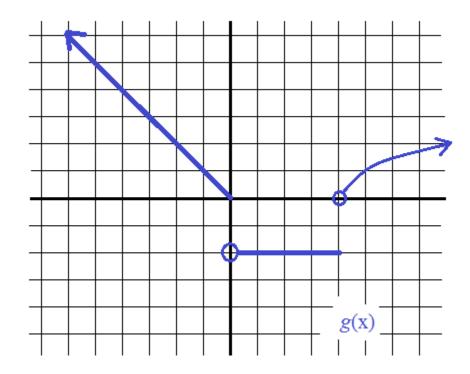
Piecewise Functions and f(x) Notation



Includes notes, examples, graphs, strategies, and practice questions (with solutions)

Functional Notation and Piecewise Functions

I. Functional Notation

What is it? A way to express a function.

Examples:
$$f(x) = 3x + 8$$

f identifies the function

x (inside the parentheses) is the "argument"

$$f(2) = 3(2) + 8 = 14$$

(substitute the x for 2)

$$f(a) = 3(a) + 8 =$$
 $3a + 8$

$$g(x) = 6x^2 - 3x + 7$$

g identifies the function

x (inside the parentheses) is the "argument"

$$g(4) = 6(4)^2 - 3(4) + 7$$

(substitute each x with a 4)

$$= 96 - 12 + 7 = 91$$

$$g(-1) = 6(-1)^{2} + 3(-1) + 7$$
$$= 6 \cdot 1 + (-3) + 7 = 10$$

(replaced each x with -1)

$$h(t) = 3x + 4t - 5$$

h identifies the function

t (inside the parentheses) is the "argument"

$$h(3) = 3x + 4(3) - 5$$

(substitute the t with a 3)

$$= 3x + 7$$

$$h(x+5) = 3x + 4(x+5) - 5$$
$$= 3x + 4x + 20 - 5 = 7x + 15$$

(replaced the t with (x + 5))

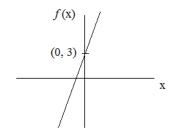
II. f(x) vs. y

What is the difference between f(x) = 4x + 3 and y = 4x + 3?

The notation is different; everything else is the same... Every input x will have the same output in either expression.

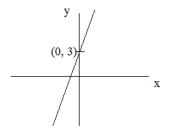
$$f(0) = 3$$

$$f(3) = 15$$



$$y = 4(0) + 3 = 3$$

$$y = 4(3) + 3 = 15$$

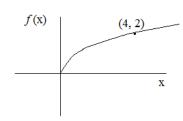


What is the difference between $f(x) = \sqrt{x}$

and
$$y = \sqrt{x}$$
?

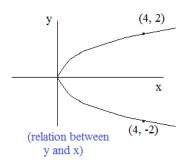
In this case, there is a subtle difference: f(x) is a function but, y could be a relation (or function).

$$f(4) = 2$$



(function: only one output for each input)

$$y = \sqrt{4} = \pm 2$$

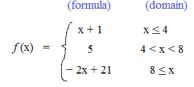


III. Piecewise Function

What is it? A function that uses different calculations in different parts of its domain. (the formula will depend on the input!)

"Piecewise defined functions" might be called *split functions*

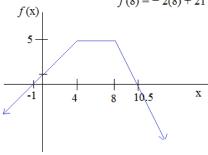
Examples:



$$f(-2) = (-2) + 1 = -1$$

$$f(4) = 5$$

$$f(8) = -2(8) + 21 = 5$$



Note: this is a continuous function

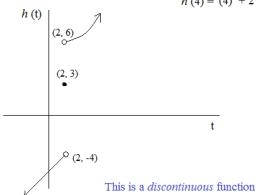


$$h(t) = \begin{cases} t-6 & t < 2\\ 3 & t = 2\\ t^2 + 2 & t > 2 \end{cases}$$

$$h(0) = -6$$

$$h(2) = 3$$

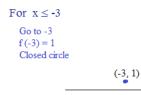
$$h(4) = (4)^2 + 2 = 18$$

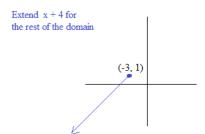


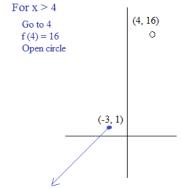
(although, it is a <u>continuous piecewise</u> <u>function</u>, because each domain piece has a continuous function)

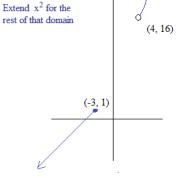
Example: Graph

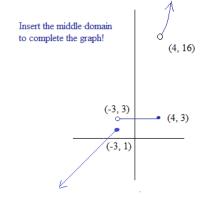
$$f(x) = \begin{cases} x + 4 & x \le -3 \\ 3 & -3 < x \le 4 \\ x^2 & x > 4 \end{cases}$$











Here are 2 approaches to graphing a piecewise function:

Method 1: "Endpoint and Extend"

Example:

$$f(x) = \begin{cases} 2x + 4 & \text{if } x < -3 \\ 1 & \text{if } -3 \le x < 4 \\ -x + 2 & \text{if } x \ge 4 \end{cases}$$

Start at x = -3:

$$f(-3) = 2(-3) + 4 = -2$$

since x < -3, it's an open circle

2x + 4 is a line with slope 2, so extend a line to the left...

Start at x = -3:

$$f(-3) = 1$$

since $x \ge -3$, it's a closed circle

"y = 1" is a horizontal line that

extends to x = 4 (open circle) Start at x = 4:

$$f(4) = -(4) + 2 = -2$$

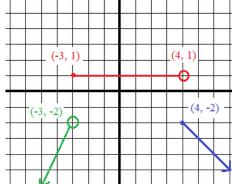
since $x \ge 4$, it's a closed circle

-x +2 is a line with slope -1, so extend a line to the right

This is more effective for linear pieces.



- 3) Extend



Method 2: "Graph and Cut"

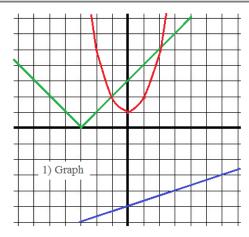
Example:

$$f(x) = \begin{cases} |x+3| & \text{if } x < -1 \\ x^2 + 1 & \text{if } -1 \le x < 2 \\ \frac{1}{3}x - 5 & \text{if } x \ge 2 \end{cases}$$

absolute value function |x + 3|

parabola
$$x^2 + 1$$

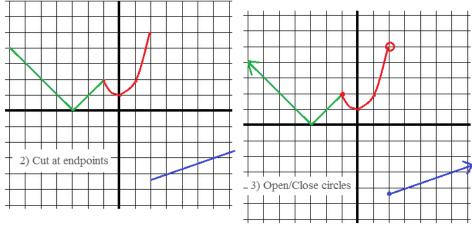
line
$$\frac{1}{3}x - 5$$



"Graph and Cut"

For each domain piece:

- 1) Graph the function
- 2) Cut at the endpoints of the domain
- 3) Open/Close circle



Example: Find the value(s) of x, such that f(x) = 2. Then, graph to confirm your answer.

$$f(x) = \begin{cases} 2x^2 - 6 & \text{if } x < 1 \\ 2 & \text{if } x = 1 \\ -8 + x & \text{if } x > 1 \end{cases}$$

obviously, f(1) = 2

then, for the 3rd equation: -8 + x...

$$f(10) = 2$$

and, for the 1st equation: $2x^2 - 6 = 2$

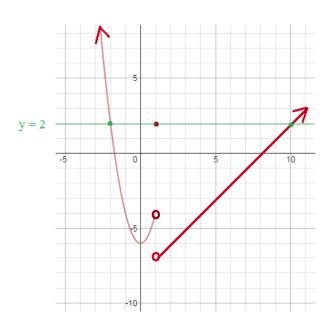
$$2x^2 = 8$$

$$2x^2 = 8$$

 $f(-2) = 2$ $x = -2 \text{ or } 2...$

Since this equation only applies if x < 1, we only consider -2

$$x = -2, 1, 10$$



Example: If g(x) is continuous, what are m and d? Graph this continuous piecewise function to verify.

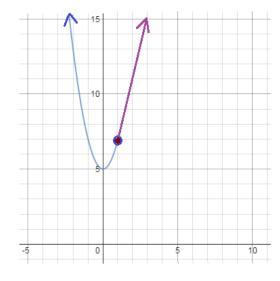
$$g(x) = \begin{cases} 2x^2 + 5 & \text{if } x < 1 \\ m & \text{if } x = 1 \\ 4x + d & \text{if } x > 1 \end{cases}$$

for x < 1, the equation $2x^2 + 5$ ends at (1, 7)

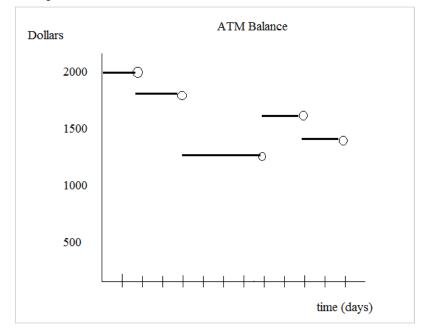
therefore, at x = 1, m must be 7

and, since m is 7, 4x + d = 7...d must be 3

(at x = 1, all 3 equations equal 7)



Example:



Models: Using Piecewise functions

What is the initial balance?

Initial balance occurs when t = 0...Therefore, initial balance is 2000 dollars

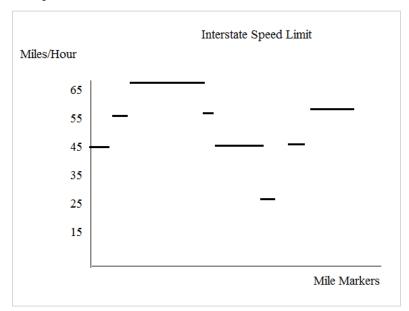
How many withdrawals were made?

If a withdrawal occurs, the amount will "gap lower"... This occurs 3 times...

How many deposits?

If a deposit occurs, the amount will "gap higher".. This occurs once..

Example:



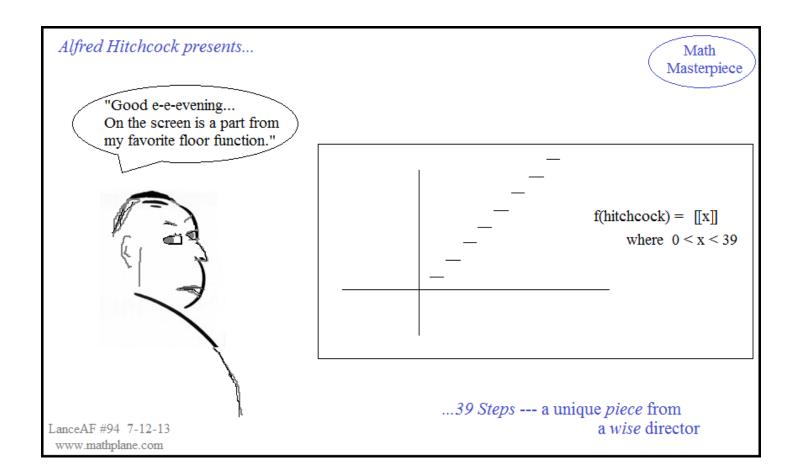
Explain a possible representation of the graph.

Each discontinuity represents a speed limit sign.

The 65 mph would occur on an interstate highway.

The drop to 25 mph would occur when the road passes through a town.

(Note: this is just a model. It's unlikely a car would <u>instantaneously</u> change speeds. Instead the graph would be continuous.)



Practice Exercises -→

Solving and Graphing f(x) Functions

Find the solutions AND graph each function.

1)
$$f(x) = 3x + 2$$

a)
$$f(2) =$$

b)
$$f(0) =$$





2)
$$f(x) = |x - 4| + 1$$

a)
$$f(5) =$$

c)
$$f(2) =$$





3)
$$f(x) = \begin{cases} x+3 & \text{if } x < 4 \\ x-3 & \text{if } x \ge 4 \end{cases}$$

a)
$$f(0) =$$

b)
$$f(7) =$$

c)
$$f(4) =$$

4)
$$f(x) = \begin{cases} 2x - 7 & \text{if } x < -7 \\ 3 & \text{if } -7 \le x < 5 \\ x^2 - 12 & \text{if } x \ge 5 \end{cases}$$

a)
$$f(-8) =$$

b)
$$f(0) =$$

c)
$$f(7) =$$





Piecewise Functions Quiz

I. Function notation - answer the following:

a)
$$f(x) = \begin{cases} x+2, & \text{if } x < 3 \\ x+7, & \text{if } x \ge 3 \end{cases}$$

$$f(5) =$$

c)
$$j(x) = \left\{ \begin{array}{l} -10 & , \ \ \text{if} \ \ x < 0 \\ 0 & , \ \ \text{if} \ \ x = 0 \\ 10 & , \ \ \text{if} \ \ x > 0 \end{array} \right.$$

$$j(-25) =$$

$$j(1/2) =$$

$$j(0) =$$

b)
$$g(x) = \begin{cases} 3x + 2, & \text{if } x < -6 \\ 5, & \text{if } -6 \le x < 10 \\ x^2, & \text{if } x \ge 10 \end{cases}$$

$$g(0) =$$

$$g(-6) =$$

$$g(10) =$$

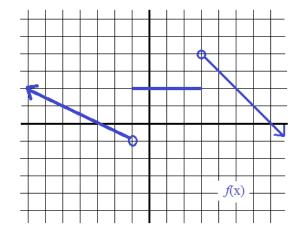
d)
$$h(t) = \begin{cases} \sqrt{(-t)} &, & \text{if } t < 0 \\ 5 &, & \text{if } 0 \le t < 5 \\ -2x &, & \text{if } 5 \le t \end{cases}$$

$$h(-4) =$$

$$h(5) =$$

$$h(10) =$$

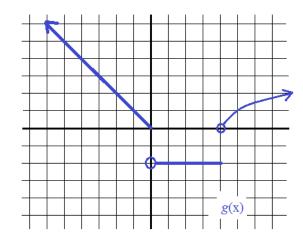
II. Using a graph -- answer the following



$$f(-5) =$$

$$f(1) =$$

$$f(7) =$$



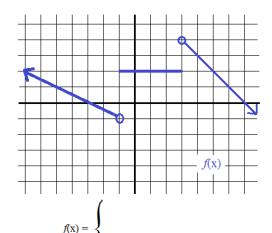
$$g(-3) =$$

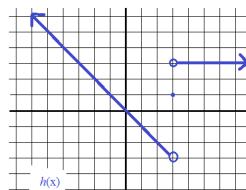
$$g(4) =$$

$$g(5) =$$

$$g(-20) =$$

III. Identifying the Piecewise function -- write an expression to describe the graph

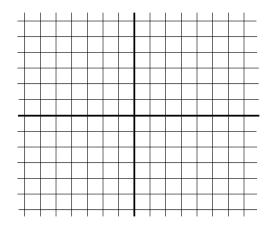


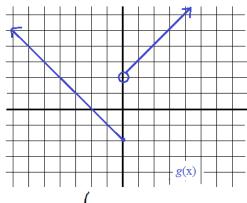


$$h(\mathbf{x}) = \begin{cases} \end{cases}$$

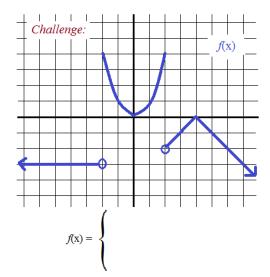
IV: Graphing Piecewise functions

$$f(x) = \begin{cases} 4, & \text{if } x < 3 \\ -x + 3, & \text{if } x \ge 3 \end{cases}$$

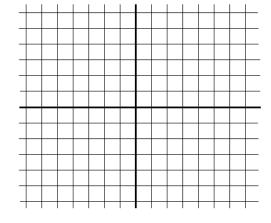




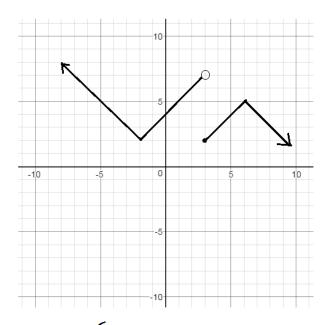




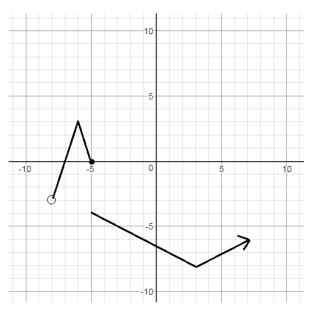
$$g(x) = \begin{cases} 2x & \text{, if } x < -3 \\ |x| & \text{, if } -3 \le x < 3 \\ 5 & \text{, if } x > 3 \end{cases}$$



1)



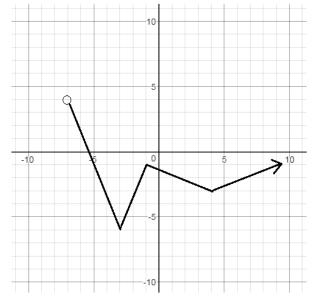
2)



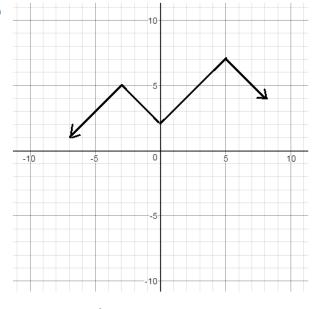
f(x) =

g(x) =

3)



4)



h(x) =

 $p(\mathbf{x}) =$

mathplane.com

1)
$$f(x) = \begin{cases} x+3 & \text{if } x < 2 \\ -1 & \text{if } 2 \le x < 6 \end{cases}$$

domain:

range:

2)
$$g(x) = \begin{cases} 3 - 4x & \text{if } x < 0 \\ 5 & \text{if } 3 \le x \le 7 \\ -x + 10 & \text{if } x \ge 12 \end{cases}$$

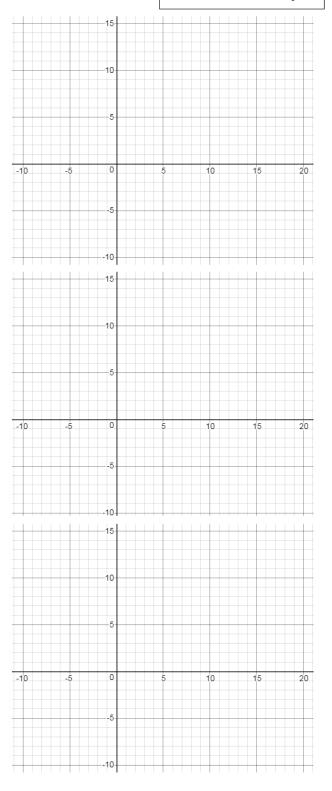
domain:

range:

3)
$$h(t) = \begin{cases} 2t + 2 & \text{if } 0 < t \le 4 \\ t + 6 & \text{if } 4 < t \le 8 \\ 14 & \text{if } t > 8 \end{cases}$$

domain:

range:



4)

$$f(x) = \begin{cases} & \text{if} \\ & \text{if} \end{cases}$$

domain:

range:

5)

$$g(x) = \begin{cases} & \text{if} \\ & \text{if} \end{cases}$$

domain:

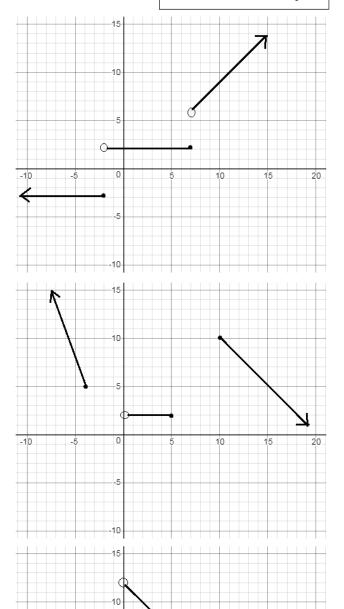
range:

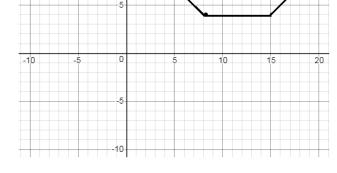
6)

$$h(\mathbf{x}) = \begin{cases} & \text{if} \\ & \text{if} \end{cases}$$

domain:

range:





Graph the following piecewise functions. Then, identify the domain and range.

$$f(x) = \begin{cases} x + 15 & \text{if } x \le -5 \\ -|x| + 2 & \text{if } -5 < x < 5 \\ \sqrt{x + 5} + 3 & \text{if } x \ge 5 \end{cases}$$

domain:

range:

8)
$$g(x) = \begin{cases} \sqrt{-6-x} + 8 & \text{if } x < -6 \\ (x+3)^2 + 1 & \text{if } -6 \le x \le 1 \\ \frac{1}{2}x + 7 & \text{if } x > 4 \end{cases}$$

domain:

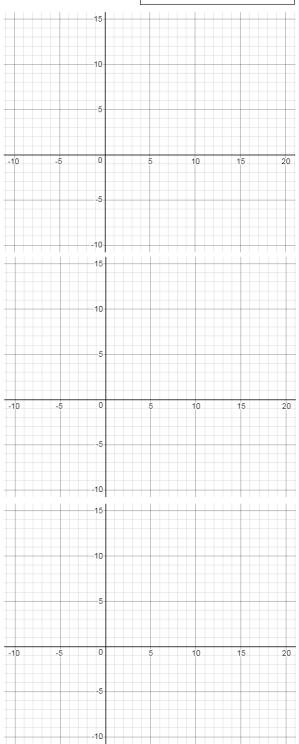
range:

9)
$$h(x) = \begin{cases} x & \text{if } x < 1 \\ \frac{1}{2}(2^{x}) & \text{if } 1 \le x < 4 \\ 2|x - 10| - 4 & \text{if } x \ge 4 \end{cases}$$

domain:

range:





VI. Piecewise Models (Word Problems) and Concepts

A discount book store charges \$4 per book..
 If a customer buys more than 5, the price drops to \$3.50 per book...

Write a piecewise function to model the cost of books.. How much would 20 books cost?

2) A store sells t-shirts...

It charges \$10 per shirt for the first batch of 50... Since the store has the screen design, the next batch of 50 would cost \$9 per shirt... And, all batches after that would cost \$8 per shirt....

Write a piecewise function describing the cost of shirts... How much would 120 shirts cost?

3) A shop down the street sells hats...

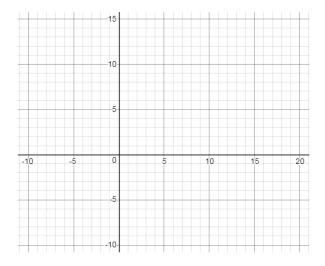
It charges \$10 per hat. If a customer purchases more than 30 hats, the owner offers a \$1 discount per hat. (\$9 per hat) If a customer buys more than 50 hats, the owner offers another \$1 discount (\$8 per hat).

Write a piecewise function to describe the cost of hats. The math club has a budget of \$300. How many hats could it buy?

4) Write and graph a piecewise function with the following characteristics.

Domain: all real numbers

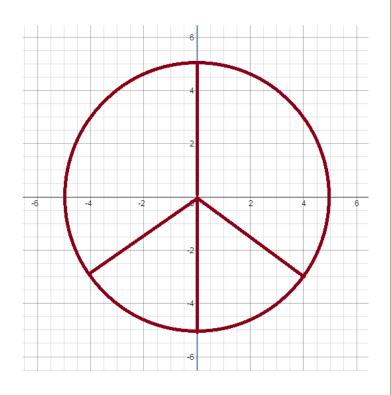
$$f(3) = 2$$
 and $f(-3) = 5$



Peace-wise Function

$$g(x) = \begin{cases} \frac{3}{4}x & \text{if } -4 \le x \le 0 \\ \frac{+}{4}\sqrt{25 - x^2} & \text{if } -5 \le x \le 5 \\ -\frac{3}{4}x & \text{if } 0 \le x \le 4 \\ \text{all real numbers} & \text{betweeen -5 and 5} & \text{if } x = 0 \end{cases}$$





LanceAF #223 (1-12-16) mathplane.com



This is a tremendous function... (even if it fails the vertical line test!)

SOLUTIONS -→

Find the solutions AND graph each function.

1)
$$f(x) = 3x + 2$$

a)
$$f(2) = 3(2) + 2 = 8$$

b)
$$f(0) = 3(0) + 2 = 2$$

c)
$$f(-6) = 3(-6) + 2 = -16$$

2)
$$f(x) = |x - 4| + 1$$

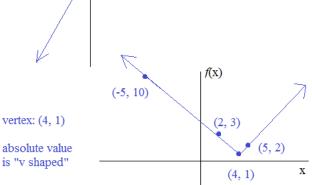
a)
$$f(5) = |(5) - 4| + 1 = 2$$

b)
$$f(-5) = |(-5) - 4| + 1 = 10$$

c)
$$f(2) = |(2) - 4| + 1 = 3$$



(-2/3, 0)



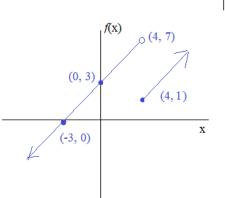
(0, 2)

3)
$$f(x) = \begin{cases} x+3 & \text{if } x < 4 \\ x-3 & \text{if } x \ge 4 \end{cases}$$

a)
$$f(0) = (0) + 3 = 3$$
 (1st piece)

b)
$$f(7) = (7) - 3 = 4$$
 (2nd piece)

c)
$$f(4) = (4) - 3 = 1$$
 (2nd piece)

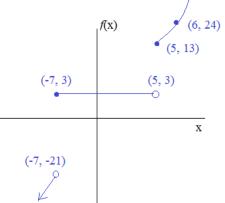


4)
$$f(x) = \begin{cases} 2x - 7 & \text{if } x < -7 \\ 3 & \text{if } -7 \le x < 5 \\ x^2 - 12 & \text{if } x > 5 \end{cases}$$

a)
$$f(-8) = 2(-8) - 7 = -23$$

b)
$$f(0) = 3$$

c)
$$f(7) = 49 - 12 = 37$$



I. Function notation - answer the following:

a)
$$f(x) = \begin{cases} x+2, & \text{if } x < 3 \\ x+7, & \text{if } x \ge 3 \end{cases}$$

$$f(-5) = (-5) + 2 = -3$$

$$f(3) = (3) + 7 = 10$$

$$f(5) = (5) + 7 = 12$$

c)
$$j(x) = \left\{ \begin{array}{l} -10 \ , \ \ \text{if} \ \ x < 0 \\ 0 \ , \ \ \text{if} \ \ x = 0 \\ 10 \ , \ \ \text{if} \ \ x > 0 \end{array} \right.$$

$$j(-25) = -10$$

$$j(1/2) = 10$$

$$j(0) = 0$$

SOLUTIONS

b)
$$g(x) = \begin{cases} 3x + 2, & \text{if } x < -6 \\ 5, & \text{if } -6 \le x < 10 \\ x^2, & \text{if } x \ge 10 \end{cases}$$

g(0) = since 0 is between -6 and 10, the output is 5

 $g(-6) = \text{ since -6 is } \ge -6$, the output is 5

$$g(10) = (10)^2 = 100$$

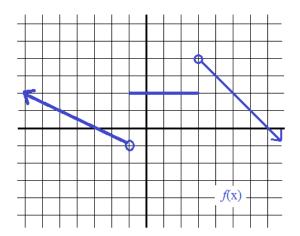
d)
$$h(t) = \begin{cases} \sqrt{(-t)} & , & \text{if } t < 0 \\ 5 & , & \text{if } 0 \le t < 5 \\ -2x & , & \text{if } 5 \le t \end{cases}$$

$$h(-4) = \sqrt{(-(-4))} = 2$$

$$h(5) = -2(5) = -10$$

$$h(10) = -2(10) = -20$$

II. Using a graph -- answer the following

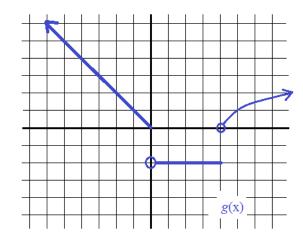


$$f(-5) = 1$$

$$f(-1) = 2$$

$$f(1) = 2$$

$$f(7) = 0$$



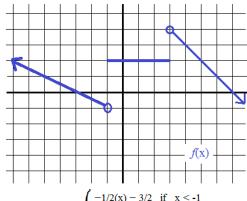
$$g(-3) = 3$$

$$g(4) = -2$$

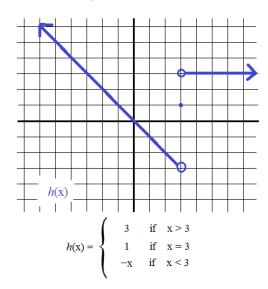
$$g(5) = 1$$

$$g(x) = -x$$
 if $x \le 0$

$$g(-20) = 20$$

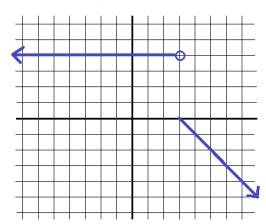


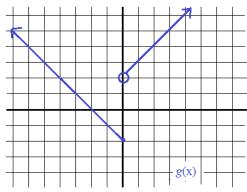
$$f(x) = \begin{cases} -1/2(x) - 3/2 & \text{if } x < -1\\ 2 & \text{if } -1 \le x \le 3\\ -x + 7 & \text{if } x > 3 \end{cases}$$



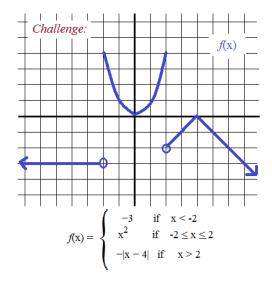
IV: Graphing Piecewise functions

$$f(x) = \begin{cases} 4, & \text{if } x < 3 \\ -x + 3, & \text{if } x \ge 3 \end{cases}$$

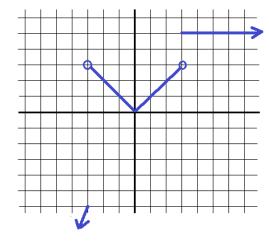




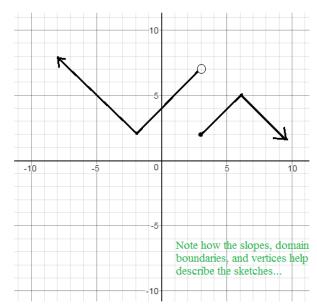
$$g(x) = \begin{cases} x+2 & \text{if } x > 0 \\ -x-2 & \text{if } x \le 0 \end{cases}$$



$$g(x) = \begin{cases} 2x & \text{, if } x < -3 \\ |x| & \text{, if } -3 \le x < 3 \\ 5 & \text{, if } x \ge 3 \end{cases}$$

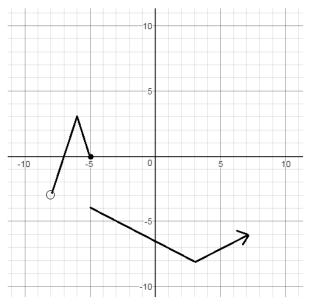


1)



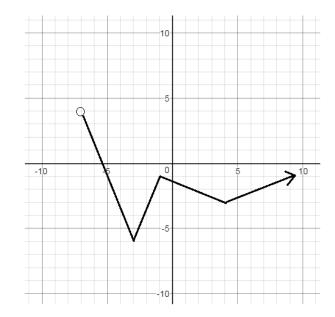
$$f(x) = \begin{cases} |x+2|+2 & \text{if } x < 3 \\ -|x-1| & \text{if } x < 3 \end{cases}$$

2)



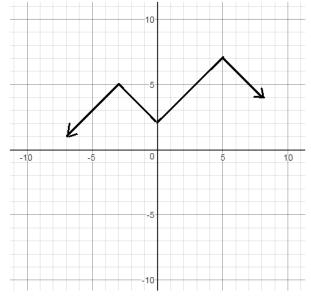
$$g(\mathbf{x}) = \begin{cases} -3|\mathbf{x} + 6| + 3 & \text{in the interval} \quad (-8, -5] \\ \frac{1}{2}|\mathbf{x} - 3| - 8 & \text{in the interval} \quad [-5, \infty) \end{cases}$$

3)



$$h(x) = \begin{cases} \frac{5}{2}|x+3| - 6 & \text{if } -7 < x \le -1 \\ \frac{2}{5}|x-4| - 3 & \text{if } x \ge -1 \end{cases}$$

4)



$$p(\mathbf{x}) = \begin{cases} -|\mathbf{x} + 3| + 5 & \text{in the interval} \quad (-\infty, 0) \\ -|\mathbf{x} - 5| + 7 & \text{in the interval} \quad (0, \infty) \end{cases}$$

SOLUTIONS

Piecewise Functions: Linear pieces

1) Since the 3 "pieces" will be lines segments or rays, we can use an 'endpoint method' to graph.

$$f(x) = \begin{cases} x+3 & \text{if } x < 2 \\ -1 & \text{if } 2 \le x < 6 \end{cases}$$

$$-x+10 & \text{of } x \ge 6 \end{cases}$$
The endpoint (boundary) of the first piece occurs at $(2, 5)$. Since it is $x < 2$ it's an open circle

All x values (i.e. places on the graph "left to right")

All f(x) values (i.e. places on the graph "bottom to top")

 $(-\infty,5)$

domain: all real numbers

$$x < 0$$

$$3 \le x \le 7$$

$$x > 12$$

domain: it's described in the list of "if" statements!!

$$x \le 0$$
 or $3 \le x \le 7$ or $x \ge 12$

(−∞ , -2] U (3, ∞)

range:
$$g(x) \le -2$$
 or $g(x) > 3$

Since the 3 "pieces" will be lines segments or rays,

Since it is x < 2, it's an open circle.

Then, pick a point left of 2 --such as (0, 3)...

Put that point on the graph and extend a ray from (2, 5) through (0, 3)

The endpoints of the second piece are (2, -1) and (6, -1). Since inputs are $2 \le x \le 6$, the left endpoint is closed and the right endpoint is open...

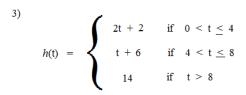
Finally, the boundary of the 3rd piece occurs at (6, 4)... Then, we can draw a ray through (9, 1)...

The 1st piece, we can use the boundary x = 0 (0, 3) open circle and, pick a point less than 0.. (-3, 15) and extend the ray...

The 2nd piece, we can use the endpoints (3, 5) and (7, 5)

The 3rd piece, we can use the

endpoint x = 12 (12, -2) closed and, pick a point greater than 12... (15, -5) and extend the ray..



domain: t > 0

range: $2 < h(t) \le 14$

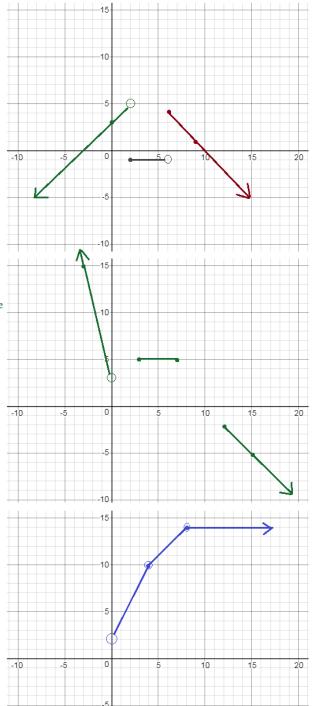
(2, 14]

Again, we have 3 straight pieces...

Endpoints of the 1st piece: (0, 2) open circle (4, 10) closed circle

Endpoints of 2nd piece: (4, 10) open circle (8, 14) closed circle

Endpoint of 3rd piece: (8, 14) open circle.. then, horizontal ray extending to the right...



SOLUTIONS

Piecewise Functions: Linear pieces

 $f(x) = \begin{cases}
-3 & \text{if } x \le -2 \\
2 & \text{if } -2 < x \le 7 \\
x - 1 & \text{if } x > 7
\end{cases}$ Looking at the domain ('movement from left to right') & the endpoints of each piece we can determine the "if" statements...

< for open circles

domain: all real numbers

 $(-\infty, \infty)$

[-3]U[2]U(6, ∞)

range: $\{-3, 2, \text{ and all reals} > 6\}$

Looking at the domain

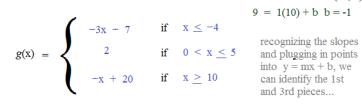
< for closed circles

1st piece is a horizontal line " y = -3 " where every output is -3

2nd piece is a horizontal line "y = 2" where every output is 2

3rd piece is ray where the slope is 1.. "y = 1x + b"To find b, plug in another point... We'll use (10, 9)..

$$9 = 1(10) + b b = -1$$

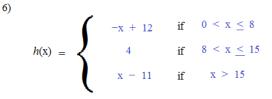


domain: (the "if" statements)
$$x \le -4$$
 or $0 < x \le 5$

or
$$x > 10$$

range: since left piece extends indefinitely upward, and right piece extends indefinitely downward, AND they overlap, the range is all real numbers

$$(-\infty, \infty)$$



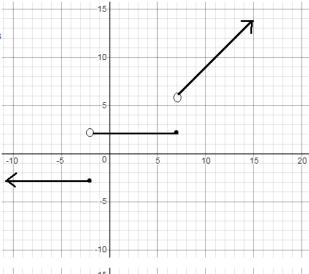
NOTE: since this is a function, there is no overlap in the "if" statements!!

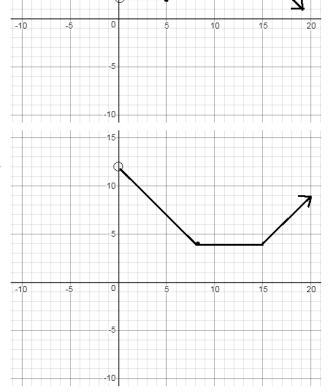
domain: x > 0 $(0, \infty)$

 $h(x) \ge 4$ range:

> (the minimum value is 4, and it extends indefinitely upward)

5)





SOLUTIONS

Piecewise Functions: mixed pieces

 $f(x) = \begin{cases} x + 15 & \text{if } x \le -5 \\ -|x| + 2 & \text{if } -5 < x < 5 \end{cases}$ endpoint method... Right boundary is (-5, 10).. And, point (-8, 7) is a point to the left. $\sqrt{x - 5} + 3 & \text{if } x \ge 5 \end{cases}$ Piece 2 is an absolute value function

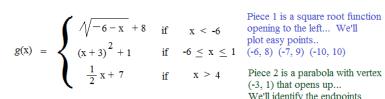
Since piece 1 is linear, we'll use endpoint method...

opening downward. The vertex is (0, 2).. And, the endpoints occur at (-5, -3) and (5, -3)... since < and <. we use open circles

Piece 3 is a square root function that starts at (5, 3) and opens to the right... We'll plot a few points..

domain: all real numbers (−∞ , ∞)

range: Since the 1st piece extends to negative infinity and the 3rd piece extends to positive infinity, the range is all real numbers...



(-3, 1) that opens up...

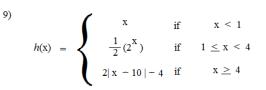
We'll identify the endpoints (-6, 10) and (1, 17)...

domain: domain is the "if statements"... $x \le 1$ or $x \ge 4$ (-∞, 1] U (4, ∞)

Piece 3 is a ray that starts at (4, 9) and extends to the right So, we can draw the ray through -10 (14, 14)

range: The minimum point is the parabola's range is $g(x) \ge 1$

[1, ∞)



domain: all real numbers

(─∞, ∞)

all real numbers

(−∞ , ∞)

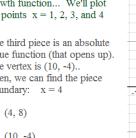
The first piece is the line y = xthat stops at x = 1

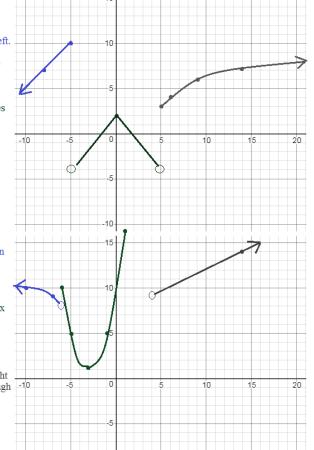
The second piece is a exponential growth function... We'll plot the points x = 1, 2, 3, and 4

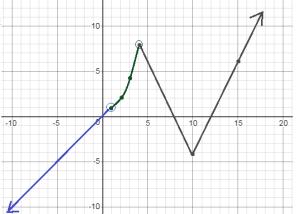
The third piece is an absolute value function (that opens up). The vertex is (10, -4).. Then, we can find the piece boundary: x = 4

(10, -4)

(15, 6)



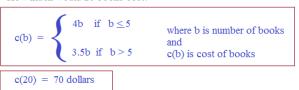




VI. Piecewise Models (Word Problems) and Concepts

A discount book store charges \$4 per book..
 If a customer buys more than 5, the price drops to \$3.50 per book...

Write a piecewise function to model the cost of books.. How much would 20 books cost?



2) A store sells t-shirts...

It charges \$10 per shirt for the first batch of 50... Since the store has the screen design, the next batch of 50 would cost \$9 per shirt... And, all batches after that would cost \$8 per shirt....

Write a piecewise function describing the cost of shirts... How much would 120 shirts cost?

$$f(x) = \begin{cases} 10x & \text{if } x \le 50 \\ 9x + 50 & \text{if } 50 < x \le 100 \\ 8x + 100 + 50 & \text{if } x > 100 \end{cases}$$

$$f(120) = 1110$$

3) A shop down the street sells hats...

It charges \$10 per hat.

If a customer purchases more than 30 hats, the owner offers a \$1 discount per hat. (\$9 per hat)

If a customer buys more than 50 hats, the owner offers another \$1 discount (\$8 per hat).

Write a piecewise function to describe the cost of hats. The math club has a budget of \$300. How many hats could it buy?

4) Write and graph a piecewise function with the following characteristics.

Domain: all real numbers

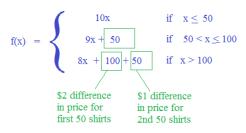
Range: { -4, 2, 5 }

$$f(3) = 2$$
 and $f(-3) = 5$

$$f(x) = \begin{cases} 5 & \text{if } x \le 0 \\ 2 & \text{if } 0 < x \le 6 \\ -4 & \text{if } x \ge 6 \end{cases}$$

SOLUTIONS

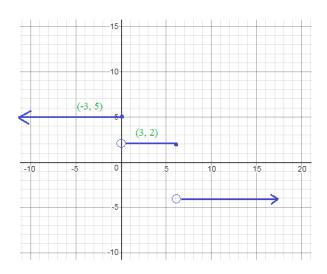
this represents the 1st 50 shirts which were not discounted



$$c(h) = \begin{cases} 10h & \text{if } h \le 30 \\ 9h & \text{if } 30 < x \le 50 \\ 8h & \text{if } x \ge 50 \end{cases}$$

If the math club buys 30 hats, it would cost 30 x \$10... HOWEVER, if it bought a few more hats, the cost drops to \$9!!

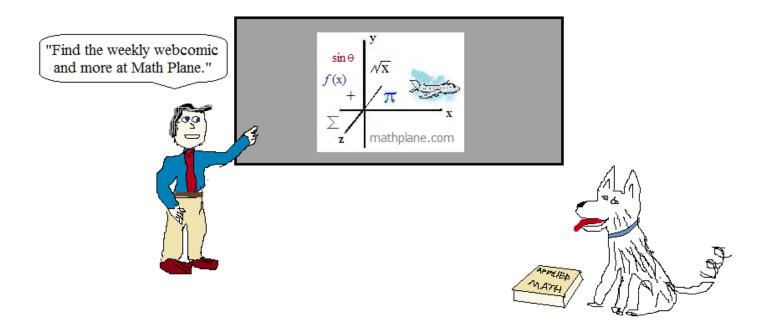
33 hats would cost \$297... (34 hats would cost \$306)



Thanks for visiting. (Hope it helped!)

If you have questions, suggestions, or requests, let us know.

Cheers



Find us at Mathplane.com

Also, Facebook, Google+, Pinterest, TES, and TeachersPayTeachers
Plus, Mathplane *Express* for mobile at mathplane.ORG

One more question:

If
$$c(x) = 3x^3 + 5x^2 + 4$$
,
what is $4c(2b)$?

If
$$c(x) = 3x^3 + 5x^2 + 4$$
,

SOLUTION

what is 4c(2b)?

reminder:
$$c(1) = 3(1)^3 + 5(1)^2 + 4 = 12$$

FIRST,
$$c(2b) = 3(2b)^3 + 5(2b)^2 + 4$$

= $3(8b^3) + 5(4b^2) + 4$
= $24b^3 + 20b^2 + 4$

THEN,
$$4 \cdot c(2b) = 4 \cdot (24b^3 + 20b^2 + 4)$$

$$= 96b^3 + 80b^2 + 16$$