

1. Criss Cross Multiplication (UT-Ukubwa-Tinyak)

a. Two digits Multiplication

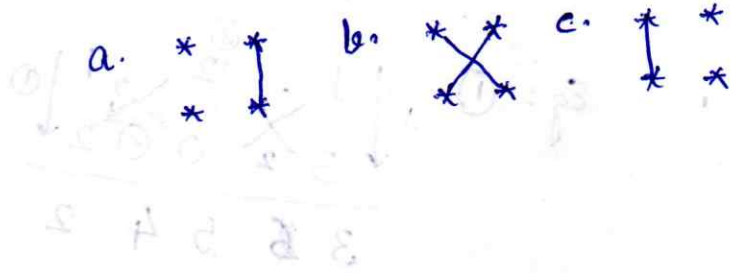
principle 1-2-1

①

$$\begin{array}{r}
 32 \\
 \times 12 \\
 \hline
 64 \\
 320 \\
 \hline
 384
 \end{array}$$

S1 $3 \times 2 = 6$
 S2 $(3 \times 2) + (1 \times 2) = 8$
 S1 $3 \times 1 = 3$

$$\begin{array}{r}
 32 \\
 \times 12 \\
 \hline
 64 \\
 320 \\
 \hline
 384
 \end{array}$$



② 31×25

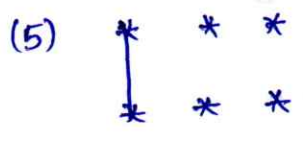
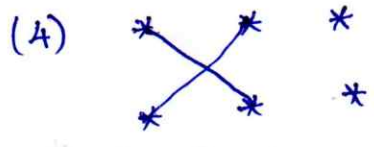
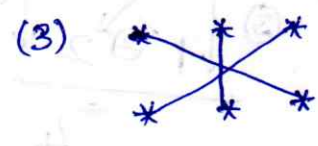
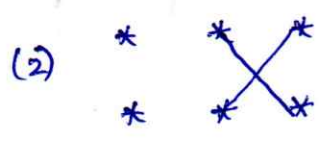
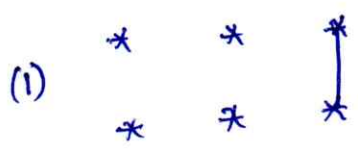
$$\begin{array}{r}
 31 \\
 \times 25 \\
 \hline
 155 \\
 620 \\
 \hline
 775
 \end{array}$$

③ 43×84

$$\begin{array}{r}
 43 \\
 \times 84 \\
 \hline
 172 \\
 3440 \\
 \hline
 3612
 \end{array}$$

b. Three Digit Multiplication

principle 1-2-3-2-1



Eg: ①

$$\begin{array}{r}
 1 \downarrow \\
 3 \ 2 \ 0 \\
 \times 2 \ 1 \ 0 \\
 \hline
 3 \ 6 \ 5 \ 4 \ 2
 \end{array}$$

Eg: ②

$$\begin{array}{r}
 0 \downarrow \\
 3 \ 1 \ 1 \ 2 \ 7 \ 3 \ 2 \ 0 \\
 \times 3 \ 1 \ 1 \ 3 \ 0 \ 2 \ 0 \\
 \hline
 3 \ 1 \ 4 \ 0 \ 2 \ 0 \\
 \hline
 4 \ 4 \ 0 \ 2 \ 0
 \end{array}$$

a.

$$\begin{array}{r}
 342 \\
 506 \\
 \hline
 173052
 \end{array}$$

b.

$$\begin{array}{r}
 412 \\
 903 \\
 \hline
 372036
 \end{array}$$

c.

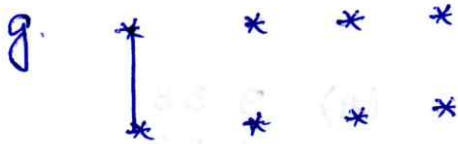
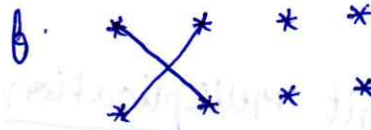
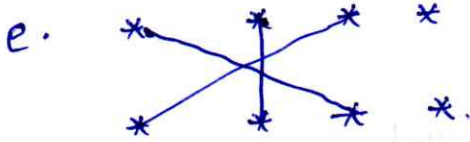
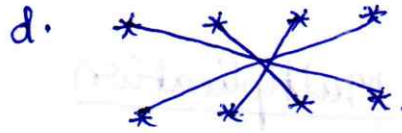
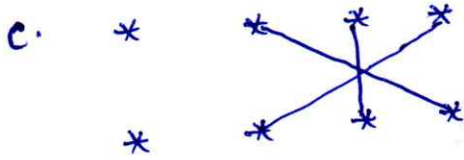
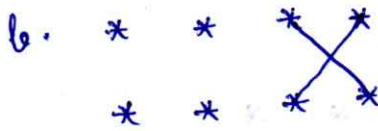
$$\begin{array}{r}
 555 \\
 222 \\
 \hline
 123210
 \end{array}$$

d.

$$\begin{array}{r}
 391 \\
 274 \\
 \hline
 107134
 \end{array}$$

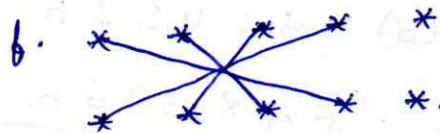
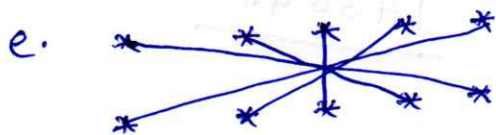
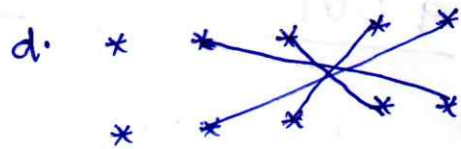
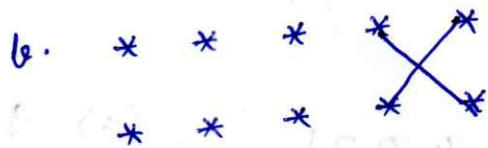
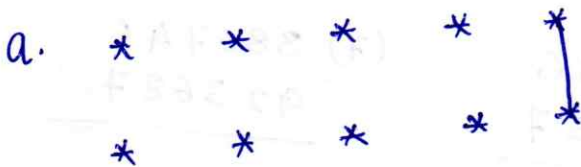
c. Four digit Multiplication

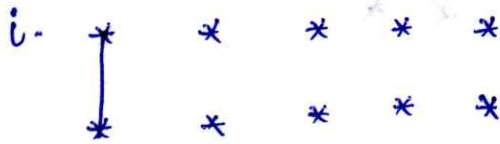
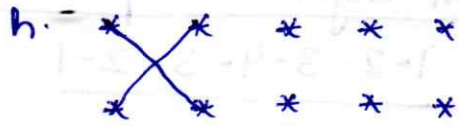
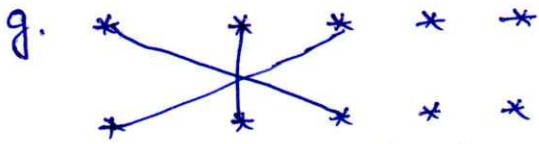
principle 1-2-3-4-3-2-1



d. Five digit Multiplication

principle 1-2-3-4-5-4-3-2-1





e. Six digit Multiplication

principle 1-2-3-4-5-6-5-4-3-2-1

f. Seven digit Multiplication

principle 1-2-3-4-5-6-7-6-5-4-3-2-1

EXERCISE

(1)
$$\begin{array}{r} 23 \\ \times 12 \\ \hline \end{array}$$

(2)
$$\begin{array}{r} 41 \\ 13 \\ \hline \end{array}$$

(3)
$$\begin{array}{r} 423 \\ 202 \\ \hline \end{array}$$

(4)
$$\begin{array}{r} 358 \\ 132 \\ \hline \end{array}$$

(5)
$$\begin{array}{r} 4321 \\ 9101 \\ \hline \end{array}$$

(6)
$$\begin{array}{r} 94386 \\ 47257 \\ \hline \end{array}$$

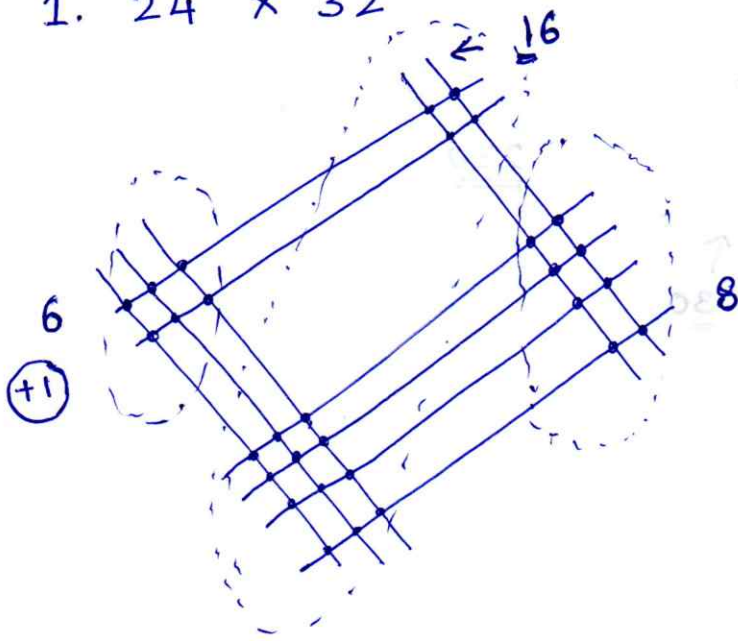
(7)
$$\begin{array}{r} 386745 \\ 923687 \\ \hline \end{array}$$

(8)
$$\begin{array}{r} 1854375 \\ 6483268 \\ \hline \end{array}$$

(9)
$$\begin{array}{r} 9483627 \\ 143648 \\ \hline \end{array}$$

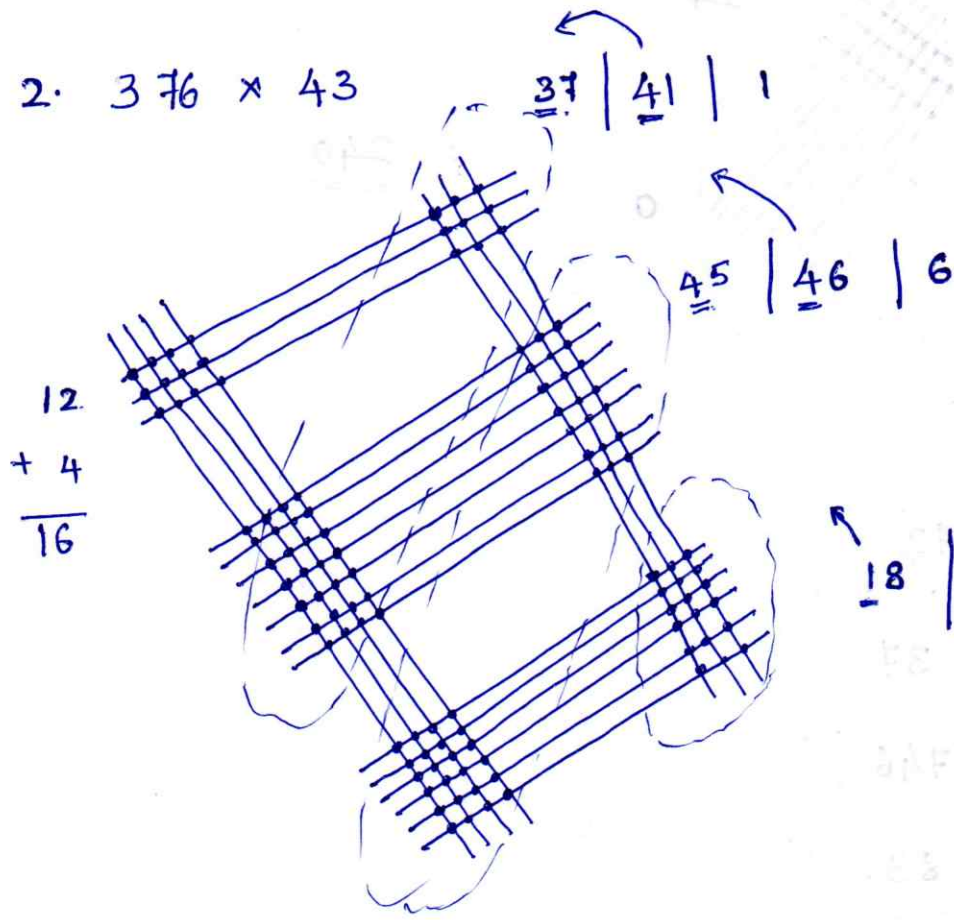
2. Multiplication Technique (Line method)

1. 24×32



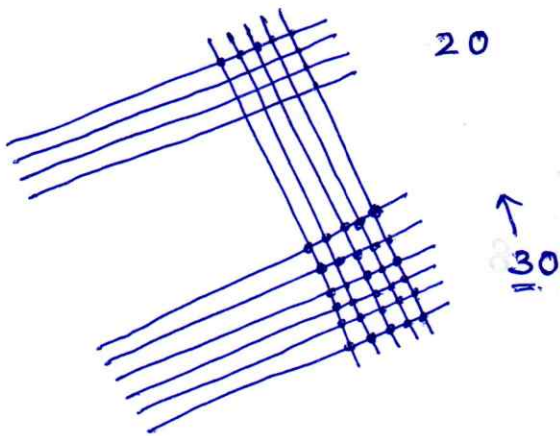
= 768

2. 376×43



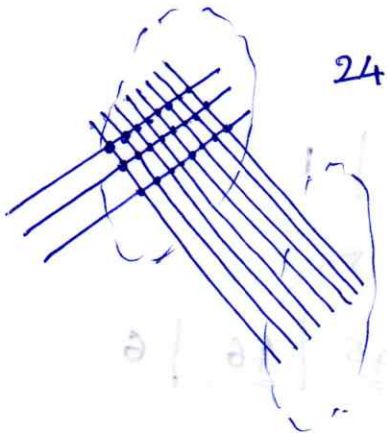
= 16168

3. 46 x 5



= 230

4. 30 x 8



= 240

EXERCISE

1. 48 x 72

2. 246 x 37

3. 482 x 746

4. 400 x 83

5. 47 x 4

6. 760 x 32

3. Base Method (Nikhilam)

* powers of 10.

a. condition: Numbers close to base Numbers

Eg:- close to 10, 100, 1000 etc.

We Find the answer in two parts
LHS & RHS.

Suppose 97 & 99 to be multiplied.
These Numbers are close to 100

Diff. 97 → -3 (base)
99 → -1

- Steps:
- ① Find the base & difference
 - ② NO. of digits on the RHS = NO. of zeros in the base
 - ③ Multiply the differences on the RHS.
 - ④ Put the cross Answer on the LHS.

Eg: ①

$$\begin{array}{r} 97 \\ 99 \\ \hline \end{array}$$

S ① Base = 100.
Diff 97 - 3.
99 - 1

S ②

LHS	RHS.
	03
	--

S ③

97 - 3	↓*
99 - 1	↓
LHS	RHS.
	03

S ④:

97 - 3	
99 - 1	
(99-3) LHS	RHS
or (97-1)	03
↓	
96	
--	
<u>ANS: 9603</u>	

3- base Method (minimizing)

Eg: ② 9989
9995

S1 ① Base - 10000

Diff: 9981 - 11
9995 - 5

S2 ② 9989 - 11
9995 - 5

LHS	RHS

S3 ③ 9989 - 11
9995 - 5

LHS	RHS
	0055

S4 ④

LHS	RHS
9984	0055

(9989-5)
or
(9995-11)

= 99840055

Eg. ③ $\begin{array}{r} 9999999 \\ 9999998 \end{array}$

SI ① $\begin{array}{r} B - 10000000 \\ \text{Diff} - \begin{array}{r} -1 \\ -2 \end{array} \end{array}$

② $\begin{array}{r|l} \text{LHS} & \text{RHS} \\ \hline & \end{array}$

③ $\begin{array}{r} 9999997 \\ 0000002 \end{array}$

Eg. ④ 9750×9998

$\rightarrow 10000$
 $\rightarrow -250$
 $\rightarrow -2$

$\rightarrow \begin{array}{r|l} \text{LHS} & \text{RHS} \\ \hline 9748 & 0500 \\ \hline 97480500 \end{array}$

⑤ $1007 \text{ by } 1010$

$\rightarrow 10000$
 $\rightarrow +7$
 $\rightarrow +10$

$\rightarrow \begin{array}{r|l} \text{LHS} & \text{RHS} \\ \hline 1007+10 & 1017 \\ 1010+7 & \\ \hline 10170070 \end{array}$

EXERCISE

$$667 - 333$$

$$997 - 3$$

$$\underline{664 \mid 999}$$

$$808 - 192$$

$$999 - 1$$

$$\underline{807 \mid 192}$$

$$1230 + 230$$

$$1003 + 3$$

$$\underline{1233 \mid 690}$$

$$9988 - 12$$

$$9996 - 4$$

$$\underline{9984 \mid 0048}$$

$$997 - 23$$

$$980 - 20$$

$$\underline{957 \mid 460}$$

$$9500 - 500$$

$$9991 - 9$$

$$\underline{9491 \mid 4500}$$

$$10020 + 20$$

$$10020 + 20$$

$$\underline{10040 \mid 0400}$$

$$123456 + 23456$$

$$100001 + 1$$

$$\underline{123457 \mid 23456}$$

b. Condition:

When the no. of digits exceed in RHS.

Eg: ① 950×950

→ 1000.

 + 50

 + 50.

→ $\underline{900 \mid 2500}$

⇒ 902500

② 1200×1020

→ 1000.

 + 200

 + 20

→ $\underline{1200 \mid 4000}$

= 1224000

③. $150 \times 140.$

$$\begin{array}{r} 100 \\ + 50 \\ + 40 \\ \hline \end{array}$$

LHS	RHS
190	2000
210000	210000
	<u>21000</u>

④ $112 + 12$
 $110 + 10$

$122 \mid \underline{20}$

12320

⑤ $1300 + 300$
 $1020 + 20$

$1320 \mid \underline{6000}$

1326000

⑥ $9200 - 800$
 $9200 - 800$

$8400 \mid \underline{0000}$

~~94040000~~

84640000

⑦ $17 + 7$
 $18 + 8$

$25 \mid \underline{56}$

306

⑧ $850 - 150$
 $993 - 7$

$843 \mid \underline{1050}$

844050

⑨ $75 - 25$
 $95 - 5$

$70 \mid \underline{125}$

7125

c. Multiplying a number above base with below base.

Eg: ① 95×115

$$\begin{array}{r} 100 \\ 95 - 5 \\ 105 + 15 \\ \hline \end{array}$$

RHS	RHS
110	(-75)

$= (110 \times 100) - 75$
 $= 11000 - 75 = \underline{\underline{10925}}$

imp:
LHS x Base

Eg: ② Multiply 1044 by 998.

$$\begin{array}{r} 1000 \\ 1044 + 44 \\ 998 - 2 \\ \hline 1042 \mid -088 \end{array}$$

$$= (1042 \times 1000) - 088$$

$$= 1042000 - 088$$

$$= \underline{1041912}$$

Eg: ③ 100032 by 99990.

$$\begin{array}{r} 100000 \\ + 32 \\ - 10 \\ \hline (-00320) \end{array}$$

$$100022 \mid$$

$$= 100022 \times 100000 - 00320$$

$$= 10002200000 - 00320$$

$$= \underline{10002199680}$$

④ 800 - 200.

$$\begin{array}{r} 1004 + 4 \\ \hline (-800) \end{array}$$

$$804$$

$$= 804 \times 1000 - 800$$

$$= 804000 - 800$$

$$= \underline{803200}$$

⑤ 120 + 20

$$\begin{array}{r} 97 - 3 \\ \hline 117 \mid (-060) \end{array}$$

$$= 117 \times 100 - 60$$

$$= 11700 - 60$$

$$= \underline{11640}$$

⑥ 14 + 4

$$\begin{array}{r} 9 - 1 \\ \hline 13 \mid -04 \end{array}$$

$$= 13 \times 10 - 04$$

$$= 130 - 04$$

$$= \underline{126}$$

d. Multiplying Numbers by different bases.

Eg: ① 85×995

* Convert the Numbers to same base.

i.e. 85 to 850.

* In the Result divided by multiplied by (the value)
Eg: 10 in this case.

$$\begin{array}{r} 850 - 150 \\ 995 - 5 \\ \hline \end{array}$$

$$845 \mid \begin{array}{l} \text{RHS.} \\ 750 \end{array}$$

$$= \underline{845750}$$

$$\text{Divide by } 10 \rightarrow \underline{84575}$$

Eg: ② ~~998~~ 102 by 999.

* Multiply 102 by 10.

$$\begin{array}{r} 1020 + 20 \\ 999 - 1 \\ \hline 1019 \mid (-020) \end{array}$$

$$= 1019 \times 1000 - 020$$

$$= 1019000 - 020$$

$$= 1018980$$

$$\div \text{ by } 10 = \underline{101898}$$

Eg: ③ 9995×86 .

$$x - 86 \times 100 = 8600$$

$$\begin{array}{r} 9995 - 5 \\ 8600 - 1400 \\ \hline \end{array}$$

$$8595 \mid 7000$$

$$\underline{85957000} \quad 85957000$$

$$\div 100 = \underline{859570}$$

Eg: ④

$$73 \times 997$$

$$\times 73 \text{ by } 10 = 730$$

$$730 - 270$$

$$997 - 3$$

$$\begin{array}{r} 727 \overline{) 810} \\ \underline{727} \\ 810 \\ \underline{727} \\ 810 \\ \underline{727} \\ 810 \\ \underline{727} \\ 810 \end{array}$$

$$= 727810$$

$$\div 10 = \underline{\underline{72781}}$$

Eg: ⑤

$$73 \times 990$$

$$\Rightarrow 990/10 = 99$$

$$73 - 27$$

$$99 - 1$$

$$\begin{array}{r} 73 - 27 \\ 99 - 1 \\ \hline 72.27 \end{array}$$

$$= 7227 \times 10$$

$$= \underline{\underline{72270}}$$

Eg: ⑥

$$99 \times 1005$$

$$\rightarrow 99 \times 10 = 990$$

$$990 - 10$$

$$1005 + 5$$

$$\begin{array}{r} 995 \overline{) 1005} \\ \underline{995} \\ 1005 \\ \underline{995} \\ 1005 \\ \underline{995} \\ 1005 \end{array}$$

$$= 995 \times 1000 - 50$$

$$= 995000 - 50$$

$$= 994950$$

$$= \underline{\underline{99495}}$$

\div by 10.

e. When Base is not power of 10.

In Base Method we take 10, 100, 1000 etc. as bases. which are called as Actual base.

But, Here we will use 40, 50, 600 etc. as the bases, which are called as Working base

Eg: ① 48×48 .

Actual base - 100.

Working base - $100/2 = 50$.

$$\begin{array}{r} 48 - 2 \\ 48 - 2 \\ \hline 2) 46 \mid 04 \\ \hline 2304 \end{array}$$

Since 50 (working base is obtained by dividing 100/2)
* We divided LHS by 2 (i.e. $46/2 = 23$).

Alternative :-

Actual base - 10.

Working base - $10 \times 5 = 50$

$$\begin{array}{r} 48 - 2 \\ 48 - 2 \\ \hline 46 \mid 4 \\ = 46 \times 5 \mid 4 \\ 230 \\ = \underline{2304} \end{array}$$

Eg: ② 27×28 .

Actual base = 100

Working base = $\frac{100}{5} = 20$.

$$\begin{array}{r} 27 + 7 \\ 28 + 8 \\ \hline 5) 35 \mid 56 \\ \hline \cancel{145} 56 \\ \hline 17556 \end{array}$$

= 756

Eq. (3)

$$59 \times 58$$

Actual base = 100

Working base = 50 = $\frac{100}{2}$

$$\begin{array}{r}
 59 + 9 \\
 58 + 8 \\
 \hline
 67 \quad | \quad 72
 \end{array}$$

Actual base = 10

Working base = $10 \times 6 = 60$

$$\begin{array}{r}
 59 - 1 \\
 58 - 2 \\
 \hline
 57 \quad 2 \\
 \times 6 \\
 \hline
 34202
 \end{array}$$

Eq. (4)

$$31 \times 32$$

AB = 10

WB = $10 \times 3 = 30$

$$\begin{array}{r}
 31 + 1 \\
 32 + 2 \\
 \hline
 33 \quad | \quad 2 \\
 \times 3 \\
 \hline
 992
 \end{array}$$

Eq. (5)

$$57 \times 57$$

AB = 10, WB = $10 \times 6 = 60$

$$\begin{array}{r}
 57 - 3 \\
 57 - 3 \\
 \hline
 54 \quad 9 \\
 \times 6 \\
 \hline
 3249
 \end{array}$$

Eg: ⑥

$$395 \times 396$$

$$AB = 100$$

$$WB = 100 \times 4 = 400$$

$$\begin{array}{r}
 395 - 5 \\
 396 - 4 \\
 \hline
 394 \mid 20 \\
 \times 4 \\
 \hline
 1564 \mid 20 \\
 \hline
 \end{array}$$

Eg: ⑦

$$228 \times 246$$

$$AB = 1000$$

$$WB = 1000 \div 4 = 250$$

$$\begin{array}{r}
 228 - 22 \\
 246 - 4 \\
 \hline
 224 \mid 088 \\
 \div 4 \\
 \hline
 56088 \\
 \hline
 \end{array}$$

Eg: ⑧

$$45 \times 45$$

$$AB = 100 ; WB = 100 \times 5 = 500$$

$$\begin{array}{r}
 45 - 5 \\
 45 - 5 \\
 \hline
 40 \mid 25 \\
 \times 5 \\
 \hline
 200 \mid 25 \\
 = \underline{\underline{2025}}
 \end{array}$$

$$AB = 10 ; WB = 10 \times 4 = 40$$

$$\begin{array}{r}
 45 + 5 \\
 45 + 5 \\
 \hline
 50 \mid 25 \\
 \times 4 \\
 \hline
 200 \mid 25 \\
 = \underline{\underline{2025}}
 \end{array}$$

P Eg: ⑨ 58×42 .

$AB = 10$

$WB = 10 \times 5 = 50$.

$$\begin{array}{r} 58 + 8 \\ 42 - 8 \\ \hline \end{array}$$

$$\begin{array}{r} 50 \mid -64 \\ \times 5 \\ \hline \end{array}$$

$$250 \mid (-64)$$

$= 250 \times 10 - 64$

$= 2500 - 64$

$= \underline{\underline{2436}}$

Eg: ⑩ 55×45

$AB = 10; WB = 10 \times 5 = 50$.

$$55 + 5$$

$$45 - 5$$

$$\begin{array}{r} 50 \mid -25 \\ \times 5 \\ \hline \end{array}$$

$$250 \mid -25$$

$= 250 \times 10 - 25$

$= 2500 - 25$

$= \underline{\underline{2475}}$

Eq: ⑪ 45×42

$AB = 100; WB = \frac{100}{2} = 50.$

$$\begin{array}{r} 45 - 5 \\ 42 - 8 \\ \hline 2) 37 \mid 40 \end{array}$$

$18\frac{1}{2} \mid 40.$

$= 18(50+40)$

$= \underline{\underline{1890}}$

$AB = 10; WB = 10 \times 4$

$$\begin{array}{r} 45 + 5 \\ 42 + 2 \\ \hline 47 \mid 10 \\ \times 4 \mid \\ \hline 188 \mid 10. \\ = \underline{\underline{1890}} \end{array}$$

Eq: ⑫ 245×248

$AB = 1000; WB = \frac{1000}{4} = 250.$

$$\begin{array}{r} 245 - 5 \\ 248 - 2 \\ \hline 4) 243 \mid 10 \\ \times 4 \mid \end{array}$$

$60\frac{3}{4} \mid 10.$

$= 60\left(\frac{3}{4} \times 1000 + 10\right)$

$= 60(750 + 10)$

$= \underline{\underline{60760}}$

EXERCISE

Q.1. Multiply the following numbers:

a. 990×994

b. 999993×999999

c. 1002×10100

d. 1050×1005

Q. 2. Multiply the following numbers where the answers in RHS exceeds the no. of zeros in the base.

- a. 16×17
- b. 1500×1040
- c. 9300×9500
- d. 860×997

$$\begin{array}{r} 50 \quad 100. \\ \underline{4} \\ 154 \mid \underline{200} \\ \underline{1560000} \end{array}$$

Q. 3. Calculate the product of the following (one number is above the base & the other number is below the base).

- a. 96×104
- b. 890×1004
- c. 10080×9960
- d. 970×1010

Q. 4. Multiply the following numbers using different bases.

- a. 73×997
- b. 94×990
- c. 82×9995
- d. 102×1010

Q. 5. Multiple the numbers using actual & working bases.

- a. 49×48
- b. 22×22
- c. 53×49
- d. 18×17
- e. 499×496

$$\begin{array}{r} 484. \\ \underline{+2} \\ \underline{+2} \\ 24 \quad 4 \\ \quad 2 \\ \underline{484} \end{array}$$