\frac{180D_A}{S}\right)\right]^2}$$
 (25-44)

where $E_{\text{std}}(\theta)$ = standard radiation [See Eq. (25-43).]

 $A = \{[E_{aug}(\theta)]^2 - [E_{std}(\theta)]^2\}$ at central azimuth of augmentation S = azimuthal span for augmentation. The span is centered on central azimuth of augmentation.

 D_A = absolute difference between azimuth of calculation and central azimuth of augmentation. D_A cannot exceed S/2 for augmentation within a particular span.

 $g(\theta)$ is as defined above.

If there are overlapping spans of augmentation, the augmentations are applied in ascending order of central azimuth beginning with true north (0° true). In this case, there is in essence an augmentation of an augmentation. If the central azimuth of an earlier augmentation overlaps the central azimuth of a later augmentation, the value of A is adjusted in the latter case to provide for the specified resulting radiation at the later central azimuth.

Choice of Orientation and Spacing in Directional-Antenna Design

The required placement of towers in a directional array is determined by the general shape of pattern desired. In-line arrays produce patterns having line symmetry; other configurations may or may not exhibit symmetry, depending upon the operating parameters. Closely spaced towers have mutual impedances which are relatively large compared with the self-resistances. This may result in low operating resistances and high circulating currents, which make for poor bandwidth and high losses and should be avoided. In general, these effects may occur when spacings less than about one-quarter wavelength are introduced.

Choice of Tower Height

The choice of tower height is governed by the effective field required, the need for adequately high base resistances, the desired vertical patterns, aeronautical restrictions, and economic limitations. These requirements are usually met by heights on the order of one-quarter wavelength. Shorter towers are sometimes employed on the lower frequencies for practical reasons, as long as the required FCC minimum effective field is obtained and adequately high base resistances are provided. Taller towers produce higher effective field strengths and may reduce radiation at high vertical angles.

Effect of Finite Radiator Cross Section on Directional Antennas

The modified current distribution due to the finite cross section of practical tower radiators results in a complex vertical-radiation characteristic different from that computed by using the simplified assumptions. When towers of unequal height are employed, the difference in amplitude (and sometimes in phase) of vertical-radiation characteristics may be taken into account. The radiation from an array employing towers of unequal height may be computed by using Eqs. (25-17) and (25-22). The difference in phase angle requires the substitution for α_n with the angle α'_n , which includes an additional term δ_n :

$$\alpha'_n = s_n \cos \phi_n \cos \theta + A_n + \delta_n \tag{25-45}$$

where δ_n = phase-angle difference between $f_1(\theta)$ and $f_n(\theta)$ at angle θ .

25-5 CIRCUITS FOR SUPPLYING POWER TO DIRECTIONAL AND NONDIRECTIONAL ANTENNAS

General

Radio-frequency power must be supplied to the individual radiators of the directionalantenna system in the proper proportions and phase-angle relationships to produce the desired radiation patterns. Means for controlling the current ratios and phase angles are required to permit adjustment and maintenance of the patterns. The circuits must provide a load into which the transmitter will operate properly.

The required functions are shown in block form in Fig. 25-15. The antenna-tun-

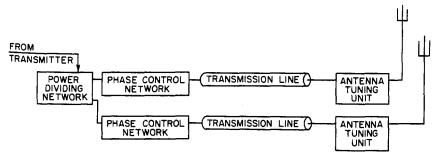


FIG. 25-15 Basic functions of array feed system.

ing units transform the operating base impedance of the radiators to the characteristic impedance of the transmission lines and provide a portion of the required phase shift. Additional phase shift is introduced by the transmission lines. The phase-control networks contain variable components for phase control. The power-dividing network supplies variable voltages to each line for power control. The networks should be designed for minimum power loss and for a broadband-frequency response. Modern network analysis methods make whole-system modeling possible. All feed-system components, and mutual and self-admittance representations for the tower bases, can be included in an overall model, from which adjustability and bandwidth characteristics can be determined. 18

Transmission-Line Requirements

Transmission lines may be either of the concentric or the open-wire, unbalanced type. Concentric lines have a lower characteristic impedance, usually requiring less transformation between tower and line. Their complete shielding eliminates any radiation from the line.

25-6 ADJUSTING DIRECTIONAL-ANTENNA ARRAYS

General Requirements

A directional antenna must be adjusted to produce a radiation pattern substantially in accordance with its design. In the United States, the construction permit issued by the FCC specifies maximum permissible values of radiation in pertinent directions.

Sampling System

An indication of the field-ratio and phase-angle relationships among the radiators is needed to adjust a directional-antenna system. Depending on the tower heights, this is provided by permanently installed sampling transformers in the antenna-tuning unit or sampling loops mounted on the towers. These devices are connected by sampling lines to an antenna monitor.

The individual sampling lines may be cut to the same length, making the phase delay on all lines equal. Excess line should be stored so as to be exposed to the same weather conditions as the longer portions of the other lines.

Initial Adjustment

The initial adjustment of a directional-antenna system is generally accomplished by setting the reactances of the antenna-tuning and power-dividing components to their computed values and supplying power to the antenna system. Usually, the phase and field-ratio indications will be different from those desired. The adjustable tuning components are then varied until the phase and field-ratio indications correspond closely to the computed values.

Preliminary field-intensity measurements are then made to determine the approximate shape of the pattern. These data are analyzed to determine if changes are required to bring the operating pattern shape into agreement with the computed pattern shape.

Proof of Performance

A proof of performance is required in the United States for all directional-antenna systems before regular operation is authorized. Part 73 of the FCC Rules and Regulations describes the procedures and required measurements for an acceptable proof of performance.

After the pattern has been properly adjusted and the adjustment confirmed by the proof of performance, monitoring points are established in directions specified by the construction permit. The field intensities for directional operation are measured at each monitor point at regular intervals to provide an indication of pattern performance and stability.

25-7 MISCELLANEOUS PROBLEMS

Guy-Wire insulation

Guy wires supporting tower radiators must be insulated from the tower and from ground and must be broken up into sections sufficiently short so that the induced currents do not distort the radiation pattern. Strain insulators are installed at the guy anchor, the point of attachment to the tower, and at intervals along the guy wire. The maximum length of any individual guy-wire section should not exceed $\lambda/8$ to $\lambda/10$. Occasionally, portions of the topmost guy wires are not insulated from the tower in order to provide top loading to the element.

Circuits across Base insulators

It is usually necessary to cross the base insulator of a tower antenna with alternatingcurrent power circuits. Power for aeronautical-obstruction lighting of the tower or other purposes may be supplied by means of chokes or transformers. Lighting chokes are wound of ordinary insulated copper wire on a suitable form, with a sufficient number of turns to provide a reactance at the operating frequency, which is high compared with the tower-base impedance. Radio-frequency bypass condensers are installed between individual windings.

Alternating current can be supplied by an Austin transformer, consisting of linked toroidal cores mounting the primary and secondary windings. There is an air gap of several inches between the two cores, and the only effect at the medium frequency is that due to the shunt capacity.

Transmission lines for other communication systems may be isolated from the tower at the medium frequency by a quarter-wave isolation section of line. The outer conductor of the coaxial cable is grounded immediately before the rise up the tower and is supported on insulated hangers to a point approximately one-quarter wavelength from ground, where it is connected to the tower. The outer conductor of the coaxial line and the tower constitute a shorted quarter-wavelength transmission line at the medium frequency, resulting in a high impedance at the tower base. A method for towers shorter than $\lambda/4$ is to install the quarter-wavelength section along the ground rather than up the tower.

Devices known as isocouplers, which couple VHF or UHF energy while providing virtually an open circuit at medium frequencies, are another means available for base circuit isolation. 19 As is the case for Austin transformers, a slight amount of shunt capacitance is introduced by such devices.

Simultaneous Use of Towers at Two or More Frequencies

It is occasionally desired to use one or more tower radiators simultaneously at two or more different frequencies. This may be done by employing suitable filters to isolate the transmitters from each other.

Selection of Transmitter Sites

Transmitter sites should be selected in an area providing sufficient ground which is reasonably flat and level, of high local conductivity, free of obstructions which might interfere with the proper functioning of the radiating system, and so located as to provide maximum signal to the principal city and the service area. This last requirement, applied to operations with a directional-antenna system, usually dictates a choice of site which will place the main radiation lobe in the direction of the city.

Effect of Signal Scattering and Reradiation by Nearby Objects

General Structures and terrain features near the transmitter site may reflect the signal from the antenna or may reradiate sufficient signal to affect the performance of the antenna. Large buildings near the transmitter site, mountains, or rugged terrain may distort the radiation pattern of directional and nondirectional antennas. The effects may be serious in the case of a directional-antenna system requiring a high degree of signal suppression, particularly if the buildings or hills are in the main radiation lobe of the antenna. Such objects are usually too irregular to permit application of analytic methods to a determination of reradiation. Their effect may often be estimated on the basis of experience with similar objects.

Tail Towers: General It is frequently desired to erect tall towers to support FM and television transmitting antennas or for other purposes in the immediate vicinity of a medium-frequency antenna. These structures are usually of sufficient electrical height to be capable of substantial reradiation in high incident fields.

Tall Towers: Control of Reradiation The tower location should be chosen to have minimum effect on the medium-frequency antenna. If the tower is to be installed in the immediate vicinity of a medium-frequency directional antenna, the field intensities should be computed at a number of locations, and a position chosen for the tower where the incident field is a minimum.

The reradiation from a tower of this height may be controlled by insulating the tower from ground and installing sectionalizing insulators at one or more levels. Where physical conditions allow, wire cages, shorted to the tower at one end and either open-circuited or tuned at the other, depending on length, may be employed instead of sectionalizing insulators. For heights up to approximately $\lambda/2$, a tower may be detuned by insulating its base and installing a suitable reactance between the tower and ground. Guy wires must be insulated at suitable intervals, and transmission and alternating-current lines must be isolated.

Protection against Static Discharges and Lightning

In the absence of suitable precautions, static charges accumulate on towers and guy wires and may discharge to ground. This discharge ionizes the path, and a sustained

radio-frequency arc may follow. Protection can be provided to minimize the accumulation or quench the arc, but it is difficult to provide protection against direct lightning hits. A lightning rod or rods extending above the beacon on the tower top will provide some protection to the beacon, and horn or ball gaps at the tower base will provide protection to the base insulator. However, depending on the magnitude of lightning current, some damage may result to the meters and tuning components.

A direct-current path from the tower to ground will minimize static accumulation. A separate radio-frequency choke, the tuning inductor, or the sampling-line inductor may be connected to maintain the tower at direct-current ground potential. Difficulty may occasionally be experienced with charges accumulating on the individual guy wires and arcing across the guy insulators. This may be eliminated by installing static drain resistors across each guy insulator. These resistors may have a value of 50,000 to $100,000~\Omega$ and should have an insulation path somewhat longer than provided by the guy insulator.

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High-Frequency Antennas*

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26-1 General Design Requirements 26-2
Important Design Parameters 26-2
Types of High-Frequency
Antennas 26-4
Analysis of Antennas 26-4

26-2 Simple Antennas Mounted above Ground 26-5 Effect of the Ground Plane 26-5

Antenna Impedance 26-5
Radiation Patterns of Horizontally
Polarized Antennas 26-6

Radiation Patterns of Vertically
Polarized Antennas 26-7

26-3 Horizontally Polarized Log-Periodic
Antennas 26-8

Single Log-Periodic Curtain with Half-Wave Radiators 26-8 Clamped-Mode Log-Periodic Curtain with Full-Wave Radiators 26-9

Multiple-Curtain Log-Periodic Arrays 26-10 Omnidirectional Log-Periodic
Array with Optimum Vertical

Radiation Pattern 26-12

Rotatable Log-Periodic
Antenna 26-13

High-Power Log-Periodic
Antenna 26-14

26-4 Vertically Polarized Antennas 26-15

Conical Monopole and Inverted
Cone 26-15

Monopole Log-Periodic Antenna 26-17

Dipole Log-Periodic Antenna 26-17

Monopole-Dipole Hybrid Log-

Periodic Antenna 26-17

Extended-Aperture Log-Periodic

Antenna 26-18

Radiation-Pattern Ground

Screens 26-19

Impedance Ground Screens 26-20

26-5 Other Types of Communications

Antennas 26-20

Vertical Whip 26-20

[&]quot;The work of the late William Wharton, coauthor of this chapter in the Second Edition, is acknowledged; his contributions to Secs. 26-1 to 26-6 remain largely intact.

Rhombic Antenna 26-20 Fan Dipole 26-21 Transmitting Loop 26-22 26-6 High-Frequency Receiving Antennas 26-23 Noise Figure 26-23 Signal-to-Noise Ratio 26-26 Practical Receiving Antennas 26-Receiving Loops 26-27 Active Antennas 26-28 Circular Arrays 26-29 26-7 Broadband Dipole Curtain Arrays 26-29 Standard Nomenclature 26-29 Radiation Pattern and Gain 26-30

Slewing 26-31 Impedance Bandwidth 26-33 Practical Considerations 26-34 26-8 Siting Criteria for High-Frequency Antennas 26-35 Fresnel Zone and Formation of Antenna Beam 26-35 Roughness in First Fresnel Zone 26-37 Horizon Obstructions 26-37 Terrain Slope 26-37 Ground Conductivity 26-38 Coupling between Co-Sited Antennas 26-38 26-9 Recent Developments 26-40 Multimode Spiral Antennas 26-40

26-1 GENERAL DESIGN REQUIREMENTS

High-frequency (HF) antennas are used in the range of frequencies from 2 to 30 MHz for communications and broadcasting by means of ionospheric propagation. Ionospheric transmission over large distances usually involves high overall transmission losses, especially under unfavorable ionospheric propagation conditions. High initial and operating costs of transmitting equipment therefore make high-gain transmitting and receiving antennas desirable to provide reliable communications. High-gain antennas are also in common use at international broadcasting stations, where transmissions are beamed to specific geographical areas. In additition to providing an increased signal in the target area, the use of high-gain directional antennas decreases radiation in undesired directions, thereby reducing potential interference to other cochannel services.

Important Design Parameters

The important design parameters of an HF transmitting or receiving antenna include its frequency range, vertical and horizontal angles at which maximum radiation is desired, gain or directivity, voltage standing-wave ratio (VSWR), input power, and environmental and mechanical requirements.

The frequency range should be established by a propagation study to determine the optimum working frequency (OWF) for the path involved, which varies according to distance and location, time of day, season of the year, and sunspot activity. Details of such a study are beyond the scope of this book but may be found in the literature. Laterature are available several computer programs which determine path losses and optimum frequencies on the basis of stored ionospheric data. Actual ionospheric characteristics may also be measured in real time by using commercially available ionospheric sounders and frequency-management systems.

The vertical angle of maximum radiation of the antenna is known as the takeoff angle (TOA). The range of vertical angles pertinent to ionospheric propagation depends on distance, effective layer height, and mode of propagation (i.e., one-hop,

two-hop, etc.). Figure 26-1 is a graph showing estimated TOA for one-hop transmission as a function of distance and virtual layer heights. The height of the E layer may be considered constant at 100 km, but the height of the F2 layer varies widely according to time of day, season of the year, and location. A detailed propagation study is required to determine the required range of TOA. As a rough estimate, however, a range of F1 and F2 virtual layer height of approximately 250 to 400 km may be used in conjunction with Fig. 26-1 to determine approximate TOA range. Multiple-hop propagation can also be assessed approximately by using Fig. 26-1 for each hop. For transmission or reception over distances of more than 4000 km, maximum signal results from low-angle transmission in the range from 2 to 15°, with the lower angles generally providing better results. Propagation over very long paths (greater than 10,000 km) is more complicated than the simple multiple-hop theory, and sophisticated methods of propagation analysis must be used.⁴

The horizontal range of angles on beamwidth (defined as the azimuth angle between the points at which radiation is 3 dB below beam maximum) is determined by the geographical area to be covered. Wide areas require large beamwidths, and narrow areas or point-to-point circuits require small beamwidths. The minimum beamwidth for point-to-point coverage depends on irregularities in the ionosphere and effects of magnetic storms, which cause deviations from great-circle paths. Directions of arrival of HF signals may vary by as much as $\pm 5^{\circ}$ in the horizontal plane because of these effects. This makes the use of antennas with extremely narrow horizontal beamwidths undesirable, especially on circuits which skirt or traverse the auroral zone. International broadcasting requires that the beamwidth subtend the target area with due allowance for path-deviation effects.

Antenna directivity (the gain, neglecting losses) depends primarily on the vertical and azimuthal beamwidths of the radiation pattern. Antenna gain is the directivity multiplied by the antenna radiation efficiency. High gain is necessary when large effective radiated power is needed to overcome large ionospheric transmission losses.

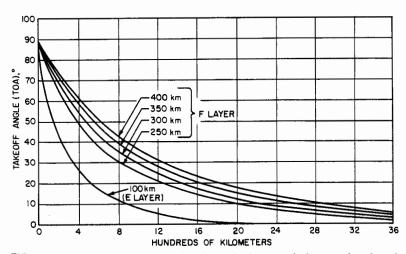


FIG. 28-1 Takeoff angles for one-hop ionospheric transmission as a function of virtual layer height. (After Ref. 5.)

High directivity is desirable for reception in the presence of interference. Low radiation efficiencies can generally be accepted for reception when there is a high level of ambient noise and the high antenna noise figure does not degrade performance. At very quiet receiving sites, high radiation efficiency (i.e., low noise figure) is necessary to prevent the antenna from degrading circuit performance.

For transmitting antennas, the acceptable level of reflected power from the antenna is usually determined by the characteristics of the transmitter. Reflected power is usually specified in terms of the VSWR. Modern solid-state transmitters operating in the 0.1- to 10-kW range tolerate maximum VSWR of 2.5:1. Many such transmitters will tolerate a higher VSWR of 3:1 or 4:1 by automatically reducing their output power. High-power broadcasting transmitters in the 100- to 500-kW range of carrier-power levels tolerate maximum VSWRs of 2:1. Older transmitters have much lower maximum VSWR limits of 1.5:1 or 1.4:1.

The power-handling capacity of a transmitting antenna is specified by both an average power and a peak envelope power (PEP). The average power determines the required current-carrying capacity of the antenna conductors. The peak power determines the voltages and electric fields on the antenna, which set requirements on insulator and conductor size to avoid arcing or corona discharge.

Mechanical requirements depend on environmental effects (wind, ice loading, temperature variation, corrosion-causing conditions), limitations on antenna size or tower height, special restrictions imposed by the site, or other considerations such as transportability.

Types of High-Frequency Antennas

Most HF antennas are very broadband and usually require little or no tuning. Several techniques are used to make HF antennas broadband: (1) lowering antenna Q, (2) using log-periodic arrays of monopole or dipole elements, and (3) automatic tuning. Antenna Q may be lowered by adding loss resistance or using "fat" radiators to decrease reactance. Examples of antennas with resistors are rhombics, terminated V's, and resistively loaded dipoles. Typical fattened antennas are fan dipoles, conical monopoles, and wide-bandwidth dipole arrays used in HF broadcasting. The bandwidth of a log-periodic antenna (LPA) is limited only by the number of radiators used, and it is easy to design such an antenna to operate over a 2- to 30-MHz range. Automatic tuning units are used with whips or loop antennas, which by themselves have unacceptably high VSWR over wide frequency ranges.

For special applications, narrow-bandwidth antennas, such as simple resonant dipoles or monopoles or Yagi-Uda arrays, are used because they are often smaller and less expensive than broadband antennas.

Analysis of Antennas

Analysis of most practical HF antennas is not possible by using simple mathematical techniques. Antennas are designed by using sophisticated computer programs which solve Maxwell's equations numerically for arbitrary antenna geometries. ⁷⁻¹⁰ Such programs calculate the current distribution on the antenna, the most important and hardest-to-calculate property of an antenna. The radiation patterns calculated by the most comprehensive computer programs are very accurate, and the results are acceptable substitutes for measured patterns. Driving-point impedances are also calculated

well, but often to somewhat less accuracy than radiation patterns because impedance depends critically on the mathematical representation of the fields in the region of the driving point.

26-2 SIMPLE ANTENNAS MOUNTED ABOVE GROUND

Effect of the Ground Plane

HF antennas are usually operated within one or two wavelengths of the ground or, in the case of base-fed monopoles, directly on the ground. The proximity of the ground modifies the input impedance and the radiation pattern of an antenna. In most practical cases, an accurate evaluation of the effect of the ground is difficult. However, many fundamental properties of HF antennas can be understood in terms of the simple theory of idealized monopoles or dipoles situated over an infinite, flat ground plane. When the ground plane is perfectly conducting, it can be represented exactly by a single image (with the ground plane removed) as illustrated in Fig. 2-7. For ground of finite conductivity, simple image theory does not give an exact solution but will often provide useful approximate results.

Antenna Impedance

The currents in the conductors of an antenna induce currents in the ground plane, and these (or, alternatively, the currents in the image antenna) modify the antenna currents from the values that would occur in free space. The interaction between the antenna and the ground is given by the mutual impedance, which varies with the height of the antenna above ground. The input impedance of the antenna is given by

$$Z_{\rm ant} = Z_{fs} + Z_m$$
 (26-1)

where Z_{fs} = self-impedance of antenna (impedance when isolated in free space)

 Z_m = mutual impedance between antenna and its image

The mutual impedance can be either positive or negative. Chapter 4 contains curves of mutual impedance for several simple but useful geometries. More complex arrangements are best analyzed by using antenna-analysis computer programs.

The mutual impedance of a thin center-fed half-wave vertical dipole whose lower point is at height S/2 above ground is given in Fig. 4-29. In this case, mutual impedance adds to self-impedance so that total antenna impedance increases as the height of the dipole decreases. The mutual impedance of a thin center-fed horizontal dipole at height d/2 above ground is given in Fig. 4-28. In this case, the currents in the image and the antenna are 180° out of phase so that the mutual impedance must be deducted from the self-impedance. For vanishingly small heights self-impedance and mutual impedance cancel, and radiation resistance approaches zero. This means that a horizontal dipole placed close to the ground has a low radiation resistance. Steps must be taken to modify its impedance so that the transmitter is presented with an acceptably low VSWR. The input resistance can be increased by adding series resistance, which improves the VSWR but reduces radiation efficiency (and hence gain). The radiation efficiency with added resistance is given by $R_{\rm rad}/(R_{\rm rad} + R_{\rm loss})$, where $R_{\rm rad}$ is the radiation resistance and $R_{\rm loss}$ is the series loss resistance. Over ground of finite conductivity,

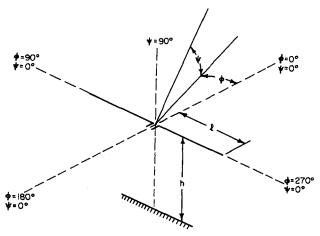


FIG. 26-2 Geometry of horizontal dipole above ground.

an extra resistance must be added in the denominator to account for losses in the ground.

Radiation Patterns of Horizontally Polarized Antennas

In terms of the geometry of Fig. 26-2, the free-space radiation pattern of a horizontal dipole of length 2ℓ is given by

$$d(\varphi') = \frac{\cos(2\pi\ell\sin\varphi'/\lambda) - \cos(2\pi\ell/\lambda)}{(1 - \cos 2\pi\ell/\lambda)\cos\varphi'}$$
 (26-2)

where φ' = angle between line of propagation and equatorial plane

 $\sin \varphi' = \sin \varphi \cos \psi$

 $\varphi = azimuth angle$

 ψ = elevation angle

 $\lambda = wavelength$

When the dipole is placed above ground as shown in Fig. 26-2, the radiation reflected from the ground adds to that from the dipole (i.e., the dipole and image fields add). For the practical situation $h/\lambda > 0.2$, the total radiation pattern, 11 with the small effect of mutual impedance ignored, is

$$D(\varphi,\psi) = d(\varphi')[1 + r_H^2 + 2r_H \cos(\rho_H + 4\pi h \sin\psi/\lambda)]^{1/2}$$
 (26-3)

where h is the height above ground and r_H and ρ_H are respectively the magnitude and the phase of the complex reflection coefficient¹²

$$r_H / p_H = \frac{\sin \psi - (\epsilon' - \cos^2 \psi - j60\sigma\lambda)^{1/2}}{\sin \psi + (\epsilon' - \cos^2 \psi - j60\sigma\lambda)^{1/2}}$$
 (26-4)

where $\epsilon' = \epsilon/\epsilon_0$, the relative dielectric constant

 σ = ground conductivity, S/m

 λ = wavelength, m

At grazing incidence ($\psi = 0^{\circ}$), $r_H = 1$ and $\rho_H = 180^{\circ}$ for all ground constants, so that $D(\varphi,0) = 0$. In the HF band, for most practical values of ϵ' and σ , ρ_H is nearly

equal to 180° for all elevation angles and r_H decreases from 1 at $\psi = 0$ ° to about 0.5 to 0.6 directly overhead at $\psi = 90$ °. In most HF applications the TOA is in the range $0 < \psi \le 30$ °, and the radiation pattern is given accurately by setting $r_H = 1$ and $\rho_H = 180$ ° in Eq. (26-4), which is equivalent to assuming that the ground is perfectly conducting. Equation (26-3) therefore becomes

$$D(\varphi,\psi) = 2d(\varphi')\sin(2\pi h\sin\psi/\lambda)$$
 (26-5)

The maxima (TOA) and minima (nulls) of this expression occur in the equatorial plane ($\phi = 0$ and 180°) at elevation angles given by

$$\psi_{\text{max}} = \sin^{-1}(n\lambda/4h)$$
 $n = 1, 3, 5, ...$ (26-6)

$$\psi_{\min} = \sin^{-1}(n\lambda/2h)$$
 $n = 1, 2, 3, ...$ (26-7)

At the maxima, $D^2=4d^2$, so that the gain is 6 dB above that obtained in free space. This value is exact for perfectly conducting ground and is nearly exact for low elevation angles above ground of finite conductivity. Thus, low-angle radiation from horizontal antennas suffers negligible loss owing to the finite conductivity of the ground, and a radiation-pattern ground screen in front of the antenna is not required. For high values of TOA, the ground losses are not always negligible. As an example, consider an antenna mounted 0.25λ above ground, for which from Eq. (26-6) $\psi_{\text{max}}=90^{\circ}$. For a typical set of ground constants, $r_H=0.5$ and $\rho_H=170^{\circ}$, so Eq. (26-3) becomes $D^2=2.24d^2$, which represents a reduction of gain of 2.24/4 or 2.5 dB compared with that for a perfect ground. However, because a high TOA is used for transmission over short paths, it is not generally necessary to use a ground screen to minimize the loss. An exception is a high-TOA, high-power HF broadcasting antenna which must deliver the maximum signal in the target service area, and in this situation, a ground screen is occasionally used.

Radiation Patterns of Vertically Polarized Antennas

The elevation pattern of a vertical dipole whose center point is at height h above ground has the same form as Eq. (26-3). For the vertical dipole the angles φ and ψ are interchanged in Eq. (26-2), and r_H and ρ_H in Eq. (26-3) are replaced respectively by r_V and ρ_V , the reflection coefficients for vertical polarization:¹²

$$r_{V} / \rho_{V} = \frac{(\epsilon' - j60\sigma\lambda)\sin\psi - (\epsilon' - \cos^{2}\psi - j60\sigma\lambda)^{1/2}}{(\epsilon' - j60\sigma\lambda)\sin\psi + (\epsilon' - \cos^{2}\psi - j60\sigma\lambda)^{1/2}}$$
 (26-8)

This reflection coefficient behaves very differently from that for horizontal polarization [Eq. (26-4)]. The phase ρ_V varies from -180° at grazing incidence to a value approaching 0° at high elevation angles. The magnitude r_V is 1 at grazing incidence, drops to a value of a few tenths, and then increases to the value equal to r_H at $\psi = 90^\circ$. The elevation angle at which r_V reaches a minimum occurs when $\rho_V = 90^\circ$ and is known as the pseudo-Brewster angle, which at HF is typically in the range $5^\circ \leq \psi \leq 15^\circ$.

The most important consequence of this behavior is that radiation at low elevation angles is drastically reduced over imperfectly conducting ground. Finite ground conductivity can cause a gain reduction of as much as 8 to 10 dB at low elevation angles, as shown later in Fig. 26-18 and in Ref. 12. For receiving antennas, losses of this magnitude are usually tolerable, but for transmitting antennas they are not. For

transmission, the loss must be reduced by having the antenna radiate over seawater (which has a high conductivity) or by installing in front of the antenna a large metallic ground screen with a mesh small in relation to the skin depth of the ground underneath the mesh.

26-3 HORIZONTALLY POLARIZED LOG-PERIODIC ANTENNAS

Single Log-Periodic Curtain with Half-Wave Radiators

The basic curtain, illustrated in Fig. 26-3, comprises a series of half-wave dipoles spaced along a transposed transmission line. Successive values of the dipole length and spacing have a constant ratio τ . In a practical LPA, τ has a value between 0.8 and

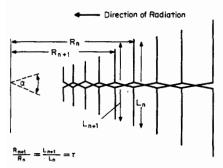


FIG. 26-3 Basic half-wave transposed dipole LPA.

0.95. The bandwidth of the LPA is limited only by the lengths of the longest and shortest dipoles. The number of radiators depends on the frequency range and the value of τ . The parameters τ and α , as discussed in detail in Chap. 14 and Refs. 13 and 14, determine the gain, impedance level, and maximum VSWR of the antenna. It is important to choose τ and α carefully because of the possibility of unwanted resonant effects. Sometimes, energy that normally radiates from the active region travels back to a second active region where the radiators are $3\lambda/2$ long. Excitation of this second active

region causes undesirable impedance and pattern perturbations.

In a well-designed horizontally polarized LPA (HLPA), at any given frequency only dipoles whose lengths are approximately $\lambda/2$ long are excited, and these form a single active region. The active region moves along the curtain from the longest to the shortest dipole as the frequency is increased. Because of this movement, it is possible to mount an HLPA so that the electrical height of the active region is constant or variable in a controlled way, as shown in Fig. 26-4a and b. In other types of horizontal

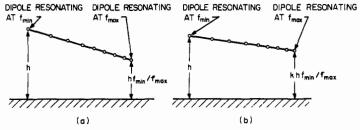


FIG. 26-4 Control of electrical height of LPA. (a) Constant electrical height. (b) Uniform variation of electrical height by a factor of K from f_{\min} to f_{\max} .

antennas, the physical height is constant, so the designer cannot control the variation of electrical height or TOA. A major advantage of the HLPA is, therefore, the ability to maximize the gain at the elevation angles required for reliable communications.

In the basic LPA shown in Fig. 26-3, the dipoles are conventional rods. It is also possible to form the dipoles into a sawtooth shape as shown in Fig. 26-5. The larger effective diameter of the sawtooth (compared with the rod) increases the bandwidth of each dipole so that a greater number are excited to form the active region at each

frequency. This increases the gain and power-handling capacity and reduces the VSWR.

The basic HLPA using half-wave radiators has a gain of 10 to 12 dBi and an azimuthal beamwidth of 60 to 80°.

Clamped-Mode Log-Periodic Curtain with Full-Wave Radiators

The gain of a half-wave LPA can be increased by 2 to 3 dB by doubling its horizontal aperture to one wavelength, thereby decreasing its azimuthal beamwidth to 30 to 40°.

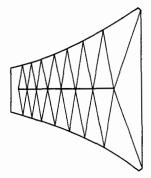


FIG. 26-5 LPA with sawtooth wire elements.

The obvious way to increase the horizontal aperture is to use two half-wave curtains in broadside array as shown in Fig. 26-6a, but the resulting structure is relatively complex. The same horizontal aperture can be achieved with a much simpler structure by use of the clamped-mode technique¹⁵ illustrated in Fig. 26-6b.

The clamped-mode arrangement is equivalent to taking one of the LPA curtains in Fig. 26-6a and pulling it apart sideways, leaving its radiators connected to the same half of the transmission line. When properly designed, a clamped-mode antenna has a gain and radiation pattern nearly identical to those of the broadside array, but it requires only half the number of radiator and transmission-line wires.

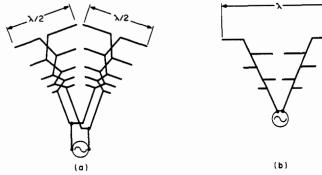


FIG. 26-6 Clamped-mode technique for increasing horizontal aperture of LPA. (a) Two LPA curtains in broadside array. (b) Clamped-mode LPA curtain with equivalent performance.

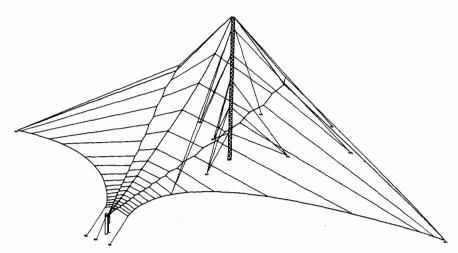


FIG. 26-7 Practical clamped-mode LPA using radiators made from single wires. (Courtesy of TCI.)

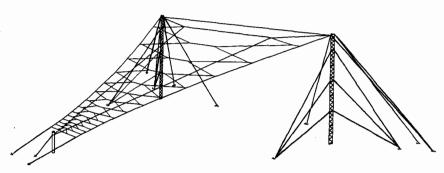


FIG. 26-8 Practical clamped-mode LPA using sawtooth radiators made from wires. (Courtesy of TCI.)

Two practical clamped-mode antennas are shown in Figs. 26-7 and 26-8. The antenna in Fig. 26-7 uses simple rod radiators made from single wires. It has only one tower in contrast to the two towers required for a conventional half-wave dipole HLPA, and consequently the radiators slope down toward the ground. This slope partially offsets the larger horizontal aperture and yields a gain of 12 dBi and an azimuthal beamwidth of 55 to 80°, the values for an equivalent conventional two-tower LPA. Figure 26-8 shows a clamped-mode antenna using sawtooth radiators and two towers. The horizontal curtain is flat, and the aperture is about 1.25λ , so the azimuthal beamwidth is 38° and the gain 14 to 15 dBi.

Multiple-Curtain Log-Periodic Arrays

LPAs can be stacked horizontally and/or vertically to decrease their beamwidths and increase their gain. Horizontal stacking can be done simply by using the clamped-mode technique described previously. Vertical stacking can be applied to simple LPAs

with half-wave dipole elements, as shown in Fig. 26-9, or in conjunction with clamped-mode antennas, as in Fig. 26-10.

Vertical stacking raises the average radiating height of the antennas to a value given by the average electrical height of the curtains, thereby reducing the TOA and vertical beamwidth. Vertical stacking with spacings of about $\lambda/2$ also suppresses high-elevation secondary lobes, which are fully formed when the radiation height is large and can substantially reduce antenna gain. The number of elements in the vertical stack depends on the TOA and gain requirements and the maximum allowed tower height.

To achieve maximum gain in a vertically stacked LPA, it is necessary that the active regions of each curtain line up vertically at each frequency. This will not occur automatically because the lengths of the curtains are different, the upper curtains being longer than the lower curtains. This effect is most noticeable in antennas with more than two curtains in the stack. One technique for aligning the active regions is to control the velocity of propagation along the curtains, making the wave go more slowly on the shorter, lower curtains than on the longer, upper curtains. Wave velocity on a curtain can be controlled by adjusting the length, effective diameter, and spacing of the dipole elements.

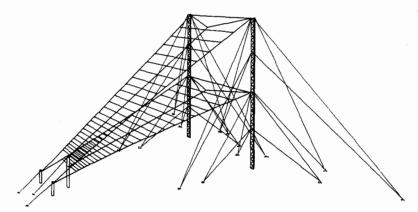


FIG. 26-9 Vertically stacked transposed dipole LPA curtains. (Courtesy of TCI.)

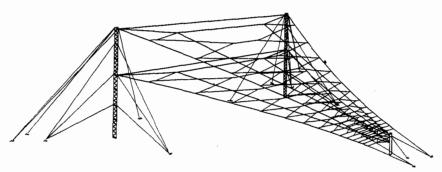


FIG. 26-10 Vertically stacked clamped-mode LPA curtains. (Courtesy of TCI.)

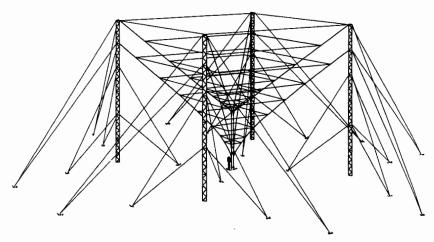


FIG. 26-11 Omnidirectional LPA with optimum TOA. (Courtesy of TCI.)

Omnidirectional Log-Periodic Array with Optimum Vertical Radiation Pattern

It has been pointed out that an HLPA can be arranged to give the optimum TOA at each frequency. A practical example of this technique is shown in Fig. 26-11, which illustrates an antenna designed for shore-to-ship and ground-to-air communication, for which an onmidirectional azimuth radiation pattern is normally required. Such an antenna must have a vertical radiation pattern in which the main lobe has a high TOA at low frequencies, dropping to a low TOA at high frequencies, in the HF band. ¹⁶ This is due to the fact that the low frequencies are used for short-distance communication, for which a high TOA is required, and the high frequencies are used for long-distance communication, for which a low TOA is required.

To meet these requirements, a number of horizontal loops which radiate omnidirectionally in azimuth are stacked vertically and connected in log-periodic form in the inverted-cone configuration shown in Fig. 26-11. The active region of the array, which comprises loops which are about two wavelengths in perimeter, is at the top of the array at the lowest frequency and at the bottom of the array at the highest frequency. A typical array operates over a 4- to 30-MHz-frequency range. The highest loop is placed 37 m above the ground, so that at 4 MHz the antenna has a broad vertical lobe with a TOA of about 30° and a gain of 7 dBi. The lowest loop is placed 10 m above the ground, so that the vertical lobe is narrow with a TOA of 10° and a gain of 10 dBi at 30 MHz.

A single inverted cone of loops suffers from the disadvantage that the vertical radiation pattern at high frequencies contains grating lobes. (See above, "Multiple-Curtain Log-Periodic Arrays.") To reduce the level of the unwanted lobes and maximize gain, a second inverted cone of loops is installed inside the first. The upper loops of the two inverted cones are nearly coincident, and the vertical radiation pattern at the lower frequencies is therefore the same as that of a single cone. However, because the lowest loops of the inner cone are at a greater height than those of the outer cone,

the antenna behaves as two stacked loops at the higher frequencies. The stacking factor of the two loops modifies the vertical radiation pattern by suppressing the high-elevation grating lobes, thereby increasing the gain of the antenna.

Rotatable Log-Periodic Antenna

When a high-gain, steerable azimuthal beam is necessary, a rotatable LPA (RLPA) can be used. An example is illustrated in Fig. 26-12. This antenna is approximately 33 m high and has a boom length of about 33 m. Its operating frequency range is 4 to 30 MHz, its gain about 12 dBi, and its azimuthal beamwidth 60°. The antenna does not require a very large area for installation and provides complete azimuthal coverage. However, such antennas have major mechanical and electrical disadvantages. The major mechanical disadvantage is their complexity, resulting from the need to rotate a very large structure. These antennas require regular maintenance to ensure mechanical reliability and are prone to failure in harsh environments. The electrical disadvantage is that the antennas have constant physical height and, therefore, their electrical height increases with increasing frequency. As a result, grating lobes form at the higher frequencies, reducing gain in the principal lobe and introducing elevation nulls at TOAs required for communications. ¹⁶

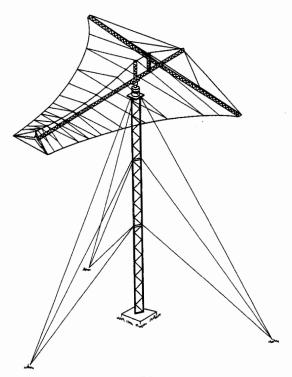


FIG. 26-12 Rotatable LPA.

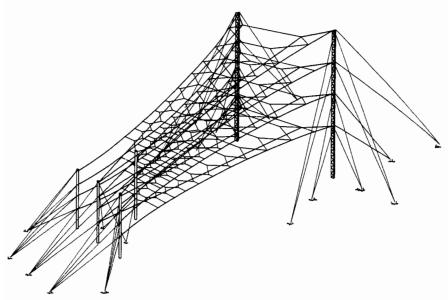


FIG. 26-13 Eight-curtain high-power LPA for HF broadcasting. (Courtesy of TCI.)

High-Power Log-Periodic Antenna

For most HF communication links, the transmitter power can be relatively low (usually 0.1 to 40 kW PEP) because high-gain receiving antennas and sophisticated receiving equipment are used at the other end of the circuit. However, for broadcasting much higher transmitter powers are necessary to provide an adequate signal for listeners using simple transistor receivers and low-gain antennas. As a result, transmitters with carrier powers between 100 and 500 kW are used, and the transmitting antenna must be designed to operate with the resulting high voltages and currents.

A high-power HLPA is useful for broadcast purposes because it has an extremely wide bandwidth and its power gain is not diminished by ground losses. In principle, a high-power HLPA can be designed to cover the whole HF band from 2 to 30 MHz. However, cost and land-area considerations require that the antenna size be minimized by selecting the highest possible low-frequency cutoff. A broadside array of horizontally stacked HLPA curtains can be slewed in azimuth electrically by setting up a phase difference between the stacks. If the electrical spacing between the radiation centers of the stacks is kept constant with frequency, the phase difference must also remain constant. Networks providing constant phase delay can be realized by using coupled transmission lines.

At the power levels used in HF broadcasting, the voltages and electric fields in an HLPA are very high. To minimize the radiator-tip voltages, which can be as high as 30 to 35 kV rms, the radiation Q of the dipoles (defined in Sec. 26-7) is reduced by constructing the dipoles in the form of a fat cylindrical cage of wires. A simpler technique, illustrated in Figs. 26-10 and 26-13, forms the wires into a sawtooth arrangement to increase their effective diameter. Large radial electric fields on the surface of the wires can initiate arcing and corona discharge, which can burn through

the wire and cause structural failure of the antenna curtain. These fields can be reduced to safe levels by using wires with the largest diameter acceptable on structural grounds. All insulators used in the antenna, and particularly those at the radiator tips, must be able to withstand high voltages and fields with a large factor of safety.

Well-designed two- and four-curtain HLPAs can handle between 100- and 250-kW carrier power with 100 percent amplitude modulation. Eight- and sixteen-curtain HLPAs can handle up to 500-kW carrier power. The VSWR of these antennas is less than 2:1 over their entire frequency range and is generally less than 1.5:1 at most frequencies. As can be seen from Fig. 26-13, HLPAs with more than four curtains are very complicated and therefore are difficult to install and are expensive.

26-4 VERTICALLY POLARIZED ANTENNAS

Vertically polarized antennas are useful when a broad target area must be covered with a wide azimuthal beamwidth. An omnidirectional radiation pattern is obtainable with a single monopole. A directional pattern with wide beamwidth is obtainable by using vertical log-periodics. However, these antennas have a vertical null which militates against short-distance sky-wave communications. A very important disadvantage of vertical antennas is that, unlike horizontally polarized antennas, their power gain is diminished by losses in the surrounding ground. To overcome these losses partially, high ground conductivity or large ground screens are necessary, particularly if low TOAs are required for long-range communications.

Conical Monopole and inverted Cone

Examples of the inverted cone and conical monopole are shown in Fig. 26-14a and b; their principal use is to provide omnidirectional coverage over a wide frequency band. The azimuthal pattern of these antennas is nearly circular at all frequencies, but the elevation pattern changes with frequency as shown in Fig. 4-14. The impedance bandwidth of the antennas is very large. The 22-m-high inverted cone illustrated in Fig. 26-14a has a VSWR of less than 2:1 over the entire 2- to 30-MHz range. The major disadvantage of this antenna is that the maximum radius of the cone is approximately equal to the height. The necessary support structure must consist of up to six nonconducting poles, which are usually expensive, and occupies a relatively large ground area.

The inverted-cone antenna can also be realized by using a single metallic support tower instead of the six nonconducting poles. The tower is placed along the cone axis on an insulated base. When designing the single-support antenna, great care must be taken to avoid internal resonances between the tower and the cone.

A more compact antenna, which also uses a single metallic mast and can be accommodated in a smaller ground area, is the conical monopole illustrated in Fig. 26-14b. The radiating structure comprises two cones, one inverted and one upright, connected at their bases. Here, the tower is grounded and the lower cone wires are insulated and fed against the ground. Midway up the tower the cone wires are connected to the tower to form an inductive loop. This acts as a built-in impedance-matching circuit, allowing the antenna to present a low VSWR when it is only 0.17λ tall. A

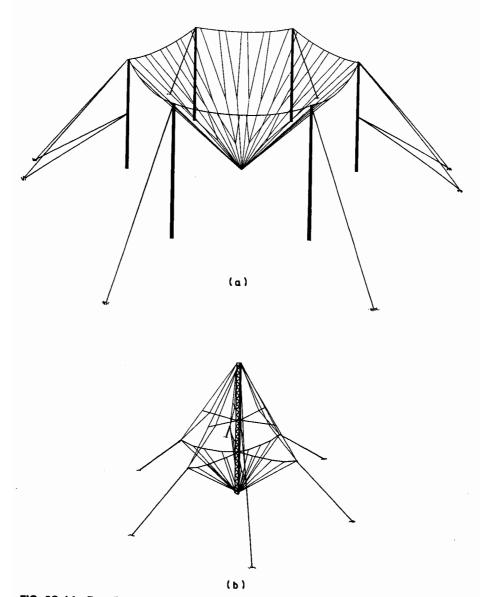


FIG. 26-14 Broadband monopole antennas. (a) Inverted cone. (b) Conical monopole. (Courtesy of TCI.)

conical monopole covering 2 to 14 MHz is 25 m high and has a maximum radius of 20 m.

All base-fed antennas usually require an impedance ground screen, which typically consists of 60 radials, each about $\lambda/4$ long at the lowest operating frequency.

Monopole Log-Periodic Antenna

At low frequencies in the HF band the height of a half-wave vertical dipole becomes undesirably large. Thus, for operation at the lower end of the HF band and in cases when directive gain is required, an LPA comprising quarter-wave monopoles operated over an impedance ground screen is a convenient antenna. A typical LPA covering 2 to 30 MHz is about 43 m tall and has a directive gain of 9 to 10 dBi and an azimuthal beamwidth of 140 to 180°.

Dipoie Log-Periodic Antenna

When greater tower height can be accommodated (81 m for a 2- to 30-MHz antenna), an LPA comprising half-wave dipoles can be used, as shown in Fig. 26-15. The larger vertical aperture yields a gain of 12 to 13 dBi, which is about 3 dB greater than that of a monopole LPA. In contrast to the requirements of the monopole LPA, an impedance ground screen is not essential to achieve an acceptable VSWR. To achieve higher power gain and lower TOAs, a long radiation-pattern ground screen is necessary.

Monopole-Dipole Hybrid Log-Periodic Antenna

In an LPA covering the 2- to 30-MHz HF band, mast height can be minimized by using monopoles for the 2- to 4-MHz radiators. Above 4 MHz, dipole radiators can

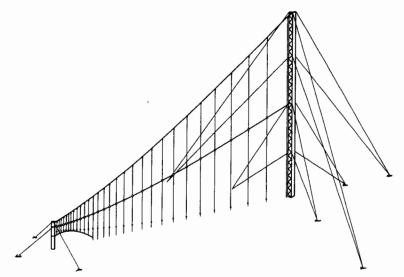


FIG. 26-15 Vertically polarized dipole LPA. (Courtesy of TCI.)

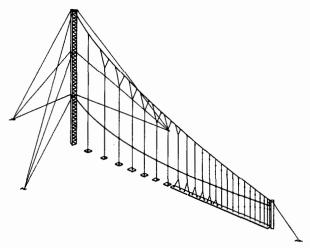


FIG. 26-16 Vertically polarized di-monopole hybrid LPA. (Courtesy of TCI.)

be used because they are fairly short and have more gain than the monopoles. A di-monopole¹⁷ hybrid LPA can be constructed (see Fig. 26-16) in which the low-frequency elements are monopoles, the high-frequency elements are dipoles, and the elements operating at intermediate frequencies are unbalanced dipoles in which the upper conductor is longer than the lower conductor. Lumped capacitors and inductors are used at the base of the lower conductor to equalize the resonant frequencies of the upper and lower radiators. The design of a di-monopole hybrid LPA must be done very carefully because unequal impedances between upper and lower radiators can cause unbalanced currents to flow along the balanced transposed feedline in the antenna. Such in-phase common-mode currents radiate overhead and can cause unwanted antenna resonances.

Extended-Aperture Log-Periodic Antenna

The principal advantage of a vertically polarized LPA is that it has very wide azimuthal beamwidth but high directivity. Its gain can be increased without decreasing its azimuthal beamwidth if the vertical aperture is extended by lengthening the radiators. However, if the radiator lengths are made longer than a half wavelength, there will be nulls in the current distribution along the active radiators which will produce undesirable radiation-pattern nulls and unacceptable variations in antenna impedance. Increased vertical aperture is effective only if steps are taken to maintain the current distribution characteristic of a half-wave dipole (or quarter-wave monopole) as the length of the radiator is increased. This can be achieved by use of the extendedaperture technique, 18 which is illustrated in Fig. 26-17 for the case of a single dipole. Capacitors are inserted in series with the dipole limbs so that the current distribution never goes to zero except at the radiator tips. An extended-aperture LPA using full-wave dipoles has about 2 to 3 dB more gain than a half-wave dipole LPA.

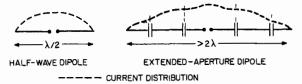


FIG. 26-17 Extended-aperture technique for eliminating current-distribution nulls on dipoles longer than $\lambda/2$. (After Ref. 18.)

Radiation-Pattern Ground Screens

The gain of a vertically polarized HF antenna is reduced and its TOA increased by the finite conductivity of the ground. To achieve maximum gain and the lowest possible TOA, a radiation-pattern ground screen extending several wavelengths in front of the antenna is necessary. The performance of a vertically polarized antenna depends on the linear dimensions of the ground screen and the conductivity of the ground. Practical ground screens are constructed by laying closely spaced wires on the earth. The wires of a ground screen must be dense enough so that the screen presents a very low resistive and reactive surface impedance. If a reactive impedance is presented, the radiation pattern is distorted because a quasi-trapped wave may be excited along the ground screen.¹⁹

A ground screen should not be buried more than a few centimeters beneath the earth, nor should it be allowed to be covered by snow. Burial or snow cover can com-

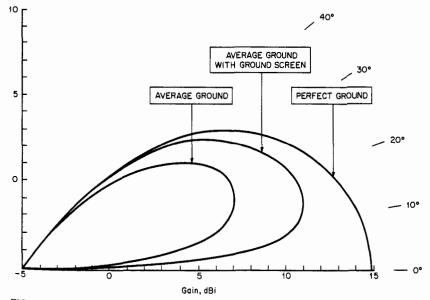


FIG. 26-18 Elevation pattern of a vertically polarized extended-aperture LPA at 10 MHz.

pletely mitigate the effectiveness of a ground screen and in some instances exacerbate the deleterious effects of the losses in the earth. There are no simple formulas for determining the radiation pattern of a vertical antenna with a ground screen. However, most of the available wire-antenna-analysis computer programs can calculate radiation patterns for antennas over lossy earth both with and without a polygonal ground screen of arbitrary size. Figure 26-18 shows the computed elevation pattern of an extended-aperture vertically polarized LPA (VLPA) over perfectly conducting ground and over ground of average conductivity, with and without a large ideal ground screen. Even with a large ideal ground screen there is a significant loss of gain owing to ground losses. Similar results are obtained for all vertically polarized antennas.

Impedance Ground Screens

For a monopole antenna, a ground screen is essential to obtain an input impedance giving an acceptable VSWR and to minimize conductive losses in the earth underneath the antenna. The input impedance of a vertical dipole is not affected by finite earth conductivity, so an impedance ground screen is not required. Impedance ground screens generally enclose an area extending no further than about $\lambda/4$ (at the lowest operating frequency) from the antenna.²⁰

26-5 OTHER TYPES OF COMMUNICATIONS ANTENNAS

Vertical Whip

The vertically polarized whip antenna is a monopole 2 to 3 m long and of small diameter. It is widely used because it is simple to construct and easy to erect on a vehicle. Because the whip has narrow impedance bandwidth, an adjustable matching unit is required to tune the whip at each frequency. The less expensive matching units are preset to several frequencies. More expensive units tune automatically. The power-handling capacity of a whip and matching unit is usually limited to 1 kW average and PEP.

The whip antenna can suffer from severely low radiation efficiencies at lower HF frequencies because its radiation resistance is very low compared with the loss resistances of the tuner, whip conductor, and ground. The whip ground is usually a vehicle, and the resulting radiation pattern is not precisely predictable but is usually well behaved enough for adequate communication.

Rhombic Antenna

In the past, the horizontally polarized rhombic antenna (see Sec. 11-3) was widely used for point-to-point communication links. It has now been almost completely superseded by the HLPA, which is smaller in size with equal or superior performance. The rhombic is a large traveling-wave antenna which is terminated at its far end by a resistive load. Radiation efficiency of a typical rhombic is 60 to 80 percent, compared with more than 95 percent for an HLPA. The rhombic behaves approximately like a matched transmission line, and this results in a nearly constant input impedance over a very wide bandwidth. However, the gain and radiation pattern vary significantly

with frequency, and this reduces the useful operational bandwidth to about 2:1 (one octave). The HF band covers a frequency range of up to 15:1, so three or four rhombics are required to give complete frequency coverage. In contrast, a single HLPA can be designed to cover the whole HF band.

Fan Dipole

A simple form of wideband transmitting antenna is a horizontal dipole in the form of a fan as illustrated in Fig. 26-19. This antenna is a broadband radiator based on the same principle as the inverted-cone monopole. With careful design it is possible to achieve a VSWR of less than 2.5:1 over the whole HF band from 2 to 30 MHz. Since the height above ground (25.9 m) is fixed, the vertical radiation pattern varies with frequency. At low frequencies there is a broad vertical lobe with a high TOA suitable for short-distance transmission. As the frequency increases, the TOA decreases and the antenna becomes suitable for transmission over longer distances. The azimuth radiation pattern at low frequencies and high elevation angles is nearly omnidirectional. This is advantageous when communication with a number of short-range targets spaced randomly in azimuthal bearing is required.

For transportable applications, it is possible to use a single-mast version (height, 12.2 m) of the fan dipole as illustrated in Fig. 26-20, which is closer to the ground than the conventional fan dipole. The lower height increases the negative mutual coupling to the ground, which results in decreased radiation resistance, particularly at low frequencies. To compensate for this, it is necessary to connect resistive loads between the ends of the fan and the ground. The resistive loading yields a low VSWR over the whole HF band but results in a loss of gain of 5 to 13 dB, the greatest loss occurring at the low frequencies.

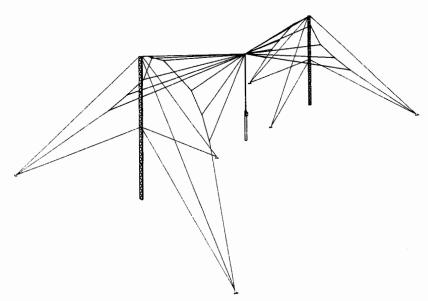


FIG. 26-19 Broadband fan dipole. (Courtesy of TCI.)

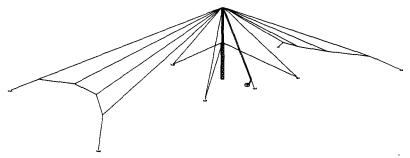


FIG. 26-20 Transportable fan dipole. (Courtesy of TCI.)

Transmitting Loop

When space is very restricted and an unobtrusive antenna is essential, it is possible to use a small-loop transmitting antenna. A small vertical loop in free space has radiation characteristics independent of frequency, and as is shown in Fig. 26-21 a, the azimuth radiation pattern becomes more circular with increasing elevation angle. Thus, unlike the whip and other monopole antennas, this antenna has no vertical null to militate against short-range communication. In practice, the loop must be mounted on the ground or possibly on the roof of a building. The performance of the free-space loop can be closely approximated by a half loop mounted on a conducting plane as shown in Fig. 26-21 b. The radiation resistance of the loop is proportional to A^2f^4 , where A

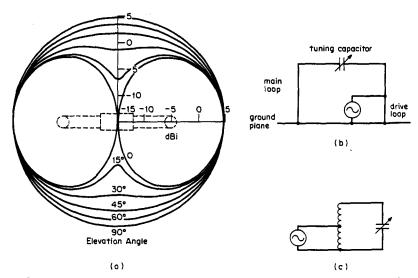


FIG. 26-21 Vertically polarized transmitting loop antenna. (a) Azimuth radiation patterns at different elevation angles. (b) Half loop mounted on ground plane. (c) Equivalent circuit of half loop on ground plane.

is the area of the loop and f is the frequency. For small loops, therefore, the radiation resistance is very low at low frequencies. The minimum acceptable size of the loop is determined by the need to achieve a bandwidth of around 2 kHz at the lowest operating frequency, which can be 3 MHz for many applications. This requirement can be met by a loop 1 m high and 2 m wide—a small and compact device. The loop has a narrow impedance bandwidth and must be tuned at each operating frequency, as illustrated in Fig. 26-21c. A variable vacuum capacitor tunes the main radiating loop to resonance. An autotransformer, comprising a small drive loop coupled into the main radiating loop, transforms the resulting resistance to a value that maintains a VSWR of less than 2:1 over a frequency band of 3 to 24 MHz. It is possible to do this tuning automatically, using, for example, a microprocessor-based system which (1) measures the transmitter frequency, (2) monitors the current in the drive and main loops, (3) sets the capacitor to an appropriate value, using a stepping motor, and (4) determines the capacitor's position by means of a variable resistor mounted on its shaft.

The small radiation resistance of the loop at low frequencies makes it inevitable that resistive losses cause a reduction in radiation efficiency. Losses are minimized by using a high-Q vacuum capacitor and by ensuring that the radio-frequency (RF) paths in the loop and ground screen have very high conductivity. At 3 MHz the radiation efficiency of a well-designed and carefully constructed loop will be about 5 percent. Because the radiation resistance of the loop increases with the fourth power of frequency but the resistive losses increase with the square root of frequency, efficiency rises rapidly with increasing frequency, achieving a value of about 50 percent at 10 MHz and 90 percent above 18 MHz.

26-6 HIGH-FREQUENCY RECEIVING ANTENNAS

For a passive linear antenna (one without nonlinear elements or unidirectional amplifiers) the gain, radiation pattern, and impedance are the same for transmission and reception. It is a consequence of the principle of reciprocity, which applies to all passive linear four-pole networks. However, the relative importance of these antenna parameters is different for transmission and reception. For transmission it is important to maximize field strength in the target area, so the antenna should be as efficient as possible. For reception the most important parameter is the signal-to-noise ratio (SNR) at the receiver output terminals, which obviously should be as large as possible. The SNR at the receiver output depends on the gain and mismatch losses of the antenna and feeder, the internal noise generated by the receiver, and the external atmospheric, human-made, and galactic noise levels. Because the external noise level at HF is often much larger than the internal noise levels in the receiver and antenna, it is possible in these instances to obtain acceptable SNR by using inefficient receiving antennas.

Noise Figure

For a simple analysis the receiver can be assumed to be linear, and the output SNR therefore equal to the input SNR. In calculating the output SNR, the signal and noise powers can therefore be referred to the receiver input and the available noise power

at the output of an HF receiver taken to be

$$n_{\text{out}} = \text{onf} \cdot kT_0 b \tag{26-9}$$

where n_{out} = available noise power, W

onf = operating noise figure

 $k = \text{Boltzmann's constant}, 1.38 \times 10^{-23} \text{ J/K}$

 T_0 = reference temperature, 288 K

b = effective noise bandwidth of receiver, Hz

The operating noise figure²² (or factor) is a power ratio which accounts for the total internal and external noise of the receiving system and is given by

onf =
$$f_e - 1 + f_a f_t f_r$$
 (26-10)

where f_{ϵ} = total external noise power divided by kT_0b

 f_a = antenna noise figure

 f_t = transmission-line noise figure

 f_r = receiver noise figure

The product $f_t f_r$ may be replaced by a single noise figure f_n of a generalized receiving system containing additional devices such as filters, preamplifiers, and power dividers and combiners. In the rest of this section, as is common practice, the decibel equivalent of these noise figures will be denoted by capital letters.

The external noise figure F_{ϵ} is the level of atmospheric, human-made, and galactic noise in a 1-Hz bandwidth in decibels above kT_0 , where $10 \log_{10} kT_0 = -204$ dBW. Atmospheric noise is generated by lightning discharges which produce enormous amounts of HF energy that propagate great distances. Human-made noise is produced by various kinds of electrical equipment such as motors, vehicular ignition systems, electric welders, and fluorescent lamps. Galactic noise is generated by extraterrestrial radio sources. F_{ϵ} can be determined from published noise maps²² or by direct measurement by using a calibrated receiver and antenna. Figure 26-22 shows a typical example of the frequency variation of atmospheric noise, which usually drops from a high value at low frequencies to a low value at the upper end of the HF band. Atmospheric noise-lével also varies with geographical location, season, and time of day. Human-made noise level depends on whether the receiving site is in an urban, suburban, or rural location; in urban areas it can equal or exceed the atmospheric noise level.

The receiver noise figure F_r is usually obtainable from the receiver's specifications table. The transmission-line noise figure F_t is the reciprocal of the attenuation, expressed in decibels. For systems with filters, preamplifiers, etc., the noise figure F_r can be determined by computing the noise figure for the equivalent cascaded network.

The antenna noise figure F_a is given by

$$F_a = D - G + L_M (26-11)$$

where D = directivity, dBi

G = gain, dBi

 $L_{M} = \text{mismatch loss} = 10 \log_{10} (1 - |\rho|^{2}), dB$

The mismatch loss is given in terms of the reflection coefficient ρ at the input terminals of the antenna, where $|\rho| = (VSWR - 1)/(VSWR + 1)$. The quantity D - G can be expressed in terms of the efficiency η by using the relation $D - G = -10 \log_{10} \eta$. The efficiency must include the resistive losses of both the antenna and the sur-

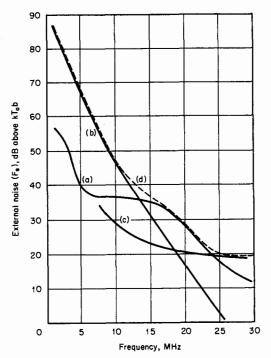


FIG. 26-22 Example of an external atmospheric and galactic noise figure. (a) Atmospheric daytime noise. (b) Atmospheric nighttime noise. (c) Galactic noise. (d) Worst noise condition.

rounding ground. For horizontally polarized antennas the ground losses are negligible. For vertical antennas ground losses may be significant, so they should be considered when there is no ground screen and earth conductivity is low.

Resistively loaded antennas, such as the small fan dipoles discussed in Sec. 26-5, usually have a VSWR of less than 2.5:1, so the mismatch loss is less than 1 dB. For these antennas the noise figure is determined primarily by the efficiency. For small nonresonant loop antennas, which will be discussed later, the mismatch loss is extremely large because the antenna has an extremely small input resistance and much larger reactance. For small loops both mismatch loss and low efficiency contribute to the noise figure. For small loops, monopoles, and dipoles the mismatch loss decreases by approximately 12-dB-per-octave increase in frequency.

Equation (26-10) has two important limiting cases. When $f_e \gg f_a f_b f_n$, the receiving system is said to be externally noise-limited because the external noise exceeds the internal noise. In this case the system performance cannot be improved by reducing antenna, feeder, or receiver noise figures. When $f_e \ll f_a f_b f_n$ the system is internally noise-limited, internal noise being greater than external noise. In this case system performance is improved by reducing the antenna or equipment noise figures.

In determining whether a receiving system is internally or externally noise-limited, it is important that actual external noise data be used. The values shown in Fig.

26-22 are for illustrative purposes only, actual variations being too extensive to display in one curve. In many geographical locations atmospheric and human-made noise levels are extremely low, and therefore receiving systems must have very low noise figures to avoid being internally noise-limited.

Signal-to-Noise Ratio

The SNR at the receiver output is the ratio s_{out}/n_{out} of the available signal and noise powers. The available signal power is given by

$$s_{\text{out}} = \frac{2.08e^2\lambda^2d10^{-15}}{\pi^2} \quad \text{W}$$
 (26-12)

where $e = \text{field strength of arriving signal, } \mu V/m$

d =antenna directivity as a power ratio

Dividing this by Eq. (26-9) and expressing the quantities in decibels gives the following equation for the SNR:

$$SNR = E + D - F - ONF - B + 97 dB$$
 (26-13)

where $E = 20 \log_{10} e$, $dB\mu$ (dB relative to $1\mu V/m$)

D = antenna directivity, dBi

 $F = 20 \log_{10} f (\text{in MHz})$

 $ONF = 10 \log_{10} (onf), dB$

 $B = 10 \log_{10} b \text{ (in Hz)}$

Practical Receiving Antennas

HF receiving antennas are divided into two classes. One class comprises antennas that are designed for transmission but are also used for reception. These antennas are very efficient, and their noise figures are often less than 3 dB, making them suitable for use at very quiet receiving sites. Full-sized vertically polarized antennas, when used for reception, do not require ground screens unless they are used in an emitter-locating system in which terrain variations must be neutralized by placing a metallic ground mesh under and in front of the antennas. The absence of a ground screen narrows the vertical beamwidth of the radiation pattern, thereby increasing directivity. However, ground losses reduce the gain by 5 to 10 dB and thus increase the antenna noise figure by the same amount. The resulting overall system noise level is nevertheless lower than most external noise levels, so a vertical antenna without a ground screen makes a highly suitable receiving antenna for many locations.

The second class of antennas consists of those specifically designed for reception. Again, because a high HF receiving-antenna noise figure is usually acceptable, a receive-only antenna can be inefficient and have high VSWR. Consequently, it can be small and, if necessary, be loaded resistively to improve its performance.

Typical acceptable values of antenna noise figure are given in the following illustrative analysis of a radioteletype receiving system. Assume that signal strength E is 34 dB μ (50 μ V/m) and antenna directivity is 5 dBi. The required SNR for moderate character error rate is 56 dB in a 1-Hz bandwidth. The receiver noise figure F_t is 13 dB, and feeder noise figure F_t is 3 dB, both reasonable values for HF devices. The maximum allowable ONF is obtained by substituting E_t , D_t , and SNR in Eq. (26-13). The corresponding allowable antenna noise figure F_d is obtained by substituting the

power ratios onf, f_e , f_r , and f_t into Eq. (26-10). In this example the external noise level F_e is assumed to be given by the dotted curve in Fig. 26-22. The accompanying table summarizes the results for several frequencies:

f, MHz	ONF, dB	F₀, dB	<i>F₄</i> , dB
2	74	80	
5	66	66	
10	60	46	44
15	56	37	40
20	54	29	38
30	50	19	34

Below 5 MHz the required SNR will not be obtained because the external noise level is too high. This can be overcome only by moving to a quieter site; improving equipment noise figures has no effect. Above 5 MHz the external noise level is smaller, and the required SNR can be obtained by using an antenna with a maximum noise figure at each frequency as given in the table. If the antenna VSWR is low so that the mismatch loss can be neglected, allowable antenna efficiency ranges from 0.004 percent at 10 MHz to 0.04 percent at 30 MHz.

Receiving Loops

A practical antenna having a noise figure near the upper limit allowable for most situations is the small vertical balanced loop. A typical loop is about 1.5 m in diameter and is mounted about 2 m above the ground on either fixed posts or transportable tripods. The antenna is usually made from a large-diameter metallic tube, which also serves to shield the feeder that runs through the tube to the feed point. The vertical radiation pattern of the loop has good response at both low and high TOAs, making the antenna suitable for both long- and short-distance reception of sky-wave signals. The loop also responds well to ground waves.

The noise figure of the loop depends strongly on its area and the operating frequency. A loop of 1.5-m diameter has a noise figure of about 50 dB at 2 MHz and 20 dB at 30 MHz. The noise figure can be reduced by making the area of the loop larger. However, if the loop perimeter is about a wavelength long, the loop will resonate and the radiation pattern will exhibit irregularities. These can be avoided in large loops by feeding the loop at several points.

A number of loops can be arrayed to provide a variety of directional radiation patterns. In most arrangements of small loops, mutual coupling between the loops is negligible and simple array theory can be used to predict radiation-pattern shape. Beams are formed by bringing the coaxial cable from each loop into a beam-forming unit located near the antenna. The most common arrangement places eight loops in an end-fire array with spacing between loops of 4 m, as shown in Fig. 26-23. The array can be made bidirectional by splitting the signal from each loop two ways and feeding each half into a separate beam former. Four such bidirectional arrays can be arranged in a circular rosette which provides eight independent beams covering 360° in azimuth.

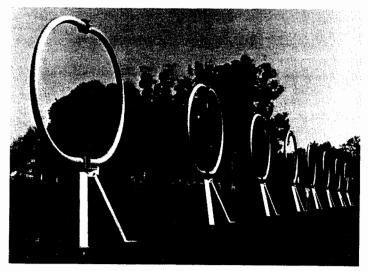


FIG. 26-23 End-fire array of eight receiving loops. (Courtesy of TCI.)

Active Antennas

Many receiving antennas, including loop arrays, are made into active antennas by interposing a broadband low-noise amplifier between the output of the antenna or its beam former and the feeder line to the receiver. For some antennas the amplifier can improve the impedance match and thus reduce mismatch loss and antenna noise figure. However, for electrically small antennas little improvement in noise figure is possible with a practical amplifier.²³ The amplifier also sets the antenna-system noise figure at the point where the amplifier is placed. The amplifier has a beneficial effect in this case only if its noise figure (usually 1 to 5 dB) is less than the feeder noise figure and its gain (usually 10 to 30 dB) is much higher. The amplifier can have a deleterious effect on receiving-system performance if high ambient signal levels cause it to produce spurious intermodulation products. These are likely to occur if there are strong medium-frequency (MF), HF, or very-high-frequency (VHF) signals from nearby transmitting antennas. It is a simple matter to filter out the MF and VHF signals by using, respectively, high- and low-pass filters ahead of the amplifier. Unwanted HF signals must be rejected by using notch filters so as not to impair the usefulness of the antenna in the HF receiving system.

The availability of cheap microprocessors has made it possible to use active antenna elements as the basis of adaptive-antenna arrays (see Chap. 22). In an adaptive system the amplitudes and phases of the signals from a multielement array are adjusted continually to give a radiation pattern maximizing the wanted signal and minimizing interfering cochannel and adjacent-channel signals. Optimum weightings of component signals must be determined from a careful study of the actual signals with which the antenna must contend. These studies are not straightforward, and designing a suitable algorithm is difficult in many cases.

Circular Arrays

Arrays of circularly disposed antenna elements are used in monitoring or emitter-locating systems (see Chap. 39). In these applications there is quite often a need to receive signals from all azimuth angles and to be able to connect a number of receivers to any of a number of beams. Antennas of this type must operate over a large part of the HF band and must have highly predictable radiation patterns with low sidelobe levels. It is often advantageous to make each element of the array an LPA. Vertical LPAs should be used if the array must respond to ground waves or to low-TOA sky waves. Horizontal LPAs, placed close to ground, should be used if high-TOA sky-wave signals from short distances are to be received.

A typical array comprises 18 to 36 elements. The output of each element is fed into a beam former, containing suitable delay lines and power splitters, which forms a narrow azimuthal beam. It is possible to generate N beams simultaneously in an N-element array by splitting the power from each element N ways. The N beams are uniformly spaced around the circle. By using multicouplers, each beam can be accessed by several receivers.

In arrays of LPAs it is best to point the elements inward so that their direction of maximum sensitivity is toward the array center. This configuration keeps the electrical diameter of the array nearly constant, thereby making the azimuthal beamwidths nearly independent of frequency and eliminating unwanted azimuthal grating lobes. The disadvantage of the inward-looking array is that each element "fires through" those opposite, and this complicates the calculation of the radiation pattern.

26-7 BROADBAND DIPOLE CURTAIN ARRAYS

Broadband dipole curtain arrays are used for high-power (100- to 500-kW) HF ionospheric broadcasting. These antennas consist of square or rectangular arrays of dipoles, usually a half wavelength long, mounted in front of a reflecting screen, as shown in Fig. 26-24. Dipole arrays have many excellent performance characteristics, such as independent selectability of vertical and horizontal patterns, high power gain, slewability of beam in azimuth or elevation, wide impedance bandwidth, low VSWR, and high power-handling capacity, which have made them virtually the standard antenna at short-wave broadcasting stations.

Standard Nomenclature

Dipole curtain arrays are described by the internationally agreed nomenclature HRRS m/n/h.

where H denotes horizontal polarization

R denotes a reflector curtain

R (if not omitted) denotes that the direction of radiation is reversible

S (if not omitted) denotes that the beam is slewable

m is the width of the horizontal aperture in half wavelengths at the design frequency

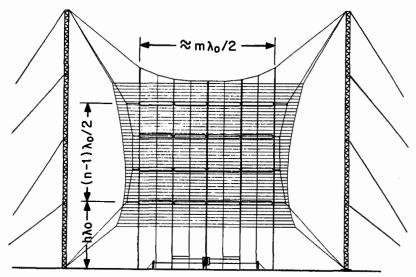


FIG. 26-24 Basic HF dipole curtain array. (Antenna shown is designated HRS 4/4/h.)

n is the number of the dipoles in a vertical stack

h is the height of the lowest dipole above ground, in wavelengths at the design frequency

The design frequency f_0 is approximately equal to $\frac{1}{2}(f_1 + f_2)$, where f_1 and f_2 are the lower and upper frequency limits; λ_0 is the corresponding design wavelength. In dipole arrays which use half-wave dipoles, the width parameter m is the number of dipoles in a horizontal row.

Radiation Pattern and Gain

The TOA and first null at frequency f depend on the average height of the dipoles in the vertical stack and are given approximately by

$$TOA = sin^{-1} (f_0 \lambda_0 / 4f H_{avg})$$
 (26-14)

Null =
$$\sin^{-1} (f_0 \lambda_0 / 2f H_{avg})$$
 (26-15)

where $H_{avg} = (H_1 + H_2 + \cdots + H_n)/n$ and H_1, H_2, \dots, H_n are the physical heights above ground of the *n* dipoles in the stack. The TOAs at f_0 are given for several configurations in Table 26-1. The lower and upper -3-dB points are located at approximately one-half and three-halves the TOA, respectively. The level of the unwanted minor elevation lobes is determined by the number of dipoles in the stack and their spacing.

The azimuthal half-power beamwidth (HPBW) depends primarily on the width of the array but also depends weakly on the TOA. The beamwidth at f_0 is given in Table 26-2. Beamwidth at frequency f is obtained approximately by multiplying the value in this table by f_0/f . Dipole arrays with adjustable horizontal beamwidth have been

TABLE 26-1 Takeoff Angle of Dipole Array with Reflecting Screen

Number of elements in vertical stack n,	Height above ground of lowest element in wavelengths, h			
half-wavelength spacing	0.25	0.5	0.75	1.0
. 1	45**	29 •	19*	15 and 48°†
2	22.	17.	14.	11.
3	15°	12.	10*	9.
4	11*	10.	8.	7*
5	9.	8.	7*	6.
6	7*	7.	6.	5.

^{*90 *} without reflector.

constructed which use an RF switching system to excite one or more pairs of vertical stacks.^{23a}

The gain at f_0 of an array of half-wave dipoles is given in Table 26-3. The approximate gain at frequencies different from f_0 can be obtained by adding 20 log (f/f_0) to the values in Table 26-3.²⁴

Slewing

Early forms of dipole arrays used full-wave dipoles. These antennas contained a very-narrow-bandwidth feed system and thin dipoles, so they were capable of operating only in one or two broadcast bands. The azimuthal beam of the antenna was slewed by using a tapped feeding arrangement. This sets up a phase difference between the two halves of the array, which slews the beam up to $\pm 10^\circ$ in azimuth. The slew angle is limited to a small value because the dipole centers are separated by one wavelength. If greater slew angles are attempted, the horizontal pattern contains large secondary lobes which reduce gain by up to 3 dB and may interfere with cochannel transmissions.

TABLE 26-2 Horizontal Beamwidth of Dipole Array*

Number of elements in vertical stack <i>n</i> , half-wavelength		ber of half- ments wid	
spacing	1	2	4
1	76°	54°	26°
2	74°	50°	24°
3	74°	49°	24°
4	73°	49°	24°
6	73°	49°	24°

^{*}Between half-power points.

[†]Two lobes present.

TABLE 26-3 Gain in dBi of Dipole Array with Perfect Reflecting Screen

Number of				Numb	Number of half-wave elements wide, m	If-wave	e elem	ents wi	de, m			
vertical stack		-				~				4		
n, half- wavelength		_	leight &	above g	leight above ground of lowest element i	f lowe	st elem	ent in v	vavelen	gths, h		
spacing	0.25	0.50	0.75 1.0	1.0	0.25	0.50	0.75	1.0	0.25	52	0.75	1.0
-	12.5	13.1	13.9	13.4	13.5	14.3	15.1	14.6	191	17.1	17.8	17.4
7	13.9	14.9	15.5	15.7	15.3	16.4	16.9	17.1	18.1	19.2	19.7	100
6	15.5	16.3	16.8	17.1	17.0	17.8	18.3	18.6	19.8	20.6	7.7	21.5
4	9.91	17.3	17.8	18.1	18.1	18.8	19.3	19.6	20.9	21.6	22.1	22.4
9	18.2	18.7	19.2	19.5	19.8	20.3	20.7	21.0	22.6	23.1	23.6	23.9

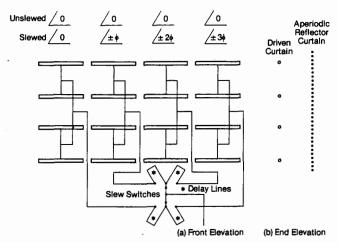


FIG. 26-25 Slewing system and corporate feed of a broadband HRS 4/4/h dipole array. Dipole length = $0.46 \ \lambda_0$, dipole spacing = $0.50 \ \lambda_0$ center to center, and screen-to-dipole spacing = $0.25 \ \lambda_0$.

To achieve larger slew angles it is necessary to reduce the horizontal spacing between the dipole stacks. In these arrays the dipole length is slightly less than $\lambda_0/2$, and the spacing between the stacks is $\lambda_0/2$. For these antennas the three-position slewing system shown in Fig. 26-25 enables slew angles to be as large as $\pm 30^\circ$. More than three slew positions can be obtained by increasing the number of switch positions and delay lines. Slewing systems with five positions are in common use.

Dipole arrays also can be slewed vertically to change the TOA of the radiation pattern and therefore the distance to the reception area. Vertical slewing is accomplished by altering the excitation of the dipoles in each vertical stack using an RF switching system which is separate from that used for horizontal slewing. Vertical and horizontal slewing can be done simultaneously.^{23a}

Impedance Bandwidth

The VSWR of a high-power broadband dipole array must be low for two important reasons. First, the voltages on the antenna and feeder lines become excessive if the VSWR is too high. Second, although most modern high-power HF transmitters will accept a VSWR of 2:1, the feeder line and switching systems introduce discontinuities so that the antenna itself must usually have a VSWR of less than 1.6:1 or 1.5:1. Low VSWR requires that the input impedance of the antenna must remain substantially constant over its entire frequency range. The bandwidth of a dipole array depends on the inherent bandwidth of the dipoles, the bandwidth of the interdipole feeder system, and the type of reflector placed behind the dipole array.

The inherent dipole bandwidth, by analogy with simple resistance-inductance-capacitance (RLC) resonant circuits, can be characterized by a radiation $Q = f_R/\Delta f$, where f_R is the resonant frequency of the dipole and Δf is the bandwidth between the frequencies at which dipole resistance and reactance are equal. In the broadband

dipole array, a very low Q of about 2 is achieved by making the dipole fat. The thin dipoles used in early arrays have Q's of about 10.

The feed system which interconnects the dipoles is made broadband by constructing it in the form of a *corporate feed*, as shown in Fig. 26-26. Wide-bandwidth transmission-line transformers, often of the optimal Chebyshev type, are used whenever impedance transformations are necessary.²⁵

Early dipole arrays used parasitic dipoles in the reflector curtain. Such antennas have very narrow bandwidth because the parasites act as reflectors over only a small range of frequencies, a phenomenon familiar to designers and users of Yagi-Uda arrays. Broadband dipole arrays use an aperiodic reflecting screen consisting of closely spaced horizontal wires placed about $0.25\lambda_0$ behind the dipoles.

A well-designed broadband dipole array has a VSWR of 1.5:1 or less in its operating bands. For some arrays and slews, mutual impedances between dipoles cause some dipoles to exhibit a negative driving-point resistance. This causes large currents to circulate in the dipole feed system over narrow ranges of frequency. Large circulating currents also produce high voltages in parts of the array and rapid changes in antenna input impedance which are often accompanied by high VSWRs. Arrays must be designed to eliminate these circulating-current resonances, if possible, or move them to frequencies outside the operating bands.

Practical Considerations

The design of modern dipole arrays is greatly facilitated by the use of comprehensive computer programs which enable the current distribution on the entire array to be analyzed.

To achieve low dipole Q, the half-wave dipoles are constructed as fat multiple-wire cages which are either flat, rectangular boxes or cylinders. The dipoles are usually "folded" to step up their impedance to a more useful level and provide additional impedance compensation. A folded dipole operates simultaneously in two modes. The radiating antenna mode, or unbalanced mode, depends only on the length and equivalent diameter of the dipole cage. The nonradiating transmission-line, or balanced, mode describes the currents which flow in a loop around the dipole and through the familiar short circuits at the end of the folded dipole. The impedance variations of the two modes tend to cancel, so the transmission-line mode can be used to compensate and tune the antenna mode.

This compensating effect is maximized by moving the position of the foldeddipole short circuit away from the end of the dipole and toward the feed point. The optimum position can be determined in a straightforward manner by using an antenna-analysis computer program.

The driving-point impedance of each folded dipole is about 600Ω when mutual impedances from other dipoles are included. This allows the impedance levels in the branch feeder to be in the range 300 to 600Ω , which is easy to realize in practice.

HRS 4/4 arrays can be designed to have a power-handling capacity of 750 kW average and 4000 kW PEP, which is large enough to accommodate two fully modulated 250-kW transmitters fed into the antenna simultaneously by using a diplexer. HRS 4/6/h arrays can be designed to handle the power of two diplexed 500-kW transmitters. Smaller dipole arrays, such as HR 2/2, can handle up to 750 kW average and

2000 kW PEP, corresponding to the power output of a fully modulated 500-kW transmitter. The wire diameters in the dipole array must be large enough to carry the high currents which flow and to prevent corona discharge. Insulators must be carefully chosen to withstand voltages of up to 45 kV rms, which can occur in the high-voltage points in the antenna.

The one-octave bandwidth of a dipole array allows three such antennas, 6/7/9/11, 9/11/13/15/17, and 13/15/17/19/21/26 MHz, to cover the whole international broadcast spectrum, with multiple-antenna coverage of many of the bands.

26-8 SITING CRITERIA FOR HIGH-FREQUENCY ANTENNAS

In the preceding sections it has been assumed that the antenna is mounted over a smooth, level ground plane of infinite extent. However, an actual antenna site is seldom smooth and level, and sites which approximate ideal conditions usually do so only over a limited area. In addition, the effects of co-sited antennas and of natural or artificial obstructions can result in degradation of antenna performance. This section assesses the effects of imperfect sites following closely Refs. 26 and 27, and presents practical criteria for obtaining acceptable performance.

Fresnel Zone and Formation of Antenna Beam

The main lobe of a transmitting or receiving antenna (the following discussion applies to both) is formed by the interaction of the direct radiation of the antenna and the reflected radiation from the ground plane. Reflections occurring near the antenna are of greater importance than those occurring far away. With a directional antenna, radiation at or near boresight angles is more important than that occurring at azimuth angles away from boresight. From these facts, it follows that there is an elliptically shaped area (with the major axis in the direction of the main lobe, as shown in Fig. 26-26) in which the ground must be level and smooth if the first lobe is to be formed without appreciable distortion.

From simple geometrical ray theory it is clear that as the TOA is decreased, the lengths of the major and minor axes of the elliptical area increase. The curvature of the earth also affects the size of the axes, but it can be ignored if the TOA is more than 3°.

The ellipse dimensions are different for vertical and horizontal polarization and in the former case are difficult to evaluate. Fortunately, the dimensions for horizontal polarization, which are easy to evaluate, give a reasonable approximation for the vertically polarized case. The ellipse dimensions correspond to the first Fresnel zone, which is the region in front of the antenna in which direct and reflected radiation of plane waves differ in phase by 180° or less. For horizontal polarization, if the antenna has a TOA of ψ_0 , the radiation will appear to come from a height above ground of

$$h = \lambda/4 \sin \psi_0 \tag{26-16}$$

The distance from this radiation point to the near and far edges of the first Fresnel

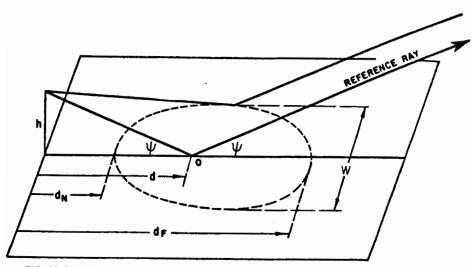


FiG. 26-26 Geometry of first Fresnel zone.

zone, denoted by d_N and d_F respectively, are given by

$$d_N = \frac{h}{\tan \psi_0} \left(3 - \frac{2\sqrt{2}}{\cos \psi_0} \right)$$
 (26-17)

$$d_F = \frac{h}{\tan \psi_0} \left(3 + \frac{2\sqrt{2}}{\cos \psi_0} \right)$$
 (26-18)

The maximum width of the Fresnel ellipse is

$$w = 4\sqrt{2}h = 5.66h \tag{26-19}$$

Equations (26-16) to (26-19) may be used to calculate a very conservative estimate of the area of flat, unobstructed land required in front of a directive antenna to ensure that the main lobe is fully formed. For very low TOA the Fresnel zone may extend for several kilometers, and it will not usually be possible to contain the zone within the boundaries of the antenna site. If the size of the controlled area is to be reduced, it is possible to limit it to the region in which the phase difference between direct and reflected radiation is 90° or less. In this case, there may be a loss of gain of up to 3 dB, but the dimensions of the ellipse will be reduced as follows:

 d_F may be reduced to 0.6 times the full value. d_N may be increased to 1.6 times the full value.

w may be reduced to 0.7 times the full value.

For antennas with large vertical apertures, such as dipole curtain arrays, the planewave assumption used to derive Eqs. (26-16) to (26-19) is not strictly true. The phase variation across the vertical aperture for such antennas causes the Fresnel zone to shrink so that the reflection zone for low TOAs may extend only up to a few hundred meters in front of the antenna, rather than kilometers.

Roughness in First Fresnel Zone

In the zone with dimensions given in Eqs. (26-16) to (26-19), the main lobe is approximately fully formed provided the ground is flat and smooth. However, if the ground is rough or has natural or artificial obstructions or depressions, reflection will not be specular. The reflected wave will be scattered, and there will be a loss of gain and distortion of the beam. Rayleigh's criterion indicates that the transition between specular and scattered reflection occurs when the maximum height H of deviations above and below the average terrain profile does exceed

$$H = \lambda_0/16 \sin \psi_0 = h/4 \tag{26-20}$$

This criterion may be relaxed if additional degradation in performance is acceptable. The relaxed criteria are based on the reasonable assumption that the permissible size of the obstruction may increase with distance from the antenna. It is usual to divide the first Fresnel zone into three regions, within which the heights of obstructions and depths of depressions should not exceed the values in the accompanying table.

Limit of departure from average smooth terrain	Region of first Fresnel zone
H/4	d_N to 0.2 d_F
H/2	$0.2 d_F$ to $0.6 d_F$
H	$0.6 d_F$ to $1.0 d_F$

It is difficult to predict with precision the degradation that occurs when the above criteria are applied, partly because the shapes of the obstructions have been ignored. However, it is reasonable to expect gain losses of several decibels. These criteria apply to cases in which the entire first Fresnel zone is rough. When a major portion of it is smooth, somewhat larger obstacles can be tolerated if they do not cover more than 5 to 10 percent of the zone. Caution must be exercised, however, when compromises in controlled-area size and roughness are made simultaneously because gain reductions may then become large.

Horizon Obstructions

Obstructions beyond the first Fresnel zone at distance $D_0 \gg d_F$ can reduce radiation at low angles even if the first Fresnel zone is perfectly smooth.²⁸ If the height of the obstruction is H_0 , antenna performance will not be noticeably degraded if the angle subtended by the obstruction as viewed from the antenna, $\psi_{\text{obs}} = \tan^{-1} (H_0/D_0)$, is less than 0.5 times the lower half-power point of the antenna elevation pattern. For TOAs of less than 30°, this criterion is given by $\psi_{\text{obs}} \leq \psi_0/4$.

Terrain Slope

If the ground at an antenna site slopes down in the direction of radiation by an angle b, the TOA is decreased from ψ_0 (the value for a flat site) to $\psi_0 - b$. Conversely, if

the ground slopes up in the direction of radiation, the TOA becomes $\psi_0 + b$. Fresnelzone theory can be applied to sloping sites by using the following modified antenna height factor:

$$h_{\text{slope}} = \lambda/4 \sin \left(\psi_0 \pm b \right) \tag{26-21}$$

in Eqs. (26-16) to (26-19). The + sign is used for upward slopes; the - sign, for downward slopes.

Ground Conductivity

For vertically polarized antennas, high ground conductivity is important for the effective operation of transmitting antennas, as explained in Sec. 26-2. Vertical transmitting antennas mounted very near seawater, which has a high conductivity of 4 S/m, do not require ground screens for radiation-pattern enhancement. For most types of soil, conductivity is significantly smaller than this value, so metallic ground screens are necessary. For horizontally polarized antennas, good ground conductivity is not important unless the TOA is very high, as explained in Sec. 26-2.

Coupling between Co-Sited Antennas

When transmitting, an antenna transfers some of its radiated energy to any other antenna in its vicinity, and this transferred energy may affect the performance of the other antenna. Antenna coupling is defined as the ratio of the power delivered into a matched load terminating the other antenna (called for convenience the receiving antenna) and the input power to the transmitting antenna:

$$C = 10 \log_{10} (P_r/P_t)$$
 dB (26-22)

where P_r = power dissipated in matched load terminating the receiving antenna P_t = input power to transmitting antenna

Coupling can be calculated accurately by solving the fundamental electromagnetic equations for the several antennas, using a comprehensive antenna-analysis computer program. However, good approximate coupling values can be obtained from two simple formulas, which assume that the antennas are separated by at least one wavelength λ . The magnitude of the coupling depends on the polarization of the antennas. For vertically polarized antennas the coupling factor is

$$C_v = 20 \log_{10} (\lambda/8\pi d) + G_t + G_r$$
 dB (26-23)

where d = spacing between antennas

 $G_t = gain of transmitting antenna, dBi$

 $G_r = gain of receiving antenna, dBi$

 G_t and G_r are the gains of the two antennas in the directions toward each other. The formula neglects ground loss, which is generally negligible when d is less than a few kilometers. For horizontal polarization the coupling factor is

$$C_h = 20 \log_{10} \left[\frac{\lambda \sin (\pi L/\lambda)}{8\pi d} \right] + G_t + G_r \quad dB$$
 (26-24)

where
$$L = [(H_t + H_r)^2 + d^2]^{1/2} - [(H_t - H_r)^2 + d^2]^{1/2}$$

 $H_t = \lambda/4 \sin \psi_t$
 $H_t = \lambda/4 \sin \psi_r$

 ψ_t and ψ_r are the TOAs of the transmitting and receiving antennas. λ , d, G_t , and G_r are defined in Eq. (26-23), except that G_t and G_r are the values at the TOAs ψ_t and ψ_r . For large values of d, C_h decreases by 12 dB each time that d is doubled.

Coupling between antennas can cause a number of effects, and one or more of the following may be relevant in a particular case.

Intermodulation If both antennas are transmitting, the energy coupled by one into the other may give rise to intermodulation products in the transmitter connected to the *receiving* antenna. The amount of coupling that can be tolerated depends on the characteristics of the transmitter, but typical values are -20 to -25 dB.

VSWR When energy from another antenna is coupled into a transmitting antenna, the VSWR presented to the transmitter will be changed because the apparent reflected power will be altered by the incoming energy. The reflection coefficient of the receiving antenna, ρ' , has a maximum magnitude given by

$$\rho' = \rho + (C_r P_t / P_r) \tag{26-25}$$

where ρ = reflection coefficient of *receiving* antenna in absence of the other transmitter, as defined after Eq. (26-11)

 C_r = coupling factor between antennas expressed as a power ratio P_t and P_r are the powers of the transmitters connected to the *transmitting* and *receiving* antennas. The apparent VSWR, in the worst case, is given by $V = (1 + \rho')/(1 - \rho')$.

Radiation-Pattern Distortion Some of the power transferred from the transmitting antenna to the receiving antenna will be reradiated and may cause distortion of the transmitting antenna's radiation pattern. The amount of power reradiated depends on the terminating impedance of the receiving transmitter, which is the value presented by its output stage. In the worst case this power can be up to 4 times the coupled power, which is the power radiated by the transmitting antenna multiplied by the coupling factor expressed as a power ratio. However, in practice the reradiated power will seldom be this large, and it is reasonable to assume that it will be equal to the coupled power. The reradiated energy changes the gain of the transmitting antenna by the following approximate amount

$$\Delta G = \pm 20 \log_{10} \left[1 + (C_r g_r / g_t)^{1/2} \right]$$
 dB (26-26)

where g_{rr} g_t = maximum gains of transmitting and receiving antennas expressed as power ratios.

This formula gives only the minima and maxima of the pattern perturbation. The detailed shape of the perturbed pattern and the locations of the azimuth angles at which the minima and maxima occur depend on the phase of the reflected energy and the relative positions of the antennas; they are difficult to calculate approximately.

Side-by-Side Antennas Horizontally polarized antennas with directive radiation patterns can be placed side by side, often using common towers, with a coupling factor

of less than -20 dB being achieved. Equations (26-23) and (26-24) do not apply in this situation because the antennas are too close. Coupling must be calculated by using a comprehensive antenna-analysis computer program.

26-9 RECENT DEVELOPMENTS

Multimode Spiral Antennas

A major problem at many HF communications stations is a lack of land available for the required number of transmitting antennas. To help solve this problem, multimode antennas have been developed which permit several HF transmitters to feed one antenna simultaneously and provide good isolation between the transmitters. A commonly used structure for such an antenna is a four-arm spiral as illustrated in Fig. 26-27. This antenna is usually between 24 and 37 m in height and occupies a diameter of between 69 and 113 m. The antenna operates from 2 to 30 MHz and has a directive gain of approximately 7 dBi. Smaller versions of this type of antenna are used for rooftop or transportable applications. These smaller antennas generally use resistive loading to achieve acceptable VSWR values so that their radiation efficiency and power gain are smaller than those of full-sized spiral antennas.

The four-arm spiral can be excited in four independent normal modes, three of which are balanced and one of which is unbalanced. The balanced modes are horizontally polarized and essentially omniazimuthal at all elevation angles. The unbalanced mode is vertically polarized and also omniazimuthal. (See Chap. 14 and Ref. 29 for theory of multiarm spirals.) Orthogonality of the normal modes theoretically provides perfect isolation between the transmitters; however, in actual practice, values of 20 to 35 dB are achieved.

The most common feed system for the multimode spiral excites the three balanced normal modes. Two of these modes radiate energy directly overhead, and the third mode

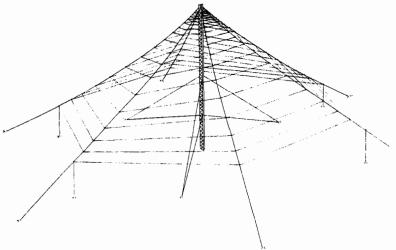


FIG. 26-27 Multimode spiral antenna. (Courtesy of TCI.)

has a null at the zenith. The configuration shown in Fig. 26-27 is optimized to provide low TOA at higher frequencies and high TOA at lower frequencies, the optimal pattern for most HF communications circuits (see Sec. 26-3, "Omnidirectional Log-Periodic Array with Optimum Vertical Radiation Pattern"). Operation with multiple transmitters requires that the antenna be equipped with a combination of hybrid and balun transformers which provide the proper connections between the transmitters and the four terminals of the spirals as well as adequate isolation between transmitters. The transformers, which may be combined into one unit, are located at the feed point, which is at the apex of the spiral near the top of the tower.

To ensure that the azimuthal pattern of the antenna is nearly circular, it is important that the antenna be excited in the normal modes of the spirals so that each transmitter produces currents in only one active region. Some feeding schemes excite mixtures of the normal modes, which produce multiple active regions, causing the patterns to be distorted and to have deep nulls in the azimuthal pattern which change with frequency.

Some multimode spiral antennas are inverted with respect to the configuration shown in Fig. 26-27, having the apex located near the ground. This arrangement produces TOAs which are nearly constant with frequency. Other configurations of multimode spirals also excite the fourth unbalanced normal mode, in which the tower and antenna are excited as a vertical radiator. This mode typically has high VSWR, and its gain is low because of the vertical polarization of the radiation.

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VHF and UHF Communication Antennas

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27-1 Introduction 27-2

27-2 System-Planning Objectives 27-2
Reliability 27-2
Choice of Polarization 27-5
Meeting Cost Objectives 27-6

27-3 Antennas for Point-to-Point Links 27-6

27-4 Base-Station Antennas 27-13

27-5 Mobile Antennas 27-20

27-6 System Considerations 27-22

27-1 INTRODUCTION

The very-high-frequency (VHF) and ultrahigh-frequency (UHF) bands are used for private and public-access services carrying speech, data, and facsimile information. The ends of a link may be installed at fixed locations or in vehicles (including ships and aircraft) or may be carried in an operator's hand. The length of a link may vary from a few tens of meters up to the maximum over which reliable communication can be obtained. This wide variety of applications generates a need for many different types of antennas. In this chapter, we examine the selection of antennas to perform various tasks, together with aspects of reliability, siting, and economics.

27-2 SYSTEM-PLANNING OBJECTIVES

The design of antennas for a radio link must provide an adequate signal-to-noise ratio at the receiver. The necessary signal-to-noise ratio will depend on the nature of the information to be transmitted and the grade of service which is required. A power budget must be drawn up to determine the total antenna gain and input power needed in the system. The antenna engineer must decide how the necessary gain can be obtained and how it should be divided between the two ends of the link. In many point-to-point applications the most economical design is obtained by using transmitting and receiving antennas of equal gain. Mobile or portable stations do not generally allow the use of high-gain antennas, so as much gain as possible must be obtained from the base-station antenna.

The electromagnetic spectrum is a limited resource, and its use is controlled by restricting the field strength which may be laid down outside the area where communication is required. This often implies a limitation on the permitted effective radiated power (ERP) both inside and outside the main-beam direction of the transmitting antenna. The sensitivity of receiving antennas must be restricted in directions outside the main beam to prevent interference being caused by the reception of signals from stations other than that intended which use the same or an immediately adjacent frequency. The system designer and antenna engineer must acquaint themselves with the requirements of the regulatory authority (Federal Communications Commission or other government agency) to make sure that a new system will work without suffering or causing interference.

To allow the largest possible number of links to be established in a given geographical area on a particular frequency band, it is desirable that each station use a very low transmitter power together with a highly directive high-gain antenna. By this means the area over which any station lays down a field which may cause interference to others is limited. A specification template for a radiation pattern defines the minimum acceptable radiation-pattern performance for an antenna and leaves scope for the designer to decide how to achieve it.

Reliability

A communication link or system must provide an adequate level of reliability. A link may become unusable if the signal-to-noise ratio falls below the design level; it is important that the design objectives for a system specify the fraction of time for which

this may occur. A downtime of 0.01 percent or even less may be necessary for a link to a lifesaving emergency service, but 1 percent downtime may be as little as can be economically justified for a radiotelephone in a boat used for leisure-time fishing.

Fading due to statistical fluctuations in the propagation path is usually guarded against by a fade margin in the power budget. In a severe case a diversity system may be used to reduce the impact of fading on system reliability. This takes advantage of low correlation between fading events over two physically separate paths, at two frequencies, or for two polarizations. Other important causes of system failure are given below.

Wind-induced Mechanical Failures The oscillating loads imposed by wind on antennas and their supporting structures cause countless failures. Aluminum and its alloys are very prone to fatigue failure, and the antenna engineer must be aware of this problem. To achieve real reliability:

- 1 Examine available wind-speed data for the location where the antenna is to be used.
- 2 Consider possible local effects such as turbulence around tall buildings or accelerated airflow over steeply sloping ground.
- 3 Use derated permissible stress levels to allow for fatigue.
- 4 Check antenna designs for mechanical resonance.
- 5 Damp out, stiffen up, or guy parts of the antenna system which are prone to vibration or oscillation.

Aerodynamic and structural analysis can be carried out on a desk-top computer workstation using finite-element methods, allowing designers to check their calculations and to optimize the shape of critical antenna components. A wide variety of commercial software is now available, and every organization engaged in antenna design needs to have access to a set of programs appropriate to the complexity of the work in which it is engaged. References 1 and 2 provide information on a wide range of the mechanical aspects of antenna design.

Corrosion The effects of corrosion and wind-induced stresses are synergistic, each making the other worse. They are almost always responsible for the eventual failure of any antenna system. Every antenna engineer should also be a corrosion engineer; it is always rewarding to examine old antennas to see which causes of corrosion could have been avoided by better design. The essence of good corrosion engineering is:

- Selection of suitable alloys for outdoor exposure and choice of compatible materials when different metals or alloys are in contact. A contact potential of 0.25 V is the maximum permissible for long life in exposed conditions.
- 2 Specification of suitable protective processes—electroplating, painting, galvanizing, etc.

There is an enormous variety in the severity of the corrosion environment at different locations, ranging from dry, unpolluted rural areas to hot, humid coastal industrial complexes.

Plastics do not corrode, but they degrade by oxidation and the action of ultra-

violet light. These effects are reduced by additives to the bulk materials. References 3 and 4 provide detailed information on corrosion mechanisms and control.

Ice and Snow The accumulation of ice and snow on an antenna causes an increase in the input voltage standing-wave ratio (VSWR) and a reduction in gain. The severity of these effects, caused by the capacitive loading of antenna elements and absorption of radio-frequency (RF) energy, increases as the frequency rises.

The fundamental design precaution is to ensure that the antenna and its mounting are strong enough to support the weight of snow and ice which will accumulate on them. This is very important, as even when the risk of a short loss of service due to the electrical effects of ice can be accepted, the collapse of even a part of the antenna is certainly unacceptable. Ice falling from the upper parts of a structure onto antennas below is a major cause of failure; safeguard against it by fitting lightweight antennas above more solidly constructed ones or by providing vulnerable antennas with shields to deflect falling ice.

In moderate conditions, antennas may be provided with radomes to cover the terminal regions of driven elements or even whole antennas. As conditions become more severe, heaters may be used to heat antenna elements or to prevent the buildup of ice and snow on the radome. A wide range of surface treatments has been tried to prevent the adhesion of ice; some of these show initial promise but become degraded and ineffective after a period of exposure to sunlight and surface pollution. Flexible radome membranes and nonrigid antenna elements have been used with some success.

Breakdown under Power An inadequately designed antenna will fail by the overheating of conductors, dielectric heating, or tracking across insulators. The power rating of coaxial components may be determined from published data, but any newly designed antenna should be tested by a physical power test. An antenna under test should be expected to survive continuous operation at 1.5 times rated mean power and at 2 times rated peak voltage; for critical applications even larger factors of safety should be specified. For multichannel systems with n channels:

$$\begin{array}{l} p_{\text{average}} = p_1 + p_2 + \cdots \\ = np_{\text{channel}} \qquad \text{if all channels have equal mean power} \\ v_{\text{peak}} = v_1 + v_2 + \cdots \\ p_{\text{peak}} = (\sqrt{p_1} + \sqrt{p_2} + \cdots)^2 \\ = n^2 p_{\text{channel}} \qquad \text{if all channels have equal power} \end{array}$$

Lightning Damage Antennas mounted on the highest point of a tower are particularly prone to lightning damage. The provision of a solid, low-inductance path for lightning currents in an antenna system reduces the probability of severe damage to the antenna. Electronic equipment is best protected by good antenna design and system grounding, supplemented by gas tubes connected across the feeder cables. Figure 27-1 shows a typical system with good grounding to prevent side-flash damage and danger to personnel. For detailed guidance see Refs. 5, 6, and 7.

Precipitation and Discharge Noise This is caused when charged raindrops fall onto an antenna or when an antenna is exposed to an intense electric field in thunderstorm conditions. Precipitation noise can be troublesome at the lower end of the VHF band and may be experienced frequently in some locations. When problems arise,

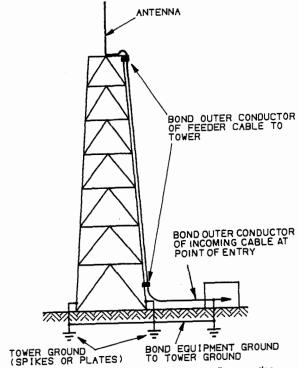


FIG. 27-1 Typical example of good grounding practice. (© Radiation Systems International, Ltd.)

antenna elements may be fitted with insulating covers. These prevent the transfer of the charges from individual raindrops into the antenna circuit and reduce the energy coupled to the antenna when a charge passes between drops.

Choice of Polarization

Base stations for mobile services use vertical polarization because it is then simple to provide an omnidirectional antenna at both the mobile terminals and the base station. There is sometimes an advantage in using horizontal polarization for obstructed point-to-point links in hilly terrain, but the choice of polarization is often determined by the need to control cochannel interference. Orthogonal polarizations are chosen for antennas mounted close together in order to increase the isolation between them.

It has been found that the use of circular polarization (CP) reduces the effects of destructive interference by reflected multipath signals, so CP should be considered for any path where this problem is expected. CP has been used with success on a number of long grazing-incidence oversea paths where problems with variable seasurface reflections had been expected to be troublesome. Each end of a CP link must use antennas with the same sense of polarization.

Meeting Cost Objectives

The designer of a communications system must strive to provide the necessary overall performance for the lowest cost. A 100 percent reliability is often very difficult and costly to achieve and is only necessary for a small number of services. By comparison, 99 percent availability will entirely satisfy many users and can be provided much more readily; the user cannot justify the high cost of that extra 1 percent.

Cost-effective design is only obtained by:

- 1 Identifying the availability needed
- 2 Determining the environment at both ends of the link
- 3 Estimating the propagation characteristics of the path and judging the reliability of the estimates
- 4 Selecting the right equipment and antennas for the link to meet the communications and reliability objectives

Trade-Offs The interdependence of various parameters deserves careful consideration. For any major scheme the following checklist should always be worked through.

- 1 Examine the interactions of structure height, transmitter power, feeder attenuation, and antenna gain.
- 2 Consider using split antennas and duplicate feeders to increase reliability.
- 3 Consider the use of diversity techniques to achieve target availability instead of a single system with higher powers and gains.
- 4 Review the propagation data, especially the probability of multipath or cochannel interference. Don't engineer a system with 99.9 percent hardware availability and find 3 percent outage due to cochannel problems. Check the cost of antennas designed to reduce cochannel problems by nulling out the troublesome signals.
- Visit the chosen sites. General wind data are useless if the tower is near a cliff edge, and a careful estimate of actual conditions must be made. Similarly, a nearby industrial area may mean a corrosive environment, and nearness to main roads indicates a high electrical noise level. Look for local physical obstructions in the propagation path.
- 6 Don't overdesign to cover ignorance. Find out!

27-3 ANTENNAS FOR POINT-TO-POINT LINKS

Yagi-Uda Antennas Yagi-Uda antennas are very widely used as general-purpose antennas at frequencies up to at least 2.5 GHz. They are cheap and simple to construct, have reasonable bandwidth, and will provide gains of up to about 17 dBi, or more if a multiple array is used. At low frequencies the gain which can be obtained is limited by the physical size of the antenna; in the UHF band, a reflector antenna may be simpler, less costly, and more reliable if a large gain is required.*

^{*}For information on the design of Yagi-Uda antennas, see Chaps. 3, 12, and 27. References 8 and 9 provide a useful understanding of the operation of Yagi-Uda and other surface-wave antennas. References 10 and 11 provide easily applied design software for IBM PCs.

Yagi-Uda antennas provide unidirectional beams with moderately low side and rear lobes. The characteristics of the basic antenna can be modified in a variety of useful ways, some of which are shown in Fig. 27-2. The basic antenna (a) can be arrayed in linear or planar arrays (b). When the individual antennas are correctly spaced, an array of N antennas will have a power gain N times as large as that of a single antenna, less an allowance for distribution feeder losses. Table 27-1 indicates typical gains and arraying distances for Yagi-Uda antennas of various sizes. Different array spacings may be used when it is required to provide a deep null at a specified bearing, but the forward gain will be slightly reduced.

The bandwidth over which the front-to-back ratio is maintained may be increased by replacing a simple single reflector rod by two or three parallel rods (c). The back-to-front ratio of a simple Yagi-Uda antenna may be increased either by the addition of a screen (d) or by arraying two antennas with a quarter-wavelength axial displacement, providing a corresponding additional quarter wavelength of feeder cable to the forward antenna (e). A well-designed screen will provide a back-to-front ratio of as much as 40 dB, while that available from the quadrature-fed system is about 26 dB.

Circular polarization can be obtained by using crossed Yagi-Uda antennas: a pair of antennas mounted on a common boom with their elements set at right angles. The two antennas must radiate in phase quadrature, so they must be fed in quadrature or be fed in phase and mutually displaced by a quarter wavelength along the boom.

There has been some interest in slow-wave end-fire arrays which use long, closed forms for their elements, e.g., rings or squares, but they have not proved popular in practice, probably because they have narrower bandwidths than an optimal Yagi-Uda antenna and are more complex to manufacture. The cigar antenna is the only alternative to have remained in currency; in this design, the linear elements of the Yagi-Uda array are replaced by flat circular disks.

Log-Periodic Antennas These are widely used for applications in which a large frequency bandwidth is needed. The gain of a typical VHF or UHF log-periodic antenna is about 10 dBi, but larger gains can be obtained by arraying two or more antennas. The disadvantage of all log-periodic designs is the large physical size of an antenna with only modest gain. This is due to the fact that only a small part of the whole structure is active at any given frequency.

The most common design used on the VHF-UHF bands is the log-periodic dipole array (LPDA) described in Chap. 14 and Ref. 12. After selecting suitable values for the design ratio τ and apex angle α , the designer must decide on the compromises necessary to produce a practical antenna at reasonable cost. The theoretical ideal is for the cross-sectional dimensions of the elements and support booms to be scaled continuously along the array; in practice, the elements are made in groups by using standard tube sizes, and the support boom is often of uniform cross section. The stray capacitances and inductances associated with the feed region are troublesome, especially in the UHF band, and can be compensated only by experiment.

The coaxial feed cable is usually passed through one of the two support booms, thus avoiding the need for a wideband balun.

Printed-circuit techniques can be applied to LPDA design in the UHF band, as the antenna is easy to divide into two separate structures which may be etched onto two substrate surfaces. At the lower end of the VHF band the dipole elements may be constructed from flexible wires supported from an insulating catenary cord.

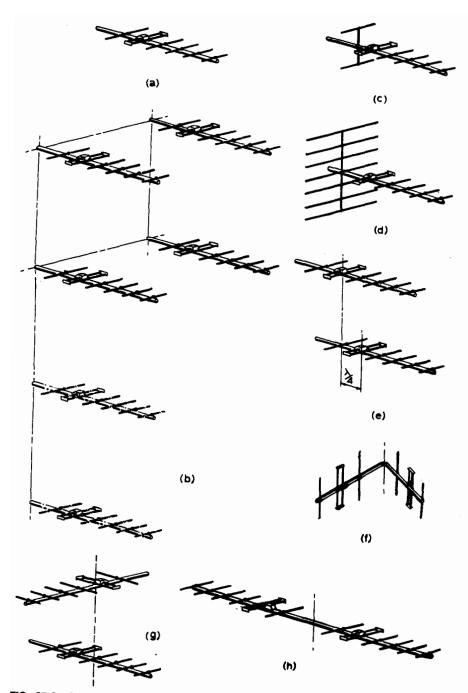


FIG. 27-2 Configurations of Yagi-Uda antennas. (a) Standard six-element antenna. (b) Stacked and bayed arrays. (c) Double reflector rods. (d) Reflector screen. (e) Increased F/b ratio by $\lambda/4$ offset. (f), (g), (h) Arrangements to produce azimuth radiation patterns for special applications.

Number of elements	Typical gain, dBì	Spacing for arraying, λ	
3	7	0.7	
4	9	1.0	
6	10.5	1.25	
8	12.5	1.63	
12	14.5	1.8	
15	15.5	1.9	
18	16.5	2.0	

TABLE 27-1 Typical Data for Yagi-Uda Antennas

A typical well-designed octave-bandwidth LPDA has a VSWR less than 1.3:1 and a gain of 10 dBi.

Helices A long helical antenna has an easily predicted performance and is easy to construct and match. A VSWR as low as 1.2:1 can be obtained fairly easily over a frequency bandwidth of 20 percent, and wider bandwidths are possible if the helix is tapered or stepped in diameter. Conductive spacers may be used to support the helical element from the central support boom, so the antenna can be made very simple and robust. At higher frequencies it may be more convenient to support the helical element by winding it onto a dielectric rod or tube. The maximum gain which can be obtained from a single helix is limited by the physical length that can conveniently be supported, typically ranging from 12 dBi at 150 MHz to 20 dBi at 2 GHz.

Helices may be arrayed for increased gain; to obtain correct phasing the start position of each helix in the array must be the same. For further information on the design of helices see Chap. 13 or Ref. 12.

Panel Antennas An antenna which comprises a reflecting screen with simple radiating elements mounted over it, in a broadside configuration, is generally termed a panel antenna. An array may comprise one or more panels connected together.

Typical panels use full-wavelength dipoles, half-wave dipoles, or slots as radiating elements (Fig. 27-3). They have several advantages over Yagi-Uda antennas:

- 1 More constant gain, radiation patterns, and VSWR over a wide bandwidth—up to an octave.
- 2 More compact physical construction—the phase center is maintained closer to the axis of the supporting structure, providing better control of the azimuth radiation pattern.
- 3 Very low coupling to the mounting structure.
- 4 Low side lobes and rear lobes.

Panel antennas for frequencies in the UHF band lend themselves to printed-circuit design methods, as the radiating structures, feed lines, and matching system may all be produced by stripline techniques. At lower frequencies the radiating elements are often mounted at voltage minimum points using conducting supports, so a strong, rigid construction can be produced. A really solidly built but lightweight panel for a military

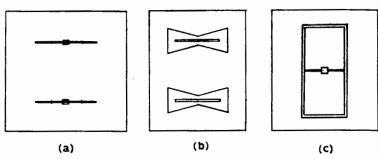


FIG. 27-3 Panel antennas. (a) Two full-wave dipole elements. (b) Two batwing slot elements. (c) Skeleton-slot elements.

application is shown in Fig. 27-4a. Here an all-welded aluminum frame and a skeleton-slot radiator are used so that the antenna will resist rough use in the field.

Corner Reflectors Well-designed corner-reflector antennas are capable of providing high gain and low sidelobe levels, but below 100 MHz they are mechanically cumbersome. Before using a corner reflector, make sure that the same amount of material could not be more effectively used to build a Yagi-Uda antenna, or perhaps a pair of them, to do the job even better.

In the UHF band, corner reflectors may be very simply constructed from solid or perforated sheet and a variety of beamwidths and back-to-front ratios obtained by the choice of the apex angle, spacing of the dipole from the vertex, and the width of the reflector. The apex of the corner is sometimes modified to form a trough (Fig. 27-5). The provision of multiple dipoles extends the antenna aperture and increases the available gain.

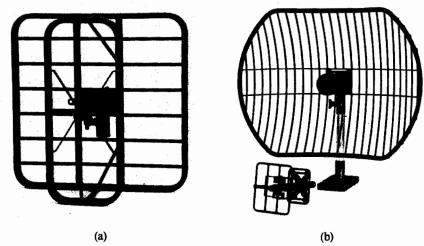


FIG. 27-4 Robustly constructed antennas for military use. (a) Skeleton-slot-fed panel (225-400 MHz). (b) Grid paraboloid (610-1850 MHz). (© Radiation Systems International, Ltd.)

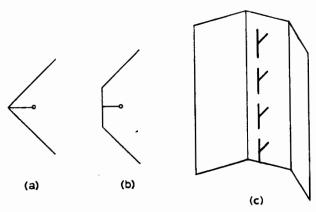


FIG. 27-5 Corner and trough reflectors.

Feeding Multiple Arrays Simple low-power arrays operating at frequencies below 500 MHz are usually fed using a coaxial-cable branching network (Fig. 27-6). Stripline power dividers are attractive for applications above about 200 MHz and can be designed to provide arbitrary power division ratios and any required number of ports; they provide a high level of reproducibility in volume production and can be designed using readily available computer software. If an array is to operate at high mean input power, it may be necessary to use large-diameter fabricated coaxial transformers, which will generally be terminated by EIA flange connections.

It is important to consider the effects of the nonideal reflection coefficient of real antennas on the way in which power will divide at each junction in an array feed network.

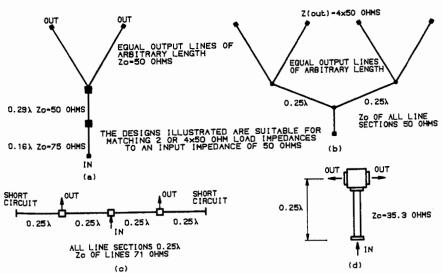


Fig. 27-8 Simple branching feeder systems. (a) Two-way. (b) Four-way. (c) Two-way, compensated. (d) Two-way, high-power.

When elements are to be driven with equal cophased currents, their input impedances (including the effects of mutual impedances) must be as close to equal as possible; where element currents are required to be unequal in amplitude or phase, the VSWR of individual elements must be made as low as possible over the whole operating frequency band, especially if close control of the radiation patterns of the array is important. For critical applications it may be necessary to adopt the use of hybrid junctions (Wilkinson or other types); these reduce, but do not completely remove, the error in the ratio of radiating currents where the impedances presented at the junction are unequal. The use of suitable network-analysis software will allow the designer to explore the impact of element reflection on the nominal element currents and on the performance of the array.

For applications in which the achievement of stringently defined radiation patterns is essential, the designer will begin by selecting a suitable current distribution using one of the established techniques for array design (Chap. 20 provides some examples). Having chosen the form of the elements and distribution system, the designer should then compile a budget of possible phase and amplitude errors, identifying each separate cause of error and assigning a value to it (in general it will be possible to assign an amplitude with some certainty, but it will not be possible to define the phase of the error, at least over any appreciable bandwidth). The confidence with which the prescribed radiation pattern is likely to be achieved can then be investigated using a Monte Carlo technique. If the required confidence is not obtained, the design can be revised. The analysis should include

Element reflection coefficients—allowing for construction tolerances Transmission-line length and Z_0 errors Errors in power division at junctions Radome reflections and an allowance for their variability Thermal and environmental effects

Further details on the design of transformers and other components for feed networks will be found in Refs. 13, 14, and 20.

Paraboloids The design of a high-gain antenna may be reduced to a problem of illuminating the aperture necessary to develop the specified radiation patterns and gain. The size of the aperture is determined only by the gain required, whatever type of elements is used to fill it. As the cost of the feed system and the radiating elements doubles for each extra 3-dB gain, a stage is reached at which it becomes attractive to use a single radiating element to illuminate a reflector which occupies the whole of the necessary antenna aperture. The design task is reduced to choosing the size and shape of the reflector and specifying the radiation pattern of the illuminating antenna. If the antenna aperture is incompletely filled or its illumination is nonuniform, the gain which is realized decreases. The ratio of the achieved gain to the gain obtainable from the same aperture when it is uniformly illuminated by lossless elements is termed the aperture efficiency of the antenna. In a receiving context, this quantity represents the proportion of the power incident on the aperture which is delivered to a matched load at the terminals of the antenna.

In the VHF and UHF bands, a reflector may be made of solid sheet, perforated sheet, wire netting, or a series of parallel curved rods. As the wavelength is large, the mechanical tolerance of the reflector surface is not very demanding, and various methods of approximating the true surface required are possible. Table 27-2 indicates some

Frequency, MHz	Diameter, m	f/d ratio	Construction	Feed type
200	10.0	0.5	Mesh paraboloid	4-element Yagi-Uda
700	3.0	0.25	Solid skin	Dipole and reflector
900	7.0	0.4	Perforated steel sheet	Horn
610-960	1.2	0.25	Grid of rods	Slot and reflector
1500	2.4	0.25	Solid skin	Dipole and disk
1350-2500	1.2	0.25	Grid of rods	Slot and reflector

TABLE 27-2 Typical Paraboloid-Antenna Configurations

of the combinations of techniques currently in use and illustrates the diversity of the methods which are successful for various purposes.

Grid paraboloids are attractive to produce because the curvature of all the rods is exactly the same; only their length varies across the antenna. A typical example is shown in Fig. 27-4b (see Ref. 15). The main deficiency of grid paraboloids is the leakage of energy through the surface, restricting the front-to-back ratio which can be achieved. For example, at 1500 MHz a front-to-back ratio of -30 dB is a typical limit. If a greater front-to-back ratio is needed, it may be possible to adopt an offset geometry. Alternatively, the reflector bars can be extended in depth, or an orthodox continuous skin of solid or perforated sheet can be used in place of the grid; the consequent increase in weight and wind-loaded area must be accepted as a necessary penalty for improved electrical performance. A mathematical treatment of grid reflectors appears in Ref. 16.

Radomes are frequently fitted to feeds or complete antennas in order to reduce the effects of wind and snow. They may be made from fiberglass or in the form of a tensioned membrane across the front of the antenna. In severe climates it is possible to heat a radome with a set of embedded wires, but this method can be applied only to a plane-polarized antenna.

Point-to-point links using tropospheric-scatter propagation require extremely high antenna gains and generally use a reflector which is an offset part of a full paraboloidal surface constructed from mesh or perforated sheet. Illumination is provided by a horn supported at the focal point by a separate tower.

For a full discussion of the design of reflector antennas refer to Chap. 17.

27-4 BASE-STATION ANTENNAS

Simple Low-Gain Antennas The simplest types of base-station antennas will provide truly omnidirectional azimuth coverage only when mounted in a clear position on top of a tower. Figure 27-7 shows standard configurations for ground-plane and coaxial dipole antennas and demonstrates that these forms are closely related. They are cheap and simple to construct and may be made to handle high power. Exact dimensions must be determined by experiment, as the stray inductance and capacitance associated with the feed-point insulator cannot be neglected. The use of a folded feed system can provide useful mechanical support and gives better control over the

antenna impedance (both the relative diameter of the feed and grounded conductors and the point of their interconnection can be varied). The satisfactory operational bandwidth of the coaxial dipole d depends critically on the characteristic impedance Z_0 , of the lower coaxial section formed by the feed line (radius r) inside the skirt (radius R). If this section has too small a Z_0 , radiating currents will flow on the outside of the feeder line unless the skirt length is exactly $\lambda/4$. The impedance, gain, and radiation pattern of the antenna then becomes critically dependent on the positioning of the feed line on the tower, severely limiting the useful bandwidth of the antenna.

Discone Antennas The discone and its variants are the most commonly used low-gain wideband base-station antennas. The useful lower frequency limit occurs when the cone is a little less than $\lambda/4$ high, but the upper frequency limit is determined almost entirely by the accuracy with which the conical geometry is maintained near the feed point at the apex of the cone.

Discones may be made with either the disk or the cone uppermost. The support for the upper part of the antenna usually takes the form of low-loss dielectric pillars or a thin-walled dielectric cylinder, fitted well outside the critical feed region.

Variants of the basic discone use biconical forms in place of the conventional cone and replace the disk by a cone with a large apex angle. At the lower end of the VHF band the antennas may be mounted at ground level, so a minimal skeleton disk which couples to the ground may be used if some loss of efficiency and the propagation effects associated with a low antenna elevation can be accepted.

Collinear Arrays The ground plane and coaxial dipole have about the same gain as a half-wavelength dipole. When more gain is needed, the most popular omnidirectional antennas are simple collinear arrays of half-wave dipoles. The original array of this type is the Franklin array shown in Fig. 27-8 a. This design is not very convenient owing to the phase-reversing stubs which project from the ends of each half-wave radiating section, but various derivatives are now widely used. The arrangement at b uses noninductive meander lines to provide phase reversal and that at c is a rearrangement of the original, while those at d and e use coaxial line sections. Arrangements such as these may be mounted in fiberglass tubes to provide mechanical support, and the designs at b and c are suitable for production by printed-circuit techniques. In each of these arrange-

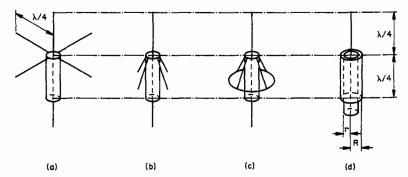


FIG. 27-7 Low-gain base-station antennas. (a) Standard ground plane with radials. (b) Ground plane with sloping radials. (c) Ground plane with closed ring. (d) Coaxial dipole.

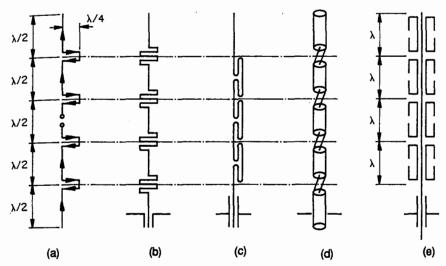


FIG. 27-8 Collinear dipole arrays. (a) Franklin array. (b) Array with meander-line phase reversal. (c) Array with transposed coaxial sections. (d) and (e) Alternative coaxial forms.

ments, the elements are connected in series; an input-matching section transforms the input impedance of the lower section, which may be $\lambda/2$ or $\lambda/4$ long, to 50 Ω . A set of quarter-wavelength radial elements or a quarter-wavelength choke is used to suppress currents on the outside of the feeder cable. The gain available from these arrays is limited by two factors:

- 1 There is mechanical instability in a very long antenna with a small vertical beamwidth.
- 2 The available excitation current diminishes away from the feed as a result of the power lost by radiation from the array.

The practical upper limit of useful gain is about 10 dBi.

In the case of the coaxial-line designs, each section is shorter than a free-space half wavelength so that the correct phase shift is obtained inside the section. The examples shown would typically provide a gain of 9 dBi at the design frequency. The useful bandwidth of these antennas is inherently narrow because of the phase error between successive radiating sections which occurs when the frequency is changed from the design frequency. The typical behavior of the major lobes of the vertical radiation pattern of these arrays is shown in Fig. 27-9. A further problem with long arrays is that as the array length is increased, the series connection of the elements results in an increased input impedance; as the transformation ratio of the input feed network increases, so the input impedance bandwidth is reduced.

Parallel-Fed Arrays Much greater control is obtained by using an array of fat dipoles with an internal, branched, parallel-connected feed system. Arrays of this type provide stable gain, radiation patterns, and input VSWR over wide bandwidths. A well optimized

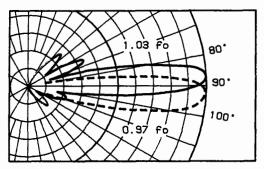


FIG. 27-9 Vertical radiation pattern of a typical endfed array.

eight-element array is able to provide acceptable gain (10 dBi) patterns and input impedance over the entire 225- to 400-MHz communications band.

Dipoles on a Pole Much ingenuity has been applied to the design of simple wideband high-gain omnidirectional antennas. A simple offset pole-mounted array is shown in Fig. 27-10a. This will provide about 10-dBi gain in the forward direction but typically only 4 dBi rearward, depending on the pole diameter and the spacing between the dipole and the pole axis. An attempt to avoid this problem is shown in Fig. 27-10b, but this type of antenna has distorted vertical radiation patterns caused by the phase shifts which result from the displacement of the dipoles; gain is also reduced to about 6 dBi for the four-element array shown.

The solution in Fig. 27-10c, in which dipoles are placed in pairs and are cophased, is more satisfactory, as the phase center of each tier is concentric with the supporting pole. However, the antenna is relatively expensive, as eight dipoles provide only 6-dB gain over a single dipole.

One possibility is to use the in-line stacked array in Fig. 27-10a and place the base station toward the edge of the service area. The rearward illumination may be improved if the spacing between the dipoles and the pole is optimized for the pole size and frequency to be used.

Analytical solutions to the azimuth pattern are available, and simple computer programs provide results in good agreement with measurements. When designing the feed networks for multielement arrays of this type, take care to allow for the effects of mutual impedances, especially when unequal currents or nonsymmetric geometries are used.

Antennas on the Body of a Tower Figure 27-11a shows a measured horizontal radiation pattern for a simple dipole mounted from one leg of a lattice tower of 2-m face width. The distortion of the circular azimuthal pattern of the dipole is very typical and is caused by blocking and reflection from the structure. By contrast, Fig. 27-11b shows what can be achieved by an antenna comprising three dipole panels mounted on the same structure. The penalty of adopting this improved solution lies in the cost of the more complex antenna, so before an optimum design can be arrived at, the value of the improved service must be assessed.

The horizontal radiation pattern of a complete panel array is usually predicted from measured complex radiation-pattern data for a single panel, using a suitable

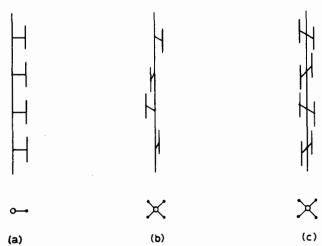


FIG. 27:10 Pole-mounted dipoles. (a) In line. (b) Four dipoles spaced around a pole. (c) Eight dipoles spaced around a pole.

computer program. For each azimuth bearing, the angle from each panel axis is found, and the relative field in that direction is obtained. The radiated phase is computed from the excitation phases and physical offsets of the phase centers of the individual panels.

Depending on the cross-sectional size of the structure, the most omnidirectional coverage may be produced with all panels driven with the same phase or by a phase rotation around the structure; for example, on a square tower the element current phases would then be 0, 90, 180, and 270°. When phase rotation is used, the individual

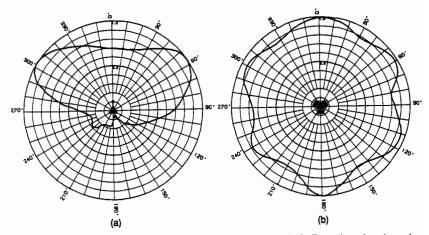


FIG. 27-11 Typical azimuth patterns of (a) VHF dipole mounted off one leg of a triangular mast and (b) three dipole panels mounted on the same structure.

simple to write an integration routine for a programmable pocket calculator. Once an array has been selected, its horizontal and vertical radiation patterns may be computed and used to predict the array gain more accurately.

The growth of cellular telephone systems has created a demand for high-gain basestation antennas with well-controlled pattern characteristics to permit intensive frequency reuse. The standard directional antenna for this application is an extended corner reflector array in which a long reflector is excited by an array of collinear dipole elements.

27-5 MOBILE ANTENNAS

A road vehicle is not an ideal environment for an antenna. To make matters worse, the owner of a vehicle usually does not want antennas to be fixed in the most electrically favored positions like the center of the roof, but expects them to work when mounted on gutters, fenders, or bumpers. The antenna is usually a severe compromise between what is ideally required and what is convenient. Figure 27-14 shows typical radiation patterns for a whip antenna measured with different mounting positions on a medium-sized automobile.

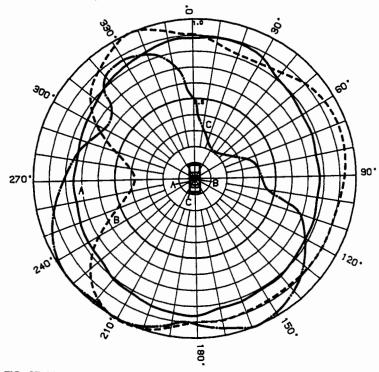


FIG. 27-14 Radiation patterns for a whip antenna on a typical automobile. Some of the data used in the preparation of this figure are from P. A. Ratliff, "VHF Mobile Radio Communications — A Study of Multipath Fading and Diversity Reception," Ph.D. thesis, University of Birmingham, 1974.

On both road vehicles and boats, antennas are subjected to severe mechanical shock, vibration, and exposure to all kinds of weather. Coaxial dipoles are widely used as VHF antennas on ships of all sizes. They can be encapsulated in a dielectric tube which protects the antenna from corrosion by seawater, and they have a vertical beamwidth which is large enough to avoid problems when the ship rolls (on small boats, yachts, and buoys, high-gain antennas cannot be used because of their limited elevation beamwidth). The most popular form of antenna for road vehicles is the simple base-fed whip. Quarter-wavelength whips require no loading, but they are inconveniently long at frequencies below about 100 MHz. Base or center loading can be used to shorten the physical length of a whip, but the efficiency of the antenna falls as the height becomes a smaller fraction of a wavelength. At higher frequencies it becomes possible to increase the gain of the antenna by using a five-eighths-wavelength whip, which has a small input coil to provide an input impedance suitably close to 50Ω . Antennas with higher gain can be used in the UHF band; they are typically short versions of the collinear arrays described in Sec. 27-4.

A variety of low-profile antennas are used on trains, buses, and security vehicles. These are usually derivatives of the inverted L or the annular slot (Fig. 27-15). Various discontinuities on a vehicle can be driven as slot radiators, although it is difficult to provide omnidirectional azimuth coverage. Antennas built into external mirrors or printed onto windows are used for applications when no conspicuous antennas must be carried, but at the cost of limitations in azimuth coverage.

During recent years much attention has been given to antennas which use active devices for matching or modification of radiating currents. As some of these antennas are physically small in terms of a wavelength, they are of particular interest for mobile use. Multielement antennas which provide steered beams or nulls offer promising lines of development, especially if control of the antenna is adaptively managed to optimize the received signal. Such techniques will become increasingly important with the growth of satellite links to vehicles.

Antennas for personal hand-held transceivers usually take the form of rigid telescopic whips, wires positioned in carrying straps, or short semiflexible whips. The helical whip is increasingly preferred, as rigid antennas are inconvenient and the perfor-

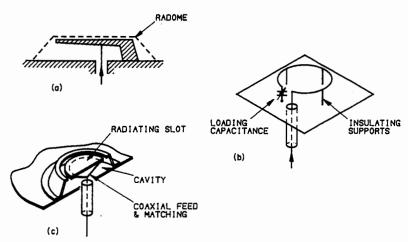


FIG. 27-15 Low-profile antennas. (a) Inverted L. (b) Hula hoop. (c) Annular slot.

mance of carrying-strap antennas varies greatly with their position. When designing these systems, the developing literature on biological hazards should be consulted.^{17,18}

27-6 SYSTEM CONSIDERATIONS

Mounting Arrangements When mounting any antenna, it is important not to impair its performance by the influence of the supporting structure. The inevitable effect of the supporting structure on the radiation pattern of a dipole has been referred to in Sec. 27-4. This effect is accompanied by a modification of the input impedance, which may be unwelcome if a low VSWR is needed. In any critical application the change of the radiation patterns and gain must be taken into account when estimating system performance. Impedance matching of the antenna must be undertaken in the final mounting position or a simulation of it.

If Yagi-Uda arrays are mounted with their elements close to a conducting structure, they too will suffer changes of radiation patterns and impedance. The effects will be greatest if tower members pass through the antenna, as they do when an array is mounted on clamps fitted at the center of the cross boom. If at all possible, when an array is center-mounted, the member to which it is clamped should lie at right angles to the elements of the array.

Currents induced in diagonal members of the supporting structure will cause reradiation in polarization planes other than that intended. This will result in the cross-polar discrimination of the antenna system being reduced from that which would be measured on an isolated antenna at a test range. When polarization protection is important, the tower should be screened from the field radiated by the antenna with a cage of bars spaced not more than $\lambda/10$ apart, lying in the plane of polarization. (A square mesh is used for circular polarization.) Panel antennas are designed with an integral screen to reduce coupling to the mounting structure.

Long end-mounted antennas are subjected to large bending forces and turning moments at their support points. These forces can be reduced by staying the antenna, using nylon or polyester ropes for the purpose to avoid degrading its electrical characteristics.

In severe environments antennas may be provided with radomes or protective paints. It is very important that the antennas be tested and set up with these measures already applied, especially if the operating frequency is in the UHF band.

Coupling A further consideration when planning a new antenna installation on an existing structure is the coupling which will exist between different antennas. When a transmitting antenna is mounted close to a receiving antenna, problems which can arise include:

Radiation of spurious signals (including broadband noise) from the transmitter Blocking or desensitization of the receiver

Generation of cross-modulation effects by the receiver

Radiation of spurious signals (intermodulation products and harmonics) due to nonlinear connections in the transmitting antenna or generation of spurious signals and cross-modulation effects caused by the same mechanism in the receiving antenna The last of these problems must be avoided by good antenna design—avoiding any rubbing, unbonded joints. The other effects depend critically on the isolation between the antennas and on parameters of the transmitters and receivers; these parameters should be specified by their manufacturers.

The isolation between two antennas may be predicted from Fig. 27-16 or from standard propagation formulas. Antenna isolations may be increased by using larger spacings between them or by using arrays of two or more antennas spaced to provide each with a radiation-pattern null in the direction of the other.

An alternative method of increasing the isolation between the antenna-system inputs is to insert filters. If a suitable filter can be constructed, the antenna isolation may be reduced until, in the limit, a single antenna is used with all equipment, transmitters and receivers, coupled to it through filters. When receivers are connected to a common antenna, the signal from the antenna is usually amplified before being divided by a hybrid network. For information on filter design, consult Refs. 19 and 20. The number of services which use a single antenna can be extended to six or more, provided adequate spacings are maintained between the frequencies allocated to different users. The whole system is expensive, but the cost may be justified if the antenna itself is large or if tower space is limited.

Coverage In free-space conditions the intensity of a radio wave diminishes as the distance from the transmitter increases in accordance with the inverse-square law. Terrestrial links are not usually in free-space conditions, and the field diminishes more

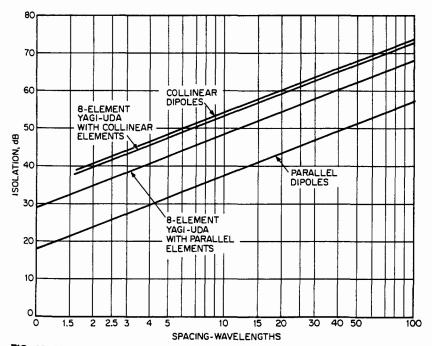


FIG. 27-16 Typical isolations between Yagi-Uda antennas.

rapidly with distance. Reference 21 provides a large variety of basic data and curves for planning point-to-point, aeromobile, and other services. References 22, 23, and 24 provide further examples of the use of the data and also provide additional information on the methods to be adopted for dealing with obstructed paths.

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TV and FM Transmitting Antennas

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28-1 Introduction 28-2

28-2 Panel-Type Antennas 28-6

28-3 Circularly Polarized Antennas 28-8
Crossed-Dipole Panel Antennas 28-9
Slanted-Dipole Antennas 28-11
Helical Antennas 28-17
Ring-Panel Antennas 28-21

28-4 Horizontally Polarized Antennas 28-24
Dipole-Panel Antennas 28-24
Corner-Reflector Antennas 28-25
Batwing Antennas 28-25
Zigzag-Panel Antennas 28-26
Slot Antennas 28-29

28-5 Multiple-Antenna Installations 28-35

The objective in this chapter is to provide the reader with specifications and descriptions of television and FM radio broadcast antennas. The various antennas to be described also may be used for other applications in the frequency range of 10 MHz to 10 GHz. Broadcast antennas have frequency, pattern, power capacity, impedance, and environmental requirements which are imposed by regulatory agencies such as the Federal Communications Commission (FCC) or by system specifications. For instance, frequency and pattern are regulated by the FCC, while impedance, power capacity, and environmental requirements are system-related.

Broadcast frequencies in the United States are allocated and regulated by the FCC. The following frequency bands are assigned to television broadcasting:

		SIOH OIOAGCASUHE.
Low VHF	Channels 2-4	54-72 MHz
	Channels 5-6	76-88 MHz
High VHF	Channels 7-13	174-216 MHz
UHF	Channels 14-83	470-890 MHz

Each channel is assigned 6 MHz of bandwidth, with visual carrier and color subcarrier at 1.25 and 4.83 MHz above the lower edge of the channel, respectively, and with aural carrier at 0.25 MHz below the upper edge of the channel. The power levels of the visual subcarrier and aural carrier usually are within 20 percent of the visual carrier.

FM radio frequencies are limited to the band between 88 and 108 MHz. There are 100 channels, each with a 200-kHz bandwidth. Pattern requirements are functions of coverage goals, site location, local terrain, and the available options on mounting structures. Coverage goals are regulated and limited by FCC specifications as spelled out in the Code of Federal Regulations¹ (CFR 47). For instance, a TV station's coverage is specified by the distance to the "city grade," "grade A," and "grade B" contours. Table 28-1 shows the minimum levels of the field strength (present at 50 percent of locations 50 percent of the time) assigned to these contours. The transmitter location and power and the antenna height and gain are chosen such that the city-grade contour covers the entire principal community to be served.

For an FM station, the coverage limits are defined by two contours. These are the 70-dBu contour (3.16 mV/m), for city grade, and the 60-dBu contour (1.0 mV/m). These limits, along with the path-loss curves (also known as the 50-50 curves), which are documented in *CFR* 47, are used to determine the ERP* and/or the gain of the antenna for a given antenna height and location.

The FCC manual specifies the maximum ERP for TV and FM stations. The maximum power² varies with regions or zones of the United States and with the antenna height above the average terrain (HAAT). Towers that support broadcast antennas are either self-supported or guyed, and their heights range from 100 to 2000 ft.

Since broadcast antenna structures usually consist of vertical arrays of radiating elements, antenna directivity is approximately equal to the product of azimuth-pattern directivity and the elevation directivity (the number of bays in some antennas). The antenna gain is always referenced to the gain of a half-wave dipole (2.15 dB above the isotropic element) and is equal to the directivity less the losses, such as impedance loss and/or polarization-mismatch loss.

The majority of applications call for omnidirectional azimuth patterns. The circularity of the pattern depends on the type of antenna when top-mounted and also on the

^{*}The effective radiated power (ERP) is equal to the product of the directive gain of the antenna (with respect to a horizontal dipole) and the input power to the antenna.

ABLE 20-1 Grade Contours of 14 Broadcast Clausins				
Channel	City grade (dBu)	Grade A (dBu)	Grade B (dBu)	
2-6	74	68	47	
7-13	77	71	56	
14-69	80	74	64	

TABLE 28-1 Grade Contours of TV Broadcast Stations

Note: dBu is decibels above $1 \mu V/m$.

configuration of the support structure when side-mounted. Other requirements call for various types of azimuth patterns, such as cardioid, skull-shaped, peanut-shaped, etc., to protect other stations or reduce radiation into low-population areas. An azimuth pattern with a circularity of ± 2 dB is considered omnidirectional. The maximum to minimum ratio of directional patterns should not exceed 15 dB for FM and UHF TV (with the ERP greater than 1 kW). For Channels 2 to 13 this ratio is 10 dB.

Since the directivity of the azimuth pattern is low, it is desirable to stack several bays of antennas to increase the gain in order to achieve the desired maximum ERP without increasing the input power to an unreasonable value. For antennas mounted at large heights, the vertical beamwidth should not be less than 1°. This implies a vertical aperture of about 50 wavelengths, which is practical only in the UHF band. Wind loading and cost considerations limit the vertical aperture to about 120 ft (36.6 m). Thus the minimum elevation beamwidths (~51 per number of wavelengths in the vertical aperture) are about 7, 4, and 2° for the lower VHF, FM, and upper VHF bands, respectively. For certain combinations of terrain and antenna heights, it may be desirable to tilt the beam to point it at certain areas below the radio horizon. The commonly used formulas for the depression angle of the radio horizon and the distance to the radio horizon are

$$A = 0.0153 \sqrt{H}$$
 (28-1)

and
$$D = 92.1518A$$
 (28-2)

where A is the depression angle in degrees, H is the antenna HAAT (height above the average terrain) in feet, and D is the distance to the radio horizon in miles. These equations assume a spherical earth with a radius of 5278 mi (8494 km), which is % times the actual earth radius to correct for atmospheric refraction effects.

Equations (28-1) and (28-2) provide a theoretical upper bound for the outer boundaries of the coverage area regardless of the ERP. Beam tilt is introduced by either direct mechanical tilt or linear progressive phasing of the elements of the array. Mechanical tilt is rarely used owing to a variation in beam tilt with azimuth direction.

Null fill of the elevation pattern is desired in cases where the coverage is to include areas in the vicinity of the antenna tower. When considering the elevation pattern, the percentage of a null fill is defined as the ratio of the value of field strength at the null to the value at the peak of the main beam. Null fills of about 15 percent in the first and about 5 percent in the second null are common. One simple technique for achieving null fill is to shift the phase of the end or middle elements of the array. There is a practical advantage, however, to shifting the phase of the end elements rather than the middle elements. For instance, the phases of elements in an array affect the mutual coupling between the array elements. Shifting the phase of a middle element affects the mutual coupling between that element and twice the number of elements that would be affected if, instead, the phase of

an end element were shifted. This leads to an increase in the complexity of the feed owing to the change in the impedances of the affected elements.

It can be shown³ that by introducing β° of phase shift in the end elements of an N-element uniform array, the amount of the null fill in the Mth null is given by

$$NF = \frac{400}{N}\sin(\beta/2)\cos(M\pi/N)$$
 (28-3)

where NF is the percentage of the null fill and β is the phase offset of the end elements.

Equation (28-3) indicates a gradual filling of successive nulls, which is considered quite desirable in many situations. It also can be shown that this method of filling the nulls increases the level of sidelobes and reduces the array gain. The gain of this new array is given by

$$G = \frac{N}{1 + \frac{8}{N}\sin^2{(\beta/2)}}$$
 (28-4)

Another method to achieve null fill is to increase the current in the upper third of the array and decrease it in the lower third by the same amount, say D. The percentage of the null fill in the elevation pattern, using this method, is given by

$$NF = 200 \frac{D}{N} \sin (2M\pi/3) \left[\frac{\sin (M\pi/3)}{\sin (M\pi/N)} \right]$$
 (28-5)

This equation indicates that the null fill is the same for the first and the second null and is zero for the third null. This method also results in an increase in the level of the sidelobes and reduction of the gain. The gain of the array in this case is given by

$$G = \frac{N}{1 + (2D/3)} \tag{28-6}$$

Figure 28-1 compares the percentage of gain reduction due to null filling in several arrays using the preceding methods.

TV and FM broadcasting was originally limited to horizontal polarization. In the 1960s, the FCC allowed circular polarization (CP) for FM broadcasting. This provided improved reception, especially for vehicles with whip antennas, which are predominantly vertically polarized. In 1977, the FCC permitted TV broadcasting in right-hand CP as well. In going from horizontal polarization to CP, the stations were allowed to maintain their maximum ERP in horizontal polarization so as to maintain the field strength existing before the conversion. By allowing the same ERP for vertical polarization, the FCC actually allowed doubling the radiated power. This has provided improved reception for receivers with indoor antennas such as monopoles and rabbit ears.

In some instances, use of CP has reduced ghosting because reflections from buildings and other objects tend to have the opposite sense of CP. The acceptable axial ratio for CP antennas is 3 dB or less. The receiving antennas are almost all linearly polarized, and because of this and the unfriendly propagation path of most broadcast environments, the importance of axial ratio is somewhat superfluous. For instance, the majority of FM antennas are omnidirectional CP antennas side-mounted on towers without regard to the effect of the tower on the axial ratio of the radiated CP wave. FCC regulations are limited to the shape and directivity of the vertical and horizontal polarization patterns and do not specify the axial ratio of the radiated CP wave.

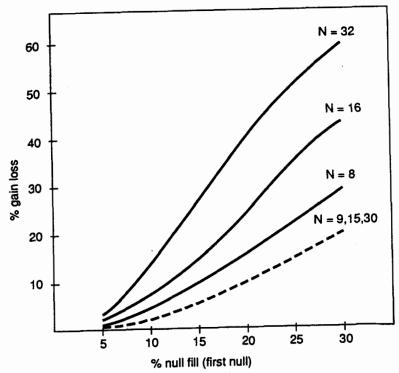


FIG. 28-1 Gain versus null fill for linear arrays. Solid lines, Eqs. (28-3) and (28-4); dashed line, Eqs. (28-5) and (28-6).

In many cases, the transmit antenna is several hundred wavelengths away from the transmitter. In order to reduce multiple reflections in the transmission line, it is desirable to keep the antenna VSWR as low as possible. In most cases, VSWR values of 1.1 or lower over one or several channels is desirable. Higher values of VSWR cause excessive reflections in the transmission line, which result in ghosts in TV signals and in degradation of stereo separation in FM signals.

The power-handling capacity is an important factor in the design of broadcast antennas. The input power typically ranges from a few hundred watts for educational FM to several hundred kilowatts for some UHF or multichannel FM applications. Typically, the FM transmitter is specified by its average output power, whereas in TV transmitters the peak power is specified. In this latter case a conversion factor of 0.8 is used to convert peak to average power. In single-channel applications, the feed and the antenna are designed to handle the average power. In multichannel applications, however, the antenna system is designed to handle the peak instantaneous power P_n . This peak power is the instantaneous power when signals from all transmitters add in phase, and it is given by

$$P_{lns} = \left(\sum_{n=1}^{N} \sqrt{P_n}\right)^2$$
 (28-7)

where P_n is the peak power of the *n*th transmitter.

In the case where all input powers are the same, this expression reduces to

$$P_{ins} = N^2 P \tag{28-8}$$

which shows that the total instantaneous power may be substantially greater than the total average power.

In designing the feed system of a high-power antenna, it is important to compensate for internal mismatches and for variations in antenna mismatch due to icing. High VSWR and high ambient temperatures reduce the power-handling capacity of transmission lines. The derating factors, usually furnished by the manufacturers, should be taken into account in the feed design. Antenna elements are designed with rounded edges to reduce the possibility of corona, breakdown, and arcing.

28-2 PANEL-TYPE ANTENNAS

In many cases, the supporting structure is a triangular or square tower. Panel antennas are primarily used to control or minimize the reflections from the supporting structure. Some panel antennas are made of a single horizontal dipole or two crossed dipoles (circularly polarized panel) in front of a reflector.

The reflector can be a flat panel, a corner reflector, or a pill box (commonly referred to as cavity-backed). The reflector is usually a wire grid for VHF or a solid sheet for UHF.

In order to obtain an omnidirectional radiation pattern, three- or four-panel antennas are placed around a triangular or square tower, respectively. In general, panel antennas with 6-dB beamwidth of 90 and 120° are used for arrays around square and triangular towers, respectively. Flat dipole panels and 90° corner-reflector panels are suitable for square towers and cavity-backed panels (with a cavity diameter of 0.65 wavelength), and so-called arrowhead panels are suitable for triangular towers. When several panels are

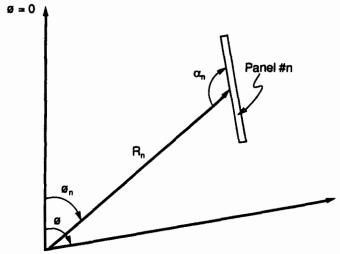


FIG. 28-2 Geometry for Eq. (28-9).

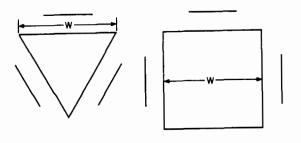


FIG. 28-3 Panel-type antennas for triangular and square towers.

arranged around a cylindrical structure in a single layer, as shown in Fig. 28-2, the combined pattern $E(\phi)$ may be calculated by using the following expression:

$$E(\phi) = \sum_{n=1}^{N} I_n M_n(\psi) \exp i[\xi_n(\psi) + \sigma_n + kR_n \cos(\phi - \phi_n)]$$
 (28-9)

where $I_n e^{i\sigma_n}$ = excitation current of the *n*th panel

 $M_n(\psi)e^{i\xi_n(\psi)}$ = pattern of the *n*th panel

 ϕ_n = polar angle of the *n*th panel

 $R_n =$ length of the radial to the *n*th panel

 $\psi = \pi - \alpha_n + \phi - \phi_n$

 α_n = tilt angle of the *n*th panel

With the panels fed with equal phase and amplitude and with the antenna elements placed in the center of the sides, as shown in Fig. 28-3, an omnidirectional-type pattern is obtained with a maximum-minimum ratio that increases with the face width of the tower. The short lines represent panels. Figure 28-4 shows this ratio for both square and triangu-

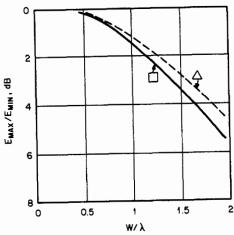


FIG. 28-4 Maximum-minimum ratio versus tower width in wavelengths for triangular and square towers.

lar towers. For good omnidirectional patterns, the tower width should not be much greater than one wavelength. The null directions occur on each side of the crossover directions where the radiation from adjacent panels does not arrive in phase. This arrangement is commonly referred to as azimuthal mode zero. Higher-order modes are obtained by progressive phasing of elements around the tower with a total phase progression of 360M, where M is the mode number. For instance, the phases of panels in the mode 1 arrangement on a square tower are 0, 90, 180, and 270°, and on a triangular tower they are 0, 120, and 240°.

Higher modes can be used to achieve a broader bandwidth for the antenna input impedance. Use of higher modes requires different lengths of feed lines from the power divider. This provides reflection cancellation at the power divider, which in turn allows lower VSWR at the power divider than at the panels. To eliminate the difference in the arrival phase of adjacent panels in the crossover direction, the elements are displaced laterally as shown in Fig. 28-5. Equations (28-10) and (28-11) give the amount of offset S for triangular and square towers for mode 1, respectively:

$$S = \lambda/(4\sqrt{2}) \tag{28-10}$$

$$S = \lambda/3 \tag{28-11}$$

An adverse effect of using higher-order modes with panels having high VSWR is that multiple reflections produce power-division errors to the panels, which result in pattern distortions.

Skewed-panel antennas^{4,5} may be placed on the corners of large-face towers (such as those measuring five wavelengths), as shown in Fig. 28-6; the antenna elements are placed on narrow panels. The panels are skewed so that the crossover direction coincides with the tower face. Thus the relative phase of the radiation from adjacent antennas varies more slowly near the crossover direction than in a nonskewed arrangement. Theoretically, this should greatly improve the pattern circularity.⁴ However, reflections from the tower members and the backside of the panel degrade the pattern. In general, it is difficult to achieve pattern circularities better than ± 2 dB.

28-3 CIRCULARLY POLARIZED ANTENNAS

The FCC allowance of circularly polarized broadcast transmission has led to the introduction of a wide variety of new transmitting antennas. The antenna types usually take the

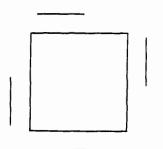


FIG. 28-5 Offset-panel type of radiators on a square tower for reflection cancellation.

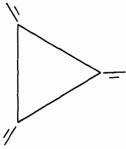


FIG. 28-6 Skewed-panel type of radiators for triangular towers.

form of crossed dipoles, circular arrays of slanted dipoles, helical structures, and travelingwave ring configurations.

Crossed-Dipole Panel Antennas

A common technique for producing circular polarization has been to place two linear dipoles at right angles in front of a reflecting screen and to feed them with equal voltage magnitudes and with a 90° phase difference. However, the azimuth beamwidth for horizontal and vertical polarization is about 60 and 120°, respectively. Thus the axial ratio is low only for directions near the normal to the screen. This deficiency may be corrected in several ways.

V dipoles, as illustrated in Fig. 28-7, may be used to increase the azimuth beamwidth for horizontal polarization. The crossed dipoles may be identical and fed in phase quadrature or be unequal in length and fed in phase with the lengths adjusted to produce quadrature currents in the dipoles. Three crossed V dipoles may be placed around a triangular tower to obtain a circularity of ± 2 dB and a maximum axial ratio of 4 dB. In this arrangement, the circularity of the vertically polarized component of the azimuth pattern is degraded relative to the circularity of the horizontally polarized component. Furthermore, the peaks of one pattern coincide with the valleys of the other. Another version of this type of antenna has three reflecting panels placed in a Y configuration and supported by a central mast. Three crossed V dipoles are placed in the 120° sectors formed by the panels. This provides a more compact structure than the triangular tower.

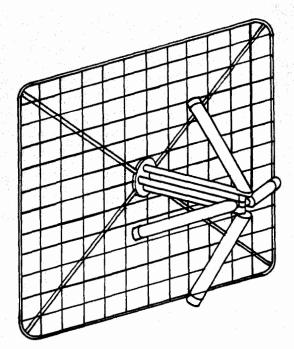


FIG. 28-7 Crossed V screen dipoles. (Courtesy of Jampro Antennas.)

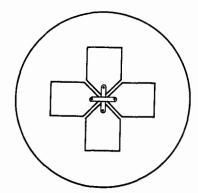


FIG. 28-8 Crossed dipoles in a cylindrical cavity.

A better technique for equalizing the azimuth beamwidth for vertical and horizontal polarization is to enclose flat crossed dipoles in a cylindrical cavity,6 as shown in Fig. 28-8. The use of cylindrical cavitybacked reflectors results in a good match of the vertically and horizontally polarized azimuth patterns. The length-to-width ratio of the flat dipoles is about 3 and provides a bandwidth of 10 percent with a VSWR less than 1.1:1. The cavity depth is 0.2 wavelength. The dipoles are fed in phase quadrature by two baluns forming a four-tube support structure. The circularity is ± 2 dB, and the axial ratio is less than 2 dB. The diameter of the cavity establishes the 6-dB beamwidth. Cavities with 0.65and 0.8-wavelength diameters have 6-dB

beamwidths of 120 and 90°, respectively. The quadrature feeding of crossed dipoles results in a broadband small VSWR. To maintain an axial ratio of less than 3 dB, it is essential that each one of the dipoles has a low VSWR over the band. This is achieved by placing a fan-shaped conducting screen (or flat sheet) over the crossed dipoles. This conductor acts as a common sleeve for both dipoles. By adjusting the dimensions of this

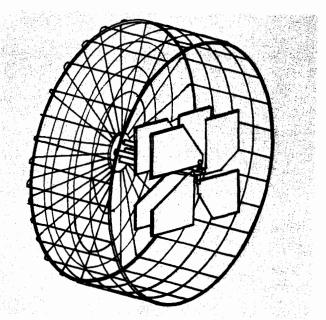


FIG. 28-9 Broadband cavity-backed antenna. (Courtesy of Jampro Antennas.)

sleeve and its height above the crossed dipoles, the axial ratio over the 20 percent bandwidth is improved considerably. Figure 28-9 shows a version of this concept.

Another approach is to place four half-wavelength dipoles in a square arrangement, with the side of the square being somewhat larger than a half-wavelength. The vertical and horizontal dipoles are fed in phase quadrature. Since the 6-dB azimuth beamwidth is about 90°, four panels around a square tower may be used for omnidirectional applications.

Stanted-Dipole Antennas

Many circularly polarized FM and TV broadcast antennas are based on the concept of a circular array of slanted dipoles. The dipoles may be linear, V-shaped, curved, or of similar configuration. Each dipole radiates linear polarization, but the slant angles and diameter of the circular array are adjusted so that an omnidirectional, circularly polarized radiation pattern is obtained. The term *circular array* is used here to include two or more dipoles placed on a circle with rotational symmetry. Figure 28-10 shows a circular array of several slanted dipoles uniformly spaced around a cylindrical conductor with a slant angle ψ . Figure 28-11 shows the coordinate system for this arrangement. If the dipoles are assumed to be fed in phase, the following is a simplified explanation of how circular polarization is achieved.

In a direction in line with opposite dipoles, the phases of the radiation from the vertical and horizontal components are vectorially added, whereas the horizontal compo-

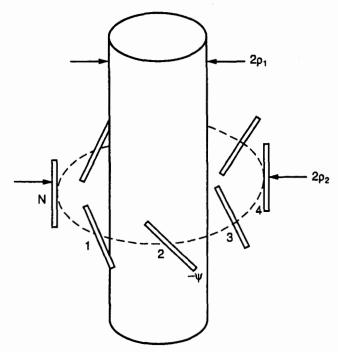


FIG. 28-10 N skewed (slamted) dipoles placed around a conducting cylinder.

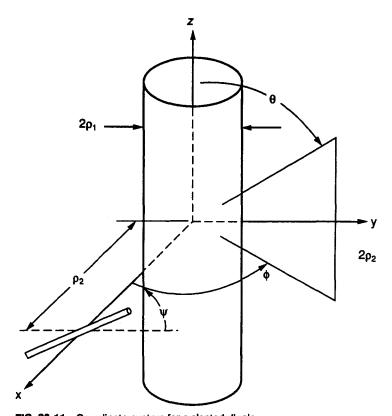


FIG. 28-11 Coordinate system for a slanted dipole.

nents are subtracted, which produces a 90° phase difference between the two polarizations. The slant angle is adjusted to produce equal magnitudes of vertical and horizontal polarization, taking into account radiation from the other two dipoles, which results in circular polarization. In general, N slanted dipoles may be placed in a circular array, of radius ρ_2 , and excited in mode M (an integer) to radiate omnidirectional circular polarization^{9,10} in the plane of the array.

In practice, the dipoles are placed around a support structure, such as a tower or a pole, with a maximum radius of ρ_1 and are fed with voltages of equal magnitude and a progressive phase shift of $360(M/N)^{\circ}$. The circularity of the pattern, in general, depends on the ratio ρ_2/ρ_1 , the number of elements N, and the mode number M. Given the mode number M, the required circularity WOW (the ratio of the maximum to the minimum electric field in decibels) of the azimuth pattern, the required number of dipoles in the circular array is given, approximately, by

$$N \approx 2.1 + 2.25M - 0.25(WOW) M/\beta \rho_2$$
 (28-12)

where $\beta = 2\pi/\lambda$. This formula is obtained by linear regression methods from a series of calculations. The end result is that the spacing between the dipoles must be about one-half wavelength for mode 0 and less than that for higher-order modes in order to obtain good circularity and low axial ratio.

In a circular array of short, slanted dipoles in free space, the vertical and the horizontal components of the field are equal in magnitude and are in phase quadrature if

$$\psi = \tan^{-1} \left(\frac{J_M''(\beta \rho_2)}{J_M'(\beta \rho_2)} \right)$$
 (28-13)

where J_M is the Bessel function of the first kind and the prime represents the derivative with respect to the argument. Positive values of ψ produce left-hand CP and negative values of ψ produce right-hand CP. Figure 28-12 shows the variation of ψ versus $\beta \rho_2/M$ for modes 0 to 4. The well-known Lindenblad antenna uses the mode 0 excitation.

The presence of a support structure introduces a phase error between the vertical and horizontal polarization components of the radiation which cannot be compensated for by changing the tilt angle ψ . Figure 28-13 shows the phase error (i.e., the deviation from the desired 90° phase between the two components) and the resulting minimum axial ratio versus $\beta p_1/M$ for modes 0 through 4. For mode 0, the pole diameter must be less than 0.03 λ in order to achieve low axial ratio. This is not practical for broadcast applications. As described below, short dipoles may be added to the tilted dipoles to compensate for the reflections from the support pole. It is apparent from the curves that for a given pole radius, we may increase the mode number M to a value such that the axial ratio is small. It is desired that the axial ratio be less than 3 dB and preferably less than 2 dB. Using linear regression curve-fitting techniques it is found that M must satisfy the following equation:

$$M \ge 0.8 - 0.13(AR) + [1.47 - 0.09(AR)]/\beta \rho_1$$
 (28-14)

where AR is the axial ratio in decibels. As an example, consider a Channel 2 antenna with a height of six wavelengths. A wind-loading analysis indicates that the mast diameter will be 20 in, for which $\beta \rho_1 = 0.304$. If we specify an axial ratio of 0.5 dB, we find that $M \ge 1.17$; i.e., we would have to use mode 2. If the axial-ratio requirement is relaxed to 1.6 dB, we then could use mode 1. We have now determined the number of radiating elements and

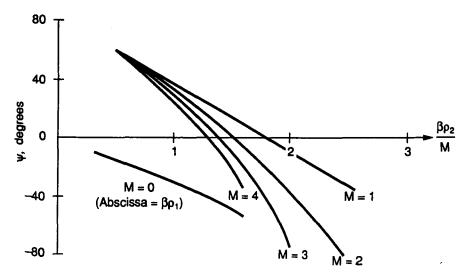


FIG. 28-12 Skew angles for a circular array of dipoles in free space for modes 0 to 4.

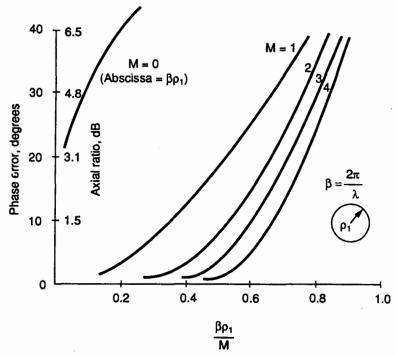


FIG. 28-13 Phase error and axial ratio for a circular array of skewed dipoles around a conducting cylinder.

the minimum mode number for the circular array of slanted dipoles. The dipole length is, in general, chosen to be about one-half wavelength because of low VSWR and low wind-loading requirements.

Figure 28-14 shows the slant angle versus $\beta\rho_2$ for several modes and pole diameters. It is concluded from several calculations that the optimal slant angle is insensitive to the pole size as long as the pole diameter is small enough to produce small phase errors. The reason for this is as follows. Modes different than 0 produce null tangential E fields on the z axis. The extent of the null region increases with the mode number. In other words, the field of the circular array, in the interior region of the array, is like a waveguide mode below cutoff. However, for larger pole sizes, the presence of the pole introduces a phase error that may require a change of tilt angle by 5 to 10°. Without this compensation, the axial ratio will increase by 1.6 to 3.1 dB.

Figure 28-15 shows one element of a circular array which consists of a slant half-wave dipole and a short vertical dipole that are fed and supported by a balun structure. For mode 0 and an array diameter of about one-half wavelength, only three elements are needed in the circular array to produce a circularity of ± 1.5 dB and an axial ratio less than 3 dB. The elements are fed in phase with equal power. The slant angle is approximately that given by Eq. (28-13) (without mast reflections), and the length of the vertical shunt dipole is adjusted to achieve a low axial ratio. A bandwidth greater than 10 percent may be

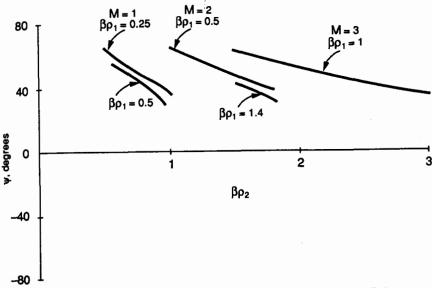


FIG. 28-14 Skew angles for a circular array of dipoles around a conducting cylinder.

achieved with a bay spacing of 0.8 wavelength. Thus the antenna may be used for both TV and FM applications. Since the wind loading is equal to or less than that for the batwing antenna, it may be used to replace the batwing on existing towers for conversion to circular polarization.

Figure 28-16 illustrates another version of this concept in which two V dipoles are supported by a horizontal mast.¹¹ With an included angle of about 90°, the V dipoles perform approximately as a four-dipole circular array. One half of each dipole is shunt-

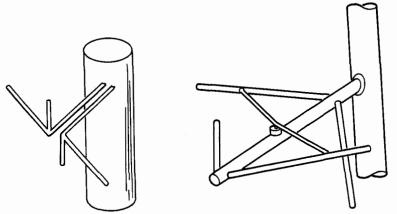


FIG. 28-15 Slant dipole with a parallel-connected vertical dipole.

Fig. 28-16 Two shunt-fed slanted V dipole antennas.

excited from the center of the support mast. If the dipole length is about one-half wavelength, then the current on the parasitic arms will be about the same as the current on the shunt-driven arms of the dipoles. The antenna is matched by adjusting the positions of the shunt feeds and the dipole lengths.

Alternatively, one-half of each dipole may be series-fed, as illustrated in Fig. 28-17, in which two dipoles are supported in a T arrangement. The internal coaxial feeds are connected to gaps in the monopoles. Since the impedance bandwidth is on the order of 1 percent or less, these antennas are most useful for FM applications. A multiplicity of bays with wavelength spacing may be fed and supported by a vertical transmission line. The array is usually supported on the side of a mast or tower. Reflections from the support distort the azimuth patterns, especially for vertical polarization, and degrade the axial ratio. Parasitic dipoles may be added to reduce these effects.

A circular array of four curved dipoles 12 is shown in Fig. 28-18. The dipoles form a short section of a four-arm helix antenna and are approximately one-half wavelength long. The array circumference is approximately one wavelength. Thus the overlap of the dipoles provides approximately the equivalent of a constant circular current distribution for both the horizontal and vertical components. The four dipoles are shunt-fed asymmetrically by four rods emanating from the center of the array. The rods are connected to the center conductor of a coaxial feed enclosed in the horizontal support structure. The same approach may be used for circular arrays of two or three curved dipoles when the array circumference is approximately one-half and three-fourths of a wavelength, respectively. The pattern circularity in free space is ± 1 dB, and the axial ratio is about 3 dB. The support mast or tower degrades these values by several decibels. The power rating and bandwidth increase with the number of dipoles in the array. An 11 percent bandwidth has been achieved for a four-element FM array with 2-in-diameter arms.

A single dipole may be bent in the form of a one-turn helical antenna to produce circular polarization. It may be fed by a slotted coaxial-line balun¹³ or by inductive loop coupling. A disadvantage is that it radiates up and down so that bay spacings of less than one wavelength must be used. For two or more dipoles in each bay there are nulls up and down for modes other than mode 1.

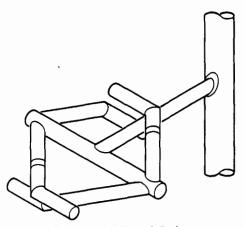


FIG. 28-17 Series-fed slanted dipoles.

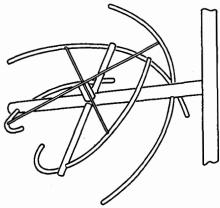


FIG. 28-18 Four shunt-fed helical-type dipoles.

Helical Antennas

The multiarm helix¹⁴⁻¹⁷ is a versatile antenna for radiating circularly polarized waves. Figure 28-19 shows a three-arm helix with a pitch angle ψ and radius ρ_2 wrapped around a conducting cylinder of radius ρ_1 , which forms the support for the antenna and allows

space for a transmission-line feed network for several bays of helices. For broadside radiation, the turn length of an arm is equal to M wavelengths, where M is an integer and defined as the mode number. For an N-arm helix, the arms are fed with equal powers and a phase progression of $360M/N^{\circ}$ such that the currents in the arms along a directrix of the helical cylinder are in phase. To obtain a low axial ratio and satisfactory radiation patterns, the number of arms N should be larger than the mode number M by a factor in the range of 1.5 to 2.0.



FIG. 28-19 Three-arm helical antenna.

The polarization characteristics may be calculated approximately by using a

continuous-current sheath model, wherein the currents flow along helical curves, have a free-space propagation constant, and the phase of the currents varies as $M\phi$, where ϕ is the azimuthal angle in a cylindrical coordinate system. The sheath current radiates a conical beam at an angle θ_0 (measured from the zenith) given by

$$\theta_0 = \cos^{-1}\left(\frac{\beta\rho_2 + M\cos\psi}{\beta\rho_2\sin\psi}\right) \tag{28-15}$$

where β is the propagation constant along the directrix and is approximated by the free-space value of $2\pi/\lambda$.

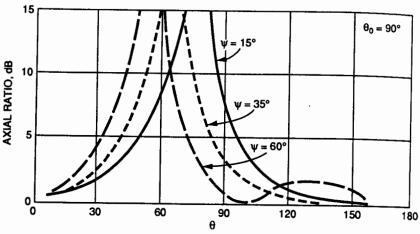


FIG. 28-20 Axial ratio versus elevation angle for a helical antenna.

For broadside radiation ($\theta_0 = 90^\circ$), without the conducting cylinder present, the ratio E_θ/E_ϕ is given, approximately, by

$$\frac{E_{\theta}}{E_{\phi}} \approx j \frac{J_{\mathcal{M}} \left[\beta \rho_{2} \sin\left(\theta\right)\right]}{J_{\mathcal{M}}' \left[\beta \rho_{2} \sin\left(\theta\right)\right]} \left[\frac{\sin\left(\psi\right) \sin^{2}\left(\theta\right) - \cos\left(\theta\right)}{\sin\left(\theta\right) \cos\left(\psi\right)}\right]$$
 (28-16)

where J_M is a Bessel function of the first kind and the prime represents the derivative with respect to the argument. Figure 28-20 shows the variation of axial ratio with elevation angle for three values of the pitch angle ψ and for M=2. The axial ratio is rather insensitive to the mode number.

The left-hand helix of Fig. 28-19 radiates left-hand CP toward the zenith, right-hand

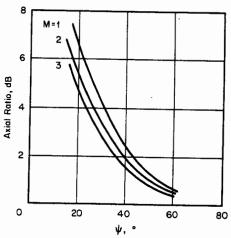


FIG. 28-21 Axial ratio versus pitch angle in the broadside direction from a helical antenna.

CP toward the nadir, and horizontal polarization at an elevation angle of approximately ψ . Figure 28-21 shows the variation of the axial ratio in the broadside direction with the pitch angle ψ for modes 1 to 3 (with no conducting cylinder present). It is seen that the average pitch angle should be at least 40° to achieve an axial ratio less than 3 dB. If the cylinder circumference in wavelengths is greater than about M-1, for M>1, then reflections from the cylinder produce a phase error between the vertical and horizontal polarizations which degrades the axial ratio by more than that shown in these figures.

Figure 28-22 shows the variation of the phase error and axial ratio (assuming 0-dB axial ratio without the cylindrical conductor) versus $\beta \rho_1$ for modes 1 through 6. Assuming a maximum phase error of 5°, the maximum diameter of the cylinder may be calculated from these curves. The spacing of the helical wires from the cylinder is a function of the helix circumference, which is given by

$$\beta \rho_2 = M \cos(\psi) \tag{28-17}$$

Assuming $\psi = 40^{\circ}$ and the 5° phase error, it is deduced that the spacing between the helical wires and the core is on the order of 0.1 wavelength. For mode 1, the circumference of the cylinder should be less than one-half wavelength.

The uniform helix is a traveling-wave antenna with an exponential attenuation rate which is a complex function of M, N, ψ , cylinder diameter, and arm diameter. Figure 28-23 shows the variation of attenuation per wavelength along the axis of the helix versus the pitch angle for a mode 3 four-arm helix. These experimental results hold for cylinder diameters of 0.08 to 0.24 wavelength and for a small wire diameter. Similar results are obtained for other modes and numbers of wires. The attenuation also may be computed with a method-of-moments wire-antenna computer program wherein the cylinder is approximated by N axial wires for an N-wire helix. The attenuation increases with arm diameter and decreases with pitch angle. Attenuation rates of up to 6 dB per axial wavelength may be achieved by using wide strips or larger-diameter helix arms. To approxi-

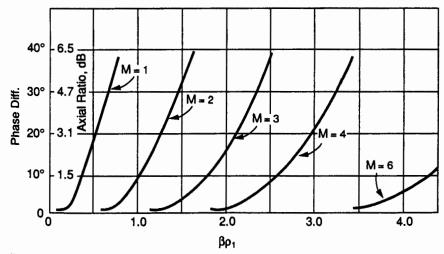


FIG. 28-22 Axial ratio and phase errors for various modes of a helical antenna with a conducting cylinder.

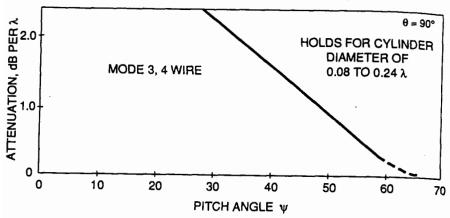


FIG. 28-23 Attenuation versus pitch angle of a helical antenna.

mate a uniformly illuminated aperture, the pitch angle may be varied along the aperture (keeping the turn length constant), which leads to a spiral-type structure. If 2M/N is not an integer, the reflected wave from the end of the helix will radiate a beam in an elevation direction other than broadside. If this is not the case, the reflected wave will radiate a broadside beam, which produces scallops in the azimuth pattern with 2M lobes. The axial ratio is not degraded because the sense of circular polarization for the reflected wave is the same as that for the incident wave in the broadside direction. This effect may be reduced by terminating the helix with radiating loads or resistors. The helix is usually designed so that the one-way attenuation is about 15 dB.

Because the helix is a traveling-wave antenna, the impedance bandwidth is large, especially if 2M/N is not an integer, since reflection cancellation occurs at the input to the feed network. However, the pattern bandwidth is limited by beam scan with frequency because it is equivalent to an end-fed array. For desirable pitch angles, the beam of a helix bay scans about 1° for a 1 percent frequency change. For Channels 2 to 6, this limits the bay length to about two to three wavelengths. Thus two or more bays are generally used. A three-arm mode 1 helix may be used for these channels and has less wind loading than a horizontally polarized batwing antenna. In order to obtain large attenuation, each arm usually consists of a wide strip or two widely spaced rods which have cross-bar connectors spaced at intervals of less than a quarter of a wavelength.

For Channels 7 to 13, bay lengths of six wavelengths may be used. Three- or four-arm mode 2 helices are used. In the UHF band, bay lengths may be in the range of 16 wavelengths, and mode numbers of 5 or more are used, with the number of arms being greater than the mode number.

Because of their symmetry, helical and spiral antennas have an excellent omnidirectional pattern, with a circularity of less than ± 1 dB. The axial ratio is about 2 dB for the low VHF channels and even less for the other channels. The arms of a helical antenna have a characteristic impedance similar to that of a rod over a ground plane, with the height equal to the spacing of the arm from the support cylinder. Thus special techniques such as inductance-capacitance tuners or transformers are required to match this impedance to the outputs of the power splitter in the feed network for the multiarm helix.

A novel feature of the higher-order-mode multiple-arm helical antenna is that it may be placed around triangular or square towers and still produce an omnidirectional pattern. This occurs because the waves radiated toward the support structure with a $360M^{\circ}$ azimuth phase variation enter a cutoff region in a manner similar to that for radial waveguides. Thus the waves are reflected, and the support structure has little effect on the radiation pattern if the mode number is about 5 times larger than the tower diameter in wavelengths.

The design of a multifilar helix antenna to produce circularly polarized omnidirectional radiation for TV or FM broadcast application makes use of the preceding information and usually starts by determination of the mode number. The mode number depends on the diameter of the support mast, which is determined from the antenna height (or gain) and environmental considerations such as wind or ice loading. The mode number is chosen such that the helix circumference is about one-half wavelength greater than the support circumference for the assumed pitch angle.

The number of bays should be minimized in order to minimize the cost of the feed network. The length of the single bay is limited by the amount of beam scan with frequency. The amount of beam scan depends on the pitch angle and the design bandwidth. The total beam scan over the channel may be determined for a given pitch angle. The maximum bay length is determined from the specified antenna gain variation.

The number of arms N usually is set equal to 3 and 4 for modes 2 and 3, respectively. For the higher-order modes, N may be less than M.

Figure 28-24 is a picture of a three-layer helical antenna which was designed for multichannel FM broadcast. ¹⁸ This antenna is rated at 160 kW for simultaneous broadcast of six FM stations at Healy Heights, Portland, Oregon. The bay length was restricted to about three wavelengths for beam stability and to satisfy the power-capacity requirement. Excellent attenuation along the helix was achieved by using multiple conductors in each arm of the helix. A definite advantage of this antenna over panel arrays is the simplicity of the feed system. In this antenna, the feed system consisted of four three-way power dividers and the coaxial lines that fed the arms, which is simple when compared with the more elaborate feed system of a panel antenna with the same gain.

Ring-Panel Antennas

The ring-panel antenna¹⁹ consists of a multiplicity of ring radiators fed in series by a transmission line. Figure 28-25 shows two circular rings formed by strips over a panel and connected by rods over the panel which provide simple, low-radiation transmission lines. The ring circumference is approximately one wavelength, as is the spacing between rings. The antenna is designed so that the characteristic impedance of the transmission-line rod over ground is the same as the strips over ground. A practical value of the characteristic impedance is 140 Ω . By using a resistive termination on the last ring and/or special tuning techniques, it is possible to achieve a traveling-wave type of antenna.

A traveling wave on a ring of one-wavelength circumference, as shown in Fig. 28-25, radiates right-hand CP. The ring is equivalent to four quarter-wave dipoles placed on a square with -90° progressive phasing. The azimuth beamwidth for horizontal polarization is usually about 10° less than that for vertical polarization. The beamwidth may be equalized and changed by means of parasitic elements such as monopoles on each side of the rings and/or dipoles in front of the rings. A cavity is not required.

Figure 28-26 shows the variation of attenuation through a ring versus its height above the panel for two strip widths W. The radiation from, or the attenuation through,

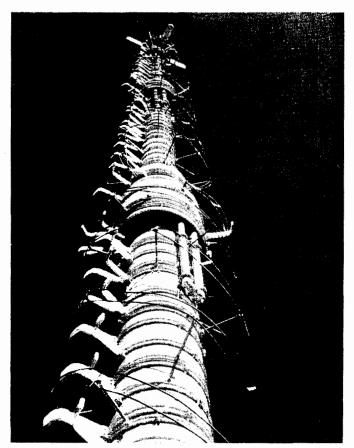


FIG. 28-24 A three-arm mode 2 helical antenna for multichannel FM broadcasts. (Courtesy of Jampro Antennas.)

the traveling-wave ring increases with the height of the ring above the panel and decreases with the width of the strip. These theoretical results were obtained with a method-of-moments computer program for a single ring with a matched resistive termination at the ground plane. A rod with a diameter equal to W/2 was used to simulate the strip width. The computer program does not give accurate results for large strip widths. Experimental results have shown that attenuations of 6 to 8 dB for $H/\lambda = 0.2$ may be obtained with larger strip widths. The axial ratio of the ring radiator increases with the ring height from a small value to 2 to 4 dB for $H/\lambda = 0.2$. Because of this attenuation, it is necessary to increase the height of the rings as one progresses from the feed point in order to approximate a uniform array.

Since the distance along the transmission line and ring between similar points on adjacent rings is two wavelengths for broadside radiation, the beam direction will scan

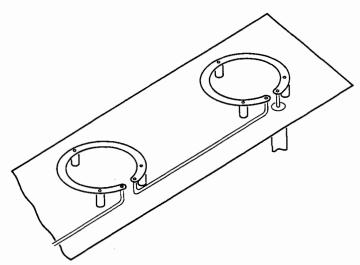


FIG. 28-25 Two elements of a series-fed traveling-wave ring-panel antenna.

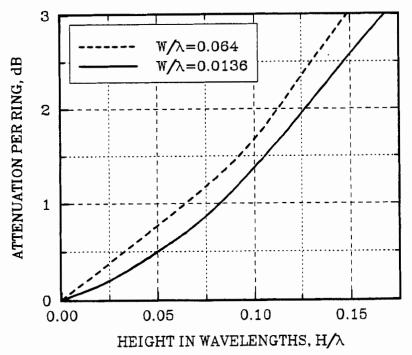


FIG. 28-26 Attenuation versus height in wavelengths.

1.15° for a 1 percent change in frequency. This limits the number of end-fed rings to 3 for Channel 2 and about 10 for the UHF channels.

The axial ratio may be reduced to a very low level by introducing reflections on the transmission-line rods which radiate left-hand CP waves. The magnitude and phase of the reflections may be controlled by the size and position of the reflecting devices to cancel undesired left-hand CP from other parts of the antenna.

There is undesired radiation from the rods which connect the ring to the transmission line over the panel. This may be reduced by using a small spacing between the rods and by adjusting the ring diameter so that the distance between the midpoints of the rods, as measured through the ring, is one wavelength. This ensures that the two currents at the rod midpoints are 180° out of phase, which reduces the radiation from the rods.

Several panels may be stacked vertically to achieve the desired gain and beamwidth. Beam tilt and null fill may be achieved by control of the amplitude and phase of the radiation from each ring and by the height of the ring and the transmission-line rod length, respectively.

28-4 HORIZONTALLY POLARIZED ANTENNAS

Reference may be made to the First Edition of the Antenna Engineering Handbook for descriptions of loop, cloverleaf, V, and other types of horizontally polarized antennas which were popular before the use of circular polarization (CP).

Dipole-Panel Antennas

A dipole-panel type of antenna is illustrated in Fig. 28-27. The dipole is usually about a half wavelength long and spaced about a quarter wavelength from the panel. The spacing between the reflector and the dipole may be used to control, to a limited extent, the azimuth beamwidth of the radiation pattern. The dipole may be fed from a balanced transmission line connected to the center of the dipole (not shown) or from a coaxial line entering one of the support arms and extending to the central feed gap, forming a balun. A bandwidth of 10 percent may be achieved with a compensated balun²⁰ and/or by using

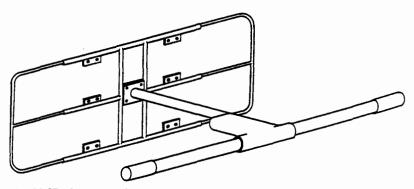


FIG. 28-27 Dipole-panel antenna.

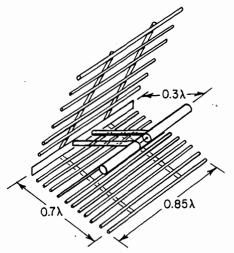


FIG. 28-28 Right-angle corner-reflector antenna.

open sleeves.²¹ Straight dipole panels are placed on square towers to obtain omnidirectional or directional patterns.

Corner-Reflector Antennas

Four corner-reflector antennas with a 90° apex angle, as shown in Fig. 28-28, may be placed around a square tower to obtain horizontally polarized omnidirectional patterns. For the dimensions shown, the azimuth pattern has a 6-dB beamwidth of 90°. When four such corner reflectors are mounted on a square tower with a face dimension of 0.7 wavelength, the resulting omnidirectional pattern has a circularity of ± 1.5 dB. The gain of the corner-reflector antenna shown in Fig. 28-28 is 9 dBd (gain relative to a dipole), which is about 3.5 dB higher than the gain of a dipole panel. The higher gain is an advantage for the corner-reflector antenna when compared with a dipole-panel antenna. For a specified gain, the required number of corner reflectors is less than the required number of panel antennas; this results in a simpler feed system. The VSWR bandwidth of the corner-reflector antenna is typically 10 percent. By using sleeved dipoles and compensated baluns, the bandwidth can be extended to over 20 percent. The finite sizes of reflectors affect the gain, the front-to-back ratio of the field strength, as well as beam shape. The data reported by Wilson, Cottony, and Ohba²²⁻²⁶ are useful in gaining insight into the proper design of the width and length as well as the element-to-apex distance. A slanted dipole in a corner reflector²⁷ produces elliptically polarized radiation. Circular polarization (CP) may be obtained by adjusting the tilt angle and the apex-to-dipole spacing.

Batwing Antennas

The batwing antenna²⁸⁻³⁰ is the most popular horizontally polarized VHF TV antenna. A single bay of a batwing antenna is shown in Fig. 28-29. Typically, a batwing antenna consists of several bays of turnstile configurations of four broadband planar wings labeled

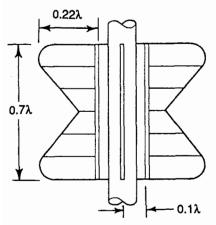


FIG. 28-29 Batwing or superturnstile antenna.

as "East-West" and "North-South." The wings are formed by a grid of rods. Each wing is supported by spacer bars which are shorted to the supporting mast at the top and bottom of the wing. The wings are fed via a triangular-shaped jumper at the midpoint between the space bars. The shape of the jumper, as well as the spacing between the wing and the pole, affects the input impedance.31 The shape of the jumper affects the reactance while the wing-to-pole spacing affects the resistance of the element The four wings are fed in mode 1 (90° phase progression) via coaxial cables. Opposite wings are fed 180° out of phase with equal-length cables. One wing is fed from a coaxial line grounded to the mast with the center conductor connected to the element

at the midpoint between the spacers. The opposite wing is fed from a coaxial line running along the inner edge of the element and with the center conductor connected to the mast midway between the space bars.

The 90° phasing of the quadrature wings may be obtained by different line lengths or from a quadrature hybrid. In the latter case, the visual and aural transmitters may be diplexed into the antenna system by insertion of the visual signal into one port of the hybrid and the aural signal into the other port. The isolation between the two ports is about the same as the return loss from the dipoles, which is greater than 26 dB. The impedance of the wing in the array varies between 72 and 79 Ω and depends on the "effective pole diameter" (diameter of the pole and the feed lines that are attached to the pole). A 20 percent bandwidth with a return loss greater than 26 dB can be achieved with relative ease.

The wings have nulls in the nadir and zenith directions. Thus the bays may be spaced by one wavelength to achieve maximum gain. Figure 28-30 shows a three-bay VHF batwing antenna under test. The azimuth pattern circularity depends on the frequency and the pole diameter. Circularities of better than ± 1 dB at low VHF and ± 2 dB at high VHF are common. For large pole diameters and modes other than mode 1, equations derived by Carter³² for radial monopoles on circular cylinders may be used to predict the azimuth pattern. By increasing the number of elements and using a higher-order mode, it is possible to achieve circular patterns on large cylindrical poles. A mode 2 batwing array composed of eight wings equally spaced around a cylinder 12 ft in diameter on the top of the John Hancock building in Chicago produced a circular pattern within ± 0.5 dB having a bandwidth of about 15 percent at Channel 2.

Zigzag-Panel Antennas

The panel-type zigzag antenna³³ shown in Fig. 28-31 is a simple type of traveling-wave antenna which may be placed around triangular or square towers to produce a wide variety of azimuth patterns. The antenna consists of a wire or rod that is bent at half-wavelength intervals to form the zigzag structure. This provides a broadside beam with horizontal polarization, since the radiation from the vertical components of the currents in adjacent half-wavelength segments cancels, whereas that for the horizontal components

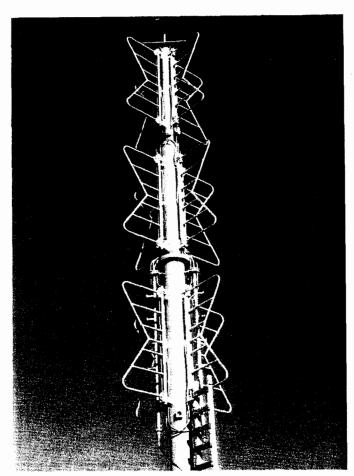


FIG. 28-30 A three-bay batwing antenna. (Courtesy of Jampro Antennas.)

adds. The azimuth 6-dB beamwidth is about 90°, which is desirable for a square tower. It is preferable to feed the zigzag in a balanced manner at the center of one rod as shown, which eliminates radiation from the feed structure. If an unbalanced feed is used, e.g., at the bend, the feed radiation will distort the azimuth pattern.

The zigzag may be designed on the basis of a leaky-wave antenna, in which the attenuation per wavelength due to radiation increases with distance from the feed point. Figure 28-32 shows the attenuation per axial wavelength versus the height of the zigzag above the panel for several pitch angles. The rod diameter and band radius are 0.01 and 0.03 wavelength, respectively. To simulate a uniform aperture distribution, the pitch angle decreases with distance from the feed point and is adjusted along with the height of the zigzag to give a one-way attenuation of about 15 dB for the current on the zigzag. It is preferable and simpler to use a constant-height zigzag. Since the beam direction of the

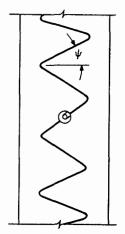


FIG. 28-31 Zigzag antenna with balanced feed.

incident and reflected waves on each half of the zigzag scan with frequency but in the opposite directions, the length of a zigzag panel is limited by the bandwidth of the channel. The average pitch angle is usually about 35°, which produces a beam scan of 1° per 1 percent change in frequency. For UHF, panel lengths of 16 wavelengths may be used.

Since reflections occur at each bend, it is necessary to compensate for these in order to achieve a traveling-wave antenna. For a bend radius of 0.05 wavelength, the reflection coefficient varies over the range of 0.1 to 0.2 for practical pitch angles and heights of the zigzag. These reflections may be reduced considerably by placing the support insulators 0.125 wavelength before each bend as viewed from the feed point. It

is usually necessary to add shunt-capacitive tuners along the zigzag to achieve a travelingwave condition, which is required for a wide-impedance bandwidth.

A convenient method of measuring the VSWR on the zigzag rod is to use a small balanced loop probe and slide it close to and along the rod, with the rod lying in the plane of the loop. The loop measures the current on the rod.

Beam tilt may be achieved by displacing the feed from the center of the middle zigzag element or changing the lengths of the rods from the feed to the upper and lower zigzags. An alternative technique is to vary the distance between bends so as to produce a progressive phase shift which in turn gives the desired beam tilt.

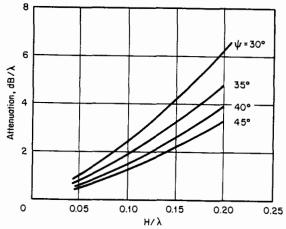


FIG. 28-32 Attenuation of a zigzag antenna versus height.

Slot Antennas

Because of their structural simplicity and ease of feed design, slot antennas are particularly useful for high VHF and UHF applications where high gain and low wind load are of critical importance and the required bandwidth is 1 to 3 percent. The majority of broadcast slot antennas are horizontally polarized. These are vertical arrays of half-wave axial slots placed around a cylindrical pole and fed from one end of the transmission line.

The end-fed slot antenna is a progressively phased linear array. The direction of the main (an all higher-order) beam(s) of such an array³⁴ is denoted by θ_M and is given by

$$kd\cos\left(\theta_{M}\right) - \sigma = 2M\pi \tag{28-18}$$

where d is the element spacing, σ is the phase progression per element, M is an integer that denotes the order of the beam, and $k = 2\pi/\lambda$. For slots on a transmission line,

$$\sigma = \frac{2\pi}{\lambda_s} d \tag{28-19}$$

where λ_g is the wavelength in the transmission line and is a function of the propagating mode in the transmission line. Combining the two, we obtain

$$\cos\left(\theta_{M}\right) = M\frac{\lambda}{d} + \frac{\lambda}{\lambda_{x}} \tag{28-20}$$

All coaxial-type slot antennas are designed to operate in the TEM mode for which $\lambda_g = \lambda$. In order for θ_M to be real, it is necessary that M = 0 or M = -1. For M = 0, the beam is along the axis of the line regardless of the spacing between the slots. This beam is actually suppressed because of the low level of slot radiation in this direction. For M = -1, we obtain

$$\theta = \cos^{-1}\left(1 - \frac{\lambda}{d}\right) \tag{28-21}$$

Equation (28-21) shows the dependence of the beam tilt on the slot spacing. It also demonstrates the "beam-scanning" (dependence of the direction of the main beam on the frequency) characteristic of end-fed slot antennas.

Depending on the spacing between the slots of a uniformly spaced array, the slot antenna may be either "standing-wave" or "traveling-wave." When the slots in the axial array are spaced by exactly one wavelength λ_g in the transmission line (coaxial line or waveguide) and the transmission line is fed from one end, the slots are all in phase and the main beam is broadside. The slot array is then referred to as resonant or standing wave. We refer to a slot antenna as traveling wave when the slots are spaced less than or greater than λ_g and the transmission line is terminated by a matched load. This array is progressively phased, and the main beam is tilted toward the feed end or the termination end when the spacing is less than or greater than λ_g , respectively. For a narrow-beamwidth slot array at a large tower height, it usually is desirable to point the beam below the horizon; this results in a traveling-wave mode for the slotted array.

Most standing-wave slot antennas are of the coaxial type. However, owing to the limited power capacity of the coaxial lines, their application is limited to powers of 100 kW or less. Owing to the absence of an inner conductor, waveguide slot antennas have higher power capacity than coaxial ones. Circular waveguides are generally used, in traveling-wave designs, for high-power applications. Power ratings of up to 250 kW are common for the waveguide slot antennas.

The azimuth pattern as well as the impedance of a slot on a cylindrical pole is the same whether it is an element of a standing-wave or traveling-wave antenna. They both, however, depend on the normalized circumference ka of the cylinder, where a is the radius and $k = 2\pi/\lambda$. The azimuth pattern $E(\phi)$ of a single slot (at $\phi = 0^-$) on a cylinder of radius a is given by 35

$$E(\phi) = \sum_{m=0}^{\infty} \left[\frac{\epsilon_m \exp(im\pi/2) \cos m\phi}{H_m^{(2)}(ka)} \right]$$
 (28-22)

where $\epsilon_m = 1$ for m = 1 and $\epsilon_m = 2$ when m > 1, $H_m^{(2)}$ is the Hankel function of the second kind, and the prime indicates the derivative with respect to the argument. Normally, the

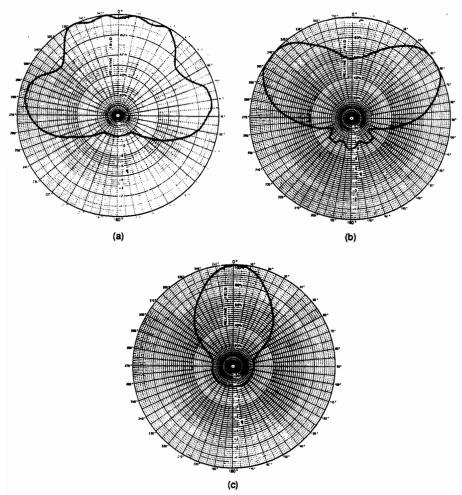


FIG. 28-33 Directionalized pattern of slot antennas. (a) Directivity 1.8, (b) directivity 2.4, (c) directivity 4.0. (Courtesy of Jampro Antennas.)

first 3ka terms of the series are sufficient for accurate results. For coaxial-type slot antennas the value of ka ranges between 1 and 1.5, whereas for the waveguide type the range is typically 2.5 to 3.5. The azimuth pattern may be controlled by either using reflectors on the sides of the slots or using combinations of slots around the pole. The pattern of a single slot is skull-shaped, and its circularity ranges from 6 to 10 dB for ka = 1 to ka = 3.5, respectively.³⁵ Figure 28-33 shows some typical patterns that are achievable by using reflectors on the sides of the slot on a cylinder. Equation (28-22) in conjunction with Eq. (28-9) (with $R_n = 0$) may be used to predict the pattern of several slots around a cylindrical pole. Typically, two opposite slots produce a peanut-shaped pattern and three slots produce a trilobed pattern. Between four and six slots are needed to achieve a circular azimuth pattern. The pattern circularity depends on the diameter of the cylinder. Figure 28-34 shows the variation of circularity as a function of ka.

The radiation conductance of a single resonant slot on a cylindrical pole depends on the radius of the pole. For values of ka between 1 and 3.5, the radiation conductance varies between 0.8 and 0.93 m Ω , respectively. The presence of reflectors increases the conductance by a factor of $2\pi/\psi$, where ψ is the angle between the reflectors. ³⁵ The active admittance of a slot in an array around a cylinder is quite different from that of an isolated slot.

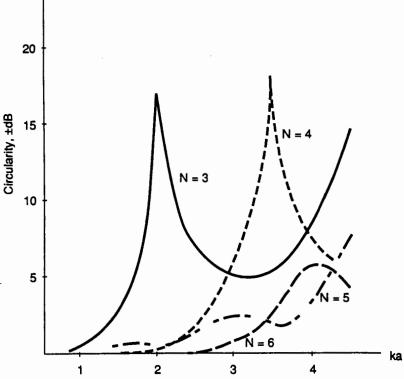


FIG. 28-34 Azimuth pattern circularity versus ka.

However, since the coupling between axially displaced slots is much less than the coupling between the circumferentially displaced slots, ³⁶ the admittance of a single layer of the slot antenna is measured directly and the complete array is then modeled as a cascaded circuit using these empirical data. ³⁷ It should be pointed out that the coupling between the azimuthally displaced slots of adjacent layers is significant and should be included for accurate modeling of the array. ³⁶

Low- to medium-power slot antennas, in general, are coaxial-type standing-wave slot antennas. The array usually is divided into subarrays, each fed independently. Each subarray consists of four to eight layers of slots and is fed at the center. One side of each slot, at its midpoint, is either directly connected to the inner conductor or coupled to the coaxial line by means of a capacitive probe or an inductive loop. 38 The inner conductor is usually extended beyond the feed points of the end slots. These extensions act as shunt-open-circuited stubs that may be used to increase the bandwidth of the subarray. The location of the feed points and the length of the end stubs are kept symmetrical with respect to the center of the subarray to maintain uniform phase along the aperture of the subarray. The beam tilt and the null fill are achieved by offsetting the phases and amplitudes of the subarrays.

The center-fed slot arrays are fed either directly from the side at the center of the array or, in the case of a top-mounted array, at the bottom by means of a triaxial line that extends to the center of the array. In this latter case, the open-end extensions are replaced by adjustable shorts.

The bandwidth of the subarray depends on the frequency and outer diameter of the coaxial line. For instance, a center-fed subarray of eight axial slots produces a 5 percent bandwidth if the pole diameter is 6 in for the frequency range of 470 to 590 MHz, 5 in for the range of 590 to 690 MHz, and 4 in for the range of 690 to 810 MHz.

The traveling-wave slot antenna is an end-fed coaxial or waveguide transmission line with a slotted outer conductor and a matched termination at the far end. The slots are collinear along the transmission line and are spaced shorter than a wavelength of the propagating mode in the transmission line. The placement of the slots around the cylindrical conductor depends on the specified azimuth pattern. Each slot is coupled to the fields in the transmission line by means of an adjustable probe or a minor tilt of the slot from the axial direction. Each column may be considered as an array of progressively phased elements.

The excitation amplitude of each slot is established by an adjustment of the coupling mechanism, and the phase is established by the location of the slot along the transmission line. When coupling is the same for all slots, an equal percentage of power is transmitted from one layer of slots to the next, which results in an exponential power distribution in the array. This produces an excessive null fill in the elevation pattern, and it also may cause breakdown in the first few layers of slots in high-power applications. An approximately uniform excitation is achieved by progressively increased coupling. The last few slots at the end of the array are spaced by one wavelength and are connected directly to the inner conductor. This resonant subarray at the end, when matched, serves as the matched termination of the traveling-wave array.

Figure 28-35 shows a variation of a traveling-wave slot antenna³⁹ in which the slots are arranged in pairs at each layer, with the pairs separated by a quarter wavelength along the length of the antenna. Adjacent pairs occupy planes at right angles to each other. The slot pairs are fed out of phase by the coaxial line to produce a figure-eight pattern. The adjacent in-line slots are spaced slightly less than a wavelength to provide a downward beam. The quarter-wavelength separation of layers in conjunction with the space-quadrature arrangement of successive layers of slots operates as a turnstile-type feed which

produces an azimuth pattern with circularity of ± 1 dB. Furthermore, reflections from adjacent layers tend to cancel, which reduces the overall return loss over a wide range of frequencies.

The absence of a center conductor in cylindrical waveguides makes them attractive for high-power applications. The diameter of this antenna is almost twice the diameter of its coaxial counterpart. Consequently, it requires more slots around the pole to produce a circular pattern.

The configuration of the waveguide traveling-wave slot antenna is somewhat



FIG. 28-35 Traveling-wave slot antenna.

different from the coaxial type. The dominant mode of cylindrical waveguide is the TE₁₁ mode, ⁴⁰ which is not circularly symmetrical and is not suitable for slot antennas with an omnidirectional azimuth pattern. This mode is used in slot antennas with skull-shaped, peanut-shaped, or other directional patterns. The next higher-order mode is the TM₀₁, which is similar to the TEM mode of the coaxial line. This mode is symmetrical and is suitable for omnidirectional patterns. For both these modes $\lambda_g > \lambda$. By choosing the inner radius a of the cylinder such that $a = 0.44\lambda$ for the TM₀₁ mode and $a = 0.33\lambda$ for the TE₁₁ mode, the wavelength in the waveguide will be twice that of the free space, i.e., $\lambda_g = 2\lambda$. It is then possible to space the slots by one free-space wavelength and alternately place the feed probes, or bars, on the opposite sides of the adjacent slots. The direction of the main beam of a waveguide slot antenna is given by

$$\theta = \cos^{-1}\left(\frac{\lambda}{\lambda_s} - \frac{\lambda}{2d}\right) \tag{28-23}$$

where d is the spacing between the slots. For broadside radiation, $d = \lambda$ and $\lambda_g = 2\lambda$, and the array becomes resonant. When $d \neq 2\lambda_g$ and there is a matched termination at the far end, the array becomes a traveling-wave array with the main beam at some angle other than broadside. The angle of the main beam is determined by Eq. (28-23).

The coupling of power to the slot is accomplished by an L-shaped probe that is placed at the midpoint along the side of the slot. The dimensions of the probe are adjusted to produce a gradual attenuation along the waveguide and uniform excitation of the slots.

An important factor in the design of the waveguide antenna is the single-mode operation. Maintaining the polarity of the mode in the TE_{11} type of antenna is essential to the uniform excitation of all slots. To prevent the azimuthal rotation of the field along the waveguide, use is made of horizontal rods that are positioned transversely in the guide in the plane perpendicular to the E field. In the TM_{01} type of antenna, any deviation from circular symmetry results in excitation of the dominant TE_{11} mode, which affects excitation of the slots. This distorts the azimuth pattern, reduces the gain, and increases the level of the sidelobes.

A combination of vertically polarized radiators and axial slots may be used to achieve circular polarization. Figure 28-36 shows a design in which dipoles are placed in between the adjacent slots and are fed separately from the slots. The dipoles are placed collinear with slots along the axis or in between slots around the cylinder. The power is coupled to each dipole by means of a probe that extends inside the transmission line. The height and number of dipoles determine the circularity of the vertical polarization pattern.

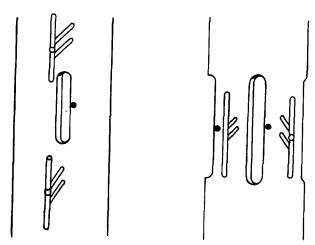


FIG. 28-36 Examples of dipole slot circularly polarized antennas.

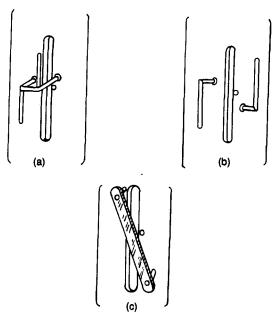


FIG. 28-37 Examples of slots combined with parasitic radiators for CP radiation.

The phase and amplitude of each dipole are adjusted by the location and extension of the

probe, respectively.

Figure 28-37a shows another design in which a slant half-wavelength parasitic bar is placed in front of each slot. The parasitic bar is directly connected, near its midpoint, to the sides of the slot. The height above the slot depends on the slant angle. For a vertical bar, the height above the slot is about a quarter of the wavelength. In another design, shown in Fig. 28-37b, two L-shaped bars are placed on the sides of the slot. In another design, shown in the two bars are adjusted empirically to achieve an optimal axial ratio. Figure 28-37c is a slot-cross-loop arrangement for producing CP radiation. The amplitude and phase of the vertical polarization are optimized by adjusting the height and slant angle of the bar.

28-5 MULTIPLE-ANTENNA INSTALLATIONS

The limited number of available antenna sites and financial considerations force many broadcasters to share a single site or a single tower. In some cases, several broadcasters share the same tower top in a candelabra arrangement³ in which antennas are mounted on the corners of a triangular support structure with a separation of 50 to 100 ft. In other cases, antennas are stacked vertically on several towers all sharing the same site and all in close proximity. A problem with such installations is that reflections from other towers and antennas in the proximity produce ripples in the pattern and/or in some situations echoes of the transmitted signal. The ripples in the pattern are sensitive to frequency. This results in a fairly strong variation which leads to distortion of the received signal in all directions. In general, it is impractical to theoretically model the scattering from complex antenna-tower structures. However, the scattering characteristics of circular cylinders are well known and can be used, by assuming an equivalent cylinder for each tower, to study the extent of deterioration in the azimuth pattern due to the presence of nearby structures.⁴⁴⁻⁴⁶

Echo^{47,48} (or ghost in the case of television signal) becomes an additional problem when the separation between the transmitting antenna and the reflecting tower exceeds 1000 ft. In general, a 2 to 3 percent echo with a 1- μ s delay becomes noticeable as a ghost to a television viewer. Delays shorter than 0.25 μ s are hardly noticeable. A 1- μ s delay corresponds to 984 ft (the distance that light travels in 1 μ s) of path difference between the original and the reflected signal. The signal-echo path difference and the echo displacement on a 19-in television screen are related by the following equation:

Displacement (in) = $0.000295 \times \text{path difference (ft)}$

The strength of the echo may be estimated by calculating the coupling to and from the scatterers,

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TV Receiving Antennas

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29-1	FCC Television Frequency Allocations 29-2
29-2	TV Signal-Strength Estimation 29-3
29-3	TV Receiving Systems 29-5
	Overview of TV Antenna Types 29-5
	Transmission Lines for TV Receiving
	Systems 29-6
	TV Receivers 29-9
29-4	TV Receiver-System Noise 29-9
29-5	Triangular-Dipole Antennas 29-12
29-6	Loop Antennas 29-12
29-7	Log-Periodic Dipole Array Antennas 29-14
29-8	Single-Channel Yagi-Uda Dipole Array Antennas 29-16
29-9	Broadband Yagi-Uda Dipole Array Antennas 29-19
29-10	Corner-Reflector Antennas 29-21

29-1 FCC TELEVISION FREQUENCY ALLOCATIONS

The Federal Communications Commission (FCC) frequency allocations for commercial television consist of 82 channels, each having a 6-MHz width. Channels 2 through 6 are known as the low-band very high frequency (VHF) and span 54 to 88 MHz, Channels 7 through 13 are known as the high-band VHF and span 174 to 216 MHz, and Channels 14 through 83 are known as the ultrahigh-frequency (UHF) band and span 470 to 890 MHz. Channels 70 through 83 are designated for translator service. Channel designations and frequency limits are given in Table 29-1.

TABLE 29-1 Designations and Frequency Limits of Television Channels in the United States

Channel desig- nation	Frequency band, MHz	Channel desig- nation	Frequency band, MHz	Channel desig- nation	Frequency band, MHz
2	54-60	30	566-572	57	728-734
3	6066	31	572-578	58	734–740
4	66-72	32	578-584	59	740-746
5	76-82	33	584-590	60	746-752
6	82-88	34	590-596	61	752-758
		35	596-602	62	758-764
7	174-180	36	602-608	63	764-770
8	180-186	37	608-614	64	770-776
9	186-192	38	614-620	65	776–782
10	192–198	39	620-626	66	782-788
11	198-204	40	626-632	67	788-794
12	204–210	41	632-638	68	794-800
13	210–216	42	638-644	69	800-806
		43	644-650		
14	470–476	44	650-656	70	806-812
15	476–482	45	656-662	71	812-818
16	482–488	46	662-668	72	818-824
17	488–494	47	668-674	73	824-830
18	494–500	48	674-680	74	830-836
19	500-506	49	680-686	75	836-842
20	506-512	50	686-692	76	842-848
21	512-518	51	692-698	77	848-854
22	518-524	52	698-704	78	854-860
23	524–530	53	704-710	79	860-866
24	530–536	54	710-716	80	866-872
25	536-542	55	716-722	81	872-878
26	542-548	56	722-728	82	878-884
27	548-554			83	884-890
28	554-560			05	304-070
29	560–566				

29-2 TV SIGNAL-STRENGTH ESTIMATION

The FCC limits the maximum effective radiated power (antenna input power times antenna gain) of commercial television stations to 100 kW for low-band VHF, 316 kW for high-band VHF, and 5 MW for the UHF band. Maximum TV transmitting-antenna heights are limited to 2000 ft (609.6 m). Figure 29-1 presents predicted field-strength levels for Channels 7 to 13 versus transmitting-antenna height and distance from the transmitting antenna for 1 kW radiated from a half-wavelength dipole antenna in free space. The figure predicts field strength 30 ft (9.14 m) above ground that is exceeded 50 percent of the time at 50 percent of the receiving locations at the specified distance.

Table 29-2 shows correction factors to be used with Fig. 29-1 to determine predicted field-strength levels for Channels 2 through 6 and Channels 14 through 69. The table presents correction factors for a 1000-ft transmitting antenna, but it is reasonable to use these factors for all transmitting-antenna heights. The table shows that field-strength levels for the low-VHF band and the UHF-band channels are typically lower than those for the high-VHF-band channels. Ground roughness between the transmitting and receiving antennas is also important in predicting field-strength levels for receiving sites more than 6 mi (9.6 km) from the transmitting antenna. It is measured along a line connecting the transmitting antenna and the receiving antenna that begins 6 mi from the transmitting antenna and terminates either at the receivingantenna location or 31 mi (49.9 km) from the transmitting antenna, whichever is least. The roughness ΔH , measured in meters, is the difference between the elevation level exceeded by 10 percent of the elevations along the line and the elevation level not reached by 10 percent of these elevations. The value of roughness assumed in the formulation of Fig. 29-1 is 50 m. The correction factor ΔF , given in decibels, to be applied to the field-strength value of Fig. 29-1 for a frequency f in megahertz is

$$\Delta F = C - 0.03\Delta H (1 + f/300)$$
 (29-1)

where C = 1.9 for Channels 2 to 6

TABLE 29-2 Correction Factors for Fig. 29-1 for an Antenna Height of 1000 Ft

Distance, mi	Channels 2-6, correction, dB	Channels 14-69 correction, dB		
1	0	0		
5	– 1	— 1.5		
10	-3	-3		
20	-3	—3.5		
30	-3	6		
40	-2.5	-9		
50	-1.5	-10		
60	-1	-9		
80	0	-6.5		
100	0	-4		
200	0	-2.5		

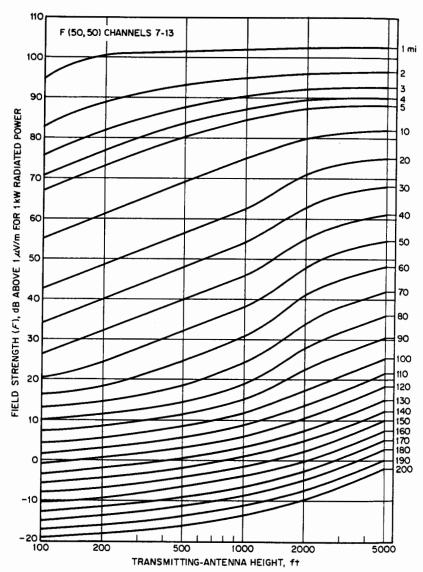


FIG. 29-1 Television Channels 7 to 13; estimated field strength exceeded at 50 percent of the potential receiver locations for at least 50 percent of the time at a receiving antenna height of 30 ft (9.14 m).

C = 2.5 for Channels 7 to 13

C = 4.8 for Channels 14 to 69

It can be seen that the correction factor lowers predicted field strength with increasing roughness and increasing frequency, reaching $-39.2 \, \mathrm{dB}$ for a roughness of 400 m and a frequency of 800 MHz.

Ground reflections cause the field strength to increase approximately linearly with height; i.e., the field strength is 6 dB less at a height of 15 ft (4.6 m) and 6 dB more at 60 ft (18.3 m). The rms signal voltage delivered to a 75- Ω load at the terminals of an antenna with gain G_A relative to a half-wavelength dipole immersed in a field with an rms field strength of E V/m at a frequency of f MHz is given by

$$V = \frac{37.75 \ E\sqrt{1.64G_A}}{f}$$
 (29-2)

As an example, f=689 MHz (Channel 50), receiving-antenna height = 10 ft (3 m), receiving-antenna gain = 12 dB ($G_A=15.8$), transmitting-antenna height = 1000 ft (305 m), transmitting effective radiated power = 5 MW, distance = 40 mi (64.4 km), and surface roughness = 50 m. Let us find the rms received voltage. From Fig. 29-1, E at a 30-ft (9.14-m) height is 83 dB above 1 μ V/m = 14,125 μ V/m (it is noted that surface roughness is negligible); E at 10 ft is 4708 μ V/m. The voltage received 50 percent of the time at 50 percent of such locations is greater than 1313 μ V.

The received-signal voltage at a given receiving location can be increased by increasing the height and gain of the receiving antenna. In addition, the effect of building attenuation must be considered for TV receiving antennas installed indoors. Measured attenuation values for a single wall between the receiving and the transmitting antennas range from 8 to 14 dB.

29-3 TV RECEIVING SYSTEMS

A TV receiving system is composed of an antenna, a transmission line, and a TV receiver. Baluns and splitters may be employed at the antenna or antennas and the TV receiver for impedance matching and for the separation or the combination of signals. Two TV receiving systems are typical: (1) an indoor antenna system using a small indoor antenna mounted on or near the TV receiver and (2) an outdoor antenna system using a larger antenna mounted high on a mast outdoors and connected to the TV receiver by an extensive transmission line. Indoor antenna systems typically are employed in high-signal-strength areas where multipath propagation is not severe. Outdoor antenna systems become necessary at a large distance from the transmitting antenna.

Overview of TV Antenna Types

A TV receiving antenna should have sufficient gain and a good impedance match to deliver a signal to a transmission line and subsequently to a TV receiver to produce a single clear TV picture and sound. Depending on its location, the antenna must reject reflected signals and other extraneous signals arriving from directions well off the direction to the transmitting antenna. Signal suppression should be particularly effective in the hemisphere directly opposite the transmitting antenna, as even small reflecting surfaces in this region can produce undesirable "ghost" images. TV receiving antennas should provide these properties over all TV channels of interest, which may include the complete 54- to 806-MHz range. They can be designed to receive all TV channels, or groups of channels such as all low-band VHF channels, all high-band

VHF channels, all VHF channels, and all UHF channels, or a single VHF or UHF channel.

TV receiving antennas fall into two major categories, indoor antennas and outdoor antennas. The most common configuration of an indoor antenna consists of two antennas, one for all VHF channels and one for all UHF channels. The most popular indoor VHF antennas are extendable monopole and dipole rods (rabbit-ear antennas) These antennas have measured average VHF gains of -4 dB with respect to a halfwavelength dipole and normally must be adjusted in length and orientation for best signal strength and minimum ghosting for each channel.3 Rabbit-ear antennas are available with 75- or 300-Ω impedance. There are several popular indoor UHF antennas, including the circular loop, triangular dipole, and triangular dipole with reflecting screen. The loop and triangular-dipole antennas have low gain; the triangular dipole with reflecting screen has increased gain and a greatly improved ability to reject signals arriving from behind the reflecting screen. Indoor UHF antennas are most commonly designed with a balanced 300-Ω impedance. A popular indoor VHF-UHF combination antenna consists of a VHF rabbit-ear dipole antenna and a UHF loop antenna mounted on a fixture containing a switchable impedance-matching network. If a preamplifier is included as an integral part, the antenna is known as an active antenna.

Outdoor antenna systems can provide up to a 15-dB increase in antenna gain (including transmission-line loss), typically 15- to 20-dB greater rejection of ghost signals, and greater immunity to electrical interference over indoor antenna systems. This advantage, combined with a typical signal-strength increase due to antenna height of 14 dB [6 to 30 ft (1.8 to 9.1 m)] plus the removal of a typical 11-dB building attenuation, could result in an overall signal increase at the TV receiver of up to 40 dB. The most common outdoor antenna configuration is a combined VHF and UHF antenna. The combined antenna usually consists of two separate antennas mounted together to form a single structure. The most common VHF antenna is some variation of the log-periodic dipole array (LPDA). This antenna may be designed for a 300-0 balanced or a 75-Ω unbalanced input impedance. There are several common types of UHF antennas including the LPDA, the broadband Yagi-Uda parasitic dipole array, the corner reflector, the parabolic reflector, and an array of triangular dipoles with a flat reflecting screen. Most UHF antenna types are designed with a balanced 300-0 input impedance. The UHF LPDA may also be designed for an unbalanced 75-\Omega impedance. Later sections treat these antenna types.

Transmission Lines for TV Receiving Systems

The standard impedances for the transmission lines used for TV and FM receiving systems are 75 Ω unbalanced and 300 Ω balanced. RG-59/U and RG-6/U types are the most commonly used 75- Ω lines, and twin-lead flat, foam, tubular, and shielded types are the most common 300- Ω lines. Table 29-3 shows average measured transmission-line losses for 100 ft (30.5 m) of the various types of lines. All measurements were performed on new dry lines suspended in free space. The standard deviation of the measurements within the types was approximately 0.5 dB at VHF frequencies and 1.5 dB at UHF frequencies except for the flat 300- Ω twin-lead type, which was 0 dB at all frequencies, and for the 300- Ω shielded twin-lead type, which was 0.5 dB at VHF and increased to 6 dB at the high UHF frequencies.

The voltage standing-wave ratio (VSWR) measured on 100-ft sections (with

TABLE 29-3 Average Transmission-Line Insertion Loss, dB, for a 100-Ft Length of New Dry Line

Cable	4	9	14	24	34	44	54	64	74	83
RG-59/U types	2.4	4.1	6.8	7.2	8.0	8.5	8.8	8.8	9.2	9.5
RG-6/U types	1.7	3.0	5.1	5.5	5.8	6.1	6.5	6.8	7.1	7.4
Flat twin-lead types	0.9	1.6	3.0	3.3	3.5	3.8	4.0	4.2	4.4	4.6
Foam twin-lead types	1.0	1.9	3.5	3.8	4.1	4.3	4.6	4.8	5.0	5.3
Tubular twin-lead types	0.9	1.7	3.2	3.5	3.7	4.0	4.2	4.5	4.7	5.0
Shielded twin-lead types	2.7	4.9	8.3	9.0	9.6	10.5	11.5	12.8	13.5	15.3

appropriate terminations) of the various types of lines is fairly independent of frequency on the VHF and UHF bands; it is shown in Table 29-4. Additional line losses and increased VSWR are reported for 50-ft (15.2-m) lengths of unshielded twin-lead transmission line because of proximity to metal and wetness. Table 29-5 presents these data for three cases: (1) 10 ft (3 m) of the 50-ft line parallel to and touching a metal mast, (2) 10 ft of the 50-ft line wrapped around a metal mast, and (3) a 50-ft section which is spray-wet.

Impedance-mismatch VSWR increases transmission loss. Such losses may occur at all junction points from the antenna to the TV receiver, including junctions at baluns, splitters, couplers, connectors, and preamplifiers. Impedance-mismatch loss is given by

Mismatch loss (dB) =
$$-10 \log_{10} \left[1 - \left(\frac{\text{VSWR} - 1}{\text{VSWR} + 1} \right)^2 \right]$$
 (29-3)

Mismatch loss is 0.2 dB for a VSWR of 1.5, 0.5 dB for a VSWR of 2.0, 1.9 dB for a VSWR of 4.0, and 4.0 dB for a VSWR of 8.0.

Baluns are used to match a 75- Ω unbalanced transmission line to a 300- Ω balanced line. Most commercially available baluns used for TV receiving systems employ bifilar transmission-line windings around a ferrite core to achieve broadband operation. Desirable features of baluns are minimum insertion loss and VSWR. Table 29-6 shows averaged measured balun insertion loss and VSWR for several TV channels. The standard deviation of these measurements is approximately 0.3 dB for insertion loss; it is 0.1 for VSWR at Channel 4, increasing to 0.5 at Channel 64.

TABLE 29-4 Average Measured Transmission-Line VSWR

Line	Average VSWR
RG-59/U types	1.2
RG-6/U types	1.2
Flat 300-Ω twin-lead types	2.0
Foam 300-Ω twin-lead types	1.8
Tubular 300-Ω twin-lead types	1.6
Shielded 300-Ω twin-lead types	2.4

TABLE 29-5	Average /	Additional	Transmission-Line	Loss and	VSWR
Because of Pro	oximity to f	Metal and	Wetness		

	Addi	tional loss	, dB	vs	VSWR increase			
Line	10 ft parallel to mast	10 ft wrapped on mast	50 ft spray- wet	10 ft parallel to mast	10 ft wrapped on mast	50 ft spray- wet		
Flat 300-Ω twin-lead types	5.8	5.8	8.4	2.1	1.2	1.7		
Foam 300-Ω twin- lead types	0.8	2.0	3.4	0.1	0.8	0.7		
Tubular 300-Ω twin- lead types	0.8	3.0	0.8	0.1	0.4	0.3		

Signal splitters are used to separate the VHF, FM, and UHF signals present on a transmission line at the receiver. They are also used as combiners to combine the signals from separate VHF, FM, and UHF antennas onto a single transmission line. Most commercially available splitters use three- to five-element high-pass and low-pass LC filters to accomplish the frequency separation. Some splitters contain input and/or output baluns to achieve 75- to $300-\Omega$ impedance transformations. Desirable features of signal splitters, in addition to frequency selectivity, are low insertion loss and VSWR. Table 29-7 shows the average measured insertion loss and VSWR of a selection of commercially available signal splitters. The standard deviation of these measurements is approximately 1.0 dB for the insertion loss and 0.5 for the VSWR.

Transmission-line connectors can cause significant VSWR on a transmission line. Properly installed F-type connectors provide reasonably low VSWR for RG-59/U and RG-6/U coaxial lines for a limited number of matings. The connector problem is particularly severe for 300-Ω-twin-lead transmission lines. Standard twin-lead plugs and sockets and screw-connector terminal boards were found to have VSWRs near 1.5. Lower VSWR for twin-lead lines can be achieved by direct soldering of the lines in a smooth and geometrically continuous manner.

The noise figure for a lossy transmission-line system is equal to its total attenuation from input to output; 5 dB of attenuation means a noise figure of 5 dB. The total transmission-system loss has a significant impact on the noise figure of the TV receiving system.

TABLE 29-6 Average Measured Balun Insertion Loss and VSWR

Channel	4	9	24	44	64
Insertion loss, dB	0.8	0.6	1.1	1.2	1.7
VSWR	1.4	1.6	1.5	1.8	2.0

TABLE 29-7 Average Measured Splitter Insertion Loss and VSWR

Channel	4	9	24	44	64
Insertion loss, dB	1.3	2.5	1.5	1.5	2.1
VSWR	1.8	2.1	1.7	1.7	2.5

TV Receivers

Typically, TV receivers have separate UHF and VHF inputs which are directly connected to the respective UHF and VHF tuners. These inputs are either 75- Ω coaxial with a Type F connector or 300- Ω twin lead with a twin-lead screw-connector terminal board. The trend is toward the 75- Ω coaxial input, as it is more compatible with cable and other video systems which use the TV receiver as a display unit. The noise figure of a typical TV receiver is 3 dB for the VHF bands, increasing to 4 dB for the UHF band. The input VSWR is approximately 2.5 for both the VHF and the UHF inputs.

29-4 TV RECEIVER-SYSTEM NOISE

The required signal strength for TV reception must be measured with respect to the TV receiver-system noise, including antenna noise. Figure 29-2 shows average observer picture-quality ratings versus the signal-to-random-noise ratio.⁶ From this figure it is seen that a signal-to-noise ratio of approximately 42 dB is required to produce a rating of excellent by the average observer. The figure also shows that a signal-to-noise ratio of 10 dB produces an unusable picture.

The equivalent noise voltage at the terminals of a TV receiving antenna when connected to a transmission-line-TV-receiving system is the rms sum of the antenna noise voltage and the equivalent noise voltage of the transmission-line-TV-receiving system.

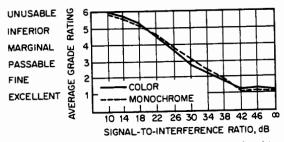


FIG. 28-2 Average observer rating versus signal-to-interference ratio. The solid line indicates color; the dashed line, monochrome. [Source: "Engineering Aspects of Television Allocations," Television Allocation Study Organization (TASO), report to FCC, Mar. 16, 1959.]

Antenna noise voltage can be estimated for low-gain antennas using the antenna temperature of an omnidirectional antenna located near the earth surface. The main contributors to antenna temperature are human-made noise, galactic noise, and ambient thermal noise due to the 290 K temperature of the earth. The equation for the noise voltage delivered to an R- Ω characteristic impedance transmission line by an impedance-matched antenna is given by

$$V_n = \sqrt{BRT_{\rm ant}k} \tag{29-4}$$

where $B = \text{bandwidth} = 6 \times 10^6 \text{ Hz}$

 $R = \text{matched impedance of antenna, } \Omega$

 T_{ant} = equivalent antenna temperature, K

 $k = \text{Boltzmann's constant} = 1.38 \times 10^{-23} \text{ W/Hz} \cdot \text{K}$

 $T_{\rm ant}$ is a function of frequency and varies due to solar activity and location with respect to human-made noise sources. Figure 29-3 gives median values of antenna temperature versus frequency. The figure shows that galactic temperature is larger than ambient temperature for VHF and less than ambient for UHF frequencies. Human-made noise temperature, primarily due to electrical ignition systems, transients on electric power delivery systems, and arcing of switches and defective insulators, follows a frequency behavior similar to galactic noise in the VHF and UHF ranges. Human-made noise temperature is seen to be approximately 33 dB larger than galactic noise temperature for urban environments and 17 dB larger than galactic noise temperature for suburban environments, being less than galactic noise temperature only in remote, rural locations. Human-made noise is the dominant noise source for VHF and UHF television in urban and suburban locations. The rms noise voltage, for Channel 2 in a suburban location, impressed on a 75- Ω transmission line by a 75- Ω antenna is 43 μ V.

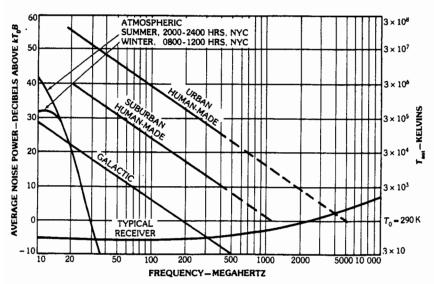


FIG. 29-3 Median values of average antenna noise temperature for an omnidirectional antenna near the earth's surface. (Reprinted from Ref. 7 with permission of Van Nostrand Reinhold Company, Inc.)

The equivalent rms noise voltage of a transmission-line-TV-receiver system with an overall noise figure N is given by

$$V_n = \sqrt{NBRTk} \tag{29-5}$$

where T is the temperature of the system in degrees Kelvin and is assumed to be 290 K. The parameters B, R, and k are as defined for Eq. (29-4). The overall noise figure of two systems connected in cascade can be calculated if the noise figures of both systems are known and the gain of the first system is known. The transmission-line system and the TV receiver form two systems in cascade as viewed from the terminals of the antenna. Let N_T represent the noise figure of the transmission line, G_T the gain of the transmission line (actually $G_T < 1$ for transmission lines), and N_{TV} be the noise figure of the TV receiver. The overall noise figure $N_{T-\text{TV}}$ of this cascade system is given by

$$N_{T-TV} = N_T + \frac{N_{TV} - 1}{G_T}$$
 (29-6)

A Channel 2 outdoor antenna system might have a transmission-line system with an attenuation of 3 dB ($G_T = 0.5$) and thus a noise figure of 3 dB ($N_T = 2$). Using a noise figure for the TV receiver of 3 dB, the overall noise figure for the transmission line-TV receiver is 4, or 6 dB. The equivalent noise voltage, calculated using Eq. (29-5), is therefore $2.7 \mu V$. The rms sum of this noise voltage and the antenna noise voltage for this Channel 2 example is 43 μ V. The required signal voltage for an excellent picture as defined above is therefore 5413 µV at the terminals of the antenna. The Channel 2 example shows that the antenna noise voltage due to human-made noise is much greater than the transmissionline loss noise and the TV receiver noise figure voltages. A Channel 69 outdoor example is quite different. Figure 29-3 shows an antenna temperature for a suburban location of 600 K, yielding a noise voltage of 1.9 μ V, substantially less than the Channel 2 example. If the transmission-line losses are 10 dB and the noise figure of the UHF receiver is 4 dB, the total system noise figure is 25, and the equivalent rms noise voltage of the transmissionline – TV-receiver system is 6.7 μ V, which is greater than for the Channel 2 example. The total equivalent system noise voltage at the terminals of the antenna is 7 μ V. The Channel 69 example shows that antenna noise is less than the transmission-line-TV-receiving system noise, the opposite being true for the Channel 2 example. An excellent-quality picture would therefore require an 88-µV signal at the terminals of the antenna.

A preamplifier mounted at the terminals of the antenna with a noise figure of 3 dB (N=2) and a gain of 20 dB (G=100) can significantly improve the noise figure of the transmission-line-UHF-receiver system. Consider a cascade system composed of two sections. The first section is the preamplifier, and the second section is the transmission-line-UHF-receiver system with a noise figure of 25. The overall noise figure of this cascade system, using Eq. (29-6) with the variables relabeled for the new cascade, is

$$N=2+\frac{25-1}{100}=2.24$$

The equivalent noise voltage is $2.0 \,\mu\text{V}$ and combined with the antenna noise voltage is $2.76 \,\mu\text{V}$. The required signal voltage at the terminals of the antenna for an excellent picture is $348 \,\mu\text{V}$, or $8.1 \,\text{dB}$ less than without the preamplifier. It is noted that greater preamplifier gain would not significantly reduce the required signal strength and might impair the large-signal performance of the preamplifier.

29-5 TRIANGULAR-DIPOLE ANTENNAS

A dipole formed from two triangular sheets of metal is sufficiently broadband with respect to gain and VSWR (with respect to 300 Ω) for all-UHF-channel reception. The flare angle α and the length 2A of the triangular dipole (also known as the bowtie antenna) are shown in Figure 29-4. The triangular dipole has many of the same

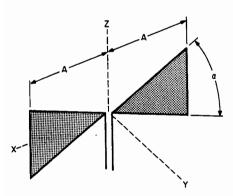


FIG. 29-4 Triangular dipole.

pattern and input-impedance characteristics of the biconical dipole discussed in Chap. 4, but it is lighter in weight and simpler to construct. Further simplification of the triangular dipole to a wire outline of the two triangles results in significant degradation of its broadband performance. However, the metal triangles can be approximated with wire mesh, provided the mesh spacing is less than one-tenth wavelength. The input impedance of a triangular monopole versus length A for a variety of flare angles α is shown in Ref. 8. The larger the values of A and α , the further the pattern in the XZ plane deviates from those in the

XY plane and the more predominant are the sidelobes. On the basis of pattern and impedance characteristics, compromise values of α between 60 and 80° may be used for values of A up to 210° (or 0.58 λ). Figure 29-5 shows the measured-gain characteristics of a triangular dipole over the UHF band. The triangular dipole can also be mounted approximately one-quarter wavelength in front of a flat reflecting screen to increase gain and decrease back radiation; typically, it is stacked vertically in two- or four-bay configurations for increased gain. The measured gain for several triangular dipoles with flat-screen-reflector configurations is also shown in Fig. 29-5. Measurements of several commercially available, vertically stacked multibay triangular dipoles with flat-screen-reflector arrays show that the VSWR is typically less than 2.0, the front-to-back ratio is greater than 15 dB, and sidelobe levels are less than 13 dB below the peak gain over 90 percent of the UHF band.

29-6 LOOP ANTENNAS

The single-turn circular-loop antenna is a popular indoor UHF antenna primarily because of its low cost. The single-turn loop in free space is discussed in detail in Sec. 5-3 in Chap. 5. Figure 5-10a shows the typical configuration used for television reception when the impedance of the balanced feed line is $300~\Omega$. Although the loop is a resonant structure, entire-UHF-band operation is possible by using a 20.3-cm-diameter single loop where the circumference varies across the band from 1.0 wavelength at 470 MHz to 1.7 wavelengths at 806 MHz. Figure 5-16 shows the directivity of a single-turn loop versus circumference and thickness. This figure shows that the directivity is above 3.5 dB for a loop circumference between 1.0 and 1.7 wavelengths. Figures 5-11 and 5-12 show the input resistance and reactance, respectively, of a single-turn circular loop. These figures show that the input resistance of a loop with a con-

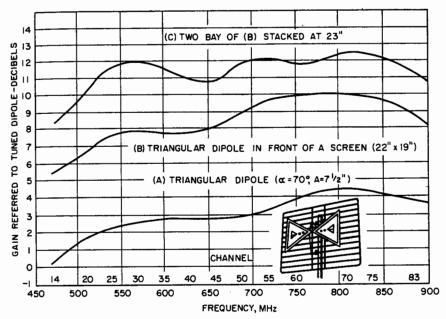


FIG. 29-5 Measured-gain characteristics. (a) Triangular dipole ($\alpha = 70^{\circ}$, $A = 7\frac{1}{2}$ in). (b) Triangular dipole in front of screen (22 by 19 in). (c) Two bays of antenna b stacked 23 in apart.

ductor thickness parameter* equal to 10 ranges from 100 to 520 Ω over the circumference range of 1.0 to 1.7 wavelengths, and the reactance is less than 100 Ω for a circumference between 1.0 and 1.45 wavelengths but increases to 210 Ω between 1.45 and 1.7 wavelengths. Thus, across the 1.0- to 1.7-wavelength band the input VSWR on a 300-Q feed line is less than 3 and is near 1 for a circumference near 1.3 wavelengths. The far-zone patterns of a one-wavelength loop with the thickness parameter equal to 10 are shown in Figs. 5-14 and 5-15b. These figures show that a one-wavelength loop has a bidirectional pattern with maximum directivity along the loop axis and that a vertical loop fed at the bottom is horizontally polarized. Measurements made on commercially available single-turn loops for UHF TV reception show that midband gain with respect to a half-wavelength dipole including mismatch losses is near 3 dB and falls off to -1 dB at both ends of the band. The measured VSWR is close to 1 near the center of the band, increasing to 4 at both ends of the band. Measurements also show that concentric groupings of loops, sometimes configured so that the loops can be turned, have lower gain but better VSWR characteristics than the single loop.

A planar reflector mounted parallel to the loop can be used to increase directivity and greatly reduce the sensitivity of the loop to signals arriving from behind the reflector. Figure 5-17 shows the geometry and directivity of a loop with a reflector. This figure shows that directivities greater than 8 dB are possible for a one-wavelength-circumference loop when the separation between the loop and the reflector is in a

^{*}The thickness parameter is 2 ln $(2\pi b/a)$, where b is the loop radius and a is the conductor radius.

range from 0.1 to 0.2 wavelength. Figure 5-18 shows the input resistance and reactance for a one-wavelength-circumference loop versus separation from the planar reflector. The impedance is seen to be primarily real, increasing from 50 to 130 Ω for separations increasing from 0.1 to 0.2 wavelength. Figure 5-19 shows measured farzone patterns for a loop with a reflector. This figure and Fig. 5-18 show the measured effects of variations in reflector size, suggesting a reflector size in the range of 0.6 to 1.2 wavelength on a side. Figure 5-23 b shows a method of feeding the antenna with a coaxial line.

Yagi-Uda arrays of loops can be used for both single-channel and whole-band reception. Figure 5-21 shows the configuration and directivity achievable for single-frequency operation.

29-7 LOG-PERIODIC DIPOLE ARRAY ANTENNAS

The log-periodic dipole array (LPDA) antenna is the most commonly used all-VHF-channel antenna; it also is becoming a popular all-UHF-channel antenna. The LPDA is a broadband antenna capable of a 30:1 constant gain and input-impedance bandwidth. It has a gain of 6.5 to 10.5 dB with respect to a half-wavelength dipole, with most practical designs being limited to gains of 6.5 to 7.5 dB. The LPDA evolved from a broadband spiral antenna and is discussed more fully in Chap. 14. Figure 29-6 shows a schematic diagram of the LPDA and defines the angle α , dipole lengths ℓ_n , element diameters d_n , and element locations with respect to the apex of the triangle x_n . τ is shown as the ratio of a dipole's length or location to the length or location of the next larger dipole. The ratio τ is constant throughout the array. This figure also shows that all dipoles are connected to a central transmission line with a phase reversal between dipoles. In practice, the central transmission line takes two forms, a high-impedance form and a low-impedance form. The high-impedance form designed for a 300- Ω balanced input inpedance consists of a single boom insulated from all array dipoles. The transmission line in this case is a high-impedance open two-wire line extending the

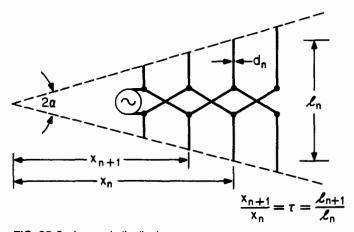


FIG. 29-6 Log-periodic dipole array.

length of the antenna with crisscross connections from dipole to dipole to accomplish the phase reversal. The high-impedance form should be limited to lower frequencies, where the required spacing between the two wires of the line is a small fraction of a wavelength. The low-impedance form designed for an unbalanced $75-\Omega$ input impedance is composed of two parallel conducting booms extending the length of the antenna, forming a low-impedance two-conductor transmission line. Phase reversal from dipole to dipole is accomplished by alternating the attachment of the dipoles along the two-boom transmission line. A coaxial feed line may be placed within one of the booms and connected to the short-dipole end of the array. In this configuration the array acts as a balun.

Log-periodic dipole arrays are routinely analyzed with a high degree of accuracy using method-of-moments computer algorithms. Log-periodic dipole arrays also can be designed and optimized through an iterative technique of array variation and analysis guided by optimization criteria. What follows is an approximate design technique for simple log-periodic dipole arrays based on the principles detailed in Chap. 14.

Figure 14-26 in Chap. 14 is a graph of equal-gain contours for the LPDA with a line showing optimal design conditions. This figure determines values of σ and τ on the basis of the desired gain. The angle α is calculated from σ and τ as

$$\alpha = \tan^{-1} \left[\frac{1 - \tau}{4\sigma} \right] \tag{29-7}$$

The longest dipole in the array has length ℓ_1 given by

$$\ell_1 = (0.995 - 0.5\tau)\lambda_{\min}$$
 for $0.8 \le \tau \le 0.95$ (29-8)

where λ_{\min} is the wavelength of the lowest design frequency of the array. The length of the shortest dipole in the array ℓ_N should be less than or equal to

$$\ell_N = [0.32 + (\tau - 0.9)(\sigma - 2\tau + 2.8) + (\tau - 1.48)(\sigma - 0.15)]\lambda_{\text{max}}$$
for $0.8 \le \tau \le 0.95$ and $0.05 \le \sigma \le 0.2$ (29-9)

where λ_{max} is the wavelength of the highest design frequency for the array. The location of the longest dipole x_1 from the apex of the triangle is given by

$$x_1 = \frac{\ell_1}{2} \cot \alpha \tag{29-10}$$

The other dipole lengths ℓ_n and locations x_n are given by

$$\ell_n = \ell_1 \tau^{(n-1)}$$
 $2 \le n \le N$ (29-11)
 $x_n = x_1 \tau^{(n-1)}$ $2 \le n \le N$

Ideally, the length-to-diameter ratio of each dipole K_n should be identical. In practice, this is not usually the case. The primary effect of the variation of the length-to-diameter ratio is variation of the input impedance versus frequency. The impedance of the central transmission line Z_0 is next designed to transform the impedance of the active-region dipoles Z_A to the desired input resistance R_0 . The impedance of the active-region dipoles is a function of the average K_n values of the elements K_{AVG} and is given by

$$Z_A = 60 \ln \frac{K_{\text{AVG}} 16\tau\sigma}{\pi(1+\tau)}$$
 (29-12)

The characteristic impedance of the central transmission line Z_0 is given by 10

$$Z_0 = R_0 \left[\frac{R_0(1+\tau)}{32\sigma\tau Z_A} + \sqrt{\left(\frac{R_0(1+\tau)}{32\sigma\tau Z_A}\right)^2 + 1} \right]$$
 (29-13)

The characteristic impedance Z_0 may be achieved with a two-conductor transmission line in which each conductor has a diameter D and the center-to-center spacing S of the conductors is given by

$$S = D \cosh (Z_0/120)$$
 (29-14)

Because of the wide bandwidth of the antenna, the accuracy of construction of an LPDA is not critical.

Several variations of the basic LPDA are also common. A large percentage of commercially available VHF LPDA receiving antennas are designed with reduced gain at the lower VHF because of the cost of the longer elements and the high signal strengths at the lower VHF frequencies. The low-frequency gain is normally reduced by elimination of the lower-frequency dipoles. A VHF LPDA can also be designed by using dipoles forming a V. This configuration allows the operation of the dipoles in their half-wavelength and **wavelength modes and therefore eliminates the need for the higher-frequency dipoles. An LPDA array designed with V dipoles for the low-VHF band will operate in the **-wavelength mode for the high-VHF band, as the frequency ratio of these two bands is approximately 3.

The high-frequency gain of an LPDA can be enhanced with the addition of parasitic directors at the short-dipole end of the array. Most home-use LPDA antennas are designed for a balanced 300- Ω input impedance, while most master-antenna-television (MATV) and community-antenna-television (CATV) applications use the 75- Ω unbalanced input-impedance configuration.

Measured performance of 19 home-use VHF LPDA antennas indicated an average low-VHF-band gain of 4.5 dB with a standard deviation of 1.5 dB with respect to a half-wavelength dipole at the same height above ground. The average high-VHF-band gain is 7.2 dB with a standard deviation of 1.4 dB. VSWR for the VHF band averages 1.9 with a standard deviation of 0.7. Three measured 300- Ω UHF LPDA antennas show an average gain of 7.1 dB with a standard deviation of 2.7 dB and an average VSWR of 2.7 with a standard deviation of 1.3. These averages are taken over frequency within the respective bands and over the antennas tested.

A circularly polarized LPDA can be formed by combining two linearly polarized LPDAs. The low-impedance configuration requires four booms, two for the horizontal LPDA and two for the vertical LPDA. All dipole lengths and locations of the second LPDA are obtained by multiplication of the respective dipole lengths and locations by $\tau^{1/2}$. The second LPDA should therefore have the same apex location, τ , α , and gain as the first. Multiplication by $\tau^{1/2}$ accomplishes the required frequency-independent 90° phase shift of the second LPDA with respect to the first.

29-8 SINGLE-CHANNEL YAGI-UDA DIPOLE ARRAY ANTENNAS

The Yagi-Uda dipole array antenna is a high-gain, low-cost, low-wind-resistance narrowband antenna suitable for single-TV-channel reception. Such antennas are popular in remote locations where high gain is required or where only a few channels are to be received. The Yagi-Uda dipole array is also discussed in Chaps. 12 and 27.

Yagi-Uda dipole arrays are routinely analyzed with a high degree of accuracy using method-of-moments computer algorithms. Yagi-Uda dipole arrays also can be designed and optimized through an iterative technique of array variation and analysis guided by optimization criteria.

An empirically verified design procedure for the design of Yagi-Uda dipole arrays which includes compensation of dipole element lengths for element and metallic-boom diameters is presented. Optimum Yagi-Uda arrays have one driven dipole, one reflecting parasitic dipole, and one or more directing parasitic dipoles as shown in Fig. 29-7. The design procedure is given for six different arrays having gains of 7.1, 9.2, 10.2, 12.25, 13.4, and 14.2 dB with respect to a half-wavelength dipole at the same height above ground. The driven dipole in all cases is a half-wavelength folded dipole which is empirically adjusted in length to achieve minimum VSWR at the design frequency. The length of the driven dipole has little impact on the gain of the array. Table 29-8 lists the optimum lengths and spacings for all the parasitic dipoles

TABLE 29-8 Optimized Lengths of Parasitic Dipoles for Yagi-Uda Array Antennas of Six Different Lengths

$d/\lambda = 0.0085$ $s_{12} = 0.2\lambda$	Length of Yagl-Uda array, λ						
	0.4	0.8	1.20	2.2	3.2	4.2	
Length of reflector, ℓ_i/λ	0.482	0.482	0.482	0.482	0.482	0.475	
l ₃	0.424	0.428	0.428	0.432	0.428	0.424	
l ₄		0.424	0.420	0.415	0.420	0.424	
l ₅		0.428	0.420	0.407	0.407	0.420	
. 4			0.428	0.398	0.398	0.407	
= l1				0.390	0.394	0.403	
5 ℓ ₈				0.390	0.390	0.398	
₹ ℓ,				0.390	0.386	0.394	
₽ e₁0				0.390	0.386	0.390	
Length of director, ℓ_1/λ \$ 19 \$ 10 \$ 11 \$ 12 \$ 13				0.398	0.386	0.390	
₫ ℓ12				0.407	0.386	0.390	
5 ℓ ₁₃					0.386	0.390	
→ ℓ14					0.386	0.390	
ℓ ₁₅					0.386	0.390	
ℓ_{16}					0.386		
ℓ ₁₇					0.386		
Spacing between directors (s/λ)	0.20	0.20	0.25	0.20	0.20	0.308	
Gain relative to half-wave dipole, dB	7.1	9.2	10.2	12.25	13.4	14.2	
Design curve	(A)	(B)	(B)	(C)	(<i>B</i>)	(<i>D</i>)	
Front-to-back ratio, dB	8	15	19	23	22	20	

SOURCE: P. P. Viezbicke, "Yagi Antenna Design," NBS Tech. Note 688, National Bureau of Standards, Washington, December 1968.

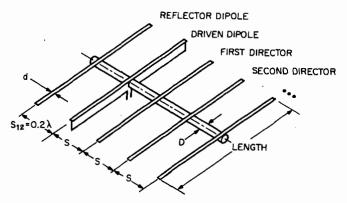


Fig. 29-7 Yagi-Uda array antenna.

for each of the six arrays. The dipole lengths in this table are for elements which have a diameter of 0.0085 wavelength. Figures 29-8 and 29-9 are used to adjust these lengths for other dipole diameters and the diameter of a metallic boom, respectively. The frequency used in the design of single-channel Yagi-Uda arrays should be 1 percent below the upper frequency limit of the channel for VHF channels because the bandwidth of the Yagi-Uda is not symmetrical and gain falls rapidly on the high-frequency side of the band. The design frequency for UHF channels should be the center frequency of the channel. On the basis of desired gain, the lengths of the parasitic elements are found in one of the columns of Table 29-8. The reflector spacing from the driven element for all six configurations is 0.2 wavelength, and all directors are equally spaced by the spacing shown in the table. The table also specifies the design curve A, B, C, or D to be used in Fig. 29-8. The parasitic-dipole lengths are next adjusted for the desired dipole diameter other than the diameter of 0.0085 wave-

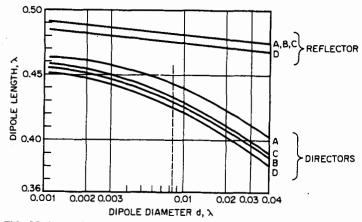


FIG. 29-8 Design curves to determine dipole lengths of Yagi-Uda arrays. (Source: P. P. Viezbicke, "Yagi Antenna Design," NBS Tech. Note 688, U.S. Department of Commerce-National Bureau of Standards, October 1968.)

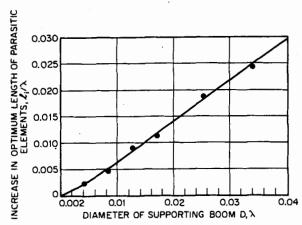


FIG. 29-9 Increase in optimum length of parasitic elements as a function of metal-boom diameter. (Source: P. P. Viezbicke, "Yagi Antenna Design," NBS Tech. Note 688, U.S. Department of Commerce-National Bureau of Standards, December 1968.)

length. The reflector length for the desired diameter can be read directly from one of the two upper curves in Fig. 29-8. Likewise, the length of the first director can be read directly from the designated director design curve for the desired diameter. This first director length is marked on the curve for subsequent use. The length of the first director for a diameter of 0.0085 wavelength is also marked on the designated design curve. The arc length along the design curve between the two marks for the first director length is measured and used to adjust the remaining director lengths as follows. The other director lengths are plotted on the designated design curve without regard to their 0.0085-wavelength diameter. Each of the points is moved in the same direction and arc length as required for the first director. The new length is the diameter-compensated length for each of the remaining directors. If a metallic boom is used to support the reflector and directors, Fig. 29-9 is used to increase the length of each by the amount shown in the figure based on the diameter of the boom.

A circularly polarized Yagi-Uda dipole array can be formed by combining two linearly polarized Yagi-Uda dipole arrays on the same boom. The dipoles of one array might be horizontal and those of the other vertical. One array is positioned a quarter wavelength ahead of the other along the boom to accomplish the required 90° phase shift, and the feed position is midway between the two driven dipoles. Such a circularly polarized Yagi-Uda dipole array for Channel 13 is shown in Fig. 29-10.

29-9 BROADBAND YAGI-UDA DIPOLE ARRAY ANTENNAS

Several approaches to widening the inherently narrow bandwidth of the Yagi-Uda array are discussed. Yagi-Uda arrays with no more than five or six elements can be broadbanded by shortening the directors for high-frequency operation, lengthening

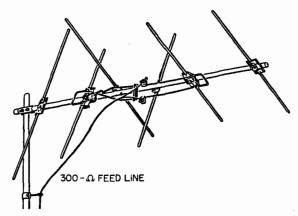


FIG. 29-10 Circularly polarized Yagi-Uda dipole array. (Channel Master Corp.)

the reflector for low-frequency operation, and selecting the driven dipole for midband operation. Figure 29-11 shows the measured gain versus frequency for a five-element single-channel and a five-element broadband Yagi-Uda array.⁹

The driven dipole of a Yagi-Uda array can be replaced with a two-element ordinary end-fire driven array. The driven array is designed for midband operation, the directors for high-frequency operation, and the reflector for low-frequency operation. An extension of this concept is the replacement of the driven element with a log-periodic dipole array. The parasitic elements are then used primarily to increase gain at the upper and lower frequency limits of the log-periodic dipole array.

Two Yagi-Uda dipole arrays of different design frequencies may be designed on

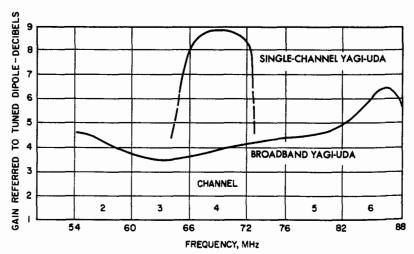


FIG. 29-11 Measured gain of five-element Yagi-Uda. (a) Single-element Yagi-Uda. (b) Broadband Yagi-Uda.

the same boom and use the same driven element. This is possible when the design frequency ratio of the two Yagi-Uda arrays is 3:1 as in the high-VHF and low-VHF bands. The interlaced parasitic elements have only a small impact on one another, and the driven element is used simultaneously in the first and third half-wavelength modes.

The reflector dipole of a Yagi-Uda array may be replaced with a corner reflector or a paraboloidal reflector. The reflector and driven element are designed for low-frequency and midfrequency operation, and the directors are designed for high-frequency operation.

The broadband Yagi-Uda is not commonly used for all-VHF-channel operation, but it is commonly used, generally with a corner reflector, for all-UHF-channel reception. Measurements of commercially available all-UHF-channel Yagi-Uda antennas typically show large variation in gain and input impedance as the frequency is varied across the UHF band. Typical of such an antenna is an average gain of 7 dB with respect to a half-wavelength dipole at the same height above ground with a variation of ± 8 dB across the UHF band. The VSWR of such an antenna is found to vary within the range of 1.1 to 3.5 across the band.

29-10 CORNER-REFLECTOR ANTENNAS

The corner-reflector antenna is very useful for UHF reception because of its high gain, large bandwidth, low sidelobes, and high front-to-back ratio. (Corner-reflector antennas are discussed further in Sec. 17-1 in Chap. 17.) A 90° corner reflector, constructed in grid fashion, is generally used. One typical design is shown in Fig. 29-12. A wide-

band triangular dipole of flare angle 40°, which is bent 90° along its axis as shown in Fig. 29-13 so that the dipole is parallel to both sides of the reflector, is a good choice for the feed element. Experimental results indicate that an overall length of 14½ in (362 mm) for the dipole gives the optimum value of average gain over the band. The dipole has a spacing of about $\lambda/2$ at midband from the vertex of the corner reflector. A larger spacing would cause a split main lobe at the higher edge of the band, where the spacing from the vertex becomes nearly a wavelength.

Figures 29-13 and 29-14 are experimental results useful in designing grid-type corner reflectors. Figure 29-13 shows the relation between grid length L and gain at three different frequencies. It is seen that beyond 20 in (508 mm) of grid length very little is gained. Figure 29-14 shows the relation between gain and grid width W. At 700 and 900 MHz, the improvement in gain for a grid over 20 in wide

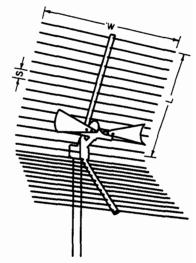


FIG. 29-12 Corner-reflector antenna.

is rather insignificant. To reduce the fabrication cost, a width of 25 in (635 mm) is considered a good compromise. In Fig. 29-15 the spacing for grid tubing of \(\frac{1}{2}\)-in (6.35-

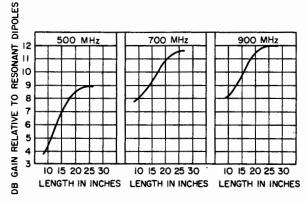


FIG. 29-13 Measured-gain characteristics versus grid length L.

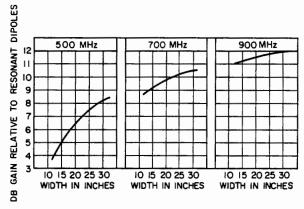


FIG. 29-14 Measured-gain characteristics versus grid width W.

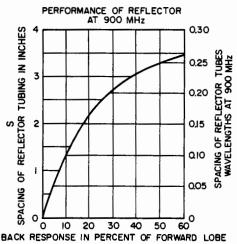


FIG. 29-15 Relation between the rear lobe in percentage of the forward lobe and the grid spac-

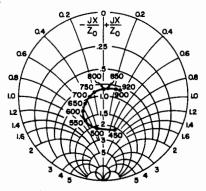


FIG. 29-16 Impedance characteristics of an ultrahigh-frequency corner reflector.

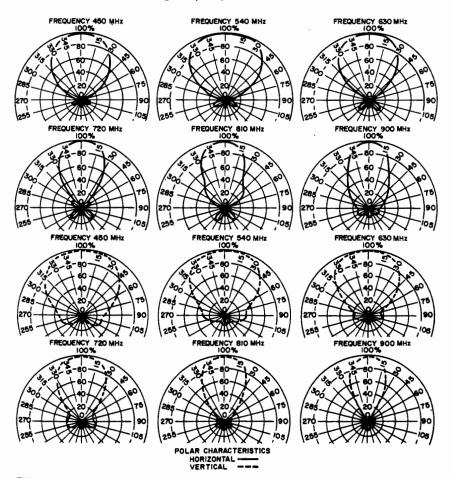


FIG. 29-17 Field patterns of an ultrahigh-frequency corner-reflector antenna.

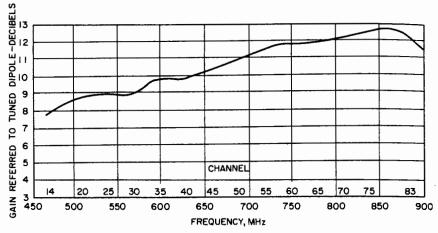


FIG. 29-18 Measured gain of an ultrahigh-frequency corner-reflector antenna.

mm) diameter can be determined from the allowable level of the rear lobe in percentage of the forward lobe at the highest frequency, 900 MHz. If 10 percent is the allowable value, the spacing should be slightly under 1½ in (38 mm). Below 900 MHz, the rear pickup will be less than 10 percent provided that the grid screen is wide enough. Thus, the width is determined by the lowest frequency, while the spacing of the grid tubing is determined by the highest frequency.

Figures 29-16 and 29-17 show impedance characteristics and field patterns respectively. Figure 29-18 shows the measured gain over the band.

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Microwave-Relay Antennas

Charles M. Knop

Andrew Corporation

30-1 Introduction 30-2 Typical Microwave-Relay Path 30-2 Specifications for Microwave-Relay Antennas 30-2 Antennas in Use 30-4 30-2 The Prime-Fed Symmetrical Paraboloidal Dish 30-4 Basic Principle of Operation 30-5 The 100 Percent Feed Horn 30-6 Trade-Off between Gain and Radiation-Pattern Envelope 30-6 Practical Feeds 30-8 Required F/D 30-9 Typical Case 30-10 Pattern and Gain Dependence on Distance 30-11 Effect of Feed Displacement 30-12 Effect of Surface Errors 30-14 Front-to-Back Ratio 30-15 Effect of Vertex Plate 30-15 Effect of Feed-Support and "Strut" Scattering 30-16 Effect of Radome 30-17 30-3 The Paraboloidal Grid Reflector 30-18 30-4 The Offset Paraboloid 30-20

30-5 Conical and Pyramidal Cornucopias

30-20

30-9 Recent Developments 30-23 Complete Radiation-Field Expressions for Symmetrical Prime-Fed Dish 30-23 Universal Design Curves for a Symmetrical Prime-Fed Dish 30-23 More on Feed Displacement 30-27 Cross-Polar Fields Produced by a Symmetrical Prime-Fed Dish 30-28 Effect of Periodic Dish Imperfections on Near On-Axis Sidelobes 30-28 Safety Concerns-Near-Field Power Densities 30-29 Near-Field Focusing 30-29 More on Blockage and Strut Effects 30-34 Improved Offsets 30-41 Improved Conical Cornucopias Improved Large-Gain Feed Horns 30-41 Angle Diversity 30-41

30-6 Symmetrical Dual Reflectors 30-21

30-7 Miscellaneous Topics 30-2230-8 Comparison of Antenna Types 30-22

Typical Microwave-Relay Path

The typical microwave-relay path consists of transmitting and receiving antennas situated on towers spaced about 30 mi (48 km) or less apart on a line-of-sight path. If we denote P_T , G_T , P_R , and G_R as the transmitted power, transmitting-antenna gain, received power, and receiving-antenna gain respectively, then these are related by the well-known free-space Friis transmission law (neglecting multipath effects):

$$P_R = P_T G_T G_R / (4\pi R/\lambda)^2$$
 (30-1)

where R = distance between receiving and transmitting antennas

 λ = operating wavelength in free space

A typical modern-day telecommunications link is designed to operate with $P_T = 5 \text{ W } (+37 \text{ dBm})$ and $P_R = 5 \mu\text{W} (-23 \text{ dBm})$. (Note that -23 dBm is the operating



FIG. 30-1 Typical tower with radio relay antennas. (Courtesy Andrew Corp.)

level. Typical receivers still give adequate signal-to-noise ratios for fade margins 40 dB below this level, i.e., down to -63 dBm.) Thus, at a typical microwave frequency in the range of 2 to 12 GHz (say, 6 GHz) and $G_T = G_R$ (identical antennas at both sites), we see that antenna gains of about 104 (40 dBi) are required if no other losses exist. However, a typical installation (usually having several antennas on a given tower; see Fig. 30-1) has the antenna connected to a waveguide feeder running down the length of the tower (typically 200 ft, or 61 m, high) into the ground equipment. The total power received is then less than that given by Eq. (30-1) because of the losses in the waveguide feeder in the antenna (typically 0.25 dB) and in the tower feeder (typically 3.0 dB). This raises the above antenna gain requirement to about 43 to 44 dBi (all these values are at 6 GHz and change accordingly over the common-carrier bands, since the freespace loss and feeder loss increase with frequency).

Specifications for Microwave-Relay Antennas

In addition to the above high gains, the radiation-pattern envelope (RPE; approximately the envelope obtained by connecting the peaks of the sidelobes) should be as narrow as possible, and the front-to-back ratio should be high to minimize interference with adjacent routes. Typical Federal Communications Commission (FCC) RPE specifications are shown in Fig. 30-2 (all patterns discussed here are horizontal-plane patterns; hence the E-plane pattern is horizontally polarized, and the H-plane is ver-

tically polarized). Figure 30-2 also shows the RPE of a conical-cornucopia antenna, which will be discussed.

The requirement of simultaneous high gain and low sidelobes is, of course, inconsistent in antenna operation; hence some trade-off is necessary. Since the gain of an antenna is given by $G = \eta 4\pi A/\lambda^2$, where η is the total aperture efficiency (typically 0.50 to 0.70) and A is the physical area, we see that for circular apertures of diameter D, we require $D/\lambda \doteq 60$ for 43-dB gain and for $\eta = 0.5$; i.e., $D \doteq 10$ ft (3 m) at 6 GHz (with corresponding sizes at other bands). This means that the beamwidth between the first nulls, θ null, will be about θ null = $120/(D/\lambda) \doteq 2^{\circ}$. Thus, the supporting structure and tower must be very stable to ensure no significant movement of the beam (and consequent signal drop and cross-polarization degradation) even during strong winds (125 mi/h, or 201 km/h).

A further specification not found in radar or other communication systems is the extremely low voltage-standing-wave-ratio (VSWR; typically 1.06 maximum) requirement at the antenna input. This is to reduce the magnitude of the round-trip echo (due to the mismatch at both the antenna and the equipment ends) in the feeder

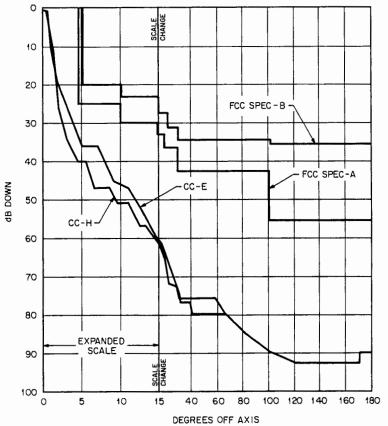


FIG. 30-2 FCC RPE specifications and conical-cornucopia RPE.

line. This echo produces undesirable effects: (1) cross talk in the baseband of a frequency-division-multiplexed-frequency modulation (FDMFM) analog system, especially in the upper telephone channels, (2) ghosts on a TV link, and (3) an increase in the bit error probability in a digital system (which does, however, tolerate higher VSWR). Also, for dual-polarization operation at a given frequency, polarization purity expressed as cross-polar discrimination (XPD) between the peak of the main copolar beam and the maximum cross-polar signal is typically required to be $-25 \, \mathrm{dB}$ minimum across an angle twice the 3-dB beamwidth of the copolar pattern. Additionally, bandwidths of up to 500 MHz at any common-carrier band are required (these bands extend from 1.7 to 13.25 GHz, with FDMFM up to 2700 channels at 3.7 to 11.7 GHz and up to 960 channels of digital system above 10.7 GHz).

Added to the above are a low-cost requirement, a necessity to operate under virtually all weather conditions, and the low near-field coupling specifications between antennas mounted on the same tower (typically -120 dB back to back and -80 dB minimum side to side). Finally, no loose contacts or other nonlinear-contact phenomena (the so-called rusty-bolt effect) are allowed, because if signals of frequencies A and B arrive simultaneously, then a third signal of 2A-B is generated. These 2A-B products must be down to about -120 dBm or more.

Antennas in Use

The most common antennas in use today which meet all the above requirements are the symmetrical prime-fed circular paraboloidal dish (and its grid equivalent, though this is suitable for only single polarization and has much worse RPE), the offset paraboloid, the conical and pyramidal cornucopias, and the dual reflector (Cassegrain and gregorian). The principles of operation and designs of these antennas will now be reviewed, with major emphasis on the symmetrical prime-fed paraboloid, which is by far the most frequently used microwave-relay antenna.

30-2 THE PRIME-FED SYMMETRICAL PARABOLOIDAL DISH

Many excellent treatments describing the operation and design of this antenna are reviewed in Chap. 17 and in the open literature²⁻¹³ (see especially Silver,² Ruze,³ and Rusch-Potter⁴). Almost all these references, however, were written prior to the ease of accessibility (for most antenna engineers) to the minicomputer (this, in turn, required analytical approximations to be made; for example, the feed-horn patterns were described by $\cos^n \psi$ -type functions) and prior to the full evolvement of Keller's geometric theory of diffraction (GTD) to the uniform geometric theory of diffraction (UGTD) by Kouyoumjian¹⁴ and the concept of equivalent rim currents of Ryan and Peters.¹⁵ Alternatively, Rusch's asymptotic physical optics (APO)¹⁶ in its corrected form (CAPO)^{17,18} can be used instead of UGTD.¹⁹⁻²⁰ Because of space limitations, we present here only results based on the above²¹ and other analyses.

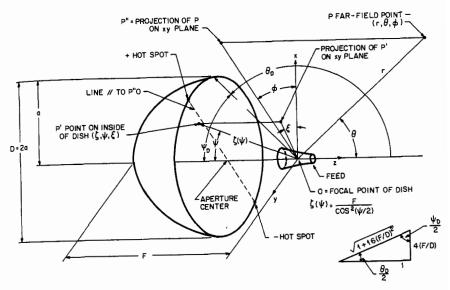


FIG. 30-3 Symmetrical-paraboloidal-dish geometry.

Basic Principle of Operation

Consider, then, the typical geometry of Fig. 30-3, depicting a prime feed illuminating a circular paraboloid. We start with the known horn E- and H-plane patterns in amplitude and phase in a computer file and assume that the horn produces a symmetrical pattern [see Eq. (1) of Ref. 17]. The surface current K produced on the dish surface is then found by using geometric optics (GO), i.e., by assuming that this surface is an infinite sheet and that the dish is in the far field of the horn, so that the E and E fields of the horn are related by the usual free-space impedance relationship. It is known that this GO approximation is questionable near the dish edge, E but this only has a consequence on the fields radiated in the 120° vicinity.

The electric field E scattered by the dish is then obtained by integration of K over the *illuminated* surface of the dish up to and *including its edges*. The resulting expressions are considered in three regions: region 1, $0 \le \theta \le \theta_1 =$ fifth sidelobe; region 2, $\theta_1 \le \theta \le \theta_2 = 175^\circ$; and region 3, $175^\circ \le \theta \le 180^\circ$. The region 1 expressions are double integrals [see Ref. 17, Eq. (2)], which can be reduced to a single integral via Bessel's orthogonality relation (Ref. 2, page 337). The region 2 UGTD (or CAPO) expressions are essentially asymptotic integrations (as given explicitly in Rusch¹⁶ with the diffraction coefficients replaced by those of UGTD^{19,20} or CAPO¹⁸) and come from the "hot spots" on the dish edge* (see Fig. 30-3). The region 3 fields come from the equivalent rim currents^{15,19,20,22-24} [and are given by Eq. (6) of Ref. 23]. Also, in the range of $0 \le \theta \le \theta_D$ horn superposition is required.

^{*}For the observation point in the horizontal plane, these hot spots are on the left and right edges of the dish.

The above expressions then give the patterns from the perfectly focused feed in a perfect paraboloid. To obtain the gain we compute the field on axis ($\theta = 0$), obtain the angular power density, and then divide by the total feed power over 4π sr. This also gives the aperture efficiency η . A program that computes both patterns and gain takes a few minutes to run on a minicomputer such as a DEC VAX 11/780.

The 100 Percent Feed Horn

Prior to considering actual feed horns, it is very instructive to create a hypothetical horn file having the pattern value* $1/\cos^2(\psi/2)$ for $0 \le \psi \le \psi_D$ and 0 for $\psi > \psi_D$ (as depicted in Fig. 30-4 for an F/D=0.30 dish). This exactly negates the $(1/\rho)$ free-space loss [since $\rho=F/\cos^2(\psi/2)$ for a perfect paraboloid], so that the magnitude of the fields illuminating the dish surface is then constant. Hence, the aperture amplitude and phase are constant, giving $\eta=100$ percent.

Using the expressions for the above three regions gives the patterns of Fig. 30-5a (near-in pattern) and 30-5b (wide-angle RPE†) for the E plane. The H-plane pattern is not shown because of lack of space, but it is similar except in the dish shadow $\theta > \theta_D$, where it is lower than the E-plane pattern since the H-plane diffraction coefficients here are smaller than those of the E plane. One notes that for small θ the patterns are close to $2J_1(U)/U$, where $U = C \sin \theta$, $C = \pi D/\lambda$.

Trade-Off between Gain and Radiation-Pattern Envelope

The above uniform case gives the highest possible gain, but its RPE is not low enough for most applications, since the dish edge illumination is 4.6 dB above that on the horn axis. Hence, a feed having lower edge illumination but still giving reasonable efficiency is required.

The opposite extreme of the 100 percent efficiency case is to illuminate the dish with a horn pattern having very low edge illumination. Now from Kelleher (see Chap. 17) we know that it is a universal characteristic of conventional single-mode horns (be they circular, rectangular, square, smooth-wall, corrugated, or whatever) that if their 10-dB beamwidths (i.e., let ψ_{10} be the angle off axis at which the power is 10 dB down from that on axis) are known, their power patterns from the 0- to about the 20-dB-down level can be described fairly well by Kelleher's formula:

DBE(
$$\psi$$
) = $10(\psi/\psi_{10E})^2$ (30-2)
DBH(ψ) = $10(\psi/\psi_{10H})^2$

where the subscripts E and H denote E and H planes respectively.

The above characteristic allows us to investigate quickly the trade-off between high gain and RPE. Four examples (all assumed to have back radiation of -40 dB and $\psi_{10E} = \psi_{10H} = \psi_{10}$ and to have zero phase error) are shown in Fig. 30-4. These

^{*}E and H planes are assumed to be equal and with zero phase error.

[†]Note that for $10^* \lesssim \theta \leq \theta_D = 100^*$, the RPE of Fig. 30-5 b is unrealistic, since this ideal feed has no spillover.

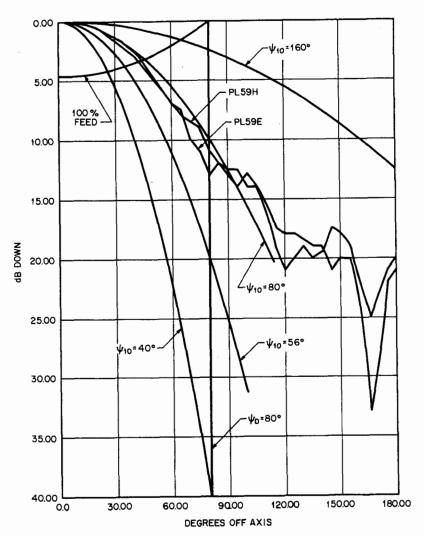


FIG. 30-4 Various feed patterns.

feeds produce the *E*-plane patterns also shown in Fig. 30-5*a* and *b*. A plot of η percent versus ψ_{10}/ψ_D (also in Fig. 30-5*b*) confirms the rule (e.g., see Silver, page 427) of choosing about a 10-dB edge taper to achieve peak gain.* One notes from Fig. 30-5*b* that for $\theta > \theta_D$ (here $\theta_D = 100^\circ$) the 100 percent feed case has the highest RPE, whereas from Fig. 30-5*a* it has the narrowest main beam and the highest gain. Also,

^{*}Note that actual gains, because of feed defocusing, dish rms, feed-support and strut scattering, etc., are lower than that of Fig. 30-5b by typically 5 to 10 percent, as discussed below.

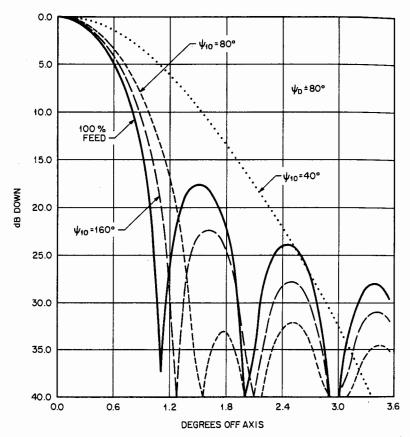


FIG. 30-5a On- and near-axis E-plane dish patterns for various feeds.

it is seen from Fig. 30-5 b that an excellent (wide-angle, $\theta \gtrsim 10^{\circ}$) RPE but (from Fig. 30-5a) a very low gain are provided by the extremely underilluminated feed ($\psi_{10} = 40^{\circ}$).

Practical Feeds

Actual feeds²⁵ have main-beam patterns close (with 1 to 2 dB at the 20-dB-down level) to the Kelleher description; some examples are given in Table 30-1. The most common feed used for terrestrial antennas consists of the circular-pipe TE₁₁-mode feed, sometimes with a recessed circular ground plate having quarter-wave-type chokes. These chokes control the external E-plane wall current that normally would flow on the horn's exterior surface, and they tend to make the E-plane pattern equal to that of the H plane, with both being flatter over the dish and having a faster falloff near the

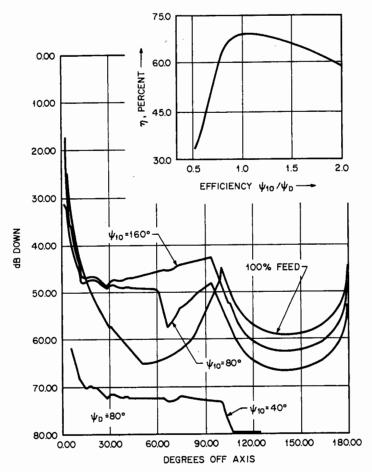


FIG. 30-5b E-plane RPE and aperture efficiency of dish with various feeds.

dish edge, causing improved efficiency. This horn has been patented by Yang-Hansen; similar work by Wohlleben has been reported (see Love²⁵). The rectangular horn is also commonly used since ℓ and w can be adjusted (at one band) to give almost equal E- and H-plane patterns.

Required F/D

For terrestrial radio work, the F/D ratios usually fall in the range of 0.25 (i.e., $\psi_D = 90^{\circ}$, focal-plane dish) to about 0.38. For deeper dishes (F/D < 0.25), the requirement of building a feed having $\psi_{10} > 90^{\circ}$ with low spillover is difficult. For shallower dishes

TABLE 30-1 Approximate 10-dB Angles for Practical Feed Horns®

Horn	Mode	ψ ₁₀ ε °	Ψ _{10H} °
Rectangular $\ell \times w$ (E perpendicular to ℓ)	TE ₁₀	42/(w/λ)	59/(ℓ/λ)
Circular,* $C \ge 1.84$	TE_{11}	$52/(DH/\lambda)$	$62/(DH/\lambda)$
Circular ²⁵ (Potter), $C \ge 3.83$	$TE_{11} + TM_{11}$	$62/(DH/\lambda)$	$62/(DH/\lambda)$
Circular (corrugated, " $\lambda/4$ HE ₁₁ teeth") zero or small (less than 10°) phase error $C \ge 2.40$	HE ₁₁	$62/(DH/\lambda)$	$62/(DH/\lambda)$
Circular (corrugated, " $\lambda/4$ HE ₁₁ teeth") large (180° or more) phase error, half angle α_0 (0 $\leq \alpha_0 \leq 85$ °)	HE ₁₁	$\alpha_0/\sqrt{2}$ (approximate)	$\alpha_0/\sqrt{2}$ (approximate)
Diagonal ²⁵ (A. W. Love), $D/\lambda \ge 0.50$ ($D = \text{side length of aperture } D \times D$); (small phase error)	Two TE ₁₁	$50.5/(D/\lambda)$	$50.5/(D/\lambda)$

^{*}All circular horns have inner-diameter DH, $C = \pi DH/\lambda$. All zero- or small-phase-error horns have their phase center on or very close to the aperture; the large-phase-error horns have it close to the horn apex. Note that the E- and H-plane phase centers are usually not exactly coincident; their average position is made to coincide with the dish focal point. As seen, the zero- or small-phase-error horns are diffraction-limited; i.e., they have beamwidths which decrease with increasing frequency, whereas the large-phase-error corrugated horn has equal E- and H-plane patterns which are frequency-independent and hence is called a scalar feed (see Chap. 15).

 $(F/D > 0.38, \psi_D < 67^\circ)$, the feed is too far from the dish, which makes it impractical to use a radome; feed losses also are higher. Thus, F/D typically is about 0.3, and we therefore seek feeds having $\psi_{10} = 80^\circ$.

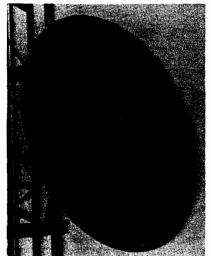


FIG. 30-6 A standard buttonhook feed in a paraboloidal dish. (Courtesy Andrew Corp.)

Typical Case

A typical feed is a rectangular horn (as described in Table 30-1) fed by a buttonhook feed (similar to that shown for a circular-horn feed in Fig. 30-6). The feed patterns (the phase patterns of which are virtually flat over the dish and hence are not shown) of this rectangular horn are shown in Fig. 30-4 (averaged over both sides in the absence of the buttonhook) and are designated by PL59 (we note they have about a 10-dB edge taper, so the horn has $w/\lambda = 0.53$, $\ell/\lambda = 0.74$). The resulting measured and predicted Eplane dish patterns are shown in Fig. 30-We see that the prediction and measurements are close in the main beam, in the first few sidelobes, and in the rear, but in the approximately -10-dBi (here

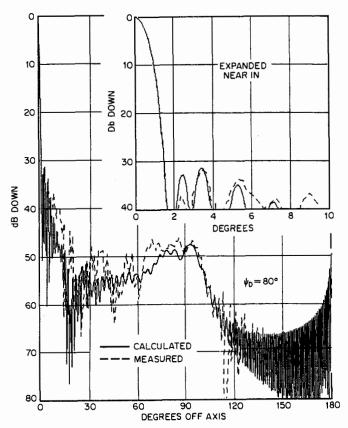


FIG. 30-7 Measured and predicted *E*-plane patterns of a paraboloidal dish with a buttonhook feed.

the 0-dBi level \doteq 43 dB down) level (10° $\lesssim \theta \lesssim$ 70°) the measured fields are typically ± 5 dB in range about the predicted envelope. The major reasons for these discrepancies are twofold: dish imperfections and feed-support scattering, as discussed below.

Pattern and Gain Dependence on Distance

The above far-field formulations are (by definition) for an infinite-observation distance. We wish to determine the effects of a finite distance r in the range of $0.2 (D^2/\lambda) \le r \le \infty$, since such short paths are necessary in many applications. To do this we use the double-integral (exact-phase) expressions (the same result, off axis, can also be obtained by GTD^{27}). The *E*-plane results are shown in Fig. 30-8a for the case of the typical buttonhook feed; the results for the 100 percent feed are shown in Fig. 30-8b. Figure 30-9 shows the on-axis gain drop relative to that at infinity for these

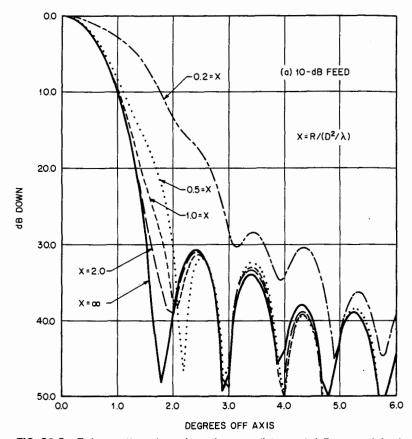


Fig. 30-8 E-plane-pattern-shape dependence on distance. (a) Buttonhook feed.

cases owing to this finite-observation distance. The gain drops because the main beam widens, the sidelobes rise, and the nulls fill in. In most practical installations, r is greater than D^2/λ ; thus, the gain is degraded by at most 0.3 dB. These results are in agreement with those of Silver² (page 199, for the uniform case) and Yang²⁸ (for $\cos^n \psi$ -type feeds). If two identical antennas are used, the total gain drop is then double the amount given by Fig. 30-9.

Effect of Feed Displacement

In general, the feed is inadvertently defocused (that is, the feed's phase center is not coincident with the focal point of the dish). This comes about because in most cases the feed is attached to a waveguide feeder, which in turn is attached to the hub of the dish, which may be distorted slightly (especially axially) from paraboloidal. It has been shown (e.g., by Imbriale et al.; see Love²⁵) that this defocusing effect can be

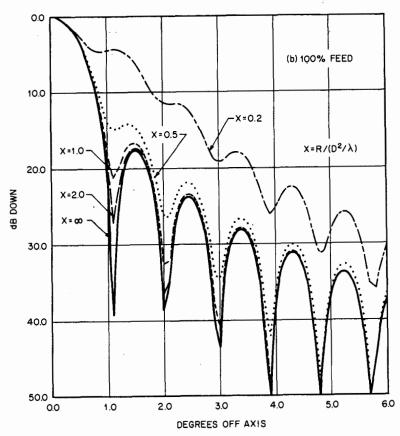


FIG. 30-8 (Continued) (b) 100 percent feed.

accounted for by inserting a phase-error term, exp $(j\Phi_D)$, multiplying the dish surface current, where (letting $k=2\pi/\lambda$)

$$\Phi_D = k \cdot DT \sin \psi \cos (\xi - \xi_D) - k DZ \cos \psi \qquad (30-3)$$

where DT, ξ_D , and DZ define the feed displacement and are respectively the transverse (DT > 0), azimuthal angular, and axial displacement (DZ > 0) for feed movement away from the dish, and DZ < 0 for feed movement toward the dish).

The pattern degradation and gain drop resulting from axial shifting of the above typical buttonhook feed (in the above F/D=0.30, $D/\lambda=60$ dish) are shown in Figs. 30-10a and 30-11 respectively.²⁹ It is seen that the pattern distortion results in intolerable (≥ 0.2 -dB) gain drops for $|DZ|/\lambda \gtrsim 0.15$. For transverse (lateral) displacements, the beam squints, but the pattern shape is not distorted as much for the same wavelength displacement as for the axial case (see Fig. 30-10b). The corresponding gain drops are also shown in Fig. 30-11, and it is seen that for $DT/\lambda < 0.15$ the gain

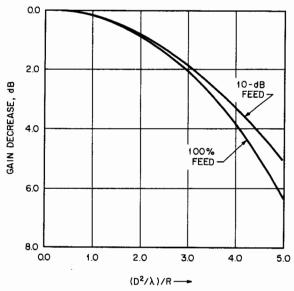


FIG. 30-9 Gain drop with distance.

drop is less than 0.04 dB. These results hold for any angular displacement ξ_D . The beam squint $(D\theta^*)$ for the subject antenna is also shown in Fig. 30-11. Although not shown here, repeating the above for a feed with the same edge taper in a deeper dish results in more distortion and gain drop than for a shallower dish.*

Effect of Surface Errors

By measuring at a sufficient number of points the normal difference Δn (ψ, ξ) between an actual dish and a fixture representing the paraboloid to be made, it is found that these surfaces are locally parallel. As such, a phase error of amount $360\Delta n$ $(\psi, \xi)/\lambda$ cos $(\psi/2)$, representing the additional path length to the reflector surface, must be included in K. This phase error degrades the gain, RPE, and XPD. Performing the necessary double integration reveals that the resulting gain drop is very close to that given by Ruze's formula 30,10 (see also Zucker 31):

$$\Delta G_{\rm rms} = -10 \log_{10} \left[\exp \left(-4\pi \epsilon_{\rm rms} / \lambda \right)^2 \right] \quad dB \qquad (30-4)$$

where $\epsilon_{\rm rms}$ is the root-mean-square deviation (in the normal direction) of the measured data points from the best-fit paraboloidal surface of these points [actually, Eq. (30-4) is based on a large F/D dish and hence is an upper bound on the gain drop]. Since we strive for $\Delta G_{\rm rms} \leq 0.15$ dB, we must make $\epsilon_{\rm rms} \leq \lambda/70$ [e.g., $\epsilon_{\rm rms} < 0.030$ in (0.76)

^{*}Similarly, for a given F/D dish and a given feed displacement, a feed with higher edge illumination produces more pattern distortion and gain drop than one with lower edge illumination (not shown here).

mm) at 6 GHz] for gain purposes. However, use of the Δn (ψ , ξ) file and double integration of many antennas reveals a rapid degradation of RPE (only in the $\theta < \theta_D$ region) with ϵ_{rms} (since this file contains many spatial harmonics³²). This work and some analytical work by Dragone and Hogg³³ using this approach, as shown in Fig. 30-12* (for a 10-dB feed and 15 ψ harmonics representing the actual surface), discloses that deviations from the parabolic should be held within about $\pm \lambda/100$ [i.e., $\epsilon_{rms} \lesssim \lambda/300$ or $\epsilon_{rms} \lesssim 0.007$ in (0.1778 mm) at 6 GHz] if approximately 3-dB or less increases from the perfect-case RPE are desired at about the 60-dB-down level (see also Fig. 30-7 for this increase in RPE in the 10* to 70* region due to rms). The XPD for realistic dishes is typically more than +50 dB down from the main beam.

Front-to-Back Ratio

Using the above analytical results to evaluate the front- and back-field expressions explicitly for the general case, one obtains the expression for f/b:²³

$$f/b = G + T + K - G_{HORN}$$
 dB (30-5)

where $G = \text{gain of dish} = 10 \log_{10} (\eta C^2)$, T = average taper of feed at dish edge, $K = 20 \log_{10} \{\sqrt{1 + 16(F/D)^2}/4(F/D)\}$, $G_{\text{HORN}} = \text{on-axis gain of horn, all in decibels.}$ Since typical values are T = 10 dB, F/D = 0.3, and $G_{\text{HORN}} = 5 \text{ dB}$, we arrive at the simple result

$$f/b = G + 7 (30-6)$$

which has been empirically known for many years³⁴ and is good, in practice, within 2 to 3 dB.²³

In many installations, f/b ratios of 65 dB or larger are required; we then see from Eq. (30-6) that (for typical 40- to 45-dB-gain dishes) it is impossible to achieve this requirement with standard circular paraboloids. To overcome this fact, edge-geometry schemes are employed (here the circular edge is replaced with a polygonal one so as to destroy, in the back of the dish, the in-phase addition from each increment of the edge). Alternatively, an absorber-lined cylindrical shroud is used (see Fig. 30-1); this decreases the RPE significantly in the shadow of the shroud.

Effect of Vertex Piate

A plane circular plate (vertex plate^{2,35} of diameter DV and thickness T having $DV = 2\sqrt{\lambda F/3}$ and $T = 0.042\lambda$; these dimensions are usually fine-tuned experimentally) is invariably used at the center of the dish (see Fig. 30-6) to minimize the VSWR contribution from the dish. The vertex-plate reflections essentially cancel the remaining dish reflections. This plate also affects the pattern and gain of the dish antenna since it introduces a leading phase error. The result is to raise the close-in radiation levels

^{*}In this figure, $\epsilon_{rms} = 2\Delta n/3$.

[†]This is due to rms effects only; other effects (especially mechanical-feed asymmetry) increase this to 25 to 30 dB down.

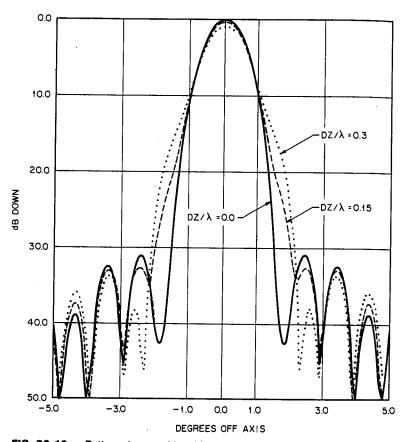


FIG. 30-10a Pattern change with axially displaced feed.

slightly and to cause a slight drop in gain. In some cases, edge diffraction from the plate degrades the RPE somewhat.

Effect of Feed-Support and "Strut" Scattering

The waveguide-bend feed support (see Fig. 30-6) is seen to interfere with the horn fields prior to their striking the dish; this results in amplitude, phase, and symmetry changes. Also, upon reflection, the dish fields pass by the same feed support and the vibration dampers (usually thin wires), where they are again diffracted or reflected. Analyses of these effects have been attempted³⁶ with some success, but in most cases they are usually best corrected by empirically determining the best positioning of absorber layers on the waveguide feed support and by making the vibration dampers from insulating material.

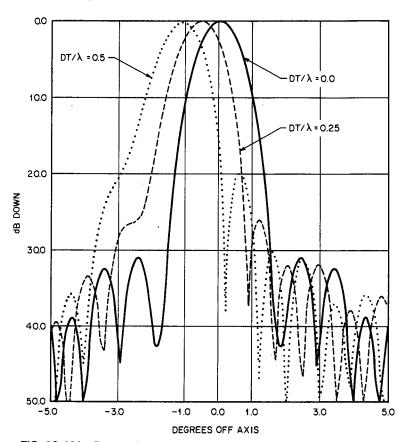


FIG. 30-10b Pattern change with laterally displaced feed.

Effect of Radome

The radome is used to protect the antenna against the accumulation of ice, snow, and dirt. General radome effects are discussed in Chap. 44, but in relay applications the fundamental problems are (1) the VSWR produced by the radome, (2) its total losses, and (3) its pattern influence. In the case of a planar radome (as seen on the antennas in Fig. 30-1), the VSWR increase is cured by tilting the radome a few degrees (moving the top further from dish) to prevent specular return to the feed horn; the loss and RPE influence are held low by using thin, low-loss material (e.g., Teglar, a fiberglass material coated on both sides with Teflon which sheds water readily³⁷). Fiberglass conical or paraboloidal radomes are also used; these reduce wind loading, although since they are thicker than planar radomes, they have higher loss and degrade the RPE somewhat.

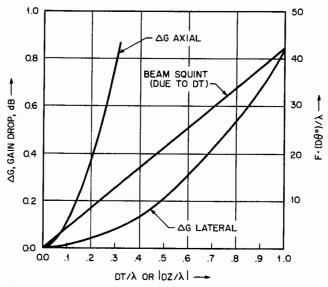


FIG. 30-11 Gain drop and beam squint due to defocusing.

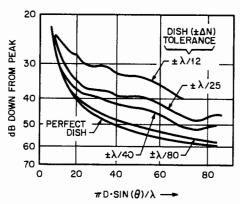


FIG. 30-12 Typical effect of surface errors on RPE. (From Dragone and Hogg.³³)

30-3 THE PARABOLOIDAL GRID REFLECTOR

Here metal (usually aluminum) tubes of outer radius r and center-to-center spacing s (where $s/\lambda \le 0.3$ and $s/r \ge 5$) and of paraboloidal contour replace the solid metal sheet (see Fig. 30-13) and act as a moderately good reflector (see Chap. 46). Typically, $s/\lambda = 0.3$ (maximum spacing possible so as to reduce cost) and s/r = 5.5 to 6

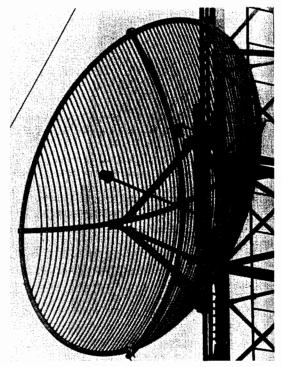


FIG. 30-13 Paraboloidal grid antenna. (Courtesy Andrew Corp.)

(to allow use of commercial aluminum tubes). Moullin's theory³⁸ based on thin wires (for which s and r are adjusted to have the self-inductance and mutual inductance cancel) has been shown³⁹ to give good results; however, it is now known (see Chap. 46) that it is not essential to meet his criterion. The efficiencies of these grid reflectors is typically 5 or so percent below that of a solid reflector (of the same F/D and D and fed with the same horn), and the front-to-back ratio is typically 3 dB lower.* The grid openings cause the wide-angle RPE (especially for $\theta > \theta_D$) to be quite inferior to that of a solid paraboloid (also the tubes have a small kr, where $k = 2\pi/\lambda$, and, as such, scatter readily to the rear). These antennas are used only in remote, uncongested areas not requiring narrow RPE and have the advantage of overall lower cost since their wind loading is much smaller than that of a corresponding solid reflector. This allows less expensive towers (the grid antenna is, however, actually more expensive than its solid counterpart). These antennas are not used above about 3 GHz because of achievable fabrication tolerances and are usable only for a single polarization.

^{*}Fortunately, however, when the grid is mounted on a typical triangular cross-section tower, the back signal is "smeared," bringing the f/b ratio back up to about its solid-dish value.

30-4 THE OFFSET PARABOLOID

To eliminate feed blockage (and its consequent drop in efficiency of about 8 to 10 percent due primarily to the degradation of the prime-feed pattern by the waveguide feed support), one can use the prime-fed offset paraboloid, the geometry of which is shown in Chaps. 17 and 36. This antenna has been known for some time, and analyses by Chu-Turrin and later by Rudge (see Chap. 36 for these references) are available for predicting the front-region fields. Using Rudge's work and trying different feeds. one again arrives⁴⁰ at the conclusion that a good compromise between high gain and narrow RPE is about a 10- to 12-dB edge taper. The copolar patterns for a typical case are similar to those of the prime-fed symmetrical paraboloid, but they have lower near-in sidelobes owing to the absence of blockage. The penalty paid for the removal of blockage is that the asymmetrical plane (i.e., the horizontal plane for terrestrial antennas) now has a rabbit-ear cross-polar pattern with the peaks of the rabbit ears being about 20 dB down from the copolar peak and being located at about the 6-dBdown angle of the copolar pattern (see Chaps. 17 and 36). Dual-polarization operation is, however, still achievable with XPD = -30 dB at the boresight null (the depth of this null being quite sensitive to reflector-surface error). The offset also has the disadvantage of high cost and higher I^2R loss associated with the typically longer feed support.

30-5 CONICAL AND PYRAMIDAL CORNUCOPIAS

These antennas have been used for some time 10,41,42 and probably represent the ultimate in terms of the best wide-angle RPE attainable. In recent years, the conical cornucopia (CC) has found preference over the pyramidal (primarily for economic reasons; also, the pyramidal horn has undesirably high diffraction lobes at 90° which require edge blinders to be suppressed^{43,44}). The CC geometry is depicted in Chap. 17, and a modern-day CC is shown in Fig. 30-14. The CC geometry has a feed offset of 90° (but also has a conical shield) and hence can be handled by the same analysis as in the previous section. However, the classic earlier analysis of Hines et al. (see Ref. 10) is generally used. Briefly, this work shows that the E fields in the projected circular aperture are the conformal transformation of the E fields in the circular aperture of the conical horn. That is, circles (and their perpendiculars) are mapped into circles (and their perpendiculars), except that concentric circles in the conical aperture are no longer concentric in the projected aperture. Double integration of the projectedaperture fields then shows that this produces cross-polarization rabbit ears in the horizontal (asymmetric) plane (again, like the general offset, of typically 20 dB down at the 6-dB angle of the copolar beam).

In most real cases, a shield with absorber lining is used to capture the horn spillover and to reduce (almost eliminate) multiple-scattering effects at wide angles. This absorber introduces a small gain drop (at most, ½ dB). Typically, total efficiencies are about 65 percent; a representative RPE for 6 GHz (also a specification for these antennas) is shown in Fig. 30-2, which is seen to be vastly superior to the A or B FCC specifications. The cornucopia has the advantage of narrow RPE, relatively high effi-

ciency, and simultaneous multiband operation at typically 4-, 6-, and 11-GHz bands (and possibly 2-GHz as well⁴⁴), though it is very costly.

30-6 SYMMETRICAL DUAL REFLECTORS

This antenna type is covered in Chaps. 17 and 36 and hence will only be briefly mentioned here. An old (but very useful) basic "back-of-the-envelope design" Cassegrain configuration is depicted in Fig. 30-15.* Typically, the horn is chosen (see Table 30-

1) to produce an 8- to 10-dB taper at the hyperboloidal subreflector edge where $DE/\lambda \gtrsim 5$. Then a Potter flange is used to capture some of the subreflector spillover energy and effectively use it to scatter back to the dish. 45,46 In this way, directive efficiencies in the mid-60s to low 70s are achievable. A typical design based on Fig. 30-15 for a focal-plane dish of $D/\lambda = 60$ is as follows: choose DE/λ = 6.84, hence DE/D = 0.114; choose M (magnification factor) = 2.81, which gives $a/\lambda = 0.996$, $c/\lambda = 2.097$, and α_E = 39.2°; choose a horn from Table 30-1 (either a corrugated or a Potter horn having zero phase error) of $DH/\lambda = 1.58$ so that $\psi_{10} = \alpha_E = 39.2^\circ$; get $\theta_E = 19.1^\circ$; choose $LE/\lambda = 2$ (not critical); therefore $DO/\lambda = 10.61$ and DO/D = 0.176, which is large but acceptable blockage. At 6 GHz this design gives over 67 percent measured directivity, and its patterns meet FCC specification A. To date, gregorians have found little terrestrial use; they are best suited for antennas with larger F/D ratios. All reasonably efficient dual reflectors suffer from large

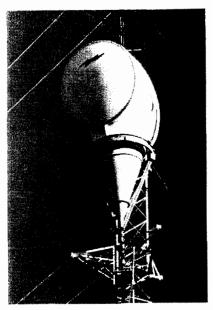


FIG. 30-14 Modern-day conical cornucopia. (*Courtesy Andrew Corp.*; for RPE see Fig. 30-2.)

subreflector blockage problems, since for sharp drop-off of the subreflector pattern near the dish edge one should make $DO/\lambda \gtrsim 5$ (preferably $DO/\lambda \gtrsim 8$, though one should limit blockage to 20 percent or less, $DO/D \lesssim 0.20$). This causes high first (typically 12 to 14 dB), third, etc., sidelobes. To achieve better results (higher efficiencies and better RPEs by minimizing spillover and VSWR) shaping of the subreflector and main reflector is mandatory⁴⁷ (see Chaps. 17 and 36).

^{*}This figure does not show a small cone on the hyperboloid tip used to reduce the VSWR. The cone dimensions are usually determined empirically.

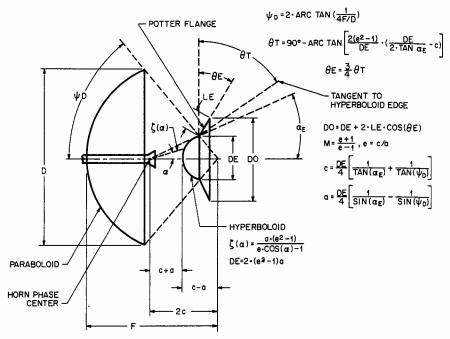


FIG. 30-15 "Back-of-the-envelope-design" Cassegrain configuration.

30-7 MISCELLANEOUS TOPICS

Most antennas usually have pressurized feeders (including the waveguide run from the antenna to the equipment building at ground location) in order to prevent moisture accumulation on the waveguide's inner walls and its ultimate increase in attenuation. Alternatively, for 2 GHz and lower, foam-filled coaxial-cable feeders are used. On paths which do not allow frequent repeater installation (e.g., when mountains or lakes intervene between two sites), gain is of the utmost importance. Here, oversized circular waveguide feeders are used (they, typically, have one-third of the attenuation of dominant-mode-size feeders). Being oversized, they can propagate higher-order modes (typically TM_{01} and TE_{21}), which are removed by mode filters. These paths invariably use Cassegrain antennas (with their typically 10 percent higher efficiency); this combination can give up to 3-dB extra gain per path.

30-8 COMPARISON OF ANTENNA TYPES

A concise summary roughly categorizing the above microwave-relay antennas regarding their efficiency, relative RPE, and cost is given in Table 30-2. Most antennas are designed to operate at their peak efficiency for a specified RPE so as to reduce their

TABLE 30-2 Summary of Microwave-Relay Antennas

Antenna	Total efficiency*	RPE*	Near-in ^e sidelobes	Cost
Solid paraboloid (symmetric prime-fed)	55–60	3	2	1
Grid paraboloid (symmetric prime-fed)	50–55	4	2	2
Offset paraboloid (prime-fed)	6070	2	1	4
Conical cornucopia	65 °	1*	3	5
Cassegrain	65-78 ^f	3	4	3

[&]quot;Including all I^2R loss, feed loss, rms loss, etc.

required dish diameter, since the total cost is approximately proportional to the diameter squared or more.⁴⁸

30-9 RECENT DEVELOPMENTS

Complete Radiation-Field Expressions for Symmetrical Prime-Fed Dish

In recent years, powerful PC computers have become available allowing programming of the complete radiation-field expressions from the prime-fed dish of Fig. 30-3. Accordingly, these expressions are given in Table 30-3. In the program one reads-in the primary horn pattern file as defined by (1) of Table 30-3, namely, ψ , $ADB(\psi)$, $\alpha(\psi)$, $BDB(\psi)$, and $\beta(\psi)$, with ψ in degrees as measured from the horn's axis. Here $A(\psi) = 10^{-ADB(\psi)/20}$, $B(\psi) = 10^{-BDB(\psi)/20}$ are the horn's E- and H-plane voltage patterns, with $ADB(\psi)$ and $BDB(\psi)$ being the corresponding decibel down-power patterns, and $\alpha(\psi)$ and $\beta(\psi)$ are the E- and H-plane phase patterns. The program then obtains, via (3), (17), and (26) of Table 30-3, the far fields produced by the dish in regions 1, 2, and 3, respectively, as there-defined, where (18) and (19) of Table 30-3 are the dish's GTD diffraction coefficients 19,20 and the Kouyoumjian transition function, 49 respectively, and $J_0(x)$ is the Bessel function of zero order of the first kind, etc.

Universal Design Curves for a Symmetrical Prime-Fed Dish

A popular feed used to illuminate symmetrical prime-fed dishes is the MD ("magic diameter") circular waveguide TE_{11} mode Croswell-type⁵⁰ feed, which has about a wavelength diameter and a small exterior $\lambda/4$ choke giving about 10 dBi directivity, with almost equal E- and H-plane patterns, as shown in Fig. 30-16a. Universal design curves can be

Excluding near-in sidelobe levels, 1 = lowest energy level.

^{&#}x27;1 = lowest energy level.

d1 = lowest cost.

With absorber in cylindrical shield.

Shaped.

TABLE 30-3 Radiation-Field Expressions for a Symmetrical Prime-Fed Dish

HORN FIELDS ($-E_r$ polarization)

(1)
$$\begin{bmatrix} E_{\theta}(\rho, \psi, \xi) \\ E_{\phi}(\rho, \psi, \xi) \end{bmatrix} = \begin{bmatrix} \frac{\epsilon_0}{k\rho(\psi)} \end{bmatrix} e^{-jk\rho(\psi)} \begin{bmatrix} A(\psi)e^{j\alpha(\psi)}\cos\xi \\ B(\psi)e^{j\beta(\psi)}\sin\xi \end{bmatrix}$$

(2)
$$A(\psi) = B(\psi) = 1.0$$
 $\alpha(\psi) = \beta(\psi) = 0$ at $\psi = 0$

REGION 1 FIELDS $[0 \le \theta \le \theta_1 \approx 360^\circ/(D/\lambda)]$

(3)
$$\begin{bmatrix} E_{\theta}(r, \theta, \phi)/E_{0} \\ E_{\phi}(r, \theta, \phi)/E_{0} \end{bmatrix} = \frac{jC}{2F/D} \begin{bmatrix} \cos \phi \ (IER + jIEI) \\ \sin \phi \ (IHR + jIHI) \end{bmatrix} + \begin{bmatrix} A(\psi)e^{j\alpha(\psi)}\cos \phi \\ B(\psi)e^{j\beta(\psi)}\sin \phi \end{bmatrix}$$
where $\psi = \pi - \theta$

(4)
$$C = (\pi D)/\lambda$$

(5)
$$\psi_D = 2 \arctan [1/(4F/D)]$$

(6)
$$E_0 = (\epsilon_0 e^{-jkr})/kr$$

(7)
$$\rho(\psi) = 2F/(1 + \cos \psi)$$

(8)
$$k = 2\pi/\lambda$$

(9)
$$\begin{pmatrix} IER \\ IEI \\ IHR \\ IHI \end{pmatrix} = \int_{DE/D}^{1.0} (1/2) \cos^2 \left[\psi(w)/2 \right] \begin{bmatrix} f_{ER}(w) \\ f_{EI}(w) \\ f_{HR}(w) \\ f_{HI}(w) \end{bmatrix} wdw$$

(10)
$$w = [\rho(\psi) \sin \psi]/(D/2) = 4(F/D) \tan (\psi/2)$$

(11)
$$\cos^2 \left[\psi(w)/2 \right] = \frac{16(F/D)^2}{\left[w^2 + 16(F/D)^2 \right]}$$

(12)
$$\begin{bmatrix} f_{ER}(w) \\ f_{EI}(w) \\ g_{HR}(w) \\ g_{HI}(w) \end{bmatrix}$$

$$= \begin{cases} A\cos(f-\alpha)\cos\theta(DBJ) - [Uw\sin\theta A\sin(f-\alpha)\tan(\psi/2) - B\cos(f-\beta)\cos\theta](SBJ) \\ -A\sin(f-\alpha)\cos\theta(DBJ) - [Uw\sin\theta A\cos(f-\alpha)\tan(\psi/2) + B\sin(f-\beta)\cos\theta](SBJ) \\ -A\cos(f-\alpha)(SBJ) - B\cos(f-\beta)(DBJ) \\ A\sin(f-\alpha)(SBJ) + B\sin(f-\beta)(DBJ) \end{cases}$$

with
$$A = A(\psi)$$
, etc.

(13)
$$f(\psi) = [2kF(1 + \cos \psi \cos \theta)]/(1 + \cos \psi)$$

(14)
$$SBJ = J_0(Uw) + J_2(Uw)$$

(15)
$$DBJ = J_0(Uw) - J_2(Uw)$$

$$(16) \quad U = C \sin \theta$$

TABLE 30-3 (Continued)

REGION 2 FIELDS $(\theta_1 \le \theta \le \theta_2 \approx 175^\circ)$

$$(17) \begin{bmatrix} E_{\phi_d}^{\pm}(r,\theta,\phi) \\ E_{\phi_d}^{\pm}(r,\theta,\phi) \end{bmatrix}$$

$$= \frac{\epsilon_0 e^{-jk\rho_D}}{k\rho_D} \begin{pmatrix} D_H^{\pm} A_D e^{j\alpha_D} \cos \phi \\ D_S^{\pm} B_D e^{j\beta_D} \sin \phi \end{pmatrix} (PF^{\pm})(CDF^{\pm}) + \begin{bmatrix} A(\psi) e^{j\alpha(\psi)} \cos \phi, \ \theta_1 \le \theta \le \theta_D \\ 0, \ \theta_D < \theta \le \theta_2 \\ B(\psi) e^{j\beta(\psi)} \sin \phi, \ \theta_1 \le \theta \le \theta_D \\ 0, \ \theta_D < \theta \le \theta_2 \end{bmatrix}$$

where $\psi = \pi - \theta$; $A_D = A(\psi)$ at $\psi = \psi_d$, etc.

(18)
$$\binom{D_{S}^{\pm}}{D_{H}^{\pm}} = \frac{-e^{-j\pi/4}f^{\pm}(\theta)}{2\sqrt{2\pi k}} \begin{bmatrix} \frac{F_{1}^{\pm}}{\sin\left[(\theta_{D} \mp \theta)/2\right]} \pm \frac{F_{2}^{\pm}}{\sin\left(\theta/2\right)} \\ \frac{F_{1}^{\pm}}{\sin\left[(\theta_{D} \mp \theta)/2\right]} \mp \frac{F_{2}^{\pm}}{\sin\left(\theta/2\right)} \end{bmatrix}$$

with

(19)
$$F_{1,2}^{\pm} = +j2\sqrt{X_{1,2}^{\pm}} \exp(jX_{1,2}^{\pm}) \int_{\sqrt{X_{1,2}^{\pm}}}^{\infty} \exp(-jx^2) dx$$

(20)
$$\left(\frac{\sqrt{X_1^{\pm}}}{\sqrt{X_2^{\pm}}} \right) = \sqrt{\frac{2C}{\sin \theta_D}} \left\{ \frac{\left| \sin \left[(\theta_D \mp \theta)/2 \right] \right|}{\left| \sin \left(\theta/2 \right) \right|} \right\}$$

(21)
$$PF^{\pm} = \text{phase factor} = \exp[-jk(r \mp a \sin \theta - \rho_D \cos \theta_D \cos \theta)]$$

(22)
$$CDF^{\pm} = \text{caustic divergence factor} = (b^{\pm}) \frac{1}{r} \sqrt{\frac{a}{\sin \theta}}$$

(23)
$$b^+ = +1$$
 $b^- = +j$

(24)
$$f^{+}(\theta) = +1$$
 for all θ

(25)
$$f^{-}(\theta) = \begin{bmatrix} +1 & 0 \le \theta \le (\pi - \theta_D/2) \\ -1 & (\pi - \theta_D/2) < \theta \le \pi \end{bmatrix}$$

REGION 3 FIELDS ($\theta_2 \le \theta \le 180^\circ$)

where

(27)
$$T_{\pm} = 1/\cos(\theta_D/2) \pm 1$$

(28)
$$B_{\pm} = J_0(U) \pm J_2(U)$$

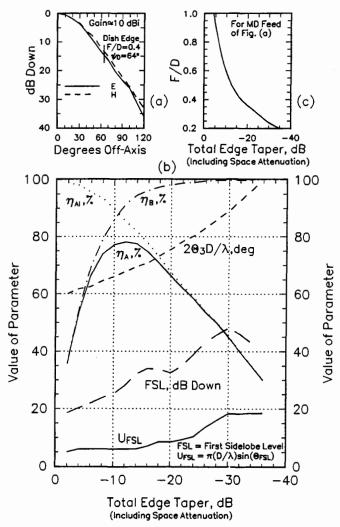


FIG. 30-16 Universal design curves for a paraboloidal dish. (a) Magic diameter (MD) feed patterns. (b) Design curves for use with "any" feed. (c) F/D choice versus dB edge taper for MD feed of (a).

obtained by inserting its feed file in the programmed results of Table 30-3 for various F/D dishes. The end results are given in Fig. 30-16b, which shows the beam efficiency (η_B) , the percent of the horn's energy captured by the dish), total aperture efficiency (η_A) , the aperture illumination efficiency (η_A) and (η_A) , the product of D/λ with the full half-power

^{*}Note: $\eta_B = I_4/I_3$, $\eta_A = \cot^2(\psi_D/2)(I_1 + I_2)/I_3$, where $I_1 = |\int_{\frac{\pi}{2}}^{\pi} (A \cos \alpha + B \sin \beta) \tan (\psi/2) d\psi|^2$, $I_2 = |\int_{\frac{\pi}{2}}^{\pi} (A \sin \alpha + B \sin \beta) \tan (\psi/2) d\psi|^2$, $I_3 = \int_{0}^{\pi} (A^2 + B^2) \sin \psi d\psi$, $I_4 = \int_{\frac{\pi}{2}}^{\pi} (A^2 + B^2) \sin \psi d\psi$, $\psi_B = 2 \arctan (1/[4(F/DE)])$, $\psi_D = 2 \arctan (1/[4(F/D)])$, η_A and η_B numerics.

beamwidth in degrees $(2\theta_3^\circ)$, the first sidelobe level, FSL (in decibels down from the main beam), and the universal angle at which it occurs $[U_{\rm FSL} = \pi(D/\lambda)\sin\theta_{\rm FSL}]$, along with the DB edge illumination's dependence on the dish's F/D for this particular MD feed. Thus, if one wishes to obtain peak efficiency operation (about $\eta_A = 76\%$, neglecting other loss factors), one can choose "any" feed/dish combination (where the feed need not be the MD feed of Fig. 30-16a but any feed having virtually identical E- and H-plane patterns, despite their width, and low wide-angle radiation) giving about a -12-dB total edge taper, for which the first sidelobe level will be about 28 dB down and occur at a $U_{\rm FSL}$ of about 6.0 (so if $D/\lambda = 120$, $\theta_{\rm FSL} = 0.9^\circ$, etc.). A choice of overillumination, i.e., an edge taper above this -12-dB value (to give a narrower beamwidth), results in a lower η_A because the product of $\eta_{AI} \cdot \eta_B$ is lowered (η_{AI} rises but η_B falls more rapidly); likewise, underillumination, i.e., an edge taper under -12 dB (to give lower sidelobes), also results in a lower η_A (η_B rises but η_{AI} falls more rapidly).

More on Feed Displacement

To supplement the results of Figs. 30-10 and 30-11 above, Fig. 30-17 shows extensive results reported by Milligan⁵¹ for a dish illuminated by a typical feed providing about a -10- to -12-dB edge taper. Thus (a) of this figure shows the gain drop due to axial defocusing and (b) shows the gain drop due to the E- and H-plane phase centers being

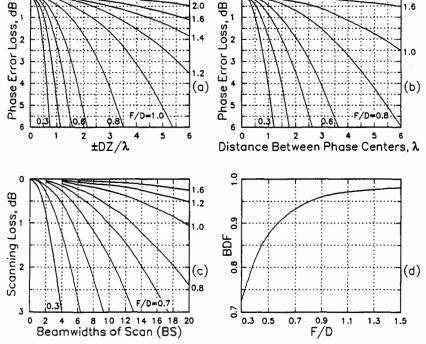


FIG. 30-17 Gain loss of main beam due to phase errors. (a) Due to phase error caused by feed's axial defocusing. (b) Due to difference between E- and H-plane phase centers. (c) Due to transverse feed movement (main beam tilts/scans). (d) The BDF factor dependence on F/D. (From Ref. 51.)

displaced. Both figures have F/D as a parameter and both are self-explanatory. Figure 30-17c shows the gain loss (of the displaced beam) as a function of the number of full half-power beamwidths BS scanned by the displaced beam due to a transverse feed movement by DT, where the beam is displaced to the side opposite the feed displacement by $[(DT/F) \cdot BDF]$ radians, where BDF is the beam deviation factor given by Fig. 30-17d. Thus, since $2\theta_3 \approx 1/(D/\lambda)$ radians, then $BS = \{[(DT/\lambda)/(F/D)] \cdot BDF\}$. Thus, for example, for a dish of F/D = 0.30 with $DT/\lambda = 1$, BS = (1/0.3)(0.73) = 2.43, so the scan loss is about 1.3 dB, etc.

Cross-Polar Fields Produced by a Symmetrical Prime-Fed Dish

The cross-polar fields (here taken as defined by Ludwig's No. 3 definition^{51a,51b}) produced by the dish can be obtained from the E_{θ} and E_{ϕ} field expressions of Table 30-3 as (for the $-E_x$ polarization chosen here) $E_{CROSS} = -E_\theta \sin \phi - E_\phi \cos \phi$ with the copolar field as $E_{\infty} = -E_{\theta} \cos \phi + E_{\phi} \sin \phi$. From (3) of Table 30-3 it can be shown that the E_{θ} and E_{ϕ} fields produced by the dish have the same form as the horn fields of (1) of that table. Hence the XPD* produced by the dish is proportional to $H \cos \phi \sin \phi$, having a peak ("rabbitear") in the 45° planes, where H is an amplitude factor proportional to the integration of the term $[A(\psi)e^{j\alpha(\psi)} - B(\psi)e^{j\beta(\psi)}]$ over the dish surface. Thus, in this physical-optics approximation, $(D/\lambda \ge 10, F/D \ge 0.2)$, there will be no cross-polar fields (XPD = $-\infty$) if the feed's E- and H-plane patterns are identical, that is, $A(\psi) = B(\psi)$ and $\alpha(\psi) = \beta(\psi)$, over the dish surface. If actual feeds are used, then the peak XPD "rabbit-ear" off the dish is, typically, predicted (via use of Table 30-3 results) to be (in the absence of struts or waveguide feeders, etc.) 4 to 7 dB lower than that of the feed itself (e.g., the MD feed having the E- and H-plane patterns of Fig. 30-16a has a peak XPD of about -35 dB, whereas that off a typical dish is predicted to be about -41 dB); this is so because the dish's gain for the cross-polar fields of the horn is less than that for the copolar fields of the horn, since the cross-polar fields of the horn effectively illuminate the dish only in areas centered at the feed's "rabbit-ears" (areas about the $\phi = 45^{\circ}$ points at ψ values corresponding to about 6 dB down of the feed's power). However, if struts or waveguide feeds of an asymmetrical type are used, then, typically, the dish's "rabbit-ear" will degrade relative to that of the feed (this usually being determined empirically). The search for superior high XPD feeds ("rabbit-ear" peaks less than about -50 dB) is currently still under way to realize superior-simultaneous dual-polarization operation at a single frequency in communication/radar systems as well as for radio astronomy applications (where the curved corrugated wall horn⁵² is probably the best achievable to date).

Effect of Periodic Dish Imperfections on Near On-Axis Sidelobes

There are two types of periodic dish imperfections which can seriously degrade the near on-axis sidelobe performance. The first, and most sensitive, is a radial periodicity (usually caused by rib periodicity and/or periodic protruding-bolt heads). Based on the work of Korman et al., 32 if a spatial periodicity of length λ_s between peaks exists on a uniform linear array, then pattern "spikes" (in the form of a duplication of the array pattern centered at these spikes) will occur at an angle off the main beam of about

$$\theta_{\rm s} = \arcsin\left(\lambda/\lambda_{\rm s}\right) \tag{30-7}$$

where λ is the operating wavelength. Using a double integration to obtain the pattern from

^{*}XPD (θ, ϕ) = 20 $\log_{10} |E_{CROSS}(\theta, \phi) / E_{CO}(\theta, \phi)|$.

a dish with imperfections, similar results are found for a symmetrical reflector having radial periodicities of λ_z , as shown in Fig. 30-18b-d, which is for a 30.5-ft dish operating at 6.425 GHz and having, respectively, three, four, and five radial sinusoidal cycles from the dish center to its edge (that is, $\lambda_z = 61.000$, 45.750, and 36.600 in, respectively) with a peak magnitude 0.100 in (about $\lambda/18$). These computer results show that the pattern with no imperfections (Fig. 3-18a) has its sidelobes raised to a peak at 1.81, 2.45, and 2.88° off-axis for these cases, respectively, which agrees fairly well with predictions using Eq. (30-7) of 1.73, 2.30, and 2.88°, respectively. It is also seen that, in agreement with Korman et al., 32 these peaks tend to rise from this level with no imperfections to a level only determined (for a given amplitude taper) by their height in wavelengths, i.e., here (for this tapered aperture distribution) to about 20 $\log_{10} (0.65 h/\lambda)$ dB relative to the main beam (here about 29 dB down), where this 0.65 factor increases toward $\pi/2$ as the aperture distribution approaches uniformity.

The second type of imperfections are those occurring in the circumferential directions (due, usually, to pie-panel construction with inadequate alignment between pie sections). Here computations disclose that for N circumferential cycles (2N panels), the patterns, at a given θ , have N cycles as a function of ϕ if N is odd and 2N cycles if N is even and that for a given peak height in wavelengths, H/λ , the amplitude of these oscillations about their perfect reflector values, decreases with increasing N (for example, for the above 30.5-ft dish at 6.425 GHz, if $H/\lambda = 1/36$, they are ± 2 dB for N = 3 and ± 0.5 dB, or less, for $N \ge 8$). This suggests using the maximum number of panels (consistent with mechanical/cost considerations) to minimize pattern distortions for a given H/λ .

FFT techniques^{53,54} also can be used to analyze pattern degradation caused by dish imperfections. These give three-dimensional representations and are faster than direct double integration. An example⁵³ is shown in Fig. 30-18e-g for this same antenna (again at 6.425 GHz) for the case of three radial cycles ($\lambda_z = 61.00$ in) of peak height $H = \lambda/72$, that is, 10° peak to peak, in the H-plane only, giving, via Eq. (30-7), $\theta_z = 1.73$ ° (i.e., the fifth sidelobe, via Fig. 30-18a). Figure 30-18a shows the difference pattern (that produced by the periodicities only), which has its peak at the fifth sidelobe (and falls off, about this peak, similar to that of the undistorted dish pattern, again in basic agreement with Korman et al. ³²).

Safety Concerns — Near-Field Power Densities

Environmental/hazard questions about the peak power densities produced by a reflector antenna are now frequently raised. As has been known for some time, ⁵⁵ the worse situation is a factor of 4 (6 dB) increase (relative to that at the aperture center) which occurs for a uniformly illuminated circular aperture for which the on-axis peak power density oscillates (by +6 dB to virtually infinity) about that at the aperture's center at on-axis points between $0 \le \gamma \le 0.12$, where $\gamma = z/[(2D^2)/\lambda]$, where the fall-off approaches 1/r as γ approaches or exceeds unity. If the aperture is tapered, the on-axis oscillations become less severe (for example, ± 1.5 dB for a cosine-type distribution with a -17-dB edge taper), as shown in Fig. 30-19a and b. The transverse behavior (important, for example, for determination of the power density produced directly below an antenna, etc.) is shown in Fig. 30-19c for this tapered case and the uniform case at constant axial distances corresponding to $\gamma = 0$ (i.e., at the aperture) and $\gamma = 0.12$.

Near-Field Focusing

Occasionally, a microwave radio-relay hop has tall buildings blocking the end of a route,

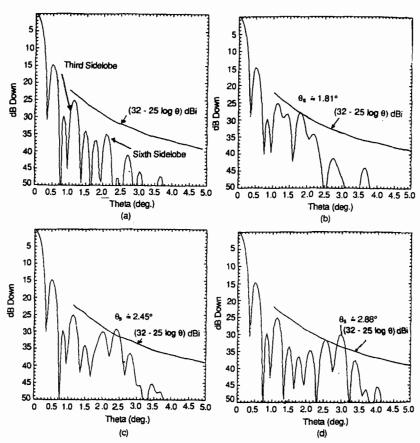


FIG. 30-18 Degradation of radiation patterns due to dish periodicities (30.5-ft dish at 6.425 GHz). (a) For perfect dish. (b) For radial periodicity of $\lambda_s=61.000$ in and H=0.100 in. (c) For radial periodicity of $\lambda_s=45.75$ in and H=0.100 in. (d) For radial periodicity of $\lambda_s=36.60$ in and H=0.100 in. (e) Three-dimensional pattern for perfect dish. (g) Three-dimensional pattern for radial periodicity of $\lambda_s=61.00$ in, $H/\lambda=1/72$ in H-plane only. (g) Difference patterns [between (e) and (f)].

in which case two closely spaced dishes are then employed to bypass the building. In this situation, the dishes can be in the near field of each other and experience a severe gain drop relative to their usual far-field gain. This is shown in Fig. 30-19 and also in Fig. 30-20b for the case of a 12-ft dish of F/D = 0.40 illuminated with an MD feed at 3.95 GHz. If the dishes are of equal diameter and are spaced very close so that $\gamma \approx 0.06$ (which is rare), then it follows from the section "Safety Concerns—Near-Field Power Densities" that their feeds can be left with their phase centers at the focal point of the dish and they can be operated as beam waveguides where the energy is, essentially, transmitted as a plane-wave cylindrical beam having the dish diameter 56,57 (realizing that an echo may exist between them unless they are offset types). If, however, the dish spacing is such that $\gamma \approx 0.06$ (as is

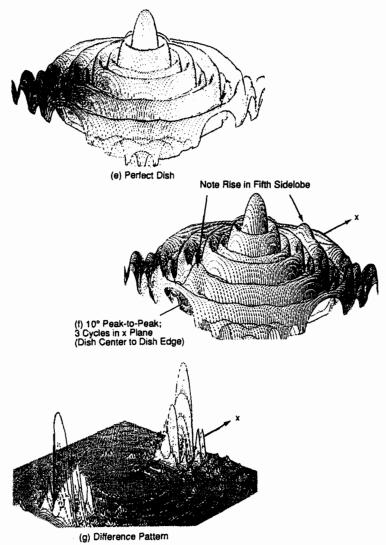


FIG. 30-18 (Continued)

usually the case), then transverse spreading occurs. In this case, the feeds can be moved axially away from the focal point and the dish by amount DZ/λ given (for $\gamma = K/2 \ge 0.06$) approximately ^{58–60} by

$$DZ/\lambda \approx (F/D)^2 \frac{1 + [4(F/D)]^{-2}}{K}$$
 (30-8)

where $K = 2\gamma$, to virtually recover the far-field gain. This relation follows from examining

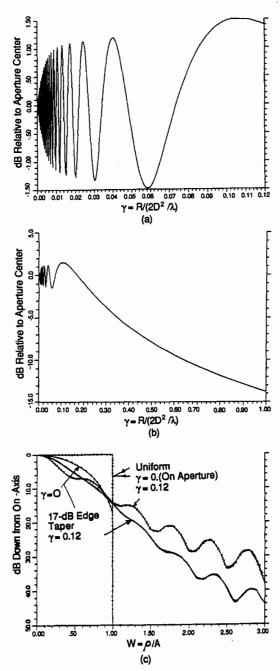
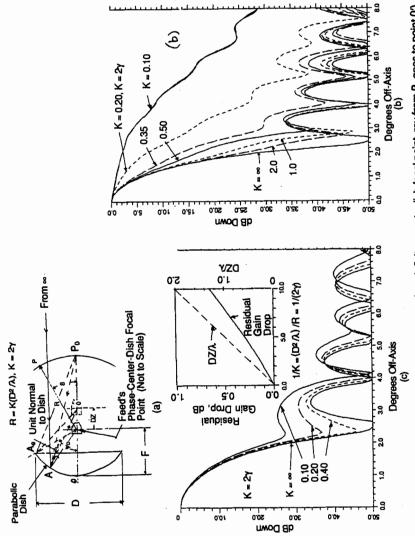


FIG. 30-19 Power density produced by a circular-aperture antenna. (a) On-axis behavior for -17-dB taper, $0 \le \gamma \le 0.12$. (b) On-axis behavior for -17-dB taper, $0 \le \gamma \le 1.00$. (c) Transverse behavior for -17-dB taper and uniform case, $\gamma = 0$ and $\gamma = 0.12$.



b) Pattern dependence on observation distance of $R = (KD^2)/\lambda$ with feed-phase center at focal point (D = 12 ft, MD)eed, 3.95 GHz, F/D=0.400). (c) Pattern dependence on observation distance of $R=(KD^2)/\lambda$ with feed-phase center at DZ = 0.200/K (DZ dependence on K shown on insert with residual gain drop), for D = 12 ft, MD feed, 3.95 GHz, FIG. 30-20 Near-field focusing. (a) Geometry (ray from infinity goes to dish focal point, ray from P_0 goes to point 0). F/D = 0.400

the geometry of Fig. 30-20a and equating the center ray path $(P_0 \ 0 \ 0')$ and the extreme-edge ray path $(P_0 \ A_e \ 0')$ from an on-axis near-field point at P_0 to its new reflected on-axis point 0' (a distance DZ to the right of the dish's focal point). This formulation neglects feed taper; actual numerical-pattern (double-integral) computations give the results of Fig. 30-20c, with the residual gain drop (that portion, relative to the far-field gain, unable to be recovered) shown on the insert. This insert gives $DZ/\lambda = 0.200/K$ for this F/D = 0.400 case, whereas Eq. (30-8) gives $DZ/\lambda = 0.223/K$; that is, Eq. (30-8) should be multiplied by about 0.90 for this -17-dB case (and hence, presumably, by factors between 0.90 and 1.00 for total edge-taper cases between -17 and 0 dB). It is also noted⁶⁰ that to achieve near-field focused patterns having a sharpest first null rather than peak gains, the result of Eq. (30-8) should be multiplied by slightly less than 0.90 and that focusing concepts similar to the above hold for linear^{61,62} and planar⁶³ arrays.

More on Blockage and Strut Effects

As noted in Sec. 30-2, feed/subreflector blockage and wires or struts can degrade pattern and gain. Exact integral-equation treatments are now, in principle, possible⁶⁴ but presently are limited to small dishes $(D/\lambda \le 10)$ due to computer matrix-inversion limitations. For degradation of gain and near on-axis sidelobes, a simple blockage approach (omission of the blocked effective area of the strut from the integration over the dish aperture or over the dish surface) has been shown⁶⁵ to give good results for angles off axis of $\theta \leq \theta_c$, where $\theta_c = (0.523/[(L/\lambda)\sin\psi_r])^{1/2}$ radians, where L is the strut length and ψ_r is the acute angle the strut makes with the axis, as shown in Fig. 30-23a. This blockage approach is similar to that used to assess feed or subreflector blockage (some results for which are shown in Fig. 30-21 for a circular feed or subreflector blockage in a dish with a - 17-dB edge taper; the factor 4.5 in the ΔG , gain drop, expression in this figure varies from unity for uniform illumination to higher values for tapered illuminations3). The gain drop, in decibels, due to the struts has an upper bound of $-10 \log_{10} (1 - A_1/A_D)$, where A₁ is the effective projected area of the struts and A_D is the dish's aperture area (less aperture blockage). The effects of feed tapering reduce the drop below this bound. 3.68 Some results for strut blockage (for a 12-ft dish at 3.95 GHz with 1.2-in-diameter struts, which have, via Fig. 30-23c, an effective width of 2 in) are shown in Fig. 30-22, which is self-explanatory. Examination of these results discloses that the most serious pattern degradation occurs in planes perpendicular to the strut. For this reason, the most common configuration is the four 90° struts of Fig. 30-22f-1 which also, due to symmetry, have cross-polar components that cancel on axis (if the construction is perfect).

For assessment of wide-angle scattering, it is normal practice to use the induced-field method, $^{66.67}$ which treats the strut as a scatterer that is illuminated by an incident plane wave off the dish establishing a traveling-wave current, like that on a thin wire, and producing a specular cone of reflection centered about the strut with its maximum lobe, in the plane of the strut, occurring at an angle along the axis in line with the dish's main beam and at an angle ψ_s , as depicted in Fig. 30-23b. For any specified azimuthal angle ϕ in the far-field (where $\phi = 0$ is taken along the upper vertical as shown in the insert of Fig. 30-23e), the polar angle θ_i at which this specular cone from a given ith strut has its peak lobe is given by

$$\theta_i = 2 \arctan \left[-\tan \psi_i \cos (\phi - \phi_i) \right]$$
 (30-9)

where ϕ_i is the azimuthal angle of the *i*th strut. Usually it suffices to determine the locations and magnitudes of the peak scattered lobes. This can be done quickly without a

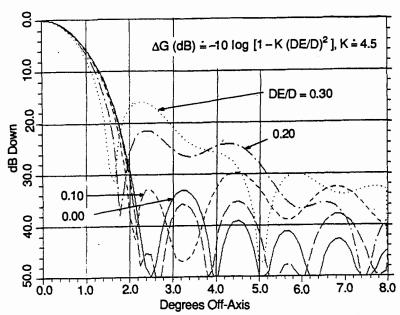


FIG. 30-21 Typical effects of circular feed (or subreflector) blockage on dish patterns (DE/D = blockage ratio; associated gain drop also indicated), for D = 12 ft, MD feed, 3.95 GHz, F/D = 0.400.

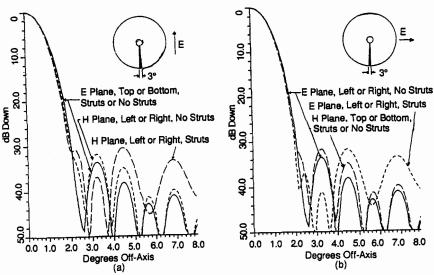


FIG. 30-22 Predicted effects on near on-axis dish patterns due to strut blockage (D=12 ft, MD feed, F/D=0.400, f=3.95 GHz, 1.2-in-diameter strut, modeled by 3° strut).

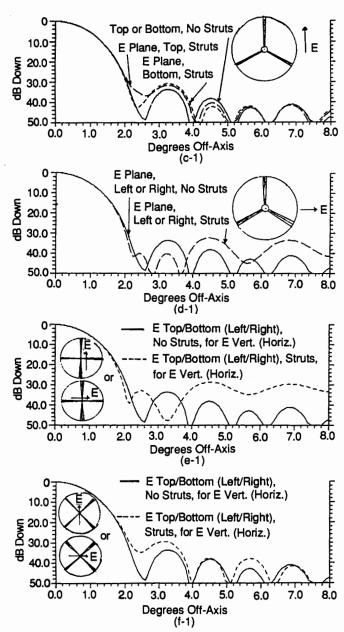


FIG. 30-22 (Continued)

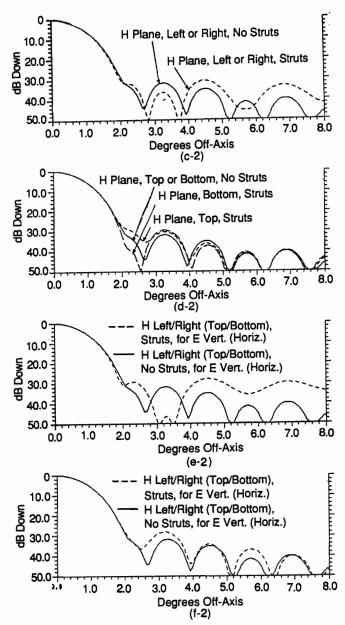


FIG. 30-22 (Continued)

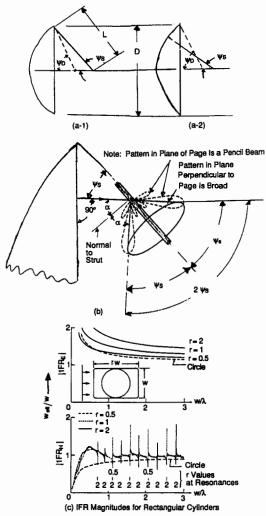
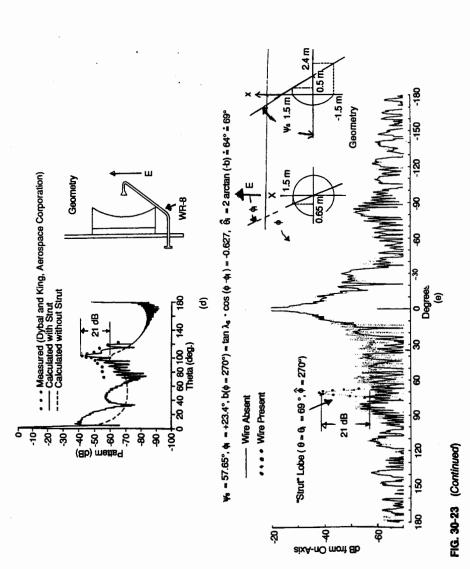


FIG. 30-23 Wide-angle strut scattering. (a-1) Desired strut geometry for minimizing pattern degradation. (a-2) Strut geometry for increased strength. (b) Typical strut and associated specular-reradiation cone. (c) Rusch's induced field ratio⁶⁰ (i.e., increase of effective strut width due to diffraction). (d) Measured and induced-field E-plane pattern of 6-in-diameter dish with and without a WR-8 strut⁶⁰ at 92 GHz. (e) Measured and Induced-field H-plane pattern of dish with and without "thin" wire⁷⁰ at 7.5 GHz.



30-39

computer as follows: For the case of a single strut, the total power density S produced at the point $P(\theta_i, \phi)$ is that from the dish S_D plus that from the strut S_S , that is, $S = S_D + S_S = S_D(1 + S_S/S_D)$. But $S_D = (P_D g_D)/(4\pi r^2)$, $S_S = (P_S g_S)/(4\pi r^2)$, where P_D is the total power passing through the dish's aperture and P_S is the power effectively captured by the strut and reradiated, which is, approximately, $P_S = (A_S/A_D)P_D$, where A_S is the capture area of the strut, $A_S = (w_{\rm eff}D)/2$, with $A_D = (\pi D^2)/4$ (assuming DE/D and A_S are small). In the preceding, g_S and g_D are the directivities in dBi, of the strut and dish, evaluated at the strut lobe location, respectively. Thus $S = S_D(1 + R)$, where $R = (A_S g_S)/(A_D g_D)$. Now, noting that $g_S = \eta_S (4\pi w_{\rm eff}L)/\lambda^2$ and $g_D = [(4\pi A_D \eta_A)/\lambda^2] \cdot 10^{-DBS/10}$, where η_S and η_A are the strut's and the dish's "aperture" efficiency factors (the former due to the aperture taper and the azimuth-dependent scattering about the strut, since it is not really a thin wire) and DBS is the number of decibels down, the dish pattern is at $\theta = \theta_I$ in the strut's absence. Thus R becomes

$$R = \frac{0.405 \, \eta_S [(w_{\text{eff}}/\lambda)/(D/\lambda)]^2 \cdot 10^{\text{DBS/10}}}{\eta_A \sin \psi_S}$$
 (30-10)

and hence the decibel increase SDB in S_D to S due to the strut is SDB = $10 \log_{10}(1 + R)$. If more than one strut produces a lobe at θ_i , then an additional 6-dB increase for a strut pair should be added to SDB as a worse (in-phase) case. In the preceding, it was mentioned that a thin wire or strut of diameter w can have a much larger effective scattering diameter were than w. This is so because the actual forward scattered field produced relative to that which would be produced by assuming an induced current equal to twice the incident tangential magnetic field (i.e., by assuming a scattering coefficient of -1 for the strut), if solved exactly, gives the results (in magnitude) obtained by Rusch^{68,69} of Fig. 30-23c. The ratios given by this figure are then w_{eff}/w and are seen to be, for a given w/λ , highest for the TM case (E field parallel to strut) and to be higher for rectangular or square struts as compared with circular struts. The limiting case of a vanishingly thin wire is not shown on these curves but is given by, for the TM case, $w_{\rm eff} = \lambda/(2\pi)$ [as can be obtained from the known directivity $(2L)/\lambda$ of a uniformly illuminated thin wire of length L and equating this times η_S to $(4\pi\eta_S Lw_{\rm eff})/\lambda^2$]. As an example, consider the strut dish case 66 shown in Fig. 30-23d, for which $\phi_i = \pi$, w = 0.14 in, $w/\lambda = 1.09$ (so $w_{\text{eff}}/w = 1.16$, via Fig. 30-23c, top figure, for a WR-8, r = 0.7, waveguide strut), $D = 47\lambda$, $\psi_s = 55^\circ$, $\eta_A = 0.70$, and $\eta_s = 0.4$, so using Eq. (30-9) with $\phi = \phi_i + \pi = 2\pi$ gives $\theta_i = 2\psi_s = 110^\circ$. From the pattern with no struts present, we see DBS \doteq 59 dB, and hence Eq. (30-10) gives $R \doteq$ 162, that is, SDB = 22 dB, which, as seen from Fig. 30-23d, is close to the measured/computed⁶⁶ value of 21 dB.

The case of a thin circular wire ($w/\lambda = 0.3$, so $w_{\rm eff}/w = 2.0$) placed in front of a dish, ⁷⁰ as shown in Fig. 30-23e (here $D/\lambda = 75$ with $\psi_S = 57.7^{\circ}$, DBS = 59 dB, $\eta_A = 0.7$, $\eta_S = 1.0$), gives SDB = 21.5 dB (where here L is doubled, that is, R is quadrupled, since the wire extends across the entire dish aperture), which is close to the 21 dB measured (it being somewhat less because the wire is at a slight angle to the E field). Thus, here, about a 6-dB increase occurs in the strut lobe level due to the increase in effective strut width by a factor of 2.0, this being significant for EMI concerns. To reduce the specular lobes, one can curve the strut in a circular or parabolic arc with a maximum displacement of S, where $S/\lambda = 1.50$ or 3.5 for dishes having strut lengths of 20 and 80λ , respectively, to achieve about a 10-dB reduction. ⁷¹⁻⁷⁴ Also, it is noted that to prevent the specular lobe from the strut from hitting the dish (and then scattering in a broad-defocused manner, since the specular lobe's source is not at the dish's focal point), one should, if possible, choose $2\psi_S < \theta_D$, that is, $\psi_S < 90 - \psi_D/2$.

Improved Offsets

The prime-fed offset is now in common use (especially as a Ku-band VSAT antenna). To reduce the level of the cross-polar "rabbit-ears," an extra TE_{21} mode in a "($TE_{11} + TM_{11}$)" feed (such as a Potter- or Turnin-type feed, see Chap. 15, giving close E- and H-plane patterns), as developed by Rudge et al., 75,76 can be used. This TE_{21} mode, properly adjusted in amplitude and phase, generates cross-polar "rabbit-ears" which, upon striking the dish, cancel (or at least reduce) those produced by the dish itself. This reduction broadens the angular region about on axis at a specified cross-polar level and allows, at a given frequency, simultaneous dual-polarization* (frequency reuse) operation even under windy conditions, etc. Alternatively, a dual-reflector parabolic offset antenna can be used with its horn/subreflector angle set at the Mizugutch et al. 77 cross-polar cancellation condition of

$$\tan \delta = \frac{(1 - e^2)\sin \beta}{(1 + e^2)\cos \beta - 2e}$$
 (30-11)

where e is the ellipticity of the subreflector (Cassegrain or gregorian), δ is the angle between the horn's axis and the line \overline{OF} (that joining the horn's phase center, where the horn is pointing down, and the dish's focal point), and β is the angle between the dish's main axis (same as that of the exiting beam off the dish) and the line \overline{OF} . An analysis of this antenna type can be done quickly using the equivalent-parabola concept as recently reported by Rusch et al.⁷⁸ It provides a broader bandwidth for the "rabbit-ear" cross-polar reductions than does the prime-fed offset with a "rabbit-ear" canceller.

Improved Conical Cornucopias

A significant improvement in the *E*-plane RPE of a CC antenna such that this RPE becomes virtually equal to the virtually unaltered, excellent *H*-plane RPE can be realized by lining its inner conical wall (starting at diameter of about 3λ up to the top diameter of this section) with a sufficiently thick layer of absorber. ⁷⁹⁻⁸¹ This layer converts the TE₁₁ type spherical wave propagating up the cone to an HE₁₁ type spherical wave with its highly tapered transverse field distribution, where, because of this taper, the insertion loss introduced is very small, typically less than 0.5 dB, and where this tapering is achieved over a very large, continuous bandwidth of over 3:1. This type of CC, then, greatly reduces EMI (by over 40 dB at wide angles relative to a standard unshielded dish of the same gain^{82,83}).

Improved Large-Gain Feed Horns

A recent improvement in large-gain (i.e., 20 dBi or more) feed horns typically employed in symmetrical dual reflectors providing excellent *E*- and *H*-plane equality with their attendant low cross-polar 45° lobes is the conical foam-loaded horn developed by Clarricoats et al., 84-86 which is gradually replacing multimode-conical or corrugated-conical feeds. 87

Angle Diversity

From Fig. 30-17c it is seen that negligible gain drop of the displaced beam occurs if the feed is slightly transversely displaced. Hence two feeds can be employed (typically one feed is

^{*}For three screws used adjacent to each other, the 120° spaced three-screw arrangement is good only for a single polarization at a time.^{76a}

displaced above the focal point, producing a beam pointing below the axis, and one feed is displaced below the focal point, producing a beam pointing above the axis) to ensure reception of multipath digital signals (one direct, one due to refraction off the atmosphere) by either receiving each signal separately using two receivers or by combining them and using a single receiver to ensure that an acceptable bit-error rate will exist "all" the time. This angle-diversity scheme is presently being evaluated for extensive microwave radiorelay use in place of the more expensive space-diversity schemes, with initial testings showing promise. 88-91

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Radiometer Antennas

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31-1 Introduction 31-2

31-2 Basic Principles 31-2

Antenna Temperature 31-2

Polarization 31-3

Beam Efficiency 31-6

Stray Radiation 31-8

Ohmic and Reflection Losses 31-9

Calibration 31-10

31-3 System Principles 31-11

Radiometer Types 31-11

Radiometer-System Types 31-12

31-4 Antenna Types 31-13

Horns 31-13

Horn-Reflector Systems 31-14

Phased Arrays 31-16

31-5 Recent Developments 31-17

Overview 31-17

Special Sensor Microwave/

Imager (SSM/I) Radiometer

System 31-17

Autocorrelation Radiometer 31-18

High-Resolution

Radiometry 31-21

Radiometer antennas are widely used as part of remote-sensing systems to infer physical properties of planetary atmospheres and the surface. Such antennas are similar in type to those used in radio astronomy except for several important differences. In the case of radio astronomy, many of the sources to be measured are stable in time for minutes or longer. In addition, the so-called radio stars or other natural sources are point sources or are of limited angular extent and immersed in a cold sky of several degrees kelvin. So For most remote-sensing applications, the radiometric system observes a distributed target of large angular extent and warm in temperature. For example, the ocean brightness temperatures in the microwave bands are in the order of 120 K, while land surfaces can be 200 K or more. Hence, antenna systems for downward-looking radiometric systems must have small, close-in sidelobes out to the angles where the surface brightness diminishes. Such techniques as interferometry used in radio astronomy to improve resolution at the expense of high sidelobes are of little value in the remote sensing of atmospheres and surfaces in a downward-looking observation.

Radiometer-antenna design requires much more precise consideration of different parameters than most antenna engineers are accustomed to. For example, beam efficiency, antenna losses, and antenna physical temperature are extremely important as well as directional gain, low sidelobes, mismatch, and polarization. Therefore, this chapter will include an extended section on basic principles and a description of basic system types in present or proposed use on spacecraft or aircraft, along with basic radiometer-antenna types commonly in use.

31-2 BASIC PRINCIPLES

For microwave remote-sensing applications, the radiometer antenna is used with a very sensitive receiver to detect and provide a measurement of the electromagnetic radiation emitted by downwelling radiation and the earth's surface. The downwelling radiation is from the cosmic-background and the sky-background radiation due to atmospheric properties including moisture. ^{4,5,6} Depending upon knowledge of the roughness and dielectric properties of the surface and the relationship of the dielectric properties to the physical properties of the surface, an indirect or remote measurement of the physical property is feasible.

The received power detected by the radiometric system is by Swift:6

$$P = KT_{\mathcal{A}}f \tag{31-1}$$

where K is Boltzmann's constant, f is the radio-frequency bandwidth of the radio-metric receiver, and T_A is the antenna temperature.

Antenna Temperature

The antenna temperature, stated in a manner suppressing polarization, is given by an expression of the form

$$T_{A} = \frac{\int_{0}^{2\pi} \int_{0}^{\pi} f(\theta, \phi) T_{B}(\theta, \phi) \sin \theta d\theta d\phi}{\int_{0}^{2\pi} \int_{0}^{\pi} f(\theta, \phi) \sin \theta d\theta d\phi}$$
(31-2)

where $f(\theta, \phi)$ is the normalized radiation pattern of a perfect plane-polarized antenna and $T_B(\theta, \phi)$ is the brightness temperature of the scene observed by the radiometer

antenna with the same polarization. A typical scene in microwave remote sensing in which the antenna is pointed toward the surface is given in Fig. 31-1. $T_{\rm sky}$ is the downwelling sky radiation in the specular direction and includes thermal radiation from the atmosphere and the cosmic background. The brightness temperature observed by the radiometer antenna, therefore, is the sum of the brightness temperature T_{Br} emitted by the surface and the amount of energy from the sky radiation scattered by the surface in the specular direction. This brightness temperature T_B (θ , ϕ) is given by

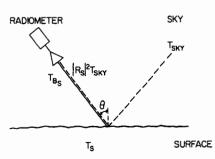


FIG. 31-1 Typical radiometer scene in microwave remote sensing.

$$T_B(\theta, \phi) = T_{Bs} + /R_s/^2 T_{\text{sky}}$$
 (31-3)

where $/R_s/^2$ is the plane-wave reflection coefficient for the air-surface interface. The emissivity of the surface is given by

$$\varepsilon_s = 1 - /R_s/^2 \tag{31-4}$$

and the brightness temperature T_{Br} is related to the physical temperature T_r by the relation

$$T_{Bs} = \varepsilon_s T_s \tag{31-5}$$

From Eqs. (31-3), (31-4), and (31-5),

$$T_B(\theta, \phi) = (1 - /R_s/^2)T_s + /R_s/^2T_{\text{sky}}$$
 (31-6)

It is emphasized that these equations were written in a conceptual form and do not include the entire vector phasor property of the antenna and the observed surface. The polarization property of the antenna and its relationship to the surface-polarization property are discussed in the next subsection.

Polarization

To include polarization properly in the antenna temperature expressions the polarization properties of both the antenna and the surface must be included. The polarization is defined relative to the plane of the aperture in the case of the antenna and to the incident plane in the case of the surface. Consider the following coordinate

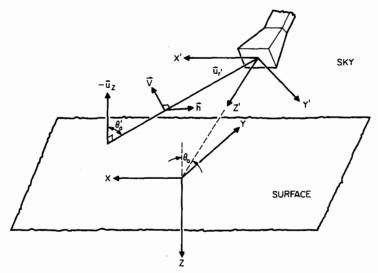


FIG. 31-2 Definition of polarization of a radiometer antenna with the surface and sky scene.

system given in Fig. 31-2, where the observed surface is in the xy plane and the antenna aperture is in the x'y' plane. In this instance,

$$h = \frac{u_z \times u_r'}{\sin \theta'} \quad v = h \times u_r$$

and ψ = the angle between **h** and \mathbf{u}_{\bullet} . Also note that

$$\mathbf{h} \cdot \mathbf{u'}_{\phi} = \cos \psi = \frac{\sin \theta' \cos \theta_0 - \cos \theta' \sin \theta' \sin \theta_0}{\sin \theta'_0}$$

and

$$\mathbf{v} \cdot \mathbf{u}_{\psi} = \sin \psi = -\frac{\sin \theta_0 \cos \phi}{\sin \theta_0'}$$

so that

$$h = \cos \psi \, \mathbf{u'_{+}} - \sin \psi \, \mathbf{u'_{+}}$$

$$\mathbf{v} = \sin \psi \, \mathbf{u'_{+}} - \cos \psi \, \mathbf{u'_{+}}$$
(31-7)

It should also be noted that h and v are the vector directions commonly referred to as horizontal and vertical polarization. This should allow the conversion of available reflection-coefficient data on natural surfaces to emissivity and produce brightness temperatures through the use of Eq. (31-6). If we assume that the far field from an aperture in the x'y' plane can be broken into vertical and horizontal components, then

$$\mathbf{E} = \mathbf{h}[-\sin\psi E_{\theta} + \cos\psi E_{\phi}] + \mathbf{v}[\cos\psi E_{\theta} + \sin\psi E_{\phi}]$$

Using these results, the antenna temperature is defined as

$$T_A$$

$$= \frac{\int_{0}^{2\pi} \int_{0}^{\pi} \left\{ \left[-\sin \psi \, E_{\theta} + \cos \psi \, E_{\phi} \right]^{2} T_{BH} + \left[\cos \psi \, E_{\theta} + \sin \psi \, E_{\phi} \right]^{2} T_{BV} \right\} \sin \theta d\theta d\phi}{\int_{0}^{2\pi} \int_{0}^{\pi} \left\{ \left[-\sin \psi \, E_{\theta} + \cos \psi \, E_{\phi} \right]^{2} + \left[\cos \psi \, E_{\theta} + \sin \psi \, E_{\phi} \right]^{2} \right\} \sin \theta d\theta d\phi}$$
(31-8)

If we assume, as given in Peake's derivation,⁷ that $E_{\theta} = C\sqrt{f_{\theta}} e^{j\alpha}$ and that $E_{\theta} = C\sqrt{f_{\theta}} e^{j(\alpha+\theta)}$, where f_{θ} and f_{θ} are the normalized radiation patterns as a function of θ and ϕ and polarized in the θ and ϕ directions respectively, the **h** and **v** terms in Eq. (31-6) are given by

$$E_h = Ce^{i\alpha}[-\sin\psi\sqrt{f_\theta} + \cos\psi\sqrt{f_\phi}e^{i\gamma}]$$

$$E_v = Ce^{i\alpha}[\cos\psi\sqrt{f_\theta} + \sin\psi\sqrt{f_\phi}e^{i\gamma}]$$
(31-9)

Using these expressions, the antenna temperature is given by⁸

$$T_{A} = \frac{\int_{0}^{2\pi} \int_{0}^{\pi} \left\{ [f_{\theta} \sin^{2} \psi + f_{\phi} \cos^{2} \psi] T_{BH} + [f_{\theta} \cos^{2} \psi + f_{\phi} \sin^{2} \psi] T_{BV} + (T_{BV} - T_{BH}) f_{\theta} f_{\phi} \sin 2\psi \cos \gamma \right\} \sin \theta d\theta d\phi}{\int_{0}^{2\pi} \int_{0}^{\pi} (f_{\theta} + f_{\phi}) \sin \theta d\theta d\phi}$$
(31-10)

The form of Eq. (31-10) is a little different for other choices of coordinate systems, but the basic properties are the same. Notice in Eq. (31-10) that, in addition to the contributions from the clearly horizontal and vertical surface-polarization terms. there is a third term which contributes to antenna temperature that is related to the difference in horizontal and vertical brightness temperatures at given angles, the relative amplitudes of the radiation pattern, and the phase difference between the polarization terms in the antenna pattern. If the cross-polarization level is small, this term can be neglected. Depending upon the application, cross-polarization levels of -30 dBor more are usually satisfactory. Further discussion of this subject is given in Refs. 9 and 10 and in later sections of this chapter. It is interesting to note that for some surfaces^{4,5,9} T_{BH} and T_{BV} have properties such that $T_{BH} - T_{BV} \approx 0$ out to 20 or 30°. Hence, if a narrow-beam low-sidelobe antenna is used for near-nadir observations, the antenna temperature as given in Eq. (31-10) will be independent of the polarization of the radiometer antenna. An additional reference useful in interpreting the importance of polarization is Classen and Fung. 11 For the antenna designer, the message at this point is rather clear. A radiometer antenna must be designed so that sidelobes, cross-polarization lobes, and backlobes do not pick up unwanted contributions. Common design parameters for comparing radiometer antennas are the beam efficiency and the cross-polarization index.

Beam Efficiency

The beam efficiency of an antenna is defined as

$$BE = \frac{\text{power radiated in cone angle } \theta_1}{\text{power radiated in } 4\pi \text{ sr}}$$
(31-11)

or

$$BE = \frac{\int_0^{2\pi} \int_0^{\theta_1} f(\theta, \phi) \sin \theta d\theta d\phi}{\int_0^{2\pi} \int_0^{\pi} f(\theta, \phi) \sin \theta d\theta d\phi}$$
 (31-12)

It should be noted that polarization is not included in Eq. (31-12) for simplicity, but it will be included later. One can observe from Eqs. (31-11) and (31-12) that to relate one antenna to another in terms of beam efficiency a choice of the angle θ_1 must be made in a standard manner. A common choice for θ_1 is the angle between the beam axis and the first null. Another choice for comparing antennas, such as the wide-angle corrugated horn or the multimode horn in which the first null is poorly defined, is to use the criterion for θ_1 as $2\frac{1}{2}$ times the half angle of the 3-dB beamwidth.

The beam efficiency of aperture antennas with variable amplitude distributions has received much attention in the past, curves to compare one aperture distribution to another being readily available. 12,13,14

Examples of the effects that the shape of the amplitude distribution has upon beam efficiency are given in Fig. 31-3 for rectangular and circular apertures as a function of $U(U = Ka \sin \theta)$. For uniform circular and rectangular amplitude distributions, the first several sidelobes cause pronounced ripples in the beam-efficiency curves, and values of BE = 95 percent are not achieved for large values of U. As more tapered distributions are assumed, the beam efficiency rises to large values rapidly and independently of the aperture shape.

This characteristic of ideal aperture distributions to approach large beam-efficiency values can be misleading in practical applications since the wide-angle sidelobes for many tapered aperture distributions are very small.^{12,14} Indeed, some antennas such as the multimode, exponential, and corrugated horns have very low sidelobes and backlobes and hence excellent beam efficiencies. On the other hand, reflector antennas are sometimes used as radiometer antennas, and in this case the overall beam efficiency is influenced by spillover, cross-polarization, and blockage in addition to aperture illumination and reflector-surface roughness. These properties will be discussed later on.

The effects of polarization on beam efficiency can be stated as BE_{dp} (direct polarization):

$$BE_{dp} = \frac{\text{power at angle } \theta_1, \text{ direct polarization}}{\text{total received power, both polarizations}}$$
 (31-13)

Stated in equation form,

$$BE_{dp} = \frac{P_{\theta_1}, dp}{P_{dp} + P_{op}}$$
 (31-14)

where P_{dp} is the total power received in the direct polarization and P_{op} is the total power received in the orthogonal polarization. The effect of the orthogonal-polariza-

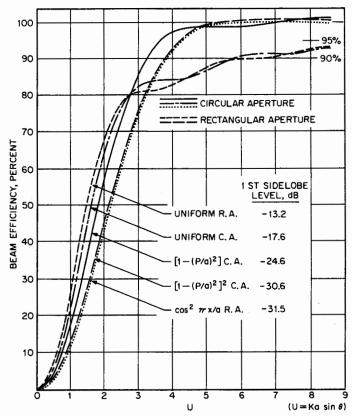


FIG. 31-3 Comparison of beam efficiencies of rectangular and circular apertures with various aperture distributions.

tion energy therefore is to decrease the direct-polarization beam efficiency of the antenna. A cross-polarization index (CPI) can be defined as¹⁰

$$CPI = BE_{dp} \frac{P_t}{P_{op}}$$
 (31-15)

For example, for $BE_{dp} = 85$ percent and on the assumption that the antenna has the property $P_{op}/P_t = 26$ dB, the cross-polarization isolation index is 25 dB.

The significance of cross-polarization levels in a radiometer antenna can be vividly demonstrated by reviewing the earlier discussion on polarization resulting in Eq. (31-10). The brightness temperature of a particular scene is polarization- and angle-dependent. In general, except at near-nadir angles the brightness temperature of a given surface will be different for, say, vertical and horizontal polarization at the same observation angle. To demonstrate the effect of cross-polarization properties of an antenna upon the radiometric measurement of a scene the curves in Fig. 31-4 are presented. The bias error ΔT_A in this figure is the error in brightness temperature produced by the integrated cross-polarization lobes observing the scene. This approx-

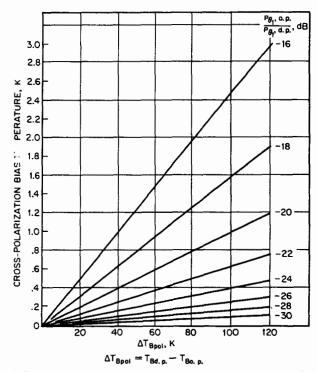


FIG. 31-4 Effect of antenna cross-polarization power on radiometer bias as a function of scene polarization difference temperature.

imation is valid for only narrow-beam antennas in which emission from the surface at a given polarization is constant over 2½ times the 3-dB beamwidths of the antenna. For precision measurements of ocean temperature in which accuracies of 0.3 K are desired, values of cross-polarization energy less than 28 dB are required.

Stray Radiation

For narrow-beam antennas, $T_B(\theta, \phi)$ is relatively constant over the main beam, and Eq. (31-2) can be written as

$$T_{\mathcal{A}} = T_{\mathcal{B}}(\theta, \phi)BE_{\theta_1} + \frac{\int_0^{2\pi} \int_{\theta_1}^{\pi} f(\theta, \phi) T_{\mathcal{B}}(\theta, \phi) \sin \theta d\theta d\phi}{\int_0^{2\pi} \int_0^{\pi} f(\theta, \phi) \sin \theta d\theta d\phi}$$
(31-16)

If the nonphysical assumption that $T_B(\theta, \phi)$ is constant in the second term of Eq. (31-16) is made, this equation may be written as

$$T_A = T_B(\theta, \phi)BE_{\theta_1} + T_B(\theta, \phi)[1 - BE_{\theta_1}]$$
 (31-17)

The second term in Eq. (31-17) is the so-called stray-radiation contribution sometimes used in radio-astronomy applications. For such applications, the near-in and relatively far-out sidelobes observe cold sky surrounding the radio source, thus justifying the assumptions made in Eq. (31-17). For radio-astronomy applications, therefore, much design emphasis must be placed upon backlobes which point toward the hot earth. For remote-sensing applications, the close-in and wide-angle sidelobes observe brightness temperatures in the same range as the main beam (100-270 K), while in many configurations the backlobes point to the cold sky. Hence, for remote-sensing applications the stray-radiation term has added significance. In general, such concepts as stray radiation are useful in that they give some indication of the ultimate accuracy of the T_A measurement. Simplistic forms to compute stray radiation such as Eq. (31-17) should be avoided unless great care has been exercised to understand the amplitude and angular distribution of brightness temperatures in the scene.

Ohmic and Reflection Losses

The ohmic losses in the antenna will modify the apparent temperature observed by the radiometric system. These ohmic losses will modify the observed temperature by the relation⁵

$$T_a = (1 - \ell)T_A + \ell T_0$$
 (31-18)

where T_a is the apparent antenna temperature of a source whose lossless observed antenna temperature of the scene is T_A , T_0 is the physical temperature of the antenna, and ℓ represents the fractional power loss in the antenna.

The significance of physical losses in the antenna upon the absolute accuracy of remotely sensed surface properties may be obtained from the following example. Assume that antenna physical temperature is that of room temperature, i.e., $T_0 \approx 300$ K. Typical ocean and land scenes exhibit lossless antenna temperatures between 100 and 300 K. Using this information, the effect of antenna losses upon measurement accuracy is given in Fig. 31-5. For some ocean-temperature applications ($T_A \approx 120$ K) absolute accuracies of 0.3 K are of importance. Hence, very small losses (≤ 0.005 dB) are of interest. For antennas in which losses are significant, antenna loss is generally treated as a fixed bias. This method is acceptable, but in such cases the physical temperature must be known and maintained to great precision. The Potter horn built for a precision S-band radiometer⁵ exhibits a loss of ≤ 0.1 dB. Studies of corrugated and multimode horns¹⁵ indicate small but significant losses when these are used as radiometric antennas. Hence, for calibration purposes both the loss and the antenna physical temperature must be known. To ensure stability in calibration, antennas may be enclosed in a thermally stable box with a very-low-loss radome.

The effect of mismatch in the input to the radiometer upon the observed antenna temperature can be expressed as⁵

$$T_a = (1 - \ell - \rho)T_A + \ell T_0 + \rho T_R$$
 (31-19)

where ρ is the reflection coefficient of the antenna and T_R is the microwave temperature seen looking into the receiver. The effects of small mismatches are very important for precision measurements. Stability of this mismatch will allow one to treat this error as a bias. Again, as in the case of physical loss, the thermal stability of the antenna impedance is important.

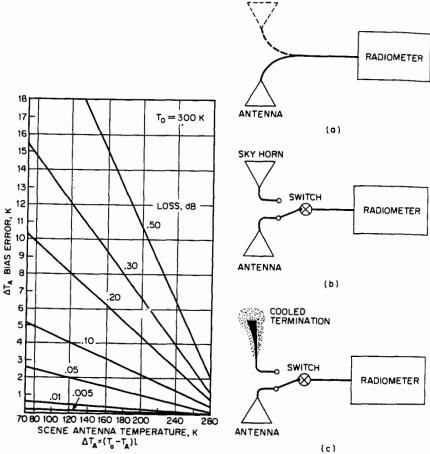


FIG. 31-5 Effects of losses upon scene antenna temperature.

Fig. 31-8 Radiometer calibration methods. (a) Steerable antenna. (b) Reference antenna and switch. (c) Cooled termination and switch.

Calibration

To provide a precision method of calibration, the normal procedure is to calibrate the radiometer antenna and radiometer as a single unit. This allows the user to obtain a relatively simple calibration factor for the entire system. Three simple methods of calibration, all of which have certain advantages and disadvantages, are given in Fig. 31-6. The steerable-antenna method (see Fig. 31-6a) requires that the radiometer antenna be pointed at the galactic pole periodically for a stable, cold reference temperature. This method has the additional advantage that the antenna can be pointed at a warm, stable surface feature such as a deep, thermally stable lake for an additional calibration point. The disadvantage of this method for spacecraft applications is that the spacecraft must be rotated. For ground applications the atmospheric atten-

uation is too large to use this method for upper-microwave or millimeter-wave frequencies. The switchable two-antenna method (see Fig. 31-6b) normally uses a so-called sky horn pointing to the galactic center and therefore eliminates the space-craft-control problem. The primary disadvantage of this method is that the extra switch has losses that may change as a function of time, depending upon the switch technology and thermal control. A secondary disadvantage is that the two antennas are usually dissimilar with different losses. The third method (see Fig. 31-6c), the so-called cooled-termination method, has the advantage of not requiring a sky horn and may be very useful for millimeter- and higher-frequency ground or airborne systems in which atmospheric effects are very significant. Of course, the switch losses are common to the methods in Fig. 31-6b and c. A disadvantage of the system is the required provisions for a cooled transmission-line load.

A fourth calibration method, which is a modification of the first method, is to point the radiometer antenna toward a special free-space load⁵ constructed from a porous microwave absorber located in a container filled with liquid nitrogen. This type of load has been successfully used in airborne radiometers when the radiometers have been designed to be very stable over long periods of time. Such a method also has advantages for millimeter and submillimeter applications.

31-3 SYSTEM PRINCIPLES

Radiometer Types

A variety of radiometer types have been used for radio astronomy and remote sensing. A very thorough tutorial discussion of radiometer designs is given by Hidy et al.⁵ The three basic types commonly in use for remote sensing are described in simplistic block-diagram form in Fig. 31-7, which is adapted from Fig. 9.1 of Ref. 5.

The simplest radiometer, the absolute-power type, is shown in Fig. 31-7a. The output voltage of this radiometer, which is not electronically modulated, can be expressed as

$$V = G(T_A + T_N)$$
 (31-20)

where T_A is the antenna temperature, T_N is the system noise temperature referred to the antenna input terminals, and G is the gain of the receiver system. The field calibration of this system is dependent upon maintaining stability after the calibration procedure by using such sources as a hot and cold load. If the latest technology in radio-frequency components is employed, this system is good but usually is not adequate to achieve accuracies of 1 K over a period of time. For some spacecraft systems the calibration of this system is improved by spinning the spacecraft antenna so that the cold sky is observed during each revolution as in the calibration method indicated in Fig. 31-6a. This spinning-spacecraft-antenna system is equivalent to the signal-modulated Dicke radiometer discussed next, except that the switching circulator is eliminated and the modulation frequency is reduced to much lower frequencies. 16,17

The next radiometer type commonly used is the Dicke radiometer, 18 as shown simplified in Fig. 31-7b. The basic improvement of the signal-modulated Dicke radiometer is that the stability of the noise from the receiver T_N is eliminated so that the output voltage is given by

$$V = G[T_A(1 - \ell_s) - T_{ref}(1 - \ell_R) + (\ell_s - \ell_R)T_0]$$
 (31-21)

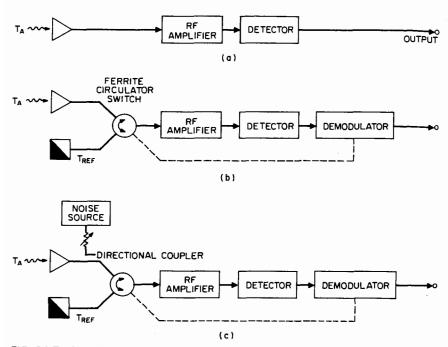


FIG. 31-7 Simplified diagram of basic radiometer types. (a) Absolute-power radiometer. (b) Dicke signal-modulated radiometer. (c) Noise-injection signal-modulated radiometer.

where ℓ_s and ℓ_r are the ohmic losses in the signal and reference arms and T_0 is the physical temperature of the radiometer components.

The next and latest improvement in radiometers is the noise-injection signal-modulated type shown in simplified form in Fig. 31-7c. The noise-injection method eliminates gain instability by allowing known amounts of noise to be put into the input of the radiometer. Various methods of performing this variable noise injection, including variable calibrated attenuators as shown in Fig. 31-7c, can be used. Variable-height pulse modulation of a noise diode feedback circuit can also be employed, as discussed in Ref. 5. A digital version of the noise-injection modulated radiometer has been devised and analyzed 19 and implemented. 20

Radiometer-System Types

The most common radiometer system used in remote sensing is the scanning-beamantenna type depicted in Fig. 31-8. This method of scanning on a spacecraft or an aircraft is usually achieved by bidirectional scanning of a reflector-antenna-feed-radiometer system relative to a stable platform. The advantage of this system is that wideswath coverage of the surface scene can be obtained. The spatial resolution of this bidirectional scanning system is limited by an antenna size that can fit within an aircraft or launch-vehicle fairings. When finer spatial resolutions are required, deployable antennas which are limited in scan rate and can require the spacecraft to spin with the radiometer antenna as a single unit may be employed. Owing to the combination

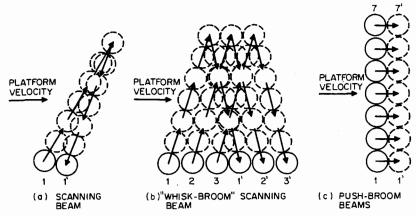


FIG. 31-8 Ground spot patterns of radiometer-antenna systems.

of scan rate and spacecraft velocity, a single-beam radiometer antenna of the scanning type may not produce contiguous resolution cells on the surface at the beginning and end of each rotation. To produce this contiguous coverage, the so-called whisk-broom radiometer-antenna system can be employed, as shown in Fig. 31-8 b. Here each beam in the whisk broom requires an independent antenna port and radiometer. ²¹ The beam patterns can be produced by multiple feeds in a reflector system.

As even larger radiometer antennas are required to obtain better surface resolution, physical movement to obtain swath coverage may not be possible. To provide swath-width coverage for nonscanning systems, the so-called push-broom radiometer system may be used, as depicted in Fig. 31-8c. In this design, an independent radiometer is connected to each antenna port. Movement of this push-broom beam along the surface can be time-gated to produce a surface-radiometric-brightness-temperature map.

Because of requirements to separate surface parameters such as salinity and temperature for the ocean, multiple frequencies are commonly required in radiometric systems that must be integrated into the scanning, ¹⁶ whisk-broom, or push-broom radiometric systems. Such multifrequency systems are usually designed as multiple feeds in a main reflector. Combining frequencies in a single broadband corrugated horn is feasible over nearly 2:1 bands with low-loss properties. A very broadband horn with over 5:1 bandwidth has been designed and used in space with a scanning system. ¹⁷ This antenna exhibits large losses, which must be compensated for as very large bias errors.

31-4 ANTENNA TYPES

Horns

A straightforward design for a moderate-beamwidth (10 to 30°) radiometer antenna—is the electromagnetic horn; however, because of the requirement for high beam efficiency (and, therefore, for low sidelobes) specialized horn designs are necessary for

radiometer applications. Radiometer horn antennas are designed so that the normally high E-plane sidelobes are reduced to an acceptable level. The H-plane sidelobes (typically -23 dB) are already low enough to achieve a sufficiently high beam efficiency for moderate beamwidths. The E-plane-sidelobe reduction can be accomplished by several techniques. The simplest technique is to utilize multimodes in the radiating-horn aperture to provide sidelobe cancellation in the far-field pattern. The higher-order modes are excited by a step or sudden change in the cross section of the wave-guide or horn taper. The bandwidth of a multimode or dual-mode horn is limited to a few percent because of the difference between the modal phase velocities in the tapered waveguide horn section. However, a shortened version of the Potter horn can exhibit good pattern characteristics over a bandwidth approaching 10 percent. The performances of the square multimode horn and the conical dual-mode horn are quite similar.

For radiometer applications requiring a larger bandwidth, the class of corrugated horns²⁴ is attractive. As with the multimode-type horn, the purpose of the corrugated-horn design is to reduce the normally high *E*-plane sidelobes. This is accomplished in the corrugated horn by designing the corrugations so as to decrease the current along the corrugated wall, thus producing a tapered (approximately cosine) *E*-plane aperture field distribution. This tapered distribution can be maintained over a bandwidth approaching 2:1 but is usually limited to the operating bandwidth of the feed waveguide.

Another type of horn which shows promise as a wideband radiometer antenna is the exponential horn with a specially flared aperture.²⁵ A similar wideband horn is one

which is flared like a trumpet.²⁶ The design approach of these wideband horns is to eliminate sharp discontinuities and provide a smooth transition between the horn modes and free space.

Beam-efficiency calculations are given in Fig. 31-9 for a circular aperture with a radial aperture distribution equivalent to that of the TE_{11} -mode H-plane distribution and with a quadratic phase taper, as being representative of the beam efficiencies obtained from radiometer horns. The figure also illustrates that, in order to achieve high beam efficiencies, the horn must be designed for small phase taper, either by decreasing the horn flare angle or by using a phase-correcting aperture lens.

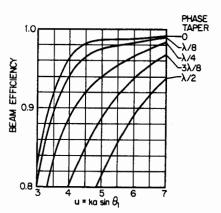


FIG. 31-9 Effect of aperture phase taper on beam efficiency for a conical corrugated or dual-mode horn.

Horn-Reflector Systems

For radiometer applications requiring narrow beamwidths, reflector antennas are more appropriate since highly tapered reflector illuminations can yield the much lower sidelobes necessary for high beam efficiency. The feed elements should be designed for spillover minimization, which represents additional beam-efficiency degradation.

The reflector surface must be constructed very accurately (usually a machined and possibly polished surface is required) to minimize loss in beam efficiency due to statistical roughness.

The beam efficiency for a reflector antenna can be expressed as

$$BE = BE_{\iota}BE_{f}BE_{\iota} \tag{31-22}$$

where BE_s is the beam efficiency obtained by integration of the reflector secondary pattern, neglecting the back radiation, BE_f is the beam efficiency of the feed evaluated at the angle of the edge illumination, and BE_s is the reduction factor due to reflector-surface roughness. Calculations of beam efficiencies BE_s for a circular aperture with a parabola-on-a-pedestal and with a parabola-on-a-pedestal-squared distribution are presented in Figs. 31-10 and 31-11 as representative of reflector illumination with an edge taper of -20, -10.5, -8, and -6 dB. The dashed curve for uniform illumination is included for reference. Figure 31-12 shows the effect of edge taper on the feed or spillover efficiency BE_f . The calculations in the figure are for a conical dual-mode horn with no phase error as being typical of feed patterns used in horn-reflector radiometer antennas. The reduction in beam efficiency BE_s due to reflector-surface roughness can be obtained from the analysis of Ruze²⁷ as

$$BE_{\delta} = BE_{\delta} \exp(-\delta^2) + \Delta BE \qquad (31-23)$$

where $\delta = 4\pi\epsilon/\lambda$, ϵ is the rms surface roughness, and ΔBE is a correction term which accounts for the nonzero correlation length c of the surface error; i.e.,

$$\Delta BE = \exp(-\delta^2) \sum_{n=1}^{\infty} (\delta^{2n}/n!) [1 - \exp(-(uc/D)^2/n)]$$
 (31-24)

where D is the reflector diameter. Figure 31-13 shows a plot of the reduction factor versus rms surface roughness and correlation length. It should be noted from Eq. (31-

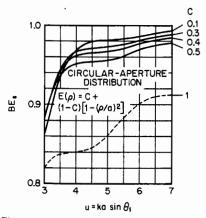


FIG. 31-10 Beam efficiency for circular aperture with parabola-on-a-pedestal distribution.

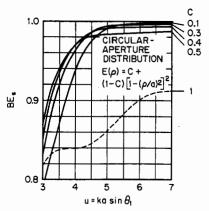
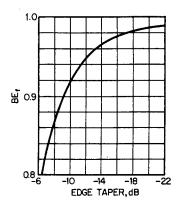


FIG. 31-11 Beam efficiency for circular aperture with a parabola-on-a-pedestal-squared distribution.



1.0 ΒĖ, 1.0 0.9 0.9 8.0 8.0 0.7 0.7 EFFICIENCY 0.6 0.5 BEAM BE $s = BE_s \exp(-\delta^2) + \Delta BE$ 0.4 0.3 0.5 0.4 0.2 0.3 *l*0.2 0.1 0 0.02 0.06 RMS SURFACE ROUGHNESS, \(\frac{1}{2}\)

FIG. 31-12 Feed-beam-efficiency factor for a reflector antenna.

FIG. 31-13 Beam-efficiency factor of a random rough-surface reflector.

23) that for a beam efficiency greater than 90 percent the reflector surface should be $\lambda/50$ or smoother.

An additional concern for offset reflectors is the cross-polarization level, which could complicate the interpretation of antenna temperature data, as discussed earlier. The cross-polarization for reflectors decreases for larger focal-length-to-diameter ratios and smaller offset;²⁸ however, these parameters must be optimized to minimize feed- and spar-blockage effects. The BE_s curves in Figs. 31-10 and 31-11 neglect the effects of feed and spar blockage. Indeed, these effects cannot be treated simply as an aperture blockage as in gain calculations, and the secondary-pattern beam efficiency BE_s therefore should be recomputed with the wide-angle scattering from feed and spars included.

Phased Arrays

Phased arrays have been successfully employed as radiometer antennas^{29,30} when beam scanning is required or volume constraints indicate that an array is the appropriate antenna type. High beam efficiency is obtained through amplitude tapering within the feed-distribution network. In the design of feed networks for radiometer array antennas, internal line losses should be minimized. If line losses are not excessive, stabilization of the losses through temperature control may be used in combination with calibration techniques to correct the radiometric temperature data. Resistors and terminations within the feed network should be avoided or used with discretion, since noise emitted by such components into the receiver could negate the radiometric measurement.

Overview

There have been several developments in recent years that are noteworthy relative to radiometer systems and radiometer antennas. These can be summarized in general terms as precision satellite meteorologic radiometers and applications and the autocorrelation radiometer. These radiometer systems will represent the basis for radiometer systems in space for a considerable period in the future.

Special Sensor Microwave/Imager (SSM/I) Radiometer System

This system was launched on June 19, 1987 and consists of a seven-channel, four-frequency, linearly polarized microwave radiometer system operating at 19.3, 22.2, 37.0, and 85.5 GHz. This system is aboard the Defense Meteorological Satellite Program (DMSP) Block 5D-Z spacecraft F8, as depicted in Fig. 31-14, which travels at a velocity of 6.58 km/s at an altitude of 833 km. The SSM/I coverage of the earth in a single day is shown in Fig. 31-15. A complete description of the SSM/I instrument along with the instrument evaluation and typical inferred remote sensed parameters is given in a special issue of the *IEEE Transactions on Geoscience and Remote Sensing*. The scanning

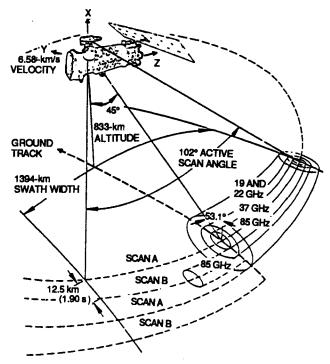


FIG. 31-14 SSM/I scan geometry. (From IEEE Transactions on Geoscience and Remote Sensing, vol. 28, no. 5, September 1990, p. 783.)

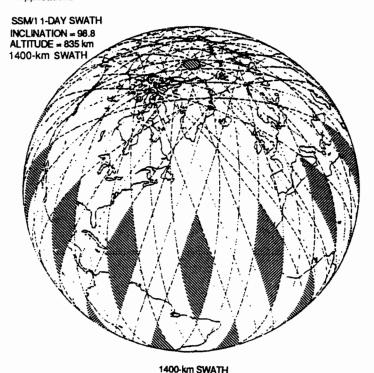


FIG. 31-15 Earth coverage of SSM/I in a 24-hour period. Shaded areas are not observed in this time period. (From IEEE Transactions on Geoscience and Remote Sensing, vol. 28, no. 5, September 1990, p. 783.)

antenna system depicted in Fig. 31-14 is an offset reflector fed by a multifrequency corrugated horn. A similar corrugated horn at low-frequency bands was used on the Scanning Multichannel Microwave Radiometer (SMMR)¹⁷ system. The SSM/I feed horn has a flare angle of 58°, giving an equivalent edge taper of about 17 dB for all frequencies. The SMMR horn used a set of ring-loaded corrugations. This horn design has been modified to include straight-sided grooves of alternating depth. The SMMR horn is depicted in Fig. 31-16, where the multifrequency performance is achieved by coupling waveguides at various points along the feed waveguide and/or horn. Special filters were placed in the various waveguide ports to minimize multiband coupling. It should be noted that both these horn feeds were designed by Dr. K. A. Green and are remarkable pieces of hardware. Both these antennas have significant losses of 0.5 to 0.7 dB, depending on operating band, which must be calibrated and removed from the antenna temperature as a bias as given in Fig. 31-5.

Autocorrelation Radiometer

The direct-imaging radiometer, such as SMMR and SSM/I, maps the brightness temperature by scanning the antenna mechanically across the field of view. The resolution of the scene is determined by the beamwidth of the antenna. Autocorrelation or interferometric

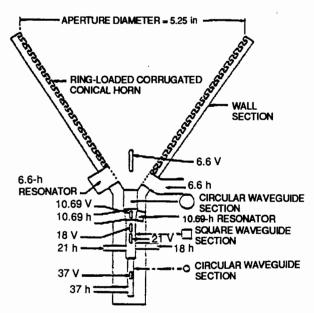


FIG. 31-16 SMMR feed hom. (From IEEE Journal on Oceanic Engineering, vol. OE-5, no. 2, April 1980, pp. 100-115.)

imaging radiometers generate the image directly by measuring the Fourier transform of the brightness-temperature distribution over the field of view. Interferometer measurements are made by cross-correlating the input signals received by spatially separated antennas that have an overlapping field of view. An example of a pair of elements is given in Fig. 31-17.³² The antenna correlator is depicted in Fig. 31-18. The absolute-power radiometer as given in Sec. 31-3 can resolve a change in scene temperature in a dynamic system as

$$\Delta T = \frac{T_B + T_R}{\sqrt{B\tau}} \tag{31-25}$$

where T_B = brightness temperature of the scene, K

 T_R = effective receiver noise temperature, K

B = predetection bandwidth, Hz

 τ = integration time, s

For the correlation radiometer, the temperature sensitivity is given by

$$\Delta T = \sqrt{\frac{(T_0 + T_{R1})(T_0 + T_{R2})}{B\tau} \frac{(2N_x + 1)(2N_y + 1)}{2}}$$
 (31-26)

where T_{R1} and T_{R2} are the receiver noises of the two receiver channels and N_X and N_Y are the numbers of antenna elements in the X and Y planes. The standard deviation in the noise floor of the image has been increased by the root sum square of the noise in individual measurements.

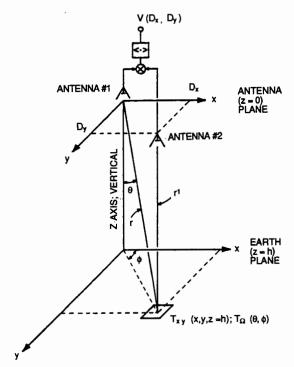


FIG. 31-17 A two-dimensional earth-viewing interferometer. The two antennas in the z=0 plane have antenna patterns directed toward the earth. (From IEEE Transactions on Geoscience and Remote Sensing, vol. 26, no. 5, September 1988, p. 598.)

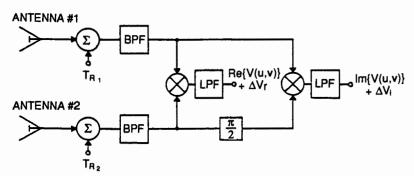


FIG. 31-18 Quadrature (complex) antenna correlator, where receiver noise is added at the antenna terminals. (From IEEE Transactions on Geoscience and Remote Sensing, vol. 18, no. 5, September 1990, p. 600.)

High-Resolution Radiometry

An extension of the correlation technique can be applied to a high-resolution thinned array as given in Fig. 31-19.³³ A conceptual schematic showing the processing required is given in Fig. 31-20. An airplane version of the high-resolution radiometer, ESTAR, has been flown and has been successful in obtaining imaging.³⁴ Other applications of the autocorrelation radiometer have been used in profiling of atmospheric water vapor.³⁵

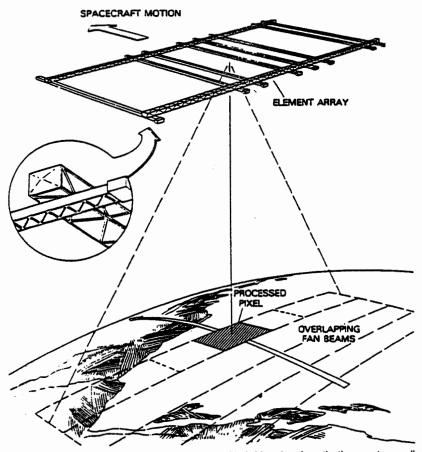


FIG. 31-19 Schematic illustrating the concept of hybrid real and synthetic aperature radiometer. (From IEEE Transactions on Geoscience and Remote Sensing, vol. 28, no. 4, July 1990, p. 615.)

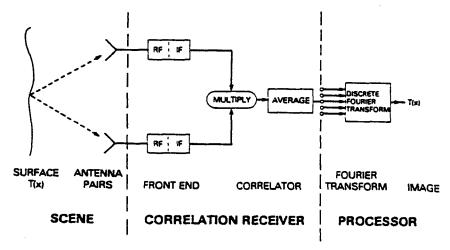


FIG. 31-20 Schematic indicating the signal processing that takes place in the ESTAR system. (From IEEE Transactions on Geoscience and Remote Sensing, vol. 28, no. 4, July 1990, p. 616.)

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Radar Antennas

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32-1 Introduction 32-2
32-2 Search-Radar Antennas 32-5
2D Systems 32-6
ARSR-3 32-7
AN/TPN-24 32-8
3D Systems 32-10
AWACS 32-11
AN/TPS-59 32-12
32-3 Tracking Radar 32-12
32-4 Multifunction Arrays 32-14
PAVE PAWS 32-15
Patriot 32-17
Limited-Scan Arrays 32-19
AN/GPN-22 32-19
AN/TPQ-37 32-20
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Radar (radio detection and ranging) is a technique for detecting and measuring the location of objects that reflect electromagnetic energy. This technique was first demonstrated in practice by Christian Hülsmeyer in 1903 by detecting radio reflections from ships. With the development of the magnetron by the British in 1940 and the incentives of World War II, the radar principle was used effectively in many applications. These early radars generally operated at microwave frequencies, using a pulsed transmitter and a single antenna that was shared for transmission and reception.

The radar antenna is an important element of every radar system and is intimately related to two fundamental parameters: coverage and resolution. A radar's volume of coverage, in particular its maximum range, is one of its most basic parameters. The radar-range equation shows that the product of transmitted power and antenna gain squared is proportional to the fourth power of range.² Because of this dependency, economic considerations in the design of a radar usually conclude that the most cost-effective system will have 20 to 40 percent of the system cost budgeted for the antenna.

Resolution, the ability to recognize closely spaced targets, is another important radar property. The better the radar's resolution, the better it is able to separate desired returns from the returns of other objects. The size of the radar antenna measured in wavelengths is inversely proportional to its beamwidth and hence determines the radar's angular resolution. While radar applications vary, antenna beamwidths typically fall between 1 and 10°.

The radars developed to date span a wide range of size and importance. Sizes range from proximity fuzes used in artillery shells to phased-array radars housed in multistory buildings for detecting and tracking objects in space. In any one application the size of the radar and also its cost may be limited either by the physical space available or by the importance of the radar information in relation to other competing techniques or operational alternatives.

The radar applications listed in Table 32-1 illustrate the wide variety of problems that radar has been called upon to solve. Few of these applications have required large production quantities, so the radar industry is characterized by a great diversity of models and small production quantities of each model. A result is an industry that is development-intensive and requires considerably more engineering personnel than most other electronic industries. The many applications combined with a large community of development engineers has resulted in many antenna developments originating for radar applications. The phased arrays developed for satellite surveillance, weapon control, and precision approach control for aircraft landing are but a few examples.

Most of the radars designed for the applications listed in Table 32-1 operate in the microwave-frequency band. While certain radars, such as long-wave over-the-horizon radar and millimeter-wave radar for short-range applications, operate outside this region, the majority of the systems operate between 1 and 10 GHz. The considerations that bound the frequency choice for a given radar application are antenna size and the angular resolution at the low end and atmospheric attenuation and the availability of radio-frequency (RF) power at the high end. The particular frequency bands allocated for radar use by international agreement are listed in Table 32-2. The letter designations, originating during World War II for security reasons, have been

TABLE 32-1 Radar Applications

Acquisition	Navigation
Air defense	Over-the-horizon applications
Air search	Personnel detection
Air traffic control	Precision approach
Airborne early warning	Remote sensing
Airborne intercept	Satellite surveillance
Altimeter	Sea-state measurement
Astronomy	Surface search
Ballistic-missile defense	Surveillance
Civil marine applications	Surveying
Doppler navigation	Terrain avoidance
Ground-controlled interception	Terrain following
Ground mapping	Weather avoidance
Height finding	Weather mapping
Hostile-weapon location	Weapon control
Instrumentation	

used in the years since then as familiar designators of the particular radar-band segments.

Because of the great variety of radar applications, radar antennas are required to operate in many different environments. Each of these environments, listed in Table 32-3, has a special impact on a radar's antenna design and the parameters listed in Table 32-4. Land-based systems are classed as fixed-site, transportable, or mobile. At

TABLE 32-2 Standard Radar-Frequency Letter-Band Nomenclature*

Band designation	Nominal frequency range	Specific radio-location (radar) bands based on international Telecommunications Union assignments for Region 2
HF	3-30 MHz	
VHF	30- 300 MHz	138-144 MHz
		216-225 MHz
UHF	300-1000 MHz	420-450 MHz
		890-942 MHz
L	1000-2000 MHz	1215-1400 MHz
S	2000-4000 MHz	2300-2500 MHz
		2700-3700 MHz
С	4000-8000 MHz	5250-5925 MHz
X	8000-12,000 MHz	8500-10,680 MHz
Ku	12-18 GHz	13.4-14.0 GHz
		15.7-17.7 GHz
K	18-27 GHz	24.05-24.25 GHz
Ka	27-40 GHz	33.4-36.0 GHz
mm	40-300 GHz	

^{*}From Ref. 1.

TABLE 32-3 Radar Environments

Location	Climate
Surface-based	Arctic
Airborne	Desert
Space-borne	Marine
Mobility	Electromagnetic environment
Fixed	Electromagnetic interference (EMI)
Transportable	Electromagnetic pulse (EMP)
Mobile	Electronic countermeasure (ECM)
Portable	(= (= (

TABLE 32-4 Radar-Antenna Parameters

Peak power	Cross-polarization rejection
Average power	Scan volume
Gain	Scan time
Beamwidths	Pointing accuracy
Sidelobe levels	Size
Bandwidth	Weight
Loss	Environment
Mismatch	Cost
Polarization	

fixed sites the larger radar antennas are often protected by a radome, especially in arctic regions that experience heavy winds, ice, and snow. Transportable systems generally require that the antenna be disassembled for transport. Mobile systems are required to move rapidly from place to place and usually do not allow time for antenna disassembly.

Marine radar systems carried by surface craft also have special requirements. The lack of space above deck often forces the radar to a smaller antenna and larger transmitter than would be used in a comparable land-based application. The rolling platform leads to requirements for broad elevation beams or stabilization in the elevation coordinate in addition to the demands of a salt and smoke environment. Airborne and space-borne radar antennas also have special requirements peculiar to their operating environments.

In addition to the physical and climatological requirements, the electromagnetic environment has an important impact on radar-antenna design. There is a distinct contrast between radar systems designed for civil applications and those designed for military applications. While the electronic environment for civil systems consists of unintentional interference with radars operating at assigned frequencies, in military applications the threat of electronic countermeasures increases the need for an antenna to have wide bandwidth and low sidelobes.

Antennas designed for radar applications have many special requirements, some of which are not encountered in other applications. Most radar applications employ pulsed transmitters that allow the radar to resolve distant targets from nearby clutter. Peak powers from a few tens of kilowatts to a few megawatts and operating at duty

ratios from 0.1 to 10 percent are typical. These high peak powers require special attention to the RF path through the antenna to the point at which power is distributed over the antenna aperture. Pressurized waveguide and feed horns are often used to prevent RF breakdown. In active array antennas the high peak power is not concentrated in a single microwave path, thus lessening the severity of this requirement.

Most radar applications require an antenna capable of scanning its beam, either mechanically or electronically or both, to search for targets in a volume of space. Scanning techniques for single or multiple beams may be classified as either mechanical or electronic. The early radar antennas developed during and after World War II relied primarily on mechanical scanning. More recently the development of highpower RF phase shifters and frequency-scanning techniques have allowed the beams to be scanned more rapidly by avoiding the inertia associated with moving mechanical components.

Accurate pointing is a requirement inherent in all radar applications that measure target location. Radar requirements are generally more demanding than those of communications antennas, especially when precision measurements of target positions are required.

Radar applications tend to be divided between two functions, search and track. The search function requires that the radar examine a volume of space at regular intervals to seek out targets of interest. In this case the volume must be probed at intervals ranging typically from 1 to 10 s and every possible target location examined.

The radar tracking function operates in a manner quite different from search. Here one or more targets are kept under continuous surveillance so that more accurate and higher-data-rate measurements may be made of the target's location. Often the interesting targets detected by a search radar will be assigned to and acquired by a tracking radar. Certain radar systems combine search and track functions by time-sharing the agile beam of a phased-array antenna.

The remainder of this chapter describes a few examples of the more common radar applications which are indicative of today's state of the art. Too few are included to give a proper perspective of the great variety of radar applications. However, those described do illustrate the differences between some of the basic types. For greater depth on the subject of radar antennas the reader is directed to Refs. 1 through 5.

32-2 SEARCH-RADAR ANTENNAS

Search radars scan one or more beams through a volume in space at regular intervals to locate targets of interest. The search function is sometimes referred to as acquisition, as in a missile-defense system in which detected targets are eventually tracked and intercepted. It is also called surveillance when targets are being monitored, as in the control of air traffic. But regardless of the term used to describe the search function, the common requirement is to scan a specified region of space at regular intervals.

The most important parameters determining the size and cost of the search radar are the coverage volume, scan time, and target size. For a given application with fixed target size and scan time, it has been shown that the requirement may be met by specifying the product of average transmitter power and antenna-aperture area. It is a fundamental property of search radars that their coverage capability is proportional

to their power-aperture product and does not depend on the radar's operating frequency. The benefits of operating at a lower frequency are that (1) higher-power RF transmitters are available, (2) antenna tolerances are less severe for a given antenna size, and (3) the peak power-handling capacity of waveguide and components in the high-power RF path is higher. Radars designed to perform only the search function therefore tend to operate at the lower microwave frequencies, and just how low is often determined by a trade-off between antenna size and desired angular resolution.

This section describes four examples of air search radars in operation today. These examples of current technology fall into two categories: two-dimensional (2D) and three-dimensional (3D) air search radars. The 2D systems use a fan beam that is broad in elevation and narrow in azimuth because only the target range and azimuth coordinates are required. In the 3D systems elevation is also measured to determine target altitude, and in this case the antenna's beams must be relatively narrow in both angular coordinates.

2D Systems

The two examples chosen to illustrate 2D search radars are both designed for air-traffic-control applications. In these applications, the radar must scan the air space every few seconds. Aircraft targets are detected and their range and azimuth measured. Modern systems use computers to track the aircraft from scan to scan to provide continuity in the radar data provided to the air traffic controllers.

Radar antennas used in air traffic control usually have an elevation beam with a pattern similar to that shown in Fig. 32-1. The particular pattern shape is matched to the desired radar coverage. Since aircraft have a maximum altitude, the pattern is shaped to provide a constant altitude cutoff; however, this is usually modified at shorter ranges to compensate for the use of sensitivity time control in the receiver.

The beamwidth in the azimuth coordinate is typically between 1 and 2° to provide sufficient resolution with today's air traffic densities. Since the beam has a much larger beamwidth in the elevation coordinate, it is clear that the width of the antenna aperture must be larger than its height.

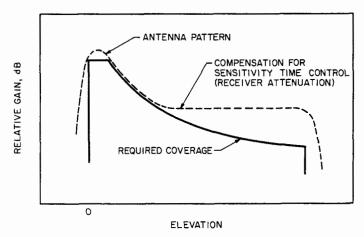


FIG. 32-1 Typical elevation pattern of a 2D surveillance radar antenna.



FIG. 32-2 ARSR-3 2D antenna. (Courtesy of Westinghouse Electric Corp.)

Other antenna requirements in air traffic control usually include selectable polarization and a second, high-elevation, receive-only beam. Circular polarization, if used during rainy weather, can provide between 10- and 20-dB rejection of rain return. However, circular polarization also has an associated target loss (about 3 dB), so a switch is often provided to allow the system to be operated with maximum sensitivity when rain rejection is not required.

A high-elevation receive-only beam is in common use in air-traffic-control radar antennas to give improved rejection of ground return at short range. An electronic switch connects the receiver to the high beam in the ground-clutter regions and then switches to the lower-elevation transmit beam pattern for the remainder of active range. Both polarization switching and beam switching add complexity to the feed of the feed-reflector antennas typically used in this application. Two examples which illustrate current designs follow.

ARSR-3

The ARSR-3 radar system was developed by Westinghouse for use in the en route air-traffic-control system of the Federal Aviation Administration (FAA).^{6,7} The L-band radars (1.25 to 1.35 GHz) are used to maintain surveillance over aircraft in the high-altitude air routes between terminals. They provide 2D search data to a range of 366 km with a 12-s data interval. For this application, an antenna must have a shaped elevation coverage, a second high-elevation receive beam, and selectable linear or circular polarization.

Figure 32-2 shows the horn-reflector antenna used in the ARSR-3. The 6.9- by 12.8-m reflector forms a fan beam 1.25° wide in the azimuth coordinate. The antenna and pedestal are supported by a steel open-structure tower and are protected from the external environment by a space-frame radome.

The shaped elevation coverage, shown in Fig. 32-3, is formed by a doubly curved reflector. The upper portion of the reflector is nearly paraboloidal to direct energy to

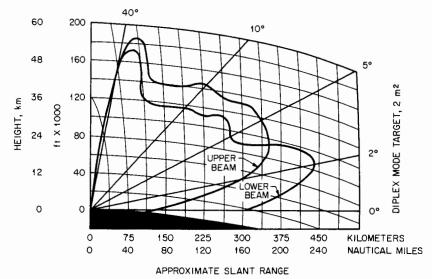


FIG. 32-3 ARSR-3 vertical coverage. (Courtesy of Westinghouse Electric Corp.)

the peak of the low-beam pattern, while the lower portion of the reflector departs from the parabola to direct more energy to elevation angles between 5 and 40°. The antenna features a rapid beam cutoff of the lower vertical pattern to minimize the lobing caused by surface reflections.

The dual-feed horns shown in Fig. 32-2 are used to provide two receive beams. One is a low-elevation beam used during transmission and reception, while the second is a higher-elevation beam which is switched in only during the time of arrival of the short-range returns in order to suppress land-clutter returns. For ranges beyond the clutter, the receiver is connected to the low-beam port to give better low-elevation coverage at far range. An important requirement of a two-beam design is the allowable gain difference in the direction of the horizon. If the gain difference is too large, the horizon range of the high-elevation beam will be shorter than the range of the farthest clutter, and hence the high beam cannot be fully utilized. This gain ratio is held to 16 dB in the ARSR-3 design by using the outputs of both horns shown in Fig. 32-2 to form the high-elevation beam.

Circular polarization (CP), needed to cancel rain return, complicates antenna and feed design. A switch is required to select either vertical or circular polarization; but, more important, symmetry is required between horizontal and vertical polarizations in order to achieve a high integrated cancellation ratio from the CP mode. An integrated cancellation ratio of better than 18 dB is realized by this design.

AN/TPN-24

The AN/TPN-24 is an airport surveillance radar developed by Raytheon for the U.S. Air Force as part of the AN/TPN-19 ground-controlled approach system. This S-band radar (2.7 to 2.9 GHz) provides 2D surveillance of the air space in the vicinity of an airfield. Air traffic controllers seeing this 2D information displayed on a plan

position indicator (PPI) vector landing aircraft onto the runway approach while communicating with the pilots via radio. For this application, a shorter-range and higher-data-rate radar is required than in the en route surveillance application described above, so the AN/TPN-24 gives coverage to 111 km with a 4-s data interval.

Figure 32-4 shows the AN/TPN-24 radar. The shelter contains all the radar electronics as well as a display, a radio, and microwave-relay equipment. The antenna mounted atop the shelter is disassembled and stowed inside the shelter for transport. When erected, the antenna reflector is 4.27 m wide and 2.4 m high, which at S band gives an azimuth beamwidth of 1.6°. The elevation beam pattern is shaped to match the desired elevation coverage, as shown in Fig. 32-5.

The requirement for transportability provides an incentive to use the smallest possible vertical aperture that will give the desired elevation pattern. In this antenna the entire reflector has a paraboloidal shape, and the elevation-pattern shaping is achieved by controlling the amplitude and phase of the power distributed to each of the 12 feed horns.

The particular feed illumination is determined by the microwave power divider mounted on the back of the reflector. Incorporated into this divider is a pin-diode switch that allows the amount of power coupled to the first feed horn (the horn contributing to the pattern near the horizon) to be varied during the receive mode. The

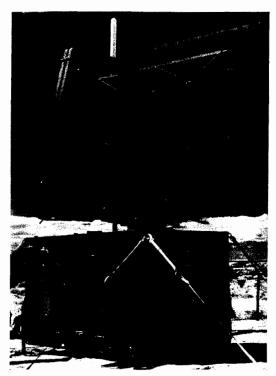


FIG. 32-4 AN/TPN-24 2D antenna. (Courtesy of Raytheon Company.)

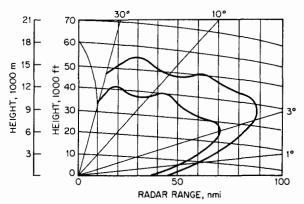


FIG. 32-5 AN/TPN-24 vertical coverage for single-channel and two-channel diversity. (Courtesy of Raytheon Company.)

switch allows the beam to be raised to reduce clutter at short range. The underside of the elevation beam pattern is tailored to produce a rapid cutoff and low sidelobes, thus minimizing lobing effects.

Linear or circular polarizations are selected by polarizers in series with each of the 12 feed horns. The polarizers are ganged and rotated mechanically to change polarization. To achieve the 20-dB integrated cancellation ratio provided by the antenna, mutual coupling between horns is minimized and compensated so as to equalize the feed pattern in both vertical and horizontal polarizations.

3D Systems

The need for 3D search radars originates in the requirements of military air defense systems. These systems protect an air space by detecting intruders and vectoring defending aircraft to intercept these intruders. This process requires that the interceptor know the altitude of an intruder, and therefore an elevation measurement by the radar is needed. Early systems used a 2D radar in combination with a separate height-finder radar that was designated to selected targets to measure altitude. More recent systems combine the 2D search and height finding into a single 3D radar system with the capability of measuring a target's position in all three coordinates.

The antenna for a 3D radar must have a narrow receive beamwidth in the elevation as well as in the azimuth coordinate. While the required vertical coverage is about the same as that shown in Fig. 32-3 for the ARSR-3, the antenna must be capable of forming a narrow elevation beam within that coverage. Since the operational requirement is for a fixed-altitude accuracy, it is possible to allow the elevation error (and hence the elevation beamwidth) to increase at higher elevation angles.

Since these 3D radars are for military applications, the antennas must have low-azimuth sidelobes and wide bandwidth to operate effectively in an electronic-counter-measure (ECM) environment. The low sidelobes reduce jamming received from directions other than that of the target, and the wide bandwidth allows the use of frequency agility, which forces the jammer to dilute its power by spreading it over a wider band.

Various antenna techniques have been used to satisfy the 3D requirement. Two common types are stacked-beam and pencil-beam antennas. Stacked-beam systems

transmit through a fan beam to illuminate the entire vertical coverage region and then receive returns through a stack of simultaneous receive beams. The pencil-beam system has a single beam, narrow in azimuth and elevation, which is used for both transmit and receive to scan the required elevations sequentially.

AWACS

The AN/APY-1,2 is an airborne air-defense radar developed in the early 70s by Westinghouse for Boeing, the AWACS prime contractor. Over 50 systems have been delivered for operation throughout the world, and the radar is still in production. The system may be deployed quickly when needed to provide surveillance over an area of current interest. 9-11

Airborne surveillance systems have an important advantage over their ground-based counterparts in the ability to see low-altitude aircraft at long range, which would be below the horizon of ground-based systems. However, the airborne system must detect these targets from a moving platform, against a background of clutter, and within the space, power, and aerodynamic constraints of the aircraft. Separating the desired targets from ground return is one of the most difficult problems. The clutter return is not confined to zero Doppler as in a ground-based system, because the moving platform causes sidelobe clutter to extend over a band of Doppler frequencies equal to twice the aircraft Doppler

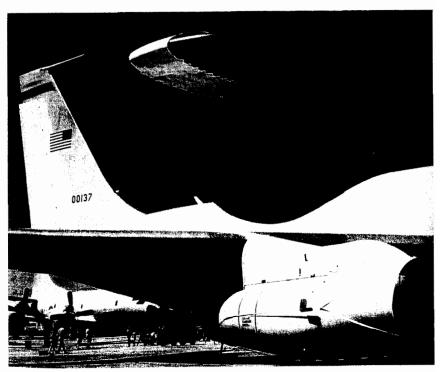


FIG. 32-6 AWACS antenna in rotodome mounted on the tail section of a Boeing 707-320 aircraft.

velocity. This leads to the requirement that the radar antenna have very low sidelobes in the direction of the ground.

The AWACS S-band antenna is one of the first low-sidelobe arrays to be manufactured in production quantities. It is a planar waveguide array of slotted waveguides with more than 4000 slots in all. The slots are designed to produce the aperture illumination necessary for low sidelobes and also to compensate for the effects of mutual coupling on the aperture illumination. Twenty-eight ferrite phase shifters are used to steer the beam in the elevation coordinate. While the elevation beamwidth is larger than would be preferred for a three-dimensional system, its height, and therefore its elevation beamwidth, is limited by aerodynamic considerations. The low sidelobes required for clutter suppression are also beneficial for suppressing electronic countermeasures.

AWACS's low sidelobes are achieved through precise control of the antenna during manufacture as well as the method of integrating the antenna with the airframe. Figure 32-6 shows the AWACS antenna mounted atop the fuselage of a Boeing 707-320 aircraft. The antenna is enclosed in an aerodynamic rotodome which rotates at 10 r/min. Since the portion of the radome in front of the radiating aperture remains fixed in relation to the antenna, there are no seams or joints moving past the radiating aperture.

AN/TPS-59

The AN/TPS-59 is a long-range 3D surveillance radar developed by General Electric for the U.S. Marine Corps. This L-band radar uses a single pencil beam formed by an active phased array to scan elevation sequentially as the antenna rotates mechanically in azimuth. The system's most distinctive feature is its solid-state transmitter, which is distributed throughout the active array antenna. 12,13

The antenna shown in Fig. 32-7 is 9.1 m high and 4.6 m wide. It is made up of 54 rows of horizontally polarized elements and their associated feed networks and row electronics. Each row contains an azimuth power divider, a solid-state row transmitter, two RF receivers, and two low-power phase shifters. Column feed networks combine the row outputs to form the pencil-shaped transmit beam and a three-beam monopulse cluster for receive. A receiver and an RF exciter are also included on the rotating portion of the antenna so that only power, IF, and control signals need be transferred to the antenna pedestal.

32-3 TRACKING RADAR

In radar applications for which target data with greater accuracy or a higher data rate than can be provided by a search radar are required, a tracking radar is used. The tracking-radar antenna usually has a pencil beam that follows a target in track to provide continuous measurement of the target's position in range, azimuth, and elevation. In some applications target signature data in the form of amplitude and phase variations of the target return are also measured. Targets are usually first detected by a search radar and then designated to the tracker for measurement. To acquire a target, the tracker must search a small volume about the designated point. When the target is detected, range and angle tracking loops close, and the range gate and beam are held centered on the target until target data are no longer required and the track is broken off.

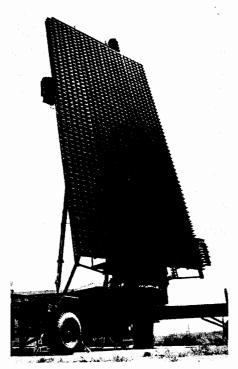


FIG. 32-7 AN/TPS-59 3D antenna. (Courtesy of General Electric Co.)

Tracking radars tend to operate at higher microwave frequencies than search radars. It has been shown that tracking-radar sensitivity is proportional to average transmitter power times the antenna aperture area squared times the operating frequencies squared. The increased importance of aperture and frequency compared with the search-radar case provides a greater incentive to use larger apertures and to operate at higher frequencies. An upper limit on the choice in these parameters is often set by atmospheric attenuation or antenna cost in relation to transmitter cost. The exceptions are radar applications for which target signature or propagation data are needed at a specific frequency, independently of cost considerations.

Fundamental to all tracking-radar antennas is the ability to measure a target's position within the beam so that the beam may be centered on the target. The two techniques used for this purpose are conical scan and monopulse. Conical scan consists of rotating the pencil beam in a circular pattern around the target in track. If the target lies off the center of the circular scan pattern, the target return is amplitude-modulated by the scanning beam. The phase and amplitude of this modulation are detected and used to measure the target's position within the beam. This process requires that at least one revolution of the beam be completed before the measurement can be made. Monopulse is another technique for measuring the target's position in the beam that is capable of measuring azimuth and elevation on a single pulse return,

but it requires two additional receiver channels. Monopulse uses a three-beam cluster consisting of a pencil beam plus two superimposed difference beams to measure the target off-axis error in both angular coordinates.

For examples of current tracking-radar antenna designs the reader is referred to Chap. 34, "Tracking Antennas." The tracking function as incorporated into multifunction phased arrays is discussed in the next section.

32-4 MULTIFUNCTION ARRAYS

Radar search and track functions are normally realized with separate antennas, optimized in frequency and aperture size. However, with the development of high-power RF phase shifters and advanced digital-processing techniques, phased arrays have been employed to furnish nonmechanical means of antenna beam scanning and, because of the highly agile characteristics of the beam positioning, to provide an opportunity to combine search and track functions in a single radar. The digital-processing and beam-steering aspects of the multifunction phased array are beyond the scope of this text but are significant contributors to both the successful operation of the radar and its cost. ^{15,16} For the most severe target environments, the use of the multifunction array can be justified, but only after careful consideration of alternatives such as mechanically scanning antennas and hybrid approaches. Table 32-5 lists some of the features available from the multifunction array. The primary disadvantages are high cost, complexity, and compromise in the choice of frequency between the optima for the search and track functions.

The high cost of these arrays has been significant in restricting the systems to which this technology has been applied. Nevertheless, there has been gradual, though sometimes unsteady, growth in the number of phased arrays in operation. Sperry Corp.'s AN/FPS-85 at ultrahigh frequency (UHF) used a separate transmit and thinned-receive aperture^{17,18} to obtain a high target resolution at reduced costs. Aperture thinning was also used by Raytheon for COBRA DANE at L band and the all-solid-state PAVE PAWS at UHF. Raytheon's mobile Patriot radar at C band uses an optical RF power-distribution system (space feed) to reduce both cost and weight.

For applications in which beam scanning in one or both planes is less than 120°, several radiating elements can share one phase shifter, as in the AN/TPQ-37 by Hughes, or hybrid scanning techniques such as a combination of a reflector and an array can be utilized, as in the AN/GPN-22 by Raytheon. The Sperry dome

TABLE 32-5 Features of Multifunction Arrays

Versatility: search and track
Multiple independent beams
Inertialess beam agility
Computer control
Planar or conformal type
Blast resistance
Independent control of transmit and receive illumination
Potential use of distributed power amplifiers
Graceful degradation

antenna¹⁷ incorporates a planar array space-feeding a dome and achieves hemispheric coverage with a significant reduction in radiating elements and phase shifters.

From an antenna engineer's viewpoint, costs are controlled by optimization of the aperture, using the minimum number of radiating elements and phase shifters to accomplish the radar mission. After the array has been optimized, the next task is to design a cost-effective radiating-element and feed-distribution network (including the phase shifters, power- and signal-distribution network, and beam-steering computer). For examples of current phased-array design practice the reader is referred to Chap. 20, "Phased Arrays." Examples of phased-array radar applications are discussed in the following subsections. For additional information the reader is directed to Refs. 15 through 19.

PAVE PAWS

PAVE PAWS (Phased-Array Warning System) is a system of four radars designated as the AN/FPS-115, located at Otis AFB in Massachusetts, Beale AFB in California, Eldorado AFB in Texas, and Robins AFB in Georgia. Each radar consists of a pair of circular planar arrays that provides early warning of a sea-launched ballistic missile attack on the continental United States. It also furnishes attack characterization to the North American Aerospace Defense Command (NORAD), the Strategic Air Command, and national command authorities. At 5500 km, the PAVE PAWS radar²¹ can detect objects as small as 10 m². Development was undertaken by Raytheon Company in 1976, with all four sites fully operational in 1987. The Ballistic Missile Early Warning Systems (BMEWS) at

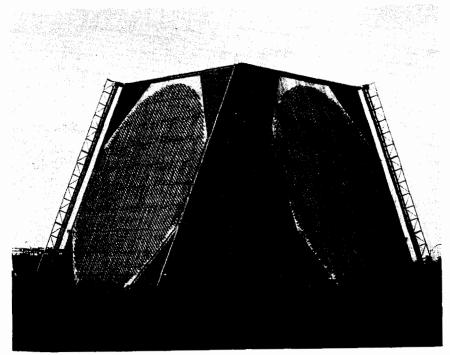


FIG. 32-8 PAVE PAWS. (Courtesy of Raytheon Company.)

TABLE 32-6 PAVE PAWS System Parameters

420-450 MHz
5355
1792
Corporate
22 m
30 m
120°
2
Solid state
1792
85 W
340 W

Thule, Greenland was upgraded with a version of the PAVE PAWS in 1987, and work is currently in progress for a three-face version at Fylingdales Moor, England, scheduled for completion in 1992.

The building housing the radar, located at Otis AFB on Cape Cod, in Massachusetts (as shown in Fig. 32-8), is approximately 32 m high. Each array face consists of 5355 crossed-dipole elements, originally designed by General Electric 19 as part of the PARCS system in North Dakota but optimized for the PAVE PAWS system. Only a center circle of 2677 elements, of which 1792 are active radiators, is presently used. The remaining annulus elements are all resistively terminated to be used for further growth.

The radar system characteristics are shown in Table 32-6. The active portion of each array is density tapered (thinned)¹⁸ to provide a 35-dB Taylor weighting. The active elements are arranged into 56 subarrays containing 32 elements, each connected to a solid-state transmitter/receiver,²² as shown in Fig. 32-9. Because of density tapering, the

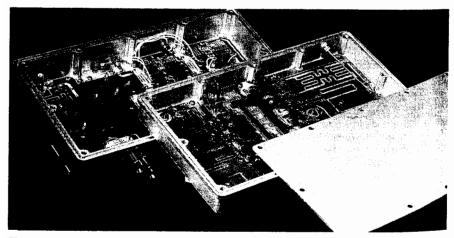


FIG. 32-9 Solid-state transmitter/receiver. (Courtesy of Raytheon Company.)

number of dummy elements per subarray varies from a minimum near the center of the active array to a maximum for the peripheral active subarrays. The solid-state transmitters are connected to a corporate feed of coaxial/low-power components. The use of a distributed solid-state architecture provides for graceful degradation, more reliable operation, and easier replacement without ever having to turn the radar off.

Patriot

The Patriot radar, AN/MPQ-53, designed and built by Raytheon is a mobile C-band phased-array radar which performs target search and track, missile search and track, communications during midcourse guidance, and target-via-missile (TVM) terminal guidance. This tactical air defense system is designed to operate in a hostile ECM environment as a replacement for the improved Hawk and Nike-Hercules systems, which typically require up to nine radars. Studies for this system were initiated in 1965, with an engineering development phase beginning in 1972. Initial production was funded in 1979, with a planned additional 12 units in 1982 and 18 per year through fiscal 1986.

The unique features of the radar antenna can be seen in Fig. 32-10. The antenna consists of a space-fed main array, a smaller TVM array, several ECM arrays, and an identification, friend or foe (IFF), antenna. 23,24 The main array, approximately 2.5 m in diameter, is filled with 5161 elements, which are contained in an array lens structure that is stowed in a horizontal position during transport and is erected hydraulically for system operation. Each element consists of a circular-waveguide dielectrically loaded front radiator, a flux-driven latching ferrite phase shifter, and a rectangular-waveguide dielectrically loaded rear radiator.

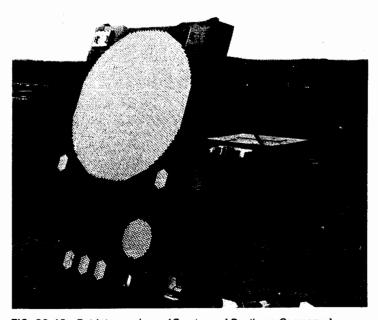


FIG. 32-10 Patriot-array lens. (Courtesy of Raytheon Company.)

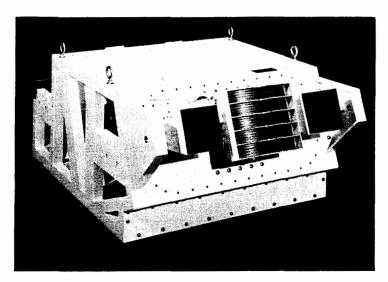


FIG. 32-11 Patriot feed assembly. (Courtesy of Raytheon Company.)

The phase shifter utilizes a dielectrically loaded nonreciprocal garnet formed into a toroid and located in the center of the rectangular waveguide. Phase commands are in the form of row and column start-and-stop pulses whose time intervals are equivalent to 4-bit phase commands. Prior to any phase command, the garnet is driven into saturation to establish a reference phase from which all phase increments are set. The amount of phase shift is obtained by applying a voltage pulse of constant amplitude and variable width.

The feed assembly shown in Fig. 32-11, which is located approximately 2.5 m from the array, consists of transmitter horns and a multimode, multilayer receive feed. Through this arrangement, the duplexing function is implemented by the space separation of the feeds rather than through the use of conventional duplexers. The receive feed is located on the array axis. Phase-shift commands for transmit and receive differ to account for the different placements of the transmit-receive feeds. The receive feed is a five-layer (*E*-plane), multimode (*H*-plane) monopulse horn with independent control of the sum-and-difference patterns. Dielectric lenses in the feed aperture provide phase and amplitude correction of the *H*-plane excitation.

A TVM array (shown below and to the right of the main array in Fig. 32-10) produces a receive sum output from the TVM downlink signals and provides mainarray sidelobe blanking and cancellation. There are 253 elements arranged in an aperture approximately half a meter in diameter. The array utilizes a stripline corporate feed. Uniform illumination is provided through a primary-distribution-network 12:1 power combiner, which in turn is connected to an aperture illumination network. This is followed by a transition to the waveguide phase-shift element, which is identical to that used in the main array.

Up to five ECM arrays are provided, three along the bottom of the antenna and two, one on each side, below the main array. These arrays each contain 51 elements identical to those used in the main and TVM arrays. The corporate feed is a single stripline layer which provides uniform amplitude and in-phase signals at each element.

The IFF antenna is located just below the main array.

Limited-Scan Arrays

Many radar applications for which antenna beam scanning in the order of $\pm 10^\circ$ is required, such as ground-controlled approach and weapon locating, can use multifunction array antennas that are considerably less complex than those previously described. Limited-scan or limited-field-of-view (LFOV) antennas have been designed to reduce the number of phase shifters in the array. ^{25,26} The most common approach is either to provide one phase shifter for a subarray of elements or an oversized element or to use a small array in combination with either a reflector or a lens. It is interesting to note that this latter hybrid approach of using a lens to reduce the number of radiating elements and phase shifters also promises to reduce the cost of wide-angle scanning (hemispheric), as demonstrated in the Sperry dome antenna. ²⁷

Two examples of the implementation of multifunction arrays to the limited-scan application are given. In the first, the AN/GPN-22 utilizes a hybrid approach, and in the second, the AN/TPQ-37, one phase shifter per several elements is used in one plane of scan.

AN/GPN-2228

The antenna used by Raytheon for the ground-controlled approach AN/GPN-22 system is similar in its concept to the AN/TPN-25 antenna. The antenna and its radar shelter are shown in Fig. 32-12. After the development of the mobile version, AN/TPN-25, in 1969 and the subsequent production of 11 systems, the antenna system

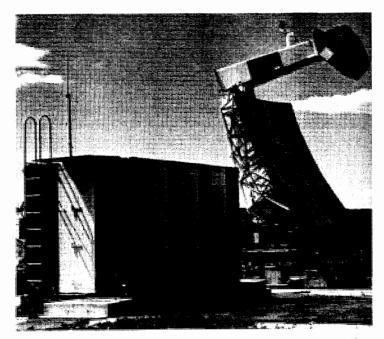


FIG. 32-12 AN/GPN-22 precision approach radar. (Courtesy of Raytheon Company.)

TABLE 32-7 AN/GPN-22 Antenna Parameters²⁸

Туре	Limited-scan phased array
Gain	42 dB
Beamwidth	
Azimuth	1.4°
Elevation	0.75*
Scan volume	
Azimuth	±10°
Elevation	8*
Polarization	Circular
Array elements	443
Phase-shifter bits	3
Reflector size	4 m by 4.7 m

was redesigned electrically and mechanically in 1975 to reduce costs further for fixedsite applications and was redesignated the AN/GPN-22. Approximately 50 of these systems have been produced. The radar searches a volume of 20° in azimuth and 8° in elevation out to a range of 36.5 km while simultaneously tracking up to six targets.

For this antenna, the parameters of which are listed in Table 32-7, a small space-fed array illuminates a large reflector. The antenna gain and beamwidths are determined by the reflector size, while the number of beam positions is determined by the number of array elements. The small phased array illuminates the reflector and, by scanning on the reflector surface with properly adjusted phase shifts, can cause the antenna's far-field beam to scan over a limited sector. Since the AN/GPN-22 system is to be used at fixed sites, the antenna reflector was made larger than in its mobile version. This, along with a reduced scan volume, reduced the number of array elements from 824 to 443. At the same time, the array was relocated above the reflector.

The antenna is on a pedestal mounted on a concrete base separate from the shelter. The pedestal base is capable of rotating the antenna through 280° of azimuth to permit its use for multiple-runway coverage. The feed array consists of 443 three-bit ferrite phase shifters space-fed from a monopulse multimode horn. The array RF monopulse receivers and phase-shifter power supplies are mounted in the base of the antenna.

AN/TPQ-37

The AN/TPQ-37 radar system is a tactical S-band phased-array system capable of being transported by surface vehicles or by helicopter lift. The combination of the AN/TPQ-37 and the AN/TPQ-36, which has a similar architecture but uses different antenna techniques at a higher frequency, is referred to as the Firefinder. The combined system provides automatic first-round location of hostile artillery positions and is designed to locate simultaneous fire from numerous weapons on the battlefield. The AN/TPQ-37 will normally be sited behind the battle area to locate opposing longrange artillery fire. Emplacement time is estimated at 30 min, with a displacement time of 15 min. Initial development was undertaken by the Hughes Aircraft Company in 1973, with limited production authorized in 1976 and an expected production of 72 systems.¹¹

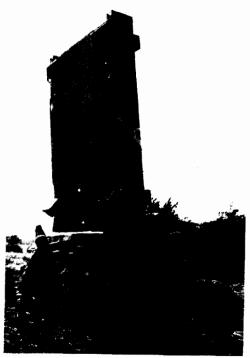


FIG. 32-13 AN/TPQ-37 radar set. (Courtesy of Hughes Aircraft Company.)

The antenna, shown in its erected position above its trailer in Fig. 32-13, remains stationary in normal operation but has phase scanning in both planes to provide a 90° azimuth sector scan and an elevation scan of a few degrees. Since the weapon-locating mission can be accomplished with a limited elevation scan, the number of phase shifters in the elevation plane is greatly reduced by having one phase shifter feed a vertical subarray of six elements.

Figure 32-14 is a block diagram of the antenna feed network.²⁹ The number of elements in the phased array is 2154, consisting of 359 vertical subarrays of 6 elements each. A vertical subarray module is shown in Fig. 32-15. Each module contains three separate microstrip diode phase shifters with the following phase states:

Phase shifter	Phase states	
Α	22.5°, 45°, 90°, 180°	
В	25°, 50°	
c	25°	

The phase shifter is fabricated by using thick film techniques on an alumina substrate. The rest of the module is a 1:6 power divider using ring hybrids and trans-

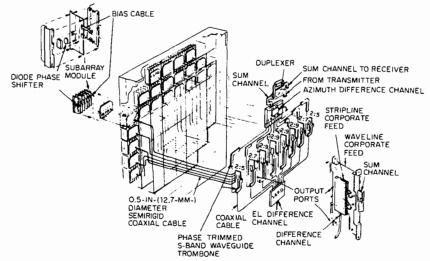


FIG. 32-14 AN/TPQ-37 antenna-feed block diagram. (Courtesy of Hughes Aircraft Company.)

mission lines to the six dipole feeds. These transmission-line lengths are designed to provide a progressive phase shift between dipoles, causing the radar beam to be tilted in the elevation plane.

Subarrays are arranged in groups of six fed by 1:6 air stripline power dividers. These groups are in turn stacked vertically into eight columns. The number of groups

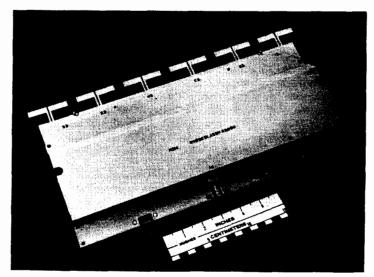


FIG. 32-15 AN/TPQ-37 antenna subarray module. (Courtesy of Hughes Aircraft Company.)

in a column increases from five at the edges to nine in the center. The 1:6 power dividers for subarrays in the last two columns on each side have unequal power split. Signals from the groups in any one column are connected through semirigid coaxial cable to a column-waveguide corporate feed with two outputs per column. One output, the sum arm, possesses even symmetry, and the other output, the difference, possesses odd symmetry in the elevation plane. The column difference signal is amplitude-weighted in a stripline feed assembly to control the elevation difference sidelobe level.

The difference signals for all eight columns are connected by a coaxial line to an 8:1 corporate feed with amplitude weighting for azimuth sidelobe control to form an elevation difference beam. The column sum signals which have been amplitude-weighted in their column networks to control the elevation sum sidelobe level are connected by waveguide to an 8:1 waveguide corporate feed to form a sum beam. The azimuth difference beam is formed by taking the difference of the eight column signals and combining them in the same manner as the elevation difference beam.

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Microwave Beacon Antennas

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33-1 Introduction 33-2

33-2 Interrogator Antenna Design Principles 33-2
 Vertical Pattern Design 33-3
 Horizontal Pattern Design 33-5
 Sidelobe Suppression 33-6

33-3 Interrogator Antennas: Practice 33-9 Ground-Based Systems 33-9 Airborne Systems 33-13 A microwave beacon system, like a radar, transmits a pulsed RF wave to locate a target, using time delay of the "echo" to determine distance and antenna directionality to determine angular location. The distinguishing feature of a beacon system is that the target cooperates in this process, using on-board electronics to enhance the returned RF wave with amplification, frequency shifting, and coding. Beacons are thus highly accurate and reliable surveillance systems and also can provide some data-link capability. Beacon systems typically consist of transponders and interrogators. Transponders are the active devices carried by the target to provide the enhanced echo. Transponders are usually located on moving platforms, although fixed transponders may be used to mark hazards, navigation points, or calibration points. Interrogators employ equipment similar to that of conventional pulsed radars, i.e., a transmitter which elicits replies from the transponder and a receiver to detect and process the replies.

By far the most widely deployed beacon system is the military IFF (Identification Friend or Foe) System and its civilian derivative ATCRBS (Air Traffic Control Radar Beacon System). The military systems are also known as Mark X, Mark XII, and Mark IV IFF. Mark IV, the latest version, is known internationally as the NIS (NATO Identification System). The civilian systems are also known internationally as SSR (secondary surveillance radar). All systems have similar waveforms and share common frequencies of 1030 MHz for interrogation and 1090 MHz for reply. 1-3 Polarization is always vertical. NIS also can be interrogated by certain radar signal formats at frequencies near C-band.

Transponders typically must respond to interrogations from any direction in space. Therefore, antennas with omnidirectional coverage in azimuth are desired for this part of the beacon link. For aircraft, the antennas are usually blade antennas (aerodynamically shaped monopoles) protruding from the aircraft skin or flush-mounted annular slots in the skin. Design of these antennas is relatively straightforward, with primary emphasis on location to minimize shadowing. A.5 A modest 8 percent bandwidth covers the interrogation and reply frequencies. Interrogators which also must respond to NIS radar interrogations must have additional bandwidth. When aircraft shadowing prevents omnidirectional coverage from a single antenna, transponders are available with a time-sharing switch to rapidly sample two antennas (e.g., one on top of the aircraft and another on the bottom).

The interrogator may be either ground-based or airborne. In either case, the interrogator antenna is highly directional, with some means for scanning the directional beam over a volume of space. Thus interrogator antennas are more complex in design and operation. These constitute the central focus of this chapter.

33-2 INTERROGATOR ANTENNA DESIGN PRINCIPLES

Requirements for interrogator antennas are similar to those for radar antennas, with the following differences:

- Beacons do not benefit from the "two-way" sidelobe suppression of radar.
- The beacon's greater link reliability mandates greater attention to suppression of false targets from reflections and sidelobes.

- Beacon power levels can be much lower because of target cooperation.
- Beacon antenna gain is often less critical than radar.

Minimization of false targets from reflections and sidelobes is a central design consideration. Colocation with a primary radar and the large physical dimensions imposed by the relatively low frequency are other factors.

Vertical Pattern Design

The preferred vertical pattern shape for surface-based interrogators is a sector pattern (uniform gain from the horizon to some prescribed upper limit) or a modified cosecant pattern. The cosecant pattern is preferred for long-range systems requiring high gain near the horizon. The upper limit of coverage is typically about 40° elevation.

Multipath reflection from surrounding terrain is a major contributor to false targets for surface-based interrogators. Multipath is minimized by shaping the vertical radiation pattern to reduce radiation below the horizon. Older antenna designs used small vertical apertures with broad vertical patterns, resulting in considerable radiation onto surround-

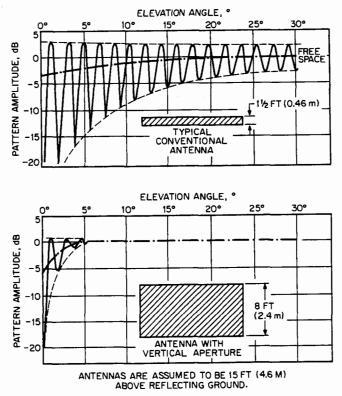


FIG. 33-1 Influence of vertical aperture on elevation lobing patterns.

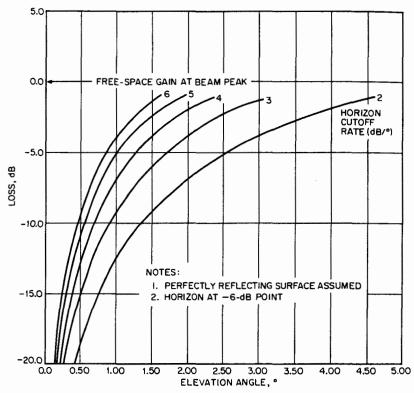


FIG. 33-2 Envelope of lobing minima for various horizon cutoff rates.

ing terrain. More recent designs have larger vertical apertures to shape the vertical pattern for substantially reduced radiation below the horizon. Figure 33-1 shows examples of vertical lobing for small and large apertures.

The antenna beam is usually tilted up slightly so that the pattern level at the horizon is -6 dB. A useful measure for multipath rejection is the slope of the vertical pattern at the horizon, measured in decibels per degree. Figure 33-2 shows the envelope of the multipath minima as a function of this cutoff rate. Since higher cutoff rates require larger apertures, the trade between antenna size and reduced multipath must be made carefully. A cutoff of 2 to 4 dB per degree has been found to be satisfactory for most installations.

Pattern-synthesis techniques have been developed to optimize horizon cutoff subject to constraints on antenna size, above-horizon coverage, and sidelobe levels. For the synthesis of sector beams, Evans⁶ has adapted a procedure originally developed for digital filters. For engineering estimates, Lopez⁷ provides curves (normalized to a vertical aperture of one wavelength) relating horizon cutoff, sidelobe level, and ripple within the sector beam (Fig. 33-3).

For urban interrogator locations, limited electronic scan of the vertical pattern is very useful to avoid direct illumination of tall buildings, thereby reducing reflected false targets. This feature, called beam hopover, allows the -6-dB pattern point to be tilted up

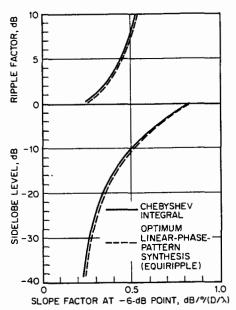


FIG. 33-3 Normalized horizon cutoff rate. (From Ref. 7, © 1979 IEEE.)

slightly when interrogating in the direction of the obstruction. Array implementations of the interrogator can use a multiple-beam feed network to achieve this feature with a minimum number of switches or phase shifters. With a reflector antenna, a secondary feed below the focus can achieve the result.

Recent designs have used dipole arrays because they provide the control of vertical illumination needed to obtain shaped patterns, good horizon cutoff, and effective use of vertical aperture. Shaped reflectors also can be used, with multiple-horn and line feeds.

Because the vertical pattern is broad, it provides no significant ability for verticalplane direction finding. This is usually not a limitation because many transponder replies include a coded report of altitude. Thus the interrogator often receives a direct report of the target's vertical coordinate.

Horizontal Pattern Design

In the horizontal plane, accurate determination of target angle and minimization of false targets are of central importance. Surface-based interrogators typically use a low-sidelobe beam with a 3-dB width of 2 to 4°. The target's location can be measured to an accuracy of about one-tenth the 3-dB beamwidth by scanning the beam across the target while interrogating continuously, with the target location estimated as the centroid of the "run" of replies that is received. For greater accuracy, a monopulse difference pattern is included in the horizontal plane. Standard off-boresight monopulse processing is used. With monopulse, angle accuracy of 1 to 2 percent of the half-power beamwidth is possible.8 For monopulse antennas, the two patterns are called the Σ (sum) and Δ (difference) beams, respectively.

For arrays, the Σ beam is formed with cophased illumination in the horizontal dimension. Amplitude tapering for -25- to -30-dB sidelobes is typical. The Δ beam is obtained by feeding opposing sides of the aperture in phase opposition. Use of the Σ amplitude taper for both the Σ and Δ patterns gives a simple feed network but results in quite high Δ sidelobes. This high-sidelobe Δ pattern is suitable only for noncritical uses. A more complex multibeam feed network, capable of producing an independently optimized Δ illumination (such as the Bayless taper), is usually required. Optimal Σ and Δ illuminations are very similar on the outer parts of the array, so the multibeam feed is only required for the center portion of the array. Figure 33-4 shows the two types of difference patterns and their respective aperture illuminations.

For reflectors, a conventional parabolic contour in the horizontal plane gives the desired pencil beam. Careful control of feed spillover is needed to ensure that backlobes are -30 dB or lower. Standard monopulse feed design will give suitably low Δ sidelobes.

Sidelobe Suppression

A procedure called interrogation sidelobe suppression (SLS) cues the transponders to avoid replying to sidelobes of the interrogator antenna. With SLS, the interrogation is transmitted first by the Σ pattern and then by an omnidirectional "control" pattern (Ω) . The Ω gain is lower than that of the Σ beam but higher than the sidelobes. The transponder replies only if the amplitude for the Σ interrogation exceeds that for the Ω by some prescribed margin, indicating that the interrogation came from the main beam. A variation called improved SLS (ISLS) provides for suppression of reflected main-beam interro-

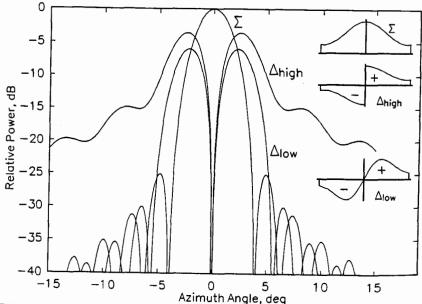


FIG. 33-4 Typical far-field horizontal patterns with the corresponding aperture distributions shown in the insets.

gations. With ISLS, a pulse is transmitted simultaneously on the Σ and Ω beams, and the transponder measures timing differences to detect an interrogation arriving via a reflected path. Some beacon systems also employ SLS on the reply link (RSLS). With RSLS, a two-channel receiver compares replies received on the Σ and Ω antennas, blanking the reply when the relative amplitude indicates a pulse received by a Σ sidelobe.

When the directional and control beams (Σ and Ω) are derived from the same aperture, they share a common phase center. Consequently, the multipath lobing (Fig. 33-1) will be the same for both beams, so the proper Σ/Ω amplitude is preserved at all elevations. If, however, the phase centers are vertically displaced, the lobing does not match, and faulty SLS operation occurs. When an Σ peak aligns with an Ω null, sidelobe amplitude may be high enough to "punch through" the Ω coverage. When an Σ null aligns with an Ω peak, even the main beam may be unable to exceed the Ω gain, and all replies are suppressed. This differential lobing can be a serious problem, so most recent designs have used common phase centers. Common types of Σ and Ω patterns are illustrated in Fig. 33-5.

Omnidirectional Pattern This pattern is usually formed by a separate antenna, often a collinear array of dipoles. Its advantage is simplicity. It does not rotate and therefore does not require an additional rotary joint channel, and it does not constrain the design of the directional antenna. The vertical pattern of this Ω antenna is often designed to match that of the Σ . To avoid mutual blockage, the two antennas are displaced vertically, causing differential lobing. Such systems exhibit marginal SLS operation^{9,10} and are avoided in critical applications.

Difference Pattern The high-sidelobe difference pattern formed by an abrupt phase reversal at the center of the Σ illumination is sometimes used for Ω coverage. The vertical patterns and phase-center locations are closely matched, so differential lobing is minimized. The pattern is easily formed, requiring only a "magic T" power divider at the center of the array, and it imposes no other design constraints. Its principal shortcoming is that it provides little Ω coverage behind the antenna, allowing possible interrogation by backlobes and reflections.

With this pattern, the Ω pulse can be transmitted at a higher power level relative to the Σ because the null precludes main-beam blanking. The higher power compensates for the relatively poorer Ω coverage. This also narrows the effective beamwidth over which replies are elicited, because a substantial part of the main beam skirts are also blanked. Airborne military interrogators, where aperture size is often limited, use this effect to improve angular accuracy. For example, with Ω power which exceeds Σ by 5 to 10 dB, an antenna with a 35° 3-dB beamwidth can elicit replies over only a 5° sector. The design must consider the substantially higher power at the Ω port.

Notch Pattern For array implementations, this type offers an excellent combination of common phase center, central null, and control of sidelobe punch-through. The pattern is produced by the broad radiation from a single central column of the array, with simultaneous out-of-phase radiation by the Σ pattern to produce the notch. Because of the Σ 's greater gain, little power is needed to produce the notch, typically about 1 percent of the total. An auxiliary "backfill" antenna is usually added to cover backlobe radiation in this approach. (A backfill antenna is also useful with the difference-pattern omni.)

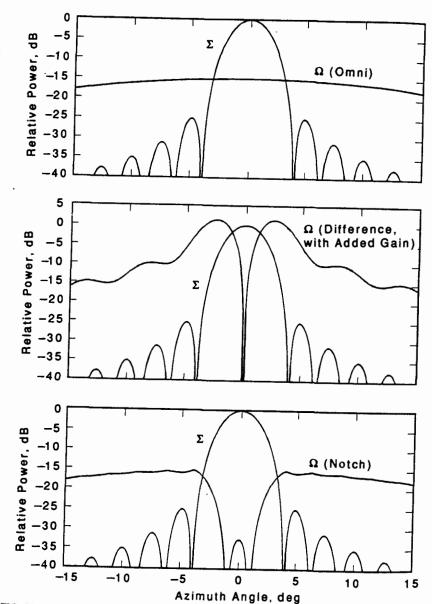


FIG. 33-5 Generic control-pattern types.

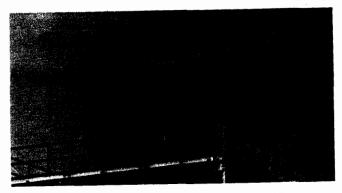


FIG. 33-6 Typical hog-trough antenna. (Courtesy of Department of Transportation, Federal Aviation Administration.)

33-3 INTERROGATOR ANTENNAS: PRACTICE

Ground-Based Systems

For many years the standard configuration for ATCRBS/IFF interrogators consisted of a linear array (commonly called a hog trough because it resembles an animal feeder) and a stationary omnidirectional antenna. The hog trough is a sectoral horn fed by a horizontal array of dipoles and is about 26 ft long. The beamwidth is 2.3° in azimuth and 42° in elevation. Peak sidelobe level is typically -23 dB. The omnidirectional antenna is a biconical horn or collinear dipole array mounted on a fixed mast beside the interrogator. Figure 33-6 shows such an installation at a Federal Aviation Administration (FAA) site. A more recent design, ¹¹ shown in Fig. 33-7, features an integral notch-type SLS pattern and also a difference pattern which can be used for monopulse angle estimation and RSLS. The military uses various shorter versions of the hog trough for its mobile interrogators. An example is shown in Fig. 33-8. These are approximately 14 ft long, have a difference-pattern Ω , and have a wider azimuth beamwidth, typically about 4°. All these antennas have little elevation beam shaping and little horizon cutoff (about 0.3 dB per degree). All are subject to problems of multipath.

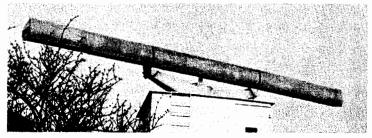


FIG. 33-7 Typical SSR antenna. (Courtesy Cossor Electronics, Ltd.)

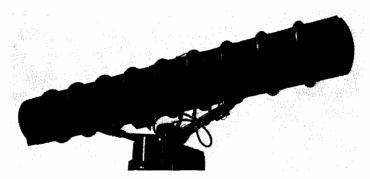


FIG. 33-8 Typical military IFF antenna. (Courtesy Hazeltine Corporation.)

More recently, designs have employed increased vertical aperture to control multipath. The open-array antenna 12 shown in Fig. 33-9 is a planar array of dipoles with a vertical aperture of 5 ft. It has a horizon cutoff of 2.2 dB per degree and employs an integral notch-type Ω pattern (with backfill radiator) for SLS, so multipath problems are greatly reduced compared with the hog trough. The dipole array is made unidirectional by columns of parasitic reflector dipoles located behind and between the columns of driven dipoles. This eliminates the need for a ground plane, giving a very open construction which has low wind loads, even with ice accumulations. Typical radiation patterns for this antenna are shown in Figs. 33-10 and 33-11. The open array has replaced the hog trough as the standard ATCRBS antenna at FAA terminal radar sites. 13

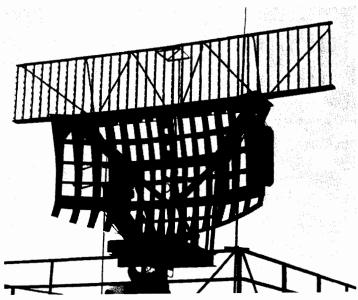


FIG. 33-9 Open-array SSR antenna. (Courtesy Texas Instruments, Inc.)

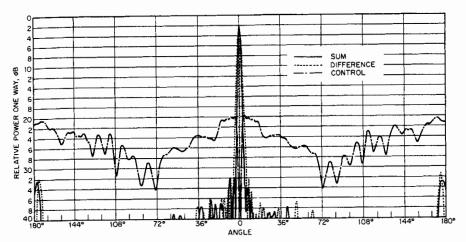


FIG. 33-10 Open-array azimuth patterns. (Courtesy Texas Instruments, Inc.)

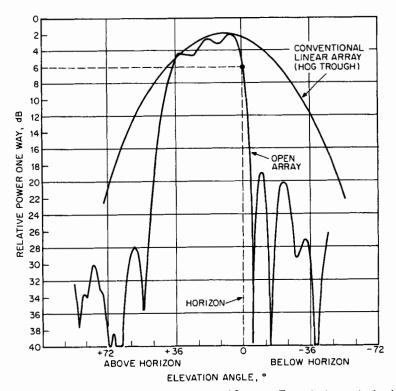


FIG. 33-11 Open-array elevation pattern. (Courtesy Texas Instruments, Inc.)

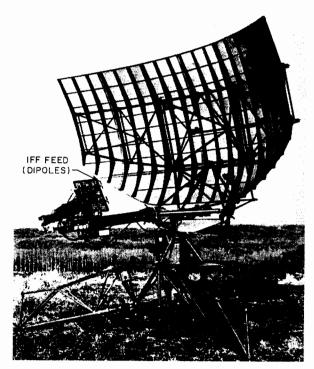


FIG. 33-12 Tactical S-band radar antenna with integral IFF feed. (Courtesy Thomson-CSF.)

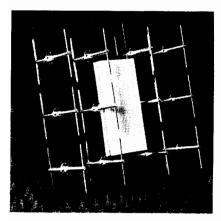


FIG. 33-13 Integral beacon feed for elevation-pattern shaping. (Courtesy AEG-Telefunken.)

At sites which have a large radar reflector as part of the surveillance equipment, a sharp horizon cutoff for the beacon can be obtained by sharing the reflector with the radar, using an *integral beacon feed*. Since both feeds must be located approximately at the reflector's focal point, the principal design problem is ensuring that each feed operates properly in the presence of the other. S-band and L-band radars are commonly associated with beacon systems. The two bands have somewhat different design concerns, as follows.

The S-band reflectors are relatively small, yielding approximately a 4° azimuth beamwidth and 2 dB per degree horizon cutoff. The 4° beam is too wide for most FAA applications but is useful for certain

less-demanding military applications. The S-band feed horn is small relative to the longer beacon wavelength, so an array of beacon dipoles can usually be disposed around the horn to make a beacon feed whose phase center is at the focal point.

The L-band reflectors are larger, giving a 2° azimuth beamwidth and 4 dB per degree cutoff. However, the larger physical size of the L-band feed horn usually precludes a separate dipole array around the radar horn. Therefore, either the beacon must be diplexed into the radar horn, or the beacon feed must be displaced from the focal point.

For either band, the beacon feed must be isolated from the radar so that it is not damaged by high radar-power levels and so that radar power is not coupled into the beacon receiver. In many cases the radar feed is circularly polarized, with both amplitude and phase patterns carefully adjusted for good axial ratio and proper illumination of the reflector. The beacon feed, being vertically polarized, can alter the axial ratio, degrading polarization performance of the radar. For either band, the elevation pattern is largely determined by the reflector contour, and it often approximates a cosecant-squared shape. The beacon feed pattern can be modified to direct more energy at the "spoiled" part of the parabolic contour, thereby increasing elevation coverage at higher angles to more nearly approximate a sector pattern.

Figure 33-12 shows beacon dipoles around the feed of an S-band radar. An array of dipoles as in Fig. 33-13 provides the feed-pattern control needed to optimize the beacon's azimuth and elevation-pattern shapes.

In the L-band ARSR-3 radar, the beacon feed is located beside the radar horn, off the focus (Figs. 33-14 and 33-15). This introduces an azimuth offset between the beacon and radar patterns. The returns are corrected with signal processing so that they appear coincident on the display. Radiation patterns for the ARSR-3 beacon feed are shown in Fig. 33-16.

Experimental beacon antennas using electronic scanning have been constructed. Cylindrical arrays are used to provide 360° azimuth scan. The version shown in Fig. 33-17, built by Hazeltine Corporation's Wheeler Laboratory, mounts on the fixed portion of the tower for an S-band radar. The vertical pattern is a sector beam with 3 dB per degree horizon cutoff. It includes beam hopover to avoid reflection obstructions. The antenna has Σ , Δ , and Ω horizontal patterns, with a 2.4° beamwidth. The azimuth beamwidth is held nearly constant for all elevation angles (see Fig. 33-18) by a multiple-angle collimation scheme. Scanning, performed by a combination of switches (sector steps) and phase shifters (fine incremental steps), can emulate the uniform continuous motion of a mechanical-scan system (for compatibility with existing systems) or can be completely agile to support more advanced interrogation management schemes. To date, this antenna has not been widely deployed.

The array shown in Fig. 33-19 has been developed for tactical applications. ¹⁵ The 65° azimuth beam is scanned in increments of 5.6° using a modal Butler-matrix feed which excites all eight dipole columns. The SLS and monopulse functions share a difference-type pattern synthesized to provide backlobe coverage. All beams have the same elevation pattern with a high horizon cutoff rate.

The cylindrical array shown in Fig. 33-20 has been developed for shipborne IFF use. The directional beam, complemented by a stationary omnidirectional SLS beam, is positioned by a Lockheed-proprietary trimode scanner system. 16

Airborne Systems

To date, most IFF interrogators on airborne platforms have been for military use. Airborne interrogators have not seen wide use in civilian aviation.

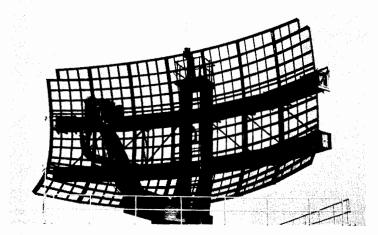


FIG. 33-14 ARSR-3 long-range surveillance radar antenna. (Courtesy Westinghouse Electric Corp.)

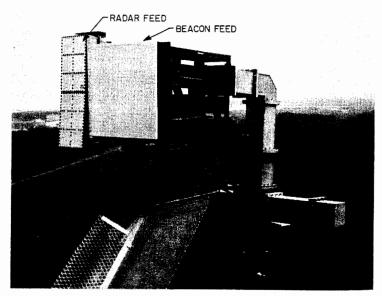


FIG. 33-15 Integral beacon feed for the ARSR-3. (Courtesy Westinghouse Electric Corp.)

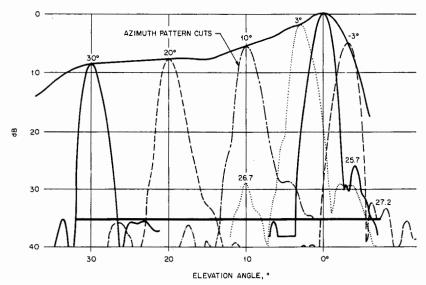


FIG. 33-16 Typical radiation patterns for the ARSR-3 beacon antenna. (Courtesy Westinghouse Electric Corp.)

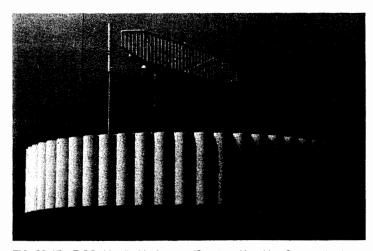


FIG. 33-17 E-SCAN cylindrical array. (Courtesy Hazeltine Corporation.)

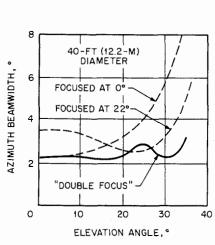


FIG. 33-18 Beamwidth variation of E-SCAN array versus elevation angle. (Courtesy Hazeltine Corporation.)

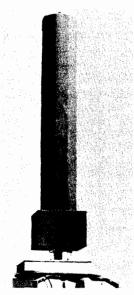


FIG. 33-19 Tactical IFF-ATM cylindrical array. (Courtesy Bendix Communication Division.)

Airborne IFF interrogators almost always have limited availability of aperture size. They are typically used in conjunction with a radar at X or Ku band. Figure 33-21 shows a typical implementation in which L-band dipoles for IFF are mounted on the surface of a radar reflector. The dipoles use resonant techniques to reduce scattering at the radar frequency. Use of thin dipole arms and baluns also reduces the effect on the radar.

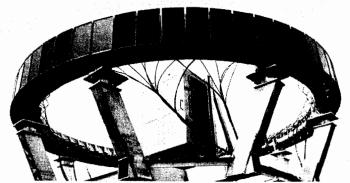


FIG. 33-20 Shipborne ATC-IFF cylindrical array AN/OE 120/UPX. (Courtesy Lockheed Electronics Co.)

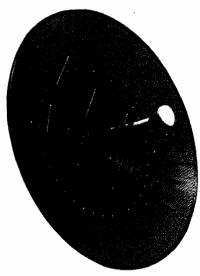
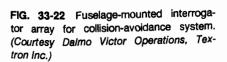


FIG. 33-21 IFF array for airborne fire-control radar. (Courtesy Hazeltine Corporation.)

Radar/beacon interaction is most easily controlled when the polarizations of the two systems are orthogonal. Because the beamwidth is always relatively large, beam sharpening using difference-pattern SLS is employed, with the power level for the difference pattern at nominally 9 dB above the sum pattern.

Other similar radar antennas have used cavity-backed L-band slots instead of dipoles. The slot apertures are flush with the reflector surface, and the slots and cavities are carefully tuned to maximize reflectivity at the radar frequency. Folded $\lambda/2$ slots in which the slots are very thin (width $<0.01\lambda$) have been found to be quite invisible to the radar.





IFF dipoles also have been added to "flat plate" radar antennas (planar arrays of waveguide slots). Thin, carefully tuned dipoles and orthogonal polarization are used to minimize interaction of the two systems.

The use of airborne interrogators on civilian aircraft has been investigated to provide traffic-alert and collision-avoidance information. To date, no such system has been deployed operationally. An experimental antenna for this purpose is shown in Fig. 33-22. This antenna can form either a directional beam or a notched beam in any one of eight azimuth directions. Using sidelobe suppression, the antenna is used to interrogate selected 45° sectors. The replies are received on multiple beams and are processed to provide 360° direction-finding capability with 8° rms accuracy. Top-loaded monopoles are used in this design to provide a low-drag antenna. Four monopoles spaced at approximately $\lambda/4$ are used. The dipoles are fed by a beam-forming network consisting of stripline couplers, diode switches, and phase shifters.

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Tracking Antennas

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34-1 Introduction 34-2
 Angle Estimation 34-2
 Tracking Techniques 34-3
 Choice of Tracking Technique 34-6

 34-2 Requirements 34-7
 Errors 34-7
 Error Budget for Reflector

Tracking Antennas
34-9
Error Budget for Phased-Array

Tracking Antennas 34-10
34-3 Electrical-Design Considerations
34-14

Aperture-Distribution Design 34-14

Feed Systems 34-15 Contributors to Pointing Errors 34-20

34-4 Mechanical-Design Considerations 34-25

Antenna Mounts 34-25
Mechanical Errors in Reflector
Tracking Antennas 34-26
Mechanical Errors in Phased-Array
Tracking Antennas 34-30

34-5 System Calibration 34-31
Calibration for Reflector Tracking
Antennas 34-32
Calibration for Phased-Array

Tracking Antennas 34-36

Tracking antennas are used in communications, direction finding, radio telescopes, and radar. The first three applications are covered in Chaps. 36, 39, and 41 respectively. This chapter is concerned with radar tracking antennas whose function is to provide accurate estimates of target location in two orthogonal angular coordinates. The reflector tracking antenna and the planar phased-array tracking antenna will be used for illustration.

Angle Estimation

Accuracy in estimating target direction is a fundamental requirement for the tracking antenna. It depends on systematic and random errors in the design of the antenna and mount, correction of these errors by calibration, and stability of the antenna and mount with respect to time. In addition, receiver linearity, the signal-to-noise ratio developed out of the signal processor, and the leads or lags in the difference-signal estimate, introduced by filters in the data processor, also affect the overall radar-system angular accuracy. Only the errors associated with the antenna and its mount are considered here.

Tracking a target requires a real-time feedback system that will direct the antenna beam to the target's angular direction when there is a difference* between the electrical reference direction, or boresight axis, and the actual target direction, as shown in Figs. 34-1 and 34-2.

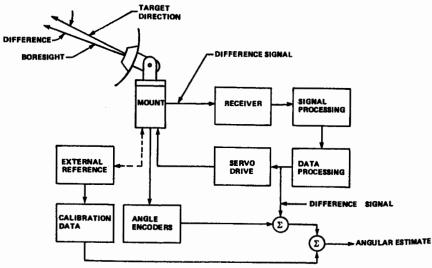


FIG. 34-1 Reflector-tracking-antenna system.

^{*}Although the term error has been used in much of the literature to describe this quantity, the term difference will be used in this chapter to avoid confusion when discussing errors in tracking-antenna output data.

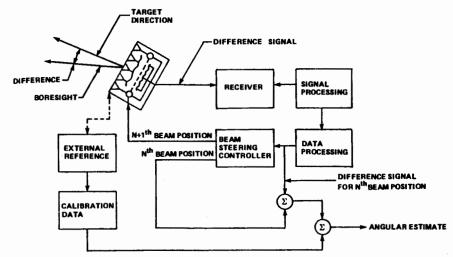


FIG. 34-2 Phased-array-tracking-antenna system.

The difference signal derived from the tracking antenna provides the information to drive the antenna boresight axis toward the target direction and also provides a correction factor in the angular estimate when boresight direction leads or lags target direction. A reflector-tracking-antenna system has an output that is the sum of its mechanical orientation, as measured by angle encoders, and the electrical-angle difference, derived from the location of the target with respect to the boresight axis. Both the mechanical position and the electrical-angle-difference data are corrected as necessary from calibration data. The phased-array tracking system provides an angle estimate that is the calibration-corrected sum of the beam-steering order, the electrical-angle difference developed between the boresight axis and the target direction, and the mechanical orientation of the array face.

Because of inertia, the reflector tracking antenna usually is limited to tracking a single target, although angle estimates may be made on several targets that are in the same beam as the target being tracked. The phased-array antenna can provide accurate angle estimates on a large number of targets at widely different angular spacing. The limitation on the number of targets that may be tracked by the phased-array tracking antenna is due not to the antenna itself but to the radio-frequency (RF) energy available, the amount of energy required to provide the accuracy of estimation for each target, and the dwell time required for each target.

Tracking Techniques

Two basic classes of tracking techniques are used to obtain the angular estimate: sequential-lobe comparison and simultaneous-lobe comparison. Both provide the magnitude and direction of the difference between target and beam position necessary to perform the tracking function. Although tracking involves the entire radar system, the type of tracking is defined by the method of sensing angular-difference magnitude and direction by the antenna.

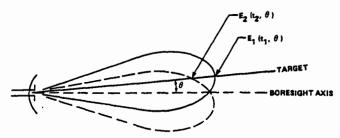


FIG. 34-3 Sequential-lobe comparison of squinted beams.

Sequential-Lobe Comparison Sequential lobe operates by displacing the antenna beam on successive transmissions and measuring the difference in relative signal strength, expressed by $\Delta = E(t_1, \theta) - E(t_2, \theta)$. The signal strength E is a function of both time t and angular position θ . The amplitude of the difference Δ indicates the magnitude of the angular difference, and the sign, positive or negative, indicates angular direction in the lobing plane.

Sequential lobing can be performed, as shown in Fig. 34-3, by using a single feed with symmetrical mechanical or electrical displacements from the boresight axis to give the two beam positions or by electrically or mechanically switching between two offset feeds.

Conical scanning is another sequential technique that can be used. One method is to use a feed that is electrically or mechanically displaced from the boresight axis. The feed maintains this displacement as it is nutated about the boresight axis.² A constant return occurs for a target on the boresight or mechanical axis, and a sinusoidal return occurs for a target that is off axis. The amplitude of the sinusoid indicates the magnitude of the difference between boresight axis and target position, and the feed position at peak response provides the angular direction of the difference. Conical scanning also can be accomplished by fixing the feed and rotating a tilted reflector, as is sometimes done in small tracking systems, or by electronically combining the outputs from a monopulse feed.

Because the sequential technique is time-dependent, changes in target-signal amplitude with time can modulate the difference signal. The influence of such amplitude fluctuations can be minimized by speeding up the beam switching or the conical-scan rate. Both the switching and the scan rates, however, are limited by the pulse-repetition period of the radar.

Simultaneous-Lobe Comparison Simultaneous-lobe comparison utilizes two different beams at the same time. Two identical beam shapes can be generated by using a reflector antenna and two feed horns that are symmetrically displaced from the boresight axis, as shown in Fig. 34-4. These "squinted" beams are identical to those received sequentially, but reception is simultaneous. Only a single signal channel following the antenna is required to make the difference estimate for sequential lobing, but two or more signal channels are required for simultaneous lobing.

If a microwave hybrid comparator is added to the feed network, a sum response, $\Sigma = E_1(t_1,\theta) + E_2(t_1,\theta)$, and a difference response, $\Delta = E_1(t_1,\theta) - E_2(t_1,\theta)$, are generated simultaneously as shown in Fig. 34-5a and b. Depending upon the comparator used, the Σ and Δ signals may occur in phase or in quadrature. If they occur in quadrature, a 90° phase shift is added to one of the signals to bring the signals in

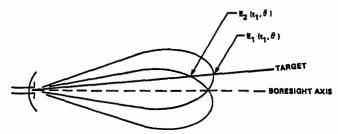


FIG. 34-4 Simultaneous-lobe comparison of squinted beams.

phase before comparison in a product detector. In the tracking technique referred to as amplitude monopulse,³ the product detector forms the vector dot product of the two normalized signals, $\Sigma/|\Sigma| \cdot \Delta/|\Sigma|$, as shown in Fig. 34-5c. Normalization often is obtained by using the sum signal for gain control of both the sum and the difference channels. Estimates out of the product detector are dependent only on the angle off axis and are independent of amplitude fluctuations of the target.

Certain objections exist to describing monopulse in terms of beams $E_1(t_1,\theta)$ and $E_2(t_1,\theta)$ because only the Σ and Δ beams are generated at the antenna ports. These expressions, however, serve as a convenient model for basic understanding. The term difference pattern resulted from taking the difference between the patterns of E_1 and E_2 .

The separation of the two feed horns in order to obtain an amplitude comparison introduces a small phase difference when the target is off the boresight axis. If the two feed horns are separated far enough on the same aperture or if two separate antennas on a common mount are used, then an estimate of the angle between boresight direction and target direction may be derived by comparing the relative phase of the two signals received simultaneously.³ In the dual-aperture implementation of this technique, known as phase-comparison monopulse, the two beams are pointed in the same direction rather than having an angular displacement, as in the amplitude-comparison

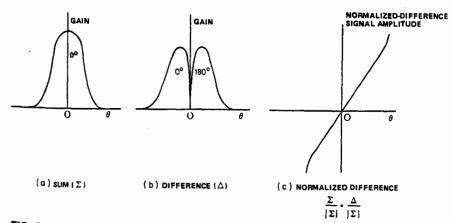


FIG. 34-5 Amplitude monopulse pattern and normalized difference-signal curve.



FIG. 34-6 Phase comparison.

method. For a target that is off axis, a phase difference occurs between the two signals, as shown in Fig. 34-6. This phase difference can be expressed as

$$\Delta \phi = \frac{2\pi}{\lambda} d \sin \theta \tag{34-1}$$

where d is the distance between antennas, λ is the wavelength, and θ is the angle between boresight and target direction. For small angles, $\sin \theta$ is equivalent to θ , and the phase difference may be used as a linear estimate of the difference between the boresight and target direction.

Choice of Tracking Technique

The investment required to design and fabricate a phased-array antenna and the limited time available in most systems point to the choice of monopulse as the tracking technique but does not preclude any other choice of technique. The monopulse technique provides Σ and Δ outputs that may be used either as an amplitude or as a phase monopulse system or, with specific orders to the beam-steering controller, for sequential lobing or conical scan.

For reflector systems, the choice is most often a trade-off between costs and accuracy. Monopulse was developed as a means of eliminating the scintillation or amplitude noise effects on tracking accuracy. Although targets with scintillation may be tracked with sequential-lobing systems, accuracy is considerably degraded, and very high scintillation may cause loss of track. This phenomenon has been the basis for radar-jamming techniques because the modulation that is introduced enables an enemy intercept receiver to readily interpret the type of radar and employ the jamming techniques to which the radar would be most vulnerable.

Consideration must be given to the gain and sidelobe levels achievable because both are influenced by the choice of tracking technique. There is an improvement in signal-to-noise ratio of 2 to 3 dB with monopulse for targets on or near the boresight axis compared with lobe switching or conical scan. Monopulse also can achieve lower levels of sidelobes than can conical scanning or other sequential-lobing methods because of the designer's ability to optimize separately the sum and difference patterns of a monopulse system.

In estimating the angular difference between target direction and the boresight axis, the standard deviation of the error in the estimate is inversely proportional⁴ to the slope of the normalized angular-difference signal:

$$\sigma_{A,E} = \frac{\theta_B}{K_m \sqrt{2 \cdot S/N}} \cdot \sqrt{1 + \left(K_m \frac{\theta}{\theta_B}\right)^2}$$
 (34-2)

where $\sigma_{A,E}$ = standard deviation in estimate of azimuth or elevation angular difference

 K_m = normalized monopulse difference slope

S/N = integrated signal-to-noise ratio

 θ_B = half-power, one-way sum-pattern beamwidth (scan-angle-dependent for phased arrays)

 θ = angle between boresight and target direction

Data in Skolnik³ show that monopulse has a difference slope potential greater than conical scan, and a more precise estimate of the angular difference may be made for the same beamwidth and signal-to-noise ratio.

Although the tracking technique of choice appears to be monopulse, sequential techniques can be used when cost is the major factor and if the targets are reasonably well behaved. The same accuracy can be achieved with sequential techniques as for monopulse for targets with high signal-to-noise ratios, low scintillation, and low dynamic performance. If the targets have considerable angle noise or glint, all techniques suffer in accuracy. The attributes of monopulse in such cases may not override the economical advantages of sequential scan.

34-2 REQUIREMENTS

In specifying tracking-antenna requirements, such parameters as gain, sidelobes, and losses are often secondary to accuracy and are specified at values that support the accuracy requirements. Accuracy is expressed in terms of the allowable angular error in each axis between the true target direction, with respect to tracking-antenna location, and the direction estimate derived from antenna pattern and mount data. The specified error is generally subdivided into a budget that identifies major contributors to the error and the size for each contribution.

Errors

The term *precision*, defined as "the quality of being exactly or sharply defined or stated," often is incorrectly substituted for the term *accuracy*, which is "the quality of correctness or freedom from error." Thus, a tracking antenna may be precise but not accurate, whereas an accurate tracking antenna must be precise.

In specifying error in each axis, the root-sum-square (rss) value of both residual systematic errors and random errors is used, although in error budgets individual errors are expressed in terms of root-mean-square (rms) values. In much of the literature, the term bias is substituted for systematic, and noise is substituted for random. In this chapter, the terms systematic and random will be used, and electrical noises due to thermal effects will be discussed as a subset of random errors.⁶

Systematic Errors A systematic error is a constant or a variable error that can be predicted as a function of antenna beam position, frequency of operation, or environmental factors. Such errors may be measured by calibration procedures and can be expressed as algorithms or in tables to correct antenna output data. Because only a finite number of measurements can be made, algorithms or tables developed for cor-

rection are approximations. Consequently, systematic residual errors remaining after data correction include error due to approximation or interpolation, error inherent in instrumentation, and error on the part of the observer. The rms value of each residual error for each contributor in each angular coordinate is the value given in the tracking-antenna error budget under systematic residual errors. The rms value of each error contributor and the rss value of the total are usually expressed in milliradians (mrad). Sometimes these values are expressed in millisines for errors that are a function of the scan angles in phased arrays. Care must be taken in summing error budgets so that the dimensions are not intermixed. In this chapter, values will be expressed in milliradians.

Random Errors The angular error due to thermal noise can be predicted on the basis of the known electromagnetic characteristics of the system. Maximum amplitude of backlash in data gearing or coupling to an encoder can be measured, but since it cannot be related to an angular position, it must be treated as a random error. Errors in a phased array due to phase-shifter quantization or rounding off in steering orders are also treated as random errors.

Random errors cannot be calibrated out of the system. They are grouped, and their rms values are squared and summed. The square root of this sum is the rss value for random error given in the antenna specification for each coordinate. The permitted error in each coordinate is the square root of the sum of the squares of total systematic residual and random errors. Though the process may be open to question from a strict mathematical interpretation, such procedures appear to be valid since measurements of targets of known trajectories and the use of regression analysis lead to similar estimates for the total error in each of the coordinates.

Thermal-Noise Errors Although the tracking error due to thermal noise is a component of the random errors, the fact that it may be the dominant error in the tracking-antenna system makes it of special importance. In Eq. (34-2), the standard deviation or error in the single-pulse angular estimate due to target noise at the boresight is inversely proportional to the square root of the signal-to-noise ratio. The signal-to-noise ratio from the radar-range equation is

$$S/N = \frac{P_t \cdot G_t \cdot A_r \cdot \sigma}{(4\pi)^2 \cdot R^4 \cdot k \cdot T_0 \cdot \Delta f \cdot \overline{NF} \cdot L_r \cdot L_p}$$
(34-3)

where P_t = peak power of transmitter

 G_t = gain of transmitted pattern (scan-angle-dependent in phased arrays)

A_r = effective receiving-aperture area (scan-angle-dependent in phased arrays)

 σ = target cross section

R = range of target

 $k = \text{Boltzmann's constant } (1.38 \cdot 10^{-23} \text{ J/K})$

 T_0 = temperature in degrees Kelvin (290 K reference)

 Δf = bandwidth of receiving channel

 \overline{NF} = noise figure of system

 L_r = ohmic and nonohmic receiving losses

 L_p = propagation losses (two-way)

The standard deviation of the target-angle estimate due to the signal-to-noise ratio is often used as a figure of merit for tracking radars and is also used to specify antenna performance. It is often used incorrectly in the literature to describe the accu-

racy of a radar system. This is correct only when thermal noise is the dominant error, for instance, when the radar tracks small targets at long ranges and available power and directivity limit the signal-to-noise ratio.

Relative Errors When the angular relationship between two or more targets within the same beam is estimated, then many of the systematic residual errors are common, i.e., correlated, and the error in the estimate is due only to uncorrelated residual systematic and random errors. In the case of phased-array tracking antennas, the relative error between two targets tracked by the same face, not necessarily within the same beam, is also reduced by those errors which are correlated over the sampling interval.

Error Spectrum Antenna systematic and random errors have frequency components that range between zero and the sampling rate used in tracking. To be able to fully predict antenna tracking performance, particularly for highly accurate systems, the correlation interval of each error in a tracking-antenna budget should be provided. As an example in a wideband phased-array tracking antenna, the monopulse estimate is random and occurs at the sampling rate, whereas the errors associated with time-delay switching are a function of the target trajectory and may be correlated over a large number of samples. Unless the error components are uncorrelated, a root sum square (rss) is not a valid summation. If the errors are partially or fully correlated over an interval, the estimate of the total error can best be accomplished by simulation.

Error Budget for Reflector Tracking Antennas

Such parameters as gain, frequency, bandwidth, and losses enter into the error budget by means of Eqs. (34-2) and (34-3). Requirements on sidelobes are generally specified to minimize multipath for instrumentation tracking systems and also to minimize sidelobe-jammer impact for tactical tracking systems. Barton⁷ points out that the difference-pattern sidelobes must be down by at least 27 dB when there is a ground-reflection coefficient of 0.3 so that the multipath return will be within a reasonable value to meet an overall accuracy requirement of 0.1 mrad.

Elements of the error budget that are electrical in nature are discussed in Sec. 34-3. Mechanical errors in the budget for an elevation-over-azimuth mount are discussed in Sec. 34-4.

Servodrive requirements for reflector-tracking-antenna systems usually are such that the torque available and the mechanical bandwidth of the antenna and mount are sufficient to keep a target of maximum dynamics well within the 3-dB sum-pattern beamwidth or within the linear region of the normalized difference signal. Because of the $\sqrt{1 + (K_m \theta/\theta_B)^2}$ factor of Eq. (34-2) and because of cross-polarization errors to be discussed later, it is desirable to track the target as near the boresight as possible.

A typical error budget for azimuth and elevation for a highly accurate reflector tracking antenna is given in Tables 34-1 and 34-2. The first column in each table gives the systematic residual errors after calibration. The second column indicates random errors that cannot be reduced by calibration. Both columns represent figures obtainable under favorable conditions, including a firm foundation to which the antenna mount is attached. The systematic residual errors are primarily a function of the calibration procedure, the capability of the observer, and the stability of the system. If the environment changes, the systematic residual errors will change, and recalibration should be initiated.

Error Budget for Phased-Array Tracking Antennas

Many of the mechanical errors associated with the determination of the tracking axis of a reflector antenna are also present in determining the direction of the normal to the array face. In addition, the phased array has errors associated with the angular displacement of the boresight axis from the direction of the array normal by means of electronic scanning. These latter errors are both dependent and independent of the amount of the displacement commanded by the beam-steering controller. However, the variation in the systematic dependent errors with scan can be accommodated in the calibration process. The measurement process by which these and the independent errors are determined is not dependent upon the scan angle, and therefore the systematic residual error remaining after the scan-dependent systematic error is corrected is independent of scan angle.

The reference system for a phased-array tracking antenna is shown in Fig. 34-7. The array face is in the X, Y plane with the Z axis as the normal to the array. The angle α defines the direction of the boresight position, or difference-pattern null, with respect to the X axis, while the angle β defines the direction of the boresight position with respect to the Y axis. On the Z axis, $\alpha = \beta = \pi/2$. The input to command the direction of the boresight position is given as α_i and β_i . The error in boresight direction is then $\alpha - \alpha_i$ and $\beta - \beta_i$.

The signals received in the monopulse difference channels are voltages V_{α} and

TABLE 34-1 Reflector-Tracking-Antenna Azimuth Error Budget, 0–85° Elevation

Contributor*	Systematic residuals, mrad rms	Random, mrad rms
Azimuth-axis tilt	0.02	
Azimuth encoder to true north	0.03	0.01
Optical-elevation-axis nonorthogonality	0.02	
Elevation-azimuth-axis nonorthogonality	0.02	
Depth of null, 10° rms postcomparator error		0.02
Optical-RF-axis collimation	0.02	
RF-elevation-axis nonorthogonality		
Mechanical	0.02	
Electrical (frequency)	0.02	
RF axis to target position	0.02	Eq. (34-2)†
Cross-polarization		0.04
Wind	0.02	0.02
Thermal-mechanical	0.02	
rss‡	0.065	0.05

^{*}Described in Secs. 34-3 and 34-4.

[†]Exclusive of S/N, multipath, and refraction.

^{*}See the subsection "Error Spectrum."

TABLE 34-2 Reflector-Tracking-Antenna Elevation Error Budget, 0–85° Elevation

Contributor*	Systematic residuals, mrad rms	Random, mrad rms
Azimuth-axis tilt	0.02	
Elevation encoder to true vertical	0.02	0.01
Depth of null, 10° postcomparator error		0.02
Optical-RF-axis collimation	0.02	
RF-axis mechanical droop	0.02	
RF axis to target position	0.02	Eq. (34-2) [†]
Cross-polarization		0.04
Wind	0.02	0.02
Thermal-mechanical	0.02	
rss‡	0.051	0.050

^{*}Described in Secs. 34-3 and 34-4.

 V_{β} , representing the difference between the direction cosines (cos α , cos β) of the boresight axis and the target direction relative to the X and Y axes in the plane of the array. These differences are added to the commanded boresight-direction cosines (cos α_i , cos β_i) along with calibration data to form an estimate of the direction cosines of the target direction relative to the array-normal direction. The direction angles of the target are then combined with the direction of the array normal to estimate the direction

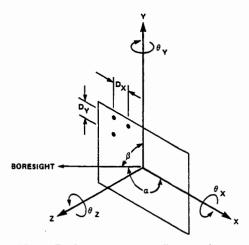


FIG. 34-7 Phased-array coordinate system.

[†]Exclusive of S/N, multipath, and refraction.

^{*}See the subsection "Error Spectrum."

tion of the target in earth-reference coordinates. By using these angles with target ranges, target position may be calculated in a rectilinear system. Predictions are then made as to the next target position. Target direction is transformed back from earth-reference to array-reference coordinates and into the α_i and β_i orders for the next beam position. The orders take into account the frequency of operation and temperature of the array.

Although thermal-noise error is not measured directly during alignment and calibration, the normalized slope of the difference patterns must be measured to estimate that error. Thermal-noise error can be estimated by Eq. (34-2) if it is interpreted to be the standard deviation in the direction cosine of the target direction and the parameters θ_B and K_m are those for the monopulse beam steered normal to the array ($\alpha_i = \beta_i = \pi/2$). In this direction the meaning of Eq. (34-2) is the same for a reflector antenna and for a phase-steered array. This estimate of error can be converted to angle measure by dividing by the square of the cosine of the angle off the array normal ($C^2 = 1 - \cos^2 \alpha - \cos^2 \beta$) for use in Table 34-4. By energy management of the phased array, that is, by making the power available proportional to $1/C^5$, the thermal-noise error is also made independent of scan angle. The fifth power term is a function of the two-way beamwidth, array factor, and mutual coupling. Other random errors dependent on scan angle are converted to angle measure by dividing by the cosine of the angle off the array normal (C).

TABLE 34-3 Phased-Array-Tracking-Antenna Array Face to Reference Error Budget

Contributor*	Systematic residuals, mrad rms	Random, mrad rms
Array face to true-north		
Alignment/calibration	0.3/cos <i>ψ</i>	
Wind	0.1	0.1
Thermal	<0.1	
Tilt		
Alignment/calibration	0.1	
Wind	0.1	0.1
Thermal	<0.1	
Rotation		
Alignment/calibration	< 0.1	
Thermal	<0.1	

^{*}Described in Sec. 34-4.

TABLE 34-4 Phased-Array-Tracking-Antenna Array Face to Target-Position Error Budget $[\pi/6 \le (\alpha \text{ or } \beta) \le 5\pi/6; \cos^2 \alpha + \cos^2 \beta \le 0.75]$

Contributor*	Systematic residuals, mrad rms	Random,
Beam command to boresight		
Position $(\alpha - \alpha_i, \beta - \beta_i)$		
Uncorrelated illumination		0.2/C
(phase-shifter		
quantization, phase-		
shifter roundoff, phase-		
shifter insertion, rf path		
insertion, array element		
position, radome)		
Precomparator and	0.1	
postcomparator phase		
(depth of null)		<0.05/C
Cross-polarization (cross coupling)		<0.05/C
Frequency	0.1	
Thermal	0.1	
RF axis to target position	0.1	Eq. (34-2)/C ^{5/2†}
rss‡	0.20	

^{*}Described in Secs. 34-3 and 34-4.

Just as for the reflector tracking antenna, the gain, frequency, and beam-switching time are specified at levels that support total system requirements with the error budgets to be met under the environment specified. Receiving sidelobe levels in a tactical phased array are generally dictated by anticipated jamming levels rather than by multipath requirements. An illustrative budget for a ground-based tactical system is given in Tables 34-3 and 34-4. The budget is for an array of equal dimensions in X and Y. Otherwise Table 34-4 should be broken into separate α and β tables.

It will be noted that the major error contributor is in the α plane. As indicated in Sec. 34-4, this is due to the use of a north-seeking gyro to provide the reference direction and make the tactical phased array independent of an external reference. The use of an external reference such as employed for the instrumentation reflector tracking system (Sec. 34-5) can reduce this error.

Neither of these phased-array tracking-antenna budgets should be assumed to be the limit in the accuracy achievable. The current state of the art should permit reduction of the total instrumentation error to less than $50\,\mu\text{rad}$ with respect to an external reference and to less than $20\,\mu\text{rad}$ when estimating one target's position relative to another. It should be noted that if the external reference can be tracked, then the relative-error value is applicable. As indicated in the subsection "Error Spectrum," the correlation interval of each error should be known in order to correctly estimate the total error.

[†]Exclusive of S/N, multipath, and refraction.

^{*}See the subsection "Error Spectrum."

34-3 ELECTRICAL-DESIGN CONSIDERATIONS

Aperture-Distribution Design

A monopulse pattern is a set of two or more patterns, formed simultaneously, that provides both the angular position and the signal-characteristic data from a source. Generally, the aperture distribution for one of these beams, designated the Σ , or sum, beam, will be designed to maximize the gain of the antenna in the principal direction while meeting sidelobe objectives in other directions. The aperture distributions for the other beams, designated Δ , or difference, beams, will be designed to produce a null response along one of two perpendicular planes* intersecting in the boresight-axis direction, to maximize the slope of the response with increasing angle away from the null plane in a direction normal to the plane, and to satisfy gain and sidelobe-level objectives in other directions. The design considerations governing the sum beam, such as gain, beamwidth, and sidelobe level, are similar to those of other antenna requirements. These have been covered adequately elsewhere in this handbook. In this section we will consider the special requirements of the difference beams in a monopulse cluster.

A measure of performance of the difference pattern is its slope at the central null. This slope may be normalized in at least two ways. The first, the difference slope K, refers only to the difference pattern. It is the slope of the pattern at the boresight null when the excitation is adjusted to radiate unit power relative to the response of a uniform aperture of the same size. In general terms,

$$K = \frac{\frac{\partial}{\partial u} \iint d(x,y) e^{-jk(ux+vy)} dxdy | u, v = 0}{\sqrt{A \iint d^2(x,y) dxdy}}$$
(34-4)

or

$$K = \frac{-jk \iint x d(x,y) \ dA}{\sqrt{A \iint d^2(x,y) \ dA}}$$
 (34-5)

where $u(\cos \alpha)$ and $v(\cos \beta)$ are the direction cosines of the observation or target direction, $k = 2\pi/\lambda$, and d(x,y) is the excitation aperture distribution.

The difference slope is maximized when the aperture has an odd linear distribution of illumination amplitude. The exact value of the slope depends upon the shape of the aperture. Two special values of K are of interest for reference purposes. For odd linear difference illumination, the difference slope for a rectangular aperture is

$$K_s = \pi/\sqrt{3}$$
 V/V/SBW

and for a circular aperture is

$$K_r = \pi/2$$
 V/V/SBW

where K_s is K times the standard beamwidth of the aperture (SBW), in radians (equal to the wavelength divided by the width of the antenna). These maximum-slope functions are seldom used in practical tracking systems because of the high sidelobe levels, -8.3 dB for the rectangular aperture and -11.6 dB for the circular aperture. The

^{*}For a phased array, these planes become conical surfaces about perpendicular axes in the array face.

aperture distributions (given by Taylor⁸ for the sum pattern and by Bayliss⁹ for the difference pattern), which maximize gain or slope for a given sidelobe level, are more practical models in designing aperture illumination for a monopulse tracking antenna. Approximate values for the difference slope K_r , derived from the Bayliss distribution for a square aperture, are given in Fig. 34-8.

The second way to normalize the difference slope, generally preferred in the literature of radar systems, is known as the normalized monopulse difference slope K_m , referred to in Sec. 34-2. This difference slope is derived from the difference slope K by normalizing the difference voltage to that of the sum beam and normalizing the angle to the half-power beamwidth (HPBW) of the sum beam. Thus,

$$K_m = K \frac{\theta_B}{\sqrt{\eta_{\rm P}}} \tag{34-6}$$

where $\theta_B = HPBW$ of sum beam

 η_{Σ} = efficiency factor for sum beam, including only aperture illumination, spillover, and blockage

Feed Systems

The feed system distributes the RF excitation over the aperture and establishes the level of excitation at each point in the aperture. The special feature of the monopulse feed is its ability to establish three orthogonal distributions of excitation simultaneously.

A feed is constrained when the excitation proceeds from a beam port through a branching transmission line or waveguide network to the individual elements of the radiating aperture. Space feeds, or optical feeds, are those feed systems that employ

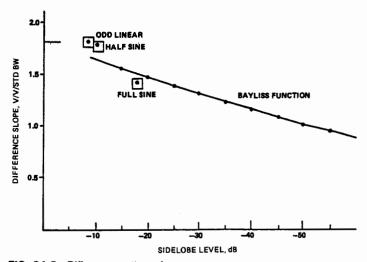


FIG. 34-8 Difference-pattern slope.

a few elements, in a primary feed system, that radiate RF excitation to be intercepted and collimated by a larger secondary aperture. In this subsection, the term *optical* feed is used for this class of feed.

Constrained Feed Systems for Phased Arrays The simplest kind of monopulse feed system for a tracking array is formed by dividing the array into equal quadrants, as illustrated in Fig. 34-9. The sum of all four quadrants forms the sum beam, and the difference between the sums of the top pair and the bottom pair forms an elevation difference beam. The sum of the left pair is subtracted from the sum of the right pair to form the azimuth difference pattern. A fourth orthogonal beam, sometimes called the Q beam, can be formed by taking the difference of the differences between the quadrants. This beam is usually terminated in a matched load to prevent signals received off axis from being reflected into a difference channel.

This simple feed system does not allow for sidelobe-level optimization or errorslope optimization among the three beams of the monopulse cluster. Large tracking array antennas will usually employ a feed system that will allow independent optimization of the sum-and-difference-beam illumination.

Feed systems that provide sufficient degrees of freedom to allow independent optimization of the monopulse aperture distributions must take full advantage of the symmetry inherent in these distributions. Array elements or subarrays equally displaced from the monopulse axes in the array face all receive the same excitation amplitude for any given function, differing only in the pattern of phase (algebraic sign) for the different beams. A network similar to that shown in Fig. 34-9 can be used to connect symmetrically located elements or subarrays. This circuit is illustrated in Fig. 34-10. The sum ports of these may be combined to provide the array sum illumination distribution. The elevation difference ports may be independently combined to optimize the elevation difference pattern, and similarly the azimuth difference pattern may be independently optimized.

An alternative arrangement that simplifies the feed network with some loss of independence in design of the illumination function is shown in Fig. 34-11. This net-

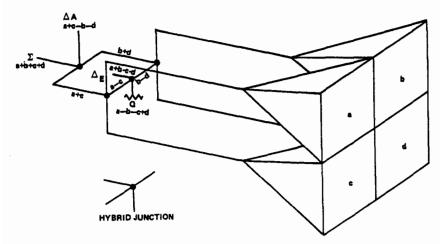


FIG. 34-9 Simple monopulse feed.

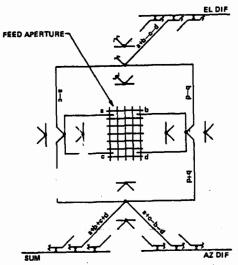


FIG. 34-10 A feed network providing complete independent control of the sum and both difference illumination distributions.

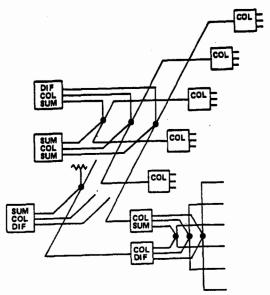


FIG. 34-11 Row-column-array monopulse feed.

work allows complete independence for the elevation difference pattern, but the column sum distribution is shared between the sum and azimuth difference distributions. Because the column functions of these two distributions are similar, a compromise design based upon this sharing has little impact on the array pattern.

A row- or column-oriented feed network, subject to the compromise described for the alternative parallel feed, can be implemented with a serial monopulse ladder network as shown in Fig. 34-12. This network can be used in place of the column network or the row network, or both. There does not appear to be a generally applicable choice between these feed types, so that both types must be considered for the requirements of a specific tracking antenna.

Optical Feed Systems The design of a monopulse feed system for an antenna with optical magnification, such as a reflector, a lens, or a transmission lens array, is complicated by the fact that there are two apertures to consider, the main aperture and the feed aperture. Feed apertures differ for the different beams, and there are fewer degrees of freedom available for aperture-distribution control. Optical monopulse feed systems are excellent examples of the art of design compromise.

The design of a monopulse optical feed, as also the design of a single-beam optical feed, involves a careful balance of aperture illumination efficiency, spillover efficiency, and, in case of a feed for a reflector antenna, blockage. The monopulse feed design is complicated by the need to balance the requirements of the difference beams with those of the sum beam. The optimization of the difference feed differs from that for an array. Spillover efficiency for an optical feed is poor for an odd linear distribution, giving it a smaller angular sensitivity than a distribution that results from placing a greater part of the primary (feed-system) difference pattern on the focusing aperture. The optimum size of the difference feed is larger than the optimum size of the sum feed. Hannan¹⁰ suggests that the linear dimension of the optimum difference aperture, in the plane of the difference pattern, is twice that of the sum pattern. Thus, an optimum monopulse feed may have 3 to 4 times the aperture area of an optimum single-beam feed for the same optics. As a result, a monopulse feed will have substantially larger aperture blockage than the optimum single-beam feed.

The performance of a conventional four-horn monopulse feed is poor because it requires a compromise between optimum size for sum-beam performance and for difference-beam performance. Several configurations that provide additional freedom to improve monopulse feed performance include both multibeam and multimode feeds

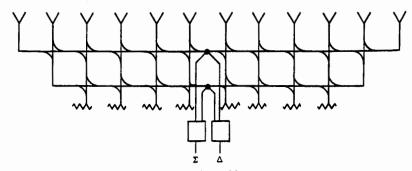


FIG. 34-12 Center-fed serial monopulse ladder network.

FEED EXCITATION	SUM		AZ DIF		EL DIF	
WITH $(\frac{aA}{2\lambda F})$ AND $(\frac{bB}{2\lambda F})$ FOR MAXIMUM SUM GAIN	GAIN	SPILLOVER EFFICENCY	SLOPE	SPILLOVER EFFICENCY	SLOPE	SPILLOVER EFFICENCY
\$ Az E! \$ AZ E!	.58	.66	.943	.28	.87	.24
7,7100	(a) FOUR-HORN					
AZ AZ S AZEI	.75	.84	1.23	.50	1.00	.31
€ □00₽	(b) TWO-HORN DUAL-MODE					
• .41 EI Az • .41 SAzEI	.75	.83	1.47	.80	1.00	× .31
1.39	(c) TWO-HORN TRIPLE-MODE					
SAZEI	.58	.66	1.29	.63	1.22	.62
1.42	(d) TWELVE-HORN					
• ,41 EI AZ S AZ EI	.75	.83	1.47	.80	1.36	.78
1,39	(e) FOUR-HORN TRIPLE-MODE					

RATIO OF MODE AMPLITUDES

FIG. 34-13 Monopulse feed characteristics. (After Ref. 10.)

(see Fig. 34-13). The multihorn feeds have network configurations similar to monopulse phased-array networks. For both multibeam and multimode feeds, the increased design complexity requires an increase in the minimum electrical size of the feed, making them more appropriate for large f/D optics.

Figure 34-13, which follows Hannan, represents comparative performance parameters of different feed configurations that are optimized on the basis of a collimating aperture of a rectangular cross section with dimensions A by B, located at a distance F from the feed aperture of dimensions a by b. The spillover efficiency given in this figure is the ratio of the energy radiating from the feed aperture intersecting the collimating aperture to the total energy radiated by the feed in that mode. A major source of the improved performance of the more complex multihorn and multimode feeds is the reduction of spillover loss in the difference beams.

The multimode feed combines the network simplicity that is characteristic of the four-horn feed with the greater design freedom of the multihorn feed. A multimode feed uses several waveguide modes in combination to achieve a desired aperture illumination. A single mode with odd symmetry is used for the monopulse difference function. The sum-beam illumination is usually achieved by using a linear combination of two different modes, each with even symmetry. This has the desirable effect of substantially increasing the primary-pattern beamwidth and thereby improving aperture illumination efficiency at the reflector. Since two modes of different orders will have different velocities of propagation, they can be held in the proper phase relationship at the aperture over only a limited bandwidth. In practice, however, multimode feeds often compare favorably in bandwidth with more complex multihorn feeds.

EI - ELEVATION

Az - AZIMUTH

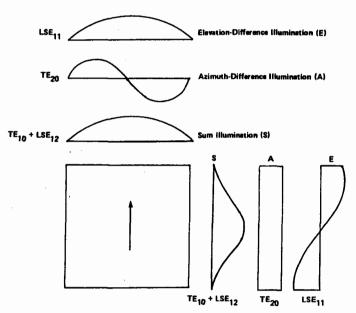


FIG. 34-14 Single-horn multimode feed-aperture distribution.

An example of a dual-polarized multimode design is shown in Fig. 34-14. This feed makes use of two waveguide modes, the TE_{10} and the LSE₁₂ modes, to form the sum-beam illumination. The azimuth difference-beam illumination uses the TE_{20} , and the elevation difference-beam illumination uses the LSE₁₁ mode. These feed-aperture illumination distributions are illustrated in Fig. 34-14. The bandwidth of the multimode feed is limited by the difference in phase velocity between the TE_{10} and LSE₁₂ modes forming the sum distribution. This feed design generates the LSE₁₂ mode in phase opposition with the TE_{10} . The length of the tapered horn section is then set by the requirement to provide a 180° differential phase shift between these two modes.

Contributors to Pointing Errors

Defects in an antenna feed system as it affects the sum-beam performance, measured by such factors as gain, beamwidth, and sidelobe level, are treated elsewhere in this handbook. Defects that affect the tracking performance of a monopulse feed system are considered here. Included in this subsection are those errors in the distribution of illumination over the antenna aperture that have relatively little correlation in the aperture. When the error* locations in the aperture are separated by more than a few wavelengths, they often can be considered independently of other errors. Errors that are correlated over the entire part of the aperture, served by one port of the comparator, are treated as precomparator and postcomparator errors. Finally, the dependence

^{*}Error as used here is that phase or amplitude error in the final aperture illumination function which contributes to the beam null shift or pointing error in Tables 34-1, 34-2, and 34-4.

of monopulse angle estimation on the polarization of the received signal will be considered. The effect of these illumination errors is an apparent shift in the position of the difference-pattern null, or a boresight shift, and a change in the relative slope of the difference pattern, or a gain shift, which may vary with frequency, time, temperature, or other environmental factors.

Uncorrelated Illumination Errors The effects of uncorrelated phase errors must be considered in the design of a tracking antenna, whether for specifying either reflectorsurface tolerance or allowable element errors in a phased array. A distribution of phase errors $\xi(x,y)$ across the aperture will produce a voltage V_e that is proportional to

$$\iint \xi(x,y) \ d(x,y) \ dA \approx V_{\bullet}$$

which to the first order of approximation is in phase with the difference voltage which would exist in the absence of uncorrelated errors. This voltage may be divided by the difference slope in Eq. (34-5) to determine the shift in the apparent position of the difference-pattern null:

$$\Delta u = \frac{\iint \xi(x,y) \ d(x,y) \ dA}{k \iint x d(x,y) \ dA}$$
 (34-7)

This expression is valid for an arbitrary distribution of any correlation interval across the array, including such periodic phase errors as those resulting from phase quantization errors in some beam-steering equipment.

The specific distribution of phase errors in the difference-pattern illumination for an antenna often is unknown, but we can infer by means of specification or measurement the statistics of such distributions that are averaged over an ensemble of similar antennas. The null shift given in Eq. (34-7) can be treated as a random variable, and the expected value of the null shift is dependent upon the distribution of the expected value of the phase error at each point in the aperture:

$$\overline{\Delta u} = \frac{\iint \overline{\xi}(x,y) \ d(x,y) \ dA}{k \iint x d(x,y) \ dA}$$
 (34-8)

Usually the phase error, and therefore the null shift, will have a zero mean (expected) value. If the error distribution is such that the rms phase error σ (radians) is the same for every independent uncorrelated region of the antenna, the rms of the null shift (boresight) error is

$$\sigma_u = \frac{\sigma}{K\sqrt{N_e}} \tag{34-9}$$

where N_e is the effective number of uncorrelated independent regions in the aperture with that phase-error statistic. If the antenna is a phased array and the statistic refers to phase errors that are independent from element to element, then N_e is just the total number of elements in the array. If the phase errors are attributable to some higher organizational level in the array, N_e is the number of components in that level.

Nester¹¹ has shown that, for practical ranges of error values, the phase error has the predominant effect on null shift. He has also shown the changes in the error slope due to phase and amplitude errors. These are second-order because both the position of the target off boresight and the error in the normalized difference slope are small, independent random variables.

Equation (34-9) is useful in providing an estimate of the pointing error for a specified

level of rms phase errors in designing a phased-array antenna. After fabrication, at a given frequency and temperature of operation, each beam position has a fixed pointing error associated with it. The pointing error is a systematic error which theoretically could be calibrated out. The illumination error distribution also may have a component due to a setability error in the phase shifters that is dependent on scan. Although such errors may be removed by calibration at the element level, the computational effort makes this approach unattractive for arrays of more than a few elements.

For wideband phased-array radars, a potential major source of pointing error is the phase error associated with time-delay units. With the relatively small number of these units, such pointing errors can be reduced by calibration at the time-delay-unit level.

Tracking antenna systems are utilized to provide estimated angular position, rates, and accelerations. Equation (34-9) is time-independent and should not be used as an error factor in such estimates without clearly stating the angular correlation period, i.e., the minimum angular step with the phase shifters, or, in wideband phased-array antenna systems, the maximum scan without a switch in a time-delay unit. The phase shifters' phase error is correlated over a beamwidth, and the time-delay units' phase errors are correlated over the beam-pointing positions available before time-delay switching is required.

The time-delay-unit phase error has the greatest potential for producing the largest errors, as compared with other errors in the antenna, in angular position, rate, and acceleration estimates. For highly accurate systems, reduction of the error through design and calibration is required.

Correlated Illumination Errors The illumination error distribution associated with the feed system of a phased-array antenna is invariant with scan. This correlated illumination error results in a systematic pointing error that can be significantly reduced by calibration. There is also the potential for an illumination error distribution caused by thermal distortions that would nominally be invariant with scan but can change with temperature. Consequently, calibration should be performed with the system at operating temperature. The thermal time constant of tactical phased-array antennas needs to be considered to achieve maximum angular accuracy.

Precomparator and Postcomparator Errors The accuracy of the monopulse estimation of target location is influenced by both precomparator and postcomparator errors. Precomparator errors affect the symmetry of the patterns, producing a modified sum-pattern error in the difference beam and a modified difference-pattern error in the sum beam. If the modified sum-pattern error is in phase with the difference pattern (resulting from a precomparator phase error), a shift in the angle of the difference null will be observed. If the modified sum-pattern error is in quadrature with the difference pattern, no shift will occur in difference-pattern-null location, but the depth of the null will be reduced. Techniques employed to improve effective null depth make use of the relative phase between the signals from the sum and the difference channels. These techniques make the monopulse performance near the null sensitive to postcomparator phase error in the presence of quadrature precomparator error. The relation between these error sources depends both upon the microwave network employed and upon the technique used in the signal processor to extract angle information.

An example is given in Fig. 34-15 of the phase errors in a monopulse feed system

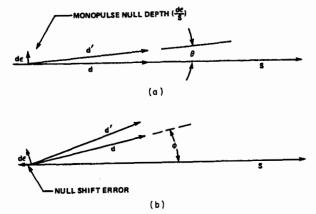


FIG. 34-15 Monopulse comparator phase errors. (a) Precomparator phase error. (b) Precomparator and postcomparator phase error.

when the difference-pattern error d_i is in quadrature with the difference pattern d_i . Figure 34-15a illustrates the situation in which no postcomparator phase error exists; d_i is a phasor slowly varying with the angle to the source, while d varies linearly (approximately) with the source angle. In this instance, the ratio

$$\frac{d'\cos\theta}{s} = \frac{d}{s} \tag{34-10}$$

is the best estimator of the source angle. In Fig. 34-15b, the effect of the postcomparator phase error ϕ is illustrated. Here, the estimator of source angle

$$\frac{d'\cos\left(\theta+\phi\right)}{s}=\frac{d}{s}\frac{\cos\theta\cos\phi-\sin\theta\sin\phi}{\cos\theta}\tag{34-11}$$

will produce a shift in the apparent null position (boresight) such that

$$e_{dn} = \frac{\theta_B}{K_m} \frac{d}{s} = \frac{-\theta_B}{K_m} \frac{d_s}{s} \tan \phi \qquad (34-12)$$

Precomparator errors that are in phase with the difference pattern produce a null shift error in source-angle prediction. Postcomparator errors produce a null shift error if precomparator errors are in quadrature with the difference pattern. Design or alignment action to reduce these errors depends upon identifying the source of the phase error. Determining the behavior with frequency will often help with this identification. When the alignment has reduced this error to an acceptable level, it may be further reduced by calibrating and correcting the observed angle data. The boresight error due to this source will be a function of frequency.

Cross-Polarization Angle Crosstalk The normalized output voltage from the two difference channels of a monopulse feed can be related to the displacement of the target from the RF axis of the antenna by the matrix equation

$$\begin{bmatrix} V_{u} \\ V_{v} \end{bmatrix} = \begin{bmatrix} K_{uu} & K_{uv} \\ K_{vu} & K_{vv} \end{bmatrix} \Delta u$$

$$\Delta u$$

$$\Delta v$$

$$\Delta v$$

$$\Delta v$$

where the main diagonal terms are the difference slope coefficients from Eq. (34-2), and the cross-diagonal terms are cross-coupling terms due to nonorthogonality between the monopulse null planes (or cones). These coefficients are generally a function of frequency and of the relative polarization of the received signal. If the receiving system does not sense the polarization of the incoming signal, this cross-polarization angle crosstalk represents an uncorrected error in the angle estimate, which can result in loss of track.^{12,13}

An example of the difference-voltage equation applied to the elevation-over-azimuth pedestal can be obtained by means of coordinate conversions:

$$\Delta v = \Delta E$$
$$\Delta u = \cos E \, \Delta A$$

giving

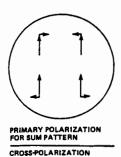
$$\begin{bmatrix} V_u \\ V_v \end{bmatrix} = \begin{bmatrix} K_{uu} \cos E & 0 \\ 0 & K_{vv} \end{bmatrix} \Delta A$$
 (34-14)

when no angle crosstalk occurs and perfect alignment exists between the RF null planes and the pedestal coordinate planes. The angle estimates in pedestal coordinates are obtained by inverting the matrix, giving the relation

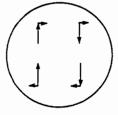
$$\Delta A \\ \Delta E$$
 =
$$\begin{bmatrix} 1/(K_{uu} \cos E) & 0 \\ 0 & 1/K_{vv} \end{bmatrix} V_u$$
 (34-15)

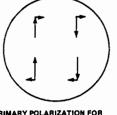
The cross-polarization angle crosstalk is a consequence of the polarization characteristics of the feed system. It tends to be most pronounced in optical feed systems but is also present in small phased-array antennas. Crosstalk is not observed in large arrays.

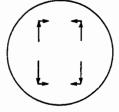
A classic explanation of cross-polarization crosstalk is derived by considering the feed for a reflector antenna with polarization characteristics identical to that of a linear electric dipole. The electric vector at the surface of the reflector will be directed along the intersection of the parabolic surface and the plane containing the feed dipole axes and a point on the reflector surface. The copolarization of the antenna is determined by the plane through the feed dipole and the vertex of the reflector. Most of the energy collimated by the reflector is polarized parallel to the principal polarization at the vertex, but each quadrant of the reflector aperture has a cross-polarized component of excitation. \(^{14}\) During sum-beam excitation, the phase of this cross-polarized energy alternates from quadrant to quadrant, as shown in Fig. 34-16, producing a cross-polarized Q beam. In the principal polarization elevation difference beam, the cross-polarization response is that of an azimuth difference pattern. Thus, a cross-polarized source displaced in azimuth would drive the beam in the elevation direction. The same situation occurs in the principal polarization azimuth difference beam, in which the cross-polarized response is that of an elevation difference pattern.



PRODUCES C-BEAM PATTERN







PRIMARY POLARIZATION FOR AZIMUTH-DIFFERENCE PATTERN

PRIMARY POLARIZATION FOR ELEVATION-DIFFERENCE PATTERN

CROSS-POLARIZATION PRODUCES
ELEVATION-DIFFERENCE PATTERN

CROSS-POLARIZATION PRODUCES AZIMUTH-DIFFERENCE PATTERN

FIG. 34-16 Cross-polarization crosstalk electric dipole feed on parabolic reflector.

If this feed were to be used as an optical feed for a planar transmission lens array, no such cross-polarization effect would be observed. This source of crosstalk depends upon both the feed polarization and the surface of the focusing element. Koffman¹⁵ has determined the "ideal" feed polarization for each type of surface derived from a conic section by showing that, in general, the strength of the electric dipole polarization should equal the strength of the magnetic dipole polarization, multiplied by the ellipticity of the focusing surface. Thus, a magnetic dipole is optimum for a sphere, an electric dipole is optimum for a plane, and a Huygens source (having equal electric and magnetic dipole strength) is optimum for the paraboloid.

Optical polarization conversion, however, is not the only source of crosstalk; it can arise because of cross coupling in the feed itself. An example of this effect in a five-horn monopulse antenna has been studied by Bridge. 16 The particular feed he investigated was designed for dual polarization and had a direct circuit for measuring the coupling or isolation between the polarizations in the monopulse network.

Multimode feeds are particularly susceptible to cross-polarization crosstalk because the relatively large size of the single aperture can support higher-order crosspolarized modes, and the feed system usually will excite them unless particular care is exercised. Multiple-aperture, single-polarization feeds may exhibit some relatively low-level cross-polarization because of edge diffraction (if we assume that the individual apertures will support only one polarization). This source of angle crosstalk becomes negligible as the size or number of apertures in the feed array becomes large.

34-4 **MECHANICAL-DESIGN CONSIDERATIONS**

Antenna Mounts

The mount not only must support the antenna and direct it in angle but must accurately provide that direction under dynamic conditions that are introduced by target and/or antenna-mount-platform motion or stress that is introduced by wind. The requirements on the mount are interdependent with the requirements on the antenna. The mechanical bandwidth of the tracking antenna as well as its mount depends upon the resonance characteristics of the antenna structure and its mount as well as upon the coupled resonance. A discussion of bandwidth and design of servo systems to drive tracking-antenna systems is given by Humphrey. 17

Many reflector tracking antennas use the mount of Fig. 34-21 below, though tracking coverage in this mount is limited near zenith. For a target (see Fig. 34-17)

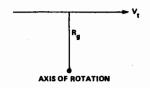


FIG. 34-17 Target geometry.

traveling normal to the line of sight and perpendicular to the axis of rotation of a tracking antenna at a ground range R_s and velocity v, the angular velocity of the tracking antenna reaches v/R_s . The acceleration about the azimuth axis of rotation reaches a value of $0.65v^2/R_s^2$ at $\pm 30^\circ$ from the normal. The transfer function that describes the angular velocity and acceleration of the tracking antenna about the azimuth axis has a "pole" when the ground range approaches zero

and the target is near overhead. A loss of track can occur. The three-axis mount described in Skolnik³ removes the pole at the expense of increasing weight, complexity, and cost.

Even though coverage is sacrificed, a two-axis mount is often chosen for reflectorantenna tracking systems for fixed earth stations or for installation on aircraft or ship platforms. The mount is oriented so that the loss in mission coverage due to the pole is minimized and has little impact on overall operation.

Phased-array-antenna tracking systems that must provide hemispherical coverage for different missions but limited coverage for a single mission may also use the elevation-over-azimuth mount or may use an azimuth-only mount. Dynamic performance requirements are usually limited, but accuracy of positioning must still be maintained.

Mechanical Errors in Reflector Tracking Antennas

This subsection discusses mechanical errors in using, for example, an elevation-over-azimuth mount. The errors are treated as being independent. Though not strictly true, the assumption appears to be valid for the size of errors expected in an accurate system. These formulas may be used as corrective algorithms to the elevation and azimuth angular estimates once the constants have been determined by calibration. More exact expressions for some of the errors will be found in Rozansky. Is In a new design or in one whose error models are not well known, these algorithms may be used initially, but the final algorithm should be adjusted to match the particular system.

Encoder Errors The angular position of the antenna is translated into digital or analog data by using angle encoders. Most designs today incorporate digital encoders. The output of these encoders is subject to both systematic and noise errors within the encoder itself; in the data gear train, if used; and in the coupling of the encoder to the mechanical takeoff from the antenna. The state of the art is such that the latter two are usually the greater source of error. If the coupling is rigid, the relative motion between the driving axis and the encoder shaft introduces bending movements in the shaft of the encoder and cyclic errors in the output. Multicyclic errors can be produced by gear trains.

When a flexible coupling between the axis takeoff and the encoder is used, mechanical eccentricities that produce systematic cyclic variations in output data may occur. Backlash produces random errors. Noise in the encoder also produces a random error. With the encoder shaft held fixed, a variation of ± 2 bits in a high-resolution (19-bit) system is not unexpected.

Torquing of setscrews or like fasteners can produce bending moments that may

distort the encoder shaft. Rather than adjusting the encoders and creating such an error, provision can be made in the calibration process to introduce the values by which the encoders are offset from the reference positions.

The equation for a combined cyclic and encoder offset error with respect to the reference position is

$$E_{Ac0} = M \cos (A_m - A) + A_0 \tag{34-16}$$

where M = maximum amplitude of cyclic error

A = azimuth reading of encoder

 A_m = azimuth reading of cyclic-error maximum amplitude

 A_0 = azimuth reading for external azimuth reference

This equation is also valid for the elevation encoder when the elevation values E, E_m , E_0 are substituted for A, A_m , and A_0 . The use of this equation, when M and A_m (or E_m) are measured during the calibration process as a correction algorithm, leads to the level of systematic residual error given in the error budgets in Tables 34-1 and 34-2.

Azimuth-Axis Tilt Leveling a reflector tracking antenna can be accomplished with three adjustable legs, using two orthogonal gravitational sensors that are parallel to

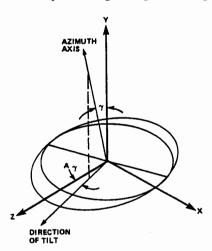


FIG. 34-18 Azimuth-axis tilt.

the azimuth plane. An accurate tracking system is usually leveled to within 0.1 to 0.2 mil of the vertical, preferably under cloudy conditions or at night to eliminate temperature gradients. Leveling to a tighter tolerance is not productive, since day-to-day variations of the pedestal vertical, as shown in Fig. 34-22 below, can be greater. In addition, the local vertical may not be the true vertical because of gravitational anomalies, and calibration with respect to the true vertical may be required.

When the azimuth axis is tilted at an angle γ from the vertical reference as shown in Fig. 34-18, errors in both azimuth and elevation that are generated may be approximated by

$$e_{A\gamma} = \gamma \sin (A_{\gamma} - A) \tan E$$

$$e_{E\gamma} = \gamma \cos (A_{\gamma} - A)$$
(34-17)

where $\gamma = \text{tilt angle}$

 $A_r = azimuth direction of tilt$

A = azimuth encoder output

E = elevation encoder output

Boresight-Telescope Nonorthogonality The boresight telescope used for system alignment and calibration usually will not be exactly orthogonal to the elevation axis. An error in azimuth, as shown in Fig. 34-19, is produced for the optical axis.

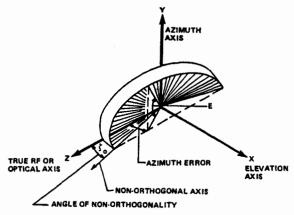


FIG. 34-19 RF- or optical-axis to elevation-axis nonorthogonality error.

Correction can be made through physical adjustment to the body of the telescope or through correction of the data by measuring the angle ζ_0 of nonorthogonality. The error-correction algorithm is approximated by

$$e_{Apo} = \zeta_0 \sec E \tag{34-18}$$

where E is the elevation angle. This equation is needed to derive the RF-axis nonorthogonality to the elevation axis and is not used directly in correcting tracking-antenna azimuth data.

RF-Axis Nonorthogonality The same type of error is produced in azimuth data if the RF axis is not orthogonal to the elevation axis. However, RF-axis-nonorthogonality errors may be a combination of mechanical and electrical boresight shifts, with the latter being a function of frequency of operation.

$$e_{A|r} = \zeta_r \sec E \tag{34-19}$$

Steps in the calibration process require that the optical nonorthogonality be determined first and that the RF nonorthogonality as a function of frequency then be determined with the use of a target that is visible both optically and at RF.

Elevation-Axis Nonorthogonality (Skew) If the elevation axis is nonorthogonal or skewed to the azimuth axis by a small angle ϵ_0 , as shown in Fig. 34-20, the resultant azimuth error and correction algorithm is approximated by

$$e_{A\epsilon} = \epsilon_0 \tan E \tag{34-20}$$

for both the optical and the RF axis.

Droop Droop is an elevation error produced by gravitational force on the boresight telescope and on the RF feed. The errors are at a maximum at 0 and 180° elevation

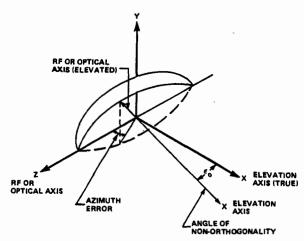


FIG. 34-20 Elevation-axis to azimuth-axis nonorthogonality error.

and at a minimum at 90°. They are normally constant with azimuth position. The droop in the telescope can be approximated as a linear equation:

$$e_{Ed_0} = d_0 (E - \pi/2)$$
 (34-21)

where d_0 is the telescope droop constant. The RF boresight-axis droop is approximated by

$$e_{Ed_r} = d_r \cos E \tag{34-22}$$

where d_r is the RF feed constant. The telescope constant is developed first during the calibration process and then, with a common target, used to determine the RF-axis droop constant.

Collimation Collimation is defined as "making parallel" or "adjusting accurately the line of sight of [a telescope]." In this chapter, collimation refers to the relationship between the RF boresight axis and the boresight telescope that is used as a reference.

The collimation error between the RF boresight axis and the optical axis is determined by the resolution of the boresight telescope and the optical recording, the depth of the null for the RF difference pattern, multipath error, and the rms phase error of the receiving system. If a common target has a high RF signal-to-noise ratio, optical visibility, reflectivity characteristics that do not depolarize the signal return, high elevation angle, and low velocity and acceleration so that the target can be tracked at or near the RF null, then the collimation error can be reduced to 0.02 mrad rms in each axis. In elevation, the residual error is the error remaining after accounting for mechanical droop, electrical boresight shift, multipath, and the differential offset constant between the optical axis and the RF axis. In azimuth the residual error is the error remaining after accounting for the electrical boresight shift of the RF axis and the nonorthogonality of both the optical axis and the RF axis with respect to the elevation axis.

Thermal Effects Thermal effects on accuracy primarily are those due to solar radiation producing thermal gradients in the reflector tracking antenna and mount. Differential heating of the mount base will produce an azimuth tilt error. Unequal expansion in the trunion arms supporting the elevation axis can produce an elevation-axis nonorthogonality error. Droop, collimation, and RF-axis-nonorthogonality errors can be accentuated or decreased by gradients in the feed supports. For highly accurate systems, material with low thermal coefficients of expansion should be used. This is particularly true for feed supports. The use of white paint for the entire antenna and mount for nontactical systems and sunshields for the mount will considerably reduce thermal gradients.

Thermal effects are long-term when compared with the time for most instrumentation radar missions. A system designed for rapid premission calibration can reduce the impact of such errors.

Wind Wind produces both systematic and random errors. A steady-state wind having a velocity V produces a small systematic deflection error:⁷

$$e_{wd} = K_w K_s V_w^2 (34-23)$$

where K_w is an aerodynamic constant that relates the torque produced about one of the angular axes to the average wind speed and $V_w K_w$ is a function of the aspect angle of the antenna with respect to wind direction. The mechanical spring constant of the antenna K_s is a measure of the deflection of the antenna about the axis per unit of torque.

Gusty winds produce a small random error with a standard deviation of

$$\sigma_{wd} = 2K_s K_w V_w \sigma_v \tag{34-24}$$

where σ_v is a measure of the variation in average wind velocities.

Consideration can be given to the use of a radome to reduce wind-load errors, but a trade-off must be made between radome and wind-induced pointing errors.

Mechanical Errors In Phased-Array Tracking Antennas

Rotation Angular displacement $(\Delta\theta_z)$ about the Z axis or the array normal produces errors in both α and β proportional to $(\beta-\pi/2)\cdot\Delta\theta_z$ and $(\alpha-\pi/2)\cdot\Delta\theta_z$ respectively, where $\Delta\theta_z$ is small. A highly damped tiltmeter, located parallel to the X axis, can be used to level the array initially and automatically monitor for subsequent rotation displacement. High damping is necessary to prevent response of the tiltmeter to vibration and to short-term wind loads but will still permit measurement of permanent shifts.

Tilt The array is usually tilted backward about the X axis to obtain elevation coverage consistent with tracking demands at the horizon. Angular displacement about the X axis can be measured with a highly damped tiltmeter mounted perpendicularly to that axis with the center of the tiltmeter range at the desired tilt angle. Angular displacement errors about the X axis directly contribute to errors in β , with a minimum amount of coupling into α . Both the rotational and the tilt sensors provide the reference to the local gravitational vertical rather than the true vertical.

Array Face to True North Alignment of the array-face normal so that its relationship is known with respect to the plane established by the local vertical and true north can be accomplished through a north-seeking gyro designed as an integral subsystem of the array. Gyros are available with an error in pointing of less than 0.3 mrad rms divided by the cosine of the latitude. They require settling times of 5 to 15 min to reach such values.

Thermal Effects In a planar phased array, a shift in boresight can occur when the overall array-face temperature changes and when there is a uniform differential expansion or contradiction between element distances D_x and D_y . At an α of 45°, a 25-ppm thermal-expansion coefficient and a 40°C differential temperature produce a 1-mrad shift. The formula for the error before correction is

$$e_{\alpha t,\beta t} = L_t (T_c - T_0) \cot (\alpha_t, \beta_t)$$
 (34-25)

where L_t is the coefficient of expansion, T_c is the calibration temperature, and T_0 is the operational temperature.

A temperature gradient across the face of the array will produce errors dependent on the thermal-gradient pattern. Such errors will be difficult to determine and correct by calibration. Consequently, the thermal design of the array face and structure should minimize such gradients.

An additional thermal error is that due to both absolute temperature and thermal gradients of the feed system. It also will be difficult to determine and correct by calibration. Thermal design must consider the feed architecture and techniques to maintain small thermal gradients between parallel elements in order to minimize differential phase errors.

Wind The potential for error due to wind and wind gusts is generally greater in a tactical than in an instrumentation tracking-antenna system. The instrumentation system usually has a solid base to which the antenna mount can be rigidly attached, whereas the tactical radar tracking-antenna support structure rests on the ground. The weight of the phased array or wind loads can produce pressure, which in turn compresses or deforms the surface supporting the mount, giving errors about one or more of the array-face axes. Such errors caused by displacement can be read out by tilt-meters and gyros that have been designed as an integral part of the array. In addition to the angular displacement caused by wind loads in θ_X and θ_Z , unless there is means of lateral bracing, angular displacements that are primarily in θ_Y can take place.

In addition to the small permanent shifts, which can be measured by the gyros and tiltmeters, shorter-term shifts due to wind deflection of the mount structure can occur. High and gusty winds can cause large errors, particularly for a system with a low resonant frequency.

34-5 SYSTEM CALIBRATION

Calibration serves two functions: (1) to provide direction for realignment or correction of faults after assembly or after transport in which the antenna may be subject to mechanical stresses; and (2) to provide constants for the algorithms to correct the systematic errors, permitting the system to operate within the accuracy required. To

provide maximum accuracy, the system should be calibrated under conditions as near as possible to the conditions under which it will operate. Knowledge of absolute temperature is important for phased-array calibration but is of limited value for reflectorantenna tracking systems. For thermal gradients that distort the antenna and pedestal for reflector tracking antennas used in highly accurate instrumentation systems, it is desirable to calibrate as close to mission time as possible.

The first method of calibration involves direct measurement to determine the errors and then correction of the errors as a function of angular direction and frequency. The second method is the tracking of targets whose trajectories are accurately known, such as satellites, and the use of regression analysis to determine the errors as a function of direction and frequency. This latter approach is generally limited to large power-aperture product systems.

The use of sensors having automatic readout under control of a computer appears to give the fastest, most consistent results and removes the possibility of observer error. When an observer is involved, the design of the readout should reduce the requirements on the observer to a minimum. Physical stress due to temperature extremes, muscular strain due to position, and lighting all contribute to potential observer error.

Frequency of calibration and number of sample measurements depend on user requirements and the stability of the system. It should be noted that in general the larger the number of independent sample points chosen for a particular calibration procedure, the more precisely one may model any particular error. Initially, a tracking-antenna system may require a large number of samples to establish a model or algorithm for the error and a lesser number on subsequent calibrations. A tracking antenna with a specified accuracy of 0.1 mrad (exclusive of thermal noise, glint, multipath, refraction, and clutter) may require calibration for each mission. A tracking antenna with a specified accuracy of 0.5 mrad (exclusive of thermal noise, glint, multipath, refraction, and clutter) may require only leveling and the use of automatic sensors to measure changes.

Calibration for Reflector Tracking Antennas

The order of calibration is chosen to minimize coupling of errors. The order, or technique, used may not be appropriate for all systems, but the principles involved may be applied to develop those required for a specific tracking antenna and user.

Optical-Axis Calibration Accurate angle encoder readouts with respect to the antenna azimuth and elevation axes of the antenna mount of Fig. 34-21 are fundamental in establishing angular errors in a tracking antenna. A multifaceted optical flat (with 17 facets, for example), temporarily mounted perpendicular to and centered on the axis of rotation and used with an optical collimator, can establish the cyclic errors in the encoder within 0.02 mrad rms. This readout should be performed after installation of the encoder in the mount. Each measurement should be made by rotating about the axis in the same direction to eliminate backlash errors. An encoder readout is made when the reflection of the collimator cross hairs from the optical flat coincides with the collimator cross hairs. Backlash can be determined by reversing the direction of antenna rotation about the axis and reading the encoder at any one of the optical flat positions to establish the backlash random error. The random error due to granularity of the encoder can be read by leaving the antenna stationary and reading the encoder output variation.

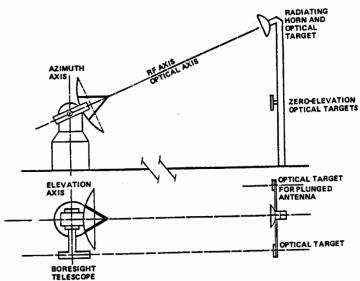


FIG. 34-21 Elevation- over azimuth-axis tracking antenna and boresight tower.

The next step in calibration for a reflector antenna after encoder cyclic errors have been established is the use of on-mount levels to bring the azimuth axis parallel to the local vertical. After leveling in one azimuth position, readings are taken at a number of azimuth locations, giving results similar to that of Fig. 34-22.

The error models or algorithms of Sec. 34-4 are used to correct the data output. The difference estimates that are furnished by use of these algorithms and true position results in residual errors that are small. Figure 34-22, for example, gives two sets of measurements made on different days. Peak-to-peak error approached 0.4 mil* on March 31 and 0.2 mil on April 3. Correction of the data left a residual error of less than 0.02 mrad for each day. If a second calibration had not been made on April 3, peak errors in excess of 0.1 mil would have been introduced, indicating the need to recalibrate highly accurate systems on a mission basis.

With an antenna capable of plunging, i.e., with an elevation motion greater than 180° , the optical-axis nonorthogonality to the elevation axis may be established by reading the azimuth position of the zero-elevation optical targets of Fig. 34-21 with the antenna in both normal and plunged positions. The difference in azimuth encoder readout should be exactly π rad. One-half of any difference is the optical- to elevation-axis nonorthogonality.

To determine the nonorthogonality or skew constant of the elevation-to-azimuth axis, azimuth encoder readings are then made in the normal and plunged portions of the upper optical targets, taking into account the calibration data from the encoder and the optical-elevation-axis nonorthogonality measurements. The readings should

^{*}This error was taken on a radar using the artillery mil., i.e., ‱ of a circle. This value should not be confused with the milliradian or the artillery-spotting mil (1 yd subtended at 1000 yd). The abbreviation of mil for milliradian is sometimes seen in the literature. Many older systems still utilize the artillery mil.

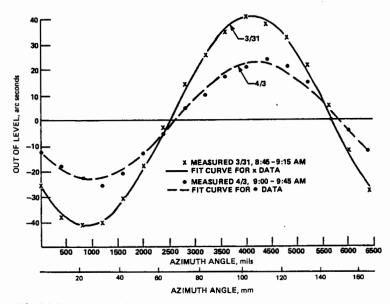


FIG. 34-22 Antenna tilt. (After Ref. 13.)

be π rad apart. If not, the skew constant ϵ for the correction algorithm is the difference in reading divided by 2 and then divided by the tan E of the elevation of the upper optical targets. The use of the zero-elevation optical targets precludes the coupling of the optical-elevation-axis-nonorthogonality error into the measurement.

Once the nonorthogonality error of the elevation to azimuth axis has been established, the azimuth encoder offset may also be established by using the upper bore-sight-tower targets as a reference, which usually is surveyed with respect to true north. If the positions of both sets of optical targets and the position of the centerline of the telescope axis and antenna elevation axis are accurately known by an external survey, the droop constant d_0 for the telescope may be determined by the difference in elevation encoder readings between the lower and upper optical targets. Once the droop constant has been established, the elevation encoder offset with respect to the optical axis may be entered into the calibration data.

RF-Axis Calibration Once the errors have been established for the optical axis and correction made, the relation of the RF axis to the optical axis must be determined. In azimuth, this is relatively simple. Usually there is no azimuth multipath. A boresight-tower RF horn radiating a polarized signal and an optical target separated by exactly the same distance as the RF boresight axis of the antenna and the optical axis of the telescope are used, as shown in Fig. 34-22. The RF axis is found at minimum reading from the difference channel in azimuth and elevation. If the depth of the null in either axis does not meet the error-budget requirements, it should be corrected since further measurements will be contaminated by postcomparator phase errors.

The elevation- to azimuth-axis nonorthogonality or skew error is the same for the RF axis as for the optical axis. The azimuth error introduced by RF boresight-axis-to elevation-axis nonorthogonality will be a function of both the mechanical position

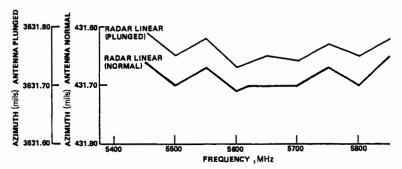


FIG. 34-23 Azimuth RF boresight shift versus frequency. (After Ref. 13.)

of the feed and the variation of the boresight axis in azimuth as a function of frequency. Since the skew error is known, the boresight tower can then be used to determine the RF boresight-axis to elevation-axis nonorthogonality as a function of frequency. The test results in Fig. 34-23 show this nonorthogonality to be approximately 0.025 mil and the peak-to-peak variation in azimuth of the boresight axis to be approximately 0.06 mil across the band. As can be seen, the RF to optical-axis collimation error is quite small, <0.01 mil rms.

The multipath, droop in the RF feed, and frequency shift of boresight are combined when measured at a single elevation. The droop is constant at that elevation, but the multipath and frequency shift of the boresight axis are variable. Multipath error may be separated by tracking a balloon-borne metallic sphere; the sphere is centered within the balloon and launched near the tracking antenna. RF tracking is initiated. Corrected data from the radar and optical recording of the boresight-telescope field of view are compared when the elevation angle is above that at which multipath is a factor. A set of 10 frequencies across the band is used for 10 different elevation angles. From this measurement, the boresight shift in elevation with frequency may be determined separately from multipath. Once the droop constant and the boresight shift with frequency have been determined, the RF- to optical-axis offsets may be determined. The remaining error is that due to the collimation error, that is, the limits of telescope resolution, depth of null, and observer.

Off-Axis Calibration Once the electrical boresight axis has been established, off-boresight positions are calibrated. A plot of error versus angle offset is given in Fig. 34-24 in both elevation and azimuth for a single frequency. These measurements were made by using a boresight-tower RF horn radiating a vertically polarized signal. There may be some cross-polarization, multipath, and droop contamination, but the amount should be negligible, since the angular change during measurement was much smaller than the beamwidth.

Star Calibration of the Optical Axis The most accurate method for optical-axis calibration of the antenna mount is that of star calibration.¹⁹ The steps are similar to those used by Meeks,²⁰ except that the sensitivity of most tracking antennas does not permit direct calibration of the RF axis. A set of stars which is visible (brightness magnitude greater than 3.8) at the time of calibration²¹ and distributed uniformly over the celestial sphere between 15 and 70° with respect to the local vertical is chosen as

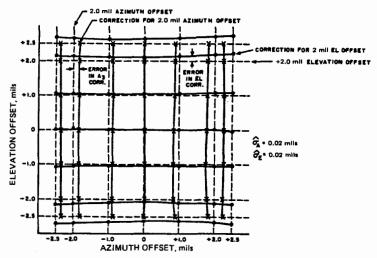


FIG. 34-24 RF off-axis error. (After Ref. 13.)

the reference base. Under computer control the azimuth and elevation positions of each star selected are measured by using the optical telescope. A timing error of ± 0.2 s contributes about 0.005 mrad rms to the instrumentation error. A telescope with a resolution of 4 s contributes about the same error.

After the measurements have been taken and corrections for refraction made, a regression analysis will permit determination of the error coefficients for each of the mechanical-error-correction algorithms. The entire process, which may be limited by cloud cover, takes only a few minutes and offers an opportunity to maintain the mechanical system at its highest level of accuracy.

The use of stars as a reference has the advantage of determining true vertical as compared with local vertical—a difference that could be as much as 0.3 mrad in certain locations. It further provides a means of assessing errors as a function of azimuth rather than just the normal and plunged positions. A boresight tower and balloon tracks are still required to establish the relationships of the RF to the optical axis.

Calibration for Phased-Array Tracking Antennas

Calibration techniques for phased arrays depend on the size, configuration, and use of the arrays. If the design is in a limited-scan phased array utilizing a two-axis mount, the mount can be calibrated by using techniques similar to those used for reflector antennas. Once the mount and the face of the array have been established with respect to the azimuth and elevation axis, the array itself may be calibrated by using the mount encoder output and a boresight tower. The same limitation in accuracy by multipath applies here as for the reflector antenna.

If the final phased-array tracking system does not use a mount but the antenna is of a size so that it can be placed on a two-axis mount, then the angular position of the array face to the boresight tower can be established with respect to a theodolite attached to the antenna. A scan-angle order can be given, and the angular position to

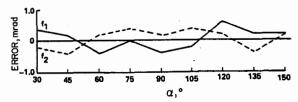


FIG. 34-25 $\alpha - \alpha_i$ error with scan angle.

which the antenna face must be rotated to obtain a difference-pattern null can be established by the theodolite. This angle is then compared with that ordered by the beam-steering controller. An example of the error expected is given in Fig. 34-25. If corrected as a function of frequency, the residual systematic error is less than 0.1 mrad rms.

Another technique that has recently been demonstrated is the use of near-field measurements. The antenna is first mounted in an anechoic chamber. A radiating probe antenna is raster-scanned across the face of the array at a constant distance from the array with the polarization of the probe antenna parallel to that of the array. Measurements are made of amplitude and phase for each of the probe positions at the sum-and-difference output ports. Once the near field is known, the far-field sum-and-difference patterns may be calculated. This technique has been validated by far-field measurements that were made with the same antenna. The near-field technique has the additional advantage of low multipath and radio-frequency interference effects.

The use of the near-field techniques provides data for the sum-and-difference pattern for any one scan angle, frequency, or temperature value. Calculations of the field pattern provide the calibration data for correcting both boresight and off-boresight errors.

A sufficient number of beam positions, both on and off the cardinal planes, must be measured to develop the error-correction algorithms. The same beam positions should be repeated with different frequencies to assure that the beam-steering algorithms in the controller are correct and that errors present in beam position as a function of frequency can be established and corrected. In addition, a set of patterns should also be measured at a different temperature if possible, to develop error-correction algorithms as a function of temperature.

When the antenna is large and cannot be assembled at the factory but must be installed and aligned on site, the position of the array face in the local coordinate system is determined by a survey. By using optical flats and prisms on the antenna face, the orientation of the face with respect to true north, tilt with respect to true vertical, and the rotation about the normal to the array face are determined.

Such an antenna is generally large enough to track such objects as satellites having well-established trajectories. A track of a sufficient number of objects, over the band of operating frequencies, permits a regression analysis that provides for calibration as a function of scan angle and frequency. Scanning about the target establishes the difference-pattern slope. Thermal and wind conditions affecting the array must be recorded concurrently so that the errors produced can be correlated with these conditions and data-correction equations can be developed.

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Satellite Antennas*†

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35-1	Spacecraft-Stab	ilization	and	Field-of-View
	Considerations	35-2		

³⁵⁻² Despun-Antenna Systems 35-6

³⁵⁻³ Antenna Polarization 35-9

³⁵⁻⁴ Three-Axis Stabilized Satellites 35-10

³⁵⁻⁵ Earth-Coverage Antenna 35-11

³⁵⁻⁶ Spot-Beam Coverage 35-14
Statistical Distribution of D 35-16

³⁵⁻⁷ Cross-Link Antennas 35-18

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The use of satellites in communication and remote-sensing systems has increased tremendously in the past decade or two, resulting in designers who specialize in satellite antennas. The uniqueness of the platform, the environment, and the applications requires antenna designers to interact with several disciplines including mechanics, structural analysis, thermal analysis, surface charging and radiation effects, and communications theory. This chapter will address fundamental spacecraft-stabilization characteristics and the related considerations of antenna design and polarization. Earth-coverage antennas will be described, and the use of higher-gain multiple-beam antennas will be discussed. Finally, a comparison of two types of cross-link antennas is presented. Although these discussions may apply to antennas used in other types of systems, the communications satellite (COMSAT) will be in mind unless otherwise specified.

35-1 SPACECRAFT-STABILIZATION AND FIELD-OF-VIEW CONSIDERATIONS

Not unlike an airplane, an automobile, a ship, and a tower, spacecraft have their unique "platform" characteristics, which determine some of the antenna's more important characteristics. In particular, a spacecraft derives its "stability" from the gyroscopic action produced by rotating all or some of its mass. Consequently, all satellites are designed so that all or a significant part of their mass rotates so as to establish a reference axis, plane, or sphere. In the early years of the satellite age, all satellites were intentionally rotated about the axis with the largest inertial moment; these satellites are commonly referred to as *spinners*. The orientation of this axis was often maintained by applying external forces to the satellite by various means, such as gas propulsion, emission of ionized particles of a solid, and interaction with the earth's magnetic or gravitational fields.

With the development of lubricated bearings that can be operated satisfactorily in the vacuum of space, three-axis stabilization became possible, resulting in a despun platform similar to a tower on which the antennas of a microwave land link are mounted. Recently it has become popular to use an inertia wheel (i.e., a three-axis gyro) to establish the needed reference system for a three-axis stabilized satellite. Of course, in all cases (except perhaps one-axis stabilization) controlling external forces are applied, in cooperation with pointing and attitude error-sensing devices, to maintain the satellite in the desired orbit or at a particular point in the orbit. The latter function is often referred to as station keeping.

Since the prime purpose of a communication satellite is to provide a relay between two or more communication terminals, the earth-bound satellite must have an antenna capable of transmitting signals to and receiving signals from the earth. The degree of stabilization and whether or not the satellite is a spinner determine the fundamental conditions under which it must perform this function. In particular, an antenna on a spinning satellite must have a radiation pattern that is uniform in the plane perpendicular to the spin axis, or it must be designed so that its radiation pattern is "despun" mechanically or electrically. Even an antenna on a three-axis stabilized vehicle must be designed to compensate for satellite attitude and station-keeping errors, again either by modification of its radiation pattern or by physical reorientation of its structure. Clearly, using the tumbling satellite as a platform presents the great-

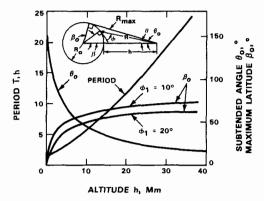


FIG. 35-1 Satellite-earth characteristics.

est challenge to the antenna designer, and the three-axis stabilized station-kept satellite allows for the most sophisticated antenna design.

Communication satellites are often placed in a nearly circular orbit and hence the angle θ_0 , subtended by the earth and measured at the satellite, is relatively constant. Since the communications requirement usually involves a relay between widely separated points on the earth, the satellite's field of view (FOV) is often defined by θ_0 and is given by

$$\theta_0 = \sin^{-1} \left(R_0 / R_0 + h \right) \tag{35-1}$$

Referring to Fig. 35-1, we see that θ_0 varies from about 145° for a low-attitude satellite to 17.3° for a satellite in a synchronous (i.e., 24-h-period) orbit.

Although most communication satellites make use of the geostationary properties of the equatorial synchronous orbit, other considerations may dictate an elliptical orbit and the concomitant change in θ_0 . For an elliptical orbit, the earth is located at one of the foci of the ellipse traced by the orbit and is defined as the barycenter. The eccentricity ϵ of the ellipse is given by

$$\epsilon = [1 - (b/a)^2]^{0.5}$$
 (35-2a)

where a and b are the semimajor and semiminor axes of the elliptical orbit, for a circular orbit a = b and $\epsilon = 0$. The orbital period T is independent of ϵ (i.e., as long as the orbit does not intersect the earth), and it is given by

$$T = 2\pi[(R_0 + h)^3/\alpha]^{0.5}$$
 h (35-2b)

where $R_0 = 6378$ km is the radius of the earth, h is the maximum altitude of the satellite above the earth's surface (measured in kilometers), and $\alpha = 5164 \times 10^9$. For a 24-hour orbital period, maximum altitude is 34.8 Mm (21,454 statute miles).

An earth terminal located at the edge of the satellite's FOV views the satellite at an elevation angle $\phi=0^\circ$; that is, the satellite is on the local earth horizon. System performance usually requires $\phi>10^\circ$; hence the satellite's FOV ϕ_0' is somewhat less than that described by θ_0 . The angle θ between the earth-satellite axis and the terminal-satellite direction determines the satellite elevation angle ϕ , as shown in Fig. 35-2. The relation between ϕ and θ is plotted for a satellite at synchronous altitude and at binary multiples of synchronous altitude. The corresponding satellite period T is

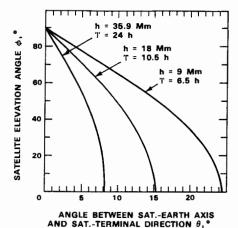


FIG. 35-2 Elevation angle of the satellite measured at the earth terminal.

also indicated for ease of reference. Clearly, $\phi = 0$ when $\theta = \theta_0$ and $\phi = 90^{\circ}$ when $\theta = 0$. Using Fig. 35-2, β_0 , the maximum latitude of a terminal, was computed by using

$$\beta_0 = 90 - \phi_1 - \theta_1 \tag{35-3a}$$

and

$$\theta_1 = \sin^{-1}[R_0 \sin{(90 - \phi_1)}/(R_0 + h)]$$
 (35-3b)

where ϕ_1 is the minimum value of ϕ and θ_1 is the corresponding value of θ for the ϕ = ϕ_1 (see Fig. 35-2). With reference to Fig. 35-1, β_0 is plotted for ϕ_1 = 10° and 20° and indicates that satellites in an equatorial orbit cannot operate with terminals located at north or south latitudes in excess of about 70° unless their altitude above the earth exceeds 40 Mm.

Inclined 12-h elliptical and 24-h polar orbits and the equatorial synchronous orbits form what might be considered a primary set of orbits that have most desirable characteristics. The geostationary orbit is most often used by systems with terminals located in the tropical and temperate zones. Satellites in the polar and, most often, the inclined elliptical orbit are used by terminals in the temperate and polar regions. Systems with satellites in both orbits provide worldwide coverage; worldwide service is obtained through the use of satellite-to-satellite links (i.e., cross links) or earth terminals as gateways. Gateway terminals must be in the FOV of at least two satellites. Cross-link-antenna design² will be discussed in Sec. 35-7; however, it is of importance to note that θ_0 and h of a critically inclined 12-h elliptical orbit³ vary as shown in Fig. 35-3. This orbit is often referred to as the Molniya orbit since it was first used by the Russians to provide "commercial" communications capacity to all populated parts of the Soviet Union. For the critically inclined orbit, solar pressure will not cause it to precess. The times indicated in Fig. 35-3 are measured either prior to or after apogee. A pair of satellites spaced about 6 h along the same orbit provide continuous coverage in the temperate regions and one polar region. Note that θ_0 and h vary by approximately 30 percent over the 6-h useful portion of the orbit, that is, during the period from 3 h before to 3 h after the satellite is at its highest altitude above the earth. It is

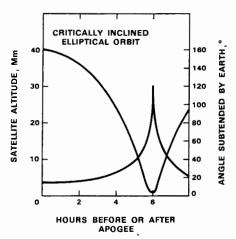


FIG. 35-3 Characteristics of a 12-h elliptical orbit.

the indicated change in θ_0 and the relative direction to the center of the earth that affect antenna-design considerations.

Before considering antenna designs as they interact with various stabilization methods, it is important to point out that satellite-antenna-pattern coverage, as viewed from the angular space conventionally used to describe antenna performance, becomes distorted when radiation-pattern contours are plotted on conventional (e.g., Mercator, gnomonic, etc.) projections of the earth. Presentation of antenna-pattern contours of constant gain on earth maps are referred to as beam footprints. The beam-contour coordinates ϕ and θ can be transferred to earth latitude and longitude to determine the beam footprint by first assuming that the satellite's nadir is located at a longitude $= a^*$ and at 0° latitude. Then use

$$\phi = \cos^{-1} (1 + h/6378) \sin \theta \qquad (35-4a)$$

$$\beta = 90 - \phi - \theta \tag{35-4b}$$

to compute β . The coordinates of a point P on the earth at longitude ζ and latitude ξ are related to θ and ψ through

$$\xi = \sin^{-1}(\sin\beta\cos\psi) \tag{35-5a}$$

$$\zeta = a + \tan^{-1}(\tan\beta\sin\psi) \tag{35-5b}$$

where ψ is the angle measured from the plane containing the satellite and the earth's polar axis to the plane determined by the earth-satellite axis and the line from the satellite to the point P (Fig. 35-4). When the satellite's nadir is not on the equator, the transformation is given by

$$\xi = \sin^{-1} \left[\sin \left(b + \beta \right) + \cos b \sin \beta \left(\cos \psi - 1 \right) \right]$$
 (35-6)

$$\zeta = a + \sin^{-1}(\sin\psi\sin\beta/\cos\xi)$$
 (35-7)

where b is the latitude of the satellite's nadir and a is its longitude.

The foregoing is presented to point out that the satellite's stabilization method

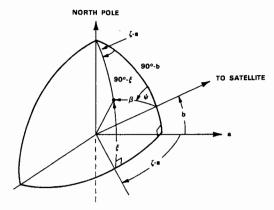


FIG. 35-4 Transformation coordinate system.

and its orbit have a serious impact on its antennas and their FOV. It is beyond the scope of this chapter to discuss these interactive design relationships in detail; however, some designs will be described to indicate methods of accommodating these characteristics.

35-2 DESPUN-ANTENNA SYSTEMS

Many earth satellites are cylindrically or spherically shaped bodies rotating about the axis for which their inertial moment is maximum. If the orientation of this axis is uncontrolled, the antenna has to produce a radiation pattern that is uniform in the plane perpendicular to the spin axis. Alternatively, one could use a directional antenna whose radiation pattern is either despun by varying the excitation of the antenna (i.e., as in the case of an array) or by mechanically rotating the antenna at the same angular rate but in a direction opposite to the satellite's rotation. Clearly if the antenna radiation pattern is not despun and the spin-axis orientation is not controlled (one-axis stabilization), the antenna pattern must be independent of direction. This leads to an isotropic antenna and the concomitant directivity and directive gain of 0 dB.

Telstar, the first active communication satellite, employed antennas⁵ having a nearly isotropic radiation pattern. The satellite rotated on its axis of maximum moment of inertia and had some attitude control; it was, therefore, a two-axis stabilized spacecraft. It was spherically shaped with an approximate radius of 35 in (889 mm). It had antennas operating at very high frequency (VHF), at 4 and at 6 GHz. All radiation patterns were uniform in a plane perpendicular to the spin axis, providing the necessary despinning function. Except for the surface occupied by the antennas, solar cells covered the satellite's outer surface.

The first Lincoln experimental satellite (LES-1) had two-axis stabilization; the orientation of the spin axis was maintained by force derived from an interaction with the earth's magnetic field. One of the major purposes of LES-1 was to demonstrate the feasibility of electronically despinning the radiation pattern by switching among eight low-directivity (about 7 dB) antennas distributed uniformly over the satellite

duodecahedron shape. This experimental satellite also demonstrated the feasibility of a simple magnetic attitude-control system that was subsequently used⁶ on LES-4 and enabled the use of antennas with higher directivity (about 14 dB).

With the exception of a VHF antenna on Telstar, communication antennas on these earlier satellites operated in the superhigh-frequency (SHF) range (i.e., 4, 6, and 8 GHz). This enabled the antenna designer to realize moderate antenna gain without significantly compromising the other satellite functions and systems. However, the SHF ground terminals were necessarily large and hence few in number, resulting in communication satellites which served only a few earth terminals or direct users. In the late 1960s, LES-5 and LES-6 were placed in synchronous orbit and operated in the ultra high-frequency (UHF) communications band to service a wide variety of military communication needs because only modest-size earth terminals were required. The antenna systems on LES-5 and LES-6 had approximately the same radiation pattern as Telstar and LES-4 respectively. It is of interest to compare the methods of achieving these radiation patterns.

Telstar employed a large number of open-ended waveguide radiators spaced one-half wavelength on center along the satellite's equator. Two such antenna arrays, one operating at 4.17 GHz and one at 6.39 GHz, were used; each was fed so as to excite each element in phase and with the same signal amplitude. This symmetry guarantees a symmetrical radiation pattern in the plane perpendicular to the satellite's spin axis. Uniformity of the radiation pattern is controlled by the number of individual radiators per wavelength along the satellite's equator and the phase and amplitude equality of the signals exciting each radiator in the array. These antennas had an equatorial-plane radiation pattern that was uniform within ± 1 dB. The feed network⁵ provided the desired excitation amplitude and phase within 0.5 dB and 5° respectively.

LES-5 was a cylindrically shaped satellite? about one wavelength (λ) long and one wavelength in diameter; that is, it was much smaller than Telstar in terms of their respective operating wavelengths. The communication antenna consisted of two circular arrays. One array was made up of eight full-wave dipoles spaced about $\lambda/2$ circumferentially on the satellite's cylindrical surface and excited in phase with equal-amplitude signals. The other array consisted of two rings of eight half-wave cavity-backed slots colocated with the dipole array. The slots were also excited in phase with equal-amplitude signals but in-phase quadrature with the dipole array so that the combined dipole-slot pair would radiate and receive circularly polarized signals. The antenna radiation pattern was uniform, within ± 1 dB, in planes perpendicular to the satellite's spin axis. Unlike Telstar, LES-5's radiation pattern in a plane containing the spin axis approximated that of a linear array of two $\lambda/2$ dipoles spaced about $\lambda/2$ on center along the satellite's spin axis.

It is of interest to note that the configuration of each satellite (Telstar and LES-5) prohibited placing the antennas at the center of the satellite, where the small single radiator could have been placed to obtain the desired circularly symmetric radiation patterns in the satellite's equatorial plane (i.e., such as that obtained in a plane perpendicular to the axis of a dipole). In fact, most of the volume within the satellite was reserved for other subsystems of the satellite. This required that the antenna be distributed around the outside surface of the satellite and appropriately excited through circuits, made up of transmission lines and n-way power dividers, integrated with the other subsystems located within the satellite's surface. Virtually any one- or two-axis stabilized satellite without a despun antenna must use this general type of antenna configuration to meet the usual requirements dictated by earth-bound stations using

a communication satellite. The antenna configuration is often similar to that of public television broadcast antennas mounted on a high tower.

Occasionally a dipole, stub, biconical, or slot antenna that will produce the desired despun radiation pattern can be mounted at one or both poles of the satellite. Alternatively, a somewhat simple antenna can be used when the small volume described by a thick disk coincident with the satellite's equator is available exclusively as the antenna site. In this case, a radial transmission line (i.e., parallel disks excited at their center) exciting a ring of open-ended waveguide radiators⁸ represents that case when antenna performance is essentially uncompromised by its necessary integration into the satellite.

Electronically despun antennas are similar in that they usually consist of an array of low- to medium-gain antennas (i.e., 5- to 15-dB directivity) dispersed uniformly around the spin axis of the satellite and excited through a switch network that connects the transmitter or receiver to only those antennas that point most closely toward the center of the earth. An alternative, less common, electronically despun antenna consists of a circular array of low-gain elements simultaneously excited with equal power and phased to produce a unidirectional beam. The phase is varied to despin the beam as the satellite rotates. However, this type of antenna must occupy a complete cylindrical section of the satellite, usually on one end of the spacecraft. Consequently, electronically despun antennas usually consist of an array of several antennas which are sequentially switched to despin the radiation pattern. The details of these antennas are very well described in the literature. 67.9

Before leaving this topic, it is important to discuss mechanically despun antennas used on Intelsat-III¹⁰ and ATS-III¹¹ (Fig. 35-5a and b). Both of these employ reflector antennas and despin the radiation pattern by counterrotating the reflector (with respect to the satellite sense of rotation) so that its focal axis always points toward the center of the earth. The ATS-III antenna system (Fig. 35-4) consists of two antennas, one operating at 6.26 GHz and one operating at 4.85 GHz. Each antenna employs a parabolic cylinder illuminated by a collinear array of dipoles located on the focal line of the reflector. The latter reflects and converges the incident energy into a beam coincident with the focal axis of the parabola that generates the reflector's surface. Since the radiation pattern of a collinear array of dipoles is uniform in a plane perpendicular to the axis of the array, rotating the reflector about the dipole array rotates the antenna's beam in a plane perpendicular to the axis of the dipole array. The latter is installed coincident with the satellite spin axis so that counterrotation of the reflector results in a despun antenna. A unique feature of this antenna permits the reflector to be ejected if the rotary mechanism fails. Without the reflector the antenna has an omnidirectional radiation pattern permitting continued operation but with about 13dB reduction in directivity.

Intelsat-III also uses a rotating reflector to despin its radiated beam; however, the reflector surface is flat and oriented at a 45° angle with respect to the spin axis of the satellite. A horn antenna produces a high-directivity (~21-dB) beam pointed along the spin axis of the satellite toward the reflector. The latter redirects the beam perpendicular to, and causes it to rotate about, the satellite spin axis. This antenna, the ATS-III despun, and similar mechanically scanned devices continuously despin the radiation pattern with essentially no variation in the antenna's directive gain. Electronically despun antennas usually scan the radiated beam in a stepwise fashion; this usually produces a significant (from 1- to 3-dB) variation in the antenna's directive gain as it would be measured by a fixed terminal on the earth.

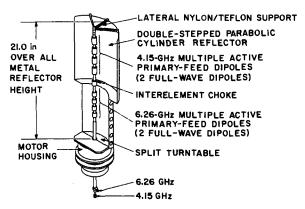


FIG. 35-5a ATS-III mechanically despun antenna.

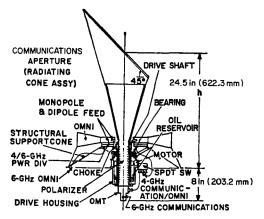


FIG. 35-5b ITS-III mechanically despun antenna.

35-3 ANTENNA POLARIZATION

Before considering three-axis stabilized satellites, it is important to discuss the antenna's polarization and why it plays an important role in satellite-antenna design. Recall that an antenna is defined by the polarization of the electromagnetic (EM) energy that it radiates. It is important to measure this polarization in the far zone of the antenna, that is, at distances sufficiently far from the antenna so that a further increase in this distance will not change the measured polarization. A distance $R = 2D^2/\lambda$ is customarily chosen as adequate for measuring the antenna's polarization and directive gain, where D is the antenna-aperture size and λ is the operating wavelength. The electric field direction defines the polarization of the EM energy.

Although essentially all polarization properties of EM waves play a role in satellite-antenna design, let us review those which are most important. For example, a linearly polarized (LP) antenna such as a dipole, oriented with its axis vertical (with

respect to the earth's surface), will radiate and receive vertically polarized signals. Conversely, it will neither radiate nor receive horizontally polarized signals. This phenomenon is commonly referred to by stating that an antenna will not radiate or receive cross-polarized signals, or that orthogonally polarized signals are rejected. This statement is not limited to LP antennas; circular and elliptically polarized EM waves and antennas have copolarized and cross-polarized properties identical to those of I.P. waves and antennas. 12 Circularly polarized (CP) waves have a right-hand sense (i.e., RHCP) if the electric field vector rotates in a clockwise sense as the wave is propagating away from the observer. The electric field vector of a left-hand circularly polarized (LHCP) wave rotates in a counterclockwise sense for receding waves. Changing both the direction of propagation (i.e., receding to approaching) and the sense of rotation (i.e., clockwise to counterclockwise) does not alter the polarization. Elliptically polarized waves result when the strength of the electric field varies as its direction rotates. In summary, virtually all antennas are, in fact, elliptically polarized, but the ellipticity is such that referring to them as CP or LP is an adequate descriptor. The important point is that copolarized antennas couple well to one another and crosspolarized antennas tend to reject one another's signals.

Now consider earth-satellite signal links when the frame of reference (i.e., vertical and horizontal) of the earth station will not, in general, coincide with the frame of reference (i.e., north and south) of the satellite. Since the satellite usually serves many users simultaneously and its antenna can assume only one polarization at any instant of time, it follows that when LP antennas are used, the earth station must adjust its frame of reference to coincide with the satellite's frame of reference. Although this is possible, it is far simpler to use CP satellite and earth-terminal antennas and remove the need to align them in order to maximize coupling between them. Consequently, it is not surprising that most satellite antennas are circularly polarized.

When an LP satellite antenna is used, orientation of the associated EM waves is altered as they propagate through the earth's ionosphere, ^{13,14} a phenomenon often referred to as the Faraday rotation effect. This rotation of LP waves is usually negligible (less than a few degrees) at frequencies above a few GHz. However, at frequencies below 1 GHz Faraday rotation effects can rotate the wave polarization more than 360°. Fortunately, the polarization of a CP wave is not altered by the Faraday rotation effect. Change in polarization due to transverse "static" magnetic fields along the propagation path is much smaller; therefore, circular polarization is preferred because CP waves propagate through the ionosphere with no essential change in polarization.

Most spacecraft and earth-terminal antennas are shared by the associated transmitter and receiver. Consequently, diplexer (or duplexer for a radar system) filtering is required. The use of antennas that are orthogonally polarized for transmitted and received radiation enhances the isolation between the transmitter and the receiver. For this and the foregoing reasons it is customary for satellite antennas to be opposite-sense circularly polarized for simultaneous transmit and receive functions.

35-4 THREE-AXIS STABILIZED SATELLITES

It is quite common to station-keep satellites whose attitude is completely controlled (i.e., orientation of the satellite's three principal axes is controlled). The satellite then takes on many of the characteristics of a relay station installed on a tower between

two earth terminals. In particular, high-gain directional antennas can be used to increase the link's data rate, or reliability, and decrease its vulnerability to external noise sources. The antenna can become much more sophisticated than antennas mounted on a satellite whose total mass is spinning. Suffice it to say, the antennas can be as common as a narrow-beam paraboloidal reflector mounted on a two-axis pedestal or as complicated and unique as the multiple-frequency, multiple-beam antenna 15,16 that makes the National Aeronautics and Space Administration's ATS-6 such a unique satellite.

Three-axis stabilization is achieved by despinning a "platform," or part of the spacecraft, or by including an inertia wheel as an integral part of the satellite. The gyroscopic action of the spinning spacecraft or inertia wheel can maintain the satellite's attitude within about 0.1° of a given frame of reference. The addition of a propulsion device keeps the spacecraft at a prescribed location in space.

35-5 EARTH-COVERAGE ANTENNA

Probably the most common spacecraft antennas are those that have a broad pattern with approximately the same directive gain over the earth as it is viewed from the satellite. These are called earth-coverage antennas and vary from simple dipole arrays to horn antennas, shaped-lens antennas, or shaped-reflector antennas. For low-altitude satellites, the angle θ_0 subtending the earth is relatively large (see Fig. 35-1); consequently the associated antenna may be a dipole, a helix, a log-periodic dipole, a backfire antenna, or a spiral antenna. Higher-altitude satellites usually use horn-type earth-coverage antennas. In all cases, however, the desired antenna pattern $P_0(\theta)$ should provide the same signal strength at its output port (terminal) as a constantpower signal source is moved on the surface of the earth within the satellite's FOV. At frequencies below about 5 GHz atmospheric attenuation is negligible, and $P(\theta)$ depends only on the variation in path length R (Fig. 35-1) from the satellite to the points on the earth's surface that are within the satellite's FOV. At frequencies above 10 GHz atmospheric attenuation becomes significant, and $P(\theta)$ should be adjusted accordingly. Atmospheric attenuation A depends on absorption by the water-vapor and oxygen molecules and particulate scattering principally due to rain. Total attenuation due to atmospheric effects is, to a first order, proportional to the path length L_a through the atmosphere. Since the height h_a of the atmosphere in the vicinity of an earth terminal is nearly constant, atmospheric attenuation is approximately inversely proportional to the cosine of the satellite elevation angle ϕ (Fig. 35-1).

The desired earth-coverage-antenna pattern $P(\theta)$ must equalize the change in R and A over the FOV; hence

$$P(\theta) \propto (R(\theta)/h)^2 A(\theta)$$
 (35-8)

To determine $A(\theta)$ refer to Fig. 35-6 and note that the path length L_a through the earth's atmosphere is given by

$$L_a = [(R_0 + h_a)^2 + R_0^2 - 2R_0(R_0 + h_a)\cos\alpha]^{1/2}$$
 (35-9)

$$L_a \approx h_a [1 + 4(R_0/h_a)^2 \sin^2(\alpha/2)]^{1/2}$$
 (35-10a)

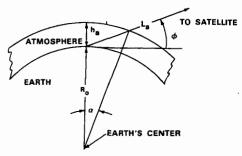


FIG. 35-6 Atmospheric path La.

where R_0/h_a is assumed $\gg 1$ and

$$\alpha \approx 90^{\circ} - \phi - \sin^{-1}(\cos\phi) \tag{35-10b}$$

Hence,

$$A(\theta) = e^{A_0(1-L_a/h_a)}$$
 (35-11)

where A_0 is the attenuation when $\phi = 90^\circ$. It remains to relate θ and ϕ and determine $R(\theta)$.

Referring to Fig. 35-1, note that

$$R = [R_0^2 + (R_0 + h)^2 - 2R_0(R_0 + h)\cos\beta]^{1/2}$$
 (35-12)

which reduces to

$$R = h\{1 + 4[(R_0/h)^2 + R_0/h] \sin^2(\beta/2)\}^{1/2}$$
 (35-13a)

where

$$\beta = 90 - \theta - \phi \tag{35-13b}$$

and

$$\phi = \cos^{-1} \left[(1 + h/R_0) \sin \theta \right]$$
 (35-15c)

The directivity of an antenna with a radiation pattern given by Eq. (35-8) can be calculated from

$$D = \frac{4\pi}{2\pi \int_0^{\theta_1} P(\theta) \sin \theta d\theta}$$
 (35-14)

where θ_1 is the edge of the coverage zone and $P(\theta) = 0$ for θ greater than θ_1 . Note that $P(\theta)$ is identical in all planes containing the $\theta = 0$ axis and that θ_1 is given by

$$\theta_1 = \sin^{-1} \left[R_0 \cos \phi_0 / (R_0 + h) \right]$$
 (35-15)

where ϕ_0 is the minimum satellite elevation angle within the desired FOV.

Having determined the optimum earth-coverage-antenna pattern $P(\theta)$, it is of interest to calculate the corresponding antenna directivity and directive gain and define a figure of merit F_{ϵ} for assessing the performance of a specific earth-coverage antenna.

Toward this end, consider an earth-coverage antenna on a synchronous satellite (i.e., h = 3.9 Mm). Operational experience indicates that $\phi_0 > 20^{\circ}$ prevents intolerable atmospheric-related diffraction effects and does not include intolerable atmospheric attenuation (i.e., atmospheric attenuation less than 1.5 dB at 10 GHz and less

than 3 dB at 45 GHz) at the higher frequencies. For $\phi_0 = 19^\circ$, Eq. (35-15) gives $\theta_0 = 8.2$. By using these values for θ_0 and ϕ_0 , the directivity of an optimum earth-coverage pattern is shown in Fig. 35-7 for $A_0 = 0$ and 1.0 dB. Note that increasing the atmospheric attenuation, in the zenith direction, from 0 to 1 dB changes the directivity

of the ideal earth-coverage pattern by about 0.4 dB. However, the directivity D (8.2°) toward the edge of the coverage area increases by 1.4 dB in order to overcome the increase in atmospheric attenuation.

A shaped earth-coverage pattern is shown to indicate a feasible approximation to the ideal pattern. Finite antenna-aperture size will permit only an approximation to the cusp (at $\theta = \theta_0$) in the ideal pattern. Nevertheless, pattern shaping that increases $D(\sim \theta_0)$ will enhance the overall system performance even if D(0) is reduced by 2 dB, as indicated by the shaped pattern (Fig. 35-7).

A typical conical-horn pattern is shown (Fig. 35-7) to indicate a primitive earth-coverage yet commonly used antenna. Note that for the shaped pattern $D(\theta_0)$ is about 4 dB greater than for the horn pattern. On the other hand, D(0) is about 1 dB greater for the horn than for the shaped pattern. This conflict in performance points out the need for a figure of merit Fe that will aid in assessing the performance of an earth-coverage antenna. For this reason, it is suggested that Fe be set equal to the maximum difference in the antenna directivity $D_a(\theta)$ and the directivity $D(\theta)$ of the ideal antenna pattern. That is,

$$F_e = \max[D_a(\theta) - D(\theta)] / \theta = 0$$
 (35-16)

where $D(\theta)$ and $D_a(\theta)$ are expressed in decibels. Therefore, F_e is negative with a maximum possible value of zero.

To estimate the maximum possible $F_{\mathbf{e}}$ assume that the antenna aperture is

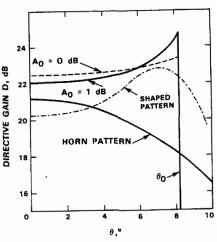


FIG. 35-7 Directive gain of an earth-coverage antenna on a synchronous satellite.

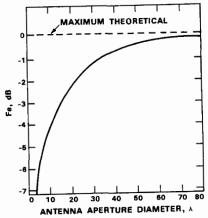


FIG. 35-8 Earth-coverage-antenna figure of merit.

inscribed in a sphere of radius a and that a set of spherical waves, with wave number $N < 2\pi a/\lambda$, is used to approximate $P(\theta)$. The directivity $D_0(\theta)$ of the pattern generated by the finite set of spherical waves is then used to compute $D_a(\theta)$ and F_e . Since the synthesis procedure guarantees a least-mean-square fit to $P(\theta)$ and the antennaperture excitation is prevented from exciting supergain waves¹⁷ (i.e., $N < 2\pi a/\lambda$), the computed F_e is maximum for the given-size antenna aperture D = 2a. The maximum value of F_e shown in Fig. 35-8 was calculated by using this procedure.

35-6 SPOT-BEAM COVERAGE

Satellite antennas designed to provide high gain to a point within view of the satellite are required to have directivity greater than that of a simple fixed-beam earth-coverage antenna. In the case of a satellite in synchronous orbit, the theoretical maximum directivity of an earth-coverage antenna is about 24 dB; practical considerations limit its directivity to about 20 dB. Hence, for a directivity greater than 20 dB and an earth FOV, the synchronous-satellite antenna must produce a beam that scans or steps over the earth or the FOV. If a sequential raster scan is desired, the antenna might be steered mechanically or electronically over the FOV. However, for pseudo-random coverage of the FOV, step scan at microsecond rates is usually preferred. When step scan is preferred, the FOV is covered by several overlapping beam footprints. The minimum gain provided by N beams, designed to cover the FOV, is required to estimate system performance and is the subject of this section.

Since the cross section of a high-gain antenna beam is usually circular, the following analysis assumes that N beams with circular cross section are arranged in a triangular grid with beam-axis-to-beam-axis angular separation θ_b (see Fig. 35-9). It is customary to indicate the beams by their uniquely defined hexagonal coverage area. For

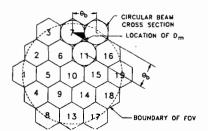


FIG. 35-9 Spot-beam coverage of the earth.

this reason, the beam coverage areas are indicated by a contiguous array of "beams" with a hexagonal cross section. Numbering of the beams is for identification; the numbers have no other meaning. A circular FOV is assumed; however, this analytic method can be readily extended to any FOV with a noncircular boundary. The analysis considers the black area in Fig. 35-9 and assumes that the directivity variation over this shaded area is replicated over the entire FOV. An edge-correction effect will be discussed following detailed consideration of the black area.

The analysis assumes a gaussian-shaped beam and determines θ_b and beam directivity D_0 that maximize the minimum directivity D_m over the black area. It follows that D_m is also the maximum value of the minimum directivity over the entire FOV with the possible exception of some small areas along the boundary of the FOV.

Since the useful directivity D of a beam will be within 5 dB of the beam directivity D_0 , the directivity of all beams can be adequately represented by the function

$$D = D_0 e^{-\alpha(2\theta/\theta_1)^2} \tag{35-17}$$

where θ_1 = the half-power beamwidth (HPBW) of the beam. It is further assumed

that when θ_1 is expressed in radians,

$$D_0 = \eta \, \frac{4\pi}{\theta_1^2} \tag{35-18}$$

where η ranges from about ½ to ¾. (Experimental data indicate that the antenna efficiency of a center-fed parabola is about 93 η percent.) By noting that $D = D_0/2$ when $\theta = \theta_1/2$ and using Eq. (35-17),

$$\alpha = \ln 2 = 0.693 \tag{35-19}$$

and

$$D = D_0 e^{-2.77(\theta/\theta_1)^2} ag{35-20}$$

Using Eqs. (35-18) and (35-20) gives an alternative expression for D, namely,

$$D = D_0 e^{-0.22\theta^2(D_0/\eta)} ag{35-21}$$

Over the FOV (not including the boundary), D_m occurs at the center of the equilateral triangle formed by the center of three adjacent beam footprints. The angle θ_m between the axis of the three adjacent beams and the direction of minimum direction gain is given by

$$\theta_m = \frac{\theta_b}{\sqrt{3}} \tag{35-22}$$

Hence, from Eqs. (35-22) and (35-21)

$$D_{-} = D_0 e^{-0.074 \sigma_D^2 (D_0/\eta)} = D_0 e^{-BD_0}$$
 (35-23)

Differentiating D_m with respect to D_0 gives

$$\frac{\partial D_m}{\partial D_0} = (1 - BD_0)e^{-BD_0} \tag{35-24}$$

where $B = 0.074\theta_0^2/\eta$. From Eq. (35-24) D_m is maximum when

$$D_0 = \frac{\eta}{0.074\theta_0^2} \tag{35-25}$$

 D_{max} , the maximum value of D_m , is given by

$$D_{\max} = D_0 e^{-1} \tag{35-26}$$

Expressing Eq. (35-26) in decibels gives

$$D_{\text{max}} = D_0 \, (\text{dB}) \, - \, 4.34 \, \text{dB} \tag{35-27}$$

Hence, for maximum gain over the FOV, the crossover level between three adjacent beams is -4.34 dB with respect to D_0 , the directivity of a beam. For most multiple-beam antennas (MBAs), spillover loss is large when θ_b is chosen to produce approximately 4 dB less gain in the direction of the intersection of three adjacent beams than in the beam's axial direction. Increasing θ_b above this value reduces spillover loss and reduces D_m . Consequently, θ_b must be chosen to achieve a best compromise between spillover loss and maximum D_m .

By returning to Eq. (35-21), the crossover level D_2 between two adjacent beams

is given by

$$D_2 = D_0 e^{-0.22(D_0/\eta)(\theta b/2)^2}$$
 (35-28)

Substituting Eq. (35-25) into Eq. (35-28) gives

$$D_2 = D_0 e^{-3/4}$$

 $D_2 \text{ (dB)} = D_0 \text{ (dB)} - 3.25 \text{ dB}$ (35-29)

or

Hence the crossover level between two adjacent beams is 1.1 dB higher than the crossover level between three adjacent beams.

Statistical Distribution of D

Having knowledge of D_m is not always satisfying to the system designer because it represents a worst case. Whenever the estimated performance indicates that D_m may not be large enough, it is important to address the probability that the worst case will occur. With this probability placed in perspective with the foregoing analysis, it is important to determine the probability that $D > D' \ge D_m$. Toward this end, consider an enlargement (Fig. 35-10) of the black area in Fig. 35-9. The probability that D > D is given by

$$P(D \ge D_2) = \frac{2(\pi/12)(\theta_0/2)^2}{(\theta_b/2)(\theta_b/2\sqrt{3})} = 0.907$$
 (35-30)

Hence less than 10 percent of the FOV has a directivity less than $D_2 = D_0 - 3.25$ dB. The probability that D > D' can be found for $D' > D_2$ [i.e., $\theta_1 \le \theta_b/2$)] by first finding the probability that $\theta < \theta_1$. That is,

$$P(\theta < \theta_1) = P(D > D') = 3.628 \left(\frac{\theta'}{\theta_b}\right)^2$$
 (35-31)

From Eq. (35-21)

$$D' = D_0 e^{-0.22(D_0/\eta)\theta^2}$$
 (35-32)

Solving Eq. (35-32) for θ'^2 , substituting in Eq. (35-31), and using Eq. (35-25) give

$$P(D \ge D') = 1.22 \ln \left(\frac{D_0}{D'} \right)$$
 (35-33)

By using Eq. (35-33) and a linear interpolation for $\theta_m > \theta > \theta_0$, the probability that $D \ge D'$ is given in Fig. 35-11.

The foregoing derives D_{max} in terms of D_0 . It remains to determine D_0 in terms of N, the number of beams required to cover the FOV. By assuming a hexagonal FOV, N is given by

$$N = 1 + \sum_{m=1}^{(M-1)/2} 6m$$
 (35-34)

where M, the maximum number of beams in a row (Fig. 35-9), is given by

$$M = \frac{\psi}{\theta_b} + 1 \tag{35-35}$$

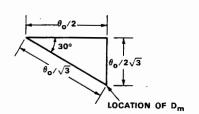


Fig. 35-10 Characteristic area of spotbeam coverage.

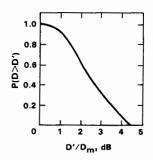


FIG. 35-11 Distribution of directivity of a multiple-beam antenna.

and ψ is the angle subtended by the major diagonal of the FOV and is measured at the antenna. From Eqs. (35-25) and (35-35)

$$M = int(1 + \psi \sqrt{0.07D_0/\eta})$$
 (35-36)

hence,

$$D_0 = \left(\frac{M-1}{\psi}\right)^2 \frac{\eta}{0.074} \tag{35-37}$$

For a synchronous satellite, the earth subtends an angle $\psi = 17.2^{\circ}$ (0.3 rad); therefore, from Eq. (35-37) the maximum directivity of a multiple-beam antenna designed to cover the earth FOV with spot beams is given by

$$D_0 = 150(M-1)^2 \eta \tag{35-38}$$

In accordance with Eq. (35-27) the corresponding minimum gain $D_m = 55(M - 1)^2 n$.

The foregoing derivation considered only those minimum-directivity points within the FOV. Usually the desired FOV does not conform to that described by the outer boundary of the footprints of the beams that cover the edge of the FOV. For example, for a circular FOV, arranging the beam footprints on a triangular grid results in the minimum number of beams to cover the circular area, but the resultant array is not hexagonal. To determine the number of beams required and their configuration, refer to Fig. 35-9 and note the location of D_m . Since the hexagonal array has sixfold symmetry, a point between beams 2 and 3 determines the edge of the FOV where $D = D_m$. As more beams are added to the array (i.e., as the FOV gets larger or as larger values of D_m are desired), the hexagonal grid gives poorer coverage along the edge of the FOV. Improved coverage is obtained by adding beams just at those points along the edge of the FOV where $D < D_m$ rather than by completing another ring of the hexagonal array of beams. The maximum directivity D_0 and the minimum directivity D_m , for a set of N beams arranged on a triangular grid and designed to cover the earth's disk from a synchronous satellite, are given in Table 35-1. The number of beams M in a diagonal of the hexagon pattern from which the set of N beams is derived is also given. For example, the 31-beam array was obtained by adding 2 beams to each side of a 19-beam array; hence M = 5 (for 19 beams) and N = 19 +

TABLE 35-1 Estimated Directivity, decibels

			$\eta = 0.5$	
M	N	Κ	D _o	D _{min}
3	7	2.30	26.0	21.7
3	13	3.06	28.4	24.1
5	19	4.16	31.1	26.8
5	31	5.04	32.8	28.5
7	37	5.76	34.0	29.7
7	43	6.10	34.5	30.2
7	55	7.02	35.7	31.4
9	61	7.36	36.1	31.8
9	73	8.08	36.9	32.6
9	85	9.02	37.8	33.5
11	91	9.22	38.0	33.7
11	97	9.44	38.3	34.0
13	109	10.26	39.0	34.7
13	121,127	11.0	39.6	35.3
15	139	11.36	39.9	35.6

 $2 \times 6 = 31$. The beam spacing θ_b is obtained from K in Table 35-1 and the relationship

$$\theta_b = 17.2^{\circ}/K$$
 (35-39)

In summary, coverage of an area or FOV by exciting any one of N beams can be achieved by arranging the beams in a triangular grid with angular spacing θ_b between adjacent beams. The minimum directivity D_m over the FOV is maximized when $\theta_b = 3.67 \sqrt{\eta/D_0}$; D_m is 4.3 dB less than D_0 , the directivity of a single beam. If adjacent beams are excited simultaneously, ^{18,19} D_m can increase by more than 2 dB.

When a single feed is excited, an MBA usually has low antenna efficiency. This low efficiency is due to large spillover loss and usually is approximately 35 percent. This decrease in D_m can be mitigated by exciting three or seven feeds (ports) to produce a single beam. In the case of seven feeds, the outer ring of six feeds is excited with significantly less amplitude than the center feed. For example, feeds numbered 1, 2, 4, 5, 6, 9, and 10 would be excited to produce a beam instead of exciting just feed number 5 (see Fig. 35-9). Exciting feeds numbered 5, 6, 9, 10, 11, 14, and 15 would move the beam an angular distance θ_b . Exciting seven feeds in this manner will increase D_m up to 2 dB and lower sidelobes to about -25 dB.

It is also possible to increase D_m by using three or more lenses (or reflectors) to form the beams. In this case, adjacent beams are produced by different lens apertures; hence the apertures of all feed horns can be enlarged, reducing spillover loss without changing θ_b , and hence increasing D_m . It is essential that the aperture diameter and the focal length be varied to optimize antenna gain and D_m .

35-7 CROSS-LINK ANTENNAS

Communication links between satellites are becoming more common for a number of reasons. Where initially satellites were used to relay communications between two earth terminals worldwide or even continent to continent, communications require more than a single satellite relay station. If communication between satellites is carried out through an earth station (i.e., a gateway), the round-trip delay, the vulnerability of the earth station, and the inherent insecurity of the earth-satellite link versus that of a satellite cross link motivate and often justify the use of cross links. Consequently, this section is addressed to a description of cross-link-antenna characteristics and some considerations essential to their design.

Although satellite cross links can operate at other frequencies (e.g., UHF), a 1-GHz band at 60 GHz (designated by international agreement) set aside for satellite-to-satellite communications is most attractive. Incidentally, operating a radiating system at frequencies different from those designated by international agreement and national law is acceptable to all provided there is no interference with those who have been allocated a frequency band. Consequently, it is wise to choose an appropriate frequency band within the designated frequency bands and obtain a frequency allocation.

The 60-GHz band has much more bandwidth than lower-frequency bands and can accommodate very-high-data-rate communications. In addition, the earth's atmosphere serves to reduce interference of human origin if not to eliminate it. For example, the attenuation of EM waves at frequencies between 55 and 65 GHz is on the order of 10 dB/km (see Fig. 35-12) at the earth's surface and decreases with increas-

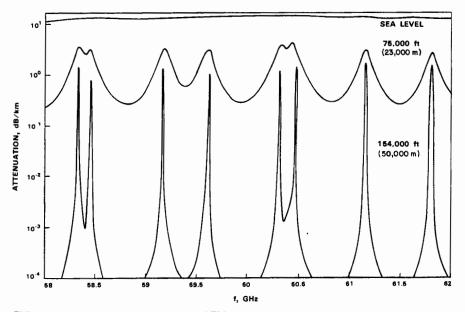


FIG. 35-12 Atmospheric attenuation of EM waves.

ing altitude above mean sea level. Wave attenuation becomes negligible at altitudes higher than 500 km (310 mi). Consequently, the cross links between satellites at altitudes greater than 500 km are shielded from signals or noise generated on or near the earth's surface. Since airplanes fly at altitudes of less than 25 km (82,000 ft), even high-flying platforms can experience substantial atmospheric attenuation unless the spacecraft is near the aircraft's zenith direction.

The natural shield provided by the earth's atmosphere is enhanced by the directivity of cross-link antennas. The short wavelength permits directive (~1°-HPBW) beams from a relatively small- (~0.5-m-) diameter antenna aperture. Thus, bandwidth, wave attenuation, and antenna directivity considered together with the difficulty with which high-power RF signals can be generated lead to 60 GHz as a preferred cross-link frequency band. Similar reasoning leads to the conclusion²⁰ that extremely high frequency (EHF) is the preferred operating frequency of military (and perhaps nonmilitary) satellite communication systems.

Having chosen a frequency of operation, the designer must determine the type of antenna and its gain. If it is assumed that the antenna will be steered in the direction of the intended satellite station, it is necessary to develop a trade-off algorithm capable of evaluating an array, a paraboloid, or some other design. For the purposes of this chapter, a conventional paraboloid will be compared with an array of elements, each of which has a beam pattern that defines the desired FOV. The paraboloid is steered by pointing it in the desired direction; the array is steered by appropriate phasing. Furthermore, the array aperture is square with side d, and the paraboloid has a circular aperture with diameter d. The number of elements in the array depends on the FOV. If the elements are assumed to be horn antennas arranged on a square grid, the number of elements versus antenna size is given in Fig. 35-13 for various angular (α) fields of view.

By assuming a receiver noise temperature of 1500 K, a 64-Mm (40,000-mi) link between satellites, an energy-per-bit-to-noise power-density ratio $E_b/N_0 = 13$ dB, and an antenna system efficiency of 10 percent for the array and 20 percent for the

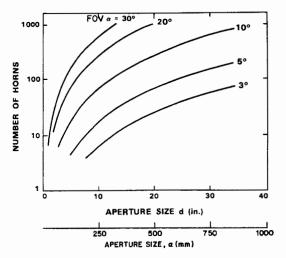


FIG. 35-13 Number of array elements.

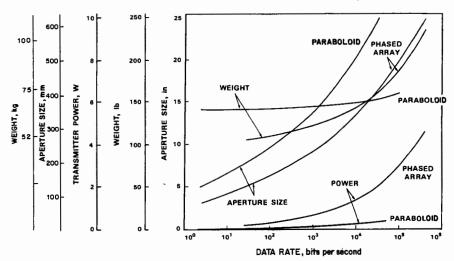


FIG. 35-14 Phased-array and paraboloid characteristics.

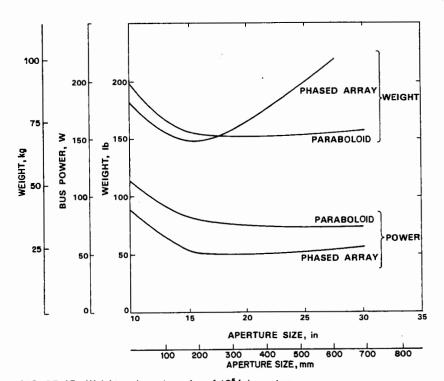


FIG. 35-15 Weight and aperture size of 105-b/s system.

paraboloid, the antenna and transmitter weight and power were estimated as a function of the aperture size and the data rate. The results shown in Figs. 35-14 and 35-15 indicate that the paraboloid requires about 40 percent more bus power but can be substantially lighter than the array. However, it is definitely clear (Fig. 35-14) that the paraboloid both is lighter and requires much less transmitter power than the array when the data rate exceeds about 10,000 bits per second (b/s). It is further clear that if an aperture size of about 0.5 m is acceptable, the paraboloid is probably the best choice for a cross-link antenna.

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Earth Station Antennas

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36-1					
36-2	Single-Beam Earth Station Antennas 36-3				
	Axisymmetric Dual-Reflector Antennas 36-3				
	Prime-Focus-Fed Paraboloidal Antenna 36-7				
	Offset-Fed Reflector Antennas 36-8				
36-3	Multiple-Beam Earth Station Antennas 36-10				
	Spherical Reflector 36-10				
	Torus Antenna 36-11				
	Offset-Fed Multibeam Cassegrain				
	Antenna 36-13				
36-4	Angle Tracking 36-14				
	Single-Channel Monopulse 36-14				
	Steptrack 36-14				
36-5					
	Appendix A: Earth Station Sidelobe				
	Requirements 36-16				
	Appendix B: Aperture Distributions 36-17				
	-				

36-1 INTRODUCTION AND GENERAL CHARACTERISTICS

An earth-station-antenna system consists of many component parts such as the receiver, low-noise amplifier, and antenna. All the components have an individual role to play, and their importance in the system should not be minimized. The antenna, of course, is one of the more important component parts since it provides the means of transmitting signals to the satellite and/or collecting the signal transmitted by the satellite. Not only must the antenna provide the gain necessary to allow proper transmission and reception, but it must also have radiation characteristics which discriminate against unwanted signals and minimize interference into other satellite or terrestrial systems. The antenna also provides the means of polarization discrimination of unwanted signals. The operational parameters of the individual communication system dictate to the antenna designer the necessary electromagnetic, structural, and environmental specifications for the antenna.

Antenna requirements can be grouped into several major categories, namely, electrical or radio-frequency (RF), control-system, structural, pointing- and tracking-accuracy, and environmental requirements, as well as miscellaneous requirements such as those concerning radiation hazards, primary-power distribution for deicing, etc. Only the electrical or RF requirements will be dealt with in this chapter.

The primary electrical specifications of an earth station antenna are gain, noise temperature, voltage standing-wave ratio (VSWR), power rating, receive-transmit group delay, radiation pattern, polarization, axial ratio, isolation, and G/T (antenna gain divided by the system noise temperature). All the parameters except the radiation pattern are determined by the system requirements. The radiation pattern should meet the minimum requirements set by the International Radio Consultative Committee (CCIR) of the International Telecommunications Union (ITU) and/or national regulatory agencies such as the U.S. Federal Communications Commission (FCC).

Earth station antennas operating in international satellite communications must have sidelobe performance as specified by INTELSAT standards or by CCIR Recommendation 580-1 (see Fig. 36-1 and Appendix A).

The CCIR standard specifies the pattern envelope in terms of allowing 10 percent of the sidelobes to exceed the reference envelope and also permits the envelope to be adjusted for antennas whose aperture is less than 100 wavelengths (100λ). The reference envelope is given by

$$G = [49 - 10 \log (D/\lambda) - 25 \log \theta]$$
 dBi $D \le 100\lambda$
= $(29 - 25 \log \theta)$ dBi $D > 100\lambda$

This envelope takes into consideration the limitations of small-antenna design and is representative of measured patterns of well-designed dual-reflector antennas.

Earth station antennas can be grouped into two broad categories: single-beam antennas and multiple-beam antennas. A single-beam earth station antenna is defined as an antenna which generates a single beam that is pointed toward a satellite by means of a positioning system. A multiple-beam earth station antenna is defined as an antenna which generates multiple beams by employing a common reflector aperture with multiple feeds illuminating that aperture. The axes of the beams are determined by the location of the feeds. The individual beam identified with a feed is pointed toward a satellite by positioning the feed without moving the reflector.

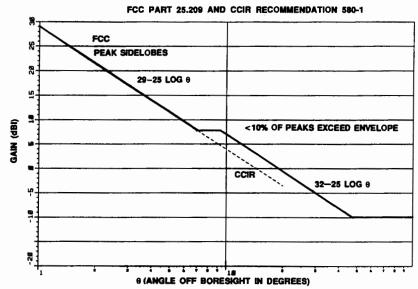


FIG. 36-1 Sidelobe envelope as defined by CCIR Recommendation 580-1 and FCC.

36-2 SINGLE-BEAM EARTH STATION ANTENNAS

Single-beam antenna types used as earth stations are paraboloidal reflectors with focal-point feeds (prime-focus antenna), dual-reflector antennas such as the Cassegrain and gregorian configurations, horn reflector antennas, offset-fed paraboloidal antennas, and offset-fed multiple-reflector antennas. Each of these antenna types has its own unique characteristics, and the advantages and disadvantages have to be considered when choosing one for a particular application.

Axisymmetric Dual-Reflector Antennas

The predominant choice of designers of earth station antennas has been the dualreflector Cassegrain antenna. Cassegrain antennas can be subdivided into three primary types:

1 The classical Cassegrain geometry^{1,2} employs a paraboloidal contour for the main reflector and a hyperboloidal contour for the subreflector (Fig. 36-2). The paraboloidal reflector is a point-focus device with a diameter D_p and a focal length f_p . The hyperboloidal subreflector has two foci. For proper operation, one of the two foci is the real focal point of the system and is located coincident with the phase center of the feed; the other focus, the virtual focal point, is located coincident with the focal

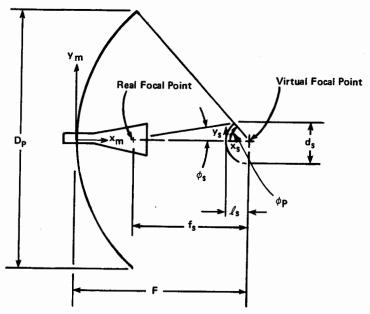


FIG. 36-2 Geometry of the Cassegrain antenna system.

point of the main reflector. The parameters of the Cassegrain system are related as follows:

$$\phi_p = 2 \tan^{-1} (0.25 D_p / F_p)$$
 (36-1)

$$f_s/d_s = 0.5(\cot \phi_p + \cot \phi_s)$$
 (36-2)

$$\ell_s/f_s = 0.5(1 - \{\sin \left[0.5(\phi_p - \phi_s)\right]/\sin \left[0.5(\phi_p + \phi_s)\right]\})$$
 (36-3)

In a typical design, the parameters f_p , D_p , f_s , and ϕ_s are chosen, and the remaining three parameters are then calculated.

The contours of the main reflector and subreflector are given by

Main reflector:
$$y_m^2 = 4F_p x_m$$
 (36-4)

Subreflector:
$$(y_s/b)^2 + 1 = (x_s/a + 1)^2$$
 (36-5)

where

$$a = (f_s/2e)$$
 $b = a\sqrt{e^2 - 1}$
 $e = \sin [0.5(\phi_p + \phi_s)]/\sin [0.5(\phi_p - \phi_s)]$

The quantities a, b, and e are half of the transverse axis, half of the conjugate axis, and the eccentricity parameters of the hyperboloidal subreflector respectively.

2 The geometry of this type consists of a paraboloidal main reflector and a special-shaped quasi-hyperboloidal subreflector. 3.4.5.6.7 The geometry in Fig. 36-2 is appropriate for describing this antenna. The main difference between this design and the classical Cassegrain above is that the subreflector is shaped so that the overall efficiency of the antenna has been enhanced. This technique is especially useful with antenna diameters of approximately 60 to 300 wavelengths. The subreflector shape

may be solved for by geometrical optics (GO) or by diffraction optimization, and then, by comparing the required main-reflector surface to a paraboloidal surface, the best-fit paraboloidal surface is found. Aperture efficiencies of 75 to 80 percent can be realized by a GO design and efficiencies of 80 to 95 percent by diffraction optimization of the subreflector (Fig. 36-3).

3 This type is a generalization of the Cassegrain geometry consisting of a special-shaped quasi-paraboloidal main reflector and a shaped quasi-hyperboloidal sub-reflector. 9,10,11,12 Green boserved that in dual-reflector systems with high magnification—essentially a large ratio of main-reflector diameter to subreflector diameter—the distribution of energy (as a function of angle) is largely controlled by the subreflector curvature. The path length or phase front is dominated by the main reflector (see Fig. 36-4). Kinber and Galindo 10,11 found a method for simultaneously solving for the main-reflector and subreflector shapes to obtain an exact solution for both the phase and the amplitude distributions in the aperture of the main reflector of an axisymmetric dual-reflector antenna. Their technique, based on geometrical optics, is highly mathematical and involves solving two simultaneous, nonlinear, first-order, ordinary differential equations. Figure 36-5 gives the geometry showing the path of a single ray. The feed phase center is located as shown, and the feed is assumed to have a power radiation pattern $I(\theta_1)$. The parameters α and β represent respectively the distance of the feed phase center from the aperture plane and the distance between

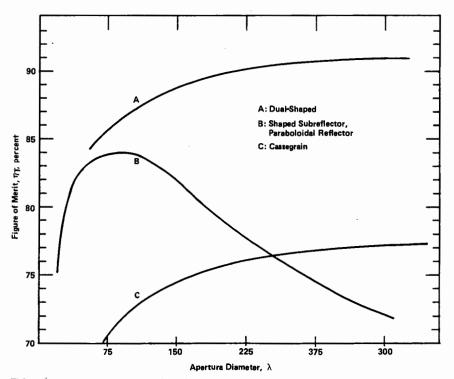


FIG. 36-3 Antenna of figure of merit versus aperture diameter.

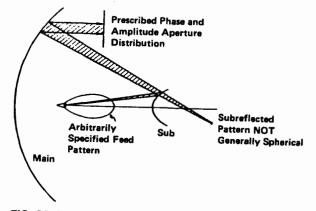


FIG. 36-4 Circularly symmetric dual-shaped reflectors.

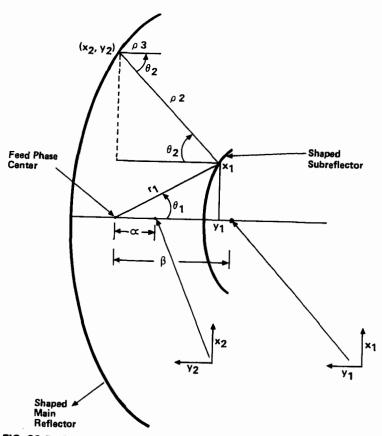


FIG. 36-5 Dual-shaped reflector geometry.

the feed phase center and the back surface of the subreflector. The constraints to the dual-reflector system are as follows:

a The phase distribution across the main-reflector aperture plane will be uniform, or

$$r_1 + p_2 + p_3 + C_p(\theta_1) = \text{constant}$$
 (36-6)

for $0 \le \theta_1 \le \theta_{1_{max}}$. $C_p(\theta_1)$ represents the phase distribution across the primary-feed radiation pattern in units of length.

b The feed energy, or ray bundles intercepted and reflected by the subreflector, is conserved and redistributed according to a specified aperture distribution, or

$$I(\theta_1) \sin(\theta_1) d\theta_1 = C \cdot I(X_2) X_2 dX_2$$
 (36-7)

where $I(X_2)$ represents the power radiation distribution across the main-reflector aperture and C represents a constant which is determined by applying the conservation-of-power principle.

$$\int_0^{\theta_{1\text{max}}} I(\theta_1) \sin \theta_1 \ d\theta_1 = C \int_{X_{2\text{min}}}^{X_{2\text{max}}} I(X_2) X_2 \ dX_2$$
 (36-8)

The lower limit of integration over the main reflector can be arbitrarily chosen so that only an annular region of the main reflector is illuminated.

c Snell's law must be satisfied at the two reflecting surfaces, which yields

$$\frac{dY_1}{dX_1} = \tan\left(\frac{\theta_1 - \theta_2}{2}\right) \tag{36-9}$$

$$\frac{dY_2}{dX_2} = -\tan\left(\frac{\theta_2}{2}\right) \tag{36-10}$$

Solving Eqs. (36-7) through (36-10) simultaneously results in a nonlinear, first-order differential equation of the form

$$\frac{dY_1}{dX_2} = f(\theta_1, \theta_2, \alpha, \beta, \text{ etc.})$$
 (36-11)

which leads to the cross sections of each reflector when subject to the boundary condition Y_1 ($X_2 = X_{2max}$) = 0, where X_2 is the independent variable. Equation (36-11) can be solved numerically by using an algorithm such as a Runge-Kutta, order 4.

The above procedure is based on GO, but it is evident that the assumptions of GO are far from adequate when reflectors are small in terms of wavelengths. An improvement in the design approach is to include the effects of diffraction. Clarricoats and Poulton⁷ reported a gain increase of 0.5 dB for a diffraction-optimized design over the GO design with a 400 λ -diameter main reflector and 40 λ -diameter subreflector.

Prime-Focus-Fed Paraboloidai Antenna

The prime-focus-fed paraboloidal reflector antenna is also often employed as an earth station antenna. For moderate to large aperture sizes, this type of antenna has excellent sidelobe performance in all angular regions except the spillover region around the

edge of the reflector. The CCIR sidelobe specification can be met with this type of antenna. The reader is referred to Chap. 17 for more information on paraboloidal antennas.

Offset-Fed Reflector Antennas

The geometry of offset-fed reflector antennas has been known for many years, but its use has been limited to the last decade or so because of its difficulty in analysis. Since the advent of large computers has allowed the antenna engineer to investigate theoretically the offset-fed reflector's performance, this type of antenna will become more common as an earth station antenna.

The offset-fed reflector antenna can employ a single reflector or multiple reflectors, with two-reflector types the more prevalent of the multiple-reflector designs. The offset front-fed reflector, consisting of a section of a paraboloidal surface (Fig. 36-6), minimizes diffraction scattering by eliminating the aperture blockage of the feed and feed-support structure. Sidelobe levels of $(29-25\log\theta)$ dBi can be expected from this type of antenna (where θ is the far-field angle in degrees) with aperture efficiencies of 65 to 80 percent. The increase in aperture efficiency as compared with an axisymmetric prime-focus-fed antenna is due to the elimination of direct blockage. For a detailed discussion of this antenna, see C. A. Mentzer.¹³

Offset-fed dual-reflector antennas exhibit sidelobe performance similar to that of the front-fed offset reflector. Two offset-fed dual-reflector geometries are used for earth station antennas: the double-offset geometry shown in Fig. 36-7a and the open

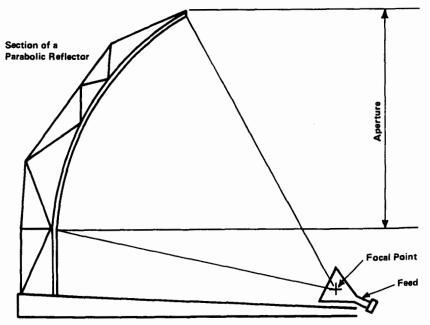


FIG. 36-6 Basic offset-fed paraboloidal antenna.

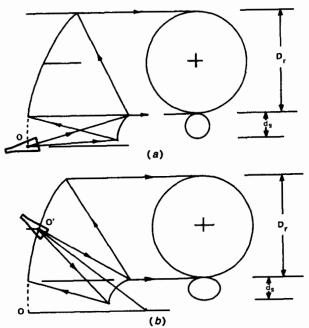


FIG. 36-7 Offset dual-reflector geometries. (a) Double-offset geometry (feed phase center and paraboloidal vertex at 0). (b) Open cassegrainian geometry (feed phase center located at 0; paraboloidal vertex, at 0).

Cassegrain geometry introduced by Cook et al. ¹⁴ of Bell Laboratories and shown in Fig. 36-7b. In the double-offset geometry, the feed is located below the main reflector, and no blocking of the optical path occurs. In contrast, the open Cassegrain geometry is such that the primary feed protrudes through the main reflector; thus it is not completely blockage-free. Nevertheless, both of these geometries have the capability of excellent sidelobe and efficiency performance.

The disadvantage of offset-geometry antennas is that they are asymmetric. This leads to increased manufacturing cost and also has some effect on electrical performance. The offset-geometry antenna, when used for linear polarization, has a depolarizing effect on the primary-feed radiation and produces two cross-polarized lobes within the main beam in the plane of symmetry. When it is used for circular polarization, a small amount of beam squint whose direction is dependent upon the sense of polarization is introduced. The beam squint is approximately given by $^{15} \psi_s = \arcsin [\lambda \sin (\theta_0)/4\pi F]$, where θ_0 is the offset angle, λ is the free-space wavelength, and F is the focal length. The effects of beam squint versus polarization for circular polarization and the relatively high off-axis cross-polarization performance for linear polarization must be considered by the antenna designer, since these characteristics may present a problem for the overall earth station operation. The offset dual-reflector geometry has the capability of employing a feed tilt to correct for the polarization problems associated with the offset geometry resulting in the equivalent polarization performance of an axially symmetric antenna. 15a,15b,15c

Galindo-Israel, Mittra, and Cha¹⁶ have studied the offset dual-reflector geometry for high-aperture-efficiency applications. Their analytical techniques are reported to result in efficiencies in the 80 to 90 percent range (see Ref. 16a). Mathematically, the offset geometry, when formulated by the method used in designing axisymmetric dual reflectors, results in a set of partial differential equations for which there is no exact GO solution. The method of Galindo-Israel et al. is to solve the resultant partial differential equations as if they were total differential equations. Then, by using the resultant subreflector surface, the main-reflector surface is perturbed until a constant aperture phase is achieved. The reader is referred to Galindo-Israel^{16b} for a discussion of the synthesis of offset-shaped reflector antennas.

36-3 MULTIPLE-BEAM EARTH STATION ANTENNAS

During the past few years there has been an increasing interest in receiving signals simultaneously from several satellites with a single antenna. This interest has prompted the development of several multibeam-antenna configurations which employ fixed reflectors and multiple feeds. The antenna engineering community, of course, has been investigating multibeam antennas for many years. In fact, in the middle of the seventeenth century, Christian Huygens and Sir Isaac Newton first studied the spherical mirror, and the first use of a spherical reflector as a microwave antenna occurred during World War II. More recently, the spherical-reflector, the torus-reflector, and the dual-reflector geometries, all using multiple feeds, have been offered as antennas with simultaneous multibeam capability. Chu¹⁷ in 1969 addressed the multiple-beam spherical-reflector antenna for satellite communication, Hyde¹⁸ introduced the multiple-beam torus antenna in 1970, and Ohm¹⁹ presented a novel multiple-beam Cassegrain-geometry antenna in 1974. All three of these approaches, as well as variations of scan techniques for the spherical reflector, are discussed below.

Spherical Reflector

The properties, practical applications, and aberrations of the spherical reflector are not new to microwave-antenna designers. The popularity of this reflector is primarily due to the large angle through which the radiated beam can be scanned by translation and orientation of the primary feed. This wide-angle property results from the symmetry of the surface. Multiple-beam operation is realized by placing multiple feeds along the focal surface. In the conventional use of the reflector surface, the minimum angular separation between adjacent beams is determined by the feed-aperture size. The maximum number of beams is determined by the percentage of the total sphere covered by the reflector. In the alternative configuration described below, these are basically determined by the f/D ratio and by the allowable degradation in the radiation pattern.

In the conventional use of the spherical reflector, the individual feed illuminates a portion of the reflector surface so that a beam is formed coincident to the axis of the feed. The conventional multibeam geometry is shown in Fig. 36-8. All the beams have

similar radiation patterns and gains, although there is degradation in performance in comparison with the performance of a paraboloid. The advantage of this antenna is that the reflector area illuminated by the individual feeds overlaps, reducing the surface area for a given number of beams in comparison with individual single-beam antennas.

The alternative multibeam-spherical-reflector geometry is shown in Fig. 36-9. For this geometry, each of the feed elements points toward the center of the reflector, with the beam steering accomplished by the feed position. This method of beam generation leads to considerable increase in aberration, including coma; therefore, the radiation patterns of the off-axis beams are degraded with respect to the on-axis beam. This approach does not take advantage of the spherical-reflector properties that exist in the conventional approach. In fact, somewhat similar results could be achieved with a paraboloidal reflector with a large f/D.

Torus Antenna

The torus antenna is a dual-curvature reflector, capable of multibeam operation when it is fed with multiple feeds similar to those of the conventional spherical-reflector geometry. The feed-scan plane can be inclined to be in the orbital-arc plane, allowing the use of a fixed reflector to view geosynchronous satellites. The reflector has a circular contour in the scan plane and a parabolic contour in the orthogonal plane (see Fig. 36-10). It can be fed in either an axisymmetric or an offset-fed configuration.

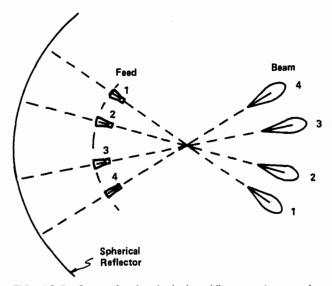


FIG. 36-8 Conventional spherical multibeam antenna using extended reflector and multiple feeds.

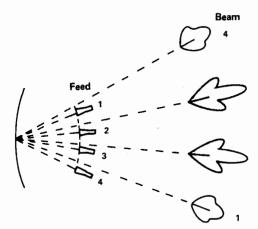


FIG. 36-9 Alternative spherical multibeam antenna using minimum reflector aperture with scanned beam feeds.

Offset geometry for use as an earth station antenna has been successfully demonstrated by COMSAT Laboratories.²⁰ The radiation patterns meet a (29-25 $\log \theta$)-dBi envelope.

The offset-fed geometry results in an unblocked aperture, which gives rise to low wide-angle sidelobes as well as providing convenient access to the multiple feeds.

The torus antenna has less phase aberration than the spherical antenna because of the focusing in the parabolic plane. Because of the circular symmetry, feeds placed anywhere on the feed arc form identical beams. Therefore, no performance degrada-

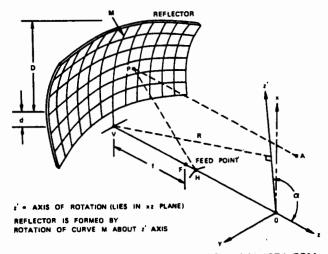


FIG. 36-10 Torus-antenna geometry. (Copyright 1974, COM-SAT Technical Review. Reprinted by permission.)

tion is incurred when multiple beams are placed on the focal arc. Point-focus feeds may be used to feed the torus up to aperture diameters of approximately 200 wavelengths. For larger apertures, it is recommended that aberration-correcting feeds be used.

The scanning or multibeam operation of a torus requires an oversized aperture to accommodate the scanning. For example, a reflector surface area of approximately 214 m² will allow a field of view (i.e., orbital arc) of 30° with a gain of approximately 50.5 dB at 4 GHz (equivalent to the gain of a 9.65-m reflector antenna). This surface area is equivalent to approximately three 9.65-m antennas.

Offset-Fed Multibeam Cassegrain Antenna

The offset-fed multibeam Cassegrain antenna is composed of a paraboloidal main reflector, a hyperbolic oversized subreflector, and multiple feeds located along the scan axis, as shown in Fig. 36-11. The offset geometry essentially eliminates beam blockage, thus allowing a significant reduction in sidelobes and antenna noise temperature. The Cassegrain feed system is compact and has a large focal-length-to-diameter ratio (f/D), which reduces aberrations to an acceptable level even when the beam is moderately far off axis. The low-sidelobe performance is achieved by using a corrugated feed horn which produces a gaussian beam.

A typical antenna design consisting of a 10-m projected aperture would yield half-power beamwidths (HPBWs) and gain commensurate with an axisymmetric 10-m antenna, 0.5° HPBW, and 51-dB gain at 4 GHz. The subreflector would need to be approximately a 3- by 4.5-m elliptical aperture. The feed apertures would be approximately 0.5 m in diameter. The minimum beam separation would be less than

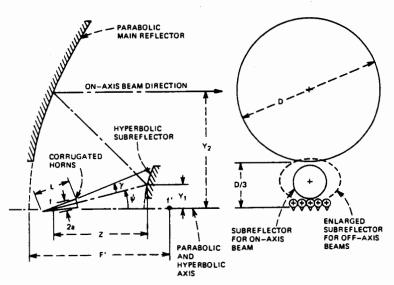


FIG. 36-11 Geometry of the offset-fed multibeam Cassegrain antenna. (Copyright 1974, American Telephone and Telegraph Company. Reprinted by permission.)

 2° , which is more than sufficient to allow use with synchronous satellites with orbit spacings of 2° or greater. For the $\pm 15^{\circ}$ scan, the gain degradation would be approximately 1 dB, and the first sidelobe would be approximately 20 to 25 dB below the main-beam peak.

36-4 ANGLE TRACKING

Automatic tracking of satellite position is required for many earth station antennas. Monopulse, conical-scan, and sequential-lobing techniques described in Chap. 34 are applicable for this purpose. Two other types of tracking techniques are also commonly employed: single-channel monopulse (pseudo monopulse) and steptrack. The single-channel monopulse is a continuous angle-tracking scheme, and steptrack is a time-sequencing, signal-peaking technique.

Single-Channel Monopulse

This technique utilizes multiple elements or modes to generate a reference signal, an elevation error signal, and an azimuth error signal. The two error signals are then combined in a time-shared manner by a switching network which selects one of two phase conditions (0° and 180°) for the error signal. The error signal is then combined with the reference signal, with the resultant signal then containing angle information. This allows the use of a single receiver for the tracking channel. This technique is equivalent to sequential lobing in which the lobing is done electrically and can be adjusted to any desired fixed or variable scan rate.

Steptrack

Steptracking is a technique employed primarily for maintaining the pointing of an earth station's antenna beam toward a geosynchronous satellite. Since most geosynchronous orbiting satellites have some small angular box of station keeping, a simple peaking technique can be used to keep the earth station beam correctly pointed. The signal-peaking, or steptrack, routine is a software technique that maneuvers the antenna toward the signal peak by following a path along the steepest signal-strength gradient or by using some other algorithm that accomplishes the same result. 21,22 Any method of direct search for maximization of signal is applicable; one such method calculates the local gradient by determining the signal strength at three points (A, B, C; see Fig. 36-12). From the signal strength at points A, B, and C, an angle α_2 , representing the unit's gradient vector angle relative to the azimuth axis, is computed. Once C_1 has been determined, A_2 is set equal to C_1 and another angle θ_2 is defined by $\theta_2 = \theta_1 + \alpha_2$ ($\theta_1 = 0$). The angle is used to relate pedestal movements to a fixedpedestal coordinate system. The procedure is repeated a number of times until the antenna boresight crosses throughout the peak. At this time the step size is reduced by one-half, and for each time that the peak is crossed it is again reduced by one-half until the peaking resolution is accomplished.

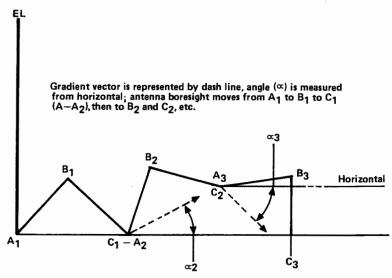


FIG. 36-12 Signal-strength gradients.

36-5 POLARIZATION

Many satellite communication systems are dual-polarized (frequency reuse) and are therefore susceptible to interference from the intended cross-polarized signals when the medium of propagation is such that the ellipticity of the signals is changed. This condition can occur during atmospheric conditions such as rain and Faraday rotation in the ionosphere. Therefore, in order to maintain sufficient polarization discrimination, special precautions must be taken in regard to the polarization purity of dual-polarization antennas; indeed, adaptive polarization-correcting circuits may be necessary. ^{23,24}

Several types of polarization-discrimination-enhancement schemes may be used. They include:

- Simple rotation of the polarization major-ellipse axis to correct for rotation due to the ionosphere (applicable for linear polarizations). Transmit and receive rotations are in opposite directions.
- 2 Suboptimal correction of depolarizations; ellipticity correction with respect to one of the signals but not orthogonalizing the two signals (differential phase).
- 3 Complete adaptive correction including orthogonalization (differential phase and amplitude).

The polarization-enhancement schemes may be implemented at the RF frequencies, or they may follow a down-conversion stage and be implemented at intermediate frequencies (IF). In either case the circuitry must operate over the full bandwidth of the communication channel. Kreutel et al.²⁴ treat the implementation of RF frequen-

cies in detail. The reader is also referred to Gianatasio^{25,26} for both RF and IF circuitry and experiments to verify performance of the circuitry.

APPENDIX A: EARTH STATION SIDELOBE REQUIREMENTS

CCIR 580-1

CCIR Recommendation 580-1 specifies the pattern envelope in terms of allowing 10 percent of the sidelobes to exceed the reference envelope and also permits the envelope to be adjusted for antennas whose aperture is less than 150 wavelengths. The standard is as follows:

With regard to antennas having a D/λ exceeding 150 New antennas of an earth station that are installed after 1988 operating with a geostationary satellite should have a design objective such that the gain G of at least 90 percent of the sidelobe peaks does not exceed

$$G = 29 - 25 \log (\theta) dBi$$

 θ being the off-axis angle in degrees referred to the main lobe axis, and G being the gain relative to an isotropic antenna. This requirement should be met for any off-axis direction which is within 3° of the geostationary-satellite orbit and for which 1° $\leq \theta \leq$ 20°, as illustrated by Fig. 36-1.

With regard to antennas having D/λ between 100 and 150 New antennas that are installed after 1988 should have a design objective such that the gain G of at least 90 percent of the sidelobe peaks does not exceed

$$G = 32 - 25 \log (\theta) dBi$$

Antennas installed after 1991 should have a design objective such that the gain G of at least 90 percent of the sidelobe peaks does not exceed

$$G = 29 - 25 \log (\theta) dBi$$

These requirements should be met for θ between 1 and 20° for any off-axis direction which is within 3° of the geostationary-satellite orbit.

With regard to antennas having D/λ between 35 and 100 New antennas that are installed after 1988 should have a design objective such that the gain G of at least 90 percent of the sidelobe peaks does not exceed

$$G = 52 - 10 \log (D/\lambda) - 25 \log (\theta) dBi$$

Antennas installed after 1991 should have a design objective so that the gain G of at least 90 percent of the sidelobe peaks does not exceed

$$G = 49 - 10 \log (D/\lambda) - 25 \log (\theta) dBi$$

These requirements should be met for D/λ between $(100\lambda/D)$ degrees and $(D/5\lambda)$ degrees with $(D/5\lambda)$ not less than 7°, which is equivalent to an antenna lower size limit of $D/\lambda = 35$. These requirements apply to any off-axis direction which is within 3° of the geostationary-satellite orbit.

FCC 25.209

The FCC requirement as stated in FCC Rules and Regulations Part 25.209 specifies that all transmit antenna's peak sidelobes must meet the

$$G = [29 - 25 \log (\theta)] dBi$$

envelope within the angular region of $1^{\circ} \le \theta \le 7^{\circ}$. The envelope becomes [32 – 25 log (θ)] dBi for $10^{\circ} \ge \theta \le 48^{\circ}$ with an allowance that 10 percent of the sidelobes may exceed the envelope by no more than 3 dB. Although no specific requirement applies for sidelobes in the receive bands, it is desirable that the same sidelobe requirements be achieved.

APPENDIX B: APERTURE DISTRIBUTIONS

The design of shaped-reflector antenna systems is driven by the desire to maximize the G/T of the system, thereby necessitating high aperture efficiency for the antenna. Experience has shown that an amplitude distribution other than uniform is desirable for axisymmetric reflectors. Amplitude distributions which have a taper at the edge of the main reflector reduce the effect of edge diffraction and not only improve the resultant aperture efficiency but also lower the wide-angle sidelobes such that the $[29-25 \log (\theta)]$ dBi sidelobe envelope may be met. For example, the amplitude distribution given by Eq. (36-12) with a taper of 4 to 6 dB at the edge of the main reflector generally produces improved gain and sidelobe performance over a uniform amplitude distribution:

$$I(X_2) = \left\{ A + (1 - A) \left[1 - \frac{(r - r_b)^2}{(r_{\text{max}} - r_b)^2} \right] \right\}^2$$
 (36-12)

where A controls the amplitude at the edge of the reflector and r_b is the blockage radius. This distribution is of the family $(1 - r^2)^n$ on a pedestal and has been used successfully in earth station antenna design. The parameter n may be chosen for efficiency optimization versus amplitude edge taper.

In recent years, the sidelobe suppression of earth station antennas has become increasingly important due to the placement of satellites in closer proximity to each other, i.e., 2° spacing rather than 4 or 5° spacing. This has led to tradeoffs of efficiency versus sidelobe level in order to decrease the effect of adjacent satellite interference. Analysis has shown that the illumination of the blocked region negatively affects the wide-angle side-lobes, and therefore, techniques to lower the sidelobes by controlling the illumination in the central portion of the dual-reflector designs is of interest. Ludwig²⁷ has investigated illumination functions for axisymmetric antennas with central blockage and suggests that amplitude distributions of the general shape represented by Eq. (36-13) are desirable for low wide-angle sidelobes.

$$f(r) = 0 r \le r_b$$

$$f(r) = \left[1 - \left(\frac{r_b}{r}\right)^2\right]^{p_1} (1 - r^2)^{p_2} r \ge r_b$$
(36-13)

Clayton and Cook²⁸ have employed other distributions such as a Fermi-Dyrac with central shading with success for the requirements of low-sidelobe envelopes and relatively

high aperture efficiency (where shading refers to extreme amplitude tapering in the central region of the aperture). The modified Fermi-Dyrac amplitude distribution is given by

$$E(\rho) = \frac{1}{1 + e^{A(\rho - \rho_{00})}} \frac{1}{1 + e^{A(\rho_{00} - \rho)}}$$
(36-14)

where $\rho = (r - r_b)/(1 - r_b)$ and r_b is the normalized radius of the central blockage. This function has two controlling parts: The first term is the amplitude taper term, and the second term is the shading control term. The constant $\rho_{0.5}$ is chosen to be the normalized radius where the field amplitude is 0.5, and the coefficient A controls the sharpness of the illumination rolloff for the amplitude taper term. The constants ρ_0 and A_0 are the half-amplitude point and the blockage rolloff constant for the shading term.

It should be pointed out that the Ludwig distributions and the modified Fermi-Dyrac functions yield somewhat lower efficiencies than an efficiency-optimized amplitude distribution with a higher first sidelobe and a narrower beamwidth, but the sidelobe falloff and wide-angle sidelobe levels are reduced such that the $[29-25\log(\theta)]$ dBi sidelobe envelope is met. The amplitude distributions discussed above are of particular benefit when the aperture size is such that the first sidelobe is inside the $\pm 1^{\circ}$ region of the pattern. This corresponds to an aperture size of approximately 175λ or a 10-m aperture at 6 GHz.

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Aircraft Antennas

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37-1	Introduction 3/-2	•
37.2	Low-Erequency As	

Low-Frequency Antennas 37-2

37-3 ADF Antennas 37-7

37-4 Moment-Method Analysis of Low-Frequency and High-Frequency Antenna Patterns 37-9

37-5 High-Frequency Communications Antennas 37-10 Wire Antennas 37-13 Probe Antennas 37-14 Shunt or Notch High-Frequency Antennas 37-14

37-6 Unidirectional Very-High-Frequency Antennas 37-17 Marker-Beacon Antennas 37-17 Glide-Slope Antennas 37-17 Altimeter Antennas 37-18

37-7 Omnidirectional Very-High-Frequency and Ultrahigh-Frequency Antennas 37-18 Airframe Effects on VHF and UHF

Patterns 37-19 37-8 GTD Aircraft Antenna Analysis 37-20

37-9 UHF/VHF Antennas 37-25 Antennas for Vertical Polarization 37-25 Antennas for Horizontal Polarization 37-27

37-10 Homing, MLS, and GPS Antennas 37-31

37-1 INTRODUCTION

The design of antennas for aircraft differs from other applications. Aircraft antennas must be designed to withstand severe static and dynamic stresses, and the size and shape of the airframe play a major role in determining the electrical characteristics of an antenna. For this latter reason, the type of antenna used in a given application will often depend on the size of the airframe relative to the wavelength. In the case of propeller-driven aircraft and helicopters, the motion of the blades may give rise to modulation of the radiated signal. Triboelectric charging of the airframe surfaces by dust or precipitation particles, known as p static, gives rise to corona discharges, which may produce extreme electrical noise, especially when the location of the antenna is such that there is strong electromagnetic coupling to the discharge point. In transmitting applications, corona discharge from the antenna element may limit the powerhandling capacity of the antenna. Also, special consideration must frequently be given to the protection of aircraft antennas from damage due to lightning strikes.

37-2 LOW-FREQUENCY ANTENNAS

The wavelengths of frequencies below about 2 MHz are considerably larger than the maximum dimensions of most aircraft. Because of the inherently low radiation efficiency of electrically small antennas and the correspondingly high radio-frequency (RF) voltages required to radiate significant amounts of power, nearly all aircraft radio systems operating at these lower frequencies are designed so that only receiving equipment is required in the aircraft.

Radiation patterns of aircraft antennas in this frequency range are simple electric or magnetic dipole patterns, depending upon whether the antenna element is a monopole or a loop. The pattern produced by a small monopole antenna will always be that of a simple dipole regardless of location; the orientation of the equivalent-dipole axis with respect to the vertical will depend upon location. A small antenna element placed on the airframe would respond to vertical, longitudinal, and transverse field components, indicating that the dipole moment of the antenna-airframe combination has projections in all three directions. Since the aircraft surface is small in terms of square wavelengths, it is appropriate to employ the method of moments (MOM) to assess pattern performance.¹⁻³ This technique is discussed in Sec. 37-4.

The sensitivity of low-frequency (LF) antennas is customarily expressed in either of two ways, depending upon whether the antenna is located on a relatively flat portion of the airframe such as the top or bottom of the fuselage or at a sharp extremity such as the tip of the vertical stabilizer. In the first case it can be assumed (at least when the antenna element is small relative to the surface radii of curvature) that the antenna performs as it would on a flat ground plane, except that the incident-field intensity which excites it is greater than the free-space incident-field intensity because of the field fringing produced by the airframe. The effect of the airframe on antenna sensitivity can be expressed by the ratio of the local-field intensity on the airframe surface to the free-space incident-field intensity. For a vertically polarized incident field (which is the case of primary importance in LF receiving-antenna design) this ratio is designated as

150

 F_v and is called the curvature factor for vertical polarization. Measurements can be performed to determine the equivalent dipole tilt angle and the factor F_v .

Effective height and capacitance data for antennas installed in locations for which this method is applicable are usually obtained by measurements or calculations for the antenna on a flat ground plane. The effective height (for vertically polarized signals) of the antenna installed on the airframe is then estimated by multiplying the flat-ground-plane effective height by the factor F_v appropriate to the installation, while the capacitance may be assumed to be the same as that determined with the antenna on a flat ground plane. The presence of a fixed-wire antenna on the aircraft may have a significant effect on F_v . Because of the shielding effect due to a wire, LF antennas are seldom located on the top of the fuselage in aircraft which carry fixed-wire antennas.

Flat-ground-plane data for a T antenna are shown in Fig. 37-1. The capacitance curves shown apply to an antenna made with standard polyethylene-coated wire [0.052-in- (1.32-mm-) diameter conductor and 0.178-in- (4.52-mm-) diameter polyethylene sheath]. Two antennas of this type are frequently located in close proximity on aircraft having dual automatic-direction-finder (ADF) installations. The effects of a grounded T antenna on h_e and C_a of a similar nearby antenna are shown in Fig. 37-2. To determine the significance of capacitance interaction it is necessary to consider the Q's of the input circuits to which the antennas are connected and the proximity of the receiver frequencies.

Sensitivity data for a flush antenna and a low-silhouette antenna consisting of a relatively large top-loading element and a short downlead are shown in Figs. 37-3 and 37-4, respectively. The antenna dimensions shown in these figures are not indicative of antenna sizes actually in use but rather are the sizes of the models used in measuring the data. Both h_e and C_a scale linearly with the antenna dimensions.

A rule-of-thumb design limit for flush antennas may be derived on the basis of a quasi-static analysis of LF antenna performance. If any electric dipole antenna is short-circuited at its feed terminals and placed in a uniform electrostatic field with its equivalent-dipole axis aligned parallel to the field, charges of +q and -q will be induced on the two elements of the antenna. It may be shown that the product of the

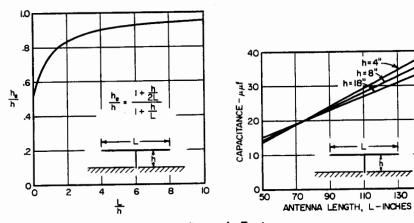


FIG. 37-1 Effective height and capacitance of a T antenna.

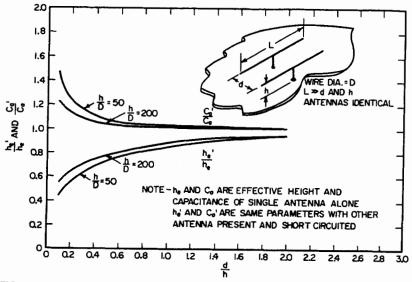


FIG. 37-2 Shielding effect of one T antenna on another.

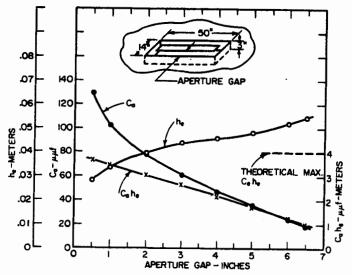


FIG. 37-3 Design data for a flush low-frequency antenna.

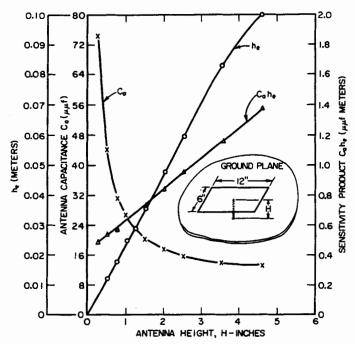


FIG. 37-4 Design data for a heavily top-loaded low-frequency antenna with flat-plate top loading.

LF parameters h_e and C_a is related to the induced charge by the equation

$$h_{\epsilon}C_a = q/E \tag{37-1}$$

where h_{\bullet} and C_a are expressed in meters and picofarads respectively, q is expressed in picocoulombs, and the incident-field intensity E is expressed in volts per meter. The quantity q/E is readily calculated for a flush cavity-backed antenna of the type shown in Fig. 37-3, at least for the case in which the antenna element virtually fills the cutout in the ground plane. In this case, the shorted antenna element will cause practically no distortion of the normally incident field, and the number of field lines terminating on the element will be the same as the number which would terminate on this area if the ground plane were continuous. The value of q/E is hence equal to $\varepsilon_0 a$, where $\varepsilon_0 = 8.85 \times 10^{-12} \, \text{F/m}$ and a is the area of the antenna aperture in square meters. For a flush antenna with an element which nearly fills the antenna aperture we have

$$h_{\epsilon}C_{a}=\varepsilon_{0}a\tag{37-2}$$

The line labeled "theoretical maximum $C_a h_e$ " in Fig. 37-3 was calculated from Eq. (37-2). With practical antenna designs, there will be regions of the aperture not covered by the antenna element, so that some of the incident-field lines will penetrate the aperture and terminate inside the cavity. As a result, the induced charge q will be smaller than that calculated above, and the product $h_e C_a$ will be smaller than the value estimated from Eq. (37-2).

The helicopter presents a special antenna-design problem in the LF range as well as in other frequency ranges because of the shielding and modulation caused by the rotor blades. Measured curves of F_v obtained with an idealized helicopter model to demonstrate the effects of different antenna locations along the top of the simulated fuselage are shown in Fig. 37-5. The MOM also may be used to compute rotor modulation effects.

It is characteristic of rotor modulation of LF signals that relatively few modulation components of significant amplitude are produced above the fundamental rotor modulation frequency, which is equal to the number of blade passages over the antenna per second. This fundamental frequency is of the order of 15 Hz for typical three-blade single-rotor helicopters. It should be noted that new sidebands will be generated about each signal sideband and about the carrier. It is hence not a simple matter to predict the effects of rotor modulation on a particular system unless tests have been made to determine the performance degradation of the airborne receiver due to these extra modulation components.

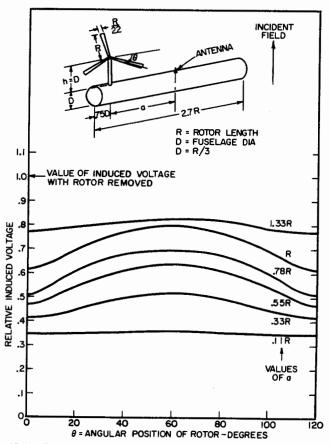


FIG. 37-5 Rotor modulation for a low-frequency receiving antenna on an idealized helicopter model.

37-3 ADF ANTENNAS

The ADF system, which determines the direction of arrival of the signal by rotating its loop antenna about a vertical axis until a null is observed in the loop response

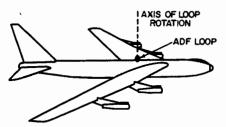


FIG. 37-6 ADF loop antenna on aircraft.

(Fig. 37-6), is subject to bearing errors because of the difference in direction of the local incident magnetic fields. The relationship between the true and the apparent directions of the signal source is given by the equation*

$$\tan \phi_i = \frac{a_{xx}}{a_{yy}} \tan \phi_a \qquad (37-3)$$

where ϕ_i and ϕ_a are respectively the true and the apparent bearings of the signal

source. A curve of the bearing error $(\phi_t - \phi_a)$ as a function of ϕ_t with the ratio $a_{xx}/a_{yy} = 2$ is shown in Fig. 37-7a. Figure 37-7b shows graphs of the maximum bearing error $|\phi_t - \phi_a|$ and the value of ϕ_t (in the first quadrant) at which the maximum bearing error occurs as functions of the ratio a_{xx}/a_{yy} .

Survey data showing the coefficient a_{xx} and the maximum bearing error for loop antennas along the top and bottom centerline of a DC-4 aircraft are shown in Fig. 37-8. The ADF loop has a 180° uncertainty in null location due to its "figure 8" pattern. An auxiliary "sense" antenna is used to resolve the null uncertainty via amplitude comparison. The ADF system is calibrated after installation to achieve proper performance.

The automatic-direction-finder loop antenna is normally supplied as a component of the ADF system, and the problem is to find a suitable airframe location. The two restrictions which govern the selection of a location are (1) that the cable between the loop antenna and receiver be of fixed length, since the loop and cable inductances form a part of the resonant circuit in the loop amplifier input, and (2) that the maximum bearing error which the system can compensate be limited to about 20°. As can be seen from the bearing-error data in Fig. 37-7, positions on the bottom of the fuselage forward of the wing meet the minimum bearing-error requirements on the aircraft type for which the data are applicable (and on other comparable aircraft). Such positions are consistent with cable-length restrictions in most cases since the radio-equipment racks are usually just aft of the flight deck.

Bearing-error compensation is accomplished in some ADF systems by means of a mechanical compensating cam.^{4,5} Standard flight-test procedures^{4,6} are generally used in setting the compensating cams. In some loop designs⁷ electrical compensation is achieved by modifying the immediate environment of the actual loop element.

Unlike the loop antenna, the sense antenna must be located within a limited region of the airframe for which the equivalent-dipole axis is essentially vertical in order to ensure accurate ADF performance as the aircraft passes over or near the ground station to which the receiver is tuned.⁸

A typical flush ADF sense-antenna installation is illustrated by the C-141 aircraft. The antenna is a cavity built into the upper fuselage fairing just aft of the wing

^{*}The ratio of local magnetic field intensity on the airframe surface to the incident magnetic field intensity is designated as a_{xx} for the case in which the incident field is transverse to the line of flight (the signal arrives from the front or rear of the aircraft) and as a_{yy} when the incident field is along the line of flight (the signal arrives from the side of the aircraft).

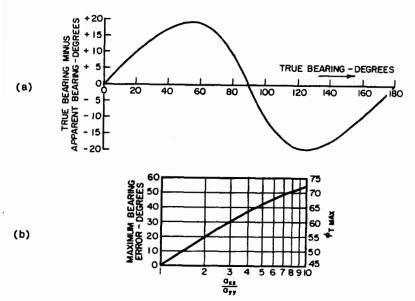


FIG. 37-7 (a) Bearing-error curve for $a_{xx}/a_{yy}=2$. (b) The maximum bearing error and the true bearing at which the maximum bearing error occurs as functions of a_{xx}/a_{yy} .

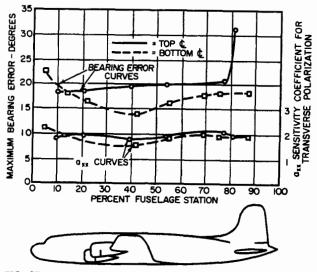


FIG. 37-8 Low-frequency loop-antenna survey data for a DC-4 aircraft showing maximum bearing error and sensitivity coefficient for transverse polarization for top and bottom centerline locations.

crossover. It was decided during the design phase to use the Bendix ADF-73 automatic-direction-finder system, which to some extent determined the sense-antenna requirements. The basic antenna requirements were (1) antenna capacitance of 300 pF,

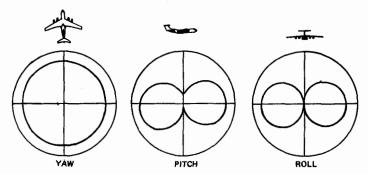


FIG. 37-9 Voltage radiation patterns for the C-141 ADF sense antenna.

(2) a minimum quality factor of 1.4, and (3) a radiation-pattern tilt angle between 0 and 10° downward and forward. Figure 37-9 shows the patterns of the dual sense antenna.

For the C-141, the electrical center of the aircraft (pattern tilt angle of zero) was initially located through radiation-pattern measurements by using a small model configuration; a tilt-angle change was noted when the feed point for the cavity ADF antenna was moved. A zero tilt angle was obtained, and it was found that an approximate 10-in (254-mm) movement of the feed point aft produced a $+10^{\circ}$ tilt angle. Since a tilt angle of 0 to 10° is required, the measurements permitted selection of an optimum feed point ($+5^{\circ}$ tilt). Figure 37-9 shows the yaw, pitch, and roll radiation patterns obtained with the optimum antenna feed point.

The recently developed Rockwell/Collins DF-206A automatic direction finder (ADF) system is unique in that the DFA-206A antenna consists of a combined sense and loop antenna assembly. The sense antenna input is used as the reference input and is coupled to a low-pass filter. The low-pass filter removes the high-frequency interference. The two loop antennas are physically oriented 90° apart, and the resulting signal strengths are related to the direction of the antennas in relation to the transmitting station.

The antenna is a self-contained unit that may be located on either the top or the bottom of the aircraft. This unit is housed in a 16.5-in-long, 8.5-in-wide, and 1.75-in-thick "teardrop" designed to mount flush with the aircraft fuselage. It should be located as near the centerline of the aircraft as possible to reduce unsymmetric quadrantal error and near the wing root to obtain the best station-crossing indication. Unlike previous ADF systems, the length of the interconnecting cables between the antenna and receiver is neither limited nor critical. However, short cable runs are preferred to reduce the exposure to ground currents and interfering fields within the airframe.

37-4 MOMENT-METHOD ANALYSIS OF LOW-FREQUENCY AND HIGH-FREQUENCY ANTENNA PATTERNS

The method of moments (MOM)¹⁻³ is a computer analysis method which can be employed to determine the radiation patterns of antennas on aircraft and missiles. A

discussion of this technique is beyond the scope of this handbook, but user-oriented computer programs are available. 10-12

The method of moments is based upon a solution of the electromagnetic-wave-scattering integral equations by enforcing boundary conditions at a number N of discrete points on the scattering surface. The resulting set of equations is then solved numerically to determine the scattered fields. This is typically accomplished by modeling the surface as a wire grid for which the self- and mutual impedances between the wires can be calculated. This technique, for a set of N wire elements which represents the aircraft such as shown in Fig. 37-10, results in an $N \times N$ impedance matrix. For a given antenna excitation, inversion of the $N \times N$ matrix yields the solution for the wire currents and hence the radiated fields of the antenna-aircraft system.

Computer programs which implement this technique for wire scatterers^{1,10-13} and for surface patches^{14,15} have been written. Supercomputers can handle matrixes on the order of 10,000 by 10,000 elements, and continuing technology advances will permit larger matrixes to be solved. Also, several MOM codes for personal computers (PCs) are available.^{11,12} These codes will become increasingly useful as the computing capability of PCs increases. The number of wire or patch elements which must be employed to ensure a convergent numerical solution varies as a function of the particular code implementation. Typically, a wire element less than $\lambda/8$ in length must be used so that a $1\lambda^2$ surface patch requires a "square" wire-grid model containing 144 wires. Thus it is seen that as the surface area increases, the required matrix increases roughly as the square of the area which, in practice, restricts the MOM to electrically small- to moderate-sized geometries. Codes based on body-of-revolution approximations are also available 4 and are particularly applicable to missiles.

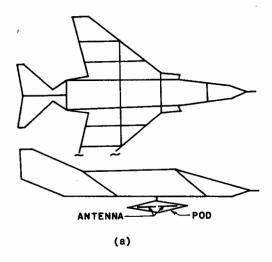
A wire-grid model which was used for the pattern analysis of a pod-mounted high-frequency (HF) folded-dipole array antenna on an RF-4C aircraft is shown in Fig. 37-10a. An MOM code employing piecewise sinusoidal basis functions 1,13 was used to calculate the roll-plane patterns for the array, and these results are compared with measured data in Fig. 37-10b.

A surface-patch method has also been employed to analyze the patterns of antennas on helicopters. ¹⁶ In this analysis, the helicopter surface was subdivided into a collection of curvilinear cells. A result of the analysis, which employed 94 surface-patch cells, is shown in Fig. 37-11 for the pitch and yaw planes. Generally, good results were obtained for this complex-shaped airframe. Also, we note that, by representing the helicopter rotor blades as wires, the rotor effects on the patterns can be computed.

For some LF applications, a simplified "stick model" of an aircraft may be sufficient, ¹⁷ and a model of an aircraft is shown in Fig. 37-12. The fuselage, wings, and empennage can be represented by either single or multiple thin wires if their maximum electrical width is approximately less than $\lambda/10$. Figure 37-12 shows a calculated result for a monopole mounted on a stick model, and the effects of the fuselage and wings can be seen by comparison with the unperturbed-monopole pattern. ¹⁸

37-5 HIGH-FREQUENCY COMMUNICATIONS ANTENNAS

Aircraft antennas for use with communications systems in the 2- to 30-MHz range are required to yield radiation patterns which provide useful gain in directions signif-



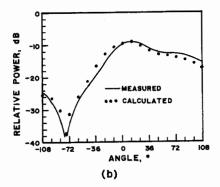


FIG. 37-10 MOM wire-grid analysis of low-frequency aircraft antenna patterns. (a) MOM wire-grid model of an RF-4C aircraft. (b) MOM calculated roll-plane pattern for a pod-mounted dipole array on the RF-4C aircraft. (From Ref. 13, © 1977 IEEE.)

icant to communications. Also, impedance and efficiency characteristics suitable for acceptable power-transfer efficiencies between the airborne equipment and the radiated field are needed. A receiving antenna which meets these requirements will deliver to the input of a matched receiver atmospheric noise power under noise field conditions which is many times greater than the input-circuit noise in the communications receiver. When this is the case, no improvement in signal-to-noise ratio can be achieved by further refinement of the antenna design. Since the transmitting mode of operation poses the more stringent requirements, the remainder of the discussion of HF antennas is confined to the transmitting case. Sky-wave propagation is always an important factor at these frequencies, and because of the rotation of polarization which is characteristic of reflection from the ionosphere, polarization characteristics are usually unimportant; the effective antenna gain can be considered in terms of the

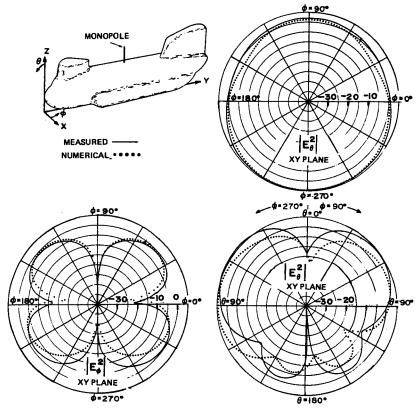


FIG. 37-11 MOM surface-patch-calculated patterns for the CH-47 helicopter. (From Ref. 16, © 1972 IEEE.)

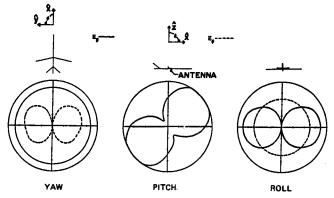


FIG. 37-12 MOM calculated voltage patterns for a blade antenna (tilted monopole) on a "stick model" aircraft.

total power density. At frequencies below 6 MHz, ionosphere (and ground) reflections make almost all the radiated power useful for communication at least some of the time, so that differences between radiation patterns are relatively unimportant in comparing alternative aircraft antennas for communication applications in the 2- to 6-MHz range. In this range, impedance matching and efficiency considerations dominate. For frequencies above 6 MHz, pattern comparisons are frequently made in terms of the average power gain in an angular sector bounded by cones 30° above and below the horizon.

In the 2- to 30-MHz range, most aircraft have major dimensions of the order of a wavelength, and currents flowing on the skin usually dominate the impedance and pattern behavior. Since the airframe is a good radiator in this range, HF antenna design is aimed at maximizing the electromagnetic coupling to the airframe. The airframe currents exhibit strong resonance phenomena that are important to the impedance of antennas which couple tightly to the airframe.

Wire Antennas

Wire antennas, supported between the vertical fin and an insulated mast or trailed out into the airstream from an insulated reel, are reasonably effective HF antennas on lower-speed aircraft. Aerodynamic considerations limit the angle between a fixed wire and the airstream to about 15°, so that fixed-wire antennas yield impedance characteristics similar to moderately lossy transmission lines, with resonances and antiresonances at frequencies at which the wire length is close to an integral multiple of $\lambda/4$. Figure 37-13 shows the input impedance of a 56-ft (17-m) fixed-wire antenna on a C-130 Hercules aircraft. Lumped reactances connected between the wire and the fin produce an effect exactly analogous to reactance-terminated lossy transmission lines. The average directive gain of these antennas in the sector \pm 30° relative to the horizon (i.e., the fraction of the total radiated energy which goes into the sector bounded by

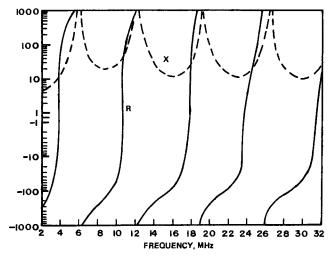


FIG. 37-13 Impedance of the C-130E right-hand long-wire antenna.

the cones 30° above and below the horizontal plane) remains near 60 percent from 6 to 24 MHz. The efficiency of wire antennas is not high because of resistance loss in the wire itself and dielectric loss in the supporting insulators and masts. The resistance of commonly used wires is of the order of $0.05~\Omega/\mathrm{ft}$ at 4 MHz. The RF corona breakdown threshold of fixed-wire antennas is a function of the wire diameter and the design of the supporting fittings. To minimize precipitation static a wire coated with a relatively large-diameter sheath of polyethylene is frequently used, with special fittings designed to maximize the corona threshold. Even with such precautions, voltage breakdown poses a serious problem with fixed-wire antennas at high altitudes. Measurements indicate that standard antistatic strain insulators have an RF corona threshold of about 11 kV peak at an altitude of 50,000 ft (15,240 m)¹⁹ and a frequency of 2 MHz. Such an insulator, placed between the vertical stabilizer and the aft end of the open-circuited antenna, would go into corona at this altitude if the antenna were energized with a fully modulated AM carrier of about 150 W at 2 MHz.

Probe Antennas

A variation of the isolated-cap antenna is the probe or bullet-probe antenna. The radiation-pattern and impedance-resonance effects of the empennage, fuselage, and wings also affect probe antennas. The marked advantage of the probe antenna over the tail-cap antenna lies in the relative ease of incorporation into the structure of the aircraft empennage. The C-141 bullet-probe antenna shown in Fig. 37-1420 makes use of a portion of the structural intersection of the horizontal and vertical stabilizers in the T-tail configuration. The antenna is composed of the forward portion of the aerodynamic bullet with a probe extension. The plastic isolation gap in the bullet extends forward 11 in (279 mm), and the overall length of the antenna including the isolation band is 112 in (2845 mm). The maximum structural gap width was 13 in (330 mm), and the minimum gap width to withstand RF potentials was 3 to 4 in (76 to 102 mm). To obtain maximum airframe coupling, a maximum resistive component is required at the lowest expected resonant frequency. This resonance occurred at 2.4 MHz, which corresponds to a half-wavelength resonant condition caused by the wing-tip-tohorizontal-stabilizer-tip distance. Another parameter considered was the capacitive reactance of the antenna at 2.0 MHz. This reactance had to remain below 1000 Ω if existing couplers were to be used. This resulted in a gap width of 11 in for satisfactory performance. Figure 37-14 shows the impedance curves for the C-141 forward bulletprobe antenna.

A solid bulkhead was installed just aft of the isolation band for two reasons: (1) the metallic bulkhead acts as an electrostatic shield between the antenna and other metallic objects, and (2) the antenna tuner will mount on the bulkhead. Connection to the antenna is made through a lightning arrester which protrudes through the bulkhead into the gap area. The lightning arrester has a "birdcage" terminal which plugs into a flared tube tied electrically to the probe and metal portions of the forward bullet.

Shunt or Notch High-Frequency Antennas

Shunt- and notch-type HF antennas are becoming increasingly popular on modern high-speed aircraft because of drag reduction and higher reliability. The basic difference in the shunt and notch configurations is the ratio of length to width of the cutout (dielectric) portion of the aircraft. Figure 37-15 shows the basic configuration.²¹

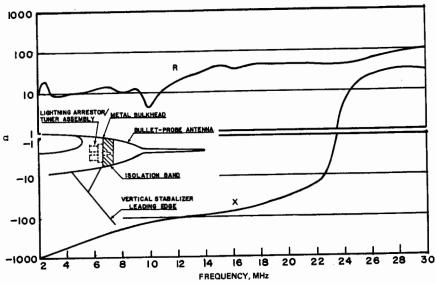


FIG. 37-14 Impedance curves for the C-141 aircraft forward bullet-probe antenna. (From Ref. 20.)

The shunt or notch antenna is a kind of transmission line that uses the vertical stabilizer or wing to feed the remainder of the aircraft. It can be located at various points on the airframe, but since it functions as an inductive coupler, it should be located at a point of low impedance or high current. The shunt-fed loop current causes the airframe itself to act as the antenna. The particular portion of the airframe sup-

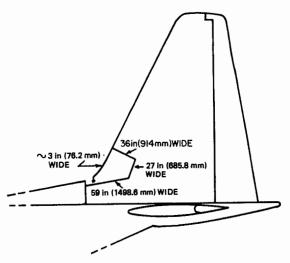


FIG. 37-15 Basic configuration of the C-130 notch high-frequency antenna. (From Ref. 21.)

porting the current path is a function of the frequency and physical lengths of parts of the airframe involved. For example, the wing-tip-to-horizontal-tip half-wavelength resonance on the C-5 aircraft occurs at approximately 2.5 MHz. The coupler feed point should always be located at the end of the shunt feed closest to the center of the aircraft.

The design of the antenna involves first finding a suitable location for the dielectric area and then arranging the dimensions of the shunt feed and dielectric area to provide an antenna that can be efficiently matched to $50~\Omega$ with a relatively simple antenna coupler. Guidelines to observe are as follows: (1) The first choice for location on the airframe from a radiation-pattern and impedance standpoint is the root of the vertical stabilizer. An alternative is the wing root, but in this case the radiated vertically polarized energy is reduced. (2) The antenna coupler should be connected to the shunt feed near the stabilizer or wing root to provide maximum efficiency. (3) The dielectric material used to fill the opening should have low-loss characteristics. (4) The exact size and shape of the dielectric area is not a critical design parameter, but the dielectric area should be as deep as possible for maximum coupling to the airframe. Radiation efficiency is generally proportional to the dielectric area.

To avoid the need for a complicated antenna-tuning network, the antenna reactance at 2.0 MHz should be no less than $+j18~\Omega$, and ideally parallel resonance should occur between 20 and 30 MHz. Series resonance should be completely avoided, and antenna reactance should be no lower than $-j100~\Omega$ at 30 MHz. To ensure good coupling to the airframe the parallel component of the antenna impedance should be less than 20,000 Ω .

Figure 37-15 shows the shunt-fed notch antenna for the C-130 aircraft. A portion of the dorsal and a portion of the leading-edge fairing are combined to yield a notch in the root of the vertical stabilizer. The total distance around the notch is approximately 160 in (4064 mm), or slightly smaller than the ideal periphery of approximately 200 in (5080 mm). This was necessary because of interference with the leading-edge deicing system. The impedance curve for this antenna is shown in Fig. 37-16.

A unique application of the shunt-fed HF antenna is found on the Lockheed Jet-

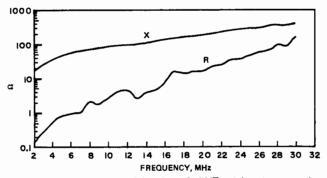


FIG. 37-16 Impedance of the shunt-fed HF notch antenna on the C-130 aircraft. (From Ref. 21.)

Star aircraft.²² Figure 37-17 is a sketch of the antenna. The antenna is fed from a coaxial feed on the upper surface of the wing, where a 32-in (813-mm) piece of phosphor-bronze stranded cable connects the center conductor to the leading lower edge of an aft-mounted engine nacelle. Excellent omnidirectional patterns are obtained, and the impedance is tuned by using an off-the-shelf coupler inside the pressurized area of the fuselage.

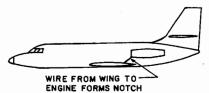


FIG. 37-17 Shunt-fed HF notch-antenna configuration on the Lockheed JetStar. (From Ref. 22.)

37-6 UNIDIRECTIONAL VERY-HIGH-FREQUENCY ANTENNAS

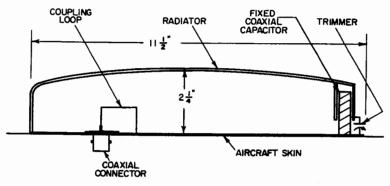
The marker-beacon, glide-slope, and radio-altimeter equipments require relatively narrowband antennas with simple patterns directed down or forward from the aircraft. This combination of circumstances makes the design of these antennas relatively simple. Both flush-mounted and external-mounted designs are available in several forms.

Marker-Beacon Antennas

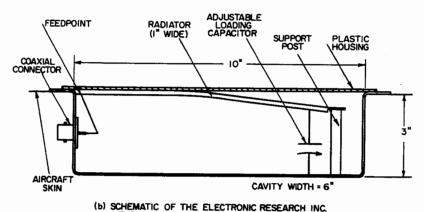
The marker-beacon receiver operates on a fixed frequency of 75 MHz and requires a downward-looking pattern polarized parallel to the axis of the fuselage. A standard external installation employs a balanced-wire dipole supported by masts. The masts may be either insulated or conducting. Low-drag and flush-mounted designs are sketched in Fig. 37-18. The low-drag design is a simple vertical loop oriented in the longitudinal plane of the aircraft. The feed line is inductively coupled to the loop, which is resonated by a series capacitor, and the antenna elements are contained in a streamlined plastic housing. The flush design is electrically similar, but in this case the structure takes the form of a conductor set along the longitudinal axis of the open face of a cavity. To achieve the desired impedance level, the antenna conductor is series-resonated by a capacitor and the feed point tapped partway along the antenna element.

Glide-Slope Antennas

The glide-slope receiver covers the frequency range from 329 to 335 MHz and requires antenna coverage only in an angular sector 60° on either side of the nose and 20° above and below the horizon. This requirement can be met by horizontal loops or by vertical slots. Because of the narrow bandwidth, the antenna element need not be electrically large. Two variations on the loop arrangement are sketched in Fig. 37-19. Configuration a is a simple series-resonant half loop which can be externally mounted on the nose of the aircraft or within the nose radome. A variation of this antenna has two connectors for dual glide-slope systems. Configuration b, which is similar to the cavity-marker-beacon antenna of Fig. 37-18, is suitable for either external or flush mounting.



(a) SCHEMATIC OF THE COLLINS 37X-I MARKER BEACON ANTENNA



AT-134/ARN FLUSH MARKER BEACON ANTENNA

FIG. 37-18 Typical marker-beacon antennas.

Altimeter Antennas

The radio altimeter, which operates at 4300 MHz, requires independent downwardlooking antennas for transmission and reception. Proper operation requires a high degree of isolation between the transmitting and receiving elements, and horns are typically used, although microstrip antennas are becoming common.

OMNIDIRECTIONAL VERY-HIGH-FREQUENCY 37-7 AND ULTRAHIGH-FREQUENCY ANTENNAS

In the frequency range in which the airframe is electrically large, the achievement of omnidirectional patterns, such as those used for short-range communications, is complicated by airframe effects. Since very-high-frequency (VHF) and ultrahigh-frequency (UHF) antennas of resonant size are structurally small, the required imped-

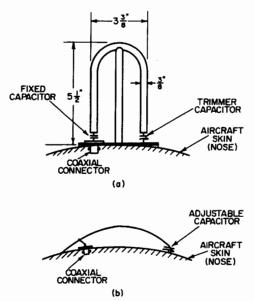


FIG. 37-19 Protruding glide-slope antennas.

ance characteristics can be achieved with fixed matching networks. Shadowing and reflection by the airframe result in major distortions of the primary pattern of the radiating element.

Airframe Effects on VHF and UHF Patterns

The tip of the vertical fin is a preferred location for omnidirectional antennas in the VHF and UHF range because antennas located there have a relatively unobstructed "view" of the surrounding sphere. At these frequencies the mean chord of the fin is approximately 10 wavelengths and the principal effect of the airframe on the radiation patterns is a sharply defined "optical" shadow region. At the lower end of this frequency range and on smaller aircraft, the effect of the airframe on the patterns is more complicated. Deep nulls in the forward quadrants can occur because of the destructive interference between direct radiation and radiation reflected from the fuselage and wings. The latter contribution is more important for small aircraft since the ground plane formed by the surface of the fin tip is now sufficiently small to permit strong spillover of the primary pattern, which also can create lobing in the transverse-plane pattern. In this frequency range the null structure is strongly influenced by the position of the radiating element along the chord of the fin, and careful location of the antenna along the chord may result in improvements in the forward-horizon signal strength.

Most external antennas are located on the top or bottom centerline of the fuselage in order to maintain symmetry of the radiation patterns. Pattern coverage in such locations is limited by the airframe shadows. Figure 37-20 shows the patterns of a 1000-MHz monopole on the bottom centerline of a C-141 aircraft. It is apparent that coverage is limited to the hemisphere below the aircraft. UHF antennas on the top of

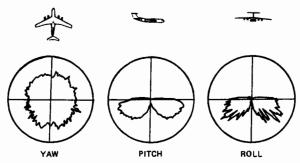


FIG. 37-20 Voltage radiation patterns of a 1000-MHz monopole on the bottom of a C-141 aircraft.

the fuselage yield patterns confined to the upper hemisphere, with a null aft owing to the shadow cast by the vertical fin. In many applications, as, for example, in scheduled-airline operations, these pattern limitations are acceptable, and fuselage locations are frequently used.

The deep lobing in the roll-plane pattern of Fig. 37-20 is due to reflections from the strongly illuminated engine nacelles. In some locations similar difficulties are encountered because of reflection from the wing flaps when they are extended. Shadows and lobing due to the landing gear, when extended, are frequently troublesome for bottom-mounted antennas.

37-8 GTD AIRCRAFT ANTENNA ANALYSIS

The MOM technique is limited to surfaces which are relatively small in terms of square wavelengths. However, as the frequency increases and the surface becomes large in terms of square wavelengths, the propagation of electromagnetic (EM) energy can be analyzed by using the techniques of geometrical optics. For example, if an incident field is reflected from a curved surface, ray optics and the Fresnel reflection coefficients yield the reflected field.

The geometrical theory of diffraction (GTD) uses the ray-optics representation of EM propagation and incorporates both diffracted rays and surface rays to account for the effects of edge and surface discontinuities and surface-wave propagation. In the case of edge diffraction, the diffracted rays lie on a cone whose half angle is equal to the half angle of the edge tangent and incidence vector. For a general curved surface, the incident field is launched as a surface wave at the tangent point, propagates along a geodesic path on the surface, and is diffracted at a tangent point toward the direction of the receiver. Each of these diffraction, launching, and surface propagation processes is described by appropriate complex diffraction and attenuation coefficients which are discussed in the literature.²³ In practice, these coefficients are implemented as computer algorithms which can be used as building blocks for a specific analysis.

In the GTD analysis, the received far- or near-zone field is composed of rays which are directly incident from the antenna, surface rays, reflected rays, and edge-diffracted rays. Also higher-order effects such as multiple reflections and diffractions can occur. Several computer models have been implemented to perform the required

differential-geometry and diffraction calculations.²⁴⁻²⁶ It is anticipated that these methods will become more user-oriented and powerful with the advent of increasingly sophisticated computer-graphics systems.

Figure 37-21 shows a model of a missile composed of a conically capped circular cylinder with a circumferential-slot antenna.²⁷ In this case, the radiated field is due to direct radiation from the slot, surface rays which encircle the cylinder, and diffracted rays from the cone-cylinder and cylinder-end junctions and from the cone tip. The computed results shown in Fig. 37-21 were obtained by employing the solution for a slot on an infinite circular cylinder to represent the direct- and surface-ray fields and by computing the diffracted fields from the junctions and tip as corrections to the infinite-cylinder result. The principal-plane pattern shown is in agreement with measured data, and comparable results have been obtained for the off-principal planes.²⁸

An analysis due to Burnside et al.²⁴ approximates the fuselage as two joined spheroids, and the wings and empennage are modeled by arbitrarily shaped flat plates. In addition, the engines can be modeled by finite circular cylinders. Figure 37-22 shows a result obtained from this analysis of a $\lambda/4$ monopole on a KC-135 aircraft for the roll plane. Reference 25 presents a complete 4π -sr plot for a monopole on a Boeing 737 aircraft. The results, which compare well with measured data, illustrate the accuracy of the GTD analysis for VHF and UHF antennas.

It should be noted that a complete GTD model may not always be required for an engineering assessment of antenna performance. For example, if wing reflection and blockage effects are dominant, one can use a simpler model consisting of two

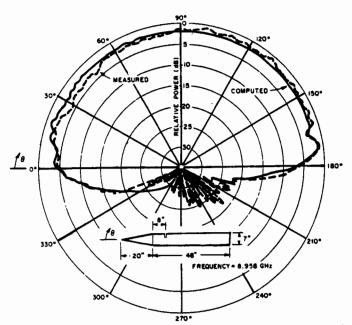


FIG. 37-21 Pattern of a circumferential slot on a conically capped circular cylinder. (From Ref. 27, © 1972 IEEE.)

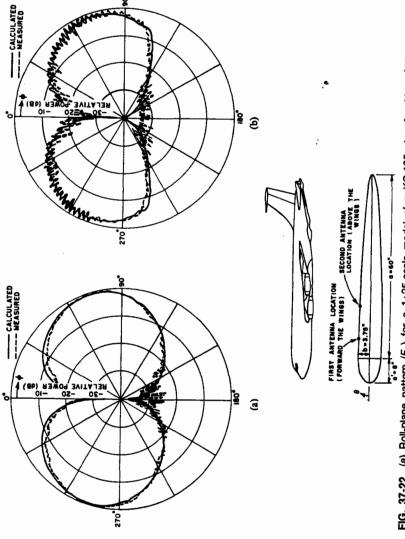


FIG. 37-22 (a) Roll-plane pattern (E_{ϕ}) for a 1:25-scale model of a KC-135 aircraft with a $\lambda/4$ monopole on the fuselage forward of the wings at a frequency of 34.92 GHz (model frequency). (b) Roll-plane pattern (E_ϕ) for a $\lambda/4$ monopole over the wings. (From Ref. 24, © 1975 IEEE.)

submodels: a submodel for an antenna on a finite (or perhaps an infinite) cylindrical fuselage and a flat-plate submodel for the wings.²⁶ In this case, the antenna-on-cylinder pattern results are used as the antenna illumination for calculation of the wing blockage, reflection, and diffraction.

The computer analysis of aircraft interference effects on scanning array antenna patterns is a subject of much interest to those working in the field of large airborne antenna arrays. Experience indicates that such analyses employing the geometrical theory of diffraction (GTD) are feasible and cost-effective. The emphasis in the technology is the use of large-aperture, low-frequency (UHF to S-band) arrays installed on large airframes such as the C-5A or B747 aircraft. Techniques usually considered are scale-model measurements. full-scale measurements, and computer simulation of the array antennas on airframes. Computer-simulation techniques have a considerable advantage from a cost standpoint over the other two options. The computer-simulation technique is a very useful tool for determining the proper array location on the airframe and the frequency sensitivity to airframe effect on radiation patterns. Wing, engine nacelles, and empennage structure in the near field of large arrays can cause devastating effects on the sidelobe structure of a well-designed array antenna. Once the airframe and the array are simulated on the computer, it is a simple matter to relocate the array on the airframe and compute the resulting pattern. While the pattern computation is very central process unit (CPU) time-intensive, it is still more cost-effective to move the array on the computer than to move the array on the full-scale aircraft or scale model.

A collection of plates and cylinders is used to model the airframe, including the empennage, wing, engine nacelles, and engine pylons. Each element in the array antenna is assumed to be a separate source controllable in amplitude and phase, allowing the use of aperture-distribution tapering and simulated electronic scanning of the beam to a desired angle.

This technique allows the computation of three parameters to help with the evaluation of antenna performance on the airframe. They are the two-way integrated sidelobe-to-mainlobe (SL/ML) ratio in decibels, the rms sidelobe level in decibels, and the 3-dB beamwidth in degrees. To calculate the SL/ML ratio, the sidelobes and mainlobe are sampled at 1° increments and integrated. The integrated sidelobe power (two-way) is divided by the integrated mainlobe power (two-way). One of the great strengths of this computer-analysis technique is the user's ability to disassemble the airframe, when desired, for identifying the primary contributor to a particular sidelobe or cross-polarized component of the radiation patterns.

The computer code used to compute phased-array antenna radiation patterns is a modified version of the "Numerical Electromagnetic Code—Basic Scattering Code" (version 3.19) developed by the Ohio State University ElectroScience Laboratory. ^{29,30} It uses the geometrical theory of diffraction (GTD) to determine the total field at a given observation point. Several basic geometric shapes can be used to model scattering objects. They are arbitrarily oriented flat plates, perfectly conducting finite elliptic cylinders, elliptic cone frustum sections, and finite composite ellipsoids. These objects should have a minimum dimension of one wavelength, and the accuracy increases as the object size in wavelengths increases. The required accuracy of the scattering model also depends on the direction of the mainbeam, while broadbeam antennas require greatest accuracy in the part of the model near the antenna.

The GTD code was used to analyze a rotodome array installed on the S3 aircraft, as shown in Fig. 37-23. The 28-in by 228-in array is composed of 32 columns spaced 7.125 in by 4 rows spaced 7.0 in. A 50-dB Taylor (n = 6) aperture distribution was chosen for the

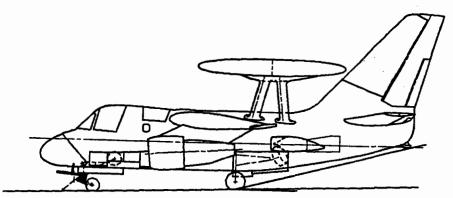


FIG. 37-23 S3 aircraft showing rotodome installation. (Courtesy of Lockheed Aeronautics Systems Company.)

horizontal plane and a 30-dB Taylor (n = 4) aperture distribution was chosen for the vertical plane. The free-space azimuth plane pattern, shown in Fig. 37-24, has a 3-dB beamwidth of 4.75° in the horizontal plane at 900 MHz. When this array is installed in the rotodome above the S3 airframe, the resulting pattern for a 45° look angle from the nose of the aircraft is shown in Fig. 37-25. The integrated two-way SL/ML ratio for the free-space

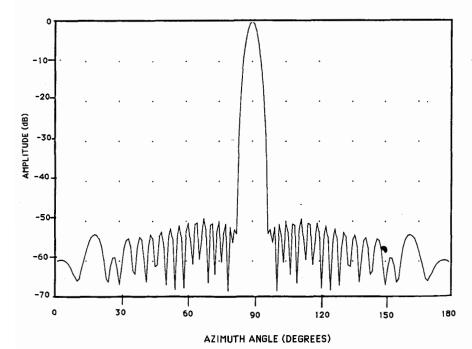


FIG. 37-24 Free-space azimuth plane array pattern. (Courtesy of Lockheed Aeronautics Systems Company.)

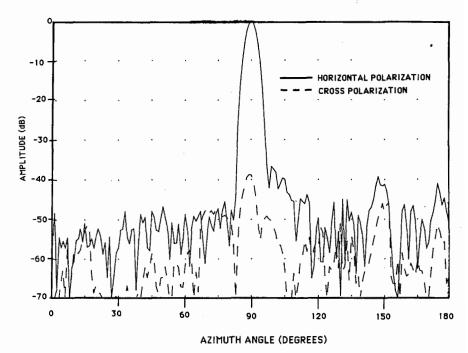


FIG. 37-25 Azimuth plane pattern with the array installed above the S3 airframe with a 45° azimuth look angle. (Courtesy of Lockheed Aeronautics Systems Company.)

radiation pattern is -91 dB. When the array is installed on the S3 airframe, the SL/ML ratio is -71.6 dB. This parameter is indicative of how severe the competing sidelobe clutter might be in a radar application. The acceptability of this much sidelobe degradation would be determined by the radar designer.

37-9 UHF/VHF ANTENNAS

Antennas for Vertical Polarization

The monopole and its variants are the most commonly used vertically polarized VHF and UHF aircraft antennas. The antenna typically has a tapered airfoil cross section to minimize drag. Simple shunt-stub matching networks are used to obtain a voltage standing-wave ratio (VSWR) below 2:1 from 116 to 156 MHz.

The basic configuration of an all-metal VHF blade antenna is shown in Fig. 37-26. This antenna employs a shunt-fed slot to excite the blade. The advantage of this configuration is its all-metal construction, which provides lightning protection and eliminates p static. Figure 37-27 shows a low-aerodynamic-drag sleeve monopole for the 225- to 400-MHz UHF communications system. The cross section is diamond-shaped, with a thickness ratio of 5:1. A feature of this antenna³¹ is the introduction into the impedance-compensating network of a shunt stub such that its inner conductor serves as a tension member to draw the two halves of the antenna together. In addition to providing mechan-

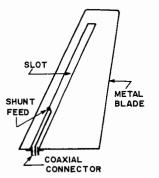


FIG. 37-26 Basic configuration of an allmetal VHF blade antenna.

ical strength, this inner conductor forms a direct-current path from the upper portion of the antenna to the aircraft skin, thereby providing lightning-strike protection.

Figure 37-28 is a broadband monopole/blade antenna matched through a pair of shunt blocks and a series feed with a capacitive section of semirigid coax. The shunt blocks are similar to L/R shunts and are ferrite-based for a gain of -24.5 dBi. There is an abrupt drop-off of antenna performance below 30 MHz.

A number of monopole designs have been developed for installation on a fin in which the top portion of the metal structure has been removed and replaced by a

suitable dielectric housing. Various other forms of vertically polarized UHF and VHF radiators have been designed for tail-cap installation. The pickax antenna, consisting of a heavily top-loaded vertical element, has been designed to provide a VSWR of less than 3:1 from 110 to 115 MHz with an overall height of 15½ in (393.7 mm) and a length of 14 in (355.6 mm).

The basic flush-mounted vertically polarized element for fuselage mounting is the annular slot,³² which can be visualized as the open end of a large-diameter, low-characteristic-impedance coaxial line. As seen from the impedance curve of Fig. 37-29, such a structure becomes an effective radiator only when the circumference of the slot appoaches a wavelength. The radiation patterns have their maximum gain in the plane of the slot only for very small slot diameters and yield a horizon gain of zero for a slot diameter of 1.22.33 This pattern variation is illustrated in Fig. 37-30. For these reasons and to minimize the structural difficulty of installing the antenna in an aircraft, the smallest possible diameter yielding the required bandwidth is desirable. For the 225- to 400-MHz band, the minimum practical diameter, considering construction tolerances and the effect of the airframe on the impedance, is about 24 in (610 mm). A VSWR under 2:1 can be obtained with this diameter and a cavity depth of 4.5 in (114.3 mm). Figure 37-31 shows a design by A. Dórne together with its approximate equivalent circuit. In the equivalent circuit the net aperture impedance of the driven annular slot and the inner parasitic annular slot is shown as a series resistance-capacitance (RC) circuit. The annular region 1, which is coupled to the radiating aperture through the mutual impedance between the two slots, and the annular region 2, which is part of the feed system, are so positioned and proportioned that they store primarily magnetic energy. The inductances associated with the energy storage in these regions are designated as L_1 and L_2 in the equivalent circuit. The parallel-tuned circuit in the equivalent circuit is formed by the shunt capacitance between vane 3 and horizontal disk 4, together with the shunt inductance provided by four conducting posts (5) equally spaced about the periphery of 4, which also serve to support 4 above 3. From this element inward to the coaxial line, the base plate is cambered upward to form a conical transmission-line region of low characteristic impedance. A short additional section of low-impedance line is added external to the cavity to complete the required impedance transformation.

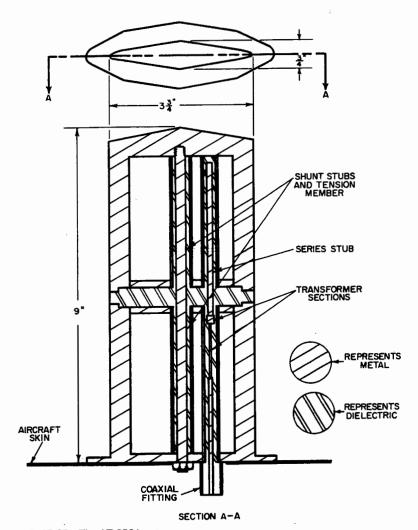


FIG. 37-27 The AT-256A antenna.

Antennas for Horizontal Polarization

There are three basic antenna elements which yield omnidirectional horizontally polarized patterns: the loop, the turnstile, and the longitudinal slot in a vertical cylinder of small diameter. All three are used on aircraft, and all suffer from a basic defect. Because they must be mounted near a horizontal conducting surface of rather large extent (i.e., the top or bottom surface of the aircraft), their gain at angles near the horizon is low. The greater the spacing from the conducting surface, the higher the horizontal gain. For this reason,

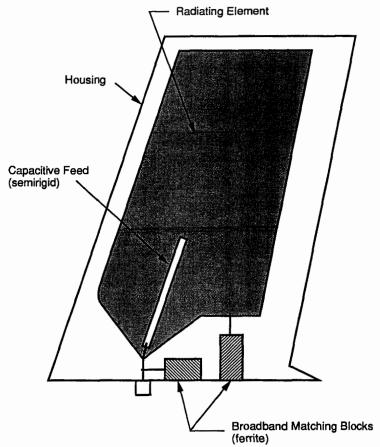


FIG. 37-28 Typical broadband (30-400 MHz) blade antenna, model DMC144. (Courtesy of Dorne & Margolin, Inc.)

locations at or near the top of the vertical fin are popular for horizontally polarized applications, particularly for the VHF navigation system (VOR) which covers the 108- to 122-MHz range.

Figure 37-32 shows an E-fed cavity VOR antenna designed into the empennage tip of the L-1011 aircraft. The antenna system consists of a flush-mounted dual E-slot antenna and a stripline feed network mounted on the forward bulkhead of the cavity between the two antenna halves. The antenna halves are mirror-image assemblies consisting of 0.020-in- (0.508-mm-) thick aluminum elements bonded to the inside surface of honeycomb-fiberglass windows. The feed network consists of a ring hybrid-power-divider device with four RF ports fabricated in stripline. The two input ports for connecting to the antenna elements are out-of-phase ports. The two output ports connect to separate VOR preamplifiers. The operating band of the antenna is 108 to 118 MHz with an

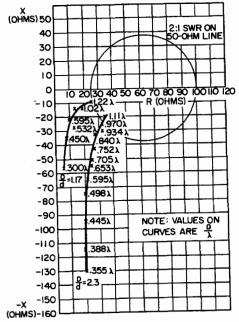


FIG. 37-29 Impedance of an annular-slot antenna.

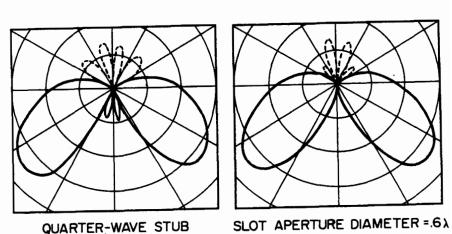


FIG. 37-30 Radiation patterns of an annular-slot antenna and a quarter-wave stub on a 2½-wavelength-diameter circular ground plane.

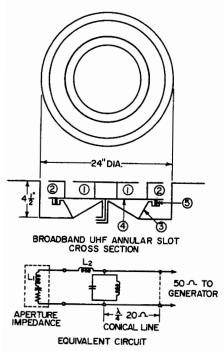


FIG. 37-31 Annular-slot antenna for the 225- to 400-MHz band and its equivalent circuit.

input VSWR of less than 2:1 referred to 50 Ω . Radiation coverage is essentially omnidirectional in the horizontal plane. The principal polarization is horizontal with a cross-polarization component of more than 18 dB below horizontal polarization. The antenna gain is 3.6 dB below isotropic at band center. Figure 37-33 shows the principal-plane voltage radiation patterns.

Figure 37-34 is a single half-loop antenna which is commonly installed on each side of the vertical stabilizer. The installed two-half-loop antenna system is basically a forced-fed balanced loop. The electrical equivalent is a single loop with a single feed with no intervening ground plane. The feed points are 180° out of phase to create a circuitous current flow with cancellation in the plane of the vertical stabilizer. Matching is achieved through one inductive and one capacitive shunt, and the feed gap is joined through a capacitive feed.

The VOR navigation system is particularly vulnerable to the modulation effects of a helicopter rotor since, with this system, angular-position information is contained in a 30-Hz modulation tone which corresponds closely to the third harmonic of the fundamental blade-passage

frequency on a typical helicopter. In Fig. 37-35 are shown two VOR antenna installations on an H-19 helicopter and the horizontal-plane radiation patterns of each. The fine structure on these patterns shows the peak-to-peak variation in signal amplitude due to passage of the rotor blades. The percentage of modulation of the signal received on the horizontal loop antenna is seen to be lower than that received on the ramshorn antenna.

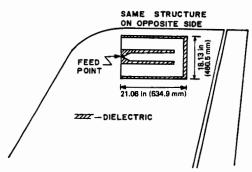


FIG. 37-32 E-slot VOR antenna for the L-1011 aircraft. (From Ref. 34.)

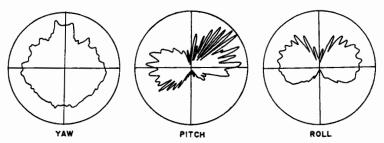


FIG. 37-33 Voltage radiation patterns for the E-slot VOR antenna on the L-1011 aircraft. (From Ref. 35.)

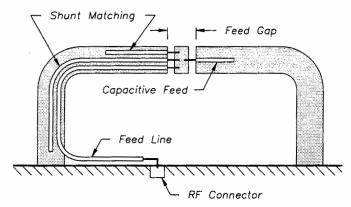


FIG. 37-34 Single half-loop antenna, model DMN4-33. (Courtesy of Dorne & Margolin, Inc.)

This is due partly to the shielding afforded the loop by the tail boom and partly to the fact that the loop antenna has inherently less response to scattered signals from the blades because its pattern has a null along its axis while the ramshorn antenna receives signals from directly above it very effectively.

37-10 HOMING, MLS, AND GPS ANTENNAS

Airborne homing systems permit a pilot to fly directly toward a signal source. Although the navigational data supplied by a homing system are rudimentary, in the sense that only the direction and not the amount of course correction required are provided, the system does not require special cooperative ground equipment. Because of the symmetry of airframes, satisfactory homing-antenna performance can be obtained in frequency ranges in which direction-finder antennas are unusable because of airframe effects.

The principle of operation used in airborne homing systems is illustrated in Fig. 37-36. Two patterns, which are symmetrical with respect to the line of flight and which ideally are cardioids, are generated alternately in time either by switching

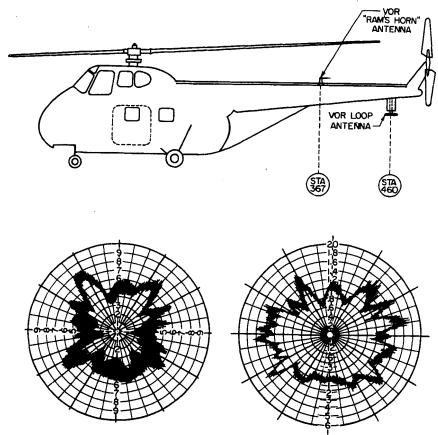


FIG. 37-35 Two VOR-antenna locations on the H-19 helicopter and horizontal-plane radiation patterns.

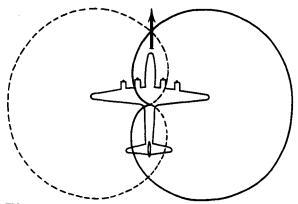


FIG. 37-36 Cardioid homing patterns.

between separate antennas or by alternately feeding a symmetrical antenna array in two modes. The homing system compares the signals received under these two conditions and presents an indication that the pilot is flying a homing course or, if not, in which direction to turn to come onto the homing course. The equisignal condition which leads to the on-course indication can also arise for a reciprocal course leading directly away from the signal source. The pilot can resolve this ambiguity by making an intentional turn after obtaining the on-course indication and noting whether the direction of the required course correction shown by his or her instrument is opposite the direction of the intentional turn (in which case the pilot is operating about the correct equisignal heading) or in the same direction (in which case the pilot is operating about the reciprocal heading).

The required cardioid pattern can be achieved by using two dipole or monopole elements which are nominally spaced 0.25 wavelength apart and which are excited at phases of 0° and $\pm 90^{\circ}$. Figure 37-37 illustrates the frequency dependence of the cardioid pattern. Early systems used a switched transmission line of 0.25 wavelength electrical length to introduce the phase shift. A 90° hybrid also may be used.

The Microwave Landing System (MLS) currently being deployed operates over the 5.031- to 5.091-GHz frequency band. The antenna requirements for this system are not severe, but an omnidirectional azimuth pattern is needed for maneuvering during the approach. Typical MLS antennas are vertically polarized with horizon gains of approximately 3 dB. The use of vertical polarization ensures that the airframe will not create a

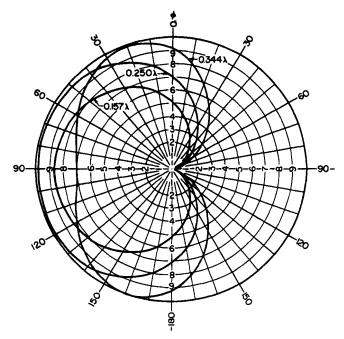


FIG. 37-37 The effect of dipole spacing on the pattern of a homing array.

pattern null at or close to the horizon so that the ground-transmitted MLS signal will be received. Monopole or biconical antenna configurations can satisfy these requirements.

The deployment of the Global Positioning System (GPS) "promises unprecedented worldwide, all-weather navigation capabilities when fully implemented in the 1990s." The GPS system certainly provides general navigation functions and may be extended for Category 1 through 3 landings by the use of Differential GPS (DGPS) techniques. 35,36 This technology is currently being evaluated [see "Comments on Alternatives to the Microwave Landing System (MLS)"]. 36 The GPS satellite transmits information on two frequencies: L_1 at 1575.42 MHz and L_2 at 1227.6 MHz. The L_1 frequency carries a code known as the $C/A\ code$ and a $P\-code$. The L_2 frequency carries only the P-code, which is controlled by the Department of Defense and is encrypted for use of classified military users. 37 Thus GPS antennas are required for both civil and military applications.

In order to obtain maximum position accuracy, a field of view which encompasses four satellites is required. In general, this dictates a near-hemispherical antenna pattern with a coverage extending from near the horizon to the zenith. However, the ideal antenna pattern would maximize horizon gain at the expense of zenith gain due to geometry considerations. That is, the satellites at the horizon are at the maximum range. The GPS satellite transmits right-hand circular polarization. Therefore, a linearly polarized antenna can be employed with a 3-dB gain-loss penalty. Although maximum gain is desirable, low antenna gain is compensated for by the processing gain inherent in the GPS code. Typical GPS antenna gains range from -7.5 to -3 dBci at the horizon to 0 to 4 dBci at zenith, depending on the antenna utilized. For civilian applications, the typical antennas consist of crossed slots, spirals, annular slots, microstrip quadrafiler helixes, and microstrip patches. The patch antennas typically consist of "stacked" patches which are tuned to the two frequencies. These antennas are categorized as "fixed reception pattern antenna (FRPA)." For military applications, which may utilize adaptive null steering to counter interfering jamming signals, a "controlled reception pattern antenna (CRPA)" may be used. These antennas are typically microstrip patch arrays which are capable of adaptive beam forming.

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Seeker Antennas

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	Introduction 38-2
38-2	Seeker-Antenna Electrical
	Considerations 38-2
38- 3	Impact of Airframe on Antenna Design 38-4
38-4	Seeker-Antenna Mechanical Consideration
	38-6
38-5	
	Reflector or Lens Antennas 38-7
	Planar-Array Antennas 38-9
	Multimode and Single-Mode Spirals 38-10

38-6 Small Arrays for Seeker Antennas 38-11

38-7 Radome Effects 38-14

38-8 Evaluation of Seeker Antennas 38-15

38-9 Recent Developments 38-16

This chapter will focus on antennas forward-mounted in a missile functioning in the role of seeker of target emissions. Such a seeker antenna is a critical part of the entire airborne guidance system, which includes the missile radome, seeker antenna, radio-frequency (RF) receiver, antenna gimbal, autopilot, and airframe. The seeker has several functions: to receive and track target emissions so as to measure line of sight and/or line-of-sight angular rate, to measure closing velocity, and to provide steering commands to the missile autopilot and subsequently to the control surfaces. ¹⁻⁶ The signals received by the missile-mounted seeker antenna or antennas are thus utilized in a closed-loop servocontrol system to guide the missile to the target.

The seeker RF elements, radome and antenna, initially discriminate in angle through the seeker antenna's pencil beam. This beam can be steered mechanically (the whole antenna moves), electromechanically (an antenna element such as a subreflector moves), or electronically (there is a phased-array movement). In some situations, the antenna is stationary and only forward-looking; thus beam motion occurs only if the entire missile airframe rotates. Fixed seeker-antenna beams are used when a pursuit navigation (or a variant) guidance algorithm is used. The use of movable seekerantenna beams occurs when a proportional navigation (or a variant) guidance algorithm is used.

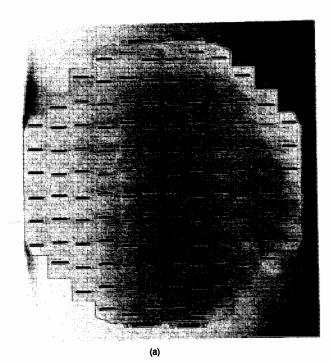
38-2 SEEKER-ANTENNA ELECTRICAL CONSIDERATIONS

Seekers generally fall into one of three categories: conscan, monopulse, or sequential lobing. Implementation details for each of these are well known. In Conscan radars locate the center of the target through the nutation of a single feed (or antenna) that is displaced from the axis. Monopulse antennas most often generate four simultaneous beams which are summed and differenced to produce azimuth and elevation-plane error voltages that are proportional to target displacement from the axis. Sequential-lobing radars sequentially sample the energy in four beams each corresponding to an antenna feed; the error voltage is derived by comparing the amplitude of the signal in opposite feeds.

Conical scan is used primarily for very-short-range, simple guidance systems, because of its vulnerability to a form of ECM known as *spin-frequency jamming*, in which the jammer reradiates the seeker transmission, amplitude modulated at the conical scan frequency, thus creating spurious angle-error signals. 1b Sequential-lobing radars are seldom used in today's high-performance missile guidance systems, giving preference to monopulse, which provides simultaneous lobing of both principal-plane error channels.

Modern polarimetric seeker radars require dual-polarized seeker-antenna performance. ¹⁶ Other parameters of particular concern include instantaneous bandwidth, transmit power capability, and low antenna sidelobe performance. ^{1d}

Seeker antennas can be realized in a variety of technologies ranging from microstrip to waveguide (Fig. 38-1). Table 38-1 presents a summary of commonly employed seekerantenna element types; virtually all these can be implemented in a body-fixed configuration. However, mounting the antenna on a mechanical gimbal is more popular for most missile-guidance applications using proportional (or modern) guidance. Detailed per-



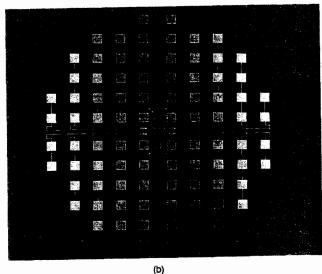


FIG. 38-1 Representative planar-seeker antennas. (a) Waveguide flat-plate antenna. (Photo courtesy of Rantec Microwave & Electronics, Inc.) (b) Microstrip dual-axis monopulse antenna with monolithic comparator. (Photo courtesy of Ball Communications Systems Division.)

Paraboloid

Waveguide

slots

Lens

Large

Large

Narrow

Basic radiator	Bandwidth potential	Polarization	Dual- polarization capability	Power
Stripline	Narrow	Linear or circular	Yes	Intermediate
Microstrip	Narrow	Linear or circular	Yes	Intermediate
Spiral	Large	Circular	No	Low

Linear or circular

Linear or circular

Linear

Yes

Yes

No

High

High High

TABLE 38-1 Seeker-Antenna Radiator Summary

formance and design criteria for the basic antenna radiator types are found in the appropriate chapters of this Handbook.

Many system factors also must be considered in the antenna-design process. Antenna beamwidth determines whether spatial resolution of multiple targets occurs. The sooner that resolution takes place on a flight path, the more time the missile will have to correct errors induced by tracking the multiple-target centroid. Low sidelobes are important because they decrease electronic-jamming effects. This is particularly important if the missile gets significantly close to the jammer during the engagement. Noise injected in this manner can increase the final miss distance.

In a monopulse tracking system, low sidelobes are necessary in both the sum and difference modes in order to reduce the antenna's susceptibility to jamming threats. This creates the problem of achieving simultaneously low sidelobes in the sum and difference radiation patterns. Also, the selection and design of a monopulse feed network cannot proceed without consideration of errors and their effects on pattern performance. Precomparator phase shifts are more critical than postcomparator errors. After the comparator, any phase shifts or amplitude imbalances do not affect the position of the null but will decrease the sensitivity of the detector.

The body-fixed antenna configuration confronts designers with unique problems. The beam may be very broad for a wide field of view (FOV), or it may be rapidly steered to form a tracking beam. The wide-FOV approach requires that the airframe and the autopilot be more restricted in their responsiveness. The steered-beam approach requires rapid beam forming and signal processing to isolate the missile-body rotational motion properly from the actual target motions.

It is often necessary to be able to integrate and test key receiver front-end elements and the RF elements of the transmitter as part of the seeker-antenna assembly. For example, it is generally possible to integrate in one package the feed antenna, monopulse comparator, mixer or mixers, local oscillator, and transmitter oscillator.

38-3 IMPACT OF AIRFRAME ON ANTENNA DESIGN

The airframe and the autopilot steer the missile according to the guidance-computer commands to minimize the final miss distance at impact. The dynamic behavior of the missile in response to commands consists of attitude changes that cause the antenna to

receive through an ever-changing portion of the radome. So This, coupled with the naturalgeometry changes that occur as an engagement takes place, makes the antenna appear to have time-varying directivity and gain properties. The response characteristics of the airframe and the autopilot generate a pseudonoise influence of the radome-antenna combination.

A definition of the angles relating to the seeker-radome and missile-target geometry is illustrated in Fig. 38-2a. Here, the seeker antenna is shown, mounted on a mechanical gimbal whose pointing function is generally controlled by a servo loop. The difference between the actual missile-to-target line of sight (LOS) and the apparent LOS shown in this figure is the radome boresight error (BSE). Missile flight angles are referenced to airframe gyros, while antenna pointing angles are referenced to rate gyros mounted on the antenna gimbal.

The missile-borne gimbaled guidance antenna enters the picture as depicted in the block diagram shown in Fig. 38-2b. This figure shows the major functional features present in missiles and projectiles with on-board guidance. Through the track loop, the antenna gimbal platform is inertially stabilized in space relative to the LOS, and the

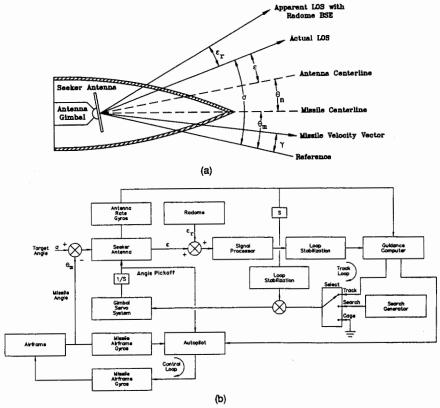


FIG. 38-2 Seeker antenna and overall guidance functional diagram. (a) Seeker/missile/target angular relationships. (b) Tracking system block diagram.

monopulse error voltage drives a feedback loop to keep the antenna pointed toward the target.

For a body-fixed on-board sensor antenna there is no track loop and the body isolation function is not present; the airframe gyros (roll, pitch, yaw) provide angular references for guidance toward the target. The implementations of these functions vary from system to system. Factors such as operational altitude and range, targets to be engaged, missile speed, and terrain over which missions are to be performed also influence the design.^{9,10}

The airframe and the autopilot steer the missile according to the guidance-computer commands to minimize the final miss distance at impact. The dynamic behavior of the missile in response to commands consists of attitude changes that cause the antenna to receive through an ever-changing portion of the radome. This, coupled with the natural geometry changes that occur as an engagement takes place, makes the antenna appear to have time-varying directivity and gain properties. The response characteristics of the airframe and the autopilot generate a pseudo-noise influence of the radome-antenna combination.

38-4 SEEKER-ANTENNA MECHANICAL CONSIDERATIONS

Generally, the seeker antenna is of the maximum size possible within the limits of the missile-body diameter in order to maximize antenna gain and minimize the antenna beamwidth. Alternately conformal- and flush-mounted antennas (most often forward-mounted) utilize the entire conical forward area to achieve maximum gain.¹¹

Gimballed antenna systems often must mechanically steer not only the antenna structure but also the attendant beam-forming network and critical transmitter and receiver elements. As the mechanical-steering rates become excessive, the conformal-mounted antenna with electronically steered beams must be used. ¹⁰⁻¹⁶ When all the seeker-antenna and associated hardware are gimballed together, the use of lightweight materials may achieve the desired results. Lightweight techniques include: ^{8,17}

- 1 The use of lightweight honeycomb materials (including low-density dielectric foams) for both filler and structural-load-bearing surfaces. Foam reflectors and waveguide elements including feed horns can be machined and then metallized by vacuum deposition, plating, or similar techniques.
- 2 The use of stripline techniques. Using multilayer techniques, one can have a layer with microstrip radiating elements, a layer with beam-forming networks, and a layer with beam-switching and signal-control elements such as a diode attenuator and phase shifters. The use of plated-through holes and/or pins to make RF connections can eliminate cables and connectors. Excess substrate can be removed and printed-circuit-board edges plated in lieu of the use of mode-suppression screws.
- 3 The use of solid dielectric lenses, above Ku band, with no significant weight penalty. Lenses can also be zoned to remove excess material.¹⁸

38-5 APERTURE TECHNIQUES FOR SEEKER ANTENNAS

Precise control of both amplitude and phase to permit aperture illumination tailoring is necessary for achieving a well-behaved antenna pattern. Page 4 Aperture tapering of rotationally symmetric illuminations starts with the feed itself and continues by varying the energy across the aperture by several methods: corporate-power splitting, aperture-element proportional size or spacing, surface control of the reflector or lens surface, and element thinning. Several of these aspects are discussed below.

Reflector or Lens Antennas

A consideration in the design of monopulse reflector antennas is the four-horn-feed design and the effects of aperture blockage. One criterion posed for an optimum monopulse feed configuration is maximizing the product of the sum times the derivative of the difference error signal. The monopulse horn size for optimum monopulse sensitivity is shown in Fig. 38-3. The impact of optimizing monopulse feed design on antenna performance is illustrated in Fig. 38-4, in which a 5.5-in- (139.7-mm-) diameter aperture is assumed in the calculations. These data illustrate that at millimeter wavelengths (above 30 GHz) the effects of aperture blockage on antenna performance are small for this size of antenna even when a reflector is used.

Other criteria, such as the requirement for equal E- and H-plane antenna beamwidths, may enter into the details of monopulse feed design. An example of a monopulse-feed antenna operating near 95 GHz that meets equal-beamwidth requirements is shown in Fig. 38-5.²⁷ Here, the subaperture dimensions are very small [0.080 by 0.100 in (2.032 by 2.54 mm)], and an electroformed process was required in the feed fabrication.

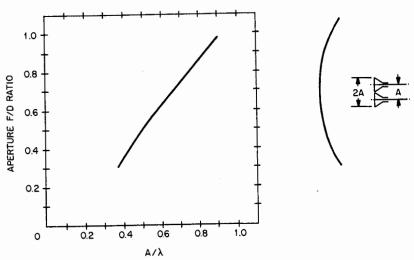
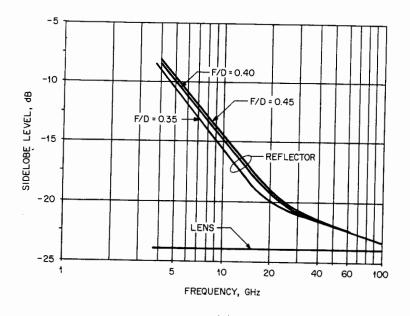


FIG. 38-3 Monopulse antenna horn size or spacing for optimum monopulse sensitivity.



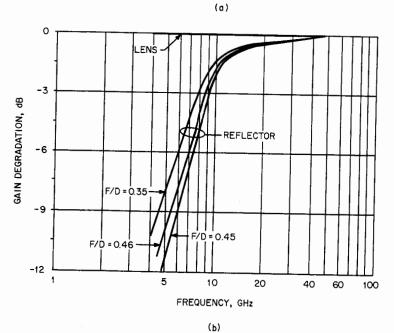


FIG. 38-4 Performance of optimized four-horn monopulse-fed 5.5-in-(139.7-mm-) diameter apertures. (a) Sidelobe level. (b) Gain degradation.

A wide-angle-scan capability can be achieved by using a twist-reflector concept with a rotatable planar mirror. 28,29 In this configuration, the forward nose of the missile can be approximately paraboloidal-shaped, or the paraboloid can be located inside a higher-fineness-ratio radome. This paraboloid is composed of horizontal metal strips. The movable planar twist reflector uses 45°-oriented strips $\%\lambda$ above the planar metallic reflector. (Grids may also be used to combine widely separated frequencies to permit dual-band operation. 30)

Beam steering is obtained by moving the planar mirror. The steering is enhanced because for every 1° that the mirror moves the beam moves 2°. By using a parallelogram gimbal to move the planar mirror, beam accelerations of 20,000°/s² have been demonstrated.²9 In this situation a 42° beam scan was achieved with 21° of mirror motion, and less than 2 dB of sidelobe degradation of the sum pattern occurred.

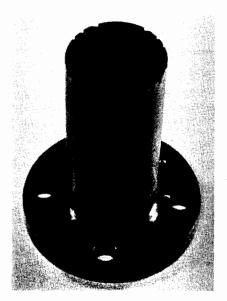


FIG. 38-5 Monopulse-feed antenna (95-GHz operation). (After Ref. 27.)

By using a corrugated horn with a rotationally symmetric feed pattern providing a -17-dB edge taper (capable of achieving a -30-dB sidelobe level), one can further taper by varying the innerand outer-surface contour of a collimating lens to achieve a circular Taylor amplitude distribution ($\bar{n}=7$) with a -40-dB sidelobe level. Practically, one can make the lens out of a material having an $\varepsilon_r = 6.45$ (titania-loaded polystyrene) and follow up with a surface-matching layer made out of a material having an $\varepsilon_r = 2.54$ (Rexolite-polystyrene).

Planar-Array Antennas

Array techniques can be used to provide a nearly planar (flat-plate) aperture. Commonly used are arrays that provide symmetric patterns and offer a maximum use of the available circular aperture with reduced grating-lobe potential. In such an array, higher aperture efficiency with low sidelobes can be achieved

because of reduced aperture blockage and spillover. In monopulse applications, it is noted that the ring array contains no central element and exhibits quadrantal symmetry, as indicated in Fig. 38-6.

The choices in a ring-array design include the number of rings and the number of elements in each ring and the feed network, 31,32 Constraints include:

- 1 Minimum distance of the outer elements to the antenna edge
- 2 Minimum spacing of the elements as impacted by excess mutual coupling (between elements and quadrants and feed geometry)
- 3 Desired radiation pattern (as impacted by the density tapering)

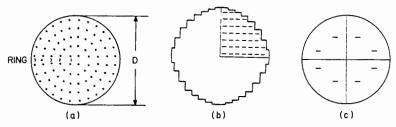


FIG. 38-6 Monopulse planar-array geometries. (a) Five-ring monopulse array. (b) Waveguide slot array. (c) Thinned-slot (image) ring array.

Optimization of small ring arrays (having diameters <10 λ) is often carried out heuristically or nonlinearly. Examples of array geometries that have been analytically determined to have -17- to -20-dB sidelobes are given in Table 38-2 for the array geometry shown in Fig. 38-6a.

Array elements can be of many types. 33-40 A two-dimensional array of waveguide slots (Fig. 38-6b) excited by a network of parallel waveguides forming the antenna structural supports has been used.³⁹ Waveguide slot arrays have demonstrated low cross-polarized response as well. The bandwidth of a waveguide slot array is inversely proportional to the size of the array. A variety of outer contours can be utilized to conform to the space available.

Techniques for thinning these types of arrays reduce complexity.⁴¹ By using an image-element approach, a reduction of the number of elements by over 90 percent is possible (Fig. 38-6c). This method also readily allows for integration of the monopulse comparator.

Multimode and Single-Mode Spirals

The multimode spiral antenna is a very broadband, broad-beamed, circularly polarized antenna which is amenable to ARH (antiradiation homing) applications.⁴² Such an

Case B†

TABLE 38-2 Data on Five-Ring Monopulse Uniformly Excited Array* Case At

	Maximum sidelobe level = -20 dB	Maximum sidelobe level = -17 db	
Ring number	Radius, λ		
r ₁	0.45	0.50	
<i>r</i> ₂	1.25	1.33	
<i>r</i> ₃	2.08	2.16	
r ₄	3.06	2.98	
<i>r</i> ₅	3.72	3.72	

^{*}After Ref. 31.

The maximum outer diameter = 8.16λ for both cases.

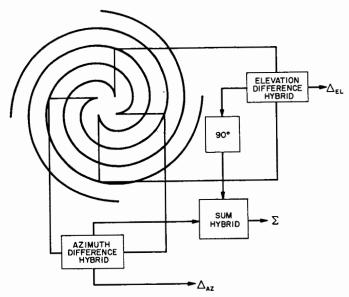


FIG. 36-7 Monopulse circuit for a four-arm spiral antenna.

antenna can also be synthesized by using a circular array.⁴³ The circuit to resolve monopulse sum-and-difference patterns is shown in Fig. 38-7; typical angular coverage is from ± 30 to 40°. The rather wide instantaneous FOV makes these antennas attractive for body-fixed applications.

The printed-circuit construction of four-arm spirals limits their use to low-power applications. Thus, this type of antenna is almost always used for passive (nontransmitting) applications. Loading techniques can be employed to reduce size, permitting operation at low frequencies. 44 Current fabrication technology permits high-frequency operation to above 40 GHz. Single-mode spirals are also very useful as elements in small arrays.

38-6 SMALL ARRAYS FOR SEEKER ANTENNAS

Arrays of two, three, four, and five elements can be used for seeker antennas in small interferometers. These types of arrays are usually fixed-mounted (nongimballed) and used when pursuit navigation algorithms are suitable. With the addition of a gyroscope to sense missile angular motion, line-of-sight data can be derived.⁴⁵

Good sum-and-difference or phase monopulse angle-tracking performance can be achieved when the array elements, the array beamwidth, and the array element spacing are properly chosen. Broadband performance is often achievable by using antenna elements such as spirals or log-periodic antennas.

The receiving arrays as shown in Fig. 38-8 are either two-element (rolling missile) or four-element (stabilized missile). The third or fifth element can be used for transmission. The equations for the receiving voltage pattern are

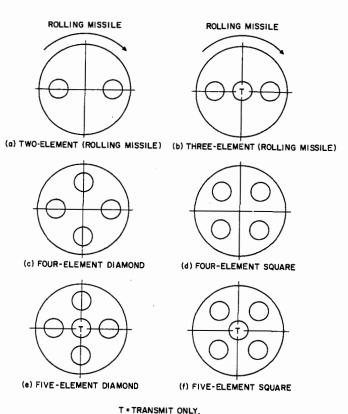


FIG. 38-8 Small-array geometries.

$$\Sigma_4 = \left[1 + \cos\left(\frac{\pi d}{\lambda}\sin\theta\right)\right] f(\theta)$$

$$\Sigma_2 = \left[\cos\left(\frac{\pi d}{\lambda}\sin\theta\right)\right] f(\theta)$$

$$\Delta_2 = \left[\sin\left(\frac{\pi d}{\lambda}\sin\theta\right)\right] f(\theta)$$

where $f(\theta)$ = element pattern [$\cos^m(\theta)$ is often used.]

d = center-to-center element spacing

 λ = operating wavelength

These equations can be used to determine either the principal-plane (0°) or the intercardinal-plane (45°) pattern. Figure 38-9 indicates the appropriate array dimensions and equations to use for each case. Also shown are the two comparator networks used for either diamond or square arrays. Small arrays can be used by themselves, or they can illuminate apertures such as reflectors or lenses. Control of the array element

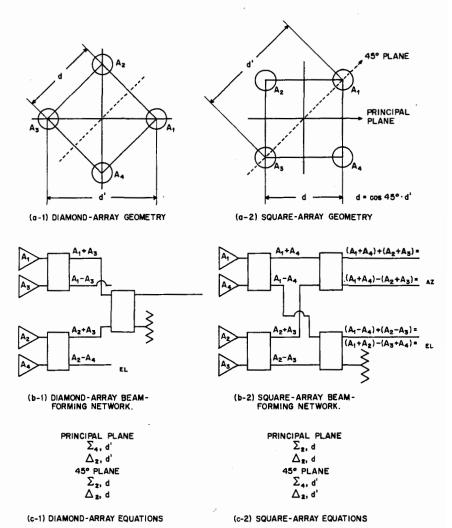


FIG. 38-9 Square or diamond interferometer array parameters.

pattern is important in reducing energy spillover beyond the difference-pattern lobes. Often one can achieve this control by using end-fire techniques with the elements. For example, dielectric rods can be used for waveguide, printed-circuit, and spiral elements. An example of this approach is shown in Fig. 38-10.

A four-element array can serve as an RF seeker by utilizing a phase processor. The effects of system errors for such an array on antenna patterns, S curves, and angular sensitivity as ascertained analytically can be used to form a catalog of results that can be employed to diagnose fabrication errors or tolerances based on measured data. 46

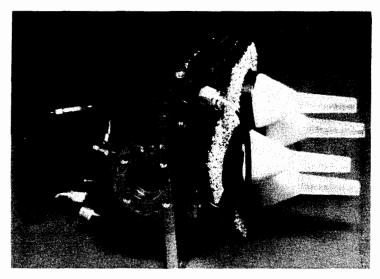


FIG. 38-10 Four-element seeker array using dielectric rods and spiral antennas. (Photo courtesy Eaton Corporation, All. Division.)

38-7 RADOME EFFECTS

The introduction of a protective radome over a seeker antenna results in an apparent boresight error (BSE) because of the wavefront phase modification over the seeker-antenna aperture. (Radome-analysis methods are discussed in greater detail in Chap. 44.) These effects need to be carefully considered in the selection of a radome design since they impact seeker-system performance. 9.47-49

In the case of pursuit guidance, the miss distance is proportional to the BSE. Conversely, in the case of proportional guidance, it is the boresight-error slope (BSES) that more directly impacts miss distance. The relationship between BSE or BSES and miss distance is not straightforward but generally is quantified only by a hardware-in-the-loop (HWIL)^{50,51} or computer simulation that takes into account a variety of scenarios and flight conditions. A BSE requirement of better than 10 mrad (or a BSES requirement better than 0.05 deg/deg and maximum transmission loss of 1.0 dB are typical for many radome types.

The method most often employed for the evaluation of radome effects on seekerantenna performance utilizes open-loop testing in a suitable anechoic-chamber facility. ⁵² This requires a precalibration of the monopulse error-channel sensitivity in volts per degree without the radome and subsequently measuring the error-channel outputs with the radome over the seeker antenna.

Broadband ARH antennas generally require the use of multilayer radome walls to obtain a required radome bandwidth commensurate with antenna performance. Figure 38-11 illustrates hemispherical-radome performance for half-wave, full-wave, A and B sandwich walls. Half-wave radomes generally have a useful bandwidth on the order of 5 to 20 percent, depending on dielectric constant and radome-fineness ratio. Higher-order wall radomes have considerably narrower useful bandwidths and

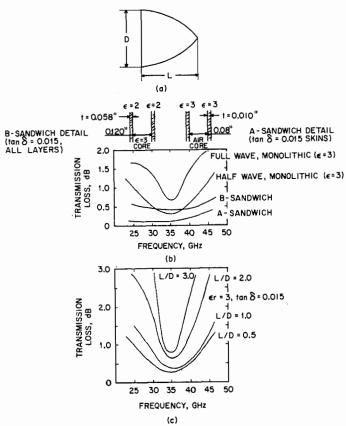


FIG. 38-11 Missile-radome transmission data. (a) Radome geometry. (b) Hemispherical-radome (L/D=0.5) performance for a low-velocity (<Mach 1) missile. (c) Monolithic half-wave radome performance for various fineness (L/D) ratios.

thus are limited to narrowband-antenna applications. Figure 38-11 also demonstrates transmission loss versus frequency for a half-wave wall radome when radome-fineness ratio is taken as a parameter.

38-8 EVALUATION OF SEEKER ANTENNAS

Seeker-antenna testing proceeds from conventional methods utilizing anechoic-chamber techniques with the antenna alone.⁵³⁻⁵⁷ Next, open-loop testing including critical elements of the seeker electronics (S curves) is most often performed. Ultimately a variety of simulations are used to ascertain the seeker-antenna performance in both benign and complex environments.

The many nonlinear elements in the guided missile make complete closed-form analytical simulations unsuitable for final analyses. The precise simulation of these elements is also difficult. The final analyses are best done with an HWIL simula-

tion. ⁴⁹⁻⁵¹ As many hardware items as possible should be inserted, leaving only the propulsion, aerodynamics, and instrument feedback to be simulated analytically.

There are several concepts for implementing a simulation with seeker hardware. Placing the seeker in an anechoic chamber with the target of appropriate characteristics moved about according to the engagement geometry is one method. Flying a target with the seeker on an orientation table is another.

The HWIL simulation serves as a tool not only for statistical performance analysis but for provision of validity information for an improved all-analytical model of the system. The HWIL method provides the only valid present means of evaluating the interaction of the radome-antenna combination in a missile-guidance-seeker environment.

38-9 RECENT DEVELOPMENTS

A number of recent technology advances 58,59 are affecting the design and fabrication of seeker antennas as summarized in the following:

- 1 Low-mass antenna techniques for high-g environments:
 - Use of negative space, i.e., plated hollow areas for feeds and transmission lines, e.g., horns, waveguides
 - Use of physically small (but electrically large) apertures, including
 - + Slots
- + Dipoles
- + Patches
- + Spirals

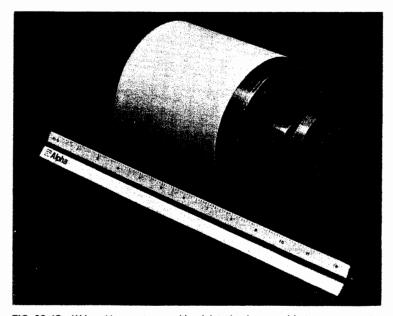


FIG. 38-12 W-band lens antenna with miniaturized waveguide-type comparator feed assembly. (Photo courtesy Alpha Industries, Inc.)

- Use of thin, flat, printed-circuit reflector antennas⁶⁰
- 2 Advanced seeker-antenna manufacturing techniques:
 - Higher millimeter frequencies, i.e., above 100 GHz
 - Nonplanar geometries, i.e., conical spirals
 - Slotted waveguide antennas at Ka-band and above⁶¹ and waveguide monopulse comparators at W-band (see Fig. 38-12)
 - Millimeter-wave microstrip antennas (including annular rings) and microstrip comparators^{1d}
 - Better packaging techniques to divide aperture space among several antenna requirements^{1b,62}
- 3 Small four-element arrays using both amplitude and phase monopulse techniques (amplitude monopulse used to resolve phase ambiguities)

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Direction-Finding Antennas and Systems*

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Technology for Communications International

39-1 Introduction 39-2 Radio Direction-Finding Systems 39-2 Applications of Direction-Finding Systems 39-2 System Approach to Direction Finding 39-3 39-2 Radio-Wave Propagation 39-4 Propagation Characteristics 39-4 Frequencies in the Low- and Medium-Frequency Bands 39-4 Frequencies in the High-Frequency Band 39-5 Frequencies in the Very-High-Frequency and Ultrahigh-Frequency Bands 39-6 39-3 Direction-Finding-System Planning 39-6 Geographic Area and Frequency Coverage 39-7 Number and Location of Stations in a Direction-Finding

Network 39-7

Speed 39-10

Measurement Accuracy and

39-4 Direction-Finding-System
Design 39-12
Types of Direction-Finding
Systems 39-12
Receivers 39-14
Direction-Finding Processor 39-15
System Control/Output
Arrangements 39-17

39-5 Direction-Finding Antenna Elements and Arrays 39-18 Antenna Elements 39-18 Arrays of Direction-Finding

Antenna Elements 39-19
39-6 Sources of Emitter-Location Error
39-28

Angular-Measurement Error 39-28 SSL Distance Error 39-31 Emitter-Location Error 39-33

39-7 Performance of HF Sky-Wave
Direction-Finding Systems 39-34
Factors Affecting Performance
39-34

Performance Comparison of HF Sky-Wave Direction-Finding Systems 39-35

Radio Direction-Finding Systems

A radio direction-finding (DF) system is basically an antenna-receiver combination arranged to determine the azimuth of a distant emitter. In practice, however, the objective of most DF systems is to determine the location of the emitter. Virtually all DF systems derive emitter location from an initial determination of the arrival angle of the received signal. Figure 39-1 a shows how the location of the emitter is found if azimuth angles are measured at two DF stations connected by a communication link and separated by a distance that is comparable with the distance to the emitter. The determination of emitter location by using azimuth angles measured at two or more DF stations is known as horizontal or azimuth triangulation.

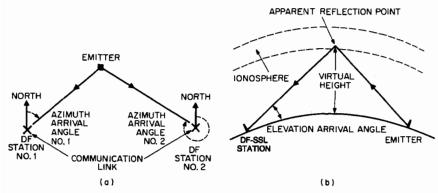


FIG. 39-1 Emitter location by triangulation. (a) Horizontal (azimuth) triangulation. (b) Vertical triangulation (single-station location).

In the high-frequency (HF) band (approximately 2 to 30 MHz), emitter location by using only a single DF station is possible. Such an arrangement is known as a single-station-location (SSL) system.² A DF-SSL system can only be used when the signal arrives at the DF station after only one refraction through the ionosphere (i.e., via single-hop sky-wave propagation), as illustrated in Fig. 39-1b. The DF-SSL system must be able to measure both the azimuth and the elevation angles³ of the signal arriving at the DF station. Furthermore, the height of the ionosphere must be either known or determined. The measured elevation angle, in conjunction with knowledge of the height of the ionosphere, enables the distance to the emitter to be established. This process is known as vertical triangulation. Emitter location is then calculated by using azimuth and SSL distance from the DF station.

Applications of Direction-Finding Systems

There are four principal applications for DF systems which influence the details of their design:

1 DF systems that are designed to determine the unknown location of an emitter. Such systems may be fixed or movable.

- 2 Navigation systems designed to determine the location of the DF system itself with respect to emitters of known location. The DF system is on a moving vehicle (ship or aircraft), and azimuth angles are measured to two or more emitters at the same time or at successive times on the same emitter. The determination of the position of the vehicle is the complement of the horizontal triangulation process illustrated in Fig. 39-1 a.
- 3 Homing systems that are designed to guide a vehicle carrying a DF system toward an emitter which may be either a beacon of known location or an emitter of unknown location.
- 4 Signal-acquisition systems, wherein azimuth angle of arrival is a useful sorting (or recognition) parameter. Such DF systems must necessarily be fast and fully automatic.

System Approach to Direction Finding

The essential components of any DF system are shown in Fig. 39-2. They comprise:

- 1 An antenna system to collect energy from the arriving signal
- 2 A receiving system to measure the response of the antenna system to the arriving signal
- 3 A processor to derive the required DF information (for example, azimuth and elevation angles and emitter location) from the output of the receiver
- 4 A system control/output device in a form convenient to the user

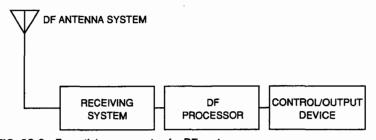


FIG. 39-2 Essential components of a DF system.

In the past, each component of a DF system was often regarded as a separate design problem. Attention was focused mainly on the antenna because in general it imposed the major constraints on performance. Some form of symmetry was usually required, and the choice of antenna type was usually quite limited. However, the advent of small high-speed digital computers has meant that DF-system designers now have more freedom in their choice of DF antennas and that full use can now be made of antenna-system responses. That is, most older systems made use of either amplitude response or phase comparison but not both. Furthermore, most older systems were restricted to the use of only one linear polarization. The employment of real-time signal-processing techniques now makes it possible to use both phase and amplitude responses, to use antennas of any polarization, to respond to signals of any polarization, and to dynamically normalize (calibrate) the responses of any multiple-receiver system so that standard communication receivers can be used. It is therefore desirable that a DF

system for all but the simplest applications be designed as a complete integrated system to take full advantage of these possibilities. This chapter will discuss antenna-design principles in the context of complete DF systems.

39-2 RADIO-WAVE PROPAGATION

Propagation Characteristics

The performance of a DF system depends on the nature of the signals arriving at the DF antenna. In turn, the nature of these signals depends on the mode of propagation, which will fall into one of two broad categories:

- 1 Signals that arrive directly at the DF antenna from the emitter with near-zero elevation angle. Included in this category are low-frequency (LF), medium-frequency (MF), and HF surface waves which will be vertically polarized and very-high-frequency (VHF), ultrahigh-frequency (UHF), and microwave direct-wave signals which may be of any polarization.
- 2 HF signals that are refracted from the ionosphere and arrive at the DF antenna with an elevation angle that may vary from a few degrees to nearly 90°. Irrespective of their transmitted polarization, these signals will be elliptically polarized upon arrival at the DF antenna system. That is, the two polarization components will vary independently with time.^{4,5}

Whether the signals arriving at the DF antenna fall into category 1 or category 2 or include both categories depends primarily on the frequency band and secondarily on the daily and seasonal variations of the ionosphere.

Frequencies in the Low- and Medium-Frequency Bands

In these bands, during the day only a vertically polarized surface wave is propagated since sky waves are absorbed in the D layer of the ionosphere. However, at night the D layer disappears, and signals are refracted from the ionosphere so that sky-wave signals can arrive at the DF antenna.

The surface wave is attenuated with distance so that, depending on time of day, transmitter power, ground conductivity, and distance of the DF site from the emitter, three types of received signal may exist:

- 1 Near the emitter the vertically polarized surface wave will predominate because the sky wave will always be small with respect to it.
- 2 With increasing distance, the surface wave becomes attenuated. At night there will be a zone (known as the *fading zone*) in which sky wave and surface wave are comparable in magnitude. Fading occurs owing to interaction between surface and sky waves.
- 3 At distances beyond the fading zone the surface wave becomes highly attenuated so that the only receivable signal at such distances will be the night-time sky wave.

Magnitude of the surface wave (which primarily determines the distance of the fading zone from the emitter) increases with increasing ground conductivity and

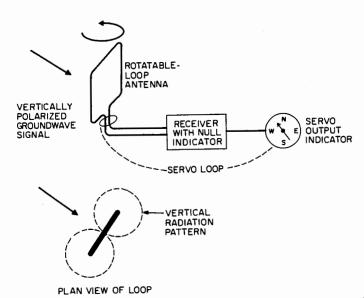


FIG. 39-3 Sample of a system using a rotatable loop.

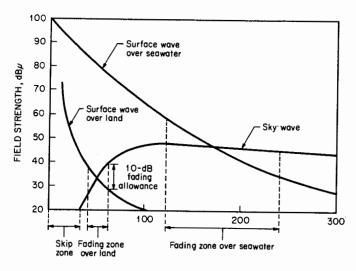
decreasing frequency. Thus, in the LF and lower MF bands the signal available at the DF site is, in most cases, predominantly a surface wave arriving at zero elevation angle. But in the upper MF band the signal may be a combination of surface and sky waves or, alternatively, a sky wave alone, especially at night.

A simple rotating-loop arrangement, as shown in Fig. 39-3, has an amplitude response to vertically polarized signals shaped like a figure of eight. During daylight hours, when only a vertically polarized field is present, the two nulls will give an accurate determination of bearing if means are provided to remove the 180° ambiguity. However, the amplitude response of the loop to horizontally polarized signals is also a figure of eight, but rotated 90° in space in relation to the vertically polarized response. At night, in the presence of a sky wave, which will have both vertically and horizontally polarized field components, there will be no nulls or maxima with a fixed relationship to the loop orientation. Consequently, an accurate measurement of bearing is impossible. This phenomenon is referred to as night effect or polarization error. It illustrates a fundamental difficulty that arises when sky waves are received by DF systems that depend only on the amplitude of the signal and when the antenna system is responsive to horizontal polarization.

Frequencies in the High-Frequency Band

In this band the attenuation of the surface wave over land is high, as is illustrated in Fig. 39-4. In many cases only a sky wave arrives at the DF site. However, over seawater the surface and sky waves will be comparable in magnitude at much greater distances.

At distances up to about 2000 km the sky-wave signal may arrive via one refraction from the ionosphere (a *one-hop mode*). But at any except the very shortest distances multihop signals, in addition to the one-hop signal, can occur. The arriving signal will then consist of a number of components of different amplitudes, of random



DISTANCE FROM EMITTER, km

FIG. 39-4 Approximate variation of HF field strength with distance for 1-kW emitter power at a frequency in the lower part of the band.

phase, and with different elevation angles. As these components vary with time in both amplitude and phase, the arriving wavefront will be distorted and the azimuth and elevation angles of the signal will vary. When DF measurements on such complex signals are necessary, simple amplitude-only DF systems are inadequate. However, systems employing digital computers and using suitable analytical programs can provide accurate measurements of bearing, elevation angle, and emitter location under these conditions (see Sec. 39-4).

Frequencies in the Very-High-Frequency and Ultrahigh-Frequency Bands

At frequencies above about 50 MHz the ionosphere becomes transparent to radio transmission. Propagation is by direct wave, and polarization is determined by the transmitting antenna. It may be vertical or horizontal or may contain both vertical and horizontal components. Furthermore, range is limited because the signal is rapidly attenuated beyond the line of sight, although diffraction over the horizon and atmospheric refraction can give rise to reception from beyond line of sight. Another cause of nondirect waves at VHF/UHF is reradiation and scattering of the transmitted signal from buildings, structures, or elevated landforms.

39-3 DIRECTION-FINDING-SYSTEM PLANNING

Planning a DF system (which may comprise a single station or a network of stations) must take into account a number of factors of major importance:

Geographic area in which the emitters are located in relation to the DF stations.

- · Frequencies of the emitters.
- Number of DF stations necessary to ensure adequate accuracy of measurement.
- Response time (the minimum time in which a measurement must or can be made).
- Physical limitations of the system. These may include the space available for antennas, the need (or not) for a movable system, and limitations on equipment size, weight, and complexity.

Geographic Area and Frequency Coverage

The geographic area in which emitters are located in relation to the available locations of the DF stations will determine the maximum and minimum distances over which signals must be received. These maximum and minimum distances, together with the frequency range in which the emitters operate, enable the most likely propagation modes to be identified so that the optimum DF system can be chosen.

Emitter-Location Systems If the area in which the emitters are situated is known and will remain fixed and if all the emitters are within propagation range of the proposed DF sites, a fixed-site emitter-location DF system will be chosen. Fixed-site DF systems have the advantage that it is possible to use electrically large antennas and antenna arrays, which are faster and more accurate than small-aperture systems. Furthermore, electrically large antenna elements have low noise figures, enabling DF measurements to be made on relatively low-field-strength signals unless the received signal-to-noise ratio is limited by external noise.

On the other hand, the area of the emitters may vary or be located so that it is not possible to receive adequate signals from the emitters at fixed DF sites. In this case it may be necessary to use a movable DF system with electrically small antenna elements. (But movable DF systems can employ large-aperture arrays. See Sec. 39-5.)

Navigation and Homing Systems If the objective is aid to navigation or homing, the DF system will be mounted on a moving vehicle. This will impose a serious limitation on the antenna system. As an offset to the antenna disadvantage, such systems normally have the advantage of operating over short ranges in a fixed and narrow frequency band using direct or surface waves. The need for electrically large antennas is not so great as would be the case if sky waves were involved.

Number and Location of Stations in a Direction-Finding Network

The number and location of stations in a DF network have a direct effect on the accuracy with which an emitter can be located. The limitations of radio propagation as well as the usual geometric limitations on the accuracy of triangulation must be considered.

Horizontal Triangulation (Azimuth) Under optimum conditions, measurements of bearing from two separated DF sites are sufficient to determine location. In practice, location of the DF sites may not be optimum so that three sites are the practical minimum. By using just two sites, minimum location error will occur when the two lines of bearing intersect at 90°. With reference to Fig. 39-5, if radius R is the standard deviation of error for two lines of bearing intersecting at right angles, then R'

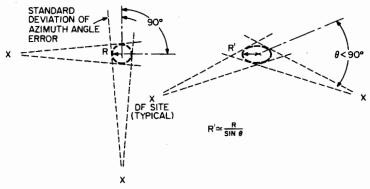


FIG. 39-5 Horizontal triangulation, using two DF sites.

will be the major-axis radius of an ellipse of error when the two lines intersect at less than 90°.

If the two sites are not optimally sited or if one site is unable to determine a line of bearing for any reason, a third site will prove valuable. A third site is likely to increase location accuracy in any case, but only a small further increase in accuracy will likely result from more than three sites. (See Fig. 39-6.)

The minimum spacing between DF sites should depend on the expected distance to the emitter. For a given site spacing, there is a maximum range at which an emitter can be located with any reasonable accuracy. This means that, quite apart from the limitation of DF range imposed by propagation conditions, a limitation is also imposed by the spacing between the DF sites.

Ideally, the sites of a DF system would be placed uniformly round the edge of the area containing the emitters, as illustrated in Fig. 39-7a, but geographic features, national boundaries, and communication problems between the DF sites sometimes make this impossible. In such cases the best arrangement is to locate the sites of a DF network as close as possible to the area containing the emitters, keeping the sites as far apart as possible.

The following general rules, which are illustrated in Fig. 39-7b, c, and d, give a useful guide for DF siting:

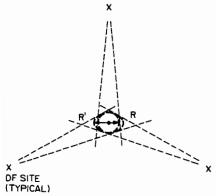


FIG. 39-6 Horizontal triangulation, using three DF sites.

- As shown in Fig. 39-7b, DF sites should be evenly spaced, and the distance between adjacent sites should be at least equal to the distance across the area containing the emitters.
- If none of the DF sites can be located close to the area containing the emitters, the distance between sites should be approximately equal to the distance between the centroid of the area and the centroid of the DF sites, as shown in Fig. 39-7c.

If one of the DF sites is so close as to be in the sky-wave skip zone of one of the emitters (so that no signal is available), the foregoing spacing criteria will maximize the probability that one or more of the other sites will receive a signal. This assumes that the emitter is transmitting a signal to a location in the area containing the other emitters.

In addition to the foregoing DF-station-siting criteria, the various DF sites

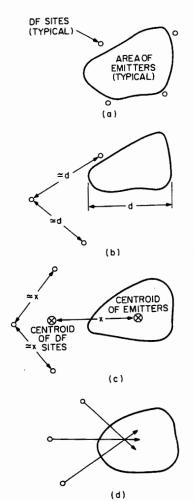


FIG. 39-7 Distribution of DF sites for minimum horizontal triangulation error. (a) Ideal distribution of DF sites. (b) Approach to ideal distribution of DF sites. (c) Optimum distribution if no DF site can be near the target area. (d) DF site location with respect to other fixed sites. Sites should be located on nonparallel baselines and as nearly in a triangle or a square as possible.

should be located with a nonparallel baseline, as illustrated in Fig. 39-7d. Arranging the sites in a triangle or a square will minimize azimuth triangulation error.

Vertical Triangulation (Single-Station Location) Single-station location (SSL) against sky-wave signals by definition requires only one site. Azimuth measurement is used to determine direction to the emitter, and elevation measurement, in conjunction with the height of the ionosphere, is used to determine distance to the emitter. Location error of the emitter will depend on the accuracies with which the DF system can determine direction and distance. These two parameters are subject to different causes of error:

- The accuracy with which direction can be determined will be identical to that of a single conventional DF system.
- The accuracy with which distance can be determined will depend on the errors inherent in measurement of elevation angle, on the accuracy with which the height of the ionosphere can be calculated or measured, and on the validity of the assumption that only a single-hop signal is being received. (See Fig. 39-8.)

The accuracy of a DF-SSL system will be higher for azimuth than for distance. Although single-station location is generally less accurate than multistation triangulation, SSL can offer significant advantages of reliability, simplicity, and speed of operation since interstation communications and correlation of separate measurements are not necessary.

A number of DF-SSL sites can be used in a network for improved emitter-

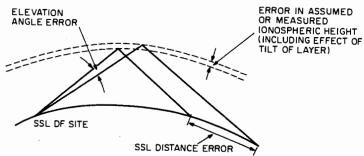


FIG. 39-8 Effect of angular and ionospheric errors on SSL distance measurement.

location accuracy. The form of the location process will be different from the conventional azimuth triangulation process. (See Sec. 39-6.)

Measurement Accuracy and Speed

The measurement accuracy of all DF and emitter-location systems is affected to a first order by six main parameters:

- 1 Aperture of the antenna system
- 2 Instrumental accuracy of the measuring system, which includes the effects of errors in antenna performance, site error due to local scattering and ground irregularity, equipment and processing error, and operator error in the case of manually operated DF systems
- 3 Ionospheric behavior in the case of systems operating in the upper part of the MF band and in the HF band
- 4 Received signal-to-noise ratio
- 5 Integration time, that is, the time over which the signal is averaged in the measurement process
- 6 The distance of the emitter from the DF site or sites

Because the effects of noise and of some forms of ionospheric error are decreased with integration time, measurement speed (inverse of the minimum time that is required for a measurement) and accuracy (the accuracy with which an emitter can be located) are linked together. There is a speed-times-accuracy product that is relatively stable for a given DF system (see Sec. 39-7). Large-aperture systems tend to be fast and accurate, whereas small-aperture systems tend to be slow and less accurate.

For this reason, it is desirable to use the largest practicable aperture for skywave HF DF antenna systems. The advantages of large antenna aperture are:

1 The effect of noise and interference can be reduced (i.e., the signal-to-noise ratio available at the antenna output for a given field strength can be increased) if the aperture of the array is used to form beams. Such arrays are able to discriminate against noise and cochannel interference arriving from directions other than that of the emitter.

- 2 The effect of sky-wave error is reduced. Sky-wave error occurs when more than one sky-wave mode is present and results in a standing-wave pattern which changes shape slowly with time (in terms of seconds or minutes). This is often referred to as wave interference. ¹⁰ See Fig. 39-9.
- 3 As a result of improved signal-to-noise ratio and reduction of sky-wave error, the integration time required for a given measurement accuracy is reduced.

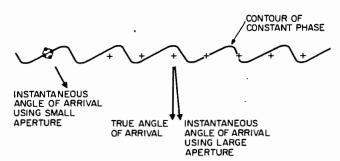


FIG. 39-9 Instantaneous angle-of-arrival errors of small and large aperture under wave-interference conditions. • = sampling ports of a small-aperture system (such as an Adcock). + = sampling ports of a large-aperture system.

4 Errors due to reradiation from obstructions in the vicinity of the DF site are reduced by the directivity of formed beams in the same way that the effect of external noise is reduced. This is true even if beams are not formed since errors contributed by scattered signals at individual elements of the array tend to be random and tend to cancel. Thus, large well-filled apertures are less sensitive to reradiation than are small or sparsely filled apertures.

The use of a large-antenna aperture therefore increases speed, accuracy, and resolution¹¹ (the ability of the system to distinguish between emitters that are in relatively close proximity).

Physical Limitations

Available Antenna Space The size of the antenna array of a DF system will be determined by its application (whether fixed or movable), by the frequency band of the emitters, and by the required accuracy and speed of measurement. The largest antenna arrays are required in the HF and upper-MF bands where sky-wave signals are received and variations of phase and amplitude of the arriving wavefront are at a maximum (see Fig. 39-9). In the LF and lower-MF bands, surface-wave signals which have stable phase and amplitude characteristics are received, so that relatively small-aperture antenna arrays provide adequate speed and accuracy. In the VHF and UHF bands, antennas having a large electrical aperture require relatively little physical space.

Thus, antenna arrays may be small when high accuracy and high speed are not primary operating requirements and when sky-wave signals are not likely to be received.

System Mobility If a DF system is to be fully mobile (meaning that the whole operational system including the antennas is vehicle-mounted), the size of the antenna system will be limited by the size of the vehicle. This restriction is most demanding for land-mobile systems, less so for ships and aircraft. The restriction is acceptable in the LF and MF bands, wherein electrically small antennas perform satisfactorily against predominant groundwave signals, and in the VHF and UHF bands because a reasonable antenna aperture can often be obtained. In the HF band, however, wherein sky waves predominate, land-mobile systems will have relatively low accuracy, low speed, and low resolution. HFDF systems for ships and aircraft, however, can be constructed so that the entire vehicular structure becomes the multiport DF antenna-receiving array. The aperture of the array is comparable to the overall dimensions of the vehicle and is often large enough to provide good HFDF performance against sky-wave signals.

If the DF system is to be transportable, as opposed to fully mobile, the restrictions on antenna-system size are far less severe. If the land area available at each DF location is sufficient, it is possible to form a large antenna array by spacing out a number of small loop or whip antennas (see Fig. 39-20). The accuracy, speed, and resolution of such a system will be greater than is possible with a fully mobile system. However, transportable antenna elements will be electrically small and consequently less sensitive than electrically large elements, so that low-level signals may not be detectable. This may not be a problem, considering that transportable systems can often be located closer to their targets than can fixed-site systems.

Size, Weight, and Complexity of Direction-Finding Equipment The advent of solid-state electronics and powerful microcomputers permits the design of sophisticated measuring, processing, and output-display equipment that is light and portable. Thus, the size and weight of such equipment is seldom a limiting system-design consideration. It is customary to use modular design so that units can be added to the basic DF system to satisfy more complex operational requirements such as networking, signal acquisition, signal monitoring, and signal processing.

39-4 DIRECTION-FINDING-SYSTEM DESIGN

Types of Direction-Finding Systems

DF systems can be grouped into two broad classifications in accordance with the way in which their antenna systems obtain information from the arriving signals of interest and in which this information is subsequently processed. Scalar DF systems obtain and use only scalar numbers about the signal of interest. Vector or phasor systems obtain vector numbers about these signals. Scalar systems work with amplitude, phase, or time, while vector systems work with both amplitude and phase.

Scalar Systems The simplest scalar system is the rotary loop illustrated in Fig. 39-3, which depends on the figure-of-eight symmetry of its vertically polarized amplitude response. Most scalar systems depend on some form of symmetry. Examples are the Adcock, Watson-Watt, dual-mode, and short-baseline time difference of arrival systems (see Sec. 39-5) and any circularly disposed system using a rotating goniometer (see Fig. 39-12).

Scalar systems employing phase response are typified by interferometer, Doppler,

and dual-mode (Butler matrix) methods. These systems employ multiport antennas that provide phase differences. Short-baseline time difference of arrival (TDOA) systems are also scalar, employing variable time delays (see Sec. 39-5). Scalar systems are capable of measuring either azimuth or elevation angles of arrival, or both. However, scalar systems of reasonable size and complexity are not well suited for the resolution of the individual angles of arrival of multimode signals (such as signals received in the fading zone).

Vector or Phasor Systems Vector systems have the ability to obtain and use vector or phasor information from the arriving signals of interest. That is, they make use of both amplitude and phase. Vector systems require the use of multiport antennas and at least two independent receiving channels. Wavefront-analysis and multisignal analysis systems, described in the following paragraphs, are a class of vector systems especially intended for the resolution of multicomponent wave fields. 13,14,15

Wavefront-Analysis Direction-Finding Systems Wavefront-analysis (WFA) systems employ multiport antenna arrays and a suitable receiver-processor-output system so that the defining parameters of the incident wave or waves can be determined. That is, a single incident wave (or a single arriving ray; either wave or ray theory may be assumed) is defined by four parameters: arriving azimuth and elevation angles and relative amplitude and phase (i.e., polarization) of the electric vector. If Similarly, a two-component wave (i.e., of two modes) is defined by 10 parameters. Thus, a WFA system must have a sufficient number of antenna ports and sufficient measuring and processing capability so that the desired number of unknown parameters can be resolved.

In practical systems, the received signals are usually processed in digital form, fully preserving relative amplitude and phase, so that the unknown wave parameters can be extracted from the set of antenna-port responses. Given the contemporary state of microcomputer capacity, two-wave (or two-ray) fields can be resolved provided sufficient antenna aperture is employed.

WFA systems require that the phase and amplitude response to signals of any arriving angle and any polarization be known for every antenna port. Such responses can be determined with considerable precision for any arbitrary antenna element or array of elements.¹² Thus, WFA systems have the important advantage that they may employ virtually any arbitrary array of antenna elements provided only that:

- 1 The aperture of the array is consistent with the desired speed and accuracy of the system.
- 2 The number of elements is large enough so that the unknown wave parameters can be determined.
- 3 The antenna angular patterns, polarization responses, and sensitivity are consistent with the desired application.

Consequently WFA systems can employ antenna arrays of virtually any shape or form, symmetrical or not, including circular or randomly placed land-based arrays or arrays mounted on irregular vehicles (such as ships or aircraft).

Multisignal-Analysis Direction-Finding Systems Multisignal analysis (MSA) DF systems are similar to WFA systems except that they are particularly designed to resolve

the simultaneous arrival at the antenna array of multiple wavefronts. ^{16a,16b} The arriving signals may be either highly correlated (a multimode signal from one transmitter) or completely uncorrelated (cochannel interference). MSA systems can employ any antenna array suitable for a WFA system.

Receivers

Receivers comprise the measuring equipment of a DF system. They are used as RF voltmeters to measure antenna responses and to provide responses to the DF processor. In systems in which the azimuth angle is determined by observation of a null or a beam maximum, a single receiver can be used, since the processor will require only information concerning the amplitude of the response pattern of the antenna system. However, in any system in which measurement is based on an amplitude and/or phase comparison, a number of alternative receiver arrangements are possible (see Fig. 39-10):

- 1 Single-channel receiver with switch to compare the outputs of two or more antenna ports sequentially (Fig. 39-10a)
- 2 Dual-channel receiver without switch to compare the outputs of two antenna ports simultaneously (Fig. 39-10b)
- 3 Dual-channel receiver with switch to compare the outputs of three or more antenna ports sequentially and allow any two to be compared simultaneously (Fig. 39-10c)
- 4 N-channel receiver without switch to compare the outputs of N antenna ports simultaneously (Fig. 39-10d). Note: A switch may be used in this arrangement (see next section).

Dual-channel and multichannel receivers are usually arranged to operate from a common frequency-synthesizer source, so that the phases of the output signals will be in the same relationship as the phases of the incoming signals.

All receiving channels must, in some way, be correlated in their gain and phase responses. They may be gain/phase matched, or they must have short-term gain/phase stability over their measurement bandwidth and then be normalized for each measurement. Alternatively, good quality standard communications receivers with short-term gain/phase stability and a common local oscillator may be used followed by analog-to-digital converters connected to digital signal processors. In this arrangement, provision is made to inject a calibrating signal into the antenna array prior to each series of measurements so that a set of normalizing data can be obtained for every receiving channel. Lee Measurements of the signal of interest are combined with these data in the DF processor.

DF receivers are usually provided with selectable-measurement bandwidths. Narrowing the bandwidth can reduce the effect of adjacent channel interference but usually requires an increase in measurement time. An alternative is to set receiver (analog) bandwidth relatively wide (say, wide enough for normal communications signals) and then employ digital filtering to achieve the required DF signal resolution against interference. This method requires no increase in measurement time assuming that the resolution of the digital filter is narrow enough to resolve the interference.

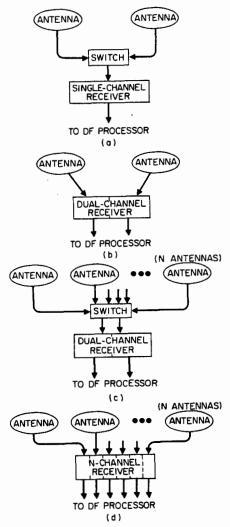


FIG. 39-10 Alternative receiver arrangements.

Direction-Finding Processor

The function of the processor is to calculate the required DF and emitter location on the basis of the signal voltages at the output of the receiver system. The complexity of the processor varies with the nature of the calculations required to deduce emitter location. At one extreme, the processor may be as simple as an angle scale on a rotating loop. At the other extreme, a digital processor such as in a multiport WFA system may be required.¹⁷

WFA and MSA DF systems usually employ powerful central microprocessors and/ or distributed digital signal processors (DSP). The ultimate objective is to calculate the required DF angles and emitter locations on the basis of the responses of the receiving channels. Much of the use of DSP is to perform fast Fourier transforms (FFT) and/or other transforms from time to frequency and from phase/amplitude to geographic space.

These processor-based systems are highly flexible and may vary from simple to complex. System speed, amount of memory, modularity of software, type and complexity of user interface, and interconnection with distant, cooperative DF-SSL locations can be accommodated to system requirements. Optional capabilities such as signal acquisition, signal monitoring, and the use of ionospheric sounders for SSL processing can be provided.

Figures 39-10c and d both show antenna-receiver arrangements suitable for use with a WFA or MSA system. The output ports of the antenna elements are connected to the switch for routing to the receivers (Fig. 39-10c) or are connected directly to the receivers (Fig. 39-10d). Alternatively, the antenna-element responses may be combined into groups to form directive beams.

The N-channel arrangement of Fig. 39-10d is very fast because no receiver/antenna switching is required during the time the signal is being measured. This permits the system to gather data quickly enough to yield the highest-quality DF results because the ionospheric wavestate of the HF signal is not likely to change significantly during the measurement process. Fast response also makes the system suitable for rapidly sorting signals on the basis of modulation type if suitable DSP equipment is provided.

The system shown in Fig. 39-10d may actually include a switch so that just prior to a DF measurement sequence all the receivers can be connected to a common antenna for the purpose of dynamic calibration. This step would occur only at each change of frequency or receiver gain.

The wavefront-analysis technique¹⁸ is essentially the inverse of the antenna-portresponse computation as previously described.¹² That is, the WFA system, under the control of its processor, measures the responses of the antenna ports to the incoming wave field. Since the current distribution on the antenna array and the resulting antenna-port responses are uniquely determined by the incoming wave field and since the antenna-port responses have previously been computed with precision, the processor is able to solve for the wave-field parameters by using a method of correlation. The computed wave-field parameters consist of the arrival angles (azimuth and elevation) and the instantaneous sense of polarization of up to two waves (or rays).

Each separate DF computation results in a complex correlation coefficient which depends on the match between the measured and stored port responses and which indicates the quality of that particular computation. The computed correlation coefficient provides a means for eliminating results seriously contaminated with noise or interference.

The DF processor may also be provided with software so that the measured elevation angle, in conjunction with either stored or measured ionospheric data, can be used to compute a distance to the target emitter, resulting in SSL capability. The software and hardware associated with real-time ionospheric-data systems can become complex and extensive if the ultimate in SSL accuracy is desired.

The WFA technique is fully automatic (human intervention is not required), and it can be very fast. Depending on the configuration of the particular WFA system, individual measurements (or *cuts*) can be made in as little as 10 ms.

MSA systems require the same number N of receiver and signal processing channels

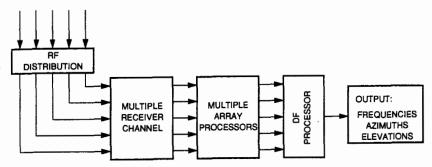


FIG. 39-11 Multisignal analysis (MSA) direction-finding equipment.

as outputs provided by the antenna array (see Fig. 39-11). The array itself may be of almost any arbitrary geometry but should employ antenna elements suitable for reception of the signals of interest. The antenna port responses must be either known quantitatively or all identical. The receiver gain and phase responses must be correlated, just as for use with WFA systems. Using the outputs of all receiving channels, the MSA system processor accumulates an $N \times N$ covariance matrix and solves for the eigenvalues and eigenvectors. The number of received signals is given by the rank of the matrix, and the directions of arrival are indicated by the eigenvectors.

Given the same antenna array, the DF accuracy, sensitivity, and speed of an MSA DF system can be identical to that of a WFA DF system provided only that the increased signal and central processing load can be handled in the same elapsed time. The advantage of the MSA method over the WFA method is its rapid ability to resolve cochannel interference and multimode signals. An MSA N-channel system is especially useful for rapidly sorting signals on the basis of both modulation type and geographic location of the emitter.

The essential conditions for fulfilling the rapid resolution potential of the MSA method are

- Precisely known amplitude and phase responses over all half space for all antenna element ports
- Wide, well-filled antenna aperture, ≥ 1λ at the lowest operating frequency of operation
- Precisely known and controlled near-field electromagnetic environment of the antenna array

System Control/Output Arrangements

Processor-based DF systems can be designed easily to permit an operator to exert system control as well as to extract system responses. These two functions are sometimes collectively referred to as the *man-machine interface* (MMI). In its simplest form, the MMI might consist of an on-off switch for system control and an azimuth scale for the orientation of a rotating-loop antenna.

More generally, the MMI will include means to direct the system with respect to frequencies of interest, times of day, kinds of signals, forms of processing, and formats of output. Simple scalar DF systems usually employ some form of analog display such as a

cathode-ray tube (CRT) or graphic plotter. Some scalar systems are equipped with automatic bearing processors so that numerical values of bearing angle can be used remotely.

Processor-based DF and SSL systems can be provided with a variety of local and remote outputs. Visual displays in graphic and tabular form can be furnished, as can hard copies of both. Interactive displays can also be provided so that operators can edit and enhance the accuracy and usefulness of results. Data can also be easily transmitted to remote locations for further processing or for combination with data from other DF sites.

39-5 DIRECTION-FINDING ANTENNA ELEMENTS AND ARRAYS

In general, a DF antenna system is an array of individual antenna elements arranged to provide the responses required by the particular system. The antenna elements and arrays are of standard types that are used in other radio-communications applications, and their basic theory of operation is explained elsewhere in this handbook (principally in Chaps. 2 through 6). In this section, therefore, only those properties of the elements and arrays that are of importance in DF applications are discussed in detail.

Antenna Elements

An antenna element for a DF system is essentially a single-port (two-terminal) arrangement of conductors for the interception and collection of radio-frequency energy. A wide variety of element types are used in DF systems. These include monopoles, dipoles, loops, log-periodic antennas, and current sensors. The choice of a particular type of element is dictated by the DF application and the frequency band in which the target emitters operate. Those scalar HF DF systems which measure only the amplitude of the signal incident on the antenna must use antenna elements that are sensitive only to vertically polarized signals (monopoles, vertically polarized dipoles, and vertically polarized log-periodic antennas). Otherwise, polarization error (or night effect) will occur in the presence of sky waves.

Monopoles Monopoles are vertically polarized elements operated over a ground plane. Since they economize in height (they are shorter than a vertical dipole resonating at the same frequency), they are suitable for applications in the LF, MF, and HF bands.

DF systems using arrays of monopole elements are sensitive only to the vertically polarized component of the signal and are thus suitable for scalar (amplitude-only) systems. However, all monopoles have a pattern null at zenith and are not well suited for short-range, high-angle signals above about 70° elevation. Sleeve monopoles (sometimes referred to as elevated-feed monopoles) provide a high sensitivity to low-elevation-angle signals over a wide bandwidth because there is no reverse loop of current when the monopole length exceeds a half wavelength.

Dipoles Dipoles are used at frequencies in the HF, VHF, and UHF bands at which their length can be accommodated. Vertically polarized dipoles have most of the same advantages and disadvantages of vertical monopoles. Horizontally polarized dipoles can be arranged to be sensitive to signals arriving at high elevation angles. Horizontal

dipoles typically have low sensitivity to signals arriving at low elevation angles so that they minimize the effect of local human-made interference, which is usually propagated by surface wave. Horizontal dipoles are sensitive to both the vertical and horizontal components of polarization of sky-wave signals, depending on the directions of their arrival.

Loops Broadband (untuned) single-turn loop antennas are particularly suitable for wideband DF applications in the HF band. Loop sizes from about 2 m² to 4 m² represent a good compromise between sensitivity (a larger size is better) and freedom from reradiation when used in arrays and ease of handling when used in transportable systems (a smaller size is better).

Loops are responsive to both vertical and horizontal polarization. Whereas this is a serious disadvantage with amplitude-only systems when sky waves are present, it is a distinct advantage when used with WFA systems. A pair of crossed loops, suitably phased, is responsive to radiation of at least one sense of polarization from virtually all angles of arrival in half space. That is, such loops are sensitive to ground waves and to sky waves from all but very low elevation angles.

Loops, being electrically small and broadband, have a high noise factor (a substantial amount of internal noise is generated by conductor, mismatch, and earth losses²⁰). Thus, when the external noise level is low (at the higher frequencies in the HF band and at quiet locations), a DF system with loop antennas may become internally noise-limited. With weak signals longer integration time may be required to provide acceptable measurement accuracy.

Current Sensors In shipboard and airborne DF-SSL systems, the incoming wave induces RF currents over the entire hull or aircraft body. If the vehicle has dimensions of the order of a wavelength or more, the vehicle itself becomes part of the antenna system, and its effect cannot be ignored. However, for any incoming wave (or set of waves) the current distribution on the vehicle will be unique and will therefore define the incoming wave. Thus, the whole hull and superstructure of the ship or the aircraft body can be used as the DF antenna if the current distribution is sampled by a WFA or MSA DF system. A convenient form of current sensor can be constructed from a small ferrite core with a coil winding mounted on a backing plate that can be secured to the hull. An essential step in designing such a system is to determine the response of every sensor, wherever located on the vehicle, to both amplitude and phase of waves arriving from any direction.

Arrays of Direction-Finding Antenna Elements

Factors to be considered in the selection of antenna arrays are:

- Coverage (the range and azimuth sector over which the target emitters are located). This will determine the form of the array.
- Expected propagation modes of the arriving signals (surface-wave, direct-wave, sky-wave, or multimode). These will determine the required elevation response of the antenna array and the type of antenna elements to be used.
- Combination of measurement speed and measurement accuracy. These will determine the required aperture of the antenna array.

Physical requirements of the DF system (fixed or movable and the related limitation on space available for the array). These will affect the physical form of the elements and the size of the array.

DF antenna arrays can be conveniently divided into three categories:

- 1 Antenna arrays with a single or multiport output that are rotated either mechanically or electrically so that azimuth can be determined by a scalar system based on knowledge of the amplitude of the directional responses
- 2 Antenna arrays with a multiport output in which the azimuth and elevation angle are determined by measuring the phase difference of the signals at the output ports
- 3 Antenna arrays with a multiport output from which azimuth angles, elevation angles, and polarizations of the components of a multimode signal can be determined by a vector system

Single-Port or Multiport Antennas with Rotation of a Directional Pattern

This type of antenna system requires a scalar system to measure the amplitude of the signal. The antenna radiation pattern will be symmetrical about some axis, forming in general either a directive beam or a sharp null. In the DF operation the antenna array may be rotated mechanically (if it is sufficiently small), in which case it will have a single port. Alternatively, the antenna array may be rotated electrically by means of a goniometer (an electromechanical device that takes a weighted sum of the outputs of a number of fixed antenna elements and produces a response pattern that can be rotated). This type of antenna will inevitably have a multiport output, and the azimuth of the emitter will be determined by the maximum response (if the beam maximum is used) or the minimum response (if a null is used). It is often convenient to use the beam maximum when searching for the emitter and the null to establish the precise azimuth.

An example of a DF system using an antenna array with a symmetrical beam of known response is the Adcock, which is shown in two-port fixed form in Fig. 39-12. A basic form of the Adcock antenna array^{21,22} comprises four vertical monopoles connected so that a figure-of-eight response pattern is produced. The pattern is rotated by a goniometer until the null is directed toward the emitter. The Adcock array differs from the rotating loop of Fig. 39-3 in that there are no unshielded horizontal conductors, so that polarization error due to the horizontally polarized component of sky waves is eliminated. Since there are two nulls in the figure-of-eight response pattern, there will be an ambiguity of 180° in the determination of azimuth. It is necessary to either switch the monopoles to provide a cardioid radiation pattern or to utilize a separate sense antenna to determine the correct azimuth. Thus, the measurement is made in two stages, the first to determine two precise azimuths by means of a null output and the second to determine which of these azimuths is the correct one.

The Adcock antenna array is typical of a narrow-aperture DF system and suffers from the disadvantages of low speed and/or accuracy, as discussed in Sec. 39-3. There are many variations of the basic Adcock design, most of which employ more than four elements with the objective of increasing aperture without increasing spacing error.²³ But all these must be considered narrow-aperture systems.

An alternative to the conventional Adcock system is the Adcock Watson-Watt

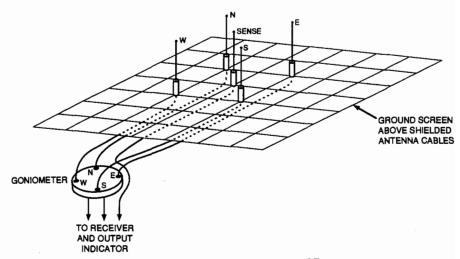


FIG. 39-12 Two-port, four-element narrow-aperture Adcock DF antenna.

arrangement, ²⁴ one form of which is illustrated in Fig. 39-13. In this arrangement, the two antenna ports are connected (by means of two receivers) to the X and Y plates of a CRT so that the display is a line indicating the azimuth of the emitter on a surrounding circular scale calibrated in degrees. The advantage of this arrangement over the Adcock with a goniometer is that an instantaneous reading of azimuth rather than the intermittent reading provided by the goniometer is obtained. The Watson-Watt display is subject to jitter and variation caused by modulation, fading, and noise so that considerable integration is required for accurate measurement.

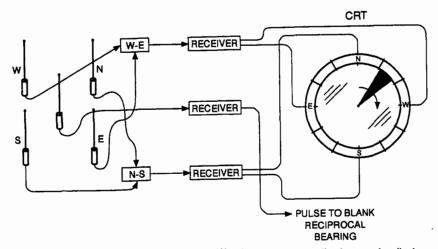


FIG. 39-13 Adcock antenna with a Watson-Watt instantaneous cathode-ray-tube display.

Some DF systems with a rotating directional pattern are capable of high speed and high sensitivity. These are wide-aperture multiport antennas of many elements disposed in a circle. Rotation of the response pattern is obtained by a rotating capacity-coupled goniometer. The goniometer usually combines responses from adjacent antenna elements so as to form highly directive sum-and-difference beams. An example of a wide-aperture DF system using a circular array of elements, together with goniometer pattern rotation, is the Wullenweber,²⁵ which is illustrated in Fig. 39-14. As in the case of the Adcock, the Wullenweber system with a goniometer measures only the amplitude (and hence only the azimuth angle) of the signal. To minimize polarization error the elements are monopoles.

The monopoles are arranged symmetrically around a cylindrical screen, and each is connected to a stator segment of the goniometer. The rotor segments span about 100° of arc and are connected to the switch by delay lines D_1 , D_2 , and D_3 , whose lengths are equal to the free-space delays of the signal, as shown in Fig. 39-14. The signals from the antenna elements in operation at any moment combine in phase at the receiver and produce a sharp beam, since the arrangement functions as a broadside array. As shown in Fig. 39-14, the delay lines can be optionally split into two groups which are connected in antiphase, thus producing a rotating null as opposed to a rotating beam. Either the sum or the difference output can be connected to the receiver input. The output of the receiver is connected to a CRT display with a synchronized rotating time base so that the response pattern of the antenna appears as a polar display centered on the direction of the emitter. When searching for an emitter, the sum mode is normally used, but when the emitter has been identified, the difference mode is used so that the sharp null in the response pattern can display azimuth angle with maximum accuracy.

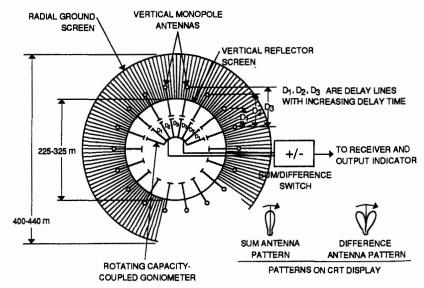


FIG. 39-14 Wullenweber wide-aperture antenna.

Multiport Antennas Using Phase Difference Measurements of phase differences between the ports of a multielement antenna enable both azimuth and elevation angle of the arriving signal to be determined. One system of this type uses the Doppler technique.26 In principle, an antenna element could be moved in a circular path so that the instantaneous frequency of the received signal would be modified. In practice, it is usually inconvenient to rotate an antenna element physically so the quasi-Doppler antenna arrangement shown in Fig. 39-15a is used instead. A rotating commutator is used to couple a receiver in rapid sequence to the elements of the array, thereby introducing a frequency shift on the received signal which is extracted by a frequency discriminator. As illustrated in Fig. 39-15b, the frequency shift is proportional to $\sin (\theta)$ $-\theta_0$) cos ϕ_0 , where θ is the angular position of the rotor, θ_0 is the azimuth angle of the received signal, and ϕ_0 is the elevation angle of the received signal. By using this expression, the azimuth angle is given by the angular position of the rotor at which zero instantaneous frequency shift occurs. Ambiguity can be removed by taking account of the angles at which maximum positive and negative frequency shifts occur. Also by using this expression, the peak-to-peak amplitude of the instantaneous fre-

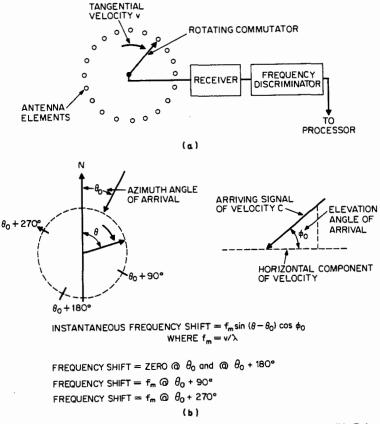


FIG. 39-15 Quasi-Doppler DF system. (a) General arrangement. (b) Relationship between frequency shift and angles of arrival.

quency shift is proportional to the cosine of the elevation angle so that the latter can be determined.

In practice, it is found that the quasi-Doppler arrangement will give accurate measurements of azimuth angle with short integration times. However, accurate measurement of elevation angle with multimode HF signals requires that one of the modes be dominant. The required integration time will depend on the relative levels of the minor modes. Furthermore, azimuth-angle accuracy drops off at high elevation angles as the amplitude of the instantaneous frequency shift approaches zero.

Another DF system making use of phase differences between the signals at the ports of a multiport antenna is the interferometer, 27 one form of which is shown in Fig. 39-16. For the purpose of explanation, only five identical antenna elements are shown, but for use against HF sky-waves, seven or nine elements are preferable. The elements can be loops, crossed loops, or monopoles. Since the distance between elements A and B is large in terms of a wavelength, the phase difference at their output ports will be large and will be very sensitive to angle of arrival relative to baseline AB. But just because AB is greater than $\lambda/2$, different arrival angles will produce the same phase difference (see Fig. 39-16). This ambiguity can be resolved by the less accurate measurement of phase difference between elements A and E, provided their spacing is less than $\lambda/2$ at the highest frequency of operation. The same principles apply to the line of elements D, E, C.

The loci of the angles of arrival with respect to the two baselines will be cones in half space, with the baselines as their axes. The line of intersection of the half cones about the two baselines will be the direction of arrival of the signal. The processor will compute the line of intersection, which will indicate both azimuth and elevation angles of arrival.

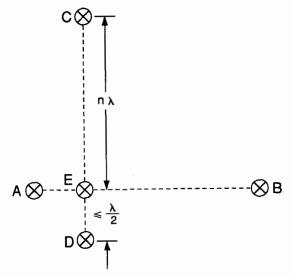


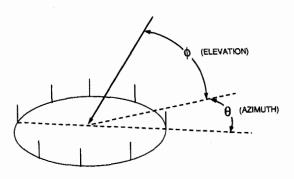
FIG. 39-16 Interferometer DF system. Example: If n=3, arrival angles of 43°, 66.5°, and 86° relative to line AB will all result in a phase difference of 70° between A and B. The phase difference between A and E will resolve this ambiguity.

Dual-mode, Butler-matrix, 27a,27b DF systems employ an N-port circular antenna (Fig. 39-17). A dual-mode beamformer (the Butler matrix) is also used. It has outputs proportional to $e^{aj\theta}$ and $e^{bj\theta}$, where a and b are positive or negative integers. When used at HF, a and b are best selected as either -1 and +1, respectively, or as +1 and +2, respectively. The -1, +1 pair provides the highest system sensitivity, especially at smaller apertures. However, it results in a 180° azimuth ambiguity which must be resolved by some other means such as a sense antenna. The +1, +2 pair has no azimuth ambiguity but is less sensitive, especially at smaller apertures.

The principal advantage of the dual-mode technique is that the calculations required to solve for angles of arrival are simple and arithmetical so that processing time can be short. Azimuth is proportional to the phase difference of the two modes, whereas elevation is derived from the amplitude ratio of them. The highest frequency of operation sets constraints on the maximum array diameter and the minimum number of elements.

Despite the aperture constraint, azimuth accuracy is good enough for use in emitter location, but elevation-angle errors (at HF) can be quite large. The dual-mode technique is widely used at VHF and above, where ionospheric propagation is not likely to be encountered.

Short-baseline time difference of arrival (TDOA) systems (see Fig. 39-18) use fixed and variable delay lines to adjust independently the time differentials across two pairs of



n-ELEMENT, VERTICALLY POLARIZED, CIRCULAR ARRAY ANTENNA

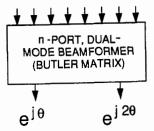


FIG. 39-17 Dual-mode antenna array and beamformer.

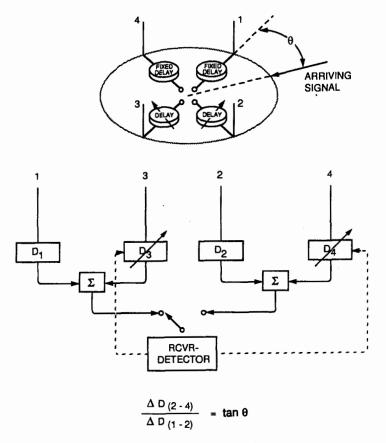
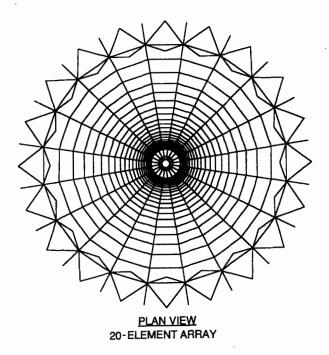


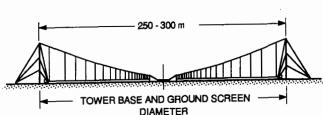
FIG. 39-18 Short-baseline time difference of arrival.

vertical antenna elements, the axes of the two pairs intersecting at 90°. The variable delays are adjusted by means of error signals from the receiver/detectors which are used to produce time coincidence at each of the summing detectors. The quotient of the two amounts of delay required to produce the two time coincidences is the tangent of the azimuth arrival angle.^{27c}

TDOA systems require only a single receiver, which can be an advantage for small, mobile systems, but they are highly susceptible to error because of cochannel interference, they report only azimuth angle of arrival, and their antenna aperture at the highest frequency of operation must be less than 0.5λ in order to prevent unresolvable ambiguities. Short-baseline TDOA systems are most useful at VHF and above, where sky-wave reception is not likely.

Scalar systems are not generally able to resolve the individual components of a multimode signal such as will occur under conditions of wave interference.





ELEVATION VIEW 2 OPPOSED ELEMENTS ONLY

FIG. 39-19 Circular array of quasi-log-periodic antennas, suitable for HF DF-SSL and monitoring, horizontally and/or vertically polarized.

Multiport Antennas for Wavefront-Analysis Direction-Finding Systems When wide-aperture systems are required, the Wullenweber type of antenna shown in Fig. 39-14 can be used, but the land area required is large. This is due to the fact that a ground screen extending well beyond the antenna elements is required for control of the near-field environment so as to minimize site errors. A more efficient wide-aperture system which achieves equal or better performance over a greater bandwidth and has a much smaller radius is shown in Fig. 39-19. This system comprises a symmetrical ring of quasi-log-periodic antennas (LPAs) arrayed so that their main lobes point inward (toward the center of the ring), thus conserving space. The array can

comprise vertically and/or horizontally polarized LPAs, as illustrated in Fig. 39-19. The ground screen need not extend beyond the outer antenna elements because each LPA faces inward toward a controlled and symmetrical environment in its near field.

Monopoles or loops are also used for medium-aperture WFA arrays suitable for fixed or movable use. Monopoles are generally more sensitive (having lower noise figures) than loops of manageable size (2 to 4 m²), except that loops tend to be more sensitive to very-high-angle sky waves. If space for the array is limited and if the number of individual elements is to be minimized, monopoles or loops or crossed loops, as illustrated in Fig. 39-20, can be used. With this type of array, beams usually are not formed. The crossed-loop responses can be combined, or they may be used individually.

39-6 SOURCES OF EMITTER-LOCATION ERROR

There are two different kinds of emitter-location error. The first, angular-measurement error, affects the accuracy of emitter location when azimuth triangulation is used and when SSL techniques are used. The second, SSL distance error, affects the accuracy of emitter location only when SSL techniques are used.

Angular-measurement error is the fundamental performance parameter of all DF systems.²⁸ SSL distance error is applicable only to sky-wave propagation.

Emitter-location error can be affected by both angular-measurement error and (if used) SSL distance error. Figure 39-21 shows the hierarchy of emitter-location errors. The terms *error* and *accuracy* tend to be used interchangeably when speaking of DF-SSL systems. Strictly speaking, accuracy/error equals true minus indicated.

Angular-Measurement Error

Angular-measurement accuracy is usually taken to mean the ability of an ideal DF system to measure direction to the target emitter. In actuality, DF systems measure direction of arrival of the signal radiated by the emitter. These two directions may be sensibly identical for ground-wave and direct-wave signals, but for sky-wave signals they will generally be different, often by a significant amount because of ionospheric error.

Thus, angular-measurement error must account for (1) direction-of-arrival errors such as those contributed by antenna, equipment, site, noise, and interference and (2) ionospheric errors.

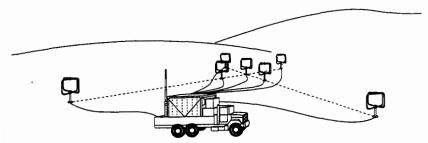


FIG. 39-20 Typical deployment of one unit of a transportable HF DF-SSL system.

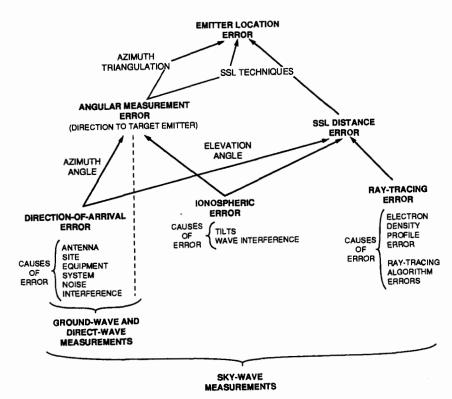


FIG. 39-21 Hierarchy of emitter-location error.

Direction-of-Arrival Error This type of error will have both systematic and random components. Systematic errors include antenna siting or construction errors, unequal cable lengths, unequal gain or phase match, antenna-pattern errors, computational or interpolation errors, and reradiation and scattering from nearby objects. For well-designed large aperture systems installed at good sites, the sum of all the errors caused by system design, construction, and siting should not exceed 0.1 to 0.3°.

Random errors caused by noise can be reduced to insignificance with sufficient integration time. Cochannel interference errors, which tend to be episodic, can be reduced by employing filtering in the domains of frequency, time, or space or some combination thereof. In view of the effect of operational choice upon the reduction of noise and interference errors, it is not practical to give a numerical allowance for them.

lonospheric Error This error results from wave interference, from large-scale ionization gradients (tilts) caused by hourly and seasonal solar variation, and from traveling ionospheric disturbances. The magnitude of ionospheric error varies with geographic location, with azimuth direction of signal propagation, and with distance to the emitter. Some of these errors are systematic, while others are random. The component of angular-measurement error due to ionospheric error can be reduced to insignificance with very long integration times (hours or days or seasons), usually much

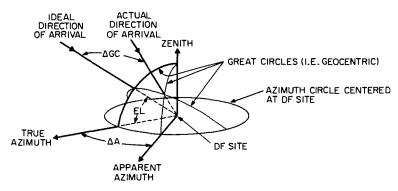
longer than is practical. Short-term statistical allowances for ionospheric errors have been suggested,^{29,30} but these are of little operational use. It is possible to apply a tilt correction either by measuring tilt in near real time or by forecasting tilt on the basis of large-scale stored ionospheric data.

Under ideal operating conditions, where random errors are small (high signal-tonoise ratio and stable, spherical, geocentric ionosphere or with groundwave reception), system (instrument) error will tend to dominate angular-measurement error. Given these conditions, system error can actually be tested. As will be clear from Fig. 39-26, welldesigned and well-constructed large-aperture systems can produce accurate results with short integration times during such conditions.

Great-Circle-Degree Concept Sky-wave DF systems present a special problem in angular terminology because they do not measure azimuth angles directly (in the conventional meaning of terrestrial geometry) except for signals arriving at 0° elevation angle. In fact, signals arriving from zenith (90° elevation angle) convey no information at all about azimuth. For these reasons, it is convenient to use the concept of *great-circle degrees* when discussing direction-of-arrival accuracy (but not when discussing azimuth angular-measurement accuracy). Figure 39-22 defines this concept.

The ionospheric-signal path from the true position of the emitter to the DF site can be idealized as two straight-line segments joined at their apparent reflection point in the ionosphere. If the ionosphere is spherical and geocentric, these two line segments would define a great-circle plane. But if the ionosphere is tilted, the two line segments from true emitter position to DF site will not define a great-circle plane, although a great-circle plane would be defined by the two line segments from apparent emitter position to DF site. The direction-of-arrival error can be defined as the difference between the actual and the ideal straight-line segments from their reflection points to the DF site. For small error angles, great-circle error angles can be converted to azimuth error angles by dividing by the cosine of the elevation angle.

The great-circle-degree concept of angular error is necessary so that azimuth



ΔGC = ERROR EXPRESSED IN GREAT-CIRCLE DEGREES

ΔA = ERROR EXPRESSED IN AZIMUTH DEGREES

 $\Delta A = \frac{\Delta GC}{\cos EL}$ (FOR SMALL-ERROR ANGLES)

FIG. 39-22 Definition of direction-of-arrival error, expressed in great-circle degrees.

error results of signals arriving from different elevation angles can be compared. For example, if the horizontal great-circle angle-of-arrival error of three signals is, say, 1.0° (great circle) and if their elevation angles happen to be 0°, 30°, and 60°, their errors expressed in azimuth degrees will be 1.0°, 1.15°, and 2.0°, respectively.

Lateral Error Lateral error is defined as the location error, perpendicular to the measured azimuth, at the true distance (see Fig. 39-23). This is the component of

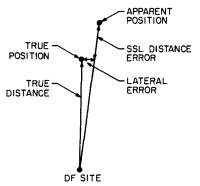


FIG. 39-23 Geometry of emitter-location error.

location error caused by angular-measurement error.

For surface waves and direct waves, in which the signal arrives at zero elevation angle, lateral error is directly proportional to angular-measurement error. If, for example, total angular-measurement error were 1°, lateral error would be as in Table 39-1.

The result of angular-measurement error as a function of true distance is very different for sky waves, in which the signal arrives at an elevation angle determined by the true distance and the height of the ionosphere. Figure 39-24 shows percent lateral and SSL distance errors as a function of true distance, assuming

1.6° (great-circle) direction-of-arrival error allowance and an ideal spherical-mirror ionosphere of 300-km height. The lateral error shown in Fig. 39-24 is presented in Table 39-2.

TABLE 39-1 Lateral Error for 1° Azimuth Angular-Measurement Error

True distance, km	Lateral error, km	Lateral error, % of true distance		
50	0.9	1.8		
100	1.8	1.8		
500	9	1.8		

SSL Distance Error

SSL distance error will be a function of elevation angle error and of the ability to trace the direction of the arriving ray backward through its zone of ionospheric refraction to the location of the emitter. Well-designated DF systems are able to measure elevation angle as accurately as they are able to measure azimuth angle except at low elevation angles, at which the projected vertical aperture of most DF antenna systems approaches zero.

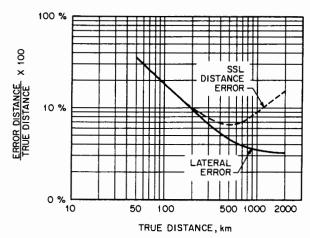


FIG. 39-24 Percent lateral and SSL distance errors as a function of true distance for sky-wave signals reflected from an ideal spherical-mirror ionosphere. Assumptions: (1) Perfect-mirror ionosphere at 300-km height. (2) 1.6° (great-circle) direction-of-arrival error.

TABLE 39-2 Lateral Error for 1.6° (Great-Circle) Direction-of-Arrival Error

True distance, km	Lateral error, km	Lateral error, % of true distance		
50	17.5	35		
100	18	18		
500	22	4.4		
1000	34	3.4		
2000	65	3.25		

The ability of a DF-SSL system to trace the direction of the arriving ray backward to the location of the emitter will depend on the accuracy of the available ionospheric data, the quality of the ray-tracing algorithm, and the degree of uncorrected ionospheric tilt. Thus elevation-angle measurement error will be greatest for HF signals arriving from the greatest distances, where a given elevation-angle error will result in the largest SSL distance error (because of the long, acute signal-path geometry).

In their simplest form, ionospheric data may consist of stored hourly median values published by a U.S. government agency.^{31,32} Such data can be used with or without tilt correction. In their most complex form ionospheric data may consist of near-real-time electron-density profiles obtained by a network of ionospheric sounders throughout the geographic area of interest and combined into a map of electron-density contours. Such a map will include tilt information.

Ray-tracing algorithms of varying complexity are available to convert elevation angles into distances. Most of these algorithms provide a one-hop distance based on a

single measured value of elevation angle. A recent example is a ray-tracing program especially designed for real-time use on a microcomputer.³³

By referring again to Fig. 39-24, it is clear that SSL distance error is equal to or greater than lateral error for reasons of geometry. That is, for distances greater than about 200 km (for a 300-km-ionosphere) distance error is more sensitive to a given arrival-angle error than is lateral error. Furthermore, Fig. 39-24 does not account for ray-tracing error, which will further degrade SSL distance error. The SSL distance error shown in Fig. 39-24 is presented in Table 39-3.

Figure 39-25 shows the data from Fig. 39-24 and Tables 39-2 and 39-3 plotted out to 1000 km.

TABLE 39-3	SSL Distance Error for 1.6°
(Great-Circle)	Direction-of-Arrival Error

True distance, km	SSL distance error, km	SSL distance error, % of true distance		
50	17.5	35		
100	18	18		
500	33.5	6.7		
1000	91	9.1		
2000	310	15.5		

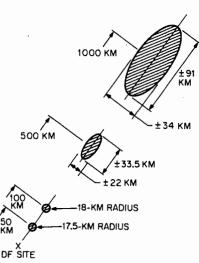


FIG. 39-25 Uncertainty of emitter location when SSL technique is used, employing data from Fig. 39-24.

Emitter-Location Error

As can be seen from Fig. 39-21, emitter-location error depends upon how emitter location is to be accomplished. Azimuth triangulation using a network of DF sites and SSL are the two techniques to be considered.

Azimuth Triangulation with a Network With azimuth triangulation, location error will depend on the lateral error of the individual lines of bearing, on the number of sites reporting, and on locations of the sites with respect both to the emitter and to each other. (See Sec. 39-3.)

If two DF sites are optimally situated with respect to the emitter, that is, if their lines of bearing intersect at 90°, then emitter-location error will approximately equal lateral error. If additional well-situated DF sites are used and if the individual lateral errors are random, then an increase in the number of DF sites will reduce emitter-location error.

Use of SSL Techniques SSL techniques are clearly of greatest utility if network operation is not possible for some reason. But if the individual DF sites of a working network do provide SSL results, overall emitter-location accuracy can be improved. This can be accomplished at the network control center where the lines of bearing and SSL results from all the sites are processed to give a best-point estimate (BPE). The most rational procedure is to require each DF-SSL site to furnish a quality rating for each line of bearing and for each SSL result. The BPE algorithm should be designed to test the available results for convergence, giving weight to the various quality ratings. This procedure, making best use of whatever results are available, will, on the average, produce the most reliable and accurate emitter-location results.

39-7 PERFORMANCE OF HF SKY-WAVE DIRECTION-FINDING SYSTEMS

Specifying and testing the performance of DF systems are more complex than might be supposed, especially for systems operating against sky waves. This section suggests how performance can be specified and what quality of results may be expected with several kinds of systems.

Factors Affecting Performance

Emitter-location accuracy of DF-SSL systems operating against sky waves is affected by at least the six kinds of parameters first given in Sec. 39-3. That is, the quality of results will be influenced to a first order by all of the following:

- 1 Antenna aperture
- 2 Instrument or system error
- 3 lonospheric behavior
- 4 Received S/N ratio
- 5 Integration time
- 6 Distance to emitter

The first two of these parameters are under the control of the system designer. For any particular system and for any frequency or band of frequencies these parameters may be regarded as fixed. Instrument or system error is the parameter most likely to be specified by system suppliers, even though only under certain special conditions will it be the dominant error affecting system performance. Furthermore, instrument or system error is difficult to measure accurately, especially with sky-wave DF-SSL systems.

The third parameter, ionospheric behavior, varies continuously. Corrections can be applied by the use of statistical ionospheric data or by the use of near-real-time ionospheric data. The last three parameters, S/N ratio, integration time, and distance, can obviously vary widely and are primarily under the control of the operator of the emitter.

It follows that a performance specification should take account of all six parameters. Furthermore, a testing program should permit separation of the different contributions to emitter-location error so the system can be rationally evaluated.

Performance Comparison of HF Sky-Wave Direction-Finding Systems

It is useful to have a method for comparing the accuracy of different DF systems or of the same system under different conditions. But in view of the six parameters having a first-order effect on DF accuracy, fully rigorous comparisons are likely to be too complex to be useful.

Figure 39-26 suggests a practical method of azimuth error comparison for different kinds of systems operating under widely different conditions. It is not meant to be rigorous, but it is useful for comparative purposes. It shows the nature of the relations between accuracy and integration time and between error and aperture.

Figure 39-26 accounts for the first two of the six parameters, namely, aperture and instrument or system error by means of the four kinds of systems, A to D. Regarding the third parameter, ionospheric behavior, Fig. 39-26 implies that there is some amount of ionospheric error which is unlikely to be eliminated within the integration times of interest, but the figure does not account for large-scale solar-induced tilts.

The fourth parameter, the received S/N ratio, is assumed to be at least high enough to yield plausible results at the shortest integration times shown for each kind of system. The slope of measurement error versus integration time reflects the fact that each doubling of integration time is equivalent to increasing the S/N ratio by 3 dB and that a 6-dB S/N improvement reduces the effect of random errors by a factor of approximately 2. The fifth parameter, time, is the independent variable. The figure is approximately independent of the sixth parameter, distance, because the dependent variable (measurement-error angle) is expressed in great-circle degrees.

Figure 39-26 is useful in visualizing the following ideas:

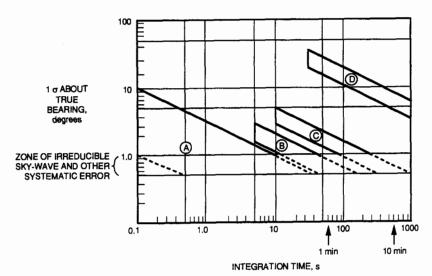


FIG. 39-26 Comparison of sky-wave DF-system performance. A = wide-aperture fully automatic WFA and MFA systems. B = medium-aperture goniometric systems such as Wullenwebers and wide-aperture interferometers. C = Adcock and Watson-Watt systems (narrow aperture). D = vehicular-mounted systems (near-zero aperture).

- 1 Large-aperture systems are faster and more accurate than small-aperture systems.
- 2 Manual systems (wherein a human operator makes the bearing estimate) probably require 5- to 10-s minimum integration to obtain any plausible result.
- 3 Fully automatic systems, combined with wide-aperture antennas, are between one and two orders of magnitude faster than manual systems.
- 4 When sky-wave and other systematic errors approach their minimum, (a) large-aperture systems will provide usable to accurate results at short integration times (say, 10 to 100 ms); (b) total measurement error may not increase as rapidly with decreasing integration time as the slope of the lines in Fig. 39-26 would suggest.

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ECM and ESM Antennas

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40-1 Introduction 40-2

40-2 Surveillance Antennas 40-2 Biconicals 40-2 Radial-Mode Horns 40-3 Ridge-Loaded Horns 40-5

40-3 Direction-Finding Antennas 40-6 Rotating Antennas 40-6 Shaped-Beam Antennas 40-7 Amplitude Comparison 40-8

40-4 Tracking Antennas 40-9 Conical Scan 40-9 Sequential-Lobing Antennas 40-10 Two-Channel Monopulse 40-13

40-5 ECM Transmit Antennas 40-14
Antenna Elements 40-14
Fixed-Beam Arrays 40-16
Arrays with Beam Control 40-17

40-6 Antenna Isolation in Jamming Systems 40-19

40-7 Advanced Array Systems 40-19 Solid-State Arrays 40-19 Multifunction Apertures 40-20

40-1 INTRODUCTION

Electronic-countermeasures (ECM) and electronic-support-measures (ESM) systems place a great variety of requirements on the antenna or antennas used, depending on the specific function being performed by the system, the characteristics of the target, and the environment within which the system is functioning. The breadth of these requirements is such that virtually any type of antenna, from a simple monopole to the most sophisticated phased array, may eventually be used in an ECM or ESM system. This chapter describes a few "typical" antenna subsystems used in ECM or ESM systems.

The functions to be performed by an antenna in an ESM system can generally be divided into two broad categories: (1) to monitor the environment for signals and (2) to determine the direction of arrival of an incoming signal (direction finding or tracking). The primary antennas on an ECM system are used to direct a significant amount of jammer power toward the threat emitter. ECM systems also use passive antennas for direction finding.

40-2 SURVEILLANCE ANTENNAS

The first and primary function of an ESM system is that of monitoring the environment for signals or, more particularly, for certain specific signals or types of signals. The knowledge that certain signals are being radiated can be of great importance to the battlefield commander or the combatant himself. A few typical examples of surveillance antennas are described in the following paragraphs.

Biconicais

One of the most useful omnidirectional antennas is the biconical horn, ^{1,2} particularly since the advent of meander-line-array³ aperture polarizers. The most popular method of feeding the biconical for broadband operation is with coaxial line. This method produces a vertically polarized antenna. Cylindrical-aperture polarizers can be used to convert the polarization to either circular or slant-45° linear polarization.

By using meander-line-array polarizers to produce circular polarization, axial ratios can typically be held to less than 3 dB. For broadband operation, a flat disk of resistance card in the biconical is needed to absorb the cross-polarized reflections off the polarizer, however small these may be. If these low-level reflections were not absorbed, they would be re-reflected by the biconical and would radiate as the undesired sense of circular polarization and rapidly degrade the axial-ratio performance. At the present state of development, meander-line-array polarizers are limited to two octaves or less, which becomes the controlling factor for a circularly polarized biconical.

Slant-45° linear polarizers can provide broader bandwidths of operation. Bandwidths of 12:1 have been achieved on biconicals by using this type of polarizer. The slant-45° linear polarizer consists of a series of cylindrical printed-circuit-board (PC-board) layers, each with a grid of linear parallel lines. The PC boards are spaced in

the radial dimension by approximately a quarter wavelength, with the innermost layer having its lines oriented orthogonally to the polarization of the antenna. On each succeeding sheet, the grid is tilted at an increased angle relative to the innermost board until the last sheet has its lines at 45° to the innermost sheet and orthogonally to the desired slant-linear-polarization orientation. Usually this is accomplished with four or five layers.

Another useful circularly polarized, omnidirectional antenna is the Lindenblad,⁴ which covers octave bandwidths with broader elevation patterns.

Radiai-Mode Horns

Radial-mode horns⁵ can provide increased gain relative to an omnidirectional antenna when the azimuthal angular sector to be monitored is less than 360°. Radial-mode horns (Fig. 40-1) consist of a wave-launching section and a radial section in which a cylindrical wave moves out and radiates from the cylindrical aperture. The azimuthal (or E-plane) pattern is relatively flat-topped with a beamwidth of 0.95 θ , independent of frequency, provided that the wave-launcher slot width w is less than 0.5 λ . Useful angles of θ have been found to vary from approximately 90° up to at least 200°. The radius R, measured from the point at which the back walls would intersect, must be greater than some minimum length (which is a function of θ) to maintain the flat-topped-pattern shape. The minimum radius R required increases rapidly as the angle θ decreases to 90°.

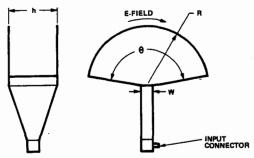


FIG. 40-1 E-plane radial-mode horn.

The elevation (or *H*-plane) pattern of this antenna varies with frequency in the normal manner of an aperture with a cosine amplitude distribution. Bandwidths of up to 2.25:1 have been achieved with this antenna.

The radial-mode horn itself generates a polarization that is perpendicular to the cylindrical axis. This linear polarization can be converted to either sense of circular polarization by using a cylindrical section of meander-line-array polarizer or to slant-45° linear polarization by the polarizer previously described. The polarization has also been converted to the orthogonal linear polarization very successfully by using essentially a double thickness of meander-line-array polarizer.

Figure 40-2 is an azimuthal (*E*-plane) pattern of an *E*-plane radial-mode horn with a meander-line polarizer taken with a linearly polarized transmit antenna rotating in polarization.

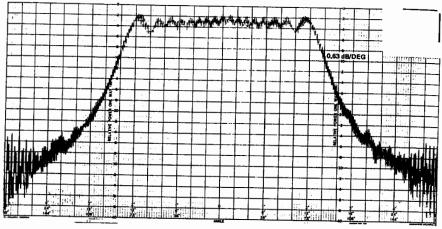


FIG. 40-2 Azimuthal pattern of an *E*-plane radial mode horn ($R = 8.9\lambda$, $\theta = 179^{\circ}$).

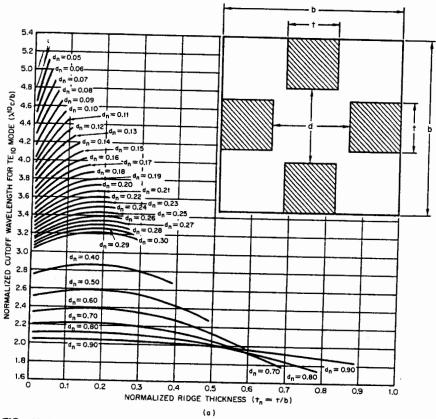


FIG. 40-3 Cutoff wavelength versus ridge thickness for various gap widths. (a) TE_{10} mode. (b) TE_{30} mode.

Ridge-Loaded Horns

Among other broadband antennas having increased gain that could be used for monitoring are the frequency-independent log-periodic dipole array and spiral antennas and ridge-loaded horns. These are used either directly or as feeds for reflectors. The frequency-independent log-periodic dipole array and spiral antennas have been discussed in Chap. 14 and will not be discussed further here.

Ridges are introduced into a pyramidal horn for the same reason that they are used in ridged waveguide, that is, to expand the frequency range of operation. Ridges on both broad walls of a rectangular waveguide (doubly ridged horns) lower the cutoff frequency of the TE₁₀ mode of the waveguide. The ridges, if properly selected, will also raise the cutoff frequency of the TE₃₀ mode slightly. (If the waveguide is straight and the input probe is centered, asymmetric modes will not be excited.) For the proper waveguide and ridge configuration, the ratio of TE₃₀ to TE₁₀ cutoff frequencies can be over 12:1 for doubly ridged horns. Curves for the design of doubly ridged horns can be found in Ref. 6.

Lenses are often employed to correct the aperture phase errors of horns operating over bandwidths of more than 5:1 to maximize their gain at the higher frequencies.

Quadruply ridged horns, 7 which provide dual orthogonal linear polarizations, can be operated over bandwidths as large as 9:1. Figure 40-3 shows the TE_{10} and TE_{30} cutoff wavelengths versus ridge thickness for various gap widths, as published in Ref. 7.

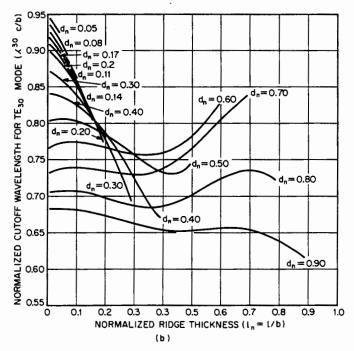


FIG. 40-3 (Continued).

40-3 DIRECTION-FINDING ANTENNAS

Direction-finding (DF; determination of the azimuth bearing to a given emitter) techniques applicable to ESM systems would include a rotating antenna sweeping a beam around in azimuth to determine the direction of highest signal intensity and amplitude- and phase-comparison techniques. If the DF system is searching for a target emitter that is relatively stable as a function of time and if sufficient time will be available for acquiring, identifying, and performing the DF function, a simple rotating-antenna beam may be adequate. On the other hand, if the emitter-signal strength varies greatly as a function of time, more sophisticated techniques, such as phase or amplitude comparison with simultaneous reception on all beams, may be required. The DF accuracy of any of the three techniques will be directly proportional to the beamwidth of the antenna in the azimuthal plane. These techniques are discussed in detail in Chap. 39.

Rotating Antennas

An example of a rotating-beam-antenna system is shown in Fig. 40-4. The antennas can be spun at up to 300 r/min or pointed for surveillance purposes. In this system a pair of conical spirals is used to cover the 0.25- to 2-GHz range. The spirals are fed through a 180° hybrid to provide both sum and difference patterns in the azimuthal plane. A coaxial switch allows selection of sum or difference patterns.

Four compound sectoral horns provide fan beams for DF or monitoring purposes over the frequency bands of 2 to 4, 4 to 8, 8 to 12, and 12 to 18 GHz. Dielectric lenses

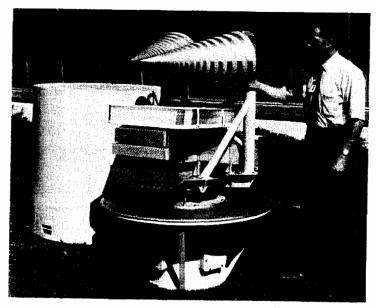


FIG. 40-4 Rotating direction-finding system.

are used in the horns for phase correction in the azimuth plane. Meander-line polarizers convert the vertical linear polarization in the horns to right-hand circular polarization in the radiated field. A horizontal absorber fence reduces the effects of the metal surfaces of the horns on the conical spiral patterns. DF accuracy of this system against emitters with high signal strength and amplitude stability varied from 5° at the low frequency to 0.4° at the high frequency of each horn.

This system used a five-channel rotary joint to bring the five RF bands off the rotating platform.

Shaped-Beam Antennas

Another form of rotating-beam antenna uses a specially shaped reflector to control the elevation pattern coverage for ESM purposes. The doubly curved reflector is used to shape the main-beam radiation pattern in the elevation plane for specific system requirements while focusing the beam in the azimuth plane for maximum directivity. For instance, for an air or surface search system, a constant-power return from the target as a function of elevation or depression angle is optimum. The amplitude pattern for such an optimization is nominally proportional to $\csc^2 \theta$. Another application of the shaped-reflector system for shipborne ESM systems is provided when the system is designed to maintain a fixed elevation-plane beamwidth across the frequency range. This type of system is often installed on unstabilized shipborne platforms. In this case the beam must be sufficiently broad to compensate for the pitch and roll of the platform and maintain a constant illumination of the potential threats.

The doubly curved reflector has no exact solution, and any solution obtained is not unique. The design methods outlined in the literature 13,14,15 are based on an iterative geometrical-optics process that tends to converge rapidly. The geometrical-optics method transforms the primary radiation pattern of the feed into the desired secondary radiation pattern in the elevation plane. Although this method of surface determination was originally developed for narrowband systems, it is useful for broadband ESM applications provided that the illuminating primary pattern is relatively constant over the frequency range of interest. Therefore, the shaped-beam technique works well with primary feeds such as log-periodics, spirals, and, to some extent, scalar electromagnetic horns, whose beamwidths are a slowly varying function over at least a waveguide bandwidth.

Measured radiation patterns of doubly curved reflectors closely approximate the desired theoretical radiation-pattern shape and hence validate the geometrical-optics design process. As one might expect, the larger the reflector in terms of wavelengths, the better the conformance to the theoretical pattern shape. However, even for small reflectors (0.6- to 0.75-m diameter) typical of some ESM applications, pattern-shaping techniques are extremely useful. Frequency ranges of 18:1 are entirely feasible by using this technique. Such an antenna (0.75-m diameter) is shown in Fig. 40-5. The antenna is linearly polarized at 45° and provides a minimum elevation beamwidth of 18° to 18 GHz. As the frequency of this antenna decreases, a crossover point is reached where the physical aperture size dominates and the elevation-plane beamwidth becomes inversely proportional to frequency. At the low end of the frequency range, the beamwidth increases to 24°. Some aperture gain is sacrificed even at the low end of the frequency range because of the phase distortion associated with shaping the radiation pattern for the high end of the frequency range.



FIG. 40-5 Shaped-beam antenna (1 to 18 GHz). (Courtesy of Condor Systems, Inc.)

Amplitude Comparison

Amplitude-comparison DF requires two or more overlapping antenna patterns whose peaks are separated by some angular extent in the azimuth angle. By measuring the relative amplitude on the two patterns and comparing the measured data with a priori data of the pattern shapes, the angle between the antenna boresight and the emitter's bearing can be determined. Narrower beamwidths provide better DF accuracy, but only over narrower azimuthal sectors. Hence, a trade-off must be made between gain and DF accuracy against sector coverage or number and volume of antennas required.

DF accuracy is reduced by the polarization sensitivity of the pattern. Because the polarization of the incident signal is normally unknown, any variation of the pattern shape as a function of polarization will introduce error in the angle determination. Pattern changes that are a function of frequency can be accommodated by storing data in the computer as a function of frequency, but polarization effects cannot be similarly accommodated unless the incoming-signal polarization is measured.

Pairs of phase- and amplitude-matched conical spirals, arrayed in a frequency-independent manner, can be used in amplitude-comparison DF systems. In a circular

array of spiral pairs, the summed outputs of each pair can be compared to obtain a DF bearing. DF is often accomplished by using a circular array of single spirals (either conical or flat cavity-backed), but the pairs provide a narrower azimuthal beamwidth and hence better accuracy. Corrugated horns are also useful in amplitude-comparison systems. A circular array of almost any type of directive antenna elements can be used for amplitude comparison; however, to obtain similar DF accuracy over a broad bandwidth, the pattern performance of the elements must be relatively independent of frequency.

40-4 TRACKING ANTENNAS

A tracking antenna is designed to provide the information required by the electronic system to change periodically the pointing of the antenna in both azimuth and elevation so that the antenna boresight is repositioned to the target emitter's location. When this is accomplished sufficiently often, the antenna will track the emitter in a smooth motion. Three main techniques are used: conical scan, sequential lobing, and monopulse. These techniques have been described in Chap. 34. Examples of how these techniques are applied in broadband systems will be described in the following paragraphs.

Conical Scan

Conical scan is achieved by mechanically moving the feed in a circle about the focal point in the focal plane of a paraboloidal reflector. Moving the phase center of the feed antenna off the focal axis causes the secondary beam to squint off the focal axis in the opposite direction; moving the feed in a circle then causes the peak of the secondary beam to move on a conical surface. If the feed maintains a fixed plane of polarization as the feed rotates, the feed is said to *nutate* as compared with a *rotating* feed, in which the plane of the polarization rotates with the feed. For ESM applications, for which linear polarization is required, the antenna must have a nutating feed because rotating the feed would modulate the signal at twice the scan rate, destroying the tracking information.

A conical-scan tracking antenna,¹⁷ which operates over the 1- to 11-GHz band, is shown in Fig. 40-6a. The feed is a linearly polarized, ridge-loaded horn. A dielectric lens is used in the aperture to correct phase error. The decrease in secondary beamwidth with frequency is limited by the fact that above approximately 4 GHz the feed horn illuminates only a portion of the reflector. As the frequency increases above 4 GHz, the area illuminated is reduced sufficiently as a function of frequency to maintain essentially a constant secondary beamwidth (Fig. 40-6b). This allows the feed to be nutated at a constant radius about the focal point, with the crossover level being maintained within 4 dB of the beam peaks. Gain and boresight shift as measured on this antenna are also shown in Fig. 40-6b. While the constant-beamwidth technique results in a system whose gain does not increase with frequency, it does result in a system with a constant acquisition angle, which minimizes acquisition time.

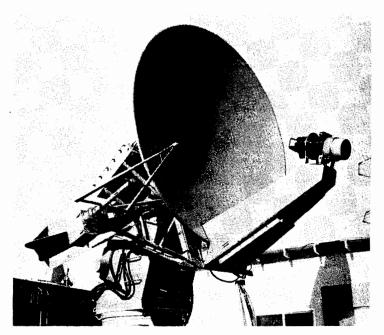


FIG. 40-6a 1- to 11-GHz conical-scan tracking antenna.

Sequential-Lobing Antennas

Sequential lobing is very similar to conical scan, the difference being that whereas in conical scan the beam is moved continuously in a conical fashion, in sequential lobing the beam is switched between four positions. The beam is stepped from beam right to beam up, to beam left, to beam down. Signal strength is sampled at each position and compared with the opposite position to obtain tracking information.

Figure 40-7a shows a four-horn sequential-lobing tracking antenna. The horns are doubly ridged and hence provide linear polarization which can be rotated by remote control. Dielectric lenses correct any phase error in the aperture.

The beam-forming network used with this antenna system is shown in Fig. 40-7b. In the normal tracking mode, all four horns are combined with the proper phase to form the beam in one of the desired beam positions, the phase being introduced by the comparator quadrature hybrids. The comparator hybrids inherently provide a crossover level of approximately 3 dB on boresight independently of frequency. Diode switches select the proper path for each horn to achieve or change the beam position. Because the horns are separated by a fixed distance, grating lobes which can provide a multiple-tracking axis develop at the higher frequencies. To ensure that the true boresight is achieved, an acquisition mode is provided. Each horn is physically pointed 5° off the boresight direction. By combining only the horns on the right side, a beam squinted to the right is obtained. The width of the beam is the same as the individual horn beamwidth and hence is sufficiently wide to cover all grating lobes. Coaxial switches bypass the comparator hybrids for this mode. This mode provides a sufficient

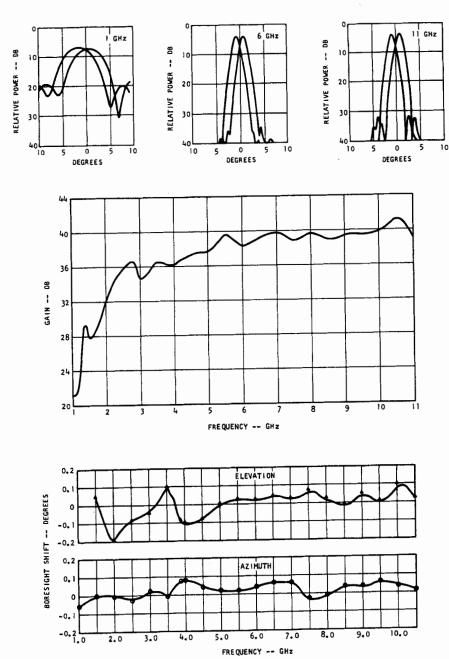


FIG. 40-6b Patterns, gains, and boresight shifts of a 1- to 11-GHz conical-scan tracking antenna.

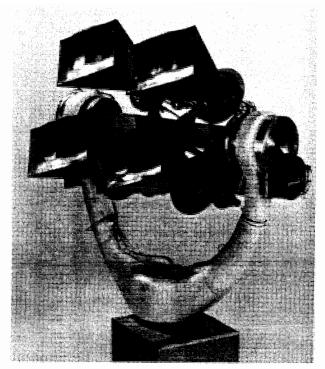


FIG. 40-7a Four-horn sequential-lobing tracking antenna (1 to 5 GHz).

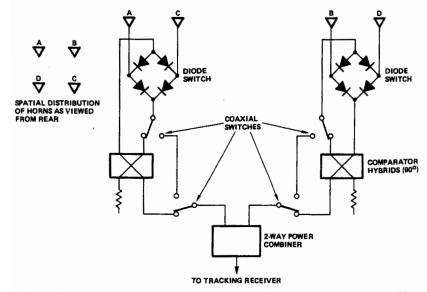


FIG. 40-7b Beam-forming network of the four-horn sequential-lobing tracking antenna (1 to 5 GHz).

error gradient to ensure that the system will lock on at the true boresight when it is switched to the normal tracking mode for better tracking accuracy.

Two-Channel Monopulse

Figure 40-8 shows a two-channel monopulse feed consisting of eight log-periodic monopole arrays on an octagonal cone. The outputs from the eight arrays are combined in a beam-forming network to form circularly polarized sum and difference patterns. For two-channel monopulse, both patterns are figures of revolution, with the difference pattern having a point null. The phase of the sum pattern changes from 0 to 360° around the boresight axis; for the difference pattern, the phase changes from 0 to 720°. Thus, the phase difference between the patterns defines the angle ϕ about the boresight axis (relative to an established reference plane) from which the target signal is arriving (Fig. 40-9), while the sum-to-difference-amplitude ratio defines the angle θ off the axis.

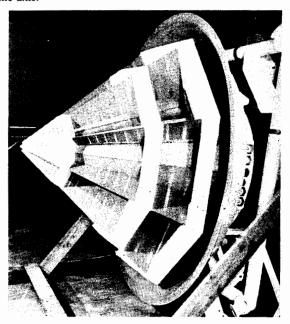


FIG. 40-8 Two-channel monopulse feed.

Two-channel monopulse systems lend themselves to broadband (36:1 bandwidth) tracking systems because beam-forming-network errors result in boresight shift rather than null fill-in, as is the case for three-channel systems. Null fill-in degrades tracking accuracy owing to degradation of error slope, while boresight shift in two-channel systems produces bias errors which in principle can be eliminated by calibration techniques.

Two-channel monopulse patterns are also inherent in multimode spiral antennas¹⁸ in addition to the multiple log-periodic monopole array configuration. However, since spiral patterns turn about the boresight axis as a function of frequency, the reference plane at which the sum and difference channels are in phase also turns

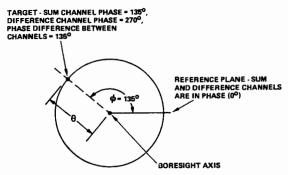


FIG. 40-9 Target location using two-channel monopulse techniques.

about the axis as a function of frequency, whereas in the log-periodic array configuration this plane is independent of frequency. Phase-compensation networks can be employed to stabilize the reference plane when spirals are used.

It should also be noted that, given a priori knowledge of the two-channel monopulse system's patterns and the orientation of the reference plane, this system can also be used for direction finding by measuring the amplitude ratio and phase difference between the sum and difference channels.

40-5 ECM TRANSMIT ANTENNAS

The antenna has been considered to be a transformer used to couple efficiently signals to or from free space. In that context, the problem for ECM-antenna designers has been to impedance-match the coupling device so that maximum power is transferred. Controlled distribution of the signal in space is a requirement of equal importance imposed upon the ECM antenna. Octave bandwidths or greater, medium to high radio-frequency (RF) power-carrying capacity, multiple-polarization response, and a low voltage standing-wave ratio (VSWR) have of course been additional requirements placed upon the ECM-antenna designer.

Antenna Elements

Many different types of antennas have been used in ECM systems. Some of the more common are broadband dipoles, broadband monopoles, spirals, horns and slots, log-periodics, and reflector types. During the past several decades, the RF power-carrying capacity and bandwidth of these basic types have been increased. As an example, the transmitting horns (shown in Fig. 40-10) used in an existing system exhibit a broad frequency bandwidth, high-power capability, high-aspect-ratio beam coverage, and circular-polarization response. Three-to-one-bandwidth, high-aspect-ratio circularly polarized horns have also been developed with satisfactory results.

The basic design problem associated with such horn configurations is the maintenance of a 90° phase differential between two (traveling-wave) quadrature fields in a waveguide structure. Frequency-compensated insertion-phase design techniques

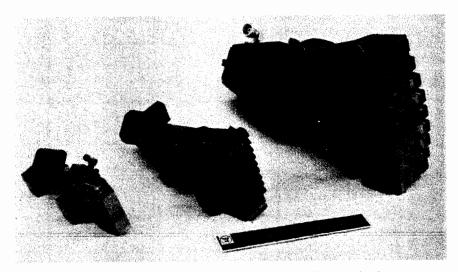


FIG. 40-10 Multiband ECM transmitting horns. (Courtesy of Transco, Inc.)

applicable to the problem have been defined. A simplified analysis of the design of an octave-band circularly polarized horn will illustrate the approach applicable to a horn that uses a dielectric slab to obtain the 90° relative phase shift for the quadrature fields. The phase shift in the plane perpendicular to the wide horn aperture (Y axis, with the phasing plate) and the phase shift in the orthogonal plane (X axis) as illustrated in Fig. 40-11 were calculated; the results are shown in the figure. The calculations are approximate because average horn dimensions were assumed and the lens

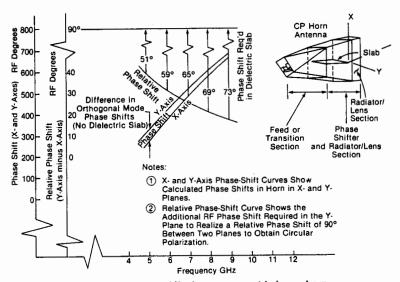


FIG. 40-11 Calculated phase shifts in an asymmetric-beam horn.

portion of the radiator section was assumed to be a waveguide section with soliddielectric loading. The phase shift in a waveguide section loaded with dielectric is given by

$$\Delta \theta = 30.5 X \left(F^2 K_e - \frac{34.9}{a^2} \right)^{1/2}$$

where X is the length of the waveguide section in inches, F is the frequency in gigahertz, K_{ϵ} is the relative permittivity of the material within the guide if dielectric material is used, and a is the guide width in inches. ($K_{\epsilon} = 1$ for air-filled guide. The formula is derived from the standard waveguide-wavelength relationship.) An additional phase delay that increases with frequency in a complementary fashion is required in the Y plane to achieve circularly polarized operation (90° relative phase shift) over the complete RF band. The increase in differential-phase-shift requirements at the higher frequencies is compatible with the dielectric-slab phase-shift characteristics.

Extremely broadband monopoles are now available. Using thick (bladelike) configurations and special impedance matching, a 2:1 bandwidth design is relatively straightforward. One company is engaged in research and development to achieve up to a 6:1 bandwidth. Many broadband blades or monopoles have been used in ECM systems.

Fixed-Beam Arrays

An array can be used to create simultaneous fixed beams or to form beams with a high aspect ratio and of a desired shape. One example of a fixed-beam array is presented to illustrate current designs. Twelve horn elements are arranged in the arc of a circle, as illustrated in Fig. 40-12, to form a beam fixed in space that has broad azimuth coverage and a narrower elevation extent. This configuration is used to combine multiple traveling-wave-tube (TWT) powers in space. The azimuth beamwidth, in the plane of the four-horn subgroups, is broad as shown; the elevation beamwidth

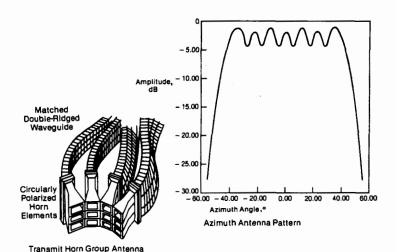


FIG. 40-12 Fixed-beam array for multiple power-amplifier application.

is dependent on the vertical (three-element) array configuration. The individual horn aperture size, both in azimuth and in elevation, must be selected with care. The horn beamwidths are chosen so that approximately one-fourth of the total desired coverage sector is "illuminated" by each horn; the flared section of the horn must be long to reduce aperture phase error, which minimizes phase center spacings. This reduces out-of-phase interference at angles on either side of the in-phase-beam-crossover points. The calculated pattern in Fig. 40-12 shows an approximate 3-dB variation in amplitude; in view of the wide variations in several "factors" affecting jammer-to-radar-signal ratios in a typical ECM application, this pattern variation is quite acceptable. The RF power of 12 TWTs feeding the horn group can be added in space if phase-tracking requirements are satisfied.

Arrays with Beam Control

Combinations of broad- and narrow-beam antenna response are often required. Narrow, or high-gain, beams can be directed to difficult-to-jam high-effective-radiated-power (ERP) pulse radars on a very-short-burst sequential basis, whereas the broad-coverage beam, used most of the time, can be employed against the high-duty-cycle, lower-ERP radars that may be spatially separated. High-quality narrow- and broad-beam patterns have been achieved over an octave bandwidth.

A patented¹⁹ matrix-hybrid array configuration is shown in Fig. 40-13. The feed-system loss depends on the number of radiating elements; amplifiers are inserted near the radiators to negate this feed-loss characteristic. Simultaneous high-ERP beams with fixed positions in space can be created with the design. Beam switching and broad-beam operation with all inputs fed in phase are also possible by using this approach.

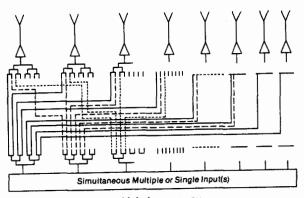


FIG. 40-13 Matrix multiple-beam array.

Another multibeam, multifeed array configuration now receiving considerable attention for both airborne and shipborne applications is the Rotman lens. RF amplifiers are normally inserted in the assembly between the lens feed and each radiating element. The Rotman lens antenna has several advantages: frequency-independent beam pointing is achieved, printed-microwave-circuit technology can be used to fabricate the lens, and very rapid control of high-ERP beams is possible because beam switching is exercised at the low-RF drive power. By using external-polarization-

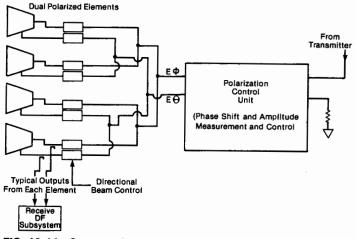


FIG. 40-14 Corporate-feed array.

adjustment techniques, a circularly polarized version of this antenna has been designed for a 3:1 bandwidth. (See Chap. 16.)

A corporate-feed array is illustrated in Fig. 40-14. This array offers some significant advantages: it is compatible with a single-output, high-power jammer; a zoom, or broad-beam pattern response, is available by adjusting the phase shifters in the array to yield a circular phase front; frequency-independent beam pointing is available if nondispersive phase shifters are used; and continuously pointed beams in any direction are available with fine phase-shifter adjustments. For applications in which single-aperture transmit-receive operation is needed, directional couplers can be added near the radiation elements for direction finding and beam control. A polarization-control unit is shown on the right side of the diagram. By using hybrids and phase shifters in the polarization section, any polarization response can be attained.

A concept for very-high-power amplifier paralleling and antenna switching is shown in Fig. 40-15. With the input switch in the position shown, the signals passing through the amplifiers will exhibit a phase front as illustrated; all the power is thus directed to the bottom horn antenna. Low-drive-power switching at the input can direct very large amounts of power to high-gain horns pointed at different angles at the outputs. Without switching, the back-to-back lens configuration can be used as a high-power broadband switch and/or power combiner.

Very-High-Power Antenna Switching (Back-to-Back Lens Configuration)

Feed Power Output Lens

Control Phase Front

FIG. 40-15 Parallel-amplifier configurations.

40-6 ANTENNA ISOLATION IN JAMMING SYSTEMS

Isolation between transmitting and receiving antennas is an important consideration in an ECM system. Analyses and expressions for the calculation of field-strength propagation beyond obstacles have been published. Propagation around a curved surface (cylinders) and beyond knife edges (dif-

fraction) is documented in Ref. 21.

Another antenna-coupling-analysis and measurements program²² addressed the problem of defining the isolation between antennas separated by two conducting planes forming a corner with a variable included angle (see Fig. 40-16). The expressions for antenna coupling, determined by physical-optics analysis and by experiment, are

Isolation =
$$\frac{K_1 G_T G_R \lambda^3}{x^2 Y}$$
 for $x > Y$
= $\frac{K_1 G_T G_R \lambda^3}{x Y^2}$ for $Y > x$

 K_1 is -36.5 dB for circularly polarized horns and spiral antennas and -39.5 dB for monopole antennas. x and Y are defined in Fig. 40-16. G_T and G_R are the transmit and receive antenna gains, each antenna being pointed at the common corner edge. The gain values are in power units with the gain values associated with the polarization perpendicular to the edge surface. These formulas yield reasonably accurate answers for antennas

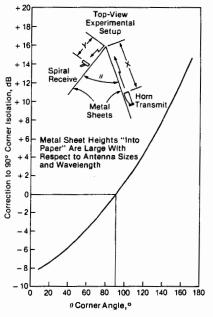


FIG. 40-16 Variation of isolation with corner angle for antenna coupling beyond a corner obstacle.

moved 10 to 20° (measured to the corner) away from the ground planes. Measurements beyond 20° were not performed. The investigation was carried out in the 2- to 4-GHz range. Measured isolations for several different corner angles and antenna types correspond to the calculated isolations to within 2 dB for large variations in x and Y.

40-7 ADVANCED ARRAY SYSTEMS

Solid-State Arrays

Solid-state arrays offer hope for significant improvements in ECM systems.²³ By using a building-block approach, significant ERPs can be obtained because the gain of the array increases with the number of elements; also the total power increases with the number of elements (one amplifier per element). Moreover, transmission-line losses will be reduced because the power amplifiers are located near the radiators. An all-solid-state array configuration, using distributed field-effect-transistor (FET) amplifiers, with potential for full-polarization-diversity capability is shown in Fig. 40-17.

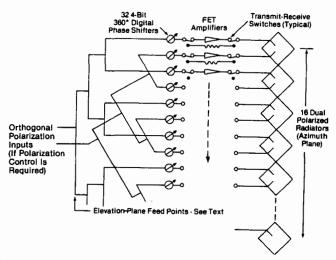


FIG. 40-17 $\,$ 30-kW-EIRP, 8 \times 16 solid-state array with full-polarization-diversity capacility.

An 8- by 16-element array is represented; only one layer of 16 elements in the azimuth plane is indicated. The orthogonal-polarization inputs near the left side of the diagram would, in turn, be fed by an elevation-plane feed network (not shown). Eight layers of antennas (one of which is shown), each layer including its own drive amplifier, are needed to achieve the 30-kW effective isotropic radiated power (EIRP) indicated in the figure. Appropriate feed-subsystem losses have been assumed. The eight layers in elevation would be fed by using a constant circular phase front so that beam control in azimuth only and direction finding in azimuth only would be required. If phase shifters are used in series with each array element, then complete beam control in azimuth and elevation is available. When cost, element power output, and FET efficiencies are improved, this concept will be used in many applications.

Multifunction Apertures

The use of a single aperture to support the operation of many avionic functions in modern and future aircraft will save cost, weight, and space and will permit the reduction of the host aircraft radar cross section (RCS). The following subsystems are candidates for use of one or a few apertures:

- Electronic countermeasures (ECM)
- Electronic support measures (ESM)
- High-gain ESM
- Radar air-to-ground modes
- Radar—air-to-air modes
- Navigation
- Communications

- Data link
- Identification friend or foe (IFF)

This section does not discuss system parameters; instead, signal and antenna characteristics which permit simultaneous operation of and isolation of multiple equipments are emphasized. Isolation between the various transmitters and receivers is a subject of prime importance. The techniques used to isolate transmitters and receivers are complex and interrelated; these techniques must receive maximum attention when a multifunction array is designed. Available isolation techniques are

- Time gating
- Frequency filtering
- Antenna isolation (aperture or array segmentation)
- Power and sensitivity control
- Polarization mismatch
- Amplitude-phase cancellation

Time gating of transmit-receive functions is a powerful tool, but, of course, the subsystems must operate with less than 100 percent duty cycle. Frequency filtering of signals is beneficial; however, close frequency spacing of signals and maximum practical filter interchannel isolations limit this approach. Antenna isolation, between two sections of one array, for example, is quite useful. Antenna isolations in the 30- to 80-dB range are typically achievable between sections of a large aperture depending on antenna (subaperture) spacing and other factors. Equipment power output and sensitivity control can be used; resulting system performance must be maintained at a satisfactory level. Polarization mismatch can be used to reduce coupling between antennas or subarrays, but if the two antennas are coupled via sidelobe radiation, controlled polarization response is not reliable over a wide frequency range. The use of amplitude - phase cancellation effects to isolate a transmitter and receiver is not now considered practical over a wide instantaneous bandwidth. The application of the first three isolation techniques is most useful; these should be considered first when any multifunction-array design is initiated. The last three also should be considered, although system degradation and/or significant complexity can result when these techniques are used. Combinations of several techniques will normally be required to arrive at a satisfactory design.

The sketch in Fig. 40-18 shows how interferometers may be integrated into a phased array. The main-array performance is not affected, since so few elements are used for the interferometer. Note that the two interferometers do not have to be orthogonal to measure azimuth and elevation. The array may be used both in a transmit and a receive mode. Figure 40-19 shows how frequency diplexing and array segmentation may be used to permit array transmission and interferometer receive at the same time. The potential for subsystem isolation is as follows: An estimate of array power induced into each interferometer element near the edge of the array, when a microwave solid-state array is transmitting, is 1 W or less. Since the interferometer receive front ends have frequency filtering near the antenna, the (array) transmitter may be operated in one of the interferometer "front end" frequency channels while the interferometer itself is operating in another channel. The "front end" interferometer phase-calibration input switch can be designed to be linear. Also, the interchannel isolations in the filter can be improved from the

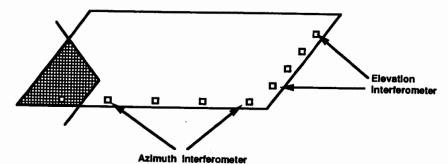


FIG. 40-18 Interferometer integration into a phased array.

presently available 55 to 60 dB or greater. Analyses have shown that the spurious responses in the interferometer receiving system, with a sensitivity of about -70 dBm, will be satisfactory.

Figure 40-20 shows an approach which uses one array to support four system functions. The two systems which require a large aperture—radar and high-gain ESM—utilize the same (large number of) array elements. Therefore, high-gain ESM and radar transmit are mutually exclusive, and array-element switching is used. Owing to the very high radar receiver sensitivity, radar receive is not allowed when the jammer is transmitting. Analyses to date indicate that ultraclean (frequency spectrum) jammer signals not available today would be required to permit jamming at the same instant that a high-

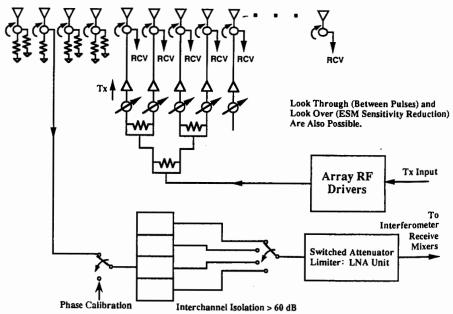


FIG. 40-19 Frequency-diplexer integration of interferometer into a phased array.

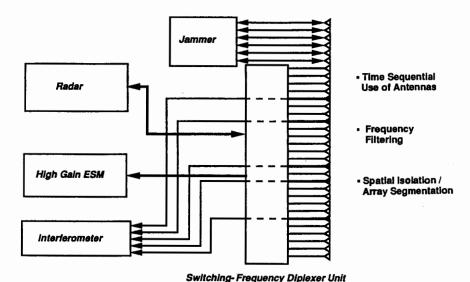


FIG. 40-20 Array segmentation/multiplexing.

sensitivity radar receiver is in operation. The jammer uses a dedicated portion of the aperture; thus such modes as simultaneous transmit with the main array and repeater mode jamming using a remote receive antenna are possible. The interferometer elements are dedicated to that function, and separate receiver front ends are permanently connected to the array elements. Frequency filtering is employed so that "off-frequency" transmissions are possible while relatively low sensitivity interferometer operation is in progress, as discussed above. In addition, look through (between pulses) and look over (sensitivity reduction) are also possible to increase intersystem isolation. The successful development of multifunction antennas will require exploitation of system, antenna, and signal characteristics.

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Radio-Telescope Antennas

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- 41-1 Radio Telescope: Definition 41-2
- 41-2 Position and Coordinates 41-2
- 41-3 Brightness and Flux Density 41-4
- 41-4 Temperature and Noise 41-5
- 41-5 Resolution 41-9
- 41-6 Pattern Smoothing 41-11
- 41-7 Celestial Radio Sources for Pattern, Squint, and Efficiency Measurements of Antennas 41-12
- 41-8 Passive Remote Sensing 41-14

A radio telescope consists of an antenna for collecting celestial radio signals and a receiver for detecting and recording them. The antenna is analogous to the objective lens or mirror of an optical telescope, while the receiver-recorder is analogous to the eye-brain combination or a photographic plate. By analogy the entire antenna-receiver-recorder system may be referred to as a radio telescope, although it may bear little resemblance to its optical counterpart. Radio telescopes are used in much the same manner as optical telescopes for the observation and study of celestial objects. However, the appearance of the sky at radio wavelengths is very different from the way in which it looks optically. Thus, the sun is much less bright. On the other hand, the Milky Way radiates with tremendous strength, and the rest of the sky is dotted with radio sources almost entirely unrelated to any objects visible to the unaided eye (see Fig. 41-1).

The earth's atmosphere and ionosphere are opaque to electromagnetic waves with two principal exceptions, a band or window in the optical region and a wider window in the radio part of the spectrum. This radio window extends from a few millimeters to tens of meters in wavelength, being limited on the short-wavelength side by molecular absorption and on the long-wavelength side by ionospheric reflection. Because of this wide range of wavelengths many forms of antennas are used.

41-2 POSITION AND COORDINATES

The accurate position of a radio source is necessary to distinguish the source from others and to assist in its identification with optical objects when possible. The position is conveniently expressed in *celestial equatorial coordinates: right ascension* α and *declination* δ . The poles of this coordinate system occur at the two points where the earth's axis, extended, intersects the celestial sphere. Midway between these poles is the *celestial equator*, coinciding with the earth's equator, expanded.

The declination of an object is expressed in degrees and is the angle included between the object and the celestial equator. It is designated as a positive angle if the object is north of the equator and negative if south. For example, at the earth's equator a point directly overhead (the zenith) has a declination of 0°, while at a north latitude of 40° the declination of the zenith is +40°.

The meridian is a great circle passing through the poles and a point directly overhead (the zenith). The hour circle of an object is the great circle passing through the object and the poles. The hour angle of the object then is the arc of the celestial equator included between the meridian and the object's hour circle. This angle is usually measured in hours.

A reference point has been chosen on the celestial equator. It is called the *vernal equinox*. The arc of the celestial equator included between the vernal equinox and the object's hour circle is termed the *right ascension* of the object. It is measured eastward from the vernal equinox and is usually expressed in hours, minutes, and seconds of time.

The right ascension and declination of an object define its position in the sky, independent of the earth's diurnal rotation. However, because of the earth's preces-

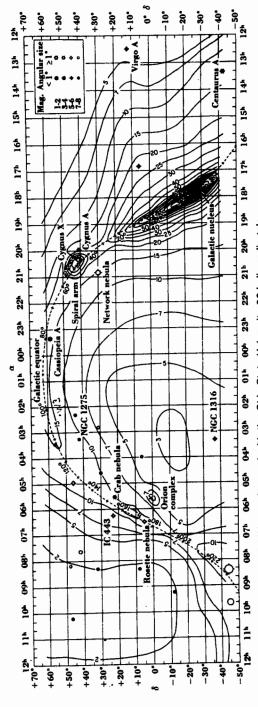


FIG. 41-1 Radio sky at 250 MHz as observed with the Ohio State University 96-helix radio telescope. (After Ko and Kraus.1)

sion, there is a gradual change in these coordinates for a fixed object in the sky, the change completing one cycle in 26,000 years. Thus, the right ascension and declination of an object will again be the same as they are now in 26,000 years. To be explicit, it is necessary to specify the date to which the right ascension and declination refer. This date is called the *epoch*. At present the epoch 1950.0 is commonly used (that is, the right ascension and declination are those of January 1, 1950), but epoch 2000.0 is being used increasingly.

Sometimes the positions of celestial objects are given in galactic coordinates, which are based on the geometry of our galaxy. These coordinates are independent of the earth and hence require no date or epoch. However, there are two systems, old (used before 1960) and new (used after 1960).² Their poles differ by about 1.5°.

By placing an antenna on an equatorial or polar mounting, that is, on axes one of which is parallel to the earth's axis and the other perpendicular to it, a source can be tracked as it moves across the sky by motion in only one coordinate (right ascension). If the antenna is mounted on vertical and horizontal axes, tracking requires motion in two coordinates. The coordinates in this case are altitude (or elevation) and azimuth (or horizontal angle around the horizon), and hence this type of mounting is called an altazimuth mounting.

41-3 BRIGHTNESS AND FLUX DENSITY

Radiation over an extended area of the sky is conveniently specified in terms of its brightness, that is, the power per unit area per unit bandwidth per unit solid angle of sky. Thus,

$$B = \text{brightness (Wm}^{-2}\text{Hz}^{-1}\text{sr}^{-1})$$

Solid angle may be expressed in steradians (sr) or in square degrees (deg2):

$$1 \text{ sr} = 57.3^2 \text{ deg}^2 = 3283 \text{ deg}^2$$

The integral of the brightness B over a given solid angle of sky yields the power per unit area per unit bandwidth received from that solid angle. This quantity is called the power flux density, S. Thus

$$S = \int \int B d\Omega = \text{power flux density (W m}^{-2} \text{ Hz}^{-1})$$

where B = brightness, $Wm^{-2} Hz^{-1} sr^{-1}$

 $d\Omega$ = element of solid angle, sr

Integrating the power flux density from a radio source with respect to frequency yields the total power flux density S_T in the frequency band over which the integration is made. Thus,

$$S_{\rm T} = \int S df = \text{total power flux density (Wm}^{-2})$$

where $S = power flux density, Wm^{-2} Hz^{-1}$

df = element of bandwidth, Hz

41-4 TEMPERATURE AND NOISE

A resistor of resistance R and temperature T matched to a receiver by means of a lossless transmission line as in Fig 41-2 α delivers a power to the receiver given by

$$P = kT \Delta f \tag{41-1}$$

where P = power received, W

 $k = \text{Boltzmann's constant} = 1.38 \times 10^{-23} \,\text{J} \cdot \text{K}^{-1}$

T = absolute temperature of resistor, K

 $\Delta f = \text{bandwidth, Hz}$

If the resistor is replaced by an antenna of radiation resistance R, this equation also applies. However, the radiation resistance is not at the temperature of the antenna structure but at the effective temperature T of that part of the sky toward which the antenna is directed, as in Fig. 41-2b. In effect, the radiation resistance is distributed over that part of the sky included within the antenna acceptance pattern. From this point of view the antenna and receiver of a radio telescope may be regarded as a bolometer (or heat-measuring device) for determining the effective temperature of distant regions of space coupled to the system through the radiation resistance of the antenna.

The power received by a radio telescope from a celestial source is

$$P = SA. \Delta f \tag{41-2}$$

where P = power received, W

S =source flux density, W m⁻² Hz⁻¹

 A_{\bullet} = effective aperture of telescope antenna, m²

 $\Delta f = \text{bandwidth, Hz}$

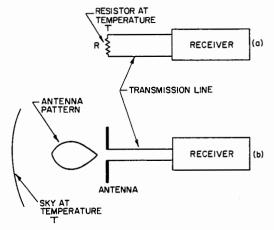


FIG. 41-2 Receiver connected to matched resistor and to antenna.

If this power equals that of a matched (calibration) resistor at temperature T connected to the receiver in place of the antenna, we have by equating Eqs. (41-1) and (41-2)

$$S = \frac{kT}{A_{\bullet}} \tag{41-3}$$

However, if the source is unpolarized (as is true of most celestial sources), only half of its power will be received by any antenna, so the flux density of the source is twice the above value, or

$$S = \frac{2kT}{A}. (41-4)$$

where T = temperature of celestial object, K.

It should be noted that the celestial object is not necessarily at the thermal temperature T. Rather, T is the temperature that a blackbody radiator would need to have to emit radiation equal to that actually emitted by the object at the wavelength of observation. Hence, T is called the *equivalent temperature* of the object. This temperature is the same as the thermal temperature that the reference or calibration resistor must have to give the same response.

Sensitivity is a function of aperture size and also a system temperature and other factors. Thus, the sensitivity, or *minimum detectable (power) flux density*, is given by

$$S_{\min} = \frac{2k}{A_{\bullet}} T_{\min} \tag{41-5}$$

where $k = \text{Boltzmann's constant} = 1.38 \times 10^{-23} \,\text{J} \cdot \text{K}^{-1}$

 T_{\min} = minimum detectable temperature, K

 A_e = effective aperture = $\epsilon_{ap}A_p$, m²

where ϵ_{ap} = aperture efficiency, dimensionless $(0 \le \epsilon_{ap} \le 1)$

 A_p = physical aperture = $\pi (D^2/4)$ for circular aperture, m²

where \hat{D} = diameter of aperture.

The minimum detectable temperature

$$T_{\min} = \frac{K_s}{\sqrt{\Delta f t}} T_{\text{sys}} \tag{41-6}$$

where K_{\bullet} = receiver sensitivity constant, dimensionless (1 $\leq K_{\bullet} \leq 2.8$)

 Δf = intermediate-frequency bandwidth, Hz

t =output time constant, s

 $T_{\text{sys}} = \text{system temperature, K}$

The system temperature depends on the noise temperature of the sky, the temperature of the ground and environs, the antenna pattern, the antenna thermal efficiency, the receiver noise temperature, and the efficiency of the transmission line or waveguide between the antenna and the receiver. The system temperature at the antenna terminals is given by

$$T_{\text{sys}} = T_A + T_{AP} \left(\frac{1}{\epsilon_1} - 1 \right) + T_{LP} \left(\frac{1}{\epsilon_2} - 1 \right) + \frac{1}{\epsilon_2} T_R \qquad (41-7)$$

where T_A = antenna noise temperature, K

 T_{AP} = physical temperature of antenna, K

 ϵ_1 = antenna (thermal) efficiency, dimensionless (0 $\leq \epsilon_1 \leq 1$)

 T_{LP} = physical temperature of transmission line or waveguide between antenna and receiver, K

 ϵ_2 = line or guide efficiency, dimensionless (0 $\leq \epsilon_2 \leq$ 1)

 T_R = receiver noise temperature, K

The antenna temperature is given by

$$T_{A} = \frac{1}{\Omega_{A}} \int \int T(\theta, \phi) P_{n}(\theta, \phi) d\Omega$$
 (41-8)

where Ω_A = antenna-pattern solid angle or antenna beam area, deg² or sr

 $T(\theta,\phi)$ = noise temperature of sky and environs as a function of position angle at wavelength of operation, K

 $P_n(\theta,\phi)$ = normalized antenna power pattern, dimensionless

 $d\Omega$ = elemental solid angle, deg^2 or sr

The elemental solid angle is given by

$$d\Omega = \sin\theta \ d\theta \ d\phi \tag{41-9}$$

where θ = angle from zenith (assuming antenna is pointed at zenith), deg or rad ϕ = azimuthal angle, deg or rad

The antenna beam area is given by

$$\Omega_{\mathcal{A}} = \bigoplus P_{n}(\theta,\phi) d\Omega$$
 (41-10)

The receiver noise temperature is given by

$$T_R = T_1 + \frac{T_2}{G_1} + \frac{T_3}{G_1 G_2} + \cdots$$
 (41-11)

where T_1 = noise temperature of first stage of receiver (usually a low-noise preamplifier), K

 T_2 = noise temperature of second stage, K

 T_3 = noise temperature of third stage, K

 G_1 = gain of first stage

 G_2 = gain of second stage

Additional terms may be required if the temperature is sufficiently high and the gain sufficiently low on additional stages.

Radio telescopes are often used at one end of a communication circuit, and for this application the *signal-to-noise ratio* is of prime importance. When a radio telescope is the receiving station, we have from the Friis transmission formula that

$$P_r = \frac{P_i A_{ei} A_e}{r^2 \lambda^2} \tag{41-12}$$

where P_r = power received, W

 $A_{\mathbf{g}}$ = effective aperture of transmitting antenna, m²

 $A_{\rm rr}$ = effective aperture of receiving or radio-telescope antenna, m²

r = distance between transmitting and receiving station, m

 λ = wavelength of operation, m

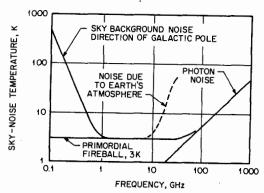


Fig. 41-3 Antenna sky noise temperature as a function of frequency. It is assumed that the antenna is pointed at the zenith, that the beam angle (HPBW) is less than a few degrees, and that the beam efficiency is 100 percent. (After Kraus and Ko³ below 1 GHz; after Penzias and Wilson⁴ above 1 GHz.)

TABLE 41-1 Radio Astronomy Units

Dimension or quantity	Symbol	Description	Unit
Brightness	В	Power flux density Solid angle	Wm ⁻² Hz ⁻¹ sr ⁻¹
Power flux density	S	$= \int \int B d\Omega$	$Wm^{-2}Hz^{-1}$
Total power flux density	S_{T}	$= \int S df$	Wm^{-2}
Power (in terms of temperature)	P	$= kT \Delta f$	w
Brightness temperature	T	$=\frac{B\lambda^2}{2k}$	K
Power flux density (in terms of temperature)	S	$=\frac{2kT}{A_{\bullet}}$	$Wm^{-2}Hz^{-1}$
Minimum detectable flux density	$S_{ m min}$	$=\frac{2kT_{\min}}{A_{\bullet}}$	Wm ⁻² Hz ⁻¹
Minimum detectable temperature	$T_{ m min}$	$=\frac{K_s}{\sqrt{\Delta ft}}$	K

NOTE: W = watts; m = meters; Hz = hertz; sr = steradians; K = kelvins = degrees celsius (°C) above absolute zero; df = infinitesimal bandwidth; Δf = finite bandwidth = $f_2 - f_1$; λ = wavelength; J = joules; K_s = receiver constant.

By dividing this received power by the minimum detectable power of the radio telescope we obtain the signal-to-noise ratio as

$$\frac{S}{N} = \frac{P_r}{S_{\min} A_{er} \Delta_f} = \frac{P_t A_{et} A_{er} \sqrt{t}}{r^2 \lambda^2 k T_{sys} \sqrt{\Delta f}}$$
(41-13)

where P_t = transmitter power, W

 A_{et} = effective aperture of transmitting antenna, m²

 A_{er} = effective aperture of receiving antenna, m²

t =output time constant, s

r = distance between transmitting and receiving stations, m

 λ = wavelength of operation, m

 $k = \text{Boltzmann's constant} = 1.38 \times 10^{-23} \,\text{J} \cdot \text{K}^{-1}$

 T_{sys} = system temperature of radio telescope, K

 Δf = intermediate-frequency bandwidth, Hz

It is assumed that the receiver is a total-power type $(K_s = 1)$ and that the radio telescope is matched to both the polarization and the bandwidth of the transmitted signal.

The antenna temperature T_A (which contributes to the system temperature T_{sys} , as discussed above) includes the contribution of the sky background and the temperature of the ground to the entire antenna pattern (main lobe and backlobes). In no case can T_A be less than 3 K, the limiting temperature of the sky resulting from the primordial fireball. The sky background temperature versus frequency is presented in Fig. 41-3.

Radio-astronomy units are summarized in Table 41-1.

41-5 RESOLUTION

The limiting resolution of an optical device is usually given by *Rayleigh's criterion*. According to this criterion, two identical point sources can just be resolved if the maximum of the diffraction pattern of source 1 coincides with the first minimum of the pattern of source 2.

Assuming a symmetrical antenna pattern as in Fig. 41-2a, Rayleigh's criterion applied to antennas states that the resolution of the antenna is equal to one-half of the beamwidth between first nulls; that is,

$$R = \frac{\text{BWFN}}{2} \tag{41-14}$$

where R =Rayleigh resolution or Rayleigh angle

BWFN = beamwidth between first nulls

An antenna pattern for a single-point source is shown in Fig. 41-4a. The pattern for two identical point sources separated by the Rayleigh angle is given by the solid curve in Fig. 41-4b, with the pattern for each source when observed individually shown by the dashed curves. It is to be noted that the two sources will be resolved provided that the half-power beamwidth (HPBW) is less than one-half of the beamwidth between first nulls, as is usually the case.

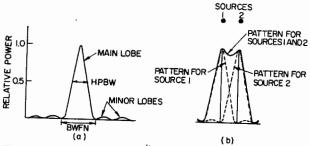


FIG. 41-4 Antenna power pattern (a) and power patterns for two identical point sources (b) separated by the Rayleigh angle as observed individually (dashed) and together (solid).

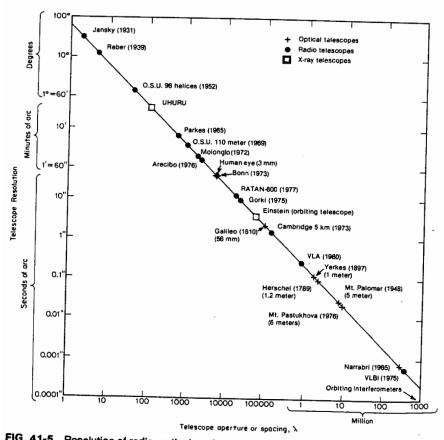


FIG. 41-5 Resolution of radio, optical, and x-ray telescopes as a function of the telescope aperture or interferometer spacing. (From J. D. Kraus.⁶)

TABLE 41-2

Uniform Apertures	Rayleigh resolution (BWFN/2)	HPBW
Rectangular (length L_{λ} wavelengths)	57.3°/L _A	50.3°/L _λ
Circular (diameter D_{λ} wavelengths)	70°/D _λ	59°/D _λ

It may be shown⁵ that the beamwidth between first nulls for a broadside antenna with a uniform aperture many wavelengths long is given by

BWFN =
$$\frac{114.6}{L_{\lambda}}$$
 (41-15)

These results are summarized in Table 41-2, which also gives the beamwidths for uniform circular apertures. The HPBWs are some 15 percent less than the Rayleigh resolution angles for both rectangular and circular apertures.

For two-element interferometers the resolution is given by $57.3^{\circ}/S_{\lambda}$, where S_{λ} is the spacing in wavelengths between the elements. For large spacings, extremely fine resolution can be obtained as indicated in Fig. 41-5, which presents the resolution of radio, optical, and x-ray telescopes.

41-6 PATTERN SMOOTHING

A unique pattern (or far-field pattern) of an antenna is obtained when the radiator is a point source situated at a sufficient distance from the antenna. The distance is sufficient if an increase produces no detectable change in the pattern. (See Sec. 41-8 for a more detailed discussion.) Let this pattern of a receiving antenna be as shown in Fig. 41-6a. If the point source is replaced by an extended source at the same distance,

the observed pattern is modified as suggested in Fig. 41-6b. The extended source results in a broadened pattern with reduced minor lobes.

The patterns in Fig. 41-6 are in polar coordinates. In rectangular coordinates, the antenna pattern is as shown in Fig. 41-7a. The extended source distribution is shown in Fig. 41-7b. The observed pattern is then as shown in Fig. 41-7c. These three patterns are superposed in Fig. 41-7d to facilitate intercomparison.

It is to be noted that the observed pattern is only an approximation of the actual source pattern or distribution, the sharp shoulders of the source distribution

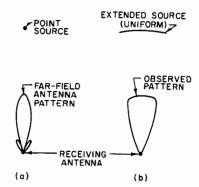


FIG. 41-6 Antenna patterns in polar coordinates for a point source and for an extended source.

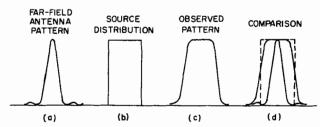


FIG. 41-7 Pattern in rectangular coordinates for antenna (a) and for uniform source distribution (b). The resultant observed pattern is at c. The three patterns are superposed for comparison in d.

being rounded off. It is said that the source distribution has been smoothed or blurred by the observing technique. The broader the antenna beamwidth compared with the source pattern, the greater the smoothing effect. On the other hand, the narrower the antenna beamwidth compared with the source pattern, the more nearly is the observed pattern an exact reproduction of the source distribution. However, there is always some smoothing, and one of the important problems of radio astronomy is to reconstruct, insofar as possible, the true source distribution from the observed pattern. It turns out that it is not possible to reconstruct the true source distribution since certain of the finer source details have no effect on the observed pattern and are irretrievably lost. However, partial reconstruction is usually possible, so that a source distribution that is more nearly like the exact source distribution than the observed pattern can be obtained. Pattern smoothing and related topics are discussed in detail in Kraus.²

41-7 CELESTIAL RADIO SOURCES FOR PATTERN, SQUINT, AND EFFICIENCY MEASUREMENTS OF ANTENNAS

Celestial radio sources are often useful for the measurement of far-field patterns, squint, and aperture efficiency of antennas, especially large-aperture antennas operating at short wavelengths when the distance to the far field is very large (10s or 100s of kilometers). (See Sec. 41-8 concerning the magnitude of this distance.)

For pattern measurements, the radio source should have a small angular extent (considerably less than the antenna HPBW), be relatively strong, and be well isolated from nearby sources. For aperture-efficiency measurements, accurate flux densities are required over a wide frequency range, and generally the source should be essentially unpolarized (less than 1 or 2 percent). For squint measurements, the position of the sources should be accurately known.

The upper part of Table 41-3 lists a few selected radio sources which meet most or all of the above requirements, that is, they are relatively strong, ½ to 1° from the nearest neighboring sources, of small angular extent, and essentially unpolarized and have accurate positions and also accurate flux densities over a wide frequency range. The lower part of the table lists three sources which do not meet all the above requirements but nevertheless may be useful for some purposes.

TABLE 41-3 Radio Sources for Pattern, Squint, and Efficiency Measurements

		ď	ositio	Position (epoch 1950.0)	och Och	195(<u>6</u>											
	æ	ght a	Right ascension	slon		Decl	Declination	Ĕ				Flu	x dens	Flux density, (Jy) †	÷		Doloria	
Source	ء	min	œ	s error	۰	Arc Arc min s	Arc	Arc s error	Size, arc min	tion,	38 MHz	178 MHz	750 MHz	1400 MHz	2695 MHz	5000 MHz	zation,	5000 zation, Distance, light-
20,00	٤	ę	10 6	40	7	47	ě	7	-	_	112	43	17	11.3	6.4	4.2	1.8	
35.20	3 8	2 8	20.7	5	48	;	6 6		0.25	_	991	89	23	13.9	7.7	4.4	1.2	$8 \times 10^{9} (z = 0.9)$
30130	3 5	3 6	22.0	7 -	3	1 2	30	~	0.35		140	63	45	40	42	45		$3 \times 10^9 \ (z = 0.16)$
30.273	7 :	3 8	32.7	5 6	3 5	. %	7 7		0.3	0	94	83.5	35	22.4	15	6.5	0.4	$7.5 \times 10^9 (z = 0.85)$
30.293	± 1	5 %	33.0	2.0	7 6	3 2	28 2	٠,			0691	351	84	44.5	22.4	11.9		$3 \times 10^9 (z = 0.15)$
3C348	2 %	ę %	13.4	0.0	3 4	2 4	3 4	2	0.25	0.5	211	29	22	14.4	01	7.5	1.2	$7 \times 10^9 (z = 0.7)$
Cygnus A	6	57	44.5	0.5	8	35	05		1.6	•	22,000	8,700	2,980	1,590	785	371	0.2	10%
10123	2	33	552	0.2	29	34	14	2	0.1	:	57-	681	72	45.8	27	91	1.2	
3C286	3 2	28	49.7	0.2	3	46	05	7	0.04	0.5	32	24	81	14.6	2	7.5	6	,
Cas A	23	21	07		28	33	48		\$	•:	* 37,200 11,600 3,880	11,600	3,880	2,410	1,470	910	:	11,000

*In complex galactic plane region. †1 Jy = 1 jansky = 10^{-26} Wm⁻²Hz⁻¹.

The source designation refers to the third Cambridge (3C) catalog. Distances are given in light-years. The red shift z is also given. The red shift is the physical quantity measured from which a distance is inferred. Cygnus A is an exploded galaxy at a distance of 1 billion (10^9) light-years. Cassiopeia A (Cas A) is a supernova remnant (plasma cloud from an exploded star) at a distance of 11,000 light-years. Cas A is the strongest source in the sky except for the sun. Positions are from Bridle, Davis, Formalont, and Lequeux, and flux densities are from Kellermann, Pauliny-Toth, and Williams. Flux densities at frequencies between those given in the table can be interpolated from the values given.

The source isolation (proximity of neighboring sources) was determined by inspection of the radio maps of the Ohio Sky Survey. This survey is in seven parts with two supplements.

From the measurement of the antenna temperature difference (ΔT in °C) produced by the observed radio source, the effective aperture (A_e) of the antenna is given by

$$A_{\bullet} = \frac{2k\Delta T}{S} \tag{41-16}$$

where S = flux density of source at frequency of measurement, Wm⁻² Hz⁻¹ $k = 1.38 \times 10^{-23} \text{ J} \cdot \text{K}^{-1}$

The aperture efficiency is then

$$\epsilon_{ap} = \frac{A_e}{A_p} \tag{41-17}$$

where A_e = effective aperture, m²

 A_p = physical aperture m²

For a detailed discussion of the measurement of celestial radio sources see Kraus.²

41-8 PASSIVE REMOTE SENSING

As pointed out in Sec. 41-4, a radio telescope acts like a bolometer (or heat-measuring device) for determining the temperature of objects (far or near) coupled to the system through the radiation resistance of the antenna.

A radio telescope is a remote sensing device whether it is earth-based and pointed at the sky for observing celestial objects or on an aircraft or satellite and pointed at the earth. In this section we consider the case where the radiation detected or sensed by the telescope originates in the objects being observed, making for a passive remote sensing system in distinction to radar, or active remote sensing, where signals are transmitted and their reflections observed and analyzed. Let us consider three examples of passive remote sensing.

Example 1: Mars temperature The incremental antenna temperature for the planet Mars measured with the U.S. Naval Research Laboratory 10 15-m radio telescope at 31.5-mm wavelength was 0.24 K. Mars subtended an angle of 0.005° at the time of the measurement. The antenna HPBW = 0.116°. Find the average temperature of Mars at 31.5-mm wavelength.

Solution We note that the solid angle Ω , subtended by the source (Mars) is less than the solid angle Ω_A within the antenna's half-power beamwidth (HPBW). The Mars temperature is then

$$T_s = \frac{\Omega_A}{\Omega_c} \Delta T_A \simeq \frac{0.116^2}{\pi (0.005^2/4)} 0.24 = 164 \text{ K}$$

This temperature is less than the infrared temperature measured for the sunlit side (250 K), implying that the 31.5-mm radiation may originate further below the Martian surface than the infrared radiation. This is an example of the *remote sensing* of another planet from the earth.

Example 2: Earth temperatures With a radio telescope on an orbiting satellite for observing the earth surface temperature T_{ϵ} and a forest area at a temperature T_{f} , the incremental satellite antenna temperature is given by

$$\Delta T_A = T_f(1 - e^{-\tau}) + T_e e^{-\tau} (K)$$
 (41-18)

where τ is the absorption coefficient of the forest. We assume here that the antenna beam is completely subtended by the forest. In the absence of forest or other cover, $\tau=0$ and the telescope measures the surface temperature of the ground ($\Delta T_A=T_e$). On the other hand, if the forest is completely absorbing, $\tau=\infty$ and the telescope measures the forest temperature ($\Delta T_A=T_f$).

As a numerical example, suppose that the remote sensing antenna of a 3-GHz orbiting satellite measures a temperature $\Delta T_A = 300$ K when directed at a tropical forest with absorption coefficient $\tau = 0.693$ at vertical incidence. If the temperature T_e of the earth's surface at ground level under the forest is 305 K, find the temperature of the forest.

Solution Since $\tau = 0.693$, $e^{-\tau} = 0.5$, so from Eq. (41-18),

$$T_f = \frac{\Delta T_A - T_e e^{-\tau}}{1 - e^{-\tau}} = \frac{300 - 305 \times 0.5}{1 - 0.5} = 295 \text{ K}$$

Knowing T_{\bullet} and τ , as above, the forest temperature T_f can be determined, or knowing T_{\bullet} and T_f , the absorption coefficient can be deduced. It is by such a technique that the whole earth can be surveyed and much information obtained about the temperature of land and water areas and from absorption coefficients about the nature of the surface cover.

Example 3: Horn absorber If a perfect absorber with the impedance of space (=377 Ω/square) is placed so as to completely cover the front of a horn antenna, it will ideally produce an antenna temperature equal to the absorber's thermometer-measured temperature. If the absorber is completely shielded from the outside (open only to the horn) and is cooled, it can provide calibration temperatures for the radio telescope. Thus, if cooled to liquid helium temperature, it will give a 4.1 K calibration. Or if the absorber temperature can be controlled so that when the absorber is in front of the horn the radio telescope response is the same as with the absorber removed, the temperature of the object or region being observed by the radio telescope is equal to the absorber temperature. This null type of measurement is used on the Cosmic Background Explorer (COBE) satellite to measure the 3 K sky background at microwave frequencies. The temperature has now been evaluated more accurately as 2.73 K. This temperature is believed to be from the remnant of the primordial Big Bang and is the lowest possible antenna temperature for a sky-scanning radio telescope. A12-14

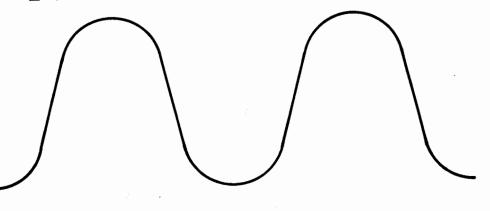
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Topics Associated with Antennas





Transmission Lines and Waveguides

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42-1	General 42-4
42-2	Open-Wire Transmission Lines 42-5
42-3	Wires in Various Enclosures 42-5
42-4	Strip Transmission Lines 42-8
42-5	Coaxial Lines: Solid Conductor 42-13
	Coaxial-Line Parameters 42-13
	Coaxial Line with Helical Center
	Conductor 42-15
	Coaxial Line, Bead-Supported 42-15
	Coaxial Line, Stub-Supported 42-15
	Semiflexible Coaxial Lines 42-17
42-6	Flexible Coaxial Lines 42-17
42-7	Hollow-Tube Waveguides 42-19
	Propagation 42-19
	Rectangular Waveguides 42-31
	Circular Waveguides 42-33
	Standard Waveguide Sizes 42-34
	Flexible Waveguides 42-35
	Hollow-Tube Waveguides with Other Cro
	Sections 42-35
42-8	Miscellaneous Types of Waveguides 42-38
	Trough Waveguide 42-38
	Radial Line and Biconical Guide 42-40
	Dielectric Waveguide 42-42
	Multimode Waveguide 42-44
	Beam Waveguide 42-44
	Optical-Fiber Waveguide 42-44
	Elliptical Waveguide 42-45

In the applications of antennas, it is necessary to use some form of transmission line to connect the antenna to a transmitter or receiver. It is essential to know the propagation characteristics of the more common forms of line.

The transmission lines in Secs. 42-2 to 42-6 are almost always used in the transverse electromagnetic (TEM) mode of propagation and therefore possess a unique characteristic impedance. In air, the guide wavelength λ_g is equal to the free-space wavelength λ . Propagation in this mode exists at any frequency, although above a certain frequency higher modes may also exist. It is assumed that the line loss is small and may be neglected in calculating the characteristic impedance.

The waveguides considered in Secs. 42-7 and 42-8 use modes of propagation having a longitudinal component and do not possess a unique characteristic impedance. Propagation may only take place above a certain unique cutoff frequency defined by the mechanical dimensions. The guide wavelength λ_g is related to the free-space wavelength λ by $1/\lambda_g^2 = 1/\lambda^2 - 1/\lambda_c^2$, where λ_c is the cutoff wavelength.

In all cases, it will be assumed that the skin depth is small compared with the dimensions of the conductors and that these conductors are nonmagnetic. The medium surrounding the conductors is often air, but for other dielectrics a loss will be introduced, and this is independent of the line dimensions. In the case of TEM modes this loss is

$$\alpha_D = \frac{\pi}{\lambda_D} \tan \delta$$
 Np/m

where λ_D (= $\lambda/\sqrt{\epsilon}$) is the intrinsic wavelength in the medium and tan δ is the loss tangent of the dielectric. ϵ is the relative dielectric constant. For waveguide modes, the wavelength in the guide must be considered, and the dielectric loss becomes

$$\alpha_D = \frac{\pi \lambda_g}{(\lambda_D)^2} \tan \delta$$
 Np/m

In circuits having discontinuities, such as bends, the open types of line will have additional loss because of radiation at these points, and therefore shielded types should generally be used for complex circuits.

The power-handling capacity of transmission lines in the following sections is given in terms of the maximum allowable field intensity E_a in the dielectric, whereas for waveguides the power is given directly for air dielectric. For such calculations, $E_a = 3 \times 10^6 \text{ V/m}$ is the theoretical maximum for air dielectric, at normal temperature and atmospheric pressure, but for proper derating a value of $2 \times 10^6 \text{ V/m}$ is more practical. Other dielectrics having a higher dielectric strength may be used to increase the power limit, but in the case of solid dielectrics, the increased field strength in air pockets, which are very likely to exist, imposes a serious limitation. A common method of increasing the power limit is to use pressurized air, the maximum power being proportional to the square of the absolute pressure.

^{*}A list of symbols is presented in Sec. 42-9.

The conditions discussed above apply to a matched line. The maximum power is inversely proportional to the standing-wave ratio.

Important transmission-line equations are shown in Table 42-1 for both TEM and non-TEM lines and waveguides.

42-2 OPEN-WIRE TRANSMISSION LINES

Open-wire transmission lines are an arrangement of wires whose diameters generally are small compared with the spacings involved. This arrangement is sometimes used in conjunction with a ground plane to which the wires are parallel. Such transmission lines have the advantage of simplicity and economy. The spacing between the wires and between the wires and the ground plane is very much less than a wavelength.

The most common of the open-wire lines is the two-wire line. For two wires of diameter d, spaced at a center-to-center distance D, the characteristic impedance is

$$Z_0 = \frac{120}{\sqrt{\epsilon}} \cosh^{-1} \frac{D}{d} \qquad \Omega$$

This relation is plotted in Fig. 42-1. In the case of unequal wire diameters d_1 and d_2 , d is replaced by $\sqrt{d_1d_2}$.

The conductor loss is

$$\alpha_c = 2.29 \times 10^{-6} \quad \sqrt{\frac{f\epsilon}{\sigma}} \frac{1}{d \log_{10} (2D/d)}$$
 Np/m

The power-handling capacity is

$$P = \frac{E_a^2 d^2 \sqrt{\epsilon}}{240} \cosh^{-1} \frac{D}{d} \qquad W$$

where E_a is the maximum allowable field intensity in the dielectric (Sec. 42-1).

Other configurations of open-wire lines are shown in Fig. 42-2, together with formulas for the characteristic impedance. Lines near a ground plane are also included. Other types of open-wire lines can be found in the literature.

42-3 WIRES IN VARIOUS ENCLOSURES

It is often advantageous to tailor a transmission line to fit a specific application when one of the more common forms is not convenient. Furthermore, with many antenna configurations a nonstandard form of line has definite advantages.

Various forms of transmission line comprising wires in different-shaped enclosures are shown in Fig. 42-3, together with formulas for characteristic impedance. It should be noted that these lines are shielded, with the exception of the corner enclosure, provided that those that are physically open have an opening less than one-half wavelength across, extend beyond the wire at least one-half wavelength, and have opposing surfaces that are maintained at the same potential.

TABLE 42-1 Transmission-Line Equations

	General line		Ideal line		Approximate results for low-loss lines	loss lines
Quantity	TEM line	Other	TEM line	Other	TEM line	Other
Propagation constant $\gamma = \alpha + j\beta$	$\sqrt{(R+j\omega L)(G+j\omega C)}$		jω√ĽČ	$j \frac{2\pi}{\lambda_g}$	(See α and β below)	(See α and β)
Phase constant β	$Im(\gamma)$	$\operatorname{Im}(\gamma) \qquad \operatorname{Im}(\gamma)$	$\omega \sqrt{LC} = \frac{\omega}{v} = \frac{2\pi}{\lambda}$	24	$\omega \sqrt{LC} \left[1 - \frac{RG}{4\omega^2 LC} + \frac{G^2}{8\omega^2 C^2} + \frac{R^2}{8\omega^2 L^2} \right]$	2,4
Attenuation constant α	Re(\gamma)	$Re(\gamma)$ $Re(\gamma)$	0	* 0	$\frac{R}{\sqrt{3}} + \frac{GZ_0}{\sqrt{3}} \approx \frac{\pi}{4} \tan \delta^*$	⊭ 1
Characteristic impedance Z ₀	$\sqrt{\frac{R+j\omega L}{G+j\omega C}}$	$\frac{R + j\omega L}{G + j\omega C}$ Geometry-	$\sqrt{\frac{L}{c}}$	Geometry- dependent	$\left[\sqrt{rac{L}{C}} \left[1 + j \left(rac{G}{2\omega C} - rac{R}{2\omega L} ight) ight]$	Geometry-dependent

$Z_0 \left[\frac{al \cos \beta l + j \sin \beta l}{\cos \beta l + jal \sin \beta l} \right]$	$Z_0 \left[\frac{\cos \beta l + j\alpha l \sin \beta l}{\alpha l \cos \beta l + j \sin \beta l} \right]$	$Z_0 \left[\frac{Z_0 + Z_L \alpha l}{Z_L + Z_Q \alpha l} \right]$	$Z_0 \left[\frac{Z_L + Z_0 \alpha l}{Z_0 + Z_L \alpha l} \right]$				
$Z_0 \left[\frac{Z_L \cos \beta l + j Z_0 \sin \beta l}{Z_0 \cos \beta l + j Z_L \sin \beta l} \right]$	$jZ_0 an eta l$ $-jZ_0 an eta l$	Z_L^3	Z_L	$V_i \cos \beta z - j I_i Z_0 \sin \beta z$	$I_1\cos eta z - jrac{V_i}{Z_0}\sin eta z$	$\frac{Z_L-Z_0}{Z_L+Z_0}$	$\frac{1+ \rho }{1- \rho }$
$Z_0 \left[\frac{Z_L \cosh \gamma l + Z_0 \sinh \gamma l}{Z_0 \cosh \gamma l + Z_L \sinh \gamma l} \right]$	$Z_0 \tanh \gamma l$ $Z_0 \coth \gamma l$	$Z_0 \left[\frac{Z_L \sinh \alpha l + Z_0 \cosh \alpha l}{Z_0 \sinh \alpha l + Z_L \cosh \alpha l} \right]$	$Z_0 \left[\frac{Z_L \cosh \alpha l + Z_0 \sinh \alpha l}{Z_0 \cosh \alpha l + Z_L \sinh \alpha l} \right]$	$V_i \cosh \gamma z - I_0 Z_0 \sinh \gamma z$	$I_i \cosh \gamma z - rac{V_i}{Z_0} \sinh \gamma z$	$\frac{Z_L-Z_0}{Z_L+Z_0}$	$\frac{1+ \rho }{1- \rho }$
Input impedance Z_l	Impedance of shorted line Impedance of open line	Impedance of quarter- wave line	Impedance of half-wave line	Voltage along line $V(z)$	Current along line $I(z)$	Reflection coefficient $ ho$	Standing-wave ratio

Symbols:

R, L, G, C =distributed resistance, inductance, conductance, and capacitance per unit length.

/ = length of line.

Subscript i denotes input-end quantities.
Subscript L denotes load-end quantities.

z = distance along line from input end.

 λ = wavelength measured in dielectric.

v = phase velocity of line equals velocity of light in dielectric of line for an ideal line. λ_g = guide wavelength. tan δ = loss tangent of dielectric.

*Case of low conductor loss.

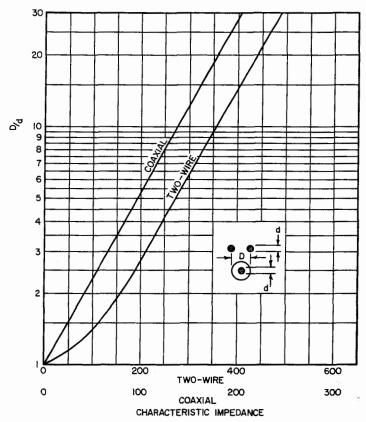


FIG. 42-1 Characteristic impedance of common lines.

42-4 STRIP TRANSMISSION LINES

In strip transmission lines the conductors are flat strips that most frequently are photoetched from a dielectric sheet which is copper-clad on one or both sides. Although not often used as uniform transmission lines, they are very useful for antenna feeds, networks, printed arrays, and slots. They are also useful for a number of microwave integrated circuits such as amplifiers, filters, and high-speed digital logic circuits.

A number of different types of these transmission lines have been suggested, but a good variety of useful characteristics are supplied by four basic types that complement each other well: microstrip, slotline, coplanar waveguide, and coplanar strip. Cross sections of these types are shown in Fig. 42-4, along with methods for computing Z_0 and λ_g or effective dielectric constant. Microstrip is made of a dielectric sheet with a narrow conducting pattern of copper on one side and a copper sheet serving as a ground plane on the other. Transmission is mostly of the TEM mode with a good part of the electric field between the broad face of the conductor and the large ground plane.

WIRES IN SPACE	CHARACTERISTIC IMPEDANCE	WIRES NEAR GROUND	CHARACTERISTIC IMPEDANCE
I. D. D. d	$Z_0 = \frac{207}{\sqrt{4}} \log_{10} 1.59 \frac{D}{d}$	4.	$Z_0 = \frac{138}{\sqrt{\epsilon}} \log_{10} \frac{4h}{d}$
2. - 0, - 1	$Z_0 = \frac{138}{\sqrt{4}} \log_{10} \frac{2D_2}{d\sqrt{1 + (D_2/D_1)^2}}$	5. BALANCED PAIR PS	$Z_0 = \frac{276}{\sqrt{e}} \log_{10} \frac{4h}{d\sqrt{1+(2h/5)^2}}$
3. <u>p/2 p/2</u> 	$Z_0 = \frac{173}{\sqrt{a}} \log_{10} 1.14 \frac{D}{d}$	6. PARALLEL d PAIR L S S S S S S S S S S S S S S S S S S S	$Z_0 = \frac{69}{\sqrt{4}} \log_{10} \frac{4h}{d} \sqrt{1 + (2h/S)^2}$
TWIN LEAD	Z _O DEPENDS ON WIRE DIAMETER, SPACING, AND THE SHAPE OF THE DIE - ELECTRIC, USUALLY POLY- ETHYLENE. IT IS MOSTLY MADE IN 300 Ω.	7. J. S. J. J. S. J.	$Z_0 = \frac{276}{\sqrt{\epsilon}} \log_{10} \frac{2S}{d\sqrt{1 + S^2/4h_1 h_2}}$

FIG. 42-2 Open-wife lines. Note that d is small compared with other dimensions.

SINGLE WIRE	CHARACTERISTIC IMPEDANCE	WIRE PAIR	CHARACTERISTIC IMPEDANCE
1. d O D/2	$Z_0 = \frac{138}{\sqrt{a}} \left[\log_{10} \frac{4D}{\pi d} - \frac{0.0367 \left(\frac{d}{D}\right)^4}{1 - 0.355 \left(\frac{d}{D}\right)^4} \right]$	5. +s+ D/2 + O O O	$Z_0 = \frac{276}{\sqrt{\epsilon}} \log_{10} \frac{4D}{\pi d} \tanh \frac{\pi S}{2D}$
2. D/2	$Z_0 = \frac{138}{\sqrt{4}} \log_{10} \frac{\sqrt{2}D}{d}$	6. D/4 0/2 D/4 8	$Z_0 = \frac{276}{\sqrt{\pi}} \log_{10} \frac{2D}{\pi d}$
3 d	$Z_0 = \frac{138}{\sqrt{\pi}} \log_{10} \frac{4D}{\pi d} \tanh \frac{\pi h}{D}$ FOR EXACT FORMULA SEE	-h-+	$Z_0 = \frac{276}{\sqrt{\epsilon}} \log_{10} \frac{2D}{\pi d \sqrt{A}}$ $A = \csc^2(\frac{\pi S}{d}) + \operatorname{csch}^2(\frac{2\pi h}{d})$
4. d D/2	$Z_0 = \frac{138}{\sqrt{\epsilon}} \log_{10} 1.08 \frac{D}{d}$	8. <u>W/2 W/2</u> 0 8 D/2 1 D/2 5/2	$Z_{0} = \frac{Z_{0}}{\sqrt{\epsilon}} \left(\log_{10} \frac{4D}{\pi d} \tanh \frac{\pi S}{2D} - \sum_{n=1}^{\infty} \log_{10} \frac{1 + u_{n}^{2}}{1 - v_{n}^{2}} \right)$ $u_{n} = \frac{\sinh \frac{\pi S}{2D}}{\cosh \frac{n\pi W}{2D}}, v_{n} = \frac{\sinh \frac{\pi S}{2D}}{\sinh \frac{n\pi W}{2D}}$

FIG. 42-3 Wires in various enclosures. Note that d is small compared with other dimensions except in case 1.

TRANSMISSION	CHARACTERISTIC IMPEDANCE	EFFECTIVE DIELECTRIC CONSTANT
MICROSTRIP	WIDE STRIP, W/h>1 $Z_0 = \frac{377}{\sqrt{\epsilon_{re}}} \left\{ \frac{We}{h} + 1.393 + 0.6672n \left(\frac{We}{h} + 1.444 \right) \right\}$ NARROW STRIP, W/h<1 $Z_0 = \frac{377}{2\pi \sqrt{\epsilon_{re}}} 2n \left[\frac{8h}{We} + 0.25 \frac{We}{h} \right]$	e +1 /e -1\ /w\
COPLANAR STRIPS	$Z_0 = \frac{377}{V_{e_{fe}}^2} \frac{K.(ke)}{K'(ke)}$ WHERE $ke = \frac{Se}{Se + 2We} \approx k - \frac{(1 - k^2)\Delta}{2W}$ AND $\Delta = \left(\frac{1.25t}{77}\right) \left[1 + 2n\left(4\pi\frac{W}{t}\right)\right]$	$\begin{split} & e_{re}^{\dagger} = e_{re} - \frac{1.4 \left(e_{re} - 1\right) t/s}{\kappa \left(k\right) + 1.4 \frac{t}{s}} \\ & \text{WHERE } e_{re} = \frac{e_r + 1}{2} \left[\tanh \left\{ 1.785 \log \left(\frac{h}{W}\right) + 1.75 \right\} + \frac{kW}{h} \left\{ 0.04 - 0.7 k + 0.01 \left(1 - 0.1e_r\right) \left(0.25 + k\right) \right\} \right] \\ & \text{AND } k = S/(S + 2 W) \end{split}$
COPLANAR WAVEGUIDE	Z_0 : $\frac{30\pi}{\sqrt{\sigma_{re}^2}} \frac{K'(ke)}{K(ke)}$ ond ke, & σ_{re} ore as above. K IS THE COMPLETE ELLIPTIC OF THE FIRS	$\begin{aligned} & \sigma_{er}^{+} = \sigma_{er} - \frac{0.7 \left(\sigma_{er} - 1\right) \text{T/W}}{\frac{K(1)}{K(1)} + 1.4 \frac{t}{w}} \\ & \text{T KIND, K'(k)} = K(k), \text{AND k'} = \{1 - k^2\}^{V_Z} \end{aligned}$
SLOTLINE W	WIDE SLOTS $0.2 \le W/h \le 1.0$ $Z_0 = 113.19 - 53.55 \log \sigma_r + 1.25 W/h \\ (114.59 - 51.88 \log \sigma_r) + 20 (W/h - 0.2) \\ (1 - W/h) \\ -[0.15 + 0.23 \log \sigma_r + W/h (0.79 \\ + 2.07 \log \sigma_r)] \\ \cdot [0.25 - 5 \log \sigma + W/h (2.1 - 1.42 \log \sigma_r) \\ - h \lambda_0 \times 10]^2$ $NARROW SLOTS 0.02 \le W/h \le 0.2 Z_0 = 72.62 - 35.19 \log \sigma \\ + 50 \frac{(W/h - 0.02)(W/h - 0.1)}{W/h} \\ + \log (W/h \times 10^2)(4.4.28 - 19.58 \log \sigma_r - 10.32 \log \sigma_r - 0.11 + W/h (1.07 \log \sigma_r + 1.44) \\ \cdot (11.4 - 6.07 \log \sigma_r - h/\lambda_0 \times 10^2)^2$	$e_{\rm et} = [0.937 - 0.483 \log W/h (0.111 - 0.0022 e_{\rm f}) - (0.121 + 0.094 W/h - 0.0032 e_{\rm f}) \log (h/\lambda_0 x 10^2)]^{-2}$ $e_{\rm et} = [0.923 - 0.448 \log e_{\rm f} + 0.2 W/h - (0.29 W/h + 0.047) \log (h/\lambda_0 x 10^2)]^{-2}$

FIG. 42-4 Stripline characteristics.

Microstrip is similar to a wire above ground that has been flattened. The field pattern is more complex, as only a part of it is in the dielectric sheet and the rest is in the air above the dielectric sheet. The other three are also mostly TEM, but their electric field is between the edges of the conductor pattern.

Coplanar strip is similar to two-wire line with flattened wires. It, too, is complex, with the fields partly in the dielectric and partly in the air above and below the sheet. The impedance is high because the capacity per unit length is low owing to the edge-to-edge position of the conductors.

Coplanar waveguide is really two coplanar strips in parallel. As might be expected, the impedance is lower for the same dimensions and dielectric. Slotline is similar to coplanar strips, with very wide conductor patterns.

The ranges of Z_0 available and the losses with the different types of strip transmission lines are compared in Table 42-2. These show that the microstrip and the coplanar waveguide are most useful for low-impedance circuits and that the slotline and coplanar strips are more appropriate for high-impedance circuits.⁵

The characteristics of microstrip are shown in Fig. 42-5. The dotted curve is the plot of Z_{0m}^a for airline. The solid curves are for finding the square root of the effective

TABLE 42-2 Comparison of Z_0 Limits and Loss for the Various Lines $(\epsilon = 10.0, h = 25 \text{ mil}, \text{ or } 0.635 \text{ mm}, \text{ and frequency} = 10 \text{ GHz})$

	Z ₀ ra	ange	Loss, d	B/cm
Transmission line	Minimum	Maximum	50	100
Microstrip Coplanar waveguide Slotline Coplanar strips	20 (m) 25 (m, d) 55 (d) 45 (m, d)	110 (d) 155 (m, d) 300 (m) 280 (m, d)	0.04 0.08* 0.15† 0.83*	0.14 0.28* 0.13*

NOTE: (m) = Z_0 limited by mode; (d) = Z_0 limited by small dimensions.

 $[\]dagger \epsilon = 16, Z_0 = 75 \Omega.$

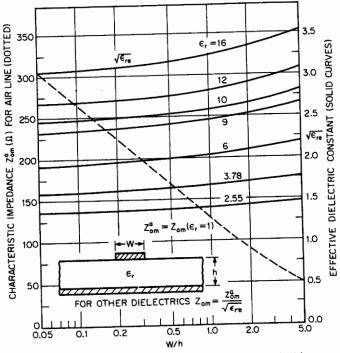


FIG. 42-5 Characteristic impedance and effective dielectric constant of microstrip lines.

dielectric constant. The Z_{0m} for other dielectrics is $Z_{0m}^a/\sqrt{\epsilon_{re}}$. Figure 42-6 shows the losses in microstrip on different substrates. Line wavelengths and characteristic impedance of coplanar strips and of coplanar waveguide are shown in Figs. 42-7 and 42-8. These same characteristics for slotline are shown in Fig. 42-9.

^{*}h/W = 2.

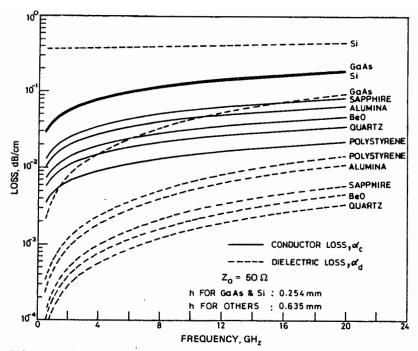


FIG. 42-6 Conductor and dielectric losses when microstrip is constructed on different substrates.

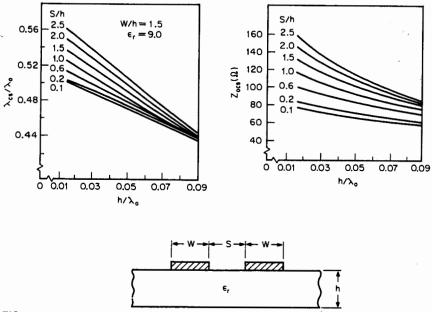


FIG. 42-7 Line wavelength and characteristic impedance of coplanar strips.

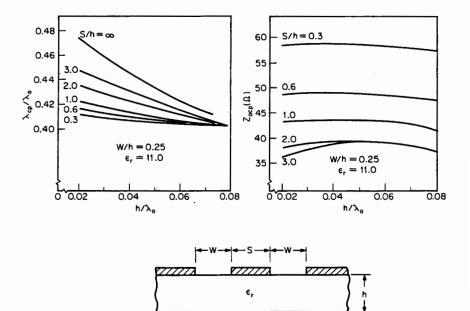


FIG. 42-8 Line wavelength and characteristic impedance of coplanar waveguide.

42-5 COAXIAL LINES: SOLID CONDUCTOR

Coaxial transmission lines using a cylindrical center conductor within a cylindrical tubular outer conductor are widely employed for the propagation of microwave power. Although more costly than open-wire transmission lines, they completely enclose the electromagnetic fields, preventing radiation losses and providing shielding from nearby circuits.

Coaxial-Line Parameters

For a coaxial line with inner-conductor diameter 2a and outer conductor diameter 2b, the characteristic impedance is

$$Z_0 = \frac{138}{\sqrt{\epsilon}} \log_{10} \frac{b}{a} \qquad \Omega$$

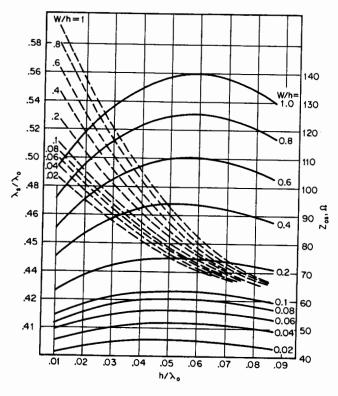
which is plotted in Fig. 42-1.

The cutoff wavelength of the first higher mode is²

$$\lambda_c = F\pi \sqrt{\epsilon} (a+b) \qquad F \cong 1$$

The conductor loss for the dominant mode is

$$\alpha_c = 1.14 \times 10^{-6} \quad \sqrt{\frac{f\epsilon}{\sigma}} \left(\frac{1}{a} + \frac{1}{b} \right) \frac{1}{\log_{10} \frac{b}{a}}$$
 Np/m



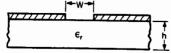


FIG. 42-9 Line wavelength and characteristic impedance of slotline.

The minimum conductor loss occurs at the limiting size for the first higher mode, in which case $\sqrt{\epsilon} Z_0 = 92.6 \Omega$ and

$$\alpha_c = 0.637 \frac{\epsilon}{\lambda_c \% \sqrt{\sigma}}$$
 Np/m

For a fixed outer-conductor size, the minimum conductor loss occurs for $\sqrt{\epsilon}$ Z_0 = 77 Ω and is

$$\alpha_c = 0.164 \frac{1}{b} \sqrt{\frac{\epsilon}{\sigma \lambda}} Np/m$$

The power transmitted by the line is

$$P = \frac{E_a^2 a^2 \sqrt{\epsilon}}{52.2} \log_{10} \frac{b}{a} \qquad W$$

where E_a is the electric field intensity at the center conductor (Sec. 42-1). The maximum power-handling capacity occurs for a 44.4- Ω line operating at the limit of the first higher mode and is

$$P_{\text{max}} = 6.53 \times 10^{-5} \frac{E_{\sigma}^2 \lambda_c^2}{\sqrt{\epsilon}} \quad \text{W}$$

For a fixed outer-conductor size, the maximum power-handling capacity occurs for $\sqrt{\epsilon}\,Z_0=30\,\Omega$ and is

$$P'_{\text{max}} = 1.53 \times 10^{-3} E_a^2 b^2 \sqrt{\epsilon}$$
 W

The effect of dimensional tolerances on the characteristic impedance may be found from

$$\frac{\Delta Z_0}{Z_0} = \frac{60}{Z_0 \sqrt{\epsilon}} \left(\frac{\Delta b}{b} - \frac{\Delta a}{a} \right)$$

while the effect of eccentricity is to change the characteristic impedance to

$$Z_0 = \frac{138}{\sqrt{\epsilon}} \log_{10} \left[\frac{b}{a} \left(1 - \frac{e^2}{b^2} \right) \right] \qquad \Omega \qquad \frac{e}{b} < \log_{10} \frac{b}{a} < 0.7$$

where e is the off-center distance.

For a balanced coaxial line (sheathed two-wire line) having two center conductors spaced at a distance s within a single outer conductor, the characteristic impedance is given by

$$Z_0 = \frac{276}{\sqrt{\epsilon}} \log_{10} \left(\frac{s}{a} \frac{4b^2 - s^2}{4b^2 + s^2} \right) \qquad \Omega$$

Coaxial Line with Helical Center Conductor

Coaxial lines with a helical inner conductor are sometimes useful to obtain a high characteristic impedance or slow propagation velocity. Design relations are given in Ref. 6.

Coaxial Line, Bead-Supported

In order to support the center conductor of an air-dielectric coaxial line, insulating beads are often used. These beads will introduce discontinuities and, if not properly designed, produce large reflection losses. The design procedure for these support beads depends upon the frequency range of application, a broad range requiring a more complex design. The more common procedures are summarized in Fig. 42-10, and others can be found in the references.⁷

In the bead-supported line, the cutoff wavelength in the bead section should be kept below the operating wavelength. The power-handling capacity is about 0.033 times that of the theoretical maximum for the unsupported line.

Coaxial Line, Stub-Supported

In many applications, particularly when high power is to be transmitted, it is desirable to support the center conductor of an air-dielectric coaxial line by means of stubs. The

TYPE	CONFIGURATION	DESIGN FORMULAS	REMARKS
I. HALF WAVE		$S = \frac{\lambda}{2\sqrt{\epsilon}}$	FREQUENCY-SENSITIVE
2. SPACED PAIR		$S = \frac{1}{\beta} \arctan \left[\frac{2\sqrt{\epsilon}}{1+\epsilon} \cot \beta \ell \sqrt{\epsilon} \right]$ $\beta = \frac{2\pi}{\lambda}$	FREQUENCY-SENSITIVE
3. SIMPLE UNDERCUT		$a' = b \left(\frac{b}{a}\right)^{-\sqrt{a}}$	GOOD AT LOW FREQUENCY. NEGLECTS FRINGING CAPACITANCE AT UNDERCUT.
4. COMPENSATED UNDERCUT	4, Z ₀₈	$\mathbf{I} = \frac{1}{\beta} \arctan \left[\frac{2\omega C Z_{OB}}{(\omega C Z_{OB})^2 + \left(\frac{Z_{OB}}{Z_O}\right)^2} \right]$ $\beta = \frac{2\pi\sqrt{4}}{\lambda}$	COMPENSATES FRING- ING CAPACITANCE AT UNDERCUT. MATCH AT I f= \(\omega / 2\pi, \) LOW REFLEC- TION AT LOWER FRE- QUENCIES.
5. COMPOUND UNDERCUT (REF. 4)	Z ₀	$\sqrt{L/C} = Z_0$ $L = \frac{138 \cancel{L}'}{v} \log_{10} \frac{b'}{a'}$ FIND a' AS IN 3) ABOVE $v = 3 \times 10^8 \text{ m/s}$	VERY LOW REFLECTION IF DISCONTINUITIES ARE OF INFINITESIMAL EX- TENT (1/2 × 1/20), GOOD WHERE MANY BEADS MUST BE USED.

FIG. 42-10 Coaxial-line beads. Capacitive discontinuities at an abrupt change in diameter (as in items 4 and 5) can be found from this curve if the discontinuities are separated by at least the space between the inner and outer conductors in the intervening line. If the ratio of the inner and outer conductors is less than 5 before and after the discontinuity, the curves are accurate to better than 20 percent.

power-handling capacity of a stub-supported line is about 0.15 times that of the theoretical maximum for the unsupported line. Such stubs take the form of a short length of short-circuited transmission line in shunt with the main transmission line. For frequencies at which the stub is an odd number of quarter wavelengths long, it presents zero admittance and therefore does not affect the main line. Obviously, it is often necessary to maintain a low stub admittance over a broad range of frequencies, and this may be effected by using an impedance transformer on the main line at the junction with the stub. The design of stubs and transformers can be found in the literature.⁷

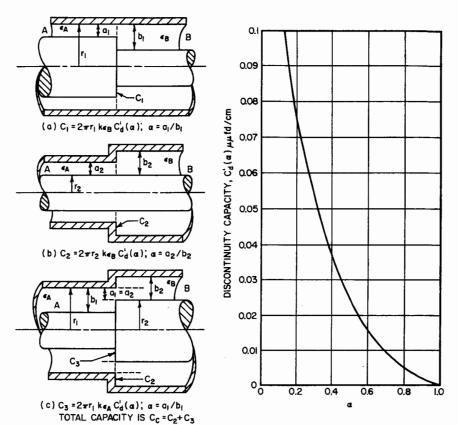


FIG. 42-10 (Continued)

Semiflexible Coaxial Lines

There are several commercially available coaxial lines having a limited permissible bending radius but exhibiting a loss only slightly greater than that of rigid coaxial lines. They are characterized by a helical-, ribbed-, or foamed-dielectric support for a copper center conductor and a solid copper or aluminum tube for the outer conductor. A number of these have been qualified as MIL spec. components and are becoming more widely used. They are useful where their greater mechanical stability permits good phase matching and control in critical RF circuits.

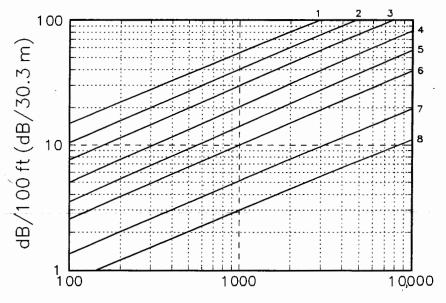
42-6 FLEXIBLE COAXIAL LINES

Flexible coaxial line using a solid or stranded inner conductor, a plastic-dielectric support, and a braided outer conductor is probably the most common means of connecting

together many separated components of a radio-frequency system. Although the transmission loss is relatively high because of the dielectric loss, the convenience often outweighs this factor in applications for which some loss is tolerable. Such lines are commercially available in a wide variety of size and impedance.

Table 42-3 summarizes the characteristics of the more common lines. The attenuation is shown in Fig. 42-11, and the power-handling capacity in Fig. 42-12.

Leakage of electrical energy through the braided outer conductor is sometimes a problem. The amount of leakage has been evaluated in two ways. One is to measure the equivalent coupling impedance to the outside environment, often another cable. 9,10 Typical coupling impedance for an M17/74 cable has been reported as 150 $\mu\mu$ h/ft from 100 to 5500 MHz. The other is to measure the shielding factor of the cable as the decibel loss through the cable-shielded braid. 11,12 The coupling loss increases linearly with length (and the shielding decreases with length) and increases slightly at higher frequencies, where the openings between wires in the shield braid become a bigger part of a wavelength. Single-braid cable typically provides 30- to 40-dB shielding from 1 ft of cable. For longer lengths shielding in decibels is reduced by 20 log (length in feet). Double-braid cable



Frequency, MHz

```
Curve 1: 154
2: 93, 119, 131, 151, 152
3: 113, 138, 153
4: 28, 54, 94, 126, 133, 134, 136, 139, 183, 187
5: 29, 60, 84, 95, 128, 137, 194
6: 2, 30, 47, 73, 75, 110, 111, 112, 116, 130, 150, 184, 185, 188, 191
7: 6, 16, 24, 31, 52, 56, 62, 65, 74, 77, 78, 86, 87, 90, 92, 97, 100, 127, 129, 135, 181, 189, 190, 192, 193
8: 64, 67, 72, 79, 81
```

FIG. 42-11 Approximate attenuation of flexible coaxial lines. (M17 numbers are indicated on each curve.)

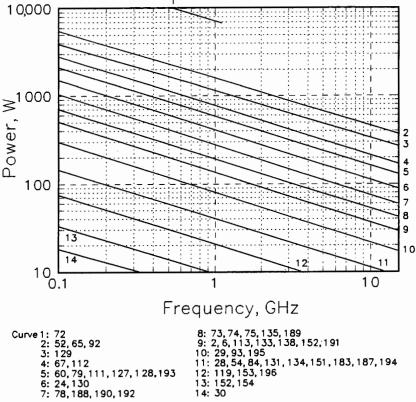


FIG. 42-12 Approximate power-handling capacity of flexible coaxial lines (M17 numbers are indicated for each curve). Conditions are the following: ambient temperature 40°C, sea level, center conductor is 80°C for polyethylene and 200°C for PTFE.

provides 60 to 80 dB. Special braid of flat metal strip provides 80 to 90 dB. Semirigid lines which have a solid sheath provide from 300 to several thousand decibels at the higher frequencies, where the skin depth becomes very small and the field inside penetrates to only a small part of the solid metal sheath.

Frequently used cable connectors are listed in Table 42-4.

42-7 HOLLOW-TUBE WAVEGUIDES

Propagation

Electromagnetic energy can be propagated down hollow metal tubes if the tubes are of sufficient size and are properly excited. The size of the tubes required usually limits their use to the very-high frequency (VHF) region or above.

The energy can be propagated in a number of different types of waves as described below. In the usual case, waveguide devices are designed for transmission of a single wave type (most often the dominant wave or that having the lowest cutoff frequency) because the design problems are very greatly simplified.

TABLE 42-3		Flexible Coaxial Lines	al Lines									
M17 Number	Inner con- ductor, in (cm)	Diame ter, die Dielec-tric, in tric (cm)	-jec	Number and type of shield braid	Jacket material	Outer Weig diame-lb/ft ter, in (kg/ (cm) m)	ħ,	Nomi- nal imped- ance, Ω	<u>(CS</u> 1	9 .	Maximum operating ating volts,	Comments
2-RG6	0.0285 CCS (0.0724)	PE	0.185 (0.469)	2: inner SC, outer BC	PVC-IIA	0.332 (0.843)	0.082 (0.122)	75.0	20.6 (67.6)	-40 +85	3,000	3,000 Use to 3 GHz; NHLS/180- 00001
6-RG11	0.0477 (0.121) 7/0.0159 TC	PE	0.285 (0.724)	1: BC	PVC-IIA	0.405	0.098 (0.143)	75.0	20.6 (67.6)	- 40 + 80	2,000	5,000 Use to 1 GHz; NHLS/181- 00001;
15-RG22	2 × 0.0456 (0.116) 7/0.0152 BC	PE	0.285	2: TC	PVC-IIA	0.420 (1.067)	0.134	95.0	16.0 (52.5)	-40 +85	1,000	armored/6- RG12; high temp 62-RG144 1,000 Balanced; use to 200 MHz; NHLS/182- 00001;
16-RG23	2 × 0.0855 (0.217) 7/0.0285 BC	2 PE	0.380	2: separate PVC-IIA inner com. outer BC	PVC-IIA	0.945 (2.400)	0.530	125.0	12.0 (39.4)	-40 +85	7,000	armored/15- RG111; NHLS/ 182-00002 7,000 Balanced; dual coaxial; use to 1 GHz; armored/ 16-RG24

-40 10,000 Triaxial pulse; use +90 to 1 MHz; armored/21- RG26	15,000 Coaxial pulse; use to 1 MHz; armored/22-RG27	15,000 Triaxial pulse; use to 1 MHz	6,500 Use to 1 GHz	1,900 SW; use to 1 GHz; NHLS/ 183-00001; NS/ 155-00001; NHLS/197-	2,300 Use to 1 GHz; NHLS/184-	1,000 Use to 1 GHz; NHLS/185-	1,000 Use to 1 GHz; armored/31- RG79
- + 90 + 90	-40 +85	- 40 + 85	- 40 + 85	- 40 + 85	-40 +85	- 40 + 80	- 40 + 80
50.0 (164.1)	55.0 (180.5)	50.0 (164.1)	20.6 (67.6)	30.8 (101.1)	20.6 (67.6)	13.5 (44.3)	(32.8)
48.0	48.0	48.0	75.0	20.0	75.0	93.0	125.0
0.205 (0.305)	0.300 (0.491)	0.400	0.231 (0.344)	0.026	0.035	0.038 (0.057)	0.085 (0.131)
0.505 (1.283)	0.595 (1.511)	0.735 (1.867)	0.630 (1.600)	0.195	0.242 (0.615)	0.242 (0.615)	0.405
Rubber- IV	Rubber- IV	Rubber- IV	PVC-IIA	PVC-IIA	PVC-IIA	PVC-IIA	PVC-IIA
2: TC	1: TC	2: TC,GS Rubber-IV	1: BC	1: TC	1: BC	1: BC	1: BC
0.288 (0.732)	0.455	0.455	0.460 (1.168)	0.116 (0.295)	0.146 (0.371)	0.146 (0.371)	0.285 (0.724)
Rubber E	Rubber D	Rubber D	PE	PE	PE	Air and PE	Air and PE
0.0585 (0.149) 19/0.0117 TC	0.0925 (0.235) 19/0.0185 TC	0.0925 F	19/0.0185 TC 0.0747 (0.190)	7/0.0249 BC 0.0355 (0.090) 19/0.0072 TC	0.0226 CCS (0.057)	0.0253 CCS (0.064)	0.0253 CCS (0.064)
19-RG25	22-00001	23-RG28	24-RG34	28-RG58	29-RG59	30-RG62	31-RG63

TABLE 42-3 Flexible Coaxial Lines (Continued)

Number Com Pielec-tric, in shield Jacket Hor, in (kg/ diame-lb/ft aliame-lb/ft aliame-lb/ft aliame-lb/ft aliame-lb/ft aliame-lb/ft aliame-lb/ft aliameter Cm) Dielec-tric, in shield backet Hor, in (kg/ diame-lb/ft aliameter) John 17											Maxi-	Maxi.	
Tric Cem Shield Jacket Iter, in Shield Jacket Iter, in Iter, in Shield Jacket Iter, in Iter, in				Diame-	Number and		Outer	ght,	÷	Nomi- Nominal mum nal capaci- temp-		mum oper-	
Rubber 0.288 2: TC Rubber- 0.460 0.220 D (0.782) I: BC PVC-IIA 0.405 0.110 PE 0.285 I: BC PVC-IIA 0.235 0.1164 PE 0.079 I: TC PVC-IIA 0.235 0.035 Air and 0.285 I: BC PVC-IIA 0.405 0.089 PE 0.724) I: BC FG braid- 0.465 0.228 PTFE 0.332 2: BC FG braid- 0.465 0.228 PE 0.096 I: TC PVC-IIA 0.160 0.021 PE 0.096 I: TC PVC-IIA 0.160 0.021			Dielec- tric	ter, dielec- tric, in (cm)	type of shield braid	Jacket material	ہ د		imped- tance, ance, pF/ft Ω (pF/m)	tance, pF/ft (pF/m)	erature range,	ating volts, rms	Comments
PE 0.285 I: BC PVC-IIA 0.405 0.110 (0.724) I: TC PVC-IIA 0.235 0.035 (0.201) I: TC PVC-IIA 0.235 0.035 (0.052) PTF 0.332 2: BC FG braid- 0.465 0.228 (0.843) PF (0.244) I: TC PVC-IIA 0.465 0.228 (0.843) PF (0.244) I: TC PVC-IIA 0.160 0.021 (0.244) I: TC PVC-IIA 0.160 0.021		0.0585	Rubber D		2: TC	Rubber- IV	0.460	0.220	48.0	55.0	- 40 + 85	10,000	10,000 Coaxial pulse; use
PE 0.079 1: TC PVC-IIA 0.235 0.035 (0.201) Air and 0.285 1: BC PVC-IIA 0.405 0.089 (0.184) PTFE 0.332 2: BC FG braid- 0.465 0.228 (0.843) PE 0.096 1: TC PVC-IIA 0.405 (0.031)		19/0.0117 TC 0.0080	ᅙ	0.285	1: BC	PVC-IIA	0.405	0.110	950	48.0	-40	1,500	1.500 Coaxial time
PE 0.079 1: TC PVC-IIA 0.235 0.035 (0.201) Air and 0.285 1: BC PVC-IIA 0.405 0.089 PE (0.724) (0.843) PTFE 0.332 2: BC FG braid- 0.465 0.228 (0.843) PE 0.096 1: TC PVC-IIA 0.160 0.021 (0.244)		(0.020) 0.128-		(0.724)			(1.029)	(0.164)		(157.5)	08+		delay; use to 5 MHz
PE 0.079 1: TC PVC-IIA 0.235 0.035 Air and (0.285) 1: BC PVC-IIA 0.405 0.089 PF (0.724) 1: BC PVC-IIA 0.405 0.089 PTFE (0.332) 2: BC FG braid- 0.465 0.228 (0.843) 2: BC FG braid- 0.465 0.228 PE (0.244) 1: TC PVC-IIA 0.160 0.021 PE (0.244) 1: TC PVC-IIA 0.160 0.021		diameter								_			
Air and 0.285 1: BC PVC-IIA 0.405 0.089 PF (0.724) 2: BC FG braid- 0.465 0.228 (0.843) 2: BC FG braid- 0.465 0.228 (0.843) PF (1.181) (0.340) PF (0.244) 1: TC PVC-IIA 0.160 0.021	45-RG108	2×0.0378	PE		1: TC	PVC-IIA	0.235	0.035	78.0	9.61	-40	1,000	1,000 Balanced line; use
Air and 0.285 1: BC PVC-IIA 0.405 0.089 PE (0.724) (1.029) (0.133) PTFE 0.332 2: BC FG braid- 0.465 0.228 (0.843) V (1.181) (0.340) PE 0.096 1: TC PVC-IIA 0.160 0.021		(0.096)		(0.201)			(0.597)	(0.052)		(64.3)	+85		to 10 MHz;
Air and 0.285 1: BC PVC-IIA 0.405 0.089 PE (0.724) 1: BC FC braid- 0.465 0.228 (0.843) 2: BC FG braid- 0.465 0.228 V (1.181) (0.340) PE 0.096 1: TC PVC-IIA 0.160 0.021		7/0.0126 TC						-		_			NHLS/186- 00001
(0.018) PE (0.724) (1.029) (0.133) (0.133) (0.218) (0.259) (0.133) (0.244) (0.0086 II: TC PVC-IIA (0.406) (0.031) (0.0078) (0.244) (0.244)	47-RG114		Air and	0.285		PVC-IIA		0.089	185.0	6.5	-40	1,000	1,000 Low capacitance;
0.1019 BC PTFE 0.332 2: BC FG braid- 0.465 0.228 (0.259) (0.843) V (1.181) (0.340) (0.0300 PE 0.096 1: TC PVC-IIA 0.160 0.021 (0.078) (0.244) (0.244)		(0.018)	E	(0.724)				(0.133)		(21.3)	8 +		use to 1 GHz
(0.259) (0.843) V (1.181) (0.340) 0.0300 PE 0.096 1: TC PVC-IIA 0.160 0.021 27/0.0050 TC (0.244) (0.244)	52-RG119	0.1019 BC	PTFE	0.332		FG braid-		0.228	20.0	29.4	-55	000,9	6,000 SW; use to 3
0.0300 PE 0.096 1: TC PVC-IIA 0.160 0.021 (0.078) (0.244) (0.244)		(0.259)		(0.843)		>	_	(0.340)		(96.5)	+200		GHz; NS/156-
0.0300 PE 0.096 1: TC PVC-IIA 0.160 0.021 (0.078) (0.244) (0.244) (0.406) (0.031)	_												00001
0.0300 PE 0.096 1: TC PVC-IIA 0.160 0.021 (0.078) (0.244) (0.244) (0.406) (0.031)													armorea/32- RG120
i0 TC (0.244) (0.406)		0.0300	PE			PVC-IIA	091.0	0.021	20.0	30.8	-40	1,900	1,900 SW; use to 1
27/0.0030 1C		(0.078)		(0.244)			(0.406)	(0.031)		(101.1)	+82		GHz; NHLS/
		2//0.0050 IC											187-00001; NS/
									-	-			157-00001;
				-									NHLS/198-

3,000 Use to 200 MHz; armored/56- RG131	1,900 SW; use to 8 GHz; NS/158-	10,000 Use to 1 GHz; armored/64- RG35	2,500 SW; use to 3 GHz; armored/ 65-RG166; NSA150-00001	11,000 SW; use to 5.6 GHz; NS/160-	7,000 SW; use to 1 GHz; NS/161- 00001	3,000 SW; use to 10 GHz; NHLS/ 188-00001; NS/ 162-00001; NHLS/199- 00001
+ 85	-55 +200	-40 +85	-55 +250	-40 +85	-55 +250	-40 +85
16.3 (53.5)	29.4 (96.5)	20.6 (67.6)	29.4 (96.5)	30.8 (101.1)	29.4 (96.5)	30.8 (101.1)
95.0	50.0	75.0	50.0	20.0	50.0	50.0
0.300 (0.447)	0.043	0.505 (0.752)	0.121	0.520 (0.774)	0.516 (0.769)	0.089
0.625 (1.588)	0.195 (0.495)	0.870 (2.210)	0.410 (1.041)	0.895 (2.273)	0.730 (1.854)	0.332 (0.843)
PVC-IIA	FEP	PVC-IIA	FG braid-V	PVC-IIA	FG braid- V	PVC-IIA
l: TC	2: SC	1: BC	1: SC	2: SC	1: BC	SC SS
0.472 (1.199)	0.116 (0.295)	0.680	0.285 (0.724)	0.680	0.620 (1.575)	0.185
PE	PTFE	PE	PTFE	PE	PTFE	PE
2 × 0.0855 (0.217)	60-RG141 0.0370 SCCS F (0.099)		64-RG165 0.0960 (0.244) 7/0.0320 SC			
56-RG130	60-RG141	64-RG164 0.1045 BC (0.265)	64-RG165	67-RG177 0.195 BC (0.495)	73-RG211 0.1920 BC (0.4877)	73-RG212 0.0556 SC (0.1412)

TABLE 42-3 Flexible Coaxial Lines (Continued)

M17 Number	Inner con- ductor, in	Dielec-	Diame- ter, dielec- Dielec-tric, in	Number and type of shield	Oute diam Jacket ter, in	796	ght,	ë, ed-	<u>. a</u>	2 .		
١.	0.0888	DE CO	385	\top	DVC IIA	1		200	_ [ء د		Comments
	(0.2256) 7/0.0296 BC		(0.724)		VIII S	(1.029)	(0.165)	0.00	30.8 (101.1)	+ 85	000,	5,000 SW; use to 1 GHz; armored/ 74-RG215:
•												NHLS/189-
												00001; NHLS/
75-RG214	0.0888	PE	0.285	2: SC	PVC-IIA	0.425	0.130	50.0	30.8	-40 +85	2,000	5,000 SW; use to 10
	7/0.0296 SC		((1.000)	(6.154)		(101.1)	6		75-RG365; NS/
												164-00002; NS/
77-RG216	0.0477	PE		2: BC	PVC-IIA	0.425	0.124	75.0	20.6	-40	2,000	5,000 Use to 3 GHz;
	(0.1212) 7/0.0159 BC		(0.724)			(1.080)	(0.185)		(9.79)	+82		NHLS/191-
78-RG217	0.106 BC	PE		2: BC	PVC-IIA	0.545	0.225	20.0	30.8	~40	7,000	7,000 SW: use to 3
	(0.269)		(0.940)			(1.384)	(0.299)		(101.1)	+82		GHz; NS/165-
												00001; armored/165-
												00002; NHLS/
79-RG218	0.195 BC	PE	0.680	1: BC	PVC-IIA	0.870	0.510	50.0	30.8	-40	1000	192-0001
	(0.495)		(1.727)			(2.210)	(0.760)		(101.1)	+85		GHz; NHLS/
												193-00001;
												armored//9-
			_									103 00003

				_				
14,000 Use to 1 GHz; armored/81-	1,900 SW; use to 12.4 GHz; NHLS/ 194-00001; NS/ 167-00001; NHLS/200- 00001	5,000 Armored/86- 00002	1,000 Use to 1 GHz; NHLS/195- 00001	5,000 SW; use to 12.4 GHz, w FEP jacket MS17/92- 00001; NS/168- 00001	1,000 SW; use to 3 GHz; high temp/93-00001, NS/169-00001	1,200 Use to 3 GHz; 95 \Omega 95-RG180	1,000 Use to 3 GHz	5,000 Use to 3 GHz
14,000	006'1	2,000	1,000	2,000	1,000	1,200	1,000	2,000
-40 +85	- 40 + 85	-55 +200	- 55 + 85	-55 +200	-55 +200	-55 +200	-55 +200	-40 +85
30.8 (101.1)	30.8 (101.1)	29.4 (96.5)	13.5 (44.3)	29.4 (96.5)	29.4 (96.5)	(64.0)	13.5	16.3
90.0	50.0	50.0	93.0	50.0	50.0	75.0	93.0	95.0
0.820 (1.221)	(0.061)	0.195	0.050 (0.075)	0.185 (0.276)	0.0060	0.010	0.050	
(2.845)	(0.539)	0.430 (1.092)	0.245 (0.622)	0.415 (1.054)	(0.180)	0.100 (0.254)	0.242	0.405
PVC-11A 1.120 (2.845)	PVC-IIA	FG braid- V	РЕ-ША	FG braid-V	FEP-IX	FEP-IX	FG braid- V	PVC-IIA
1: BC	2: SC	2: SC	2: TC	5: SC	1: SC	1: SC	1: SC	1: BC
0.910 (2.311)	0.116	0.285	0.146 (0.371)	0.255	0.033	(0.160)	0.146	
<u> </u>	E	PTFE	Air and PE	Taped PTFE	PTFE	PTFE	Air and	PE
0.260 BC 0.660	0.035 SC (0.089)	0.0936 (0.238)		0.0840 (0.213)	0.0120 (0.030) 7/0.0040	0.0120 (0.0305) 7/0.0040 SCCS	0.0253 SCCS	100-RG133 0.0252 BC PE (0.064)
81-00001	84-RG223	10000-98	90-RG71	92-RG115	93-RG178	94-RG179	95-RG210	100-RG133

	Comments	3 GHz	3 GHz	V; use to 3 GHz; NS/170-	00001 V; use to 8 GHz; NS/171-	00001 N; use to 3 GHz; NS/172- 00001	ı GHz	V; use to 1 GHz; NHLS/ 196-00001; NS/	173-00001 e to 3 GHz	1 GHz
		3,000 Use to 3 GHz	2,300 Use to 3 GHz	1,900 SW; use to	S	5	1,000 Use to 1 GHz	1,500 SW; use to 1 GHz; NHI 196-00001	173-00001 15,000 Use to 3 GHz	15,000 Use to 1 GHz
	Maxi- mum oper- ating volts,	3,000	2,300	1,900	3,000	1,200	1,000	1,500	15,000	15,000
	Maxi- mum temp- erature range,	-55 +200	- 55	-55 +200	-55 +200	-55 +200	- 55 + 80	- 40 + 85	-55 +85	- 10 + 90
	Maxi- Nomi- Nominal mum nal capaci- temp imped-tance, eratu ance, pF/ft range Ω (pF/m) °C	29.4	19.5	(96.5)	29.4 (96.5)	29.4 (96.5)	16.9	30.8 (101.1)	85.0 (278.9)	50.0 (164.1)
		20	75.0	50.0	50.0	50.0	75.0	50.0	25.0	50.0
	Weight, Ib/ft (kg/ m)	0.056	0.031	0.031	0.094 (0.140)	0.012 (0.018)	0.080	0.009 (0.013)	(2.186)	0.353 (0.524)
	- <u>4</u> -	0.245	0.206	0.170	0.280 (0.711)	0.098	0.265 (0.673)	0.110 (0.279)	1.460 (3.708)	0.700
	Oute diam Jacket ter, i material (cm)	FEP-IX	FEP-IX	FEP-IX	FEP-IX	FEP-IX	PE-IIIA	PVC-IIA	Neoprene	GS neo- prene
ntinued)	Number and type of shield braid	1: HR	1: SC	1: SC	2: SC	1: SC	2: SC PUR inter-	layer 1: TC	3: TC, GS, TC	3: TC, TC GS neoprene
Flexible Coaxial Lines (Continued)	Numbe Diame- and ter, dielec- type of tric, in shield (cm) braid	0.185	0.146	0.116	0.185 (0.470)	0.060 (0.152)	0.146 (0.371)	0.060	1.065 (2.705)	0.380 (0.980)
e Coaxi	Diame ter, die Dielec-tric, in tric (cm)	PTFE	PTFE	PTFE	PTFE	PTFE	Foam PE	PE	Rubber H,J,H	TC rubber H,J,H
	Inner con- ductor, in (cm)	0.0009	110-RG302 0.0250 SCCS (0.064)	111-RG303 0.0370 SCCS (0.094)	112-RG304 0.0590 SCCS (0.150)	0.0201 (0.051) 7/0.0067 SCCS	116-RG307 0.0290 11 (0.074) 19/0.0058 SC	0.0189 (0.048) 7/0.0063 CCS	0.4850 TC braid	
TABLE 42-3	M17 Number	109-RG301 0.0009	110-RG302	111-RG303	112-RG304	113-RG316 0.0201 (0.051) 7/0.006	116-RG307	119-RG174 0.0189 (0.048) 7/0.006	124-RG328 0.4850 TC braid	125-RG328 0.0585 (0.1486) (19/0.0117

5,000 Use to 1 GHz; armored/126- RG392	2,500 SW; use to 11 GHz; NS/174- 00001	1,900 SW; use to 12.4 GHz; NS/175- 00001	1,000 SW; triaxial; use to 10 GHz	1,000 Use to 1 GHz	1,900 SW; water- blocked; blocked;	5,000 SW; water-blocked; triaxial; use to 3 GHz; nonWB	5,000 SW; water- blocked: triaxial; use to 3 GHz; nonWB M17/135- 00004
-40 +85	-55 +200	-55 +200	-55 +200	-40 +200	-40 +70	-40 +70	- + 70 + 70
23.0 (75.5)	29.4 (96.5)	29.4 (96.5)	29.4 (96.5)	30.4 (99.7)	30.8 (101.1)	30.8 (101.1)	30.8 (101.1)
72.0	20.0	50.0	50.0	20.0	90.0	50.0	50.0
0.100 (0.148)	0.175 (0.261)	0.050 (0.075)	0.015 (0.022)	0.018 (0.027)	0.045 (0.067)	0.160	0.185
	0.390 (0.991)	0.195 (0.495)	0.116 (0.295)	0.071	0.245 (0.622)	0.500	0.500
PUC-IIA 0.405 (1.029)	FEP-1X	FEP-1X	FEP-1X	FEP-1X	PE-IIIA	PUR	PE-IIIA
1: TC P	2: SC F	2: SC	2: SC FEP inter-	layer 1: SC FE inter-	layer 2: SC PE inter-	2: SC PE interlayer	2: SC PE interlayer
0.295 1	0.285 (0.724)	0.116 (0.294)	0.033	0.033		0.285	0.285
Cond PE	PTFE	PTFE	PIFE	PTFE Cond.	PTFE PE	E .	BE
	0.094 SC 0.239)	7/0.312 0.0384 SC (0.0975)	0.012 SCCS	7/0.004 0.012 SCCS	7/0.004 PTFE 134-00001 0.033 SC PE (0.083)	0.088 SC (0.224) 7/0.0296	0.081 SC (0.207)
126-RG391 0.0477 (0.1212)	127-RG393 0.094 SC (0.239)	7/0.312 128-RG400 0.0384 SC F (0.0975)	131-RG403	132-RG404	134-00001	135-00001	135-00003

TABLE 42-3 Flexible Coaxial Lines (Continued)

M17 Number	Inner con- ductor, in (cm)	Diame ter, die Dielec-tric, in tric (cm)	- - 6	Number and type of shield braid	Jacket	- 6 -	jt.	ni- ed-	<u>. 20</u>	Maxi- Maximum mum mum temp- oper- erature ating range, volts.	Maxi- mum oper- ating	
136-00001	0.012 SCCS	PTFE	0.063	5		(call)	(III	3		ပ္	TE S	Comments
	(0.030)		_	ر ا	FFA-XIII	0.100	(0.0181)	75.0	19.5 (64.0)	- 55	1,200	1,200 Use to 3 GHz
13/-0000	13/-00001 0.012 SCCS (0.030) 7/0.004	PTFE	0.102	I: SC	PFA-XIII	0.141	0.020 (0.0297)	95.0	15.4 (50.5)	55 + 200	1,500	1,500 Use to 3 GHz
138-00001	0.020 SCCS (0.051) 7/0.0067	PTFE	0.060 (0.152)	l: SC	PFA-XIII	0.098 (0.249)	0.012 (0.1810)	50.0	29.4	-55	1,500	1,500 SW; use to 3 GHz
139-00001	0.012 SCBerC (0.030)	PTFE	0.102 (0.259)	1: SC F	PFA-XIII	0.141	0.0178	95.0	15.4 (50.5)	-55 +200	1,500	1,500 Use to 3 GHz
152-00001	0.020 SCCS (0.0511)	PTFE	0.060 2: (0.152)	2: SC F	FEP-IX	0.114 (0.289)	0.0185	50.0	29.4	-55	1,200	1,200 SW; use to 12.4
176-00002	2 cond. 19 0.0235 SCBerC (0.597)	TEE	0.042 1: (0.107) SC	1: SCBerC	PFA-XIII	0.129 (0.328)	0.018 (0.267)	77.0	24.0 (78.8)	-55 +200	000,1	1,000 Use to 10 MHz
177-00001	177-00001 19/0.005 PTFE (0.031) 7/0.004	TFE	0.102 2: (0.259) FE	2: SC FT FEP inter- layer	FEP-IX (0.184 (0.467)	0.034	95.0	15.4 (50.5)	-55 +200	1,500 [[1,500 Use to 3 GHz

-55 1,500 Use to 3 GHz								-55 1,200 Use to 3 GHz							
1,500 1								1,200							
-55	+150							-55	+150						
	(50.5)							19.5	(64.0)			,			
95.0								75.0							
0.020	(0.029)							0.010							
0.305	(0.775) (0.029)							0.240	(0.610)						
SC: NC:	poly-	ester	CPC tape	braid	NC FEP	inter-	layer	SC: NC:	poly-	ester	CPC tape	braid	NC: FEP	inter-	layer
	(0.259)							0.063							
PTFE								PTFE							
0.012 SCCS	(0.031)	7/0.004						0.012 SCCS	(0.031)	7/0.004					
178-00001								179-00001							

Abbreviations:

Dielectric

PIB = polyisobulylene, Type B per MIL-C-17 PTFE = solid polytetrafuoroethylene PE = solid polyethylene Rubber per MIL-C-170 SIL = silicone rubber PS = polystyrene

Conductors and braid materials

SC = silver-covered copper CCS = copper-covered steel TC = tinned copper BC = bare copper

SCCadBr = silver-covered cadmium bronze GS = galvanized steel

SCCS = silver, copper-covered steel

CPC = copper polyester copper laminate TCCS = tinned copper-covered steel NC = nickel-covered copper SSC = silver-covered strip

Jacket material

PVC-IIA = black polyvinylchloride, noncontaminating, Type IIA, per MIL-C-17E PVC-11 = gray polyvinylchloride, noncontaminating, Type II, per MIL-C-17E PVC-1 = black polyvinylchloride, contaminating, Type I, per MIL-C-17E

PE-IIIA = high-molecular-weight black polyethylene, Type IIIA, per MIL-C-17E PE-III = clear polyethylene

FEP-IX = fluorinated ethylene propylene, Type IX, per MIL-C-17E FG braid-V = fiberglass-impregnated, Type V, per MIL-C-17E PUR = polyurethane, black specific compounds

SIL/DAC-VI = dacron braid over silicon rubber, Type VI, per MIL-C-17E

XLPE = cross-linked polyolefin Rubber per MIL-C-17E

Comments

SW indicates spec. requirement for swept frequency attenuation and SWR testing.

NS/ indicates the M17 number for the unswept version of the same cable (recommended only to 400 MH: NHLS/ indicates similar cable for nonhalogen, low-smoke environments (uses cross-linked polyolefin jack Armored/ indicates the M17 number for the same cable with armor.

TABLE 42-4 Characteristics of Frequently Used Cable Connectors

		BNC	TNC	C	SC	N
Cable size, ou	iter	in 0.150			0.300-	0.330-0.55
diameters		0.250 cm 0.381	0.381 - 0.63 l-	35 0.550 0.762-	0.550 0.762-	0.762-1.40
Coupling type		0.635		1.40	1.40	
Bayonet	•	В		В		
(quick disconnec	et)	-		ь		
Screw Maximum			7/16-28		11/16-24	5/8-24
operating vo	1te	500	500	1000	1500	1000
Frequency	113	4	11			
range, GHz.		7	11	11	11	11
DC to -						
RF leakage, dl		-55	-60	-55	-90	-90
Insertion loss, of At GHz	1B	0.2	0.2	0.5	0.15	0.15
		3	3	10	10	10
Cable type	s Use	UG-	M39012/	UG-	M39012/	UG-
M17/28,	Plug (m)	88/U	26-0001			
111,	Plug, right-angle	913/U	30-0001			
	Cable jack (f)	89/U	27-0001			
04	Panel jack (f)	262/U	29-0001		Flange	
		909/U	28-0001	704C/U	nut	
M17/29,	Plug (m)	260/U	26 0000			
, ,	Plug, right-angle	200/0	26-0002 30-0002			
90, (Cable jack (f)	261/U	27-0002			
110, 1	Panel jack (f)	291/U	29-0002		Flange	
97		910/U	28-0002	631B/U	nut	
F	anel jack (f)	290/U	32-0001	Flange		
		625/U	31-0001	nut		
M17/17,* P	lug (m)			626C/U	25 0001	
73, P	lug, right-angle			71 0C/U	35-0001 39-0001	18/U
112 C	able jack (f)			633B/U	39-0001	20/11
P	anel jack (f)		Flange	629B/U	1	20/U 59 B /U
					40-0001	יושיט
M17/74, P	ug (m)				35-0002	21 /11
75, C	able jack (f)			572B/U	JJ-000Z	21/U 23/U
77, Pa	inel jack (f)			571B/U	14	23/U 60C/U
			_			594/U
Pa	nel jack (f)		Flange	568A/U 4	1-0001	58/U
				706D /11		,
			nut	706B/U 4	l2-0001 €	680/U

NOTE: Underscored cables are not matched to connectors, m = male; f = female.

^{*}Fits Types C and SC only.

[†]Fits Type N only.

42-31

 TE_{mn} waves: In the transverse electric waves, sometimes called H_{mn} waves, the electric vector is always perpendicular to the direction of propagation.

 TM_{mn} waves: In the transverse magnetic waves, sometimes called the E_{mn} waves, the magnetic vector is always perpendicular to the direction of propagation.

The propagation constant γ_{mn} determines the amplitude and phase of each component of a wave as it is propagated along the waveguide. Each component may be represented by $A \exp(jwt - \gamma_{mn}z)$, where A is a constant, z is the distance along the direction of propagation, and $\omega = 2\pi f$. When γ_{mn} is real, there is no phase shift along the waveguide, but there is high attenuation. In fact, no propagation takes place, and the waveguide is considered below cutoff. The reactive attenuation L along the waveguide under these conditions is given by

$$L = \frac{54.58}{\lambda_c} \left[1 - \left(\frac{\lambda_c}{\lambda} \right)^2 \right]^{1/2}$$
 dB/unit length

where λ is the wavelength in the unbounded medium and λ_c is the cutoff wavelength of that wave (a function of waveguide dimensions only). Waveguides are often used at frequencies far below cutoff as calibrated attenuators, since the rate of attenuation is determined by cross-section dimensions of the waveguide and the total attenuation in decibels is a linear function of the displacement of the output from the input.¹³

When γ_{mn} is imaginary, the amplitude of the wave remains constant but the phase changes with z and propagation takes place. γ_{mn} is a pure imaginary quantity only for lossless waveguide. In a practical case, γ_{mn} has both a real part α_{mn} which is the attenuation constant, and an imaginary part β_{mn} , which is the phase constant; that is, $\gamma_{mn} = \alpha_{mn} + j\beta_{mn}$.

The wavelength in a uniform waveguide is always greater than the wavelength in the unbounded medium and is given by

$$\lambda_g = \frac{\lambda}{[1 - (\lambda/\lambda_c)^2]^{1/2}}$$

The phase velocity is the apparent velocity, judging by the phase shift along the guide. Phase velocity, $v = c (\lambda_g/\lambda)$, is always greater than that in an unbounded medium.

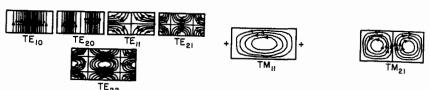
The group velocity is the velocity of energy propagation down the guide. Group velocity, u = c (λ/λ_o), is always less than that in an unbounded medium.

For air-filled guide and guides filled with dielectric having very low loss, the attenuation is mainly due to conductor losses in the walls. For any particular type of wave, the loss is high near cutoff and decreases as the frequency is increased. For all excepting the TE_{0n} waves in circular waveguide, the attenuation reaches a minimum value for that wave and that waveguide, then increases with frequency. For most waves, this minimum is slightly above $2f_c$. To avoid high loss near cutoff and the complexity of multiwave transmission, the useful band is usually considered to lie between $1.3f_c$ of the desired mode and $0.9f_c$ of the next higher mode. For rectangular waveguides having a width equal to twice the height, the useful range is about 1.5:1.

Rectangular Waveguides

For TE_{mn} waves in rectangular waveguides, m and n may take any integer value from 0 to infinity, except for the case m = n = 0. For the TM_{mn} waves, m and n may take

any value from 1 to infinity. The m and n denote the number of half-period variations of the electric field for TE waves or magnetic field for TM waves in the direction of the small and large dimensions of the waveguide respectively. Field patterns for some of the simpler waves are shown in Fig. 42-13.



E LINES FOR TE MODES

H LINES FOR TM MODES

FIG. 42-13 Field configurations for rectangular waveguide.

The propagation constant for rectangular guides is given by

$$\gamma_{mn} = \sqrt{\left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 - \omega^2 \mu \epsilon} = \frac{2\pi}{\lambda_g}$$

where a is the wide dimension, b is the narrow dimension, ϵ is the dielectric constant, and μ is the permeability of the dielectric in the waveguide. Since propagation takes place only when the propagation constant is imaginary, the cutoff frequency for rectangular waveguide is

$$f_c = \frac{c}{2\sqrt{\mu\epsilon}} \sqrt{\left(\frac{m}{a}\right)^2 + \left(\frac{n}{b}\right)^2}$$
$$\lambda_c = \frac{2\sqrt{\mu\epsilon}}{\sqrt{(m/a)^2 + (n/b)^2}}$$

and

Most frequently, operation is limited to the TE_{10} or dominant wave in rectangular waveguide. For this simplified case, the important formulas reduce to

$$\lambda_c = 2a \sqrt{\mu\epsilon}$$

$$\gamma = 2\pi \sqrt{(1/4a) - f^2\mu\epsilon}$$

In order to relate the waveguide properties to similar properties of low-frequency circuits, the impedance concept has been developed. Three characteristic impedances can be defined, differing from each other by a constant:¹⁴

$$Z_{VI} = \frac{V}{I} = 377 \frac{\pi}{2} \frac{b}{a} \frac{\lambda_g}{\lambda} = 592 \frac{b}{a} \frac{\lambda_g}{\lambda}$$

$$Z_{PV} = \frac{V^2}{2P} = 754 \frac{b}{a} \frac{\lambda_g}{\lambda} = 754 \frac{b}{a} \frac{\lambda_g}{\lambda}$$

$$Z_{PI} = \frac{2P}{I^2} = 377 \frac{\pi^2}{8} \frac{b}{a} \frac{\lambda_g}{\lambda} = 465 \frac{b}{a} \frac{\lambda_g}{\lambda}$$

Any one of the three is reasonably satisfactory if used consistently throughout, since the most frequent use is in determining mismatch at waveguide junctions and it

is the ratio of impedance that matters. Ratios involving only different values of b give accurate indication of impedance mismatch. Differences in a give ratios nearly correct for small changes in a from the usual cross-section dimensions of rectangular waveguide, but errors are appreciable for large differences in a. Z_{PV} is most widely used, but Z_{VI} is found to be more nearly correct in matching coaxial line to waveguide.

Circular Waveguides

The usual coordinate system is ρ , θ , z, where ρ is in the radial direction, θ is the angle, and z is the longitudinal direction.

For TE_{mn} waves in circular waveguides m denotes the number of axial planes along which the normal component of electric field vanishes and n the number of cylinders including the boundary of the guide along which the tangential component of electric field vanishes. The number m may take any integral value from 0 to infinity, and n may take any integral value from 1 to infinity. The dominant wave in circular waveguide is the TE_{11} . For TM_{mn} waves, m denotes the number of axial planes along which the magnetic field vanishes and n the number of cylinders to which the electric field is normal. The number m may take any integral value from 0 to ∞ , and n may take any integral value from 1 to ∞ . Of the circularly symmetrical waves, the TM_{01} has the lowest cutoff frequency.

Field patterns for some of the simpler waves in circular guides are shown in Fig. 42-14.

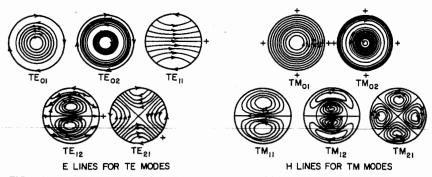


FIG. 42-14 Field configurations for circular waveguide.

The cutoff wavelength in lossless circular guide is given by

$$\lambda_c = \sqrt{\mu \epsilon} D_{mn} a$$

where a is the radius, ϵ the relative dielectric constant, and μ the relative permeability of the dielectric, and the constant D_{mn} is as shown in Table 42-5.

A summary of the cutoff and attenuation constant formulas for circular and rectangular waveguides is given in Table 42-6,

where
$$A = \frac{\sqrt{c/\lambda}}{\sqrt{1 - (\lambda/\lambda_c)^2}}$$

 $c = \text{velocity of light in free space} \approx 3 \times 10^8 \text{ m/s}$

TABLE 42-5 Cutoff Constants for Circular Waveguide

	D _{mn} fo	or TE _m ,	waves	
m	0	1	2	3
1	1.640	3.412	2.057	1.496
2	0.896	1.178	0.937	0.764
3	0.618	0.736	0.631	0.554
4	0.475	0.54	0.48	0.44
	D _{mn} fo	r TM _m	waves	
m	0	1	2	3
1	2.613	1.640	1.224	0.966
2	1.139	0.896	0.747	0.644
3	0.726	0.618	0.541	0.482
4	0.534	0.475	0.425	0.388

TABLE 42-6 Summary of Cutoff and Attenuation Constant Formulas

TYPE OF GUIDE	<u></u>		20	1
	RECTANGULAR TEMO	TMoI	TEII	TEOI
CUTOFF WAVELENGTH	<u>2a</u> m	2.6130	3.412a	1.640a
ATTENUATION CONSTANT (NEPERS/METER DUE TO CONDUCTION LOSSES ONLY	$\frac{4\alpha_0 A}{a} \left(\frac{a}{2b} + \frac{\lambda^2}{\lambda_c^2} \right)$	2 <u>a_oA</u>	$2\frac{\alpha_0}{\alpha}A(0.415+\frac{\lambda^2}{\lambda_c^2})$	$2\frac{\alpha_0}{a}A\frac{\lambda^2}{\lambda_c^2}$
ATTENUATION FAR BELOW CUTOFF	27.28 DB PER GUIDE WIDTH	41.78 DB PER DIAMETER	31.98 DB PER DIAMETER	66.56 DB PER DIAMETER

For copper and air, $\alpha_0 = 3.5 \times 10^{-8}$ Np/m. To convert nepers per meter to decibels per 100 ft, multiply by 264.

Standard Waveguide Sizes

The waveguide sizes which have become standardized are listed in Table 42-7, together with the flanges used in connecting them together. (See pages 42-36 and 42-37.)

Flexible Waveguides

Flexible rectangular waveguides are made to match most of the standard waveguides. These differ primarily in mechanical construction. Waveguides using seamless corrugations, spiral-wound strip with adjacent edges crimped and soft-soldered, and spiralwound strip with heavier crimping to provide sliding contact, as well as vertebra type (consisting of cover-choke wafers held in place by a rubber jacket), are available. The first two will bend in either plane, stretch, or compress but will not twist. The other two twist as well as bend and stretch. When the guide is flexed during operation or pressurized, it is nearly always covered with a molded-rubber jacket. When unjacketed, all are subject to a minimum bending radius (of the guide centerline) of 2 to 3 times the outer guide dimension in the plane of the bend, and when jacketed, to about 4 to 6 times the outer dimensions. The mismatch between rigid and flexible guide is small when straight and designed for lower frequencies. Mismatch increases as the waveguide size decreases, since the depth of convolutions cannot be decreased as fast as the waveguide dimensions (mismatch also increases as the bending radius is decreased). Similarly, attenuation which is only slightly greater than that in rigid guide for low frequencies becomes about twice as great at 40 GHz. Power capacity is nearly equal to that of rigid guide.

Hollow-Tube Waveguides with Other Cross Sections

One of the most useful of the many cross sections that might be used is the ridged waveguide as shown in Fig. 42-15, which is useful in wideband transmission. For

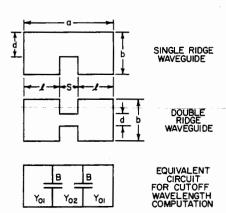


FIG. 42-15 Ridged-waveguide configurations.

ridged waveguide¹⁵⁻¹⁷ (and waveguide of arbitrary cross section), the best method of obtaining cutoff wavelength is by resonance in the cross section. A convenient longitudinal plane is chosen. At cutoff, the susceptance looking into the shorted parallel-plate guide to the right of this plane is equal in amplitude and opposite in phase to that looking to the left. If the guide is symmetrical, only half of the guide need be used since Y at the center is zero. For the ridged guide this gives

$$\cot \frac{2\pi l}{\lambda_c} - \frac{B}{Y_{01}} = \frac{b}{a} \tan \frac{2\pi S}{\lambda_c 2}$$

where B is the capacitive discontinuity at the height change.

The loading in the center of the guide lowers the cutoff frequency of the

dominant mode so that a useful bandwidth of over 4:1 may be obtained with single-mode transmission. The impedance is reduced by the loading and can be adjusted by proportioning the ridges for impedance matching of waveguides to coaxial line, for example.

The ridged guide for a given frequency band is smaller than the regular guide, but the losses are higher.

TABLE 42-7 Standard Rectangular Waveguides and Flanges

			ľ	1	100	177				Attenuation	Theoretical	Th. 0.000 1000	Flanges	808
EIA	00	AN	BiTet	dimen	ance,	Thick-	<u> </u>			(dB/30.5 m)	<u>Q</u>	maximum		
tion WR- M85 / 1- tion	M85/1-	tlon	вМ	in (mm)	(mm)	(mm)	TE ₁₀	for TE ₁₀	۶ ۳	Lowest and highest	d highest	wave, kW	Cover	Cover Choke
650	-210		- B	6.500 × 3.250	+0.008	0.080	1.12-1.70	0.908	330.2	0.3160209	41.3–59.7	80.5-122	323/11	11/221
	810		4	(165.1 × 82.55)	(0.20)	(2.03)				0.273-0.180		88.5-136	1720/11	2/22
910	023-	337/U	<u>B</u>	5.100×2.550	₹0.008	0.080	1.45-2.20	1.154	259.1	0.440-0.299	26.2-37.0	47.9-70.4	1715/0•	
	025-	338/U	۷	$\overline{}$	(0.20)	(5.03)				0.380-0.258		53.2-78.3	•U/7171	
430	929		<		+0.008	0.080	1.70-2.60	1.375	218.4	0.502-0.334	18.2-26.3	35.3-53.1	437/U•	
	<u>8</u>		<u> </u>	$\overline{}$	(0.20)	(2.03)				0.583-0.387		31.7-47.7	435A/U*	
340	035-		۷ ،		1+0.006	0.080	2.20-3.30	1.737	172.7	0.682-0.474	11.9-16.4	21.7-31.3	554/U*	
	037.		m	(86.36×43.18)	(0.15)	(5.03)				0.791-0.550		19.5-28.1	\$53A/U*	
284	<u>\$</u>		<	2.840 × 1.340	+0.006	0.080	2.60-3.95	2.080	144.3	0.950-0.651	7.65-10.9	13.4-19.6	584/U	585A/U
	943-		<u>m</u>	(72.14×34.04)	(0.15)	(2.03)				1.10-0.754		12.1-17.6	53/U	54B/U
229	-24		<	2.290 × 1.145	+0.004	0.064	3.30-4.90	2.577	116.3	1.21-0.858	5.48-7.55	8.99-12.7	1727/0•	
	94	_	<u> </u>	(58.16 × 29.08)	(0.15)	(1.63)				1.40-0.996		8.08-11.4	1726/U•	
187	053-	_	<	1.872×0.872	+0.005	0.064	3.95-5.85	3.155	95.10	1.79-1.24	3.30-4.70	5.17-7.45	401/U	406B/U
	-550	_	B	$\overline{}$	(0.13)	(1.63)				2.07-1.44		4.64-6.69	149A/U	148C/U
129	-650	_	۷	1.590 × 0.795	± 0.005	0.064	4.90-7.05	3.705	80.77	1.99-1.49	2.79-3.72	4.20-5.62	1731/.0•	
	-190		<u> </u>	(40.39×20.19)	(0.13)	(1.63)				2.31-1.72		3.77-5.05	247/U	248/U
137	-590		<	1.372×0.622	+0.00+	0.064	5.85-8.20	4.285	02.69	2.53-2.00	1.98-2.53	2.90-3.67	441/U	440B/U
	-290		<u> </u>	$\overline{}$	(0.10)	(1.63)				2.94-2.32		2.60-3.29	344B/U	343B/U
112	-120		<	_	+0.004	0.064	7.05-10.0	5.260	27.00	3.55-2.76	1.28-1.70	1.79-2.30	138/U	137B/U
	073-		<u> </u>	=	(0.10)	(1.63)				4.11-3.20		1.61-2.07	0/15	52B/U
8	-770		<		+0.004	0.050	8.20-12.4	9.560	45.72	5.54-3.83	0.758-1.12	0.959-1.39	135/U	136B/U
	620		m	÷	(0.10)	(1.27)				6.42-4.45		0.862-1.25	39/0	40B/U
75	083-	_	<		+0.003	0.050	10.0-15.0	7.847	38.10	6.55-4.58	0.622-0.903	0.737-1.06		
	-580		-	(19.05 × 9.53)	(0.08)	(1.27)				7.60-5.31		0.662-0.948		
62	-680		 _	0.622 × 0.311	±0.0025	0.040	12.4-18.0	9.490	31.60	9.58-7.04	0.457-0.633	0.451-0.614	419/U	541A/U
	-060		۷	(15.80×7.90)	(0.06)	(1.02)				8.26-6.07		0.502-0.683	1665/U	1666/U
	-669		သွ							6.91-5.08		0.602-0.818	419/U	541/U
- 15	96				±0.002\$	0.040	15.0-22.0	11.54	25.91	13.1-9.48	0.312-0.433	0.290-0.400		
_	-/60	_	<u> </u>	(12.95 × 6.48)	(0.0%)	(1.02)	_		_	11.3-8.17		0.323-0.445		

S96A/U	298A/U	296A/U				00A/U																						
0/s6s	0/16S	0/s6s	1530/U•			289/U		383/U•		1529/U•		385/U•		387/U•		1528/U•		1527/0		1525/U		1524/U•		1526/0				
0.157-0.213	0.174-0.237	0.209-0.284	0.118-0.169	0.131-0.188	0.175-0.252	0.212-0.310	0.242-0.347	0.134-0.197	0.149-0.219	0.111-0.155		0.052-0.077	0.058-0.085	0.047-0.067	0.049-0.074	0.032-0.045	;	0.015-0.024		0.010-0.016		0.006-0.01		0.005-0.007		0.003-0.008		
0.171-0.246			0.139-0.209			0.096-0.146		0.064-0.097		0.048-0.070		0.030-0.044		0.020-0.030		0.014-0.020		0.009-0.013		0.006-0.009		0.004-0.006		0.003-0.005		0.0004-0.0005		
20.5–15.0	17.7-13.0	14.8-10.9	25.0-17.4	21.6-15.0	16.2-11.3	24.6-16.8	22.0-15.1	34.5-23.5	31.0-21.1	38.0-27.3		64.2-43.9	57.6-39.3	87.8-58.9	78.7-52.7	101-71.0		154-98.7		214-135		308-194		377-251		512-341		
21.34	_		17.27			14.22		11.38		9.550		7.518		861.9		5.080		4.064		3.302		2.591		2.184		1.727		
14.08			17.28			21.10		26.35		30.69		39.90		48.40		58.85		73.84		90.85		115.8		137.5		173.3		
18.0-26.5			22.0-33.0			26.5-40.0		33.0-50.0		40.0-60.0		50.0-75.0		0.06-0.09		75.0-110		90.0-140		110-170		140-220		170-260		220-325		
0.040	(1.02)		0.040	(1.02)		0.040	(1.02)	0.040	(1.02)	0.040	(1.02)	0.040	(1.02)	0.040	(1.02)	0.040	(1.02)	0.020	(0.51)	0.020	(0.51)	0.020	(0.51)	0.020	(0.51)	Round		
±0.002	(0.05)		±0.002	(0.05)		±0.0015	(0.04)	±0.0010	(0.03)	±0.0010	(0.03)	±0.0010	(0.03)	± 0.0005	(0.01)	±0.0005	(0.01)	+0.0003	(0.01)	±0.00025	(0.01)	±0.00025	(0.01)	±0.0002	(0.01)	±0.000	(0.01)	
0.420 × 0.170			0.340 × 0.170			0.280×0.140		0.224 × 0.112	(5.69×2.84)	0.188 × 0.094	(4.78×2.39)	0.148 × 0.074	$0(3.76 \times 1.88)$	0.122 × 0.061	(3.10×1.55)	0.100 × 0.050	(2.54×1.27)	0.080 × 0.040	(2.03×1.02)	0.065×0.0325	(1.65×0.83)	0.051×0.0255	(1.30×0.65)	0.043×0.0215	(1.09×0.546)	0.034×0.0170	(0.864×0.432)	ResistivityO . cm
-		SC	_		SC	s	SC	s	SC	SC	_	s	သွ	s	SC	ပ္တ		သွ		သွ		SC		$^{\circ}$		s		
83/0	12/10	N/99	354/U	355/U	357/U)/96	2/1/C	0/16	272/U	358/U		0/86	273/U	0/66	274/U	359/U		278/U		J/9/Z		275/U		U/172		139/N		
103-	60	-60	60	<u>ė</u>	13-	4	117-	<u>*</u>	121-	124		125-	128-	129-	132-	135		138-		141-		144		147-		152-		
42	:		34	:		28	-	22	}	61		15	!	12	!	01				7		\$		4				

Materials	Resistivity, All · cm	
A = aluminum alloy 1100 B = brass	2.90	
SC = silver-clad copper S = silver	1.63	

^{*}These flanges mate with themselves.

Designs exist, and there are government standards for both single- and doubleridge guide with bandwidth ratios of 2:4 and 3:6. The loss of the 3:6-bandwidth guide approaches that of some of the low-loss coaxial lines and has not had wide acceptance. The 2:4-bandwidth double ridge is being used above 3.5 GHz, and the characteristics of the more popular sizes are listed in Table 42-8.

Fin-Line Guide Shown in Fig. 42-16, fin-line guide uses central loading as in ridge guide, but the central-loading fin is an etched pattern on a suitable plastic or ceramic and may be insulated from the rest of the structure. It has the same wide bandwidth and concentration of the electric field at the guide center as the ridge guide, providing excellent excitation of the etched circuit patterns and any lumped circuit elements mounted on the center fin. Although not widely used as a uniform transmission line, fin-line guide is very useful when it is desirable to build filters, mixers, and other circuit elements right into the antenna feed. 18,19

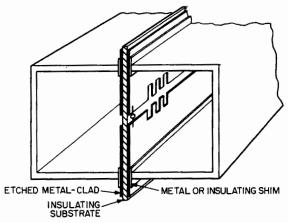


FIG. 42-16 Fin-line guide.

42-8 MISCELLANEOUS TYPES OF WAVEGUIDES

Trough Waveguide20

Trough waveguide having the cross section shown in Fig. 42-17 is derived from the lowest TE mode on symmetrical stripline by inserting a longitudinal electric wall at the center of the strip. Energy is transmitted in the TE modes in which the electric fields are symmetrical about the center vane. The cross section is such that probes, tuning, or attenuating devices may easily be inserted and moved from the open side with a minimum of electrical disturbance. Trough waveguide is a broadband transmission device since the cutoff of the second propagating mode is 3 times that of the dominant mode instead of twice as in rectangular waveguide. It is easily fed from an end-on transition from coaxial or symmetrical stripline. The outer conductor of the TEM line is connected to the outer walls of the trough guide. The inner conductor of the line is connected at a point on the center vane of the trough guide at a distance S

Tvpe des-	DOD part	Ishe	Inside	Toler-	Outside	Toler- ance,		Fre- quency	Cutoff fre quency, GHz	f fre- icy, Iz	Cutoff fre- cal atten- quency, uation, GHz dB/100	Theoreti- cal	
ignation WRD no.	no. M23351/4-		dimensions, in (mm)	i (iiii	dimensions, in (mm)	(E E	Gap, In (mm)	range, GHz	TE10	TE20	30.5m)	k₩.	- Pag
				10003	1 608 × 0 816	+00004	0.2920	3.50-8.20	2.915	8.620	3.07	151.3	1574/U
350	030	< B	(37.59×017.48)		$\overline{}$		±0.002				3.03		U/5751
	031	ပ	-				(+0.05				2.18		1575/U
į	032	S <	1 000 × 0 506	+0.003	1.190 × 0.606	+0.003	0.215	4.75-11.00	3.961	11.705		83.72	U/1781
475	034	< 🛭	(27.69 × 12.85)	(80.0)	$\overline{}$		± 0.002				4.81		U/8/21
	035	ပ					(5.46)				3.24		15/8/U
	036	S			107.0	1	(± 0.05)	7 50-18 00 6 239	6 2 3 9	18 464		33.58	1580/U
750	037	<	0.691×0.321	± 0.003	0.791×0.421	100 E	+0.000	00.01_00.7	ì				1581/U
	038	m	(c1.8 × 8.11)	(0.09)	(20.01 × 20.02)	(00:0)	(3.45)				6.41		1581/U
	039	O ((+0.05)				98.9		1581/U
3	9 5	γ 4	0.471 × 0.219	+0.003	0.551 × 0.299	±0.003	0.0930	11.00-26:50 9.363	9.363	27.080		15.63	1583/U
211	045	m	_	(0.08)	(14.00×7.59)	(0.08)	±0.002				16.9		1584/U
	043	ပ	_				(2.362)				4.5.		1584/U
	440	S			710000	1	CD:0 ±)	18 00 40 00 14 495 44 285	14 495	44 285		5.834	1586/U
180	8 5	<		±0.003	0.305 × 0.214	000	+000	200		_			1587/U
	046	B	(7.32×3.40)	(0.08)	(**.5 × 5.4)	90.0	(1 448)				23.8		1587/U
	047	<u>၂</u>					(+0.05)				25.5		U/287/U
	048	S					(50.07)						
Materials		Resi.	Resistivity, 40 · cm										

Resistivity, 40 · cm	1) 4.0 3.9 1.77 2.03	Pi
Materials	A = aluminum (6061) B = brass C = copper	

NOTE: Attenuation is computed at $f=3/\epsilon_{10}$. Actual attenuation may be considerably higher, depending on operating frequency and temperature. Actual power handling may be considerably less, depending on temperature, altitude, operating frequency, etc. For further information on both attenuation and power-handling capacity and on other design characteristics, see Ref. 18.

S = coin silver

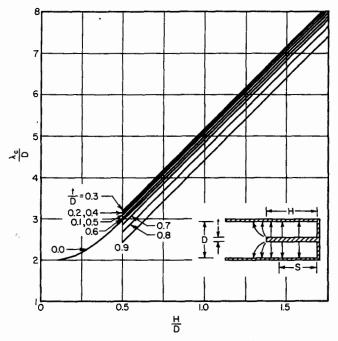


FIG. 42-17 Cutoff wavelength of trough waveguide.

up from the bottom of the center vane, as determined from the relation for the power-voltage characteristic impedance at that point,

$$Z_{PV}(S) = 754 \frac{D}{\lambda_c} \frac{\lambda_g}{\lambda} \sin^2 \left(\frac{2\pi S}{\lambda_c} \right)$$

Similarly, a crystal may be attached at an appropriate point to provide a crystal mount. The cutoff wavelength of the dominant mode in trough waveguide may be determined from the graph in Fig. 42-17.

Radial Line and Biconical Guide

Two circular parallel conducting plates, separated by a dielectric and fed at the center or outer edge, form a line in which the transmission is radial. This type of line is frequently used in choke junctions and resonant cavities such as microwave oscillator tubes. The simplest wave transmitted by this type of line is a TEM wave. The phase front of this wave is a circle of ever increasing or decreasing radius. The radial current in one plate returns radially through the other plate. With radial lines it is very useful to know the input impedance with (1) known termination, (2) output shorted, and (3) output open. Input impedance is

$$Z_i = Z_{0i} \left[\frac{Z_L \cos(\theta_i - \psi_L) + j Z_{0L} \sin(\theta_i - \theta_L)}{Z_{0L} \cos(\psi_i - \theta_L) + j Z_L \sin(\psi_i - \psi_L)} \right]$$

where Z_i = input impedance, Ω

 Z_{0i} = characteristic impedance, Ω , at input (Z_0 of Fig. 42-18 at $r = r_i$)

 Z_{0L} = characteristic impedance at output (Z_0 of Fig. 42-18 at $r = r_L$)

 Z_L = terminating impedance, Ω

 θ_b , θ_L , ψ_b , ψ_L = angles as plotted in Fig. 42-18

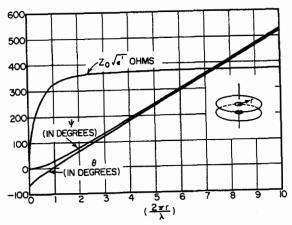


FIG. 42-18 Radial transmission-line quantities.

In one special case of this, $Z_L = 0$; then

$$Z_i = jZ_{0i} \frac{\sin(\theta_i - \theta_L)}{\cos(\psi_i - \theta_L)}$$

In another, $Z_L = \infty$; then

$$Z_i = jZ_{0i} \frac{\cos(\theta_i - \psi_L)}{\sin(\psi_i - \psi_L)}$$

Many higher-order modes are possible. Those with variations in ϕ only will propagate with any spacing of plates. Those having variations in z propagate only if the plate separation is greater than a half wavelength. More complete descriptions can be found in Refs. 1, 2, and 21.

Two cones with their apices facing and fed by a balanced input at the center as shown in Fig. 42-19 form a biconical waveguide. This structure also simulates a dipole antenna and certain classes of cavity resonators.

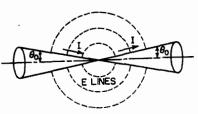


FIG. 42-19 Biconical waveguide.

One important wave transmitted by this type of guide has no radial components and propagates with the velocity of light along the cones. It is analogous to the TEM wave in cylindrical systems. The ratio of voltage to current or characteristic impedance is

$$Z_0 = 120 \log_e \cot \frac{\theta}{2} \qquad \Omega$$

where θ is the conical angle. From this it is seen that the characteristic impedance is independent of radius and not variable as in the radial line.

Many higher modes can propagate on this system. These will all propagate at a velocity different from that of light. For transmission of higher modes, see Refs. 1 and 2.

Dielectric Waveguide

Electromagnetic waves will propagate along a dielectric rod^{22} if the rod is of sufficient size. At low frequencies, there is little advantage to dielectric waveguides since low loss in metal waveguide makes them a convenient shielded carrier of microwave energy. At frequencies above 20 GHz, the lower loss possible with dielectric waveguides makes their use attractive. For lossless dielectric waveguides, the propagation constant can never be real, so there is no cutoff frequency as with metal waveguides. For a given waveguide, VHF energy is confined entirely within the dielectric. The velocity of propagation and the loss correspond to that in the waveguide dielectric. As the frequency is reduced, more of the field is outside the waveguide, and the velocity and loss approach that of the surrounding air, but the dielectric ceases to guide the wave. The only TE and TM modes possible in a circular rod are those having axial symmetry. One hybrid mode, the HE₁₁ (hybrid because it has both E_z and H_z components), is particularly well adapted for microwave transmission. It can be small (it

is the only mode which can be propagated when the ratio of diameter to wavelength is low; less than 0.6 for polystyrene). It can be launched from the dominant TE metallic waveguide mode, and it has low loss. The approximate field configuration of this mode is shown in Fig. 42-20.

Figures 42-21 to 42-23 show variation of guide wavelength with diameter, loss as a function of diameter, and a waveguide launcher for the HE₁₁ hybrid mode. The polarization of the hybrid mode in circular rod is subject to rotation because of internal stresses, dimensional

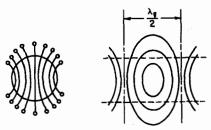


FIG. 42-20 Approximate E-field configuration of HE₁₁ mode on a dielectric rod waveguide.

nonuniformity, and bends. A rectangular or oval cross section prevents this depolarization. Measurements of loss and radius of field extent (radius at which field decreases to 1/e times that at surface) for cross sections of the oval type are shown in Table 42-9 for 24 and 48 GHz.

Transmission with dielectric tubes as well as rods is possible. Tubes can have lower loss than rods, and theoretical calculations indicate²³ that with a polystyrene tube attenuation at 30 GHz compares with TE₀₁ guide.

Other calculations shown in Fig. 42-23 indicate that losses of a few decibels per kilometer can be attained up to the infrared region by choice of the proper diameter. 24,25

The image line²⁶⁻²⁸ is a variation of the dielectric guide which simplifies the support problem. The HE₁₁ mode, being symmetrical, can be split longitudinally and one-half replaced by a metal plate as shown in Fig. 42-24. Losses at bends are lower for concave bends than for convex. Losses in the image plane are lower than those in the dielectric for all commonly used materials.

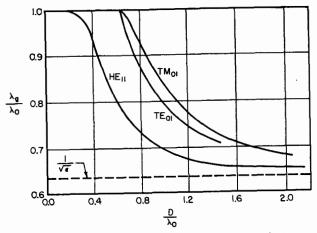


FIG. 42-21 Guide wavelength versus diameter for polystyrene waveguide.

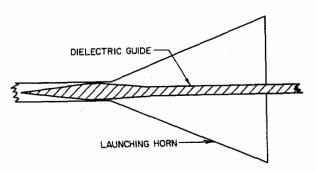


FIG. 42-22 Waveguide launcher for HE,1 mode.

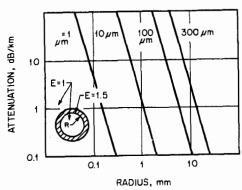


FIG. 42-23 Attenuation of dielectric tube wavelength with a dielectric of 1.5 for the HE₁₁ mode.

TABLE 42-9 Loss for HE₁₁ Mode in Dielectric Waveguide

MATERIAL POLYSTYRENE	DIMENSIONS in (cm)	E DIRECTION	RADIUS OF FIELD EXTENT, in (cm)	LOSS dB/km	FREQ
SHEET STOCK	.095 x .156 (.241 x .396)	Ô	1.5 (3.8)	164	GHz
EXTRUDED	.086 x .155 (.218 x .394)	ð	4 (10.2)	164	24
EXTRUDED	.086 x .155 (.218 x .394)	+ Đ	7 (17.8)	82	
EXTRUDED	.056 x .142 (.142 x .361)	•€⊃	.4 (1.0)	3281	
EXTRUDED	.056 x .142 (.142 x .361)	.	.8 (2.0)	886	
EXTRUDED	.038 x .114 (.097 x .290)	.	1.5 (3.8)	148	48_
EXTRUDED	.032 x .096 .081 x .244)	ф	3 (7.6)	23	

A variation of the image line has been suggested for use in integrated circuits. In this version²⁹ a rectangular dielectric strip is laid on top of an integrated circuit board which is copper-clad on the lower surface.

Multimode Waveguide

Normally waveguides are used in the lowest mode, and the higher modes are avoided. At millimeter-wave frequencies



FIG. 42-24 Image line using HE₁₁ mode.

losses in the lowest-mode-only waveguide become very high because of conductor losses. By using low-loss modes in circular waveguide far above cutoff, most of the energy is carried in the fields in the air inside and losses are reduced. Operating far from cutoff also reduces the dispersion and increases the signal bandwidth. Special efforts must be taken to prevent excitation of unwanted modes. Multimode circular guide has demonstrated a signal bandwidth of 40 to 117 GHz and transmission losses of less than 1 dB/km.³⁰

Beam Waveguide

Another method of avoiding conductor loss is to use lenses to focus the energy into a converging beam or at least a nondiverging beam, refocusing periodically along the transmission path. For more information on this type see Ref. 31.

Optical-Fiber Waveguide

Optical fiber is usually a single strand of glass designed to hold an electromagnetic wave closely bound to the glass signal path. Since it is not a carrier of the fundamental signal frequency (a microwave signal would ordinarily be modulated on a light beam), it is not covered in detail here. It has many of the advantages of the multimode wave-

guide, the beam waveguide, and the dielectric waveguide, principally low loss and large bandwidth. A small amount of dispersion limits the distance that a wideband signal can go before some frequencies overtake others and cause information degradation. However, operational use has demonstrated losses well under 1 dB/km and bandwidths of over 1 GHz divided by the distance in kilometers.³² It will undoubtedly become a major transmission medium for wideband signals.

Elliptical Waveguide

Waveguide with an elliptical cross section is very useful for antenna feeds. It has many of the same characteristics as rectangular waveguide, including a similar waveguide mode (so it mates easily with rectangular guide), and about the same loss and guide wavelength. It does have a narrower bandwidth. It is formed with corrugations along its length, which gives it high transverse stability and crush strength yet allows bending in both planes and a small amount of twist. This makes installation easier than with rectangular guide. It is usually covered with tough black polyethylene to protect it during the hanging, installation, and use. Elliptical waveguide is made in long lengths or is assembled in desired sections with an adapting flange to rectangular guide. Although not yet standardized, it is made by several manufacturers. Most give it a prefix indicating elliptical waveguide such as EW or WE, followed by the lowest frequency or a midfrequency in tenths of a gigahertz. Characteristics of typical sizes are shown in Table 42-10.

42-9 LIST OF SYMBOLS

f = frequency, Hz

 $\omega = 2\pi f$

 $c = \text{velocity of light} \approx 3 \times 10^8 \,\text{m/s}$

 $\lambda = wavelength$

 ϵ = relative dielectric constant

 μ = relative permeability

 $\sigma = \text{conductivity}, S/m$

 α = attenuation constant, Np/m (Np = 8.686 dB)

 $E_a = breakdown of air, V/m$

P = power, W

 $\tan \delta =$ loss tangent or dissipation factor

The properties of some commonly used metals will be found in Chap. 46. The conductivity σ can be found from the resistivity values by the relationship

$$\sigma(S/m) = \frac{10^8}{\text{resistivity } (\mu\Omega \cdot \text{cm})}$$

Values for ϵ and $\tan \delta$ of some commonly used dielectrics will be found in Chap. 46.

TABLE 42-10 Typical Characteristics of Elliptical Waveguide

			00000000000000000000000000000000000000			
	Maximum potential operating	TE ₁₁ - mode cutoff	Major and minor	Bendli minimum	Bending-radii minimum, in (mm)	
Туре	range, GHz	frequency, GHz	dimensions over jacket, in (mm)	E plane	H plane	Recommended
EW20	1.9-2.7	091	5 02 × 2 82 (12 5 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8			(1111) 31 / (2011)
EW28	2.6-3.5	2 20	3.65 × 3.33 (0.27.3 × 71.9)		(1800)	0.25 (0.75)
EW37	3.3-4.3	2.81	3.63 × 2.33 (92.5 × 59.2)		52 (1320)	0.25(0.75)
WE37	3442	10.7	2.50 × 1.80 (13.7 × 47.2)	17 (430)	41 (1040)	(51) 50
EW44	4 2 - 5 1	707	$3.04 \times 1.93 (71.0 \times 49.0)$	19.7 (500)	39.4 (1000)	(5.1) 5.0
:	1:0-4:4	3.38	$2.31 \times 1.59 (58.7 \times 40.4)$	15 (380)	32 (810)	0.3 (1.3
WE44	4.2-5.0	3 58	20 ct 50 063/ 03 1 × 10 C			(5.1)
EW52	4.6–6.425	3.63	2.24 × 1.35 (3.50 × 43.0)	15.7 (400)	47.2 (1200)	0.5 (1.5)
WES6	54-6425	600	$2.25 \times 1.31 (57.2 \times 33.3)$	12 (305)	32 (810)	(3)
WF50	31.2 0.5	90.4	$1.97 \times 1.30 (50.0 \times 33.0)$	19.7 (500)	39 4 (1000)	<u> </u>
2011	C.7-7.13	4.34	$1.85 \times 1.22 (47.0 \times 31.0)$	11.8 (300)	22 5 (200)	(s) -
EWOS	5.85-7.125	3.96	$2.01 \times 1.16 (51.1 \times 29.5)$	(000) 011	^	1 (3)
FW64	327 53		(5:05)	(007) 01	29 (740)	1 (3)
	3.3-1.73	4.36	$1.91 \times 1.12 (48.5 \times 28.4)$	(0)()		
WE64	6.4–7.75	4.16	184 × 114 (40 0 × 20 0)	10 (200)	7/ (685)	1 (3)
WE71	7.1-8.6	5 23	(0.62 × 0.54) +1.1 × 45.1	11.8 (300)	23.6 (600)	(e) -
EW77	6.1-8.5	2 5	$1.34 \times 0.98 (390 \times 25.0)$	11.8 (300)	23.6 (600)	6
EW85	7.7-10.0	7/7	$1.72 \times 1.00 (43.6 \times 25.4)$	9 (230)	25 (635)	6
}	0.01-1	6.50	$1.32 \times 0.90 (33.5 \times 22.9)$	8 (200)		<u> </u>
WE85	8.5-10.2	5.83	138 × 004/350 × 310			(c) I
EW90	8.3-11.7	05.9	1 32 × 0.00 (23 € 24.0)	88 (200)	16 (400)	1 (3)
WE107	8.5-11.7	06.7	1.32 × 0.80 (33.5 × 20.3)	(180)	19 (480)	9
WE122	12 2 13 35	0.00	$1.18 \times 0.79 (30.0 \times 20.0)$	(150)	16 (400)	99
E11/13	10.0	67.7	$1.09 \times 0.71 (28.0 \times 18.0)$	(051)	(00)	(0) 7
EW 122	10.0-13.25	8.46	$1.07 \times 0.72(27.2 \times 18.3)$	(051)	16 (400)	2 (6)
EW132	11 02.15 25			(001)	(380)	2 (6)
	0000	7.33	$0.96 \times 0.61 (24.4 \times 15.5)$	5 (130)	14 (360)	(9) (
						(0) 7

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Impedance Matching and Broadbanding

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Antenna Consultant

43-1 General 43-2
Impedance Matching for Maximum
Power Transfer 43-2
Impedance Matching for Minimum
Reflection 43-2

Reflection-Coefficient Charts 43-5
43-2 Impedance Matching with Lumped

Elements 43-5

L Section 43-6

T and π Sections 43-6

Lattice Section 43-7

Inductive Coupling 43-7

Lumped Matching Reactance 43-8

43-3 Impedance Matching with Distributed
Elements 43-9

Transmission-Line Stubs 43-10
General Line Transformer 43-10
Line Transformer for Matching to
Resistance 43-11
Quarter-Wave Transformer 43-12
Zo Trimmer 43-12

Frequency Sensitivity of Line
Transformer 43-12
Cascaded Quarter-Wave
Transformers 43-14
Binomial Transformer 43-14
Chebyshev Transformer 43-15
Dual-Band Transformers 43-17

Short-Step Transformer 43-17
43-4 Tapered Lines 43-18
Exponential Line 43-18
Other Tapered Lines 43-19

43-5 Combinations of Transformers and
Stubs 43-21
Transformer with Two
Compensating Stubs 43-21
Transformer with Single
Compensating Stub 43-22
Tapped-Stub Transformer 43-22

43-6 Baluns 43-23

43-7 Broadbanding 43-27

Impedance matching is the control of impedance for the purpose of obtaining maximum power transfer or minimum reflection. This chapter describes circuits and techniques used for impedance matching with emphasis on those most suitable for broadband operation. The impedance-matching methods of this chapter are limited to the use of linear, passive, and reciprocal elements.

Impedance Matching for Maximum Power Transfer

A variable load impedance connected to a source will receive the maximum possible power from the source when it is adjusted to equal the complex conjugate of the impedance of the source (Fig. 43-1a). The load impedance and source impedance are then matched on a conjugate-impedance basis.*

A fixed source impedance and a fixed load impedance may be coupled for maximum power transfer by a properly proportioned network (Fig. 43-1b) interposed between them. This "matching" network transforms the source impedance to the conjugate of the load impedance, and vice versa. Thus a conjugate-impedance match occurs at the input to the network and at the output of the network. It is true of any lossless transmission circuit that if a conjugate-impedance match is obtained at any point along the transmission path, then a conjugate-impedance match is obtained at all other points along the path.

Impedance Matching for Minimum Reflection

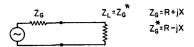
A length of lossless transmission line may form one link in a lossless transmission circuit. Lines commonly used in antenna systems have characteristic impedances that are purely or nearly real. Characteristic impedances designated by Z_0 in this chapter are real unless otherwise noted. Electrical length is denoted by $\beta\ell$. Maximum power transfer will occur when the circuit is adjusted for a conjugate-impedance match (Fig. 43-1c). However, in general, the line will be subject to two waves, a direct and a reflected wave, propagating in opposite directions. The interference between these waves creates standing-wave patterns of voltage and current. These effects may be tolerable, but usually they are undesirable.

If the line has finite attenuation, maximum power transfer from the source to the load is obtained only when the following conditions are met:

- 1 The generator is loaded by the conjugate of its internal impedance.
- 2 The line is terminated in its characteristic impedance.

The first condition provides maximum power delivery from the source. The second condition provides minimum power dissipation in the line by eliminating the reflected wave on the line.

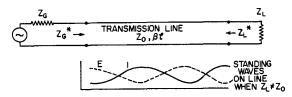
^{*}This is distinct from impedance matching on an image-impedance basis in which the source and load impedances are equal. Image-impedance matching is sometimes used for convenience, often when the impedances are nearly resistive. However, it does not result in the maximum-power-transfer condition unless the impedances are purely resistive.



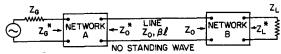
A. A SOURCE AND A LOAD MATCHED ON A CONJUGATE-IMPEDANCE BASIS



B. A SOURCE AND A LOAD MATCHED ON A CONJUGATE-IMPEDANCE BASIS BY A MATCHING NETWORK



C. A SOURCE, LOSSLESS LINE AND A LOAD MATCHED ON A CONJUGATE-IMPEDANCE BASIS



D: A SOURCE, A LINE AND A LOAD MATCHED ON A CONJU-GATE IMPEDANCE AND CHARACTERISTIC IMPEDANCE BASIS BY NETWORKS

FIG. 43-1 Impedance matching of transmission circuits.

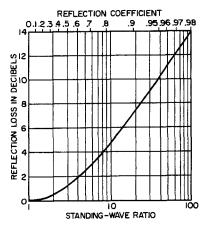


FIG. 43-2 Reflection loss.

Figure 43-1d shows a "matched" system, that is, a system matched both on a conjugate-impedance basis and on a characteristic-impedance basis. This represents an ideal condition.

The importance of matching can be seen by an examination of the detrimental effects of a mismatch. A measure of mismatch at the load junction is the voltage reflection coefficient.

$$\rho = \rho \exp(2\psi) = \frac{Z_L - Z_0}{Z_L + Z_0}$$

This defines vectorially the reflected voltage wave for a unit wave incident on the junction. The power in the load is thus reduced from the maximum available power by the ratio of $1 - \rho^2$.

The reduction in transmission is called a reflection loss or transition loss. Reflection loss expressed in decibels is shown as a function of the standing-wave ratio (SWR)

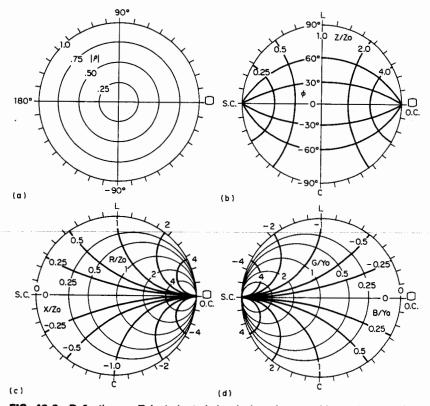


FIG. 43-3 Reflection coefficient charts in hemisphere form; positive real axis to the right. (a) Reflection coefficient in polar coordinates of $|\rho|$ and 2ψ . (b) Impedance coordinates of $|z|=|Z/Z_0|$ and ϕ , the Carter chart. (c) Impedance coordinates of $|r|=|R/Z_0|$ and $|x|=|X/Z_0|$, the Smith chart. (d) Admittance coordinates of $|g|=|G/Y_0|$ and $|b|=|B/Y_0|$, a variant of the Smith chart.

in Fig. 43-2. The reflected wave combines with the incident wave on the line to form a standing wave having an SWR (maximum to minimum) of

$$S = \frac{1+\rho}{1-\rho}$$

The presence of the standing wave increases the maximum voltage and current limits on the line for the same delivered power by the ratio \sqrt{S} . The efficiency η of the line may be expressed by

$$\eta = \frac{S_2 - 1/S_2}{S_1 - 1/S_1}$$

$$= \frac{4S_1}{10^{0.14}(S_1 + 1)^2 - 10^{-0.14}(S_1 - 1)^2}$$

where subscripts 1 and 2 refer to the load and source ends of line, respectively, and A is the normal line attenuation in decibels.

Reflection-Coefficient Charts

The reflection coefficient is a vector quantity related directly to impedance ratio and mismatch. Its magnitude does not exceed unity, so a plot of all possible reflection ratios for passive impedances may be charted within a circle of unit radius (see Fig. 43-3 a). Furthermore, the representations of a mismatch referred to different distances along the length of a line lie at a constant radius from the center of the chart at angles proportional to the distances. Coordinate systems of immittance normalized to the characteristic or reference immittance are superimposed to give the useful Carter and Smith charts, ^{2,3} shown in skeleton form in Fig. 43-3b, c, and d. Usage varies on the orientation of the axes. Positive interpretation is aided by labels for open- and short-circuit points and inductive and capacitive sides.

43-2 IMPEDANCE MATCHING WITH LUMPED ELEMENTS

Throughout the lower range of radio frequencies, it is convenient to use lumped reactance elements such as coils and capacitors in impedance-matching networks. In higher frequency ranges, pure inductance or capacitance may not always be obtained from practical elements, but it is convenient to analyze circuits in terms of their lumped reactance (and resistance) elements.

Any two complex impedances may be matched by a simple L section of two reactance elements. If, in addition to matching, it is necessary to maintain given phase relationships between the source and load voltages and currents, a third element must be used to form a T or π section. A lattice section using four elements is more convenient for some applications. The primary use of the simple sections is for matching at a single frequency, although it is possible to obtain matching at two or more separate frequencies by replacing each reactance element of the basic network with a more complex combination giving the required reactance at each specified frequency. Har-

monic reduction can be effected in a similar manner by introducing high series reactances or low shunt reactances at the harmonic frequencies.

L Section

The expressions for the required reactance values for an L section providing a match between pure resistances is shown in Fig. 43-4a. (Here and in the remainder of this chapter, X and B will designate reactance and susceptance values respectively.) If X_s is positive, the network will delay the phase of the wave by angle θ . If X_s is negative, it will advance the phase by that angle. The reflection coefficient of R_1 with respect to R_2 is reduced by a factor of at least 10 over a frequency ratio of at least 1.1 by introducing the proper L section of one capacitor and one inductor for R_2/R_1 , up to 2.0.

If two complex terminations are to be matched, the series reactance X', is made to include a compensation for the series reactance of the right-hand termination and the shunt susceptance B'_p is made to include the susceptance of the left-hand termination as shown in Fig. 43-4b. For this case θ represents the phase between the current in the left- to the voltage on the right-hand termination.

T and π Sections

Design expressions are given in Fig. 43-5 for T and π sections matching between resistive terminations. If the terminations contain reactive or susceptive components, it is

$$X_{S}$$

$$X_{P} = \pm R_{2} \sqrt{\frac{R_{1}}{R_{2} - R_{1}}} = -\frac{1}{B_{P}}$$

$$X_{S} = \mp \sqrt{R_{1} R_{2} - R_{1}^{2}}$$

$$R_{2} R_{2} > R_{1}$$

$$X_{S} = \pm R_{2} \sqrt{\frac{R_{1}}{R_{2} - R_{1}^{2}}} = -\frac{1}{B_{P}}$$

$$X_{S} = \pm \sqrt{R_{1} R_{2} - R_{1}^{2}}$$

$$MUST BE OF OPPOSITE SIGN X_{P} X_{S} = -R_{1}R_{2}$$

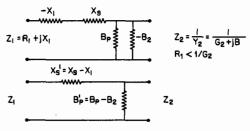
$$R_{2} > R_{1}$$

$$R_{2} > R_{2} > R_{1}$$

$$R_{2} > R_{2} > R_{1}$$

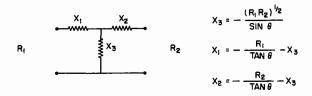
$$R_{2} > R_{2} > R_{1}$$

A. L SECTION FOR MATCHING BETWEEN RESISTANCES

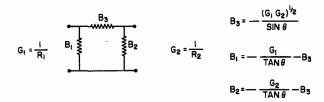


 L SECTION FOR MATCHING BETWEEN COMPLEX IMPEDANCES

FIG. 43-4 Impedance matching with reactive L sections.



A. T SECTION FOR MATCHING BETWEEN RESISTANCES



B. π SECTION FOR MATCHING BETWEEN RESISTANCES FIG. 43-5 Impedance matching with reactive T and π sections.

necessary to include an appropriate compensating component in the end elements as in the case of the L section.

L, T, and π sections may be used in unbalanced circuits as shown or in balanced circuits by moving one-half of each series element to the opposite conductor of the line. The lattice section is inherently balanced.

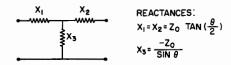
Lattice Section

The elements of a lattice section as well as T and π sections are given in Fig. 43-6 in terms of an equivalent transmission line having the same characteristic impedance and phase shift. The required equivalent line may be determined as described in latter parts of this section.

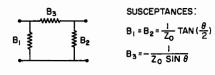
Inductive Coupling

A pair of inductively coupled coils is useful in a wide variety of impedance-matching circuits. Figure 43-7 shows two possible equivalent circuits of lossless coupled coils. The first is expressed in terms of reactance elements, including the mutual reactance X_m . The second is in terms of susceptance elements including the transfer susceptance B_T . (The transfer susceptance is the susceptance component of the transfer admittance, which is the ratio of the current induced in the short-circuited secondary to the voltage applied to the primary.) If capacitive tuning reactances are added, the equivalent circuits can be proportioned in accordance with the T and π matching sections described above. The capacitive reactances required for (1) series tuning and (2) parallel tuning are given in Fig. 43-8 for matching from R_1 to R_2 .

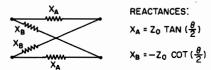
The series and parallel capacitors may be used for tuning out the series reactance or shunt susceptance, respectively, of a complex termination.



A. T SECTION



B. π SECTION

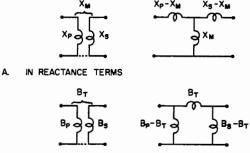


C. LATTICE SECTION

FIG. 43-6 T, π , and lattice equivalents of transmission-line section of characteristic impedance Z_0 and electrical length θ .

Lumped Matching Reactance

The standing wave on a transmission line may be eliminated on the source side of a matching reactance that is properly proportioned and positioned, as shown in Fig. 43-9. The choice of series or parallel connections, inductive or capacitive elements, may be determined by the position of the standing-wave pattern and other practical considerations.



B. IN SUSCEPTANCE TERMS

FIG. 43-7 Inductively coupled circuits and equivalent T and π sections.

$$X_{C1} = -X_{P} - R_{1} \left(\frac{X_{M}}{R_{1}R_{2}} - 1 \right)^{1/2}$$

$$X_{C2} = -X_{P} - R_{2} \left(\frac{X_{M}}{R_{1}R_{2}} - 1 \right)^{1/2}$$

$$X_{C2} = -X_{P} - R_{2} \left(\frac{X_{M}}{R_{1}R_{2}} - 1 \right)^{1/2}$$

$$\theta = SIN^{-1} \left(-\frac{\sqrt{R_{1}R_{2}}}{X_{M}} \right)$$
A. SERIES TUNING
$$X_{C1} = -\frac{1}{1}B_{C1} \qquad B_{C1} = -B_{P} - G_{1} \left(\frac{B_{M}}{G_{1}G_{2}} - 1 \right)^{1/2}$$

$$X_{C2} = -\frac{1}{1}B_{C2} \qquad B_{C2} = -B_{S} - G_{2} \left(\frac{B_{M}}{G_{1}G_{2}} - 1 \right)^{1/2}$$

$$X_{C3} = -\frac{1}{1}B_{C3} \qquad B_{C3} = -B_{C3} - G_{2} \left(\frac{B_{M}}{G_{1}G_{2}} - 1 \right)^{1/2}$$

$$X_{C4} = -\frac{1}{1}B_{C4} \qquad B_{C4} = -B_{C4} - B_{C4} - B_{$$

FIG. 43-8 Tuned inductively coupled circuits for matching between resistances.

43-3 IMPEDANCE MATCHING WITH DISTRIBUTED ELEMENTS

In many frequency ranges, it is desirable to use sections of transmission line having distributed reactances rather than lumped reactances in the form of coils and capac-

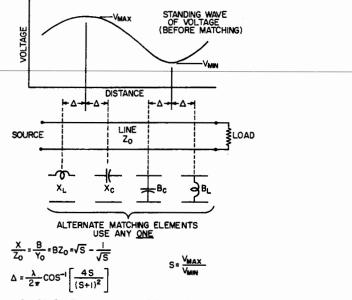


FIG. 43-9 Determination of lumped reactance to match a transmission line.

itors. The lines are usually proportioned to yield negligible loss so that the following expressions for impedance relationships in lossless lines apply:

$$Z_{\text{in}} = Z_0 \frac{Z_L \cos \beta \ell + j Z_0 \sin \beta \ell}{Z_0 \cos \beta \ell + j Z_L \sin \beta \ell}$$
= input impedance of line Z_0 , $\beta \ell$ terminated in Z_L
(43-1)

For a short-circuited line, $Z_L = 0$, so that

$$Z_{\rm in} = Z_{\rm oc} = jZ_0 \tan \beta \ell \tag{43-2}$$

For an open-circuited line, $Z_L = \infty$, so that

$$Z_{\rm in} = Z_{\rm oc} = -jZ_0 \cot \beta \ell \tag{43-3}$$

Transmission-Line Stubs

Lengths of transmission line short-circuited or open-circuited at one end are often used as reactors in impedance-matching circuits. Inspection of Eqs. (43-2) and (43-3) will show that the designer by choice of characteristic impedance and line length has control of reactance value and slope (with respect to frequency) at any given frequency. Alternatively, the designer has control of the value of reactance at any two frequencies. The available slope of reactance is always greater than unity, the value obtained from a single lumped reactance element. Unfortunately, the available slope of reactance is always positive, although a negative slope would be ideal in many applications. However, an effect similar to that of a series-connected or parallel-connected reactance having the unattainable negative slope may often be obtained over a limited frequency range by the use respectively of a parallel-connected or series-connected reactance.

General Line Transformer

The expression for Z_{in} [Eq. 43-1] may be recast to relate generator and load impedances ($Z_G = R_G + jX_G$, $Z_L = R_L + jX_L$) to the characteristic impedance and electrical length of a line section, providing a perfect match between them. The new expressions are

$$Z_{0} = \sqrt{\frac{R_{L}|Z_{G}|^{2} - R_{G}|Z_{L}|^{2}}{R_{G} - R_{L}}}$$

$$= \sqrt{\frac{|Z_{G}Z_{L}| \frac{R_{L}|Z_{G}|}{R_{G}|Z_{L}|} - \frac{|Z_{L}|}{|Z_{G}|}}{1 - \frac{R_{L}}{R_{G}}}}$$

$$\tan \beta \ell = \frac{Z_{0}(R_{L} - R_{G})}{R_{L}X_{G} - R_{G}X_{L}}$$

$$= \frac{Z_{0}(X_{G} - X_{L})}{R_{L}R_{G} + X_{L}X_{G} - Z_{0}^{2}}$$

For Z_0 to be a positive finite real number, it is necessary that

$$\frac{1}{2} < \frac{\log \left| \frac{Z_L}{Z_G} \right|}{\log \left(\frac{R_L}{R_G} \right)} < \infty$$

Instead of using the above expression for $\tan \beta \ell$, one may determine $\beta \ell$ from a plot of Z_L/Z_0 and Z_0^*/Z_0 on a Carter chart or a Smith chart once Z_0 has been determined. The two points will be at the same radius. The electrical angle measured clockwise from Z_L/Z_0 to Z_0^*/Z_0 is $\beta \ell$. (Note that $Z_0^*=R_G-jX_G$.)

The Z_0 and $\beta\ell$ quantities for the required line section may be used to compute T, π , and lattice sections of lumped reactances to perform the same function by using expressions given in Fig. 43-6.

Line Transformer for Matching to Resistance

For the frequently encountered case in which either the load impedance or the source impedance is a pure resistance, a solution for the required matching line may be

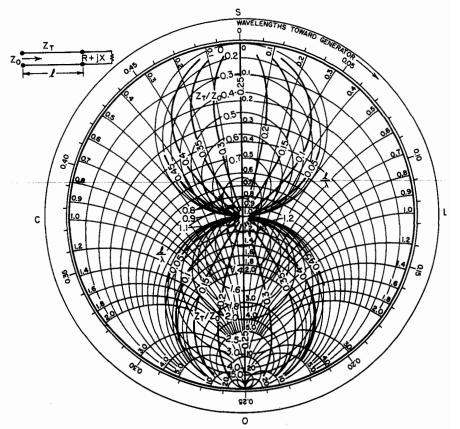


FIG. 43-10 Line transformer to match to a resistance.

obtained from Fig. 43-10. The complex impedance R+jX is located on the Smith chart in terms of its normalized components R/Z_0 and X/Z_0 , where Z_0 is the resistance to which a match is desired. The point so found is located within an area having a second set of coordinates if a solution is possible. These coordinates Z_T/Z_0 and ℓ/λ give the characteristic impedance and length of the required line.

Quarter-Wave Transformer

The useful quarter-wave transformer results from the general line transformer when $\beta \ell = \pi/2$. It has an impedance-inverting property, as seen from an inspection of

$$Z_{\rm in}=\frac{Z_0^2}{Z_L}$$

The input impedance is thus proportional to the reciprocal of the load impedance. The phase angle of the input impedance is the negative of that of the load impedance. The quarter-wave line can be used, for example, to transform an inductive low impedance to a capacitive high impedance.

The quarter-wave transformer is often used to match between different resistance levels. In this case

$$Z_0 = \sqrt{R_1 R_2}$$

In a mismatched coaxial line a quarter-wave transformer formed by a simple sleeve can be used to tune out the reflection. The sleeve forms an enlargement of the inner conductor or a constriction of the outer conductor which may be stationed where required. The characteristic impedance of the line is reduced over the quarter-wave length by the sleeve to a value of

$$\frac{Z_0}{\sqrt{S}}$$

where S is the initial SWR of the line. The load end of the sleeve is positioned at a voltage minimum on the standing-wave pattern. The impedance, here looking toward the load, is Z_0/S . The transformer transforms this to Z_0 so that the line on the source side is perfectly matched.

Z_o Trimmer

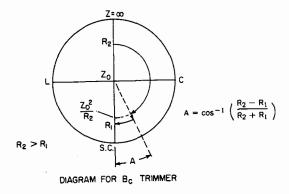
The transformation ratio of a quarter-wave section can be adjusted by a reactive trimming immittance, as shown in Fig. 43-11, to obtain a match when other control of circuit values is not convenient. The immittance required is approximated by

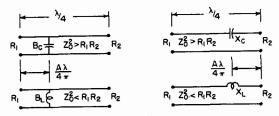
$$|X/Z_0| = |B/Y_0| = 2.29 \log (R_1 R_2/Z_0) / \sin A$$
 for $2/3 \le R_1 R_2/Z_0 \le 3/2$

The resulting network is nearly equivalent to a line for which $Z_0 = R_1 R_2$.

Frequency Sensitivity of Line Transformer

The mismatching effect of a departure from the design frequency for the general line transformer (and hence the quarter-wave transformer) can be estimated from Fig. 43-12.





ALTERNATE FORMS OF TRIMMER

FIG. 43-11 Reactive transformation trimmer for a quarter-wave transformer.

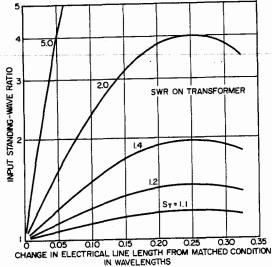


FIG. 43-12 Frequency sensitivity of a transmissionline transformer.

Cascaded Quarter-Wave Transformers 4,5

A number of quarter-wave transmission-line sections may be arrayed in cascade to realize great improvement in wideband performance over a single-section transformer. The characteristic impedances of the successive sections are proportioned to divide the overall transformation systematically. Figure 43-13 defines the terms that will be used in the discussion below.

Binomial Transformer

The binomial (or binomial-coefficient) distribution gives almost maximally flat performance. In this distribution the logarithms of the impedance ratios of the steps between sections are made to be in the ratio of the binomial coefficients.

Table 43-1 may be used to determine the characteristic impedance Z_n of the *n*th section in an *N*-section binomial transformer as a function of R_2/R_1 .

The input SWR of an N-section binomial transformer can be expressed by $S = 1 + (\cos \theta)^N \ln \frac{R_2}{R_1}$

N=1

$$R_1 = \frac{Z_1 = R_0}{Z_1} R_2$$

N=2

 $R_1 = \frac{Z_1}{Z_2} = R_0 Z_3 R_2$

N=3

 $R_1 = \frac{Z_1}{Z_2} = \frac{Z_2}{Z_3} = \frac{Z_4}{Z_5} R_2$

N=4

 $R_1 = \frac{Z_1}{Z_2} = \frac{Z_2}{Z_3} = \frac{Z_4}{Z_5} = \frac{Z_4}{Z_5} R_2$

N=6

 $R_1 = \frac{Z_1}{Z_2} = \frac{Z_2}{Z_3} = \frac{Z_4}{Z_5} = \frac{Z_6}{Z_6} = \frac{Z_6}{R_2}$
 $R_1, R_2 = \text{TERMINATING RESISTANCES}$
 $R_1 < R_2$
 $R_0 = \sqrt{R_1 R_2} = \text{MEAN IMPEDANCE}$

SECTIONS ARE EACH A QUARTERWAVE AT form of the properties of

FIG. 43-13 Cascaded quarter-wave transformers.

N =	7 =	2	3	4	5	6	7
2	½ ¼	%					
3	<i>7</i> 4 1∕4	%	%				
4	ж Жв	% 56	11/16	¹ /16			
5	/10 1/22	% ₂	16/32	26/32	31/22		
6	164	% 4	22/64	42/64	57/64	63/64	
7	⅓ ₂₈	% ₂₈	29/ ₂₈	64/ ₂₈	99/128	120/128	127/128

TABLE 43-1 Design Ratios for Binomial

Ratios = $\frac{\log (Z_n/R_1)}{\log (R_2/R_1)} = 1 - \frac{\log (R_2/Z_n)}{\log (R_2/R_1)}$

where θ is the electrical length of each section. This expression is subject to the assumptions of small steps, zero-discontinuity capacitance, ^{6,7} and equal lengths of the sections.

The two-section transformer has maximally flat bandwidth curve for all transformation ratios. For other values of N the performance approximates the maximally flat curve for transformation ratios near unity.

Chebyshev Transformer

If a certain maximum reflection coefficient ρ_m may be tolerated within the operating band, an optimum design which allows the reflection coefficient to cycle between 0 and ρ_m within the band and to increase sharply outside the band is possible. This is called the Chebyshev transformer, since Chebyshev polynomials are used in its design.

The input SWR of the Chebyshev transformer is given by

$$S = 1 + \ln\left(\frac{R_2}{R_1}\right) \frac{T_N\left(\frac{\cos\theta}{\cos\theta_-}\right)}{T_N\left(\frac{1}{\cos\theta_-}\right)}$$

where $T_{M}(x)$ is the Chebyshev polynomial of mth degree defined by

$$T_0(x) = 1$$

$$T_1(x) = x$$

$$T_2(x) = 2x^2 - 1$$

$$T_{m+1}(x) = 2xT_m(x) - T_{m-1}(x)$$

and where θ is the electrical length of each section and θ_{-} is the length at f_{-} . The expression is subject to the same assumptions as were made in the bionomial case.

Another expression of Chebyshev transformer performance, which does not require the assumption of small steps, is

$$P_L = 1 + \frac{\left(\frac{R_2}{R_1} - 1\right)^2}{\frac{4R_2}{R_1}} \frac{T_N^2 \left(\frac{\cos \theta}{\cos \theta_-}\right)}{T_N^2 \left(\frac{1}{\cos \theta_-}\right)}$$

where P_L is the power-loss ratio defined by $1/(1 - |\rho|^2)$.

The above equation may be converted to an implicit relationship among four principal quantities, namely,

 R_2/R_1 , the transformation ratio

 $ho_{\it m}$, the maximum tolerable reflection coefficient within the band

N, the number of sections

F, the frequency coefficient

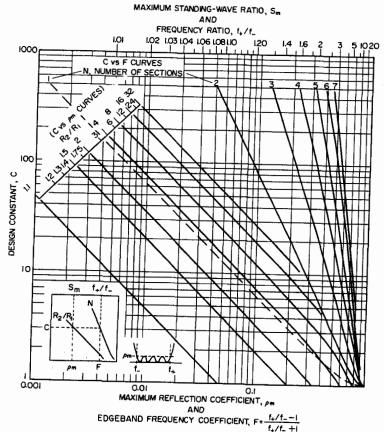


FIG. 43-14 Performance of Chebyshev transformer.

N	$\frac{\log (R_2/R_1)}{\log (Z_1/R_1)}$	$\frac{\log (Z_2/R_1)}{\log (Z_1/R_1)}$	$\frac{\log (Z_3/R_1)}{\log (Z_1/R_1)}$
2	$4-2C_1^2$		
3	$8-6C_1^2$		
4	$16 - 16C_1^2 + 2C_1^4$	$5-4C_1^2$	
5	$32 - 40C_1^2 + 10C_1^4$	$6-5C_1^2$	
6	$64 - 96C_1^2 + 36C_1^4 - 2C_1^6$	$7-6C_1^2$	$32 - 30C_1^2 + 9C_1^4$

TABLE 43-2 Design Ratios for Chebyshev Transformer

NOTE: $C_1 = \cos \theta = \cos \left[(1 - F) \pi / 2 \right]$

Any one of these may be determined by reference to Fig. 43-14 if the other three are known. Design constant C of Fig. 43-14 can be used as a measure of difficulty of transformation. It may be expressed as a function of R_2/R_1 and ρ_m or as a function of N and F:

$$C(R_2/R_1, \rho_m) = (R_2/R_1 - 1) \sqrt{(1/\rho_m^2 - 1)R_1/4R_2}$$

$$C(N,F) = T_N (1/\cos (\pi/2(1 - F))) \ge C(R_2/R_1, \rho_m)$$

The characteristic impedances may be calculated from functions given in Table 43-2. The impedance of the center section when N is odd is simply $\sqrt{R_1R_2}$ and is independent of F.

Dual-Band Transformers8

Multisection transformers can be synthesized for dual or multiple passbands by systematic distribution of the available reflection-coefficient zeros over the passbands. The series of impedance levels of the sections becomes nonmonotonic for a large frequency ratio between the two passbands. A nonmonotonic design for one operating band can be made with an arbitrarily short length by placing a second dummy passband at an arbitrarily high frequency.

Short-Step Transformer

A two-section transformer, as shown for N=2 in Fig. 43-13 but with a much shorter overall length at midband, is useful for narrow bandwidth or for transformation ratios near unity. Z_1Z_2 is set equal to R_1R_2 . The electrical length of each section at the exact-match or design frequency f_0 is set to

$$\beta \ell = \tan^{-1} \sqrt{\frac{R_2/R_1 - 1}{(Z_1/R_1)^2 - Z_2/Z_1}}$$

The length can be made as short as desired by selecting Z_1/Z_2 sufficiently high within limits imposed by increasing effects of abrupt discontinuities. Within the ranges $R_2/R_2 < 2$ and $Z_1/Z_2 < 2$, the total bandwidth 2 Δf is equal to $kf_0\rho_m/\rho_0$, where ρ_m/ρ_0 is the ratio of maximum inband reflection coefficient to the reflection coefficient

without the transformer, and k is a coefficient greater than unity. The coefficient becomes much greater than unity for $\beta\ell=\pi/8$ or more. The special case with $Z_1=R_2$ and $Z_2=R_1$ is a handy design for matching two dissimilar transmission lines simply by the use of sections of those lines. For this special case, $\beta\ell \le \pi/6$ and $k \ge 1.1$.

Much advanced theory has been developed for lumped-constant circuits. Useful adaptation to distributed-constant circuits is often possible by transformation of the frequency variable.9

43-4 TAPERED LINES

If the characteristic impedance of a long section of transmission line varies gradually with distance along the line, a nearly perfect match between resistive terminations may be obtained. Since a line of such length and such small taper can seldom be afforded, much attention has been directed toward the design of tapered lines giving acceptable transforming performance over short lengths and broad bandwidths. 10-21

Exponential Line

The exponential line is a simple form of tapered line that may be analyzed exactly with simple relations. Sections of exponential line are useful both as simple impedance transformers and as cascaded elements in a more complexly tapered line. The name comes from the function describing the magnitude of the characteristic impedance:

$$K_0(x) = \sqrt{L_x/C_x} = K_0(0) \exp \delta x$$

where L_x/C_x is the ratio of the per-unit-length inductance and capacitance of the line, δ is the taper constant, and x is the length coordinate that is positive in the direction of increasing impedance. Usually, the product L_xC_x is constant.

Above a critical cutoff frequency, the exponential line supports the propagation of independent characteristic waves traveling in opposite directions. The wave voltages are determined by the boundary conditions at the ends of the line. The impedance at any point or the reflection coefficient at that point may be found by transforming the known reflection coefficient at some other point. The analysis is like that for a uniform line except for several significant differences:

1 The characteristic impedance, which is the impedance seen by a traveling wave, is complex. The magnitude varies exponentially with x. The impedance phase varies with frequency and reverses sign with direction of travel.

$$Z_0(x) = K_0(x) \exp \pm j\phi_0$$
$$|\phi_0| = \sin^{-1} (\delta/2\beta)$$

where $\beta = 2\pi/\lambda$ is the phase constant for L_xC_x . The sign of ϕ_0 is positive for a wave traveling in the negative-x, or decreasing-impedance, direction and negative for the other direction. The characteristic impedances for oppositely traveling waves constitute a conjugate pair.

2 The characteristic waves propagate with a higher phase velocity and lower phase constant than on a uniform line with the same $L_x C_x$. The phase constant is $\beta_0 = \beta \cos \phi_0$.

- **3** The cutoff condition occurs for $\delta/2\beta=1$, $|\phi_0|=\pi/2$, and $\beta_0=0$. Traveling-wave analysis is not useful below the cutoff frequency.
- 4 A more general expression for the reflection coefficient of load Z_L must be used.

$$\rho = \frac{Z_L - Z_{0L}}{Z_L + Z_{0G}} = \frac{Z_L - Z_{0G}^*}{Z_L + Z_{0G}}$$

where Z_{0L} and Z_{0G} are the complex characteristic impedances seen looking toward the load and toward the generator, respectively. The (voltage) reflection coefficient at x with respect to $Z_0(x_1)$ for load Z_L at $x = x_1$ is

$$\rho_1 = \frac{Z_L - K_0(x_1) \exp \mp j\phi_0}{Z_L + K_0(x_1) \exp \pm j\phi_0}$$

where the upper or lower signs apply when the direction of looking into Z_L from the line is in the positive- or negative-x direction, respectively.

The corresponding reflection coefficient with respect to $Z_0(x_2)$ at $x = x_2$ a distance ℓ toward the generator is

$$\rho_2 = \rho_1 \exp - j2\beta_0 \ell$$

5 The input or driving point impedance at x_2 is

$$Z_{\text{in}}(x_2) = K_0(x_2) \exp(\mp j\phi_0) \frac{1 + \rho_2 \exp(\pm j2\phi_0)}{1 - \rho_2}$$

where the signs follow the same rule.

6 The traveling waves experience changing impedance, voltage, and current with x, but the reflection coefficient changes only in phase angle, not in magnitude. Thus, if a length of exponential line is well matched at the load end to a first-impedance level, the source end presents a well-matched impedance at another impedance level, related by the ratio $\exp \delta \ell$ to the first.

The exponential line is commonly employed to transform between two resistance levels equal to the magnitudes of characteristic impedance at the ends. Equal mismatches of opposite sense occur at the ends so that reflection zeros exist for section lengths of $n\pi$ rad where n is an integer. The reflection coefficient in the passband is

$$\rho = 0.5 \ln (R_2/R_1) \sin (\beta_0 \ell)/\beta_0 \ell$$

The mismatches at the ends may be improved by the use of reactive elements. 10,11

Other Tapered Lines

Several tapered lines²¹ are attractive for special simplicity in analysis. Optimum highpass tapers have been described in Refs. 13 and 14. The taper of Klopfenstein¹³ is optimum in the sense that for a given taper length the input reflection coefficient has the minimum peak magnitude or that for a specified peak magnitude the taper has the minimum length. The design is based on the multisection Chebyshev transformer, in which the number of sections is increased without limit to raise the upper cutoff frequency without limit. The resulting reflection coefficient in the passband is

$$\rho \exp(j\beta \ell) = 0.5 \ln (R_2/R_1) \cos [(\beta \ell)^2 - A^2]/\cosh A$$

where $\beta \ell$ is the electrical length. At the low-frequency cutoff, $\beta \ell = A$, and the length is approximately 0.019 (20 log cosh A) + 0.1 wavelength. Maximum inband reflection coefficient is

$$\rho_m = 0.5 \ln (R_2/R_1)/\cosh A$$

The characteristic impedance taper over the section length ℓ against coordinate x, measured from the midpoint of ℓ toward the high-impedance (or R_2) end, is

$$Z_0(x,A) = (R_1/R_2)^{1/2} (R_2/R_1)^{1/L}$$

Values of the function L for a wide range of cosh A are given in Table 43-3. The table is based on the following expressions evaluated by a simple routine of Grossberg:¹⁹

$$L(x) = -L(-x) = A^{2} \phi(2x/\ell, A)/\cosh A$$

$$\phi(2x/\ell, A) = -\phi(-2x/\ell, A) = \int_{0}^{2x/\ell} \frac{I_{1} (A\sqrt{1-y^{2}})}{A\sqrt{1-y^{2}}} dy$$

$$2x/\ell \le 1.0$$

where I_1 is the first kind of modified Bessel function of the first order.

TABLE 43-3 Values of the Function L for Klopfenstein Taper

		20 log	(cosh A)			
2x/l	20	30	40	50	60	70
0.0	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000
	0.058765	0.073036	0.084713	0.094889	0.104038	0.112422
0.10	0.117280	0.145568	0.168607	0.188594	0.206487	0.222811
	0.175301	0.217099	0.250881	0.279970	0.305820	0.329230
0.20	0.232583	0.287148	0.330773	0.367944	0.400634	0.429934
	0.288894	0.355261	0.407580	0.451551	0.489702	0.523442
0.30	0.344006	0.421013	0.480668	0.529960	0.572017	0.608 59 8
	0.397706	0.484017	0.549490	0.602495	0.646819	0.68 460 8
0.40	0.449793	0.543931	0.613597	0.668653	0.713613	0.751053
	0.500080	0.600460	0.672641	0.728109	0.772175	0.807880
0.50	0.548399	0.653361	0.726384	0.780718	0.822535	0.8553 69
	0.594597	0.702447	0.774696	0.826505	0.864957	0.894082
0.60	0.638543	0.747585	0.817555	0.865656	0.899908	0.9248 0 7
	0.680125	0.788700	0.855039	0.898497	0.928012	0.9484 8 7
0.70	0.719251	0.825770	0.887318	0.925470	0.950013	0.9661 5 0
	0.755851	0.858829	0.914647	0.947108	0.966722	0.9788 4 3
0.80	0.789876	0.887959	0.937349	0.964007	0.978975	0.987577
	0.821300	0.913291	0.955802	0.976799	0.987594	0.993283
0.90	0.850116	0.934994	0.970429	0.986124	0.993355	0.996772
	0.876338	0.953277	0.981675	0.992607	0.996955	0.998725
1.00	0.900000	0.968377	0.990000	0.996838	0.999000	0.999683

43-5 COMBINATIONS OF TRANSFORMERS AND STUBS

Transformer with Two Compensating Stubs

The simple quarter-wave transformer has rather poor performance over a wide band. Its wideband performance may be improved greatly by the addition of a compensating stub at each end, as shown in Fig. 43-15. The reactance introduced by each stub counteracts the variation with frequency of one-half of the transformer length at and near the design frequency. For the impedance proportions shown, the performance is maximally flat and comparable with that of a three-section binomial transformer.

Equiripple performance within the band, for a maximum reflection coefficient of ρ_m , is obtained with modified stub impedances. Table 43-4 lists some examples of equiripple performance, showing an improvement in bandwidth by a factor of about 1.2 over the maximally flat case for $\rho_m = 0.1 \ \rho_0$.

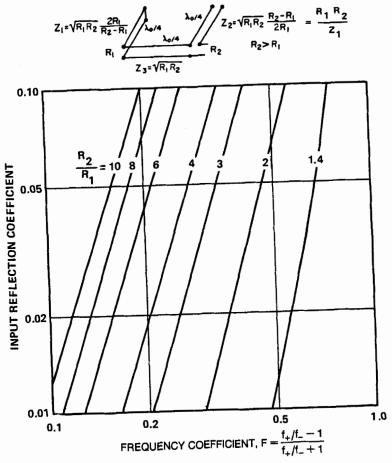


FIG. 43-15 Transformer with two compensating stubs; maximally flat case.

TABLE 43-4 Transformer with Two Compensating Stubs, Equiripple Case, $\rho_m = 0.1\rho_0$

R_2/R_1	$Z_2/Z_3=Z_3/Z_1$	Design F
2	0.6572	0.515
4	2.1205	0.351
6	3.6308	0.286
8	5.1574	0.248

Transformer with Single Compensating Stub

If it is convenient to use only one compensating stub with the transformer, one of the circuits shown in Fig. 43-16 may be used. In this equiripple design the allowable maximum standing-wave ratio S_m affects the choice of Z_1 and Z_2 .

Tapped-Stub Transformer

The tapped-stub transformer, shown in Fig. 43-17, is a useful circuit for matching between two widely different resistive terminations. The design chart shows the rela-

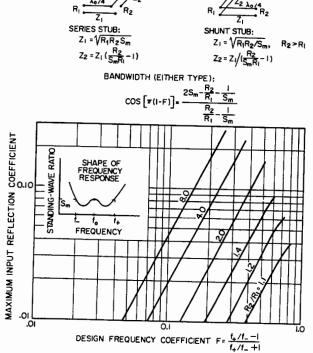


FIG. 43-16 Transformer with single compensating stub.

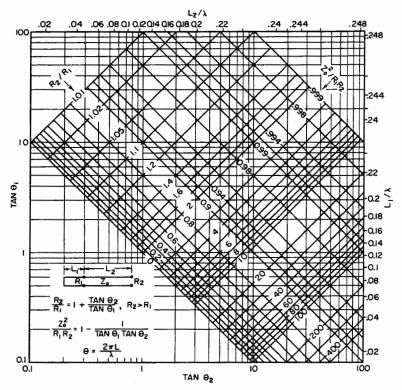


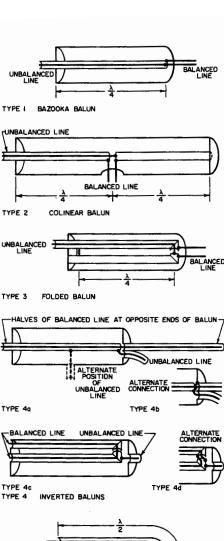
FIG. 43-17 Tapped-stub transformer.

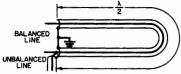
tionship existing between R_2/R_1 , Z_0^2/R_1R_2 , and the two line lengths L_1 and L_2 for the matched condition. The total stub length is a minimum of one-quarter wavelength and increases with increasing Z_0 . The chart is based on a lossless transmission line. For very high transformation ratios the effect of even a small loss is appreciable and must be accounted for separately. For moderate transformation ratios, a 5 or 10 percent bandwidth over which the maximum reflection coefficient is no more than $0.1(R_2 - R_1)/(R_2 + R_1)$ usually can be obtained.

43-6 BALUNS

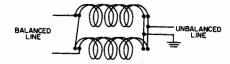
A balun is an impedance transformer designed to couple a balanced transmission circuit and an unbalanced transmission circuit. The impedance transformation may be accomplished usually with established techniques.^{22,23} The conversion between a balanced mode and an unbalanced mode, however, requires special techniques. Several basic techniques are exemplified by the balun types shown in Fig. 43-18.

A balanced circuit is obtained in type 1 by introducing a high impedance of a



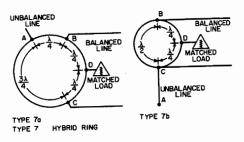


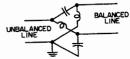
TYPE 5 HALF WAVE-LINE BALUN



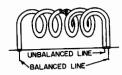
TYPE 6 BIFILAR-COIL OR ELEVATOR BALUN

FIG. 43-18 Basic types of baluns.

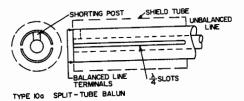




TYPE 8 LATTICE

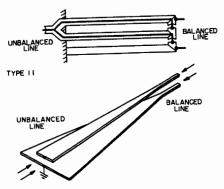


TYPE 9 COILED-CABLE BALUN



BALANCED LINE
TERMINALS

TYPE 106 THREE-WIRE BALUN



TYPE 12 TAPERED BALUN

resonant coaxial-choke structure between the outer conductor of the unbalanced coaxial circuit and ground. There is no counterpart of the choke impedance in the other side of the balanced circuit. Hence the balun does not present a well-balanced impedance at any frequency for which the choke impedance is not high.

The shortcoming of type 1 is overcome in types 2 and 3. Symmetry of the balanced circuit is maintained independently of frequency by a two-conductor choke (type 3) or by two identical opposed coaxial-choke cavities (type 2). The first three types have been widely used because of their simplicity and mechanical adaptability. The impedance bandwidth is limited by the shunting effect of the choke. Thus it is advantageous to keep the characteristic impedance of the choke lines as high as possible for wideband operation.

Type 4 represents an improvement for many applications, particularly those involving impedance-level transformation. Unlike types 2 and 3, type 4 has the balanced circuit in the innermost line. Coupling is attained through a gap between line sections, as before. The necessary choke cavity, however, is around this gap in the unbalanced side of the structure. An unbalanced or single-ended cavity can be used without disturbing the perfect balance. The connections at the gap may be either of the series type, as in types 4a and 4c, or of a parallel type, as in types 4b and 4d. The parallel connection results in a balanced-to-unbalanced impedance ratio of 4.

An additional impedance control is available in any of the type 4 baluns at some expense of bandwidth by application of the principle of the tapped-stub transformer. This is illustrated by the alternative position of the unbalanced line in the drawing of type 4a. The desired impedance transformation ratio determines the length of coaxial-choke line on each side of the unbalanced-line tap position in accordance with Fig. 43-17. Broadband compensation techniques²² may be applied to types 2, 3, and 4.

The type 5 balun employs a half-wave delay line. It is connected between the two balanced-line terminals as shown, forcing the potentials to ground to be equal and opposite at the design frequency. A balanced-to-balanced impedance ratio of 4 is obtained.

Type 6 employs helically wound transmission lines. At the unbalanced end, they are connected in parallel. Enough line length is used to develop high impedances to ground at the opposite ends. There the lines are connected in series to form the balanced terminals. A balanced-to-unbalanced impedance ratio of 4 is obtained.

Type 7a is a conventional $6\lambda/4$ hybrid ring which operates similarly to type 5. The path length from A to C is one-half wave longer than the path from A to B. Each path is an odd number of quarter waves long so that impedance transformation may be incorporated by proper selection of wave impedances. Furthermore, a load resistor at D is connected to terminals B and C by quarter-wave lines. This arrangement tends to dissipate the energy in an unbalanced wave without affecting a balanced wave.

Type 7b is a $4\lambda/4$ hybrid ring that operates similarly, except that the impedance-matching function is performed by the separate quarter-wave line AC.

Type 8 is the familiar lattice circuit. In it the incoming unbalanced wave energy is divided equally between two channels, one providing a 90° lead, the other a 90° lag. The output voltage is balanced with respect to ground and is in quadrature with the input voltage. The lattice may be proportioned to match any two resistance values.

Type 9 is similar in principle to type 6. It is most suitable for operation at the longer wavelengths where the size of a type 4 tends to become excessive. It may be connected for an impedance ratio of 1 or of 4.

Type 10a is a convenient balun type for feeding balanced dipoles. The slotted

portion of transmission line supports two modes of transmission simultaneously. Energy in a coaxial mode from the unbalanced input is substantially unchanged by the presence of the slots. The field of this mode is almost completely confined within the outer conductor. There is also a balanced mode in which the halves of the slotted cylinder are at opposite potentials and the center conductor is at zero potential. The field is not confined to the space within the slotted cylinder. (If leakage and radiation are to be minimized, another cylinder may be added overall for shielding.) The connection strap between the inner conductor and one-half of the slotted cylinder requires that the coaxial-mode voltage be equal and opposite to that half of the balanced-mode voltage. Thus a balanced-to-unbalanced impedance ratio of 4 is obtained.

Type 10a will give almost perfect balance over a wide frequency range if the slot width is kept small and symmetry is maintained at the strap end. A variation of this basic type of balun is the three-wire balun shown in type 10b. It is sufficiently well

balanced for use in noncritical applications.

Type 11 illustrates another method by which an impedance transformation may be obtained by a connection independently of frequency. Two coaxial lines are connected in parallel at the unbalanced terminal and in series at the balanced terminal. A third cylinder is added to preserve symmetry. The impedance transformation ratio for this structure having two lines is 2^2 , or 4. More coaxial lines could be added to give impedance transformation ratios of 9, 16, etc., but practical limits are soon reached in this direction. Bifilar coils can also be used in a balun operating on this principle.

Baluns, for example, those of types 1 through 4, 6, 9, and 11, can be improved for very wideband operation by the inclusion of such high-permeability materials as ferrite or powdered iron. The material in the form of toroidal cores, cylindrical cores, pot cores, or beads, placed in the magnetic field of a low-frequency-limiting shunt element, increases the length of that element, raises its impedance, and improves the low-frequency match. The influence of the material is much less at the high-frequency end, which can be as high as 1 GHz, because of a reduced effective permeability. Compact baluns and transmission-line transformers of the bifilar-coil and coiled-cable types, having ferrite cores, typically operate over bandwidths of two to three decades. ^{24,25} Core loss is low because the core does not interact strongly with the transmission-line mode.

The wideband balun of type 12 is a half wave or more of tapered transmission line that converts gradually, in cross-sectional characteristics, from an unbalanced line (coaxial line or stripline) at a first impedance at one end to a balanced two-conductor line at a second impedance at the other end, using a Chebyshev taper. 26,27

43-7 BROADBANDING

The most general problem of broadbanding is that of synthesizing a circuit to match one arbitrary impedance to another arbitrary impedance over a prescribed frequency range to within a prescribed tolerance. Fortunately, the broadbanding problems found in practice involve impedances that are not completely arbitrary, inasmuch as they are composed of a combination of physically realizable inductances, capacitances, and resistances. A further simplification of the broadbanding problem often occurs because at least one of the impedances to be matched usually is the characteristic impedance of a transmission line and thus is either constant and resistive or nearly so.

Nevertheless, the impedances to be matched are functions of frequency that usually are too complex for simple analysis. An iterative approach is often taken. The subject impedance, prescribed by theoretical or experimental data, is examined to perceive a suitable step toward optimum broadbanding. Graphical representations of the function are usually helpful for this. The matching network or a portion of it is added to the circuit. The resulting impedance is found by calculation or experiment. The steps are repeated until the required broadband match is obtained. Modern computational tools and measuring instruments minimize the tedious detail and impart the needed accuracy and so make the iterative approach rapid and efficient.

The problem of matching two resistive impedances is treated in earlier parts of this section. The problem of matching a load of frequency-varying impedance to a constant resistance is so common that the following discussion will be limited to this case.

Several broad rules that apply to broadbanding practice are given, as follows:

- 1 The difficulty of obtaining a prescribed tolerance of match increases with the required bandwidth. Refer to performance charts of a Chebyshev transformer for an example of this and of the following rule.
- 2 The difficulty increases with transformation ratio (expressed as a quantity greater than 1).
- 3 The difficulty increases with the electrical length of the transmission circuit between the load and the first point of control.
- 4 Improvement of match throughout one sector of the frequency range will generally be accompanied by an increase in mismatch in other sectors of the frequency range.
- 5 Any physically realizable passive impedance plotted on the reflection-coefficient plane, using the conventions of Fig. 43-3, displays a circular or spiral motion having a clockwise sense of rotation with frequency.

The effect of a length of mismatched transmission line between the load terminals and the first impedance-matching control is to introduce an additional variation with frequency that is seldom favorable over an appreciable bandwidth (Rule 3). For this reason it is advantageous to conduct impedance-matching control at a position close to the load terminals. In fact, if control of the load impedance is available from within the load itself, advantage should be taken of this circumstance to select the most suitable shape and position of the impedance locus on the reflection-coefficient plane.

Transformation of the given impedance locus on the chart to one that is compactly situated about the desired impedance point requires, first, a method of moving the impedance locus and, second, a method of compensating for the variation with frequency inherent in the original impedance locus and that introduced by the moving process. Means for moving the impedance locus may include lumped or distributed constant elements forming shunt or series reactances, cascade transformers, or a combination of these. Selection is made to introduce as little adverse variation of impedance with frequency as possible.

Compensation of variation of impedance with frequency is usually limited to a band including less than one complete convolution of the original impedance locus if a high degree of compensation is required. Typically, a sector of the original impedance locus which may be made to appear similar to those shown in Fig. 43-19 is

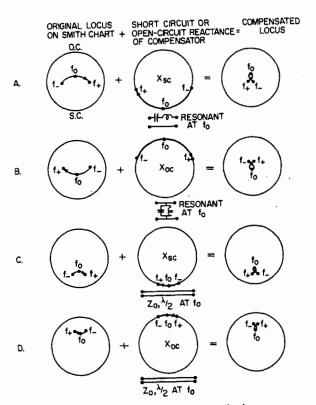
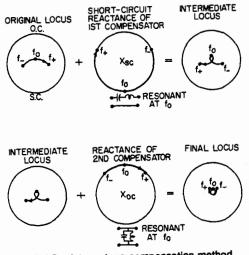


FIG. 43-19 Broadband compensation methods.

ORIGINAL LOCUS



INTERMEDIATE LOCUS

FIG. 43-20 A two-stage compensation method.

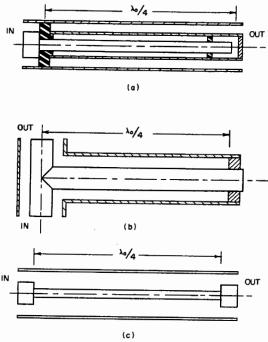


FIG. 43-21 Possible physical embodiments of Fig. 43-19.

selected. Then a matching circuit having a variation of reactance of opposite sense (and of the proper magnitude) is added to yield the tightly knotted transformed locus as shown. Essentially all the reactance variation may be eliminated; however, a small reactance variation and a larger resistance variation remain. In certain instances it may be advantageous to utilize two stages of compensation, as illustrated in Fig. 43-20, in order to accomplish a doubly knotted transformed locus.

There are many ways of forming these matching circuits into physical structures.

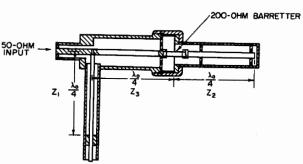


FIG. 43-22 Structure to match barretter to $50-\Omega$ impedance.

A few simple examples are shown in Fig. 43-21. A more complex structure utilizing a transformer with two compensating stubs in a circuit described earlier in this chapter is shown in Fig. 43-22.

Resonant lengths of the transmission line may be used in place of the lumped-constant resonant circuits. The LC product or the length of the line is selected for resonance at f_0 , the midfrequency of the sector. The L/C ratio or the characteristic impedance of the line section is selected to give the proper amount of compensating reactance at f_+ and f_- , the edge-band frequencies.

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Radomes

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44-1 General Discussion 44-2
Definition and Function 44-2
Electrical Considerations 44-3
Environmental Considerations 44-4
Radome Materials 44-6

44-2 Radome Configurations 44-7 Shape 44-7 Wall Structure 44-8

44-3 Electrical-Design Data 44-13
General 44-13
Design Procedure 44-13
Electrical Effects 44-14
Aerothermal Analaysis 44-19

44-4 Fabrication and Testing 44-19
Fabrication 44-19
Mechanical Testing 44-20
Electrical Testing 44-21

Definition and Function

A radar dome, or radome, is a protective dielectric housing for a microwave or millimeter-wave antenna. The function of the radome is to protect the antenna from adverse environments in ground-based, shipboard, airborne, and aerospace applications while having insignificant effect on the electrical performance of the enclosed antenna or antennas. The frequency band of application for radomes is approximately from 1 to 1000 GHz.

Radomes are generally composed of low-loss dielectrics of thickness comparable to a wavelength which are shaped to cover the antenna and, if necessary, to conform





FIG. 44-1 Two airborne radome applications. (a) Relatively blunt aircraftnose radome. (b) Streamlined missile radome.

to aerodynamic streamlining (Fig. 44-1). Radomes are used with virtually all aperture-type airborne antennas and with many ground-based and shipboard aperture antennas which must withstand severe weather conditions, blast effects, or water pressures (submarine applications). In most applications, the radome must be large enough to allow scanning of the antenna inside the radome.

Electromagnetic windows and radants are variations of the radome. Originally, an electromagnetic window was a planar or slightly curved dielectric covering for a stationary antenna. Original applications included protective covers for communications and radar altimeter antennas on reentry spacecraft where temperatures in excess of 2000°F were encountered and ceramic materials were required.² A radant is a radome which includes the antenna as an integral part; e.g., antenna elements imbedded in a streamlined dielectric nose structure for an aircraft.³ Currently, the term electromagnetic window applies to all types of radomes, windows, and radants.

Electrical Considerations

A radome always changes the electrical performance of the antenna because of wave reflections and refractions at interfaces between material media and because of losses in the radome materials. These changes manifest themselves as pattern distortion (Fig. 44-2), including changes in gain, sidelobe levels, beamwidth, null depth, and polarization characteristics. ^{4,5} For tracking antennas, boresight errors are invariably introduced by a streamlined radome; for proportional navigation systems, the rate of change of boresight error with antenna scan (boresight-error slope or rate) can be a major problem. ^{5,6} Excessive reflections from the radome may cause magnetron pulling. For high-power applications, excessive losses in the radome material may raise its

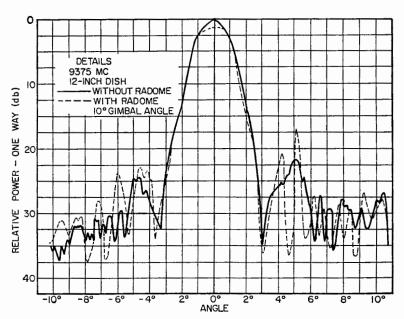


FIG. 44-2 Typical radiation patterns showing the effects of the radome.

temperature to a point at which its structural properties and electrical performance are degraded.⁷ Radome losses also will raise the system noise temperature.

Radome effects can be qualitatively explained and understood in terms of TEM (plane) wave propagation through and reflection from planar dielectric panels. The curved radome wall is considered to be locally plane at each point. Waves emanating from the enclosed transmitting antenna are also considered to be locally plane at each point of incidence on the radome wall. The reflected and transmitted waves can then be approximated from plane-sheet theory, and the resultant effects on overall antenna performance can be calculated. By reciprocity, the effect of the radome on the antenna as a receiver can be determined in the same manner.

The transmission properties of a plane dielectric sheet vary with frequency, incidence angle, and polarization of the incident plane wave. In Fig. 44-3, the plane of incidence is defined by the unit normal $\hat{\mathbf{n}}_{0s}$ and the direction of wave propagation $\hat{\mathbf{k}}$. The incidence angle is given by $\sin^{-1}(\hat{\mathbf{k}} \times \hat{\mathbf{n}}_{0s})$. Arbitrary wave polarizations are resolved into an electric field component perpendicular to the plane of incidence (E_{i1}) and a component parallel to the plane of incidence (E_{i1}) . The power-transmission coefficient (transmittance) and insertion phase delay (IPD) are generally different for the two polarizations, so that the polarization, power density, and phase of the transmitted wave are different from those of the incident wave. (The insertion phase is the phase of the transmitted wave relative to the phase of the incident wave at the same point if the panel were removed. IPD is the negative of the insertion phase.)

The electrical characteristics of flat panels are important because radome-wall design is based on them. Refinements in the wall design are often determined from subsequent analyses which account for antenna and radome geometry and for radome-wall curvature. A number of computer-aided analyses have been developed for this purpose and will be described below.

Environmental Considerations

The operating environment of a radome is the primary factor in determination of material type, wall design, and radome shape. Temperature, structural loads, vibration, wind, sand, hail, and rain are to be considered in an initial design.

For ground-based radomes, wind loading is the most important factor in the selection of a radome design. Other factors to be considered are humidity, blowing dust or sand, rain, ice, snow, and moisture buildup on the outer wall. The radome configuration and mounting scheme evolve from these environmental considerations and the desired electrical performance. Typical ground-based structures include the metal space-frame, and with monolithic-wall, and inflatable radomes.

Missile and aircraft radome designs are dictated primarily by aerodynamic loading and the thermal environment. The radome design becomes a trade-off of materials and shapes based on vehicle speed, trajectory, and desired electrical performance. Other design considerations include rain erosion, water absorption, and static electrification.

Mechanical stresses are produced in the radome by aerodynamic loading due to airflow, acceleration forces, and sudden thermal expansion due to aerodynamic heating (thermal shock). ¹² In high-speed radomes, thermal shock is perhaps more important than other mechanical loading factors. The attachment of the radome to the airframe can be a critical design problem in high-temperature applications.

Airborne-radome electrical performance is affected by the elevated temperatures

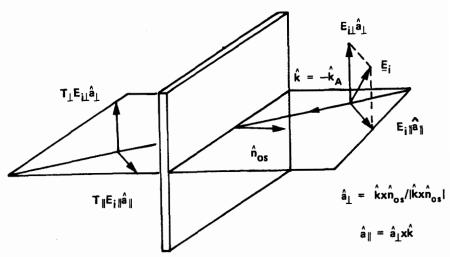


FIG. 44-3 Plane-wave propagation through a flat dielectric panel.

(up to 2300°F) caused by aerodynamic heating during flight. Dielectric constant and loss tangent normally increase or decrease with temperature, and the generally non-uniform heating of the radome produces changes in the boresight-error performance. Aerodynamic heating has been suspected of increasing boresight errors to a level to cause in-flight oscillations of a missile. Measurements made on Pyroceram radomes using concentrated solar energy for nonuniform radome heating have shown that measured changes in boresight error are significant.¹³

Rain erosion can be a severe problem in missile-radome operation and is a continuing problem in aircraft radomes for speeds over 250 mi/h (400 km/h). The radome shape, material type, and velocity influence rain erosion. Essentially all leading-edge surfaces are susceptible to raindrop impact, and a sharp-nose radome is less susceptible to rain damage than a blunted-nose radome. Rain erosion manifests itself as pitting of the radome surface and, in severe cases, catastrophic failure of the radome itself. Degradation of performance can result from rain erosion. Special rainerosion coatings, metal tips, and aerodynamic spikes are used to provide resistance to rain erosion.

Water absorption by the radome increases the dielectric constant and loss tangent of the radome wall; hence, materials which do not readily absorb water or ones which have been treated with protective coatings are used. Protective coatings for high-speed radomes must be selected carefully because charred residues may hamper electrical performance during the terminal phase of flight.¹⁴

Static electrification of radomes by moving air can present a serious shock hazard. Thin antistatic coatings are used to provide a means of conducting static charge to nearby structures for its safe neutralization. Lightning strikes to aircraft radomes are not uncommon, and metallic lightning-diverter strips are often employed on aircraft radomes. Antistatic coatings are usually thin at the wavelengths of interest, but they can produce some effects on electrical performance. Diverter strips also affect electrical performance. 16

Radome Materials

Electrical and structural performance and application are the prime factors in selection of the radome material. A number of thermal plastic materials, some of which are listed in Table 44-1 along with other organic radome materials, are suitable for radome use.¹⁷ A more comprehensive list of materials is presented in Chap. 46 and in Refs. 18 and 19.

The thermal plastic materials are limited to applications involving modest temperature increases, whereas the common laminates using the polyimide or polybenzimidazole resins can withstand temperatures near 750°F. For higher temperatures, either ceramic materials or ablative coatings are usually required. Fiber-loaded Teflon (Duroid) materials, depending on the specific application, can be used at very high temperatures for a short period of time.

The ceramic materials of prime interest are aluminum oxide, beryllium oxide, boron nitride (pyrolytic and hot-pressed), magnesium aluminate (spinel), magnesium oxide, silicon dioxide, sintered silica, and silicon nitride. The electrical properties of commonly used ceramic radome materials are tabulated in Table 44-2. The electrical parameters are a function of material density for the ceramics. The electrical properties of the organics (Table 44-1) are functions of both density and resin content.

A radome for multimode missile seekers requires materials that have low transmission losses at microwave, millimeter-wave, optical, and intermediate-range (IR) wavelengths. A number of materials offer the appropriate physical parameters for use at these wavelengths:²⁰ silica mullite, germanium mullite, boron aluminate, zinc germanate, thorium germanate, sapphire, Mg F₂, spinel, pollucite, hafnium titanate, aluminum nitride, calcium lanthanate sulfide, zirconia-toughened zirconia, and zirconiatoughened (Al, Cr) oxide.

For high-speed homing missiles, the most popular radome material has been Pyroceram 9606. Other materials in use include slip-cast fused silica and epoxy glass, of which the latter is used on lower-speed missiles. Duroid 5650 has been chosen as the

TABLE 44-1	Organic Radome	Materials	(8.5	×	10° Hz)
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Material	Dielectric constant	Loss tangent
Thermal plastics		
Lexan	2.86	0.006
Teflon	2.10	0.0005
Noryl	2.58	0.005
Kydox	3.44	0.008
Laminates		
Epoxy-E glass cloth	4.40	0.016
Polyester-E glass cloth	4.10	0.015
Polyester-quartz cloth	3.70	0.007
Polybutadiene	3.83	0.015
Fiberglass laminate polybenzimidazole resin	4.9	0.008
Quartz-reinforced polyimide	3.2	0.008
Duroid 5650 (loaded Teflon)	2.65	0.003

TABLE 44-2 Ceramic Radome Materials (8.5 × 10⁹ Hz)

Material	Density, g/cm³	Dielectric constant	Loss tangent
Aluminum oxide	3.32	7.85	0.0005
Alumina, hot-pressed	3.84	10.0	0.0005
Beryllium oxide	2.875	6.62	0.001
Boron nitride, hot-pressed	2.13	4.87	0.0005
	2.14	5.12	0.0005
Boron nitride, pyrolytic	3.57	8.26	0.0005
Magnesium aluminate (spinel) Magnesium aluminum silicate	2.44	4.75	0.002
(cordierite ceramic) Magnesium oxide	3.30	9.72 5.58	0.0005 0.0008
Pyroceram 9606		•	0.003
Rayceram 8	2.20	4.72 3.82	0.003
Silicon dioxide Silica-fiber composite (AS-3DX)	1.63	2.90	0.004
	1.93	3.33	0.001
Slip-cast fused silica Silicon nitride	2.45	5.50	0.003

best performer in a high-supersonic-rain environment. Silicon nitride also holds promise for such environments.

Polyurethane and fluoroelastomer coatings are generally used for rain-erosion protection and as antistatic coatings. ^{21,22,23} These are typically from 0.010 to 0.020 in (0.254 to 0.508 mm) thick. For higher-speed missiles, rain-erosion coatings of either polyurethane or neoprene are not used because of the higher temperatures involved. Duroid-material coatings appear to offer the radome designer a method to reduce rain erosion. ^{24,25} Duroid does ablate, and the resulting changes in wall thickness during flight should be considered in the radome electrical design. Ceramic coatings over plastic radomes have had limited success as rain-erosion coatings. Avcoat materials, which are ablative, can be used to provide thermal protection and rain-erosion resistance.

44-2 RADOME CONFIGURATIONS

Shape

Radome shape and wall structure comprise the radome configuration. Unstreamlined radome shapes include the cylinder, the sphere, and combinations thereof (Fig. 44-4). Since the incidence angles encountered in these shapes are usually less than 30°, such radomes are called normal-incidence radomes. The transmission properties of suitable wall structures are relatively independent of polarization and incidence angles between 0 and 30°, provided that small tolerances on thickness variations are maintained and that a narrow frequency band of operation is specified. Reflections are a problem in normal-incidence radomes since they may be returned directly to the antenna and increase the voltage standing-wave ratio (VSWR) in the feed system.²⁶

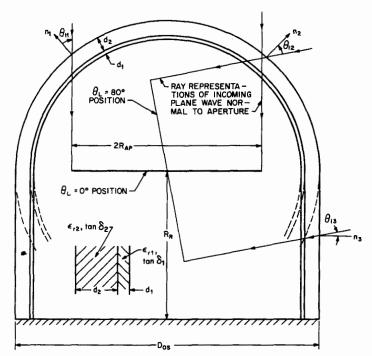


FIG. 44-4 Hemisphere-on-cylinder radome design for ground-based application.

Streamlined radome shapes are used primarily in airborne applications for aircraft and missiles. Common streamlined shapes are the ogive (Fig. 44-5), von Kármán, Sears-Haack, conical, ellipsoidal, power-series, and log-spiral.²⁷ Incidence angles range from 0 to 80° and higher, depending on the degree of streamlining as quantified by the ratio of radome length to diameter (fineness ratio). Fineness ratios typically range from 0.5 (hemisphere) to 3.26. Antenna-radome interaction (VSWR) is not significant in streamlined radomes, but focusing effects, Lloyd's mirror effect, and effects of trapped waves may cause significant resultant effects on electrical performance.²⁸

Radome shape affects both aerodynamic and electrical performance. Generally, the more streamlined shapes have less drag (hence, greater range) and more resistance to rain damage; however, electrical performance usually improves for less streamlined shapes. Sound radome-design practice dictates that radome-shape selection be coordinated to satisfy both aerodynamic and electrical requirements.

Wall Structure

Radome wall structures combine materials technology and plane-sheet electrical principles; whereas the former is continually changing to meet ever-increasing requirements, the latter remains as unchanged as Maxwell's equations. Common wall struc-

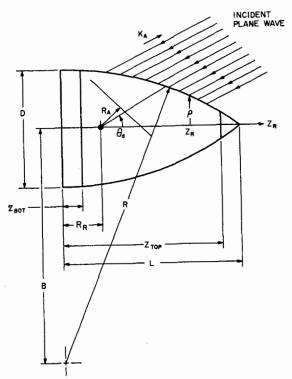


FIG. 44-5 Antenna-radome geometry for a tangent ogive radome.

tures include homogeneous single-layer (monolithic), multilayer, metallic, spaceframe, and grooved structures.

A monolithic-wall structure consists of a single slab of homogeneous dielectric material whose thickness is less than approximately one-tenth wavelength (thin-wall) or is an integer multiple of one-half wavelength in the dielectric (n-order half-wave design). Thin-wall designs are applicable at lower frequencies, at which the permissible electrical thickness (Fig. 44-6) also provides adequate strength and rigidity.

For adequate strength at higher frequencies, the monolithic-wall thickness is chosen according to

$$d = \frac{n\lambda}{2(\epsilon_r - \sin^2 \theta)^{\nu_2}} \tag{44-1}$$

where n = integer

 λ = free-space wavelength

 $\epsilon_r = \text{dielectric constant} = \epsilon/\epsilon_0$

 θ = incidence angle

The integer n is called the order of the radome wall. The case n = 1 is the half-wave wall. The angle θ at which Eq. (44-1) holds is called the design angle. For both per-

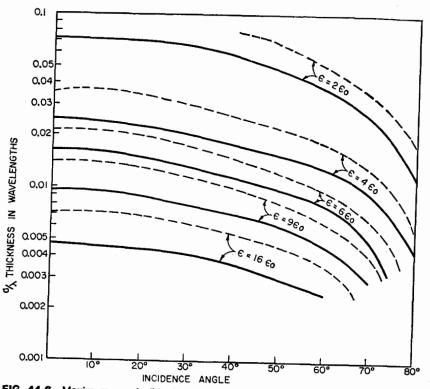


FIG. 44-6 Maximum permissible thickness of thin-wall radome versus incidence angle and dielectric constant for 95 percent power transmission (solid curves) and for 90 percent transmission (dashed).

pendicular and parallel polarization, reflection will be zero at this angle of incidence, maximum and equal transmittance will be obtained, and equal insertion phase delays will be introduced by the plane dielectric sheet. These features are illustrated in Fig. 44-7 for a low-loss alumina half-wave wall with design angle $\theta=55^{\circ}$. Equation (44-1) strictly holds for lossless materials but is a good approximation for the low-loss materials normally used for radomes. Complete transmission curves for monolithic wall designs can be found in Refs. 29 and 30.

The transmittance versus incidence angle for parallel polarization is always equal to or better than that for perpendicular polarization. In addition, at Brewster's angle defined by

$$\theta_B = \tan^{-1} \sqrt{\epsilon_r} \tag{44-2}$$

a transmittance of unity can be attained in the lossless case for parallel polarization and is independent of panel thickness. No similar condition exists for perpendicular polarization.

Monolithic radome walls are used in many ground-based and shipboard applications for which weight is not a problem and simplicity of design and construction is

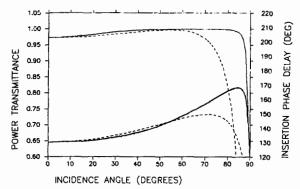


FIG. 44-7 Power transmittance (upper curves) and insertion phase delay versus incidence angle for alumina half-wave panel having a design angle of 55° for parallel (solid curves) and perpendicular (dash) polarizations ($\epsilon_r = 9.3$, $\tan \delta = 0.0003$, $d = 0.17\lambda$).

desired. Half-wave and full-wave walls are prevalent in ceramic missile radomes. Lighter sandwich structures are used in many aircraft and lower-speed missile applications.

Multilayer structures include the A sandwich, B sandwich, C sandwich, and others. The A sandwich consists of three layers: two thin, dense high-strength skins separated by a low-density (~10-lb/ft³) core material of foam or honeycomb. The B sandwich also consists of three layers: a dense core material with two lower-density skin materials which serve as quarter-wave matching layers. The C sandwich consists of two A sandwiches joined together for greater strength and rigidity. Other multilayer structures utilize an arbitrary number of dielectric layers to achieve high transmittance over a broad frequency band. 32

Design formulas and graphical data for A-sandwich structures are presented in Refs. 29 and 30. In the symmetrical sandwich, the inner and outer skins are identical and are thin with respect to wavelength. The spacing d_c of the skins (core thickness) is chosen so that the reflected wave from the second skin cancels the reflected wave from the first skin at a desired incidence angle. The angle θ at which this cancellation occurs is called the *core design angle*. The smallest value d_c at which cancellation occurs is called the *first-order spacing*. Salient transmission properties of an A-sandwich panel are shown in Fig. 44-8.

A-sandwich designs are used in many aircraft and in some missile radomes for both narrowband and broadband applications. Skins as thin as 0.005 in (0.127 mm) have been developed for use in radomes which achieve good circular polarization performances over an octave or greater bandwidth in the X/Ku frequency bands.³³ B-sandwich designs can be used in applications where the lower-density skins can withstand the environment; in some cases, the outer skin can be omitted to obtain a two-layer structure with good transmission properties (Fig. 44-4).

A metal-inclusions radome structure consists of dielectric layers containing metal inclusions which together form a high-frequency circuit element.³⁰ A metallic radome^{34,35} uses a perforated metal outer skin. Metallic radomes offer advantages of

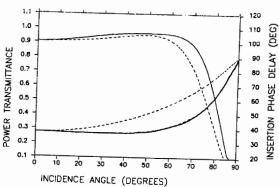


FIG. 44-8 Power transmittance (upper curves) and insertion phase delay versus incidence angle for an Asandwich panel having a core design angle of 50° for parallel (solid curve) and perpendicular (dash) polarizations ($\epsilon_{rs}=4.0$, tan $\delta_s=0.020$, $d_s=0.025\lambda$, $\epsilon_{rc}=1.2$, tan $\delta_c=0.005$, $d_c=0.293\lambda$).

better rain-erosion resistance, high strength-to-weight ratio, decreased static-charge buildup, and ease of handling.

A space-frame radome consists of a network of structural beams covered with a electrically thin dielectric material. 10,36 It is often in the shape of a truncated sphere and is used in ground-based applications. The dielectric or metallic structural beams form triangular sections networked together to support the loads applied to the dielectric material. Although some antenna gain reduction is caused by the beams, their size and random orientation prevent unwanted beam deflection and boresight errors.

The grooved radome wall structure is a nonresonant panel consisting of a thick dielectric into which V-shaped grooves have been cut on both sides of the panel.³⁷ The grooves cut on one side can be oriented 90° with respect to those on the other side to help cancel the anisotropic effects of the structure and to equalize the transmission properties for orthogonal polarizations. The grooves provide a gradual transistion from air to dielectric and back again, thus furnishing a continuous match to the incident wave in a manner analogous to that used in pyramidal absorber materials. The depth of the grooves determines the lowest frequency of operation, and the spacing of the grooves determines the upper frequency limit. Panels have been built and tested to operate from 5 to 40 GHz for incidence angles up to 50°. Similar anisotropic dielectric structures have been used to improve the performance of a streamlined radome.³⁸

A broadband radome wall structure is designed to provide high transmittance over a broad frequency band of operation. Loyet³⁹ has compared the broadband frequency properties of solid, sandwich, Oleesky, and gradient wall structures. The multilayer (Oleesky) and gradient walls are electrically superior, but their weight, thickness, and cost inhibit their use. The boresight error and error-slope performance of broadband radomes varies considerably over the bandwidth of high transmittance and is usually inferior to that obtainable with a solid half-wave wall in its optimum (6 percent) band of operation.

44-3 ELECTRICAL-DESIGN DATA

General

Theoretical electrical-design data are presented in this section for a tangent ogive, alumina ($\epsilon_r = 9.3$), half-wave wall radome containing a gimballed, uniformly illuminated, vertically polarized monopulse X-band antenna. The data illustrate both the computer-aided radome-design procedure and the predicted electrical performance of the tracking antenna as functions of radome wall thickness, fineness ratio, wall-thickness variations, and operating frequency. Electrical performance is quantified in terms of boresight error and gain in two orthogonal (pitch and yaw) planes. Some comparisons with measured boresight-error data are also presented for corroboration.

The antenna-radome geometry of Fig. 44-5 is applicable with radome diameter $D=6.6\lambda$, length $L=14.4\lambda$, constant wall thickness $d=0.17\lambda$, position of the gimbal point along the radome axis $R_R=2.14\lambda$, antenna offset $R_A=1.35\lambda$, and antenna diameter $D_A=5.0\lambda$, where λ is the free-space wavelength. The pitch plane of radome scan is the plane of the figure, in which the positive gimbal angle corresponds to the upward scan of the radome tip with respect to R_A or, equivalently, the downward scan of the antenna. The yaw plane of radome scan is perpendicular to the plane of the figure and contains the gimbal point and the antenna axis R_A . The positive gimbal angle in the yaw plane corresponds to the scan of the radome tip out of the page toward the reader.

Boresight errors are expressed in milliradians and can have positive and negative values. The boresight error is defined to be the true direction to the target with respect to the antenna axis R_A when electrical boresight is indicated by the outputs of the elevation-difference and azimuth-difference ports of the monopulse antenna. For an observer positioned behind the antenna and looking in the direction of R_A as indicated in Fig. 44-5, a positive pitch error indicates that the actual target location is above the R_A axis; a positive yaw error indicates that the actual target location is to the left of R_A in the yaw plane. A complete description of the coordinate systems is contained in Ref. 40.

Design Procedure

The design procedure for the missile radome starts with the specified tangent ogive shape (L/D=2.18). For high-speed applications, a ceramic radome material is dictated by operating temperatures. Alumina is chosen for its strength, resistance to rain erosion, and fabricability. A half-wave wall structure is chosen for simplicity in fabrication and superior boresight-error performance. Electrical design consists of choosing the uniform or tapered wall thickness which minimizes boresight error and gain loss as functions of gimbal angle and frequency in a narrow (6.5 percent) band centered at f_M .

Computer-aided radome analysis is used to determine the effects of the radome on boresight error and gain. A receiving formulation based on geometrical optics and Lorentz reciprocity is used. Briefly, the antenna near fields are represented by a sampled data array of 16×16 points spaced equally in the x and y directions approximately $\lambda/4$ apart. A vertically polarized plane wave (target return) is assumed to be incident on the outside of the radome from the direction k_A . From each sample point

in the antenna aperture, a ray is traced in the direction $\hat{\mathbf{k}}_A$ to determine the point of intersection and the unit inward normal $\hat{\mathbf{n}}_R$ to the inner radome-wall surface. The unit vectors $\hat{\mathbf{k}}_A$, $\hat{\mathbf{n}}_R$ are used to transform the incident plane wave through the radome wall by using the insertion-voltage transmission coefficients for a plane dielectric sheet having the same cross section as that of the radome wall (Fig. 44-3). The voltage V_R received in each channel of the monopulse antenna is computed according to

$$V_R = \int_{S_1} (\mathbf{E}_T \times \mathbf{H}_R - \mathbf{E}_R \times \mathbf{H}_T) \cdot \hat{\mathbf{n}} \, d\mathbf{a}$$
 (44-3)

where $\mathbf{E}_T \mathbf{H}_T = \text{antenna near fields when transmitting (sum, elevation difference, or azimuth difference)}$

 $\mathbf{E}_{R}, \mathbf{H}_{R}$ = fields incident on the antenna after traversing the radome $\hat{\mathbf{n}}$ = unit normal to antenna aperture

The integration is carried out over the planar surface S_1 coinciding with the antenna aperture. It is the choice of the surface S_1 and the approximations used to find the fields on it which distinguish the various methods of radome analysis.

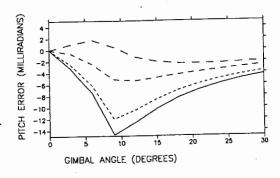
Gain loss caused by the radome is determined by comparing the maximum voltage received on the sum channel with the radome in place to that received for the case of a "free-space radome." Boresight error is determined in the pitch and yaw planes by finding the direction of arrival $\hat{\mathbf{k}}_0$ which produces a null indication in each tracking function defined by the ratio of difference-channel voltage to sum-channel voltage.

Electrical Effects

The effects of design angle (wall thickness) on boresight error and gain are illustrated in Figs. 44-9 and 44-10. It is clear from the figures that the smallest boresight errors and least gain loss are realized for the larger design angles of 55 and 75°. This result is expected from consideration of the incidence angles of rays drawn normally from the antenna aperture to the radome wall and the transmission characteristics of the half-wave wall. The difference in thickness of the walls with $\theta = 0^{\circ}$ and $\theta = 75^{\circ}$ is 0.009λ at band center f_M .

To demonstrate the accuracy of the predictions, Fig. 44-11 shows comparisons of measured and predicted boresight errors at three frequencies for the alumina radome having a uniform wall thickness of 0.17λ (design angle $\theta=55^{\circ}$ at midband). In each graph, the measured error is shown by the solid curve. The small dashed curve is the error predicted by using the ray-tracing radome analysis described above. The large dashed curve is the error predicted by using a surface-integration method of radome analysis based on Lorentz reciprocity and the Huygens-Fresnel principle.⁴¹ Whereas the latter method required approximately 30 s per pattern point, the former required approximately 1 s on the same type of computing system. Boresight-error computations require at least two pattern points.

The predicted effects on boresight error of tapering the wall thickness from tip to base are illustrated in Fig. 44-12. For the positive taper, the radome wall is thicker at the tip than at the base: at the base, the wall thickness corresponds to a design angle of $\theta = 0^{\circ}$; at the tip, the thickness corresponds to a design angle of $\theta = 75^{\circ}$. For the negative taper, the thickness at the base corresponds to $\theta = 75^{\circ}$, and the thickness at the tip corresponds to $\theta = 0^{\circ}$. Examination of Fig. 44-12 shows an improvement in pitch error by using the positive taper; however, yaw error is made worse. Pitch and yaw gains were little affected by the positive taper, whereas the neg-



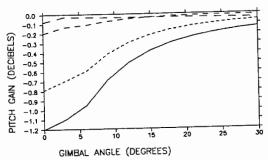


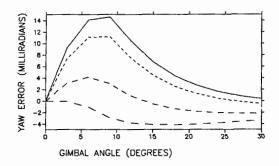
FIG. 44-9 Predicted boresight error and gain versus pitch-plane gimbal angle of alumina (L/D=2.18) tangent ogive radome at frequency f_M for four design angles: $\theta=0^\circ$ (solid curve), 30°, 55°, and 75° (largest dash).

ative taper caused gain reductions of approximately 0.7 dB in both planes. Other wall-tailoring prescriptions may yield better boresight-error and error-slope performance than those considered here.

Boresight errors are also affected by the fineness ratio (L/D) of the radome, as shown in Fig. 44-13. Generally, the higher fineness ratios produce larger boresight errors over a given frequency bandwidth; however, at a single frequency the wall thickness can be optimized to give comparable boresight errors over a range of fineness ratios. In Fig. 44-13, the wall thickness is $d = 0.17\lambda$ for each case, and no attempt has been made to optimize performance for each fineness ratio.

Variations in the wall thickness can have strong effects on the boresight errors, as illustrated in Fig. 44-11 for uniform thickness changes and as illustrated in Fig. 44-14 for a cosinusoidal thickness variation of 0.006λ from radome tip to base. The wide departure, especially in the yaw plane, of the boresight error due to such a thickness variation emphasizes the importance of mechanical tolerances in the manufacturing process.

At frequencies higher than X band, a solid-wall ceramic radome must often have a thickness greater than one-half wavelength to meet structural-strength requirements. Higher-order half-wave walls are inherently more frequency-sensitive than the



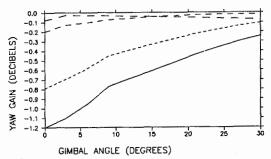


FIG. 44-10 Predicted boresight error and gain versus yaw-plane gimbal angle of alumina (L/D=2.18) tangent ogive radome at frequency f_M for four design angles: $\theta=0^\circ$ (solid curve), 30°, 55°, and 75° (largest dash).

first-order (n = 1) wall, as illustrated by the data in Fig. 44-15. Although not illustrated, an *n*-order half-wave wall of material with high dielectric constant is more frequency-sensitive than the same-order wall of lower dielectric constant.

The boresight error and boresight-error slope produced by the radome can affect missile performance in different ways, depending on the type of guidance system employed. 42.43 Consequently, radome specifications may vary from one system to another. Some investigators have seriously questioned the necessity of tight specification on error and error slope. 44 Electronic compensation to correct radome boresight errors has been implemented and shown to be feasible at ambient temperatures; 45 however, questions have been raised concerning the accuracy of the technique at elevated operating temperatures and for wave polarizations other than those for which the boresight-error map of the radome was made.

From the foregoing discussion, the importance and usefulness of accurate, practical computer-aided radome-analysis methods should be apparent. Development of such methods has paralleled the development of airborne radar systems, whose complexities have increased over the years. Silver⁴⁶ illustrates the geometrical-optics approaches taken up to 1949 and developed during the previous war years. Kilcoyne⁴⁷

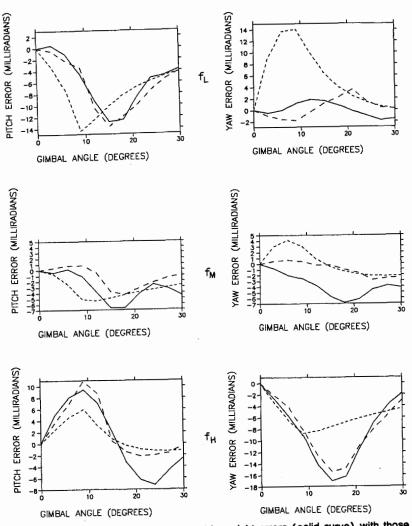


FIG. 44-11 Comparisons of measured boresight errors (solid curve) with those computed by using ray tracing (small dash) and surface integration (large dash) for alumina half-wave wall ($d = 0.17\lambda$), tangent ogive radome 6.6 wavelengths in diameter and 14.4 wavelengths long. X-band frequencies f_L and f_H are the edges of a 6.5 percent band; f_M is band center. (After Ref. 41.)

presents a two-dimensional ray-tracing method for analyzing radomes which utilizes the digital computer and is an extension of work done earlier by Snow⁴⁸ and by Pressel.⁴⁹ A more rigorous method of analysis, using an integral equation to compute fields inside the radome caused by an incident plane wave, was introduced in the same year by Van Doeren.⁵⁰ Tricoles⁵¹ formulated a three-dimensional method of radome anal-

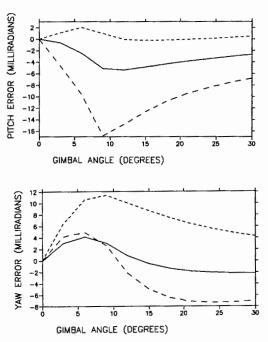


FIG. 44-12 Predicted boresight errors versus gimbal angle of alumina (L/D = 2.18) radome at frequency f_M for uniform wall thickness (solid) and for positive (small dash) and negative (large dash) taper of wall thickness.

ysis based on Shelkunoff's induction and equivalence theorems. Tavis⁵² describes a three-dimensional ray-tracing technique to find the fields on an equivalent aperture external to an axially symmetric radome. Paris⁵³ describes a three-dimensional radome analysis wherein the tangential fields on the outside surface of the radome due to the horn antenna radiating inside the radome are found. Wu and Rudduck⁵⁴ describe a three-dimensional method which uses the plane-wave-spectrum (PWS) representation to characterize the antenna. Joy and Huddleston⁵⁵ describe a computationally fast, three-dimensional radome analysis which utilizes the plane-wave-spectrum representation and exploits the fast Fourier transform (FFT) to speed up the computer calculations. Chesnut⁵⁶ combined the program of Wu and Rudduck with the work of Paris to form a three-dimensional radome-analysis method. Huddleston⁵⁷ developed a three-dimensional radome-analysis method which uses a general formulation based on the Lorentz reciprocity theorem. Siwiak et al.⁵⁸ applied the reaction theorem to the analysis of a tangent ogive radome at X-band frequencies to determine boresight error. Hayward et al.⁵⁹ have compared the accuracies of two methods of analysis in the cases of large and small radomes to show that ray tracing does not accurately predict wavefront distortion in small radomes. Burks⁶⁰ developed a raytracing analysis which includes first-order reflections from the radome wall. Kvam and Mei⁶¹ have applied the unimoment method to the solution of the radome problem.



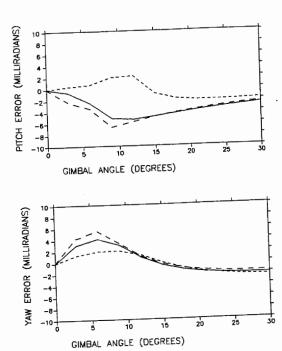


FIG. 44-13 Predicted boresight errors versus gimbal angle of alumina radome at frequency f_M for three fineness ratios: L/D = 2.18 (solid), L/D = 1.5(small dash), L/D = 2.5 (large dash).

Aerothermai Anaiysis

Computer-aided analyses have also been developed to determine temperatures and mechanical stresses in the radome due to aerodynamic loading and heating as functions of trajectory, altitude profile, velocity, and maneuvers of the missile or aircraft. URLIM is one such computer program. 62 It calculates thermal stress, melting, dielectric changes, and maneuver loads versus trajectory time for hypersonic radomes. In addition, it estimates bending stresses at the base of the radome due to aerodynamic pressure and maneuver.

FABRICATION AND TESTING

Fabrication

Fabrication methods depend on the radome material, and it is often the availability of a reliable manufacturing method which makes the final selection of material. Typical construction methods for organic radomes include molding (vacuum bag, autoclave, pressure bag, matched die), filament winding, resin infiltration, and foam in place. 63 Injection molding is also used. 64 Inorganic (ceramic) radomes have been con-

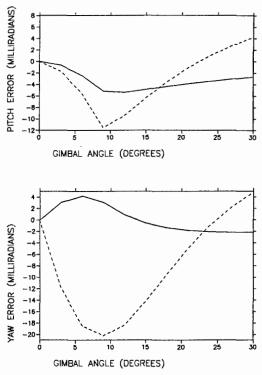


FIG. 44-14 Predicted boresight errors versus gimbal angle of alumina (L/D=2.18) radome at frequency f_M for uniform wall thickness of $d=0.17\lambda$ (solid) and for cosinusoidal longitudinal thickness variation of 0.006λ (dash).

structed by using slip casting, cold pressing, injection molding, hot pressing, glass forming, and flame spraying.⁶⁵ Machining is often required for both organic and inorganic radomes to provide the necessary tolerances on wall thickness.

Mechanical and electrical tests are performed throughout production. Before fabrication, tests are performed on panels of candidate radome wall structures to ensure that the required mechanical and electrical properties can be attained reproducibly and within the margins required. During fabrication, quality-control tests are carried out to ensure correct shape, size, dielectric constant, loss tangent, and wall thickness. After fabrication, laboratory and operational tests are performed to help ensure successful radome performance in the field.

Mechanical Testing

Mechanical testing includes measurements of physical dimensions and testing of the structural, thermal, and rain-erosion properties of the complete radome. Ultrasonic-and microwave-interferometer techniques are used to measure wall thickness. Struc-

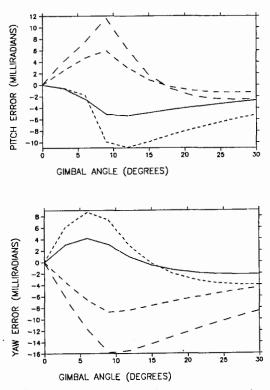


FIG. 44-15 Predicted boresight errors versus gimbal angle of alumina (L/D=2.18) radome for two wall thicknesses at two frequencies: half-wave wall $d=0.17\lambda$ at f_M (solid); full-wave wall $d=0.34\lambda$ at f_M (smallest dash); half-wave wall at $f_H=1.032~f_{Mi}$ full-wave wall at f_H (largest dash).

tural testing involves static loading of the radome, using mechanical, pressure, and vacuum methods in a manner simulating operational conditions, and is often done at design temperatures. High-temperature and thermal-shock testing has been carried out by using oxyacetylene torches, quartz lamps, rocket motors, ramjet engines, ¹⁸ solar furnaces, ^{12,66} and supersonic wind tunnels. ⁶⁷ Rain-erosion testing has been carried out by using rocket sleds, rotating arms, and shotgun lead pellets. ⁶⁸ Electrical tests are sometimes combined with thermal testing. ¹⁴

Electrical Testing

Electrical testing of radomes includes measurements of complex permittivity of radome materials and electrical characteristics of the complete antenna-radome combination. The dielectric constant and loss tangent of material samples can be determined at microwave and millimeter waves by using free-space-bridge, ⁶⁹ Fabry-Perot-

resonator, 70 and short-circuit-waveguide 71 techniques. Below millimeter wavelengths, cavity and capacitance bridge techniques can be used. 72,73

Radome electrical testing includes measurement of transmission efficiency, boresight error, boresight-error slope, beam deflection, radome reflection, antenna-pattern distortion, and depolarization as functions of antenna-radome orientation (scan) and frequency. Standard antenna range equipment, with the addition of a radome-test fixture, can be used to measure pattern distortion, transmission efficiency, reflection (VSWR), and depolarization. Boresight-error and beam-deflection measurements are more demanding and are made by using automated closed-loop 4,76 and electronically calibrated systems.

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Microwave Propagation

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45-1 Introduction 45-2

45-2 Clear-Sky-Induced Propagation Effects 45-2

45-3 Rain-Induced Propagation Effects 45-7

45-4 Other Effects 45-13

Microwave propagation as considered here deals with the propagation of radio waves through the atmosphere. Propagation through the earth, in tunnels in the earth, or in bound modes (indeed, other than in radio line of sight) will not be considered. In general, the range of frequencies given most detailed examination is 3 to 30 GHz, although propagation effects from 1 to 100 GHz will be treated. The effects on radio-wave propagation through the clear troposphere will be considered, and then the effects of rain will be examined. Finally, effects arising in the ionosphere will be touched upon.

Microwave antennas can be considered transducers coupling energy from a guided-wave system into the unbound-wave-propagation medium. As such, microwave antennas are necessarily affected by both regimes, but since the properties of the one can be controlled by the antenna designer and the other cannot, until recently propagation effects were given short shrift by antenna designers. More usually, these effects appear as entries in system link budgets or error budgets. The need for more careful control of where energy is directed to or received from (interference-coordination and security), for polarization control (dual-polarized systems), and, as frequencies in common use rise above 10 GHz, for limiting radio-frequency (RF) power requirements to practical values, has given rise to the need for information on propagation effects.

45-2 CLEAR-SKY-INDUCED PROPAGATION EFFECTS

At most antenna sites, for most of the time the path between two antennas within radio line of sight will be occupied by atmosphere and/or free space which is clear to the eye, that is, free of obstructions, clouds, rain or other hydrometeors, and dust or other particulates. This gaseous atmosphere^{1,2} has two main constituents, nitrogen and oxygen. The proportions of these constituents are fixed, and their effects for a particular link are constant. But it is a third constituent, water vapor, whose proportions vary, that causes most of the clear-sky impairments. Table 45-1 lists the constituents

TABLE 45-1 Gases in the Atmosphere

Gases	Percent volume (dry air)*
Nitrogen	78.1
Oxygen	20.9
Argon	0.9
Other†	0.1

^{*}Water vapor ≤ 4 percent near surface (very variable)

^{≤ 0.01} percent above 15 km.

[†]Carbon dioxide ~ 0.03 percent (variable).

of the normal atmosphere. Figure 45-1 shows mean temperature as a function of altitude. The pressure falls off approximately exponentially. This is modeled in the U.S. Standard Atmosphere.³

Only water vapor and oxygen cause appreciable absorption of radio waves in the range of frequencies of concern. Water-vapor distribution and gravity-induced variation of the density and pressure of the atmosphere as a function of altitude contribute to systematic ray bending through variation of the radio refractive index. However, because at times the atmosphere develops local inhomogeneities, which result in local changes in the radio refractive index, other impairments to radio waves at microwave frequencies may arise, among them ducting, fluctuations in angle of arrival, fluctuations of amplitude and phase, phase-delay variation, and defocusing. Absorption brings along with it the corollary effect of noise-temperature increase. The longer the path through the atmosphere, the more severe these impairments tend to be. Consequently, for nearly horizontal paths at low elevation angles, these impairments tend to be more severe. The situation is further complicated by the fact that the transmission properties of the atmosphere vary diurnally (throughout the day) and seasonally as well as geographically.

Antenna design is affected by absorption in the clear atmosphere A_a , as increased gain may be required to overcome this absorption, which is given by

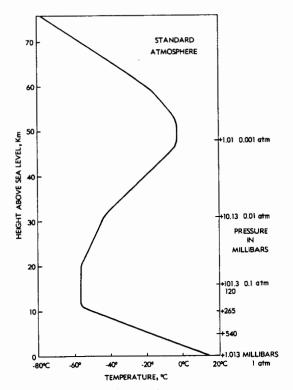


FIG. 45-1 Standard atmosphere.

$$A_a = \int_0^d \gamma_a(r) dr \tag{45-1}$$

Over a horizontal path of length d, if it is assumed that the absorption coefficient γ_a dB/km is uniform along the path,

$$A_a = \gamma_a d = d[\gamma_o(f) + \gamma_w(f,\xi)]$$
 (45-2)

where γ_o = absorption coefficient due to 0_2

 γ_w = absorption coefficient due to water vapor

f = frequency

 ξ = water-vapor concentration, g/m³

To a first approximation, the effects of water vapor can be estimated as linear (except for the higher concentrations). Thus

$$\gamma_o(f,\xi) = \gamma_o(f) + (\xi/7.5)\gamma_w(f,7.5)$$
 (45-3)

Curves for $\gamma_o(f)$ and $\gamma_w(f, 7.5)$ are given in Fig. 45-2. For the slant path $\gamma_o \gamma_w$ and hence γ_a are affected by the distribution of oxygen and water vapor as a function of altitude and pressure. 4.5 The effects of oxygen on slant-path absorption are reasonably straightforward to access, as oxygen distribution is not a strong function of climate and is estimated to be equivalent at zenith to 7 to 10 km of attenuation on a horizontal path, complicated by the effects of starting altitude. But water-vapor absorption is quite a bit more complex. Obviously, the slant path contains little water vapor above the 0° isotherm, which changes its altitude diurnally, seasonally, and geographically. Additionally, to a first approximation, water vapor at altitude is a function of water-vapor content at the surface. More approximately and simplistically, Fig. 45-3 gives the approximate dry gaseous absorption $(1 \le f \le 100 \text{ GHz})$ and the approximate contribution due to water vapor for 7.5 g/m³ at zenith. Down to 5° elevation angle,

$$\gamma_d(\theta) \cong \gamma_d(90^\circ)/\sin\theta$$
 (45-4)

 $\theta \equiv$ elevation angle

$$\gamma_a (90^\circ) \cong \gamma_o (90^\circ) + \frac{\xi}{7.5} \gamma_w (90^\circ)$$
 (45-5)

For more precise calculations, or for calculations near the absorption lines of water vapor and oxygen, equations for γ_0 and γ_w are given in Refs. 5a to 5c that contain terms needed to account for these absorption lines. Ray bending arises because of the variation in the index of refraction of the atmosphere for radio waves. For lower-elevation-angle paths, the systematic ray bending caused by this has been calculated. The average radio refractive index for an exponential atmosphere is given in CCIR, Volume V, Report 564-46 as

$$n(h) = 1 + N \times 10^{-6} = 1 + 315 \times 10^{-6} \times \exp(-0.136 h)$$
 (45-6)

where h =altitude above sea level

$$N = \text{radio refractivity} = 77.6 \ p/T + 3.73 \times 10^5 \ p_{\omega}/T^2$$
 (45-7)

p = atmospheric pressure, mb

T = temperature, K

 $p_{\omega} = \text{water-vapor pressure, mb}$

At any point on the ray path, ray curvature $(1/\rho)$ is given by

$$\frac{1}{\rho} = \frac{\cos \theta}{n} \times \frac{dn}{dh} \tag{45-8a}$$

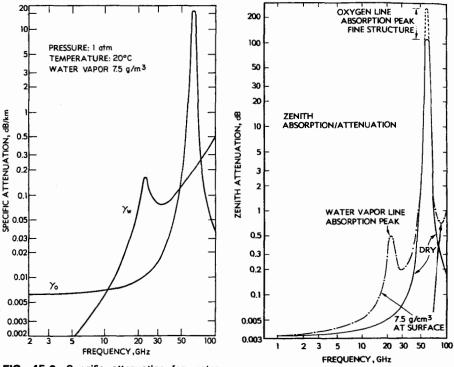


FIG. 45-2 Specific attenuation for water vapor and oxygen.

FIG. 45-3 Zenith absorption.

$$\frac{1}{\rho} \cong \frac{dn}{dh}$$
 for low elevation angles (45-8b)

For earth space (i.e., slant paths), this ray bending, in general downward, requires an apparent increase in elevation-angle pointing of the antenna. Detailed calculations of the required increment in elevation angle have been made by Crane, who has calculated the average increments for different climate zones and also the day-to-day variations in the increment, all as a function of elevation angle.

Signal fluctuations caused by the clear troposphere impact antenna design because telecommunications systems are designed to have gain margin to overcome such fluctuations, part of which may be contributed by antenna gain, and because the antenna aperture size enters into fluctuation phenomenology directly.^{8,9}

For line-of-sight paths, the atmosphere can behave in such a way that for some percentage of time rays are bent so that the earth appears to block transmission for certain path geometries, and transmission is then dominated by diffraction considerations¹⁰ with an apparent loss of gain. Variations in atmospheric properties can cause the propagation-path bending owing to refraction due to the gradient in refractive index to change, thus changing the apparent angle of arrival of signals, i.e., the angle to which the antenna must be pointed. (Otherwise, the signals will appear to fluctuate slowly.) As might be expected, this occurs principally in the vertical plane;

variations up to 0.75° have been reported, 11,12 and the antenna pattern obviously enters into the fluctuation effects. Another serious source of signal fluctuation is interference of signals traversing different paths from transmitter to receiver (i.e., multipath transmission). This is thought to arise because of local variations in water-vapor content and temperature, which imply local fluctuations in refractive index, which means that "rays" that start off in directions different from line of sight to the receive antenna can have trajectories that terminate at that antenna. As many as six such trajectories have been shown to exist simultaneously. The probability of a deep multipath fade of depth F(dB) is given by the relationships 14,15

$$F = 10 \log_{10} \frac{P}{P_0} \tag{45-9}$$

 $(P_0 \equiv$ reference power level for no fade) and, obtained by regression from empirical data,

$$p(F) = k_c k_t \, 10^{-F/10} \, f \, d^3 \tag{45-10}$$

where k_c , k_t are climate- and terrain-dependent parameters whose product has been evaluated empirically for the United States. ^{14,15} f is in GHz,

$$10^{-5} \le (k_c k_t) S_1^{1.3} \le 4 \times 10^{-5}$$
 (45-11)

where S_1 is the terrain-roughness factor (the standard deviation of terrain-elevation samples taken at 1-km intervals). Internationally, the frequency and path-length dependencies and terrain-roughness factors have not been fully reconciled. But it has been shown that antenna beamwidth and path-clearance factors enter into those effects and must be taken into account in reconciling effects of antenna beamwidth of the different sets of measurements.

Multipath fade durations in the United States have been shown empirically to follow a log-normal distribution, ^{17,18} with the median fade duration given by

$$\bar{t} = 57 \ 10^{-F/20} (d/f)^{1/2}$$
 (45-12)

The use of two antennas, spatially separated, to overcome fading is called *diversity*. A vertical separation of several meters has been found to improve the fading characteristics of line-of-sight links with small ground reflections. Vigants¹⁸ has proposed a formula for improvement:

Improvement
$$\equiv I \cong (\Delta h)^2 f/d \ 10^{-F/10} \ 10^{\Delta G} \times k$$
 (45-13)

where Δh = vertical separation, m

 ΔG = difference in antenna gains

 $k = \text{constant} \cong 1.2 \times 10^{-3} n$

where η is the efficiency of the diversity-combining arrangement. It is thought that this equation is useful only for $I \ge 10$, $2 \le f \le 11$ GHz, $24 \le d \le 70$ km, and $5 \le h \le 15$ m.

Signal fluctuations also occur on the slant path. One mechanism is thought to be scattering of radio waves by small-scale spatial variations of refractive index arising under appropriate conditions. Measurements¹⁹ seem to indicate that the presence of high humidity and some wind makes amplitude scintillation more probable. Analytic considerations²⁰ also show that amplitude scintillations of radio-wave signals may be produced by turbulent fluctuations of the troposphere. Tatarski²⁰ has shown that, in addition to the signal fluctuations, there is an apparent loss in gain arising from the

averaging of signals over the antenna aperture. Crane and Blood⁴ have developed a model for the variation of the rms signal-fluctuation level.

$$\left(\frac{\delta(f,\theta,D)}{\delta_{\text{Reference}}}\right) \propto f^{7/12} (\csc \theta)^{0.85} \left(\frac{G(R)}{G(R)_{\text{Reference}}}\right)^{1/2} \quad \text{dB} \quad (45-14)$$

where $R = \sqrt{\eta}D/2$ = effective antenna radius

 η = antenna efficiency factor

G(R) = Tatarski's aperture-averaging factor

Thus, it is seen that antenna aperture size and efficiency enter into signal-fluctuation modeling. A step-by-step procedure for estimating signal-fluctuation statistics is given in CCIR, Vol. V, Report 564-4.^{20a}

Measurements made in the INTELSAT system¹⁹ indicate that for elevation angles of 6.5° signal fluctuations of 4.5 dB or greater peak to peak occurred for about 0.01 percent of the time, and of 3 dB or greater for 0.3 percent of the time, for a single path (up at 6 GHz, down at 4 GHz). For the combined paths (up at 6 GHz, down at 4 GHz), signal fluctuations in the worst month (July 1974) exceeded 3 dB peak to peak for about 16 percent of the month.

Antenna gain loss due to defocusing has been demonstrated for low-elevationangle slant paths.²¹ But it appears that this loss is negligible (less than 0.2 dB) for paths with elevation angles above 4°.

45-3 RAIN-INDUCED PROPAGATION EFFECTS

Rain is a major cause of impairments to radio-wave transmission in the frequency ranges of concern. Rain absorbs radio waves and scatters them. Both actions extract energy from the incident wave, causing signal attenuation. Both cause a change of polarization state from that in the incident wave, causing signal depolarization. Both can cause a net increase in noise temperature to receiving systems. The scattering also diverts radio-wave energy into directions which might otherwise not receive energy, causing interference between telecommunications systems operating at the same frequency from common volume scattering. Attenuation affects antenna design, as increased antenna gain and/or antenna site diversity are means of ameliorating radio-wave attenuation and noise-temperature increase (although they are not the only means). Depolarization also can be mitigated at the antenna, in the microwave system behind the feed. Common-volume-scattering-induced interference is dependent on antenna gain and sidelobe characteristics.

To assess these impairments it is necessary to know the rainfall climate (rainfall, rain rate, drop-size distributions, etc.) in and around the sites of concern. Ideally one would like to know the rainfall characteristics for many years for each radio link of concern, but this information is not generally available. References 22, 23, 24, and 25 are good starting points for worldwide information (including the United States) on climate parameters in general and precipitation in particular. More detailed and finegrained data are obtainable through weather services in the various countries. In the United States, this would be the National Weather Service Library, NOAA Library, Executive Blvd., Rockville, MD 20852, or the National Weather Service National Climatic Center, Asheville, NC 28801, from which various detailed records can be obtained. One very useful type of record is climatalogical data by state, by recording site, by month,

and by year. With enough back issues of such data, one can readily construct a data file on precipitation measurements near and around almost any desired site in the United States. In Canada, data can be obtained from the Atmospheric Environment Office, Downsview, Ontario.

Noise energy enters the antenna from the atmosphere, as is well known. The effects of the normal environment on "antenna" noise-temperature contributions are well understood and documented elsewhere. Portions of these contributions arise in the troposphere. The dependence of the contributions on atmospheric attenuation \mathcal{A} (dB) is given by

$$\Delta T_s = T_m \left[1 - 10^{-A(dB)/10} \right] \tag{45-15}$$

where ΔT_s is the sky noise-temperature increase, K, and T_m is the effective temperature of the clear atmosphere, which has been determined empirically.²⁶

$$T_m = [1.12 (T_{\text{surface}}) - 50] \text{ K}$$
 (45-16)

for frequencies above 10 GHz.

Relationship (45-15) applies reasonably well for the noise-temperature contributions arising from hydrometeors in the troposphere, including and especially rain. It means that the noise-temperature increase due to rain approaches the temperature of the rain. But the rain itself is cool, generally between 273 K (freezing) and 283 K. Radiometric measurements tend to verify this. $T_m(\text{rain})$ of 270 to 280 K are commonly used.

Rain-induced attenuation and depolarization are functions of the impairment per unit path length and the path length through the medium. For example, for rain

$$A = L_{\epsilon}(R)\gamma(R) \tag{45-17}$$

where A = attenuation, dB

 $L_e(R)$ = equivalent path length in rain at rain rate R

 $\gamma(R)$ = attenuation per unit path length at rain rate R

The impairment per unit path length is dependent on the cumulative rain-rate distribution,²⁷ the distribution of rain into various drop sizes,²⁸ and several other parameters. For attenuation, one can write²⁹

$$\gamma(R) = aR^b \qquad \text{dB/km} \tag{45-18}$$

where R = surface-point rain rate

a, b = constants

Figure 45-4 gives $\gamma(R)$ for $1 \le R \le 150$ mm/h for spherical raindrops. Unfortunately, not all raindrops are spherical.³⁰ For sizes larger than 0.5-mm radius, their shape evolves through spherical to oblate spheroidal, to oblate spheroids flattened on the down side (distorted by the air pressure when falling) to almost cardioids of revolution (equal-volume-sphere radius > 3 mm), as shown in Fig. 45-5. As a result, attenuation due to rain is polarization-sensitive,³¹ and attenuation perpendicular to the inclination of the raindrop major axes is less than that parallel to them. In general, most nonspherical raindrops fall with their major axis only slightly inclined to the horizontal. Thus, a radio wave which is vertically polarized is less attenuated than one horizontally polarized, and this has been demonstrated repeatedly by measurements (for example, Ref. 32). The difference (in decibels) is termed differential attenuation. Similarly, and most important for rain depolarization, phase shift due to rain is polarization sensitive,³¹ and below about 20 GHz, differential phase shift is the dominant mechanism causing rain depolarization.

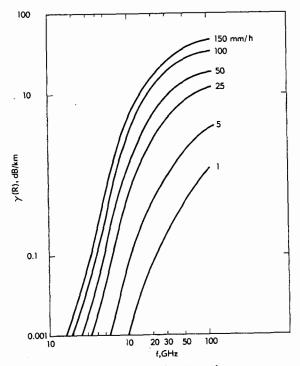


FIG. 45-4 Rain-induced specific attenuation.

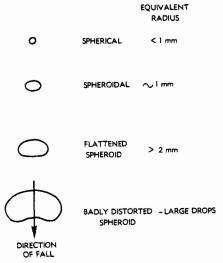


FIG. 45-5 Raindrop shapes.

There remains the matter of the path length through the medium. The problem is that rain does not fall everywhere on the path, whether the path links terrestrial sites or is a slant path into space. And where rain falls, the rain rate on the path is not uniform. This has led to the concept of effective path length, $L_{\epsilon}(R)$, such that if the rain were falling uniformly at a rain rate R on this portion of the total path, then Eq. (45-17) would give values of A consistent with measured data.

The cumulative probability in percentage of a surface-point rainfall rate R is given by 27,33

$$p(R) = \frac{M}{87.66} \left[0.03\beta e^{-0.03R} + 0.2(1 - \beta) \cdot (e^{-0.258R} + 1.86e^{-1.63R)} \right]$$
 (45-19)

where M = mean annual rainfall accumulation, mm

 $\beta \equiv \text{Rice-Holmberg}^{27} \text{ thunderstorm ratio*}$

The effective path length has a number of representations. Based on data collected in western Europe and eastern North America,³⁴ the effective path length L_{e1} has been approximated by

$$L_{el}(R,\theta) = [0.00741R^{0.766} + (0.232 - 0.00018R) \sin \theta]^{-1}$$
 (45-20)

On the basis of data collected in Japan, curves given in Fig. 45-6 provide effective path length for 1.0, 0.1, 0.01, and 0.001 percent of the mean year, L_{e2} (R, θ). L_{e1} is most useful for a benign climate (lower thunderstorm ratios); L_{e2} , where there are tropical storms and the like. It has been found³⁴ that for attenuation calculations for f < 10 GHz, L_{e2} is more generally accurate, whereas for f > 10 GHz, $L_{e} = 0.75$ $L_{e2} + 0.25$ L_{e1} has proved effective.

This subject has been much discussed in the literature. 34,35,36 More recently, 4,37 procedures based on climatological considerations have evolved. It is hoped, but not yet fully established, that these procedures will be both generally applicable and accu-

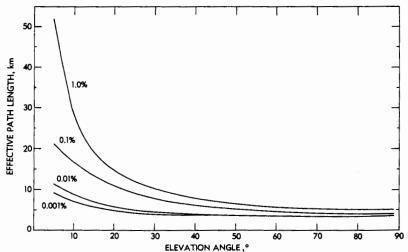
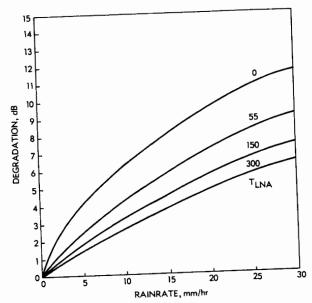


FIG. 45-6 Effective-path-length curves derived from measurements made in Japan.



Degradation of C/T versus rain rate. FIG. 45-7

rate. A plethora of measured data exists, 33,35,37-41a and new data are continually being presented. Truly, one hopes for verified modeling.

In the end, the result is effectively a loss of signal power in both transmission and reception and a degradation of system noise temperature. These effects can be offset by increased antenna gain, or by increased transmitter power and decreased receiversystem noise temperature, or by site diversity. Figure 45-742 shows a typical trade-off between antenna gain and low-noise receiver noise temperature on a slant-path link. The trade-off between transmitter power and antenna gain is a 1-dB decrease in transmitter power required for each decibel increase in antenna gain on a terrestrial or slant-path link. The trade-off between receiver noise temperature and antenna gain shown in Fig. 45-7 arises out of the equations for carrier-to-noise ratio for the downlink.

$$\left(\frac{C}{T}\right)_{\text{downlink}} = \text{eirp} - L + \left(\frac{G}{T}\right)_{\text{sys}}$$
 all in dB (45-21)

where eirp = effective isotropic radiated power

 $L = loss = L_{fs} + L_a + L_w$, all in dB

G = antenna gain

 T_{sys} = system noise temperature,* K

or earth-space paths may be approximated by
$$T_{sys} \simeq (0.95/L_aL_w) \left[T_c + T_m(L_a - 1) \right] + (T_0/L_w) \left[0.05 + (L_w - 1) \right] + T_R$$

where $T_c =$ clear-sky noise-temperature contribution

 $T_0 =$ ambient temperature of equipment

 T_R = noise temperature of receiver

 T_{sys} for earth-space paths may be approximated by

 L_{fs} = free-space-path loss, dB

 $L_a = loss$ in the atmosphere, dB, due to rain

 $L_{\omega} = loss in feed system, dB$

Under degraded conditions caused by rain, the degradation of C/T can be shown to appear to be equivalent to operating with a reduced G and an increased T. It can be shown⁴² that the effect of increasing antenna gain by ΔG dB is independent of rain effects, whereas decreasing the receiver-system noise temperature by ΔT dB is most effective when there is no rain, and the heavier the rain rate (i.e., the higher the rain-induced attenuation), the less effective the improvement in receiver-system noise temperature.

Depolarization is a particularly damaging impairment, especially when encountered in a polarization-sensitive system such as a dual orthogonally polarized communications system using a dual orthogonally polarized feed system. As noted above, rain can change the polarization state of a radio wave, i.e., depolarize it. The departure of raindrops from spherical shapes³⁰ is the mechanism.³¹ Further, the more intense the rain rate, the higher the proportion of large drops²⁸ and the greater the depolarization.³¹ For frequencies above about 8 GHz, the relationship between attenuation due to rain and the depolarization also caused by the rain is well established^{43,44} for earth-space paths:

$$XPD = U - V \log_{10} \text{ (copolarized attenuation, dB)}$$
 (45-22)

where

$$U = \kappa^2 - 10 \log_{10} \left[1/2(1 - \cos(4\tau)e^{-c_m^2}) \right]$$
 (45-23)

$$+ 30 \log_{10}(f) - 40 \log_{10}(\cos \theta)$$

for $8 < f \le 35$ GHz, and f in GHz $10^{\circ} \le \theta \le 60^{\circ}$

$$V = 20 \text{ for } 8 < f \le 15 \text{ GHz}$$
 (45-24a)

$$V = 23 \text{ for } 15 < f \le 35 \text{ GHz}$$
 (45-24b)

where θ = elevation angle

 τ = polarization tilt angle to horizontal (for circular polarization, τ = 45°)

 $\kappa \cong 0$ for conservative estimations of XPD

 $\kappa_m \cong 0.25$ for conservative estimations of XPD

Thus, for frequencies above 8 GHz, calculations of XPD (cross-polar discrimination) can be made either from measured values of copolarized attenuation or from estimations made with Eq. (45-22) and its companion equations. Above 8 GHz, XPD is increasingly affected by differential attenuation, but below 8 GHz it is heavily dominated by differential phase shift, the difference in phase shift of a radio wave orthogonal to the principal axis of the spheroidal drops and parallel to this axis, i.e., almost vertical and almost horizontal, 31,45,46,47 and attenuation effects are much less important. A different approximation 36,43 has proved useful for earth-space paths for circular polarization over the range $1 \le f < 8$ GHz, although it has some validity up to 35 GHz:

$$XPD = U - V \log_{10} R - 20 \log_{10} L_e$$
 (45-25)

where $U = 90 - 20 \log_{10} f - 40 \log_{10} (\cos \theta)$ (45-26)

$$V = 25 1 \le f \le 15 \text{ GHz}$$

= 27 - 0.13f 15 <
$$f \le$$
 35 GHz
and f in GHz, R in mm/h (45-27)
 $L_e \cong 0.7 L_{e2}$ for $f < 10$ GHz
 $L_e \cong L_{e1}$ for $f \ge 10$ GHz

Statistics for depolarization measurements are available both above and below 10 GHz. 48,49

For terrestrial paths, horizontal or vertical polarization has been shown to be better than circular polarization,⁵⁰ and the corresponding relationships are

where
$$XPD = U - V(f) \log_{10} (\text{copolar attenuation, dB})$$
 (45-28)
 $U = U_0 + 30 \log_{10} (f)$ (45-29)
 $V = 20$ (45-30)

where for f in GHz 8 $\leq f \leq$ 20 GHz and $U_0 \cong$ 9 for attenuation \geq 15 dB.

Means of ameliorating the effects of rain are available. One approach is to use site diversity. Whereas for multipath fading [Sec. 45-2, Eqs. (45-9) to (45-13)] a diversity spacing of several meters is often effective, now spacings of the order of 5 to 50 km must be considered.^{51-53a} If this is done, it is very effective for ameliorating attenuation and depolarization effects for frequencies above 10 GHz, but at the cost of the extra site or sites. Below 10 GHz, attenuation is not so strong an effect, and it is possible to ameliorate XPD by depolarization compensation.^{54,55}

45-4 OTHER EFFECTS

There are several other mechanisms, such as clouds and dust or sand, which can affect the propagation path and thus antenna design, but perhaps the most important remaining mechanism is the ionosphere for transionospheric links. Ionospheric effects 56,57 that may have to be considered above 1 GHz include Faraday rotation (the rotation of linearly polarized signals), propagation time delay and dispersion, and gigahertz ionospheric scintillation. Faraday rotation and propagation delay vary as $1/f^2$, and dispersion as $1/f^3$. The numbers in Table 45-2 were derived from JPL Publication 77-71. 58

TABLE 45-2

	Frequency						
	1 GHz	3 GHz	10 GHz	30 GHz			
Faraday rotation	108*	12*	1.1*	0.12*			
Propagation delay Dispersion	0.25 μ s 4 × 10 ⁻⁴ ps/Hz	$0.028 \mu s$ $1.5 \times 10^{-5} \text{ ps/Hz}$	2.5 ns $4 \times 10^{-7} \text{ ps/Hz}$	0.28 ns 1.5×10^{-8} ps/Hz			

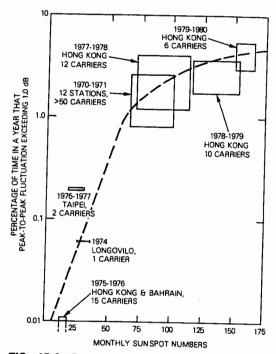


FIG. 45-8 Dependence of 4-GHz equatorial ionospheric scintillation on monthly averaged Zürich sunspot numbers. (After Ref. 57.)

The numbers given in Table 45-2 are based on an ionospheric total electron content of 10^{18} electrons/m², most likely to be encountered at low latitudes during the daytime in periods of high solar activity, and as such should be considered near the maximum values likely to be encountered for any length of time.

Gigahertz ionospheric scintillation⁵⁷ is encountered on earth-space paths typically near the spring and fall equinoxes and can vary from 1 dB peak to peak a few times an equinox during periods of low solar activity to 14 dB peak to peak at the peak of solar activity (both measured on 30-m-diameter antennas). It is inversely dependent on antenna diameter (the smaller the antenna, the worse the effects). Solar activity peaks every 11 years with a major peak every 22 years, the last major peak having occurred in 1981. A peak can be expected in 1992–1993, and a major peak in 2003–2004. Figure 45-8 gives data on peak-to-peak ionospheric scintillation over the half cycle 1970–1981.

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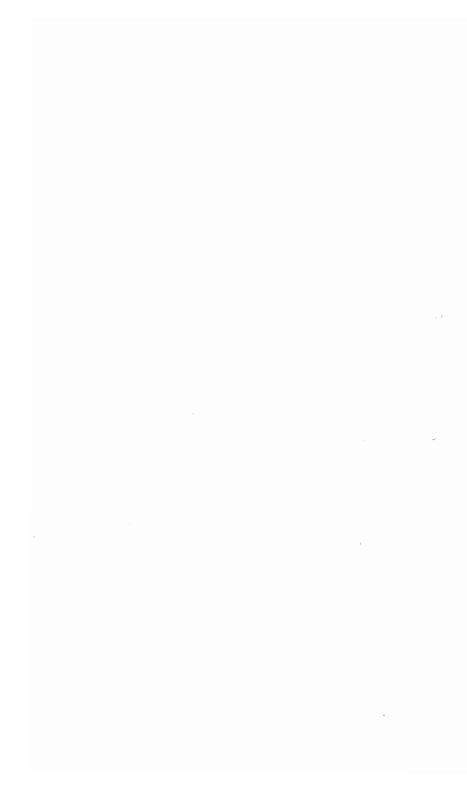
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Materials and Design Data

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- 46-1 Properties of Materials 46-2
 Dielectrics 46-2
 Metals 46-2
 46-2 Absorbing Materials 46-3
- 46-3 Nonsolid Surfaces 46-3
 Gratings 46-3
 Transmission-Type Circular Polarizers 46-10
 Wind Loading 46-14
- 46-4 Radio-Frequency-Band Designations 46-14
- 46-5 Antenna-Pattern Characteristics 46-15
 Continuous Line-Source Distributions 46-17
 Continuous Circular-Aperture
 Distributions 46-19
 Blockage 46-21
- 46-6 Electrically Small Horns 46-22

The design of many types of antennas, radomes, and impedance-matching devices requires the selection of appropriate dielectric materials. Strength, weight, dielectric constant, loss tangent, and environmental resistance are primary parameters of interest. Handbooks of mechanical properties are readily available ^{1,2} and will not be reproduced here. Instead, emphasis will be on electrical properties. The permittivity ϵ , permeability μ , and conductivity σ must be known at the operating frequency for a material to be completely specified electrically. For the dielectrics presented in this section, conductivity is zero, permeability equals that of free space (4 π × 10⁻⁷ H/m), and permittivity is a complex number given by

$$\epsilon = \epsilon' - j\epsilon'' = \epsilon' (1 - j \tan \delta)$$

where ϵ'/ϵ_0 and $\tan \delta$ are the dielectric constant and loss tangent, respectively, of the material and ϵ_0 is the permittivity of free space (8.854 \times 10⁻¹² F/m). For the metals discussed in this section permeability equals that of free space, permittivity is unimportant, and skin depth equals $(\pi f \mu \sigma)^{-1/2}$, where f is the operating frequency.

Dielectrics

Foam dielectrics may be obtained in stock shapes or be foamed in place (Table 46-1). They are widely used as sealers for microwave components, spacers in twist reflectors or transreflectors, and low-cross-section target supports. Specially loaded foams can be used to create a variable dielectric constant which is useful in a beam-collimation device such as a Luneburg lens. Foams are typically used in low-power applications.

High-average-power applications (in the kilowatt range) rule out all known dielectrics except ceramics. In addition, high-speed missiles with their high surface and internal temperatures typically require ceramic radomes. Commonly used ceramics are listed in Table 46-1.

Reinforced plastics (Table 46-1) are widely used as structural members for antennas, feeds, and mounting structures. Conducting surfaces can be added by flame spraying, painting, etc., to form reflectors. Sandwich construction techniques are used in radomes and polarizers. Here, two or more thin skins are stabilized against buckling with a lightweight core. The core material can be rigid foam (Styrofoam), foam-in-place foam (Eccofoam S), or a honeycomb material (Hexcell HRP). The skins can be epoxy-fiberglass, Teflon, or Mylar. The thicknesses of the skins and core are chosen to make the sandwich transparent electrically. Careful control of tolerances, glue-line thickness, and materials can produce repeatably accurate devices. Photoetched printed-circuit boards are used in polarizers, spatial filters, and frequency-selective reflecting surfaces. Additional information on dielectric porperties is given in Von Hippel.³

Metals

Copper, brass, and aluminum are the most important metals in antenna construction today. If weight is not of primary importance, brass and copper are used extensively. These two metals machine, solder, and plate so easily, with little or no special equip-

ment, that they are favorites of the model shop and the production shop alike. Complicated assemblies can be built with practically no radio-frequency (RF) discontinuities due to contact between parts. Aluminum equals or surpasses both copper and brass on all counts except plating. Although special equipment is required to weld aluminum, the resulting structure is lighter in weight than brass or copper. Very complicated shapes such as flat-plate arrays can be fabricated by dip-brazing aluminum. Table 46-2 lists the conductivity of commonly used metals.

46-2 ABSORBING MATERIALS

Microwave absorbing material is commercially available in sheet, pyramidal, block, and rod form. Pyramidal absorber is commonly used to create an RF anechoic chamber for indoor-antenna range measurements since it offers the best performance (reflected energy 50 dB down at normal incidence). Pyramidal absorber is usually constructed by loading a spongelike rubber with graphite, and it is available in 2- by 2-ft (0.6- by 0.6-m) pieces ranging in thickness from 3 in (76 mm) to 12 ft (3.7 m). It is rated in decibels of incident to reflected energy at stated frequency, polarization, and incidence angle (see Table 46-3). Performance degrades if the pyramidal tips are broken or if the absorber is exposed to weather for extended periods.

Flat sheets of absorber are available when space is limited or when the absorber must be exposed to weather, wear, or high power. The reflected energy for sheet absorber is 15 to 25 dB below the incident level. Blocks and special shapes of absorber are available for waveguide-load applications, or they can be machined to the desired shape.

The above types of absorber are currently available commercially from Advanced Absorber Products, Inc., Amesbury, Massachusetts, and Emerson and Cuming, Inc., Canton, Massachusetts.

NONSOLID SURFACES 46-3

Antenna structures are sometimes made from nonsolid metal in order to make the structure lighter, to reduce wind loading, or for special RF purposes (e.g., a frequencyselective reflector). Typical construction techniques employ metal wires, rods, strips, and patches, perforated metal, and expanded mesh. How large the "holes" in the structure can be depends on how much transmitted or reflected loss can be tolerated.

Gratings

An array of identical parallel metal wires or rods can be used to reflect energy polarized parallel to the wires and, consequently, to shield the region on the other side of the wires from parallel polarization. The perpendicularly polarized energy is negligibly affected by the wires for most geometries. The parallel and perpendicularly polarized power-transmission coefficients are given respectively by⁴

TABLE 46-1 Dielectric Data

		Freque	ncy f, Hz; v	Frequency f , Hz; values of tan δ multiplied by 10^4	8 multiplied	1 by 104
		$f = 10^2$	$f = 10^4$	$f = 10^{8}$	$f = 10^8$	$f = 10^{10}$
Ceramics						
Alsimag 243	6/60	6.30	6.28	6.22	6.10	5.76
	tan 8	12.5	4.0	3.7	m	8.5
Alsimag 393	6/60	4.95	4.95	4.95	4.95	4.95
1	tan 8	38	16	10	10	7.6
Aluminum oxide; Coors AI-200	6/60	8.83	8.82	8.80	8.80	8.79
	tan 8	14	4.8	3.3	3.0	18
Beryllium oxide	6//60	4.61	4.41	4.28	:	4.20
	tan 8	170	74	38	:	2
Magnesium oxide	6/60	9.65	9.65	9.65	9.65	:
•	tan 8	3	3	3	٣	:
Porcelain, dry-process	6/60	5.50	5.23	2.08	5.02	4.74
•	tan 8	220	105	75	86	156
Silicon nitride	6/60	:	:	:	:	5.50
	tan 8	:	:	:	:	30
Steatite 410	6/60	5.77	5.77	5.77	5.77	5.7
	tan 8	55	91	7	9	22
Titania	€//60	100	100	100	100	06
	tan 8	23	6.2	3	2.5	20
Glasses						
Fused quartz	6//50	3.78	3.78	3.78	3.78	3.78
•	tan 8	8.5	9	2	-	1
Fused silica	€//€0	3.78	3.78	3.78	3.78	3.78
	tan 8	9.9	1.1	0.1	0.3	1.7
E glass	€//€0	6.43	6:39	6.32	6.22	6.11
,	tan 8	42	27	15	23	09
Low-density materials						
Eccofoam S	¢//e0	1.05	:	1.18	:	1.47
	tan 8	20	:	9	:	0/

Hexcel HRP, 1/4-4.5; honeycomb	€/€0 tan δ	<u>:</u> :	: :	: :	: :	30
Hexcel HRH-10, 3/16-4.0; honeycomb Styrofoam 103.7	ϵ'/ϵ_0 tan δ ϵ'/ϵ_0 tan δ	1.03	 1.03	1.03		30 30 1.03 1.5
Plastics Bakelite	€/€0 tan δ	8.2 1350	6.5	5.4	4.4	3.52
Duroid 5650	¢/¢0 tan δ	: :	: : :	: : :	: : :	30
Epoxy resin RN-48	€/€0 tan δ	3.64 31	3.61 68 -	3.32 142 5.3	264 264	184
Fiberglass; laminated BK-174	¢'/¢ ₀ tan δ	14.2 2500	7.2 1600	5.3 460	260	360
Lexan	€//€0 tan δ	: :	: : :	: : ;		60
Plexiglas	€/⁄ε₀ tan δ	3.40 605	300	2.76		67
Polystyrene	€/€0 tan δ	2.56 0.5	2.56	0.7	1 2 55	4.3
Rexolite 1422	€/€0 tan δ	2.55	2.55	1.3	3.8	4.7
Polyethylene	€/€0 tan ô	2.25	2.23	2.23	2 2 2 2 00	9.9
Polyvinyl chloride, W-176	€/⁄€0 tan δ	6.21 730	1070	720	500	2.08
Teflon	€/€0 tan δ	2.1 5	2.1	2.1	2	3.7

NOTE: Properties are typical for a class of materials. Consult manufacturers for exact properties of their material.

SOURCE: Ref. 3.

Material	Conductivity, s/m at 20°C
Aluminum, commercial hard-drawn	3.54×10^{7}
Brass, yellow	1.56×10^{7}
Copper, annealed	5.80×10^{7}
Copper, beryllium	1.72×10^{7}
Gold, pure drawn	4.10×10^{7}
Iron, 99.98 percent pure	1.0×10^{7}
Iron, gray cast	$0.05 - 0.20 \times 10^7$
Steel	$0.5 - 1.0 \times 10^7$
Lead	0.48×10^{7}
Nickel	1.28×10^{7}
Silver, 99.98 percent pure	6.14×10^{7}
Tin	0.869×10^{7}
Tungsten, cold-worked	1.81×10^{7}
Zinc	1.74×10^{7}
Titanium	0.182×10^{7}

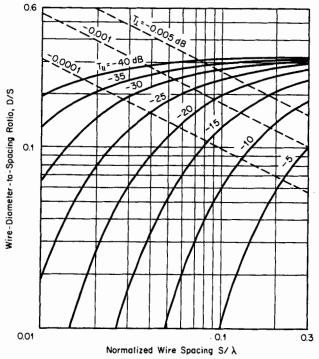


FIG. 46-1 Transmission coefficient for parallel polarization and for perpendicular polarization for a grid of round wires of diameter *D* and center-to-center spacing *S*.

TABLE 46-3 Reflection Coefficient of Typical Commercial Pyramidal Absorbing Material

				Ě	eflection	Reflection Coefficient, dB	t, dB			
Nominal	120 M H7	200 MHz	300 MHz	500 MHz	- 꽃	S	C	band	Ku band	K band
INCRIESS, III								 	,	3
				:	:	:	2	40	45	2
m	:	:	:	:	. :	Ş	40	45	20	20
5	:	:	:	:	: ;	2 4	45	05	20	20
•	:	:	:	:	٠ ک	04 6	45	20	20	20
12	:	:	:	: 6	દ્ર ૬	5 4	£ &	20	20	20
18	:	:	:	30	€	f	2	; ;	ç	Š
			90	35	40	20	S	20	2	3
24	:	. :	2 5	5	¥	5	20	S	20	20
45	:	30	35	3 ;	£ 5	3	5	20	20	8
70	30	35	40	\$ 5	2 2	R &	8 5	9	20	20
106	35	40	45	S (2 8	3 5	8 8	20	20	20
144	40	45	20	90	2	PC	3			

$$T_{\parallel} = 1 - \frac{1}{1 + \left(\frac{2S}{\lambda} \ln \frac{S}{\pi D}\right)^2}$$

$$T_{\perp} = 1 - \frac{\left(\frac{\pi^2 D^2}{2\lambda S}\right)^2}{1 + \left(\frac{\pi^2 D^2}{2\lambda S}\right)^2}$$

Figure 46-1 is a plot of these equations, where the grating has wires of diameter D, center-to-center spacing of S, and wavelength λ . These curves are derived from Lamb's work⁵ and agree well with Mumford's nomograph.⁶ The grating can be envisioned as waveguides below cutoff. Thus to be effective, (1) the electric field of the incident wave must lie in the plane determined by the axis of the grating element and the direction of propagation, and (2) S must be less than $\lambda/(1 - \sin \theta)$, where θ is the angle between the direction of propagation and the normal to the axis of the grating element. Larger spacings result in undesirable secondary reflection lobes.5

The round wires may be replaced by thin metal strips of width W perpendicular

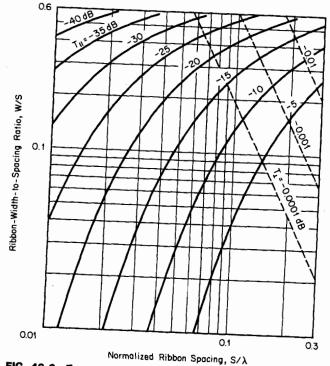


FIG. 46-2 Transmission coefficient for parallel polarization and for perpendicular polarization for a grid of broadside ribbons of width W and center-to-center spacing S.

to the direction of propagation by using metal bars or printed-circuit-board construction techniques. The transmission coefficients for the thin broadside strips are given in Fig. 46-2, which are plots of the equations⁴

$$T_{\parallel} = 1 - \frac{1}{1 + \left(\frac{2S}{\lambda} \ln \sin \frac{\pi W}{2S}\right)^2}$$

$$T_{\perp} = 1 - \frac{\left(\frac{2S}{\lambda} \ln \cos \frac{\pi W}{2S}\right)^2}{1 + \left(\frac{2S}{\lambda} \ln \cos \frac{\pi W}{2S}\right)^2}$$

Increased attenuation of the transmitted signal is obtained by orienting the strips edgewise to the direction of propagation. The length of parallel-plate waveguide below cutoff is greater, resulting in greater attenuation than for the round wires or broadside strips. Figure 46-3 gives the percentage of transmitted power for infinitely long edgewise strips of width W, center-to-center spacing S, and depth t.

The polarization sensitivity of the preceding wire and strip gratings can be eliminated by using (1) a grid of wires composed of two crossed gratings, preferably contacting each other or at least closely spaced, (2) a metal sheet periodically perforated by round or square holes, ^{8,9} or (3) expanded metal mesh¹⁰ (see Fig. 46-4).

The above structures are relatively broadband devices. Narrowband structures can be constructed by using a periodic array of strip-metal dipoles. 11 Operation below the resonant frequency of the dipoles results in little transmission loss versus essen-

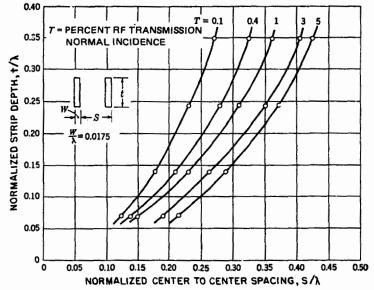


FIG. 46-3 Grating of edgewise strips: relation between strip depth and spacing for constant transmission. (*Ref. 7, page 450.*)

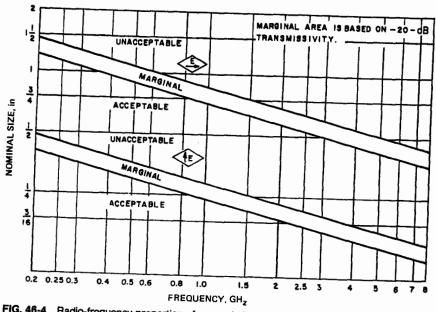


FIG. 46-4 Radio-frequency properties of expanded-metal-mesh screens. (After Ref. 10.)

tially total reflection at resonance. Dipole and crossed-dipole arrays are used in dichroic subreflectors for dual-frequency operation of a reflector antenna. Frequency-selective surfaces also may be used to scan the far-field beam of an antenna.¹²

Transmission-Type Circular Polarizers¹³

Transmission-type polarizers are anisotropic media which, when placed over a radiating aperture, convert linearly polarized signals to circularly polarized signals. They may take several forms, including the following:

- Parallel-plate structures using metal slats¹⁴
- 2 Alternating dielectric plates of differing materials¹⁵
- 3 Lattice structures using strips or rods 16,17
- 4 Meander-line photoetched structures 18
- 5 Etched-dipole arrays

These types of polarizers have been applied to linearly polarized antennas when other means of achieving circular polarization cannot be economically or easily achieved. For example, simple horns, biconical horns, and slot, horn, and dipole arrays have been successfully equipped with these devices. Recent advances in precision-photoetching technology permit close-tolerance photoetched structures which exhibit excellent uniformity of insertion phase and loss characteristics and which have been designed for use over greater-than-3:1-frequency bandwidths and with power-handling densities of up to 100 W/in² (average). Structures 1, 2, and 3 are older

approaches; the reader is referred to the References for background design information.

Structures 4 and 5 above consist of bonded sandwiches of alternating etched sheets of Mylar or Teflon-fiberglass copper-clad dielectric material (e.g., MIL-P-631 Type G Mylar or MIL-P-13949 Type GT Teflon-fiberglass). (See Fig. 46-5.) Bonding is done by using a low-loss bonding film (e.g., 3M Type HX-1000) and spacer material such as Hexcell Type HRH-10 honeycomb or Eccofoam SH polyurethane foam. A dielectric layer is generally added to these sandwiches for outer-surface environmental protection; this may consist of epoxy-fiberglass Type G-10 approximately 0.010 to 0.015 in (0.254 to 0.381 mm) thick. Structures of this type have been used on both flat and cylindrical apertures with essentially identical performance.

In use, these structures are oriented so that the incident electric field is 45° to the slow axis of the polarizer. That component of the field which lies in the slow or perpendicular direction travels through an equivalent circuit which consists of a ladder network of shunt capacitive elements. The parallel-field component travels through a network of shunt inductive elements. In meander-line polarizers, which are in predominant use today, the shunt capacitance elements arise between the parallel meandering strips 19 and, for some very broadband designs, also from added dipole elements which can extend the frequency bandwidth to higher frequencies for a given meander line.

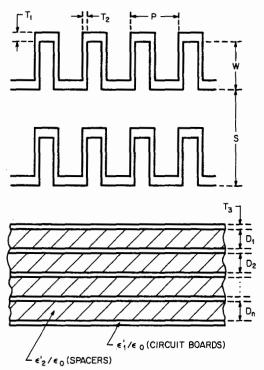


FIG. 46-5 Geometry of a meander-line circular polarizer showing meander-line and sandwich dimensions.

TABLE 46-4 Parameters of Meander-Line Polarizers Shown in Fig. 46-5

	Polarizer 121	Polarizer 223	Polarizer 324
Frequency range	4.0-8.0 GHz	7.0-14.0 GHz	2.6-7.8 GHz
Axial ratio (maximum)	3.0 dB	3.0 dB	3.0 dB
Return loss increase	5.0 dB	3.0 dB	3.0 dB
(polarizer)			
Power handling	001	:	20
(Average W/in²)			
No. of circuits	4	S	9
Circuit board			
Material	:	:	MIL-P-631 Mylar
Thickness (T3)	0.010	:	0.003
Dielectric constant	2.52	:	3.00
Spacers			
Material	Foam	Styrofoam	HRH-10-OX Honeycomb
Thicknesses (D,)	0.200, 0.300, 0.200	All 0.194	All 0.312
Dielectric constant	1.08	:	1.08

0.750 0.215 0.058 0.007	Same as outer circuit with dipoles* 0.063 by 0.500 and spaced 1.500 added on alternate meander lines	Same as outer circuit with dipoles 0.063 by 0.500 and spaced 1.500 added on each meander line	0.015 G-10 fiberglass window attached
0.570 0.154 0.118 0.031	Same as outer circuit	Same as outer circuit	
0.707 0.280 0.3535 0.018		0.707 0.370 0.3535 0.027	0.027
Outer circuit S W P T1	Next circuit S W P T1	Inner circuit S W P T1	T2 Other features

*Dipoles oriented in the w direction. NOTE: All dimensions are in inches.

Shunt inductive elements are realized by meandering copper lines etched from the copper-clad material. Because of the broadband nature of the multilayer meander-line polarizer, tolerances on the etching, alignment, and bonding of the sandwich are somewhat looser than for earlier devices such as the metal-slat or dielectric polarizers.

Etched multilayer polarizers are usually designed to be optimum in plane-wave field conditions; they can achieve better than 2-dB axial ratios, insertion losses of less than 0.2 dB, and a return loss of better than 17 dB over more than octave bandwidths. When they are applied to apertures which are less than approximately one wavelength in size or when they are forced into the flares of small horns, performance can be expected to deteriorate seriously. In addition, as with all circular polarizers, the best axial-ratio performance will be achieved when provisions are made for dissipating the cross-polarized wave which scatters from the polarizer and reenters the antenna. The latter can be accomplished by the use of a terminated orthomode coupler or by the use of a resistive sheet inside the feeding horn and aligned with the H plane.

Reflection-type polarizers can be derived from the full-transmission-type polarizers described above by using half the number of layers, which are then mounted onto a metal sheet. ¹² For narrower-band applications, simple etched-construction transmission-type polarizers can be designed by using narrow-line-width strips as in Lerner ²⁰ or two-layer arrays of etched dipoles. In the latter, phase-shift quadrature is achieved by the shunt capacitance of a dipole medium only; the differential phase shift due to the longitudinal component of the incident field is negligible. For two layers, axial ratios of less than 0.5 dB can be achieved for bandwidths of a few percent.

Multilayer polarizers are best designed by formulating a model of the susceptance of the metallic circuits on each layer²¹⁻²⁴ and then iterating the parameters of a ladder network by using an ABCD-matrix (or equivalent) analysis on a computer. Analysis is performed for both parallel and perpendicular field components. The network's insertion phase and reflection properties are then optimized for a minimum reflection coefficient for both field components and for an insertion phase-shift differential as close as possible to the ideal 90°. Such an analysis can readily model the thickness of the sandwich materials, their electrical properties, the incidence angle, and the frequency-varying nature of the individual susceptances. Reference 21 is useful in this respect. Examples of three documented broadband polarizers are tabulated in Table 46-4 and Fig. 46-5.

Wind Loading

The primary forces to which an antenna is subjected are wind, ice, vibration, and acceleration. The wind-loading force is given in Fig. 46-6 for solid and open surfaces. The loading increases the stress on a structure because of the increase in areas presented to wind and because of the additional weight due to the ice loading [approximately 57 lb/ft 3 (913 kg/m 3)].

46-4 RADIO-FREQUENCY-BAND DESIGNATIONS

Historically, letter band designations originated during World War II for secrecy reasons. These designations were continued after they had been made public, but different authors used different definitions for the band edges. One set of common-usage band

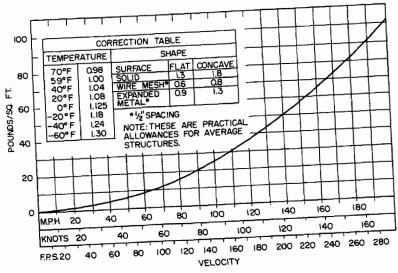


FIG. 46-6 Wind-loading data.

designations is listed in Table 46-5. Standardized bands have been defined by two official international organizations and are also listed in Table 46-5. The Institute of Electrical and Electronics Engineers (IEEE) standard is the preferred radar band designation. The International Telecommunications Union (ITU) assigns frequency allocations by international treaty. Specific frequency ranges within the ITU bands shown in Table 46-5 are assigned for radar use, and these ranges differ slightly depending on which region of the world is involved. ITU band designations are used as a general indication of the frequency of operation.

In addition, the U.S. Department of Defense has issued a directive concerning the designation of frequencies used in electronic-countermeasures (ECM) operations. Each of the 13 letter bands listed in Table 46-5 is further subdivided into 10 equal-bandwidth channels and given a phonetic and number designation such as Delta-4 (1.3 to 1.4 GHz). It is improper usage to designate a radar by an ECM band designation since the ECM designations only apply to ECM equipment.

46-5 ANTENNA-PATTERN CHARACTERISTICS

Both the initial design of an antenna and the validation of measured antenna data are greatly facilitated through the use of theoretically derived pattern characteristics. The patterns produced by a variety of one- and two-dimensional aperture distributions have appeared in the literature over the years. The task of engineers is to determine which theoretical aperture distribution best fits their physical situations so that they can assess antenna performance from the theoretical data. This can be done by measuring or calculating the actual aperture distribution and then comparing it with a variety of theoretical distributions.^{28,29} The three primary factors of concern to antenna

TABLE 46-5 Frequency-Band Designations

1555	IFFE raday hands	į					
	SDURG IRANGE	ITU freq	TU frequency bands†	Com	Common-usage bands‡	Count	Electronic- countermeasures
Rand	Frequency		Frequency				bands§
	range, GHz	Band	range, GHz	Band	Frequency	9	Frequency
HF	0.003-0.03	HF	0000		71 D (26)	Dand	range, GHz
VHF	0.03-0.3	VHF	0.003-0.03	HF.	0.003-0.03	V	
JE O	0.3-1	UHF	0.3–3	VHF	0.03-0.3	: 6	0.25
S S	7-7	SHF	3-30	I I	0.3-1	ပ	0.5-1
ပ	1 4 1 8-1	EHF	30-300	s o	7 7	Q	1-2
×	8-12			ပ	8-4-8	म ए	2-3
Κu γ	12-18			×	8-12.4	ב כ	%
¥ ½	18–27			Κu	12.4–18) H	9 %
mm mm	27–40			¥ ½	18–26.5	П	8-10 8-10
	40-200			0	26.5–40 32 so	7	10-20
				'>	50-75	ϫ,	20-40
				¥	75-110	; ۱	40-60
*From Institute	*From Institute of Electrical and Electronics Programs Control	Cs Fingineers Ct.				M	001-09

*From Institute of Electrical and Electronics Engineers Standard 521-1976, Nov. 30, 1976.

†From International Telecommunications Union, Art. 2, Sec. 11, Geneva, 1959. ‡No official international standing.

\$From AFR 5544(AR 105-86, OPNAVINST 3430.9B, MCO 3430.1), Oct. 27, 1964.

designers are gain, beamwidth, and sidelobe level. This section presents data on these three parameters for both line-source and circularly symmetric distributions.

The gain of an antenna is usually compared with that of an antenna with the same aperture dimensions but having a constant phase and amplitude distribution (i.e., uniformly illuminated). The power gain G of the antenna then is

$$G = G_0 \eta_a$$

where $G_0 = 4 \pi A/\lambda^2$ = gain of uniformly illuminated aperture

A = antenna aperture area

 λ = wavelength

 $\eta_a = \eta \eta_L = \text{antenna efficiency}$

 η = aperture illumination efficiency

 η_L = all other efficiency factors

The aperture illumination efficiency represents the loss in gain resulting from tapering the aperture distribution in order to produce sidelobes lower than those achievable from a uniform illumination. For a circular aperture η is given by a single number. For separable rectangular aperture distributions it equals the product (sum in decibels) of the efficiencies in each of the two aperture directions.

The half-power beamwidth BW of an antenna is related to the beamwidth constant- β by (Ref. 7, Chap. 6)

BW =
$$2 \sin^{-1} \left(\frac{\beta \lambda}{2L} \right) \simeq \beta \frac{\lambda}{L}$$
 (linear aperture)
BW = $2 \sin^{-1} \left(\frac{\beta \lambda}{2D} \right) \simeq \beta \frac{\lambda}{D}$ (circular aperture)

where L is the length of the linear aperture and D is the diameter of the circular aperture. The small-argument approximation for the arcsine is typically used for calculating BW. Values of β and η will be given as a function of sidelobe level for a number of distributions in the following subsections.

Continuous Line-Source Distributions

The problem of determining the optimum pattern from a line source has received considerable attention. The optimum pattern is defined as one that produces the narrowest beamwidth measured between the first null on each side of the main beam with no sidelobes higher than the stipulated level. Dolph³⁰ solved this problem for a linear array of discrete elements by using Chebyshev polynomials. If the number of elements becomes infinite while element spacing approaches zero, the Dolph pattern becomes the optimum continuous line-source pattern³¹ given by

$$E(u) = \cos \sqrt{u^2 - A^2}$$

where
$$u = \frac{\pi L}{\lambda} \sin \theta$$

 λ = wavelength

 θ = angle from the normal to aperture

The beamwidth constant β in degrees and the parameter A are given by

$$\beta = \frac{360}{\pi^2} \sqrt{\left[\operatorname{arccosh}(R)\right]^2 - \left[\operatorname{arccosh}\left(\frac{R}{\sqrt{2}}\right)\right]^2}$$

where $A = \operatorname{arccosh}(R)$

R = main-lobe-to-sidelobe voltage ratio

This Chebyshev pattern provides a useful basis for comparison even though it is physically unrealizable since the remote sidelobes do not decay in amplitude. In fact, all sidelobes have the same amplitude in the Chebyshev pattern. The aperture distribution which produces the Chebyshev pattern has an impulse at both ends of the aperture³² and produces very low aperture efficiency. In addition, the pattern is very sensitive to errors in the levels of these impulses.

Taylor³¹ developed a method for avoiding the above problems by approximating arbitrarily closely the Chebyshev pattern with a physically realizable pattern. Taylor approximated the Chebyshev uniform sidelobe pattern close to the main beam but let the wide-angle sidelobe decay in amplitude. Taylor used a closeness-parameter \bar{n} in his analysis. As \bar{n} becomes infinite, the Taylor distribution approaches the Chebyshev distribution. By using the largest \bar{n} that still produces a monotonic aperture distribution, one obtains the beamwidth constant and aperture efficiency shown in Figs. 46-7 and 46-8. Notice that the beamwidth from this Taylor distribution is almost as narrow as that from the Chebyshev distribution while still producing excellent aperture efficiency.

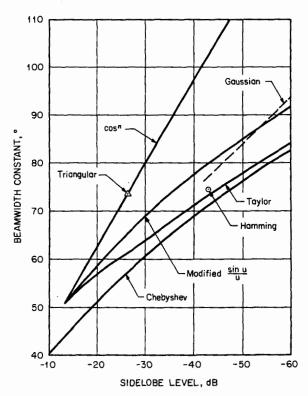


FIG. 46-7 Beamwidth constant versus sidelobe level for several line-source aperture distributions.

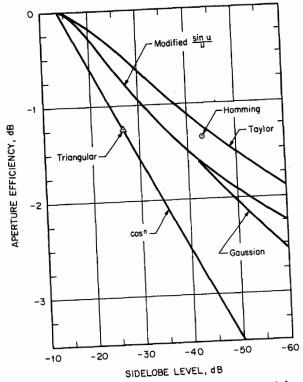


FIG. 46-8 Aperture efficiency versus sidelobe level for several line-source aperture distributions.

Several other common distributions^{7,33} are also listed in Figs. 46-7 and 46-8. The advantage of the cosⁿ $(\pi x/L)$ distribution and the sin $(\sqrt{u^2 - B^2})/\sqrt{u^2 - B^2}$ pattern is that both the distribution and the pattern for them may be obtained in closed form. This mathematical convenience is obtained at the expense of poorer beamwidth and efficiency performance as compared with the Taylor distribution.

Continuous Circular-Aperture Distributions

The Chebyshev pattern of the preceding section can also be shown to be optimum for the circular aperture. Taylor has generalized his line-source distribution to the circular case, 34,35 and his pattern approaches the Chebyshev pattern as his closeness-parameter # for the circular aperture approaches infinity. The beamwidth constant and aperture efficiency shown in Fig. 46-9 and 46-10 are obtained by using the largest # that still produces a monotonic distribution.36

The Bickmore-Spellmire distribution 37 is a two-parameter distribution which can by considered a generalization of the parabola to a power distribution.32 The Bickmore-Spellmire distribution f(r) and pattern E(u) are given by

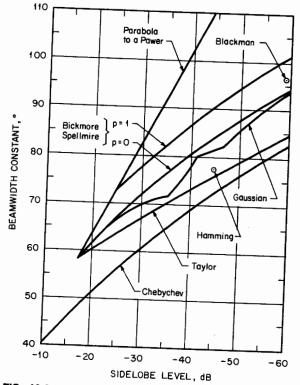


FIG. 48-9 Beamwidth constant versus sidelobe level for several circular-aperture distributions. (After Ref. 36.)

$$f(r) = p \left[1 - \left(\frac{2r}{D} \right)^2 \right]^{p-1} \Lambda_{p-1} \left(jA \sqrt{1 - \left(\frac{2r}{D} \right)^2} \right)$$

$$E(u) = \Lambda_p (\sqrt{u^2 - A^2})$$

where p and A are constants that determine the distribution, Λ is the lambda function, and

$$u = \frac{\pi D}{\lambda} \sin \theta$$

The Bickmore-Spellmire distribution reduces to the parabola to a power distribution when A = 0 and to the Chebyshev pattern when $p = -\frac{1}{2}$.

A gaussian distribution 36 produces a no-sidelobe gaussian pattern only as the edge illumination approaches zero. In general, the aperture distribution must be numerically integrated to obtain the far-field pattern. The second sidelobe of this pattern is sometimes higher than the first, which accounts for the erratic behavior of β and η in Figs. 46-9 and 46-10.

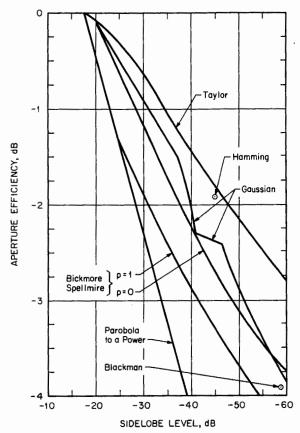


FIG. 46-10 Aperture efficiency versus sidelobe level for several circular-aperture distributions. (After Ref. 36.)

Blockage

The placement of a feed in front of a reflector results in blockage of part of the aperture energy. In the geometric-optics approximation, no energy exists where the aperture is blocked, and the undisturbed aperture distribution persists outside the blocked region.³⁸ Using a line source of length L with a \cos^n aperture distribution and a centrally located blockage of length L_b produces the gain loss and the resulting sidelobe level shown in Fig. 46-11. The corresponding changes are shown in Fig. 46-12 for a circular aperture of diameter D and a parabola to a power distribution blocked by a centrally located disk of diameter D_b . Notice that the line-source blockage affects the pattern much more rapidly than in the circular case since it affects a larger portion of the aperture. Calculation of strut-blockage effects is given by Gray.³⁹

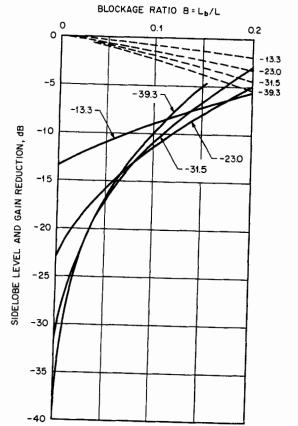


FIG. 46-11 Gain loss (----) and resulting sidelobe level (------) for a centrally blocked line-source distribution having a specified unblocked sidelobe level.

46-6 ELECTRICALLY SMALL HORNS

Aperture theory does not accurately predict the pattern characteristics of electrically small horns (on the order of a wavelength or less in size). Diffraction effects from the flange or rim around the horn (also considered to be edge currents flowing on the outside surface of the horn) markedly influence the pattern. Experimental beamwidth data⁷ for small horns without a flange are given in Fig. 46-13. These curves were obtained from measurements of a larger number of 10-dB beamwidths. Empirical formulas for these E- and H-plane curves are given respectively by

$$BW_E(10 \text{ dB}) = 88 \cdot \frac{\lambda}{B}$$
 for $\frac{B}{\lambda} < 2.5$

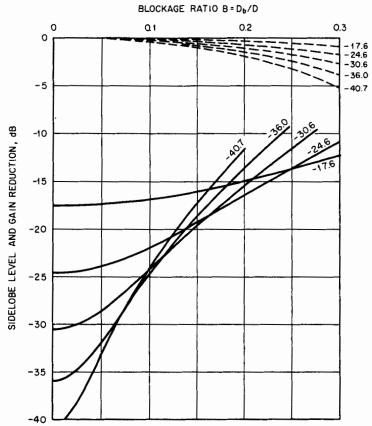


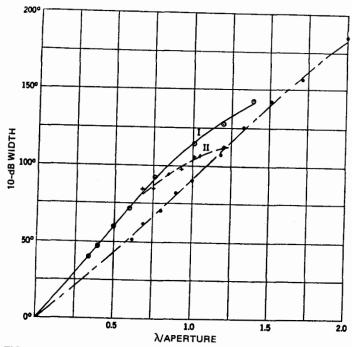
FIG. 48-12 Gain loss (————) and resulting sidelobe level (————) for a centrally blocked circular-aperture distribution having a specified unblocked sidelobe level.

$$BW_H(10 \text{ dB}) = 31^{\circ} + 79^{\circ} \frac{\lambda}{A} \qquad \text{for } \frac{A}{\lambda} < 3$$

where B and A are the E- and H-plane aperture dimensions respectively. The actual beamwidth of any particular horn may vary from the above values since different flare angles produce different phase variations over the aperture.

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Index

Abbe sine condition, 16-5, 18-8

initiate united has (Corner).
T antennas, 37-3
unidirectional VHF, 37-17 to 37-18
vertical polarization, 37-25 to 37-26
wire antennas, 37-13 to 37-14
(See also Small antennas, flush)
Altimeter antennas, 37-18
AN/FPS-85, 32-14
AN/GPN-22, 32-19 to 32-20
AN/MPQ-53, 32-17 to 32-18
AN/TPN-24, 32-8 to 32-10
AN/TPQ-37, 32-20 to 32-23
AN/TPS-59, 32-12
Angle diversity, 30-41
Annular slot (see Slots)
Antenna:
effective length, 2-3
efficiency, 1-6
pattern characteristics, 46-15 to 46-22
(See also Radiation patterns)
temperature, 31-2 to 31-3
Antennas above ground, 2-7
Aperture:
blockage, 17-20, 17-32, 30-16, 30-34 to
30 -40, 46 -21
effective, 1-6, 4-23
efficiency, 1-6
multifunction, 40-20 to 40-23
Applebaum-Howells algorithm, 22-15
Array factor, 19-9, 20-5
Arrays:
Adcock, 39-20
array of, 3-29 to 3-33
binomial, 3-21
broadband dipole curtain, 26-29 to 26-35
broadside
isotropic elements, 3-3 to 3-7
optimum, 3-24 to 3-26
practical elements, 3-7 to 3-9
circular, 26-29

	Arrays (Cont.):	Broadbanding 42 27 to 42 24
	collinear, 27-14	Broadbanding, 43-27 to 43-31
	cylindrical, 21-9 to 21-20	Bullet-probe antennas, 37-14
	Dolph-Chebyshev, 3-18, 20-9	Butler matrix, 19-10, 20-59
	ECM, 40-17 to 40-20	
	end-fire	Consultation of an ac
	improved, 3-15 to 3-17	Cancellation ratio, 23-28
	isotropic elements, 3-10 to 3-12	Candelabra antennas, 28-35
	optimum, 3-26 to 3-29	Cap-type antennas, 37-14
	practical elements, 3-12 to 3-13	Cardioid patterns, 37-31
	grating lobes, 3-7, 3-26, 19-6 to 19-7, 20-6	Cassegrain antennas, 17-33, 17-43 to 17-44
	of line sources, 12-18 to 12-19	30-21, 36-3 to 36-7
	linear	open geometry, 36-9, 36-13 to 36-14
		Casshorn, 17-23
	tapered excitation, 3-17 to 3-29 uniform, 3-2 to 3-13	Cheese antennas, 17-8
	log-periodic elements 14 47 . 14 50	COBRA DANE radar, 32-14
	log-periodic elements, 14-47 to 14-53 loops, 5-16 to 5-19	Complementary dipole and slot, 2-6
	microstrine 7 10 to 5 20	Conductors:
	microstrips, 7-19 to 7-29 open arrays, 33-10	LF antennas, 24-16 to 24-18
	optimum 2 19 4 2 2 2	Conformal arrays:
	optimum, 3-18 to 3-29 planar, 30-8	conic and generalized surface, 21-20 to
	rhombio 11 16	21-22
	rhombic, 11-16	cylindrical, 21-9 to 21-20
	slotted-waveguides, 9-16 to 9-35	fundamental principles, 21-3 to 21-9
	superdirective, 3-26	introduction, 21-2 to 21-3
	Wullenweber, 39-22	(See also Arrays; Phased arrays)
	Yagi-Uda (see Yagi-Uda antennas)	Conical monopoles, 26-15 to 26-17
	(See also Conformal arrays; Phased arrays)	Conical scanning, 34-4, 40-9
	ARSR-3, 32-7 to 32-8	Corner-reflector antennas (see Reflectors)
	AWACS, 32-11 to 32-12	Cornucopias (see Horn reflectors)
	Axial ratio, 1-7, 23-2	Corporate feed, 40-18
		Corrosion, 27-3
	Rahinet's minerals 0.12	Cosecant-squared pattern, 1-14
	Babinet's principle, 9-17	(See also Radiation patterns, shaped)
	Backfire antennas, 12-14, 17-5	Coupling, 7-9 to 7-10, 26-38 to 26-40, 27-22
	Baluns, 43-23 to 43-27	(See also Isolation)
	infinite, 14-26	Cross-polarization (see Polarization)
	TV systems, 29-7 to 29-8	Curtain antennas, 3-31
	Batwing antennas, 28-25	, = =,=
	Beacon antennas (see Marker-beacon anten-	
	nas; Microwave beacon antennas)	DF (see Radio direction finding)
	Beam efficiency, 31-6 to 31-8	Dicke radiometer, 31-11
	Beam footprints, 35-5	Dielectric channel guide, 12-22 to 12-23
	Beam waveguides (see Waveguides)	Dielectric-rod antennas, 12-21 to 12-22
	Beamwidth constant, 1-15, 46-17	Dielectric sheets and panels, 12-23 to 12-24
	Beverage antennas, 11-17	Dielectrics, 46-2
,	Biconicals, 40-2 to 40-3	Difference slope (see Monopulse)
,	Blade antennas, 37-25	Dipoles:
,	Blass matrix, 20-58	biconical, 4-12 to 4-13
1	Blockage (see Aperture)	corner reflector, 28-25
1	Breakdown, 27-4, 42-4	coupled, 4-24 to 4-25
1	Brightness temperature, 31-3	crossed, 28-9 to 28-11

Dipoles (Cont.):	Electromechanical scanning (Cont.):
cylindrical, 4-4 to 4-12	Lewis, 18-20 to 18-21
in direction-finding antennas, 39-18	Luneburg-type lenses, 18-2 to 18-7
effective length, 2-12	organ-pipe, 18-23 to 18-24
fan, 26- 21	parallel-plate, 18-11 to 18-15
folded, 4-13 to 4-17	reflectors, 17-41 to 17-52, 18-15 to 18-19
input resistance, 2-13	ring switch, 18-26
panel, 28-24	Robinson, 18-21
patterns, 4-10 to 4-12	surface of revolution, 18-11 to 18-12
on a pole, 27-16	tape scanner, 18-24 to 18-25
radiation resistance, 2-12	Element factor (pattern), 19-9, 20-27
slanted, 28-11 to 28-16	Ellipticity (see Axial ratio)
sleeve, 4-18 to 4-23	Equiangular antennas, 14-2
triangular, 29-12	Equivalence principle, 2-8 to 2-10
V, 28- 9	applications of, 2-10 to 2-11
Direction-finding antennas, 40-6 to 40-9	ESM antennas (see ECM and ESM antennas)
(See also Radio direction finding)	
Directivity, 1-5	
standard, 1-6	Fan dipole, 26-21
Discone antennas, 27-14	Far field (see Radiating far-field region)
Disk-capacitor antennas, 6-11	Far-field boundary, 1-11, 20-3
Dolph-Chebyshev distribution, 3-18, 20-9	Faraday rotation (see Polarization)
Dome antennas, 16-23 to 16-25	Ferrod antennas, 12-21 to 12-22
Dual polarization (see Polarization)	Field:
	from current distribution, 2-3
	from electric current element, 2-2
E-slot antennas, 37-28	from half-wave dipole, 2-4
Earth station antennas:	regions, 1-9
angle tracking, 36-14	FM transmitting antennas (see TV and FM
characteristics of, 36-2	transmitting antennas)
multiple-beam, 36-10 to 36-14	Foster scanner, 18-22 to 18-23
polarization, 36-15 to 36-16	Fraunhofer zone (see Radiating far-field re-
single-beam, 36-3 to 36-10	gion)
ECM and ESM antennas:	Frequency-independent antennas:
arrays, 40-19 to 40-20	basic principles, 14-2 to 14-4
direction finding, 40-6 to 40-9	log-periodic antennas, 14-32 to 14-65
introduction, 40-2	arrays of log-periodic elements, 14-47
isolation in jamming, 40-19	to 14-53
surveillance, 40-2 to 40-5	circularly polarized structures, 14-62 to
tracking, 40-9 to 40-14	14-64
transmitting, 40-14 to 40-19	dual-polarized sinuous, 14-53 to 14-62
Effective area (aperture), 1-6, 4-23	feeds for reflectors and lenses, 14-64 to
Effective height, 4-23 to 4-24	14-65
Effective length, 2-3	special considerations, 14-47
short dipole, 2-12	spiral antennas, 14-4 to 14-32, 38-9
Electromechanical scanning:	Archimedean, 14-4 to 14-8
basic principles, 18-2	cavity-backed, 14-18 to 14-28
feed motion, 18-20 to 18-26	modal characteristics of multiarm spi-
Foster, 18-22 to 18-23	rals, 14-8 to 14-10
helical slot, 18-25	multimode, 26-40 to 26-41

Frequency reuse (see Polarization) Frequency scan:	High-frequency antennas (Cont.): horizontally polarized log-periodic, 26-8
design considerations, 19-15 to 19-26 equation, 19-4	to 26-15 multimode spirals, 26-40 to 26-41
grating lobes, 19-6	other types, 26-20 to 26-23
introduction, 19-2	receiving, 26-23 to 26-29
millimeter wave, 19-26 to 19-28 monopulse, 19-10 to 19-13	simple antennas above ground, 26-5 to 26-8
practical antennas, 19-13 to 19-15 scan bands, 19-6	siting criteria for, 26-35 to 26-40 vertically polarized, 26-15 to 26-20
scan bands and multiple beams, 19-7 to 19-10	Hog-trough antennas, 33-9 Homing arrays, 37-31
theory of, 19-2 to 19-7	Horizontal rhombic antennas:
Fresnel integrals, 2-22	arrays, 11-16
Fresnel zone, 16-27, 26-35 to 26-37	circuital properties, 11-15
(See also Radiation near-field region)	crosstalk between feeders, 11-14 to 11-15
Friis transmission formula, 1-12	double rhomboid, 11-12 to 11-13
	feed-point impedance, 11-15
Coin 1.5	for HF communications, 26-20 to 26-21
Gain, 1-5	land saving, 11-12
conical horns, 15-15 to 15-17	optimum design and bandwidth, 11-11 to
corrugated horns, 15-39 to 15-40	11-12
limitations for an aperture, 2-39 to 2-40 multimode horns, 15-27 to 15-28	symmetry, 11-13
optimum horns, 15-11 to 15-12, 15-17	terminating resistance of, 11-15 to 11-16
rule of thumb, 1-15	Horn reflectors (cornucopias), 17-23, 30-20
sectoral horns, 15-8 to 15-11	to 30-21, 30-4 1
uniformly illuminated aperture, 2-39	radiometers, 31-14 to 31-16
Geometrical theory of diffraction (GTD),	Horns:
8-14, 37-20 to 37-25	absorber lined, 15-48
Glide-slope antennas, 37-17	conical .
Grating lobes (see Arrays)	corrugated, 15-34 to 15-38
Gratings, 46-3 to 46-10	dominant mode, 15-13 to 15-17
Gregorian antennas, 17-33, 17-42 to 17-44	corrugated, 15-28 to 15-45, 17-47, 23-19
GTD (see Geometrical theory of diffraction)	compact, profiled, 15-42
, , , , , , , , , , , , , , , , , , , ,	conical, 15-34 to 15-38 rectangular, 15-45
Hansen-Woodyard condition, 3-15	scalar, 15-37 to 15-39
Helical antennas:	wide-band, 15-42
arrays, 13-17 to 13-18	diagonal, 15-18 to 15-19
axial mode, 13-3 to 13-15, 13-20	dual-mode, 15-19 to 15-25, 23-16 to 23-25
fractional turn, 13-19 to 13-20	ECM transmit, 40-14 to 40-17
introduction, 13-2 to 13-3	feed patterns, 17-18, 30-10, 46-22 to 46-23
normal mode, 13-18 to 13-19	flare, effect of, 15-3 to 15-4
for TV and FM transmitting, 28-17 to 28-21	gain conical, 15-15 to 15-17
for VHF and UHF communications, 27-9	corrugated, 15-39 to 15-40
Helicone, 13-22	multimode, 15-27 to 15-28
High-frequency antennas:	optimum, 15-11 to 15-12, 15-17
for aircraft, 37-10 to 37-17	sectoral, 15-8 to 15-11
broadband dipole curtain arrays, 26-29 to	hard horns, 15-48
26- 35	improved large-gain, 30-41
general design requirements, 26-2 to 26-5	multimode, 15-18 to 15-28

	Inverted-L antennas, 24-8 to 24-10
Horns (Cont.):	Isolation, 40-19
obliquity factors of, 15-4 to 15-5	(See also Coupling)
pyramidal, 15-7 to 15-8	(000
radial-mode, 40-3	
radiometers, 31-13 to 31-14	Leaky-wave antennas:
ridge-loaded, 40-5	orray of transverse strips, 10-22
scalar, 15-37 to 15-39, 17-47	arrays, scan in two dimensions, 10-50 to
sectoral, 15-5 to 15-7	10-55
small, 46-22 to 46-23	asymmetrical slitted ridge waveguides,
soft horns	10-49
with dielectric lining, 15-47	design principles
with elliptical apertures, 15-51	periodic, 10-13 to 10-15
hard boundaries, 15-45 to 15-4/	uniform, 10-7 to 10-13
two-hybrid-mode, 15-43 to 15-45	general principles, 10-2
types of, 15-2 to 15-3	general principles, 10-2
, F,	groove guides, 10-39 holes or slots in rectangular waveguide,
Ice and snow, 27-4	10-20
Images above conducting plane, 2-7	microstrip line, 10-30 NRD guides, 10-35, 10-38, 10-52
Impedance:	NRD guides, 10-35, 10-36, 10-32
antenna, 4-6	open dielectric waveguides, 10-32
biconical dipoles, 4-12	periodic dielectric waveguides, 10-26,
coaxial lines, 42-8	10-28
conical horns, 15-17	printed circuit, 10-44, 10-53, 10-54
corrugated horns, 15-40 to 15-42	slits in circular waveguides, 10-20
cylindrical dipoles, 4-4 to 4-10	slits in rectangular waveguides, 10-18
folded dipoles, 4-13 to 4-17	specific structures
helical antennas, 13-3 to 13-5	closed waveguides, 10-17 to 10-25
horizontal rhombic, 11-15	overview, 10-15 to 10-17
HF antennas, 26-5 to 26-6	periodic open waveguides, 10-25 to 10-
microstrip antennas, 7-3 to 7-5	32
monopoles, 4-27	uniform open waveguides, 10-33 to 10-
multimode horns, 15-27 to 15-28	50
mutual, 2-13 to 2-14, 4-24 to 4-25, 25-18	stub-loaded rectangular waveguides, 10-41
pyramidal horns, 15-13	trough waveguides, 10-31
sectoral horns, 15-12 to 15-13	Lenses:
self-impedance, 2-11 to 2-13	Archer, 16-21
terminal conditions, 4-6	basic operation of, 16-2 to 16-3
two-wire lines, 42-8	bifocal, 16-5
Impedance matching and broadbanding:	bootlace, 16-19 to 16-22
baluns, 43-23 to 43-27	constrained, 16-12 to 16-22
broadbanding, 43-27 to 43-31	dielectric, 18-7 to 18-9
combinations of transformers and stubs,	dome, 16-23 to 16-25
43-21 to 43-23	Fresnel zone plate, 16-27
with distributed elements, 43-9 to 43-18	gain and sidelobe levels, 16-7 to 16-9
with distributed elements, to yet as	Luneburg, 16-26 to 16-27, 18-2 to 18-7
general, 43-2 to 43-5 with lumped elements, 43-5 to 43-9	geodesic analog, 16-27, 18-6 to 18-7
tapered lines, 43-18 to 43-20	matched surfaces, 16-9, 16-16 to 16-1/
	metal-plate 18-9 to 18-10
Insulators:	metal-plate and waveguide media, 10-12
LF antennas, 24-14 to 24-16	to 16 -17
Interferometer, 39-24 Inverted-cone antennas, 26-15 to 26-17	phased array, 16-23
Inverted-cone antennas, 20-15 to 20-17	

Lenses (Cont.):	Low-frequency antennas (Cont.):
R-2R, 16-22, 18-11 to 18-12	general applications of, 24-4
R-KR 16-22	ground systems, 24-25 to 24-28
Rotman, 16-20, 40-17	loss budget, 24-23 to 24-25
Schmidt, 18-13 to 18-14	multiantenna arrays, 24-13
for seekers, 38-7	practical design considerations, 24-8 to
surface formulas, 16-3 to 16-11	24- 20
waveguide, 16-17 to 16-19	scale-model measurements, 24-28 to 24-33
zoned, 16-6 to 16-7, 16-10 to 16-11, 16-27	typical systems, 24-33
Lewis scanner, 18-20 to 18-21	
Lightning, 27-4	
Log-periodic antennas, 27-7	Marker-beacon antennas, 37-17
HF antennas, 26-8 to 26-15, 26-17	Meander line (see Polarizers)
quasi-LPA, 39-27	Medium-frequency broadcast antennas:
TV antennas, 29-14 to 29-16	adjusting directional-antenna arrays, 25-
(See also Frequency-independent anten-	24 to 25-25
nas)	characteristics of vertical radiators, 25-5
Log-spiral antennas (see Frequency-inde-	to 25- 11
pendent antennas)	circuits for supplying power, 25-23 to 25-24
Long-wire antennas:	directional antennas, 25-13 to 25-23
Beverage, 11-17	ground systems, 25-11 to 25-13
equations for far-field strength, 11-5 to 11-7	introduction, 25-2 to 25-4
horizontal rhombic, 11-7 to 11-16	miscellaneous problems, 25-25 to 25-27
radiation patterns of, 11-2 to 11-3	Metals, 46-2 to 46-3
(See also Wire antennas)	Method of moments (see MOM)
Loops:	Microstrip antennas:
additional topics, 5-21	array design principles, 7-19 to 7-27
for aircraft antennas, 37-7	bandwidth, 7-7 to 7-9
circular, 5-9 to 5-13	circularly polarized elements, 7-14 to 7-16
coaxial arrays, 5-16 to 5-19	dual-frequency, dual polarization, 7-16 to
with planar reflector, 5-15 to 5-16	7-18
in direction-finding antennas, 39-19	efficiency of, 7-10 to 7-14
electrically large, 5-9 to 5-19	element design parameters of, 7-2 to 7-18
electrically small, 5-2 to 5-9	element patterns of, 7-5 to 7-7
ferrite-loaded receiving, 5-6 to 5-9	fixed beam arrays, 7-23 to 7-24
receiving, 5-4 to 5-5	impedance, 7-3 to 7-5
transmitting, 5-2 to 5-4	monolithic phased arrays, 7-29
	• • • • • • • • • • • • • • • • • • • •
HF receiving, 26-27 introduction, 5-2	mutual coupling, 7-9 to 7-10 omnidirectional arrays, 7-19 to 7-21
-	
parasitic, 5-17	phased arrays, 7-25 to 7-26
resonant circular, 5-13 to 5-15	series-fed arrays, 7-26 to 7-29 Microwave beacon antennas:
shielded, 5-19 to 5-21	
transmitting, 26-22 to 26-23	airborne systems, 33-13 to 33-18
TV receiving, 29-12 to 29-14	ground-based systems, 33-9 to 33-13
Yagi-Udas, 5-17 to 5-19	interrogator antennas
Loss dielectric, 42-4	design principles, 33-2 to 33-9
Low-frequency antennas:	practice, 33-9 to 33-18
for aircraft, 37-2 to 37-6	introduction, 33-2
antenna and tuning-network parameters,	Microwave propagation:
24-20 to 24-22	clear-sky-induced effects, 45-2 to 45-7
basic configuration of, 24-4 to 24-5 characteristics of, 24-5 to 24-7	introduction, 45-2 other effects, 45-13 to 45-14
CHARACTERISTICS OF 74-3 to 74-7	oniei enecis, 43-13 to 43-14

Microwave propagation (Cont.): rain-induced effects, 45-7 to 45-13 (See also Propagation) Microwave-relay antennas: cornucopias, 30-20 to 30-21 comparison of antennas, 30-22 offset paraboloidal, 30-20 paraboloidal grid reflector, 30-18 to 30-20 prime-fed paraboloidal, 30-4 to 30-18 specifications, 30-2 to 30-4 symmetrical dual reflectors, 30-21 typical path, 30-2 MOM (method of moments), 37-9 Moment-method analysis, 37-9 to 37-10 Monopoles, 4-26 to 4-32 conical, 26-15 to 26-17 in direction-finding antennas, 39-18 impedance, 4-27 pattern, 4-27 to 4-32 sleeve, 4-18 to 4-23 top-loaded, 24-8, 24-20 Monopulse, 34-4 to 34-6 cross-polarization angle crosstalk, 34-23 to 34-25 difference slope, 34-14 to 34-15 feeds, 34-15 to 34-20 in frequency-scan plane, 19-10 to 19-13 postcomparator errors, 34-22 to 34-23 precomparator errors, 34-22 to 34-23 seeker antennas, 38-7 to 38-9 single-channel, 36-14 two-channel, 40-13 to 40-14 Multibeam antennas, 17-41 to 17-52, 40-17 to 40-18

Near field (see Radiating near-field region) Night effect, 39-5 Noise (in TV receivers), 29-9 to 29-11 Notch antennas, 37-14 to 37-17 Notch pattern, 33-7

Obliquity factors:
horn antennas, 15-4 to 15-5
Omnidirectional antennas:
microstrip arrays, 7-19 to 7-21
Organ-pipe scanners, 18-23 to 18-24

Panel antennas, 27-9 to 27-10, 28-6 to 28-8 Paraboloids (see Reflectors) Patriot radar, 32-17 to 32-18 PAVE PAWS, 32-15 to 32-17 Phase errors: effects on line sources, 2-21 to 2-25 periodic, 2-32 to 2-34, 30-28 (See also Random errors) Phase shifters: Faraday rotator, 20-36 performance of, 20-44 to 20-48 Reggia-Spencer, 20-35 to 20-36 semiconductor-diode, 20-36 to 20-44 toroidal, 20-32 to 20-35 Phased arrays: bandwidth, 20-60 to 20-65 calibration for tracking antennas, 34-36 to 34-37 feed-network design, 20-48 to 20-60 introduction, 20-2 to 20-3 limited scan, 32-19 mechanical errors in tracking antennas, 34-30 to 34-31 microstrip antennas, 7-25 to 7-29 phase shifters, 20-31 to 20-48 radar multifunction, 32-14 to 32-23 radiation design, 20-25 to 20-31 radiometers, 31-16 theory of, 20-3 to 20-25 tracking antennas, 34-10 to 34-13 (See also Arrays; Conformal arrays) Pickax antennas, 37-26 Pillbox, 17-8 double-layer (folded), 18-12 to 18-13, 19-13 Poincaré sphere, 1-9 Polarization, 1-7, 23-2 to 23-10 axial ratio, 1-7, 23-2 combinations of antennas, 23-13 to 23-16 cross-polarization, 30-28 cross-polarization index, 31-7 dual-mode horns, 23-16 to 23-25 earth station antennas, 36-15 to 36-16 efficiency (loss), 1-8 23-8 error, 39-5 Faraday rotation, 45-13 frequency reuse, 23-10 to 23-13, 36-15 to **36-**16 matched incident wave, 1-7 plane of, 1-7 Poincaré sphere, 1-9 radar precipitation-clutter suppression, 23-28 to 23-30 radiometer antennas, 31-3 to 31-5

Polarization (Cont.): satellite antennas, 35-9 to 35-10 sense of, 1-7 tilt angle, 1-7	Radiation (Cont.): from electric current elements, 2-2 to 2-5 hazards, 30-29 intensity, 1-5
Polarizers, 23-25 to 23-28, 46-10 to 46-14 Polyrod antennas (see Dielectric-rod anten-	from magnetic current elements, 2-5 to 2-7 from thin slot, 2-6
nas)	Radiation patterns, 1-13
Power density, 1-5	cardioid, 37-31
Power-handling capacity (see Breakdown)	characteristics of, 46-15 to 46-22
Power transfer, 1-12	circular aperture, 2-19 to 2-21, 46-19 to
Probe antennas, 37-14	46-20
Propagation, 39-4 and 39-6	tabular data, 2-20
(See also Microwave propagation)	cosecant-squared, 1-14
Push-broom beams, 31-13	dipole, 2-4
	feed horns, 17-18, 30-10, 46-22 to 46-23
	line sources, 2-15 to 2-18, 46-17 to 46-19
Quad antennas, 5-17	prime-fed dish, 30-23
	tabular data, 2-16
	rectangular aperture, 2-19
Radar antennas:	shaped, 2-34 to 2-39, 17-14 to 17-16, 40-7
AN/FPS-85, 32-14	Radio direction finding (RDF): accuracy, 39-28
AN/GPN-22, 32-19 to 32-20	antenna elements and arrays, 39-18 to
AN/MPQ-53, 32-17 to 32-18	39-28
AN/TPN-24, 32-8 to 32-10	applications of, 39-2 to 39-3
AN/TPQ-37, 32-20 to 32-23	performance of, 39-34 to 39-36
AN/TPS-59, 32-12	propagation characteristics of, 39-4 to 39-6
applications, 32-3	system approach, 39-3
ARSR-3, 32-7 to 32-8	system design, 39-12 to 39-18
AWACS, 32-11 to 32-12	system planning, 39-6 to 39-12
COBRA DANE, 32-14	systems, 39-2
environments, 32-4	(See also Direction-finding antennas)
frequency bands, 32-3	Radio-frequency bands, 46-14 to 46-15
(See also Radio-frequency bands)	Radio-telescope antennas:
introduction, 32-2 to 32-5	brightness and flux density, 41-4
limited-scan arrays, 32-19	celestial radio sources, 41-12 to 41-14
multifunction arrays, 32-14 to 32-23	definition of, 41-2
parameters of, 32-4	passive remote sensing, 41-14 to 41-15
Patriot, 32-17 to 32-18	pattern-smoothing, 41-11 to 41-12
PAVE PAWS, 32-15 to 32-17	position and coordinates, 41-2 to 41-4
search, 32-5 to 32-12	resolution of, 41-9 to 41-11
tracking, 32-12 to 32-14	temperature and noise, 41-5 to 41-9
3D systems, 32-10 to 32-11	Radiometer:
2D systems, 32-6 to 32-7	absolute-power, 31-11
Radar equation, 1-12	autocorrelation, 31-18 to 31-20
Radar targets, 17-25 to 17-26	high resolution, 31-21 to 31-22
Radiating far-field region, 1-10, 20-3	special sensor microwave/image, 31-17 to
Radiating near-field region, 1-10	31-18
focusing, 30-29	Radiometer antennas:
Radiation:	antenna types, 31-13 to 31-16
from apertures, 2-8 to 2-11	basic principles of, 31-2 to 31-11
efficiency, 1-4, 6-4	system principles of, 31-11 to 31-13

Radomes:	Reflectors (Cont.):
configurations of, 44-7 to 44-13	periscope, 17-24 to 17-25
electrical-design data, 44-13 to 44-19	planar, 17-5 to 17-6
fabrication and testing of, 44-19, 44-22	polarization-sensitive, 17-28 to 17-30
general discussion, 44-2 to 44-7	radar targets, 17-25 to 17-26
on microwave-relay antennas, 30-17	repeaters, 17-24 to 17-25
on seekers, 38-14 to 38-15	for seekers, 38-7 to 38-9
Random errors, 2-25 to 2-34	scanning, 17-41 to 17-52, 18-15 to 18-19
continuous apertures, 2-31 to 2-32, 30-14	Schwarzschild, 18-14
to 30- 15	shaped-beam, 17-14 to 17-16, 40-7
discrete-element arrays, 2-27 to 2-31	shielded apertures, 17-22 to 17-24
Dolph-Chebyshev array, 2-29	sidelobes, 17-35 to 17-39
Rayleigh's criterion, 41-9	spherical, 17-9 to 17-10, 17-45, 18-17 to
RDF (see Radio direction finding)	18 -18, 36 -10 to 36 -11
Reactive near-field region, 1-10	surface errors, 30-28 to 30-29
Reciprocity theorem, 20-3	(See also Random errors)
Reflected lobe, 19-19	toroidal, 17-9, 17-46 to 17-52, 18-18 to
Reflection-coefficient charts, 43-5	18-19, 36-11 to 36-13
Reflectors:	transreflector, 17-28 to 17-30
Cassegrain (see Cassegrain antennas)	twist reflector, 17-28 to 17-30, 38-9
conical reflectors, 17-13	vertex-plate, 30-15 to 30-16
corner reflectors, 17-2 to 17-5, 27-10, 29-	Zeiss-cardioid, 18-14 to 18-15
21 to 29 -24	(See also Horn reflectors)
cross polarization, 30-28	Rhombic (see Horizontal rhombic antenna)
defocused, 30-12 to 30-14, 30-27 to 30-28	Ring-panel antennas, 28-21 to 28-24
dual-shaped reflectors, 17-39 to 17-41, 36-	Robinson scanners, 18-21
3 to 36- 7	Rotating-loop antennas, 39-5
ellipsoidal, 17-11 to 17-12	
elpar, 17-12	Satellite antennas:
feed displacement, 30-27	cross links, 35-19 to 35-22
feed displacement, 30-27 feed support and "strut" scattering, 17-20,	despun systems, 35-6 to 35-8
feed support and "strut" scattering, 17-20,	despun systems, 35-6 to 35-8
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas)	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas)	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas:
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10,
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning;
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14 100 percent feed, 30-6	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning; Frequency scan; Phased arrays)
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14 100 percent feed, 30-6 parabolic cylinder, 17-7 to 17-8	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning; Frequency scan; Phased arrays) Schwarzschild reflector, 18-14
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14 100 percent feed, 30-6 parabolic cylinder, 17-7 to 17-8 parabolic torus, 17-9, 17-46 to 17-52, 18-	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning; Frequency scan; Phased arrays) Schwarzschild reflector, 18-14 Seeker antennas:
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14 100 percent feed, 30-6 parabolic cylinder, 17-7 to 17-8 parabolic torus, 17-9, 17-46 to 17-52, 18-18 to 18-19, 36-11 to 36-13	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning; Frequency scan; Phased arrays) Schwarzschild reflector, 18-14 Seeker antennas: aperture techniques, 38-7 to 38-11
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14 100 percent feed, 30-6 parabolic cylinder, 17-7 to 17-8 parabolic torus, 17-9, 17-46 to 17-52, 18-18 to 18-19, 36-11 to 36-13 paraboloidal, 17-17 to 17-22, 27-12 to 27-	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning; Frequency scan; Phased arrays) Schwarzschild reflector, 18-14 Seeker antennas: aperture techniques, 38-7 to 38-11 effect of airframe, 38-4 to 38-6
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14 100 percent feed, 30-6 parabolic cylinder, 17-7 to 17-8 parabolic torus, 17-9, 17-46 to 17-52, 18-18 to 18-19, 36-11 to 36-13 paraboloidal, 17-17 to 17-22, 27-12 to 27-13, 30-4 to 30-18, 30-23 to 30-41, 36-	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning; Frequency scan; Phased arrays) Schwarzschild reflector, 18-14 Seeker antennas: aperture techniques, 38-7 to 38-11 effect of airframe, 38-4 to 38-6 evaluation of, 38-15 to 38-16
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14 100 percent feed, 30-6 parabolic cylinder, 17-7 to 17-8 parabolic torus, 17-9, 17-46 to 17-52, 18-18 to 18-19, 36-11 to 36-13 paraboloidal, 17-17 to 17-22, 27-12 to 27-13, 30-4 to 30-18, 30-23 to 30-41, 36-7 to 36-8	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning; Frequency scan; Phased arrays) Schwarzschild reflector, 18-14 Seeker antennas: aperture techniques, 38-7 to 38-11 effect of airframe, 38-4 to 38-6 evaluation of, 38-15 to 38-16 introduction, 38-2
feed support and "strut" scattering, 17-20, 17-32, 30-16 frequency-sensitive, 17-30 front-to-back ratio, 30-15 gregorian (see Gregorian antennas) hourglass reflector, 17-8 to 17-9 hypar, 17-12 hyperboloidal, 17-11 large-aperture, 17-31 to 17-52 multiple-beam, 17-41 to 17-52, 36-13 to 36-14 offset-fed, 30-20, 30-41, 36-8 to 36-10 multibeam Cassegrain, 36-13 to 36-14 100 percent feed, 30-6 parabolic cylinder, 17-7 to 17-8 parabolic torus, 17-9, 17-46 to 17-52, 18-18 to 18-19, 36-11 to 36-13 paraboloidal, 17-17 to 17-22, 27-12 to 27-13, 30-4 to 30-18, 30-23 to 30-41, 36-	despun systems, 35-6 to 35-8 earth coverage, 35-11 to 35-13 polarization of, 35-9 to 35-10 spot-beam coverage, 35-14 to 35-17 stabilization and field of view, 35-2 to 35-6 three-axis stabilized, 35-10 to 35-11 Satellite orbits, 35-3 Scale models, 2-40 Scanning antennas: leaky-wave antennas, 10-3, 10-7 to 10-10, 10-13 to 10-15 reflectors, 17-41 to 17-52, 18-15 to 18-19 (See also Electromechanical scanning; Frequency scan; Phased arrays) Schwarzschild reflector, 18-14 Seeker antennas: aperture techniques, 38-7 to 38-11 effect of airframe, 38-4 to 38-6 evaluation of, 38-15 to 38-16

Seeker antennas (Cont.):	Slotted-waveguide array (Cont.):
recent developments, 38-16 to 38-17	longitudinal-shunt-slot, 9-22 to 9-25
RF considerations, 38-2 to 38-4	planar array, 9-22
small arrays, 38-11 to 38-13	tolerances, 9-33
Sequential-lobe comparison, 34-4	traveling-wave, 9-25 to 9-30
(See also Monopulse)	non-uniformly spaced, 9-29 to 9-30
Shaped-beam antennas (see Radiation pat-	uniformly spaced, 9-27 to 9-28
terns)	Small antennas:
Sidelobes:	definition of, 6-2 to 6-3
large reflectors, 17-35 to 17-39	design procedure, 6-8 to 6-9
suppression of in microwave beacons, 33-	effective volume of, 6-5 to 6-7
6 to 33-7	efficiency over bandwidth, 6-5
Signal splitters (in TV systems), 29-8 to 29-9	efficiency over losses, 6-4
Simultaneous-lobe comparison (see Mono-	flush, 6-11 to 6-14
pulse)	radiation power factor, 6-3 to 6-4
Slots:	radiation shield, 6-7 to 6-8
annular, 6-11, 8-11, 37-26	typical, 6-9 to 6-11
	for VLF, 6-14 to 6-16
C, 9-4	(See also Loops, electrically small)
cavity-backed, 8-7 to 8-9	
characterization of, 9-6 to 9-10	Space attenuation, 17-18
moment method, 9-10	Spiral antennas (see Frequency-independent
scattering modal analysis, 9-9 to 9-10	antennas)
Stevenson's solution, 9-7	Steptrack, 36-14
variational technique, 9-7 to 9-9	Stereographic computing aids, 11-10 to 11-11
crossed, 8-9	Superdirective antenna, 2-40
on cylinders, cones and spheres, 8-16 to	Surface-wave antennas:
8-19	design principles, 12-8 to 12-20
design parameters of, 9-10 to 9-16	introduction, 10-5, 12-2
edge-wall, 9-3, 9-11 to 9-14, 9-36 to 9-37	properties and measurements of, 12-2 to
equivalent impedance, 9-5 to 9-6	12-8
on finite and curved ground planes, 8-14 to 8-16	specific structures, 12-20 to 12-25
flared, 8-4 to 8-7	T antenna, 24-8 to 24-10, 37-3
I, 9-4	T-bar transition, 8-8
inclined series, 9-4, 9-15 to 9-16	Tapered lines, 43-18 to 43-20
introduction, 8-2	Taylor distribution, 2-17, 20-8
longitudinal shunt, 9-4, 9-11, 9-35	Tracking accuracy, 34-7
ridged waveguide, 9-37	Tracking antennas:
scattering matrix, 9-5	conical scan, 34-4, 40-9
tapered, 8-4 to 8-7	electrical design of, 34-14 to 34-25
TV and FM antennas, 28-29 to 28-35	introduction, 34-2, 34-7
in waveguides, 8-2 to 8-4, 9-2 to 9-6	mechanical design of, 34-25 to 34-31
waveguide-fed, 8-9 to 8-14	requirements, 34-7 to 34-13
Slotted-waveguide array:	sequential-lobing, 40-10 to 40-13
design methods, 9-16 to 9-20	system calibration, 34-31 to 34-37
fabrication techniques, 9-33 to 9-35	two-channel monopulse, 40-13 to 40-14
introduction, 9-2, 10-5	Tracking precision, 34-7
power handling, 9-31 to 9-33	Transformer:
resonant, 9-20 to 9-25	binomial, 43-14 to 43-15
edge wall shunt-slot, 9-25	Chebyshev, 43-15 to 43-17
linear array, 9-20 to 9-22	quarter-wave, 43-12
	demon

Transmission lines: coaxial flexible, 42-17 to 42-19 semiflexible, 42-17 solid conductor, 42-13 to 42-17 equations, 42-6 to 42-7 general characteristics of, 42-4 open-wire, 42-5 strip, 42-8 to 42-13 TV systems, 29-6 to 29-9 wires in enclosures, 42-5 to 42-8 (See also Waveguides) Transreflector, 17-28 to 17-30 Triatic antenna, 24-11 Trideco antenna, 24-12 TV and FM transmitting antennas: broadcast bands, 28-2 circularly polarized, 28-8 to 28-24 horizontally polarized, 28-24 to 28-35 introduction, 28-2 to 28-6 multiple-antenna installations, 28-35 panel-type, 28-6 to 28-8 TV frequency allocations, 29-2 TV receiver-system noise, 29-9 to 29-11 TV receiving antennas: broadband Yagi-Uda, 29-19 to 29-21 corner-reflector, 29-21 to 29-24 log-periodic dipole array, 29-14 to 29-16 loops, 29-12 to 29-14 single-channel Yagi-Uda, 29-16 to 29-19 triangular dipole, 29-12 types of, 29-5 to 29-6 TV receiving systems, 29-5 to 29-9 TV signal strength, 29-3 TV transmission lines, 29-6 to 29-9 Twist reflector, 17-28 to 17-30, 38-9

UHF communication antennas (see VHF and UHF communication antennas)

Valley-span antennas, 24-12 to 24-13 Variometers, 24-22 VHF and UHF communication antennas: base-station, 27-13 to 27-20 introduction, 27-2 mobile, 27-20 to 27-22 point-to-point links, 27-6 to 27-13 system considerations, 27-22 to 27-24 system planning, 27-2 to 27-6 Visible space, 20-6 Vivaldi aerial, 8-4 Volutes, 13-19 VOR, 37-28

Waveguides: beam, 17-26 to 17-28, 42-44 circular, 42-33 to 42-34 dielectric, 42-42 to 42-44 elliptical, 42-45 fin-line, 42-38 flexible, 42-35 groove, 10-39 hollow-tube, 42-19 to 42-38 multimode, 42-44 NRD, 10-35, 10-38, 10-52 open dielectric, 10-32 optical-fiber, 42-44 to 42-45 radial line and biconical, 42-40 to 42-42 rectangular, 42-31 to 42-33 ridged, 42-35 to 42-38 simulators, 20-27 standard sizes of, 42-34 to 42-36 trough, 10-33, 42-38 to 42-40 (See also Transmission lines) Wavelength: cutoff, 42-4 guide, 42-4 Whip antenna, 26-20 Whisk-broom scanning, 31-13 Widrow algorithm, 22-17 Wind, 27-3, 46-14 Wire antennas, 37-13 to 37-14 (See also Long-wire antennas)

Yagi-Uda antennas, 3-13 to 3-15, 12-23, 27-6 to 27-7 loops, 5-17 to 5-19 TV broadband, 29-19 to 29-21 TV single-channel, 29-16 to 29-19

Wullenweber array, 39-22

Zeiss-cardioid reflector, 18-14 to 18-15 Zigzag antennas, 28-16 to 28-17, 28-26 to 28-28

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Di Giacomo • VLSI Handbook

Fink and Beaty • Standard Handbook for Electrical Engineers

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Kaufman and Seidman • Handbook for Electronics Engineering Technicians

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Williams and Taylor • Electronic Filter Design Handbook

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Skolnik • Introduction to Radar Systems

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