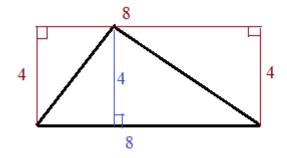
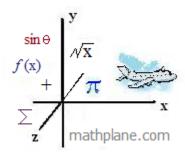
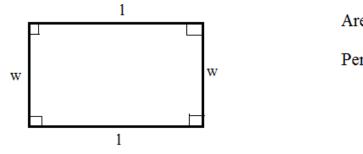
Area and Perimeter of Polygons 1



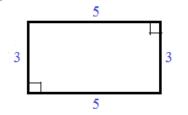
Includes formulas, examples, and practice questions (w/answers)



Area and Perimeter of a Rectangle



Example:



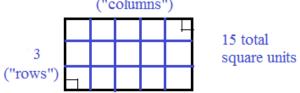
Area = 1w

Perimeter = 21 + 2w

l = lengthw = width

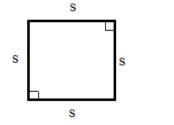
Area = 1w = (5)(3) = 15 square units Perimeter = 21 + 2w = 2(5) + 2(3) = 16 units

Observations: the perimeter is simply adding up every side -- 3 + 5 + 3 + 5the area is the number of 1 unit boxes -- 5("columns")



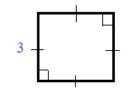
Area and Perimeter of a Square

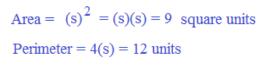
A square is a special type of rectangle. So, using substitution:



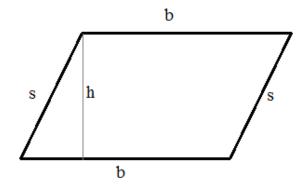
Area = s^2 Perimeter = 4s s = side (length)

Example:





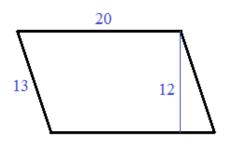
Area and Perimeter of a Parallelogram



Area = bh Perimeter = s + b + s + b = 2(b + s)s = side

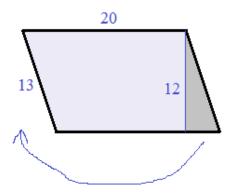
b = baseh = height

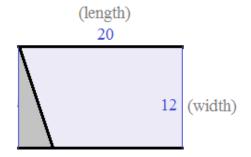




Area = bh = 20(12) = 240 square units Perimeter = 2(b + s) = 66 units

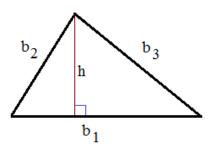
Observation: To verify the area of a parallelogram, transform the figure into a rectangle!





Area of rectangle is 1w = 20(12) = 240 square units

Area and Perimeter of a Triangle



Area = $\frac{1}{2}$ bh Perimeter = $b_1 + b_2 + b_3$ b = baseh = height

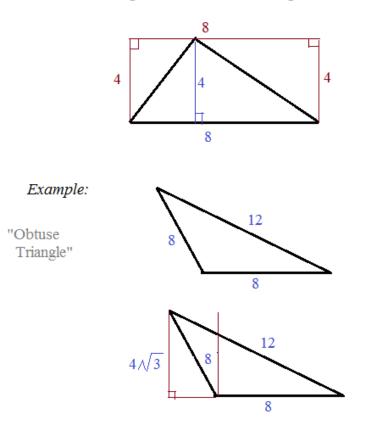
Example:

5 4 7 4 8

Area = $\frac{1}{2}$ bh = $\frac{1}{2}$ (8)(4) = 16 square units

Perimeter = sum of the sides = 8 + 5 + 7 = 20 units

Observation: A triangle is one-half of a rectangle, so the triangle's area is one-half!



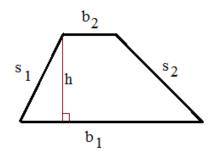
Area of rectangle = bh (i.e. length x width) = 32

Area of triangle = 16

The base is 8....

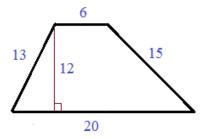
.... And, the height is $4\sqrt{3}$

Perimeter = 8 + 8 + 12 = 28 units Area = $\frac{1}{2}$ bh = $\frac{1}{2}$ (8)($4\sqrt{3}$) = $16\sqrt{3}$ sq. units



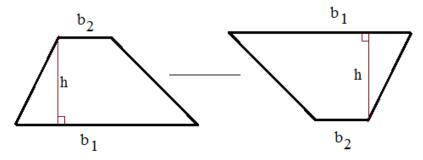
Area = $\frac{1}{2}$ (b₁ + b₂) h Perimeter = b₁ + b₂ + s₁ + s₂ b = base s = side h = height

Example:

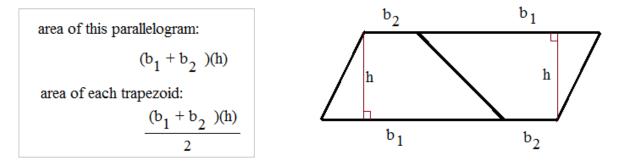


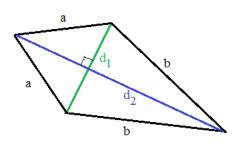
Perimeter = 20 + 13 + 6 + 15 = 54 units Area = $\frac{1}{2}$ (b₁ + b₂)h = $\frac{1}{2}$ (20 + 6)(12) = 156 square units

Observation: a trapezoid is one-half of a parallelogram



When we double the trapezoid, we get a parallelogram.



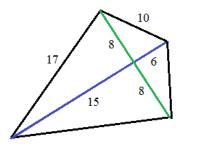


Area =
$$\frac{1}{2}$$
 d₁ d₂

Perimeter = 2a + 2b

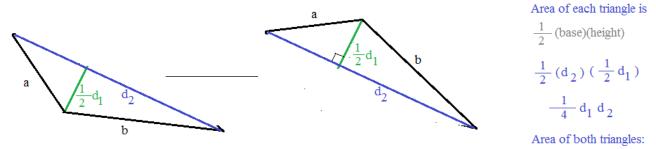


Example:



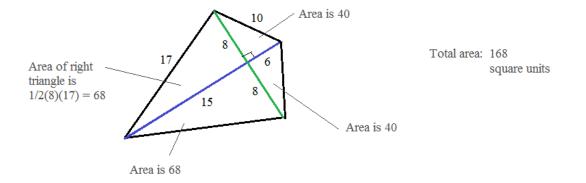
Area = $\frac{1}{2} d_1 d_2 = \frac{1}{2} (16)(21) = 168$ square units Perimeter = 2a + 2b = 2(10) + 2(17) = 54 units

Observation: A kite is 2 congruent triangles.

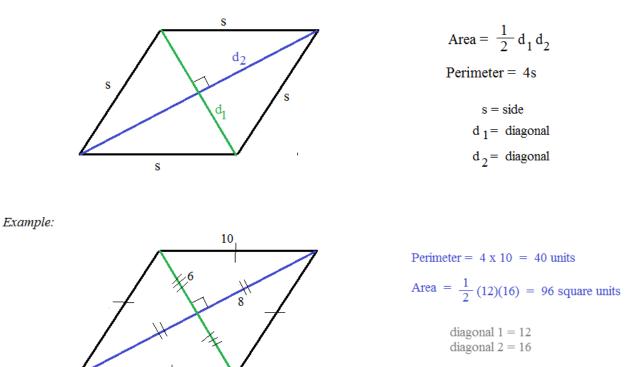


 $\frac{1}{2}$ d₁d₂

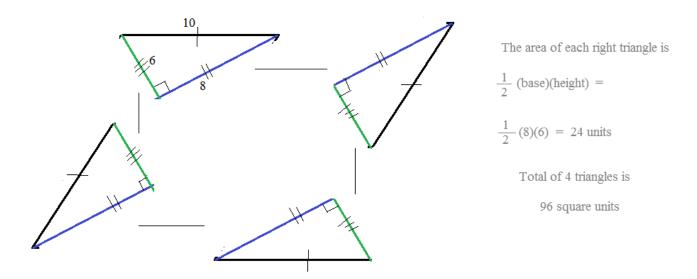
Observation: Since one diagonal is a perpendicular bisector, the kite consists of 4 right triangles.

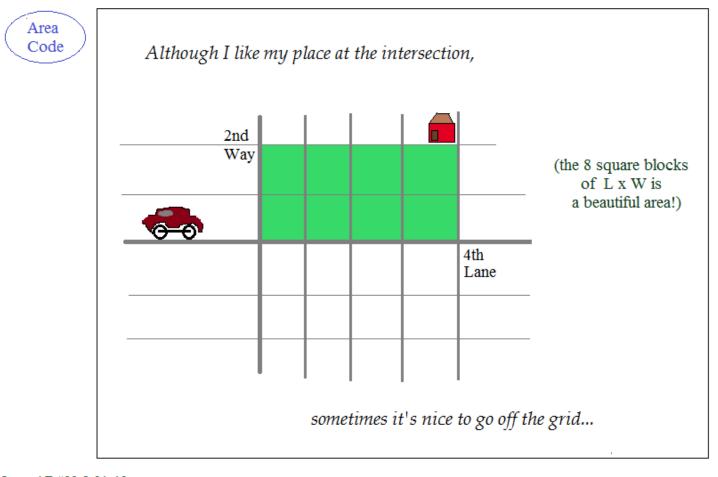


Area and Perimeter of a Rhombus



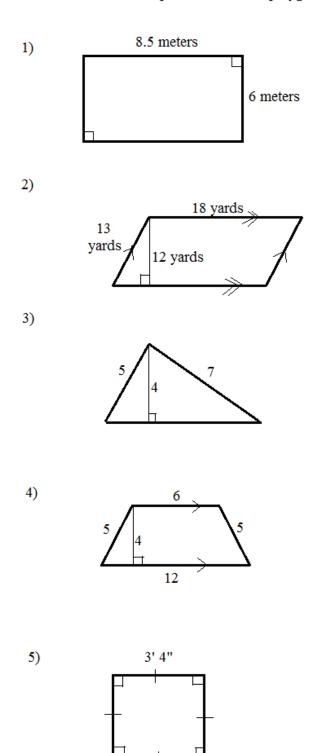
Observation: Since diagonals of a rhombus are perpendicular bisectors, there are 4 congruent right triangles.





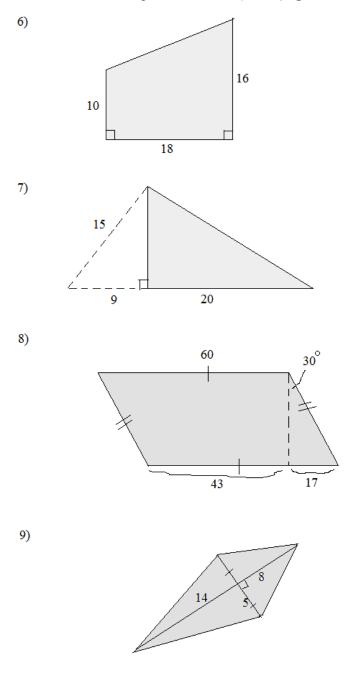
LanceAF #88 5-31-13 www.mathplane.com

Practice Quiz (w/solutions)

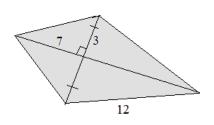


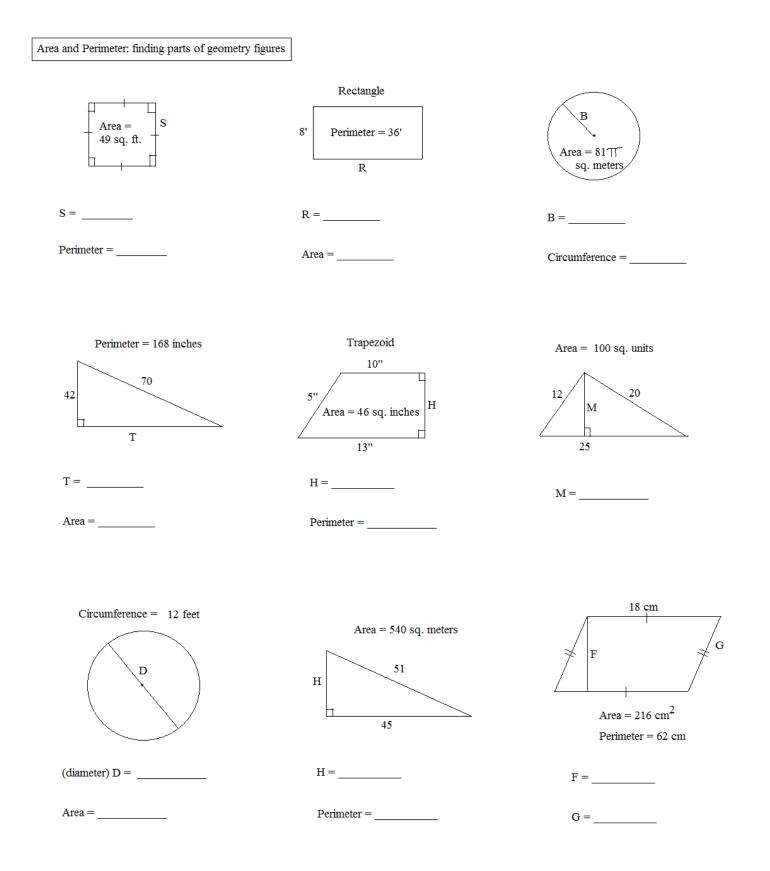
Determine the area and perimeter of each (shaded) figure:

Area and Perimeter of Polygons Quiz



10)

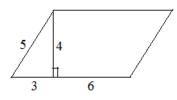




Answer the following questions:

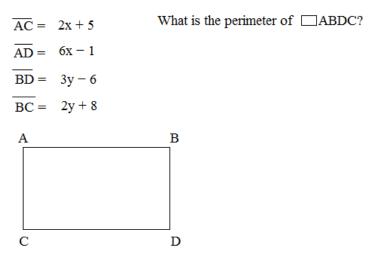
Area and Perimeter of Polygons Quiz

1) What is the area of the parallelogram? The perimeter?



- 2) If the area of a square is 144 square feet, what is the perimeter?
- 3) The length of a rectangle is twice its width. If the perimeter is 66cm, what is the area?
- 4) What is the area of a 5-12-13 special right triangle?

**Challenge: Given: Rectangle ABCD



www.mathplane.com

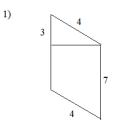
Can you answer the following?

A) The diagonals of a rhombus are 6 and 8. What is the height?

Area and Perimeter of Polygons Quiz

B) A trapezoid with perimeter 44 has non-parallel sides of length 8 and 10. If the height is 5, what is the area of the trapezoid? What is the length of each base?

C) What is the area and perimeter of each parallelogram?

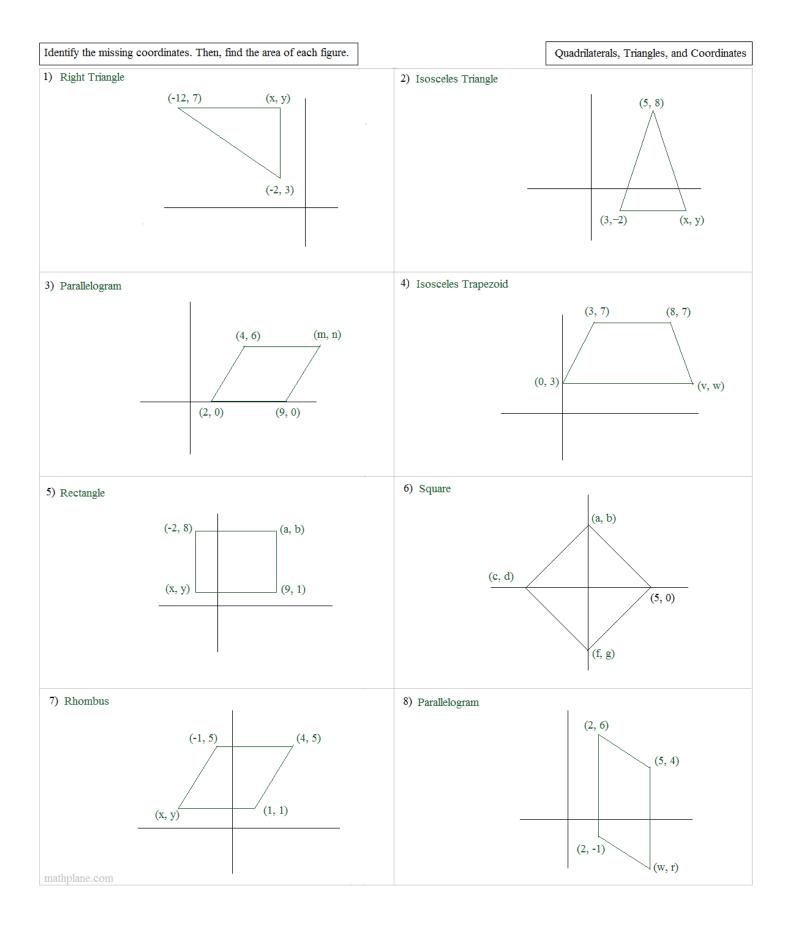




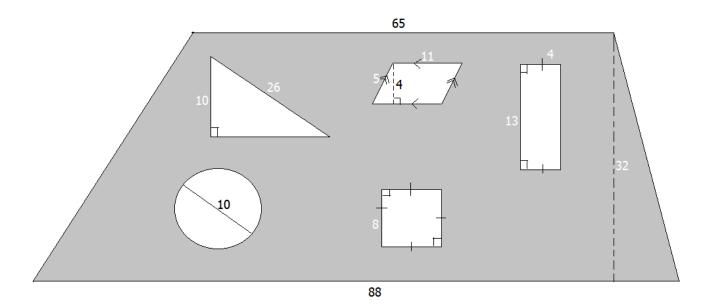
12

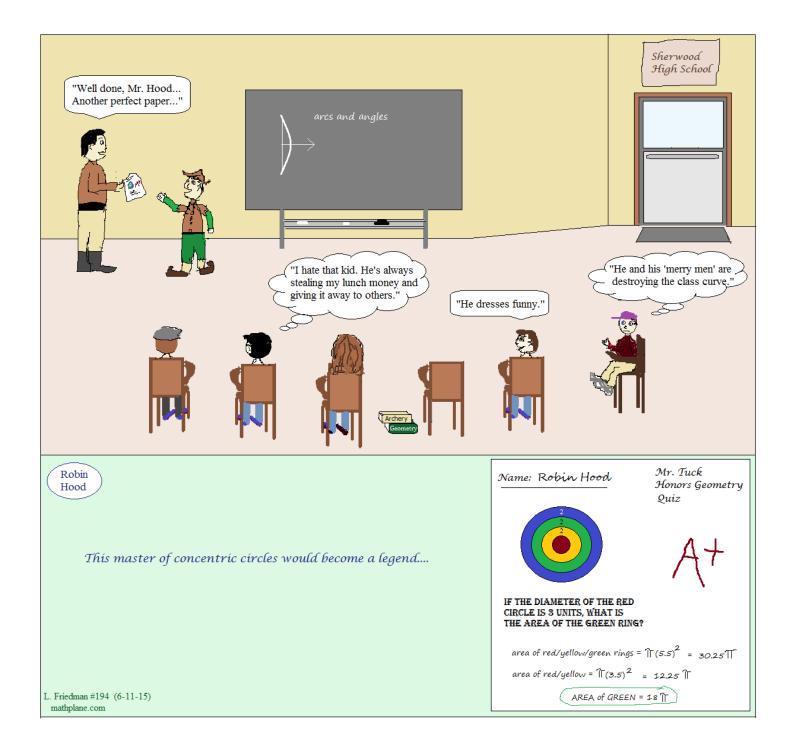
13

D) Find the area of a trapezoid with sides 12, 17, 40, and 25 where 12 and 40 are the bases.

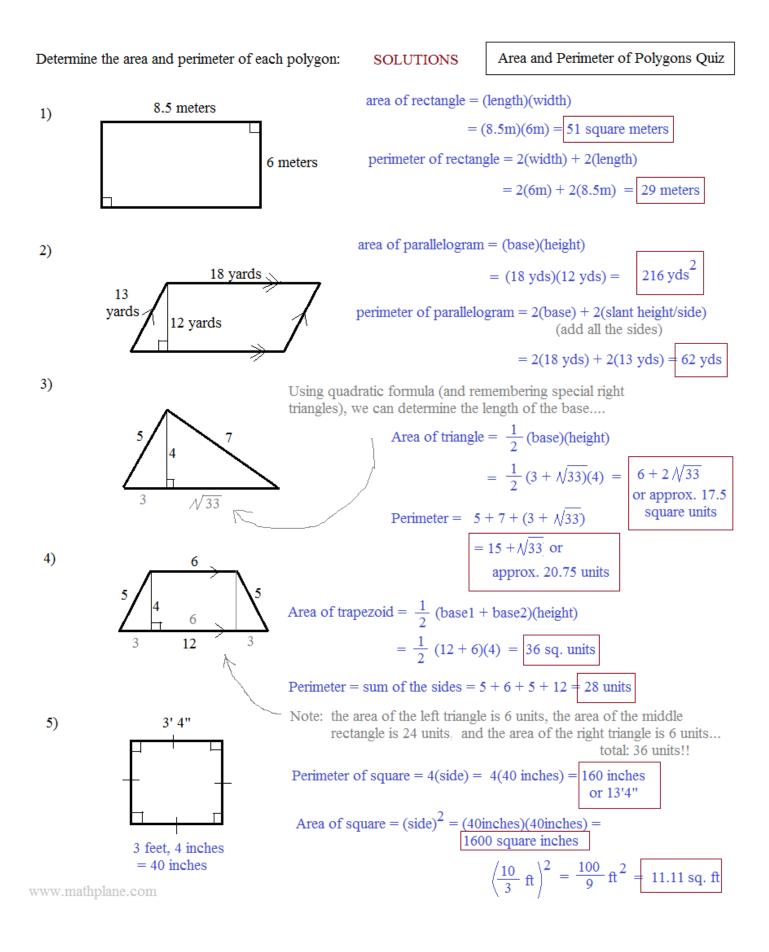


What is the shaded area?





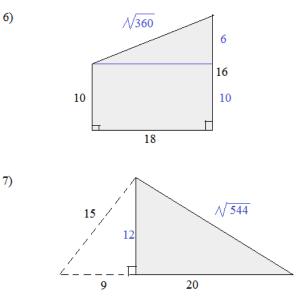
SOLUTIONS-→



Determine the area and perimeter of each (shaded) figure:

SOLUTIONS

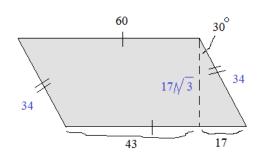
Area and Perimeter of Polygons Quiz



Area of upper triangle:Perimeter is sum of all the sides.. $\frac{1}{2}$ (6)(18) = 5410 + 18 + 16 + ?Area of lower rectangle:10 + 18 + 16 + ?(10)(18) = 180 $18^2 + 6^2 = c^2$ total area: 234 sq. units $c = \sqrt{360} = 6 \sqrt{10}$ Using the small right triangle, we find the height is 12Using Pythagorean Theorem

find the height is 12 (9-12-15 Pythagorean Triple) then, A = 1/2 (base)(height) A = 1/2 (20)(12) = 120 perimeter = $44 + 6\sqrt{10}$ Using Pythagorean Theorem: $12^2 + 20^2 = c^2$ $c = \sqrt{544} = 4\sqrt{34}$ Perimeter = $32 + 4\sqrt{34}$

8)



Recognizing the 30-60-90 right triangle, we can find the length of the parallelogram's, small sides.

 $2 \ge 17 = 34$ perimeter = 2(34) + 2(60) = 188 Then, we know the height of the parallelogram is $17 \sqrt{3}$ (30-60-90 right triangle)

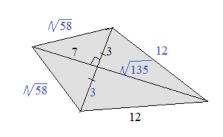
area = base x height
=
$$60 \times 17 \sqrt{3} = 1020 \sqrt{3}$$

9) Label all the sides $\sqrt{89}$ (utilizing pythagorean theorem and properties of a kite) 14 5 $\sqrt{89}$ $\sqrt{89}$ $\sqrt{89}$ $\sqrt{89}$ $\sqrt{89}$

Also, area of kite is sum of 4 right triangles' areas:

$$35 + 35 + 20 + 20 = 110$$
 sq. units

10)

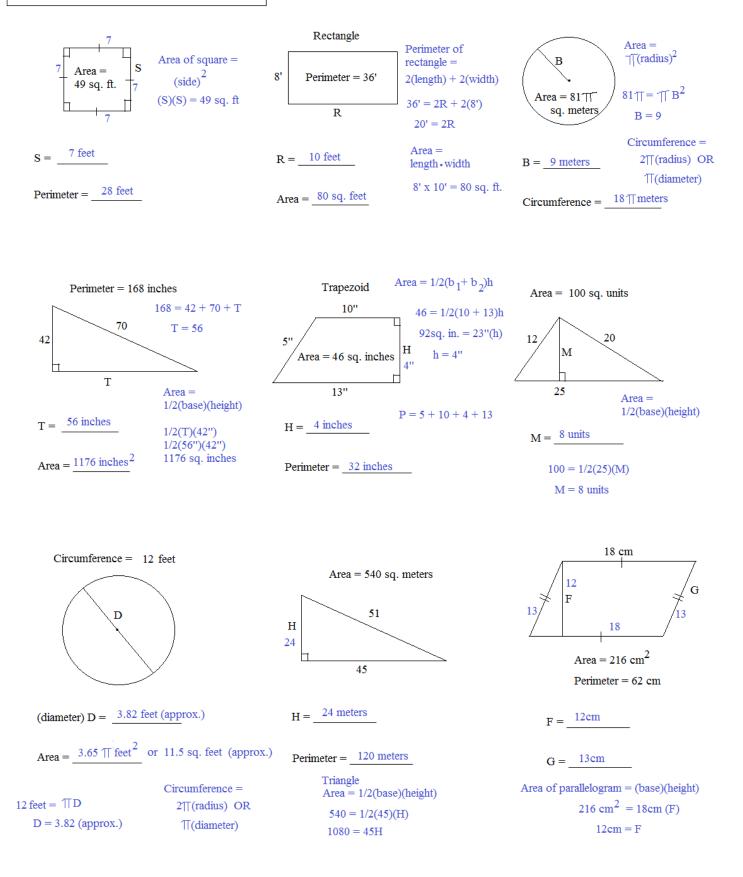


Perimeter =
$$24 + 2 \sqrt{58}$$

Area = $\frac{21}{2} + \frac{21}{2} + \frac{3}{2} \sqrt{135} + \frac{3}{2} \sqrt{135}$
= $21 + 9 \sqrt{15}$
or, $\frac{1}{2}$ (6)(7 + $\sqrt{135}$) = $21 + 3 \sqrt{135}$

Area and Perimeter: finding parts of geometry figures

SOLUTIONS

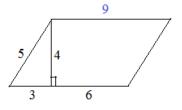


Answer the following questions:

SOLUTIONS

Area and Perimeter of Polygons Quiz

1) What is the area of the parallelogram? The perimeter?



Area = (base)(height) = (9)(4) =
$$36 \text{ sq. units}$$

Perimeter = sum of the sides = $5 + 9 + 5 + 9 = 28$ units

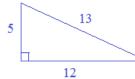
2) If the area of a square is 144 square feet, what is the perimeter?

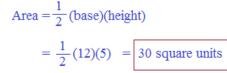
Area = (side)(side)			If each side = 12 , then the perimeter	12	area = 144
$144 = (\text{side})^2$	square root both sides	12 = side	is $4 \ge 12 = 48$ units	144	

3) The length of a rectangle is twice its width. If the perimeter is 66cm, what is the area?

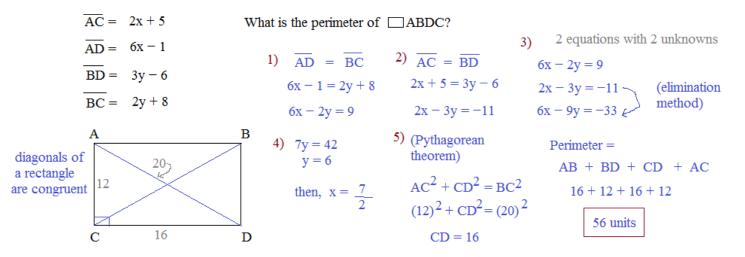


4) What is the area of a 5-12-13 special right triangle?





**Challenge: Given: Rectangle ABCD



Can you answer the following?

SOLUTIONS

 $8 + 10 + 2x + \sqrt{39} + 5\sqrt{3} = 44$

2x + 6.24 + 8.66 = 26

2x = 11.1

x = 5.55

Bases: 5.55 20.45 height = 4.8

Area of Trapezoid =

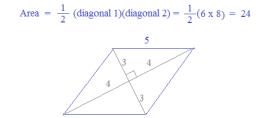
(26)(5)

 $\frac{1}{2}$ (base 1 + base 2)(height)

65 sq units

A) The diagonals of a rhombus are 6 and 8. What is the height?

Step 1: Use the formula for a rhombus to find the area...



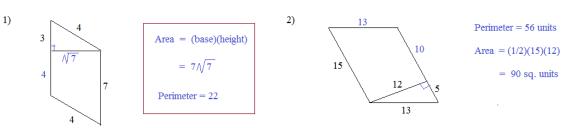
Diagonals are perpendicular bisectors...

B) A trapezoid with perimeter 44 has non-parallel sides of length 8 and 10. If the height is 5, what is the area of the trapezoid? What is the length of each base?

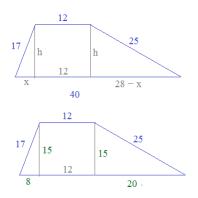


(Use Pythagorean Theorem to get missing lengths)

C) What is the area and perimeter of each parallelogram?



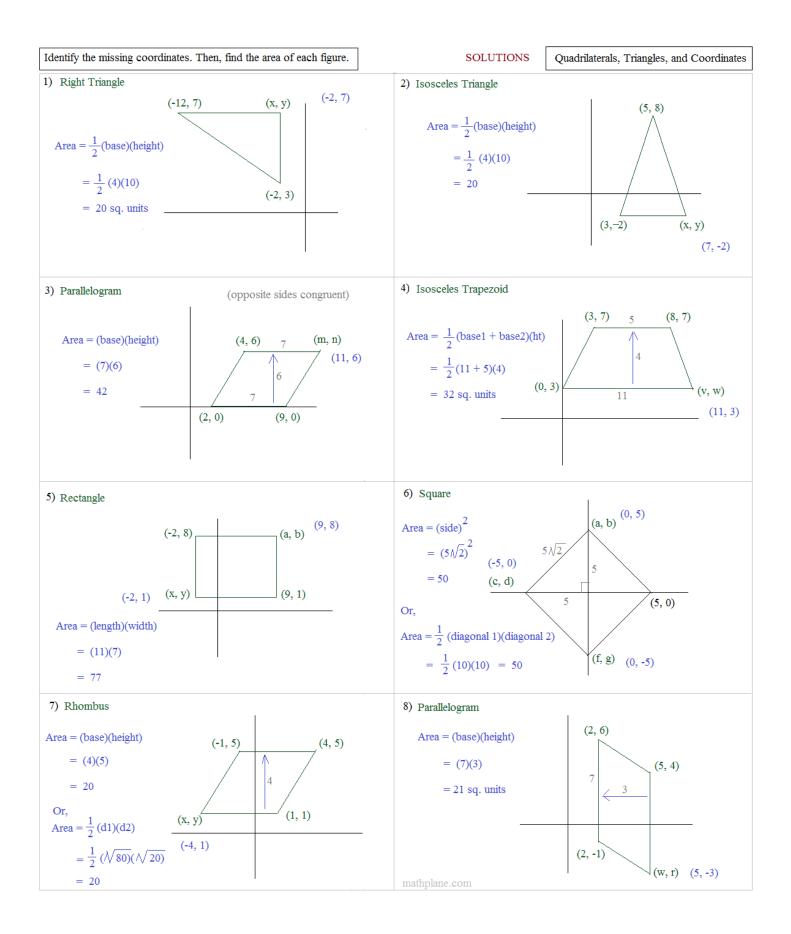
D) Find the area of a trapezoid with sides 12, 17, 40, and 25 where 12 and 40 are the bases.



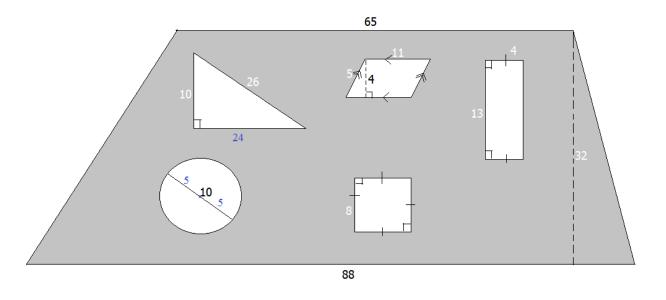
$x^2 + h^2 = 17^2$	$h^2 = 289 - x^2$
$(28 - x)^2 + h^2 = 25^2$	$h^2 = 625 - (784 - 56x + x^2)$
	$289 - x^2 = 625 - 784 + 56x - x^2$
	448 = 56x
	x = 8 then, $h = 15$
	area = $(1/2)(40 + 12)(15) = 390$ sq units

Step 2: Use the formula for a parallelogram to identify the height...

4.8



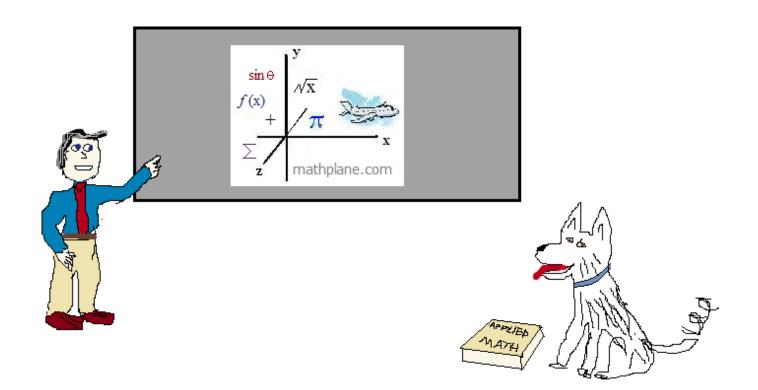
What is the shaded area?



square: $S^2 = (8)^2 = 64$ circle: π (radius)² = π (5)² = 25 π triangle: $\frac{1}{2}$ (base)(height) = $\frac{1}{2}$ (10)(24) = 120 parallelogram: (base)(height) = (11)(4) = 44 rectangle: (length)(width) = (13)(4) = 52 total ("cut out") area = 280 + 25 π or approximately 358.5

mathplane.com

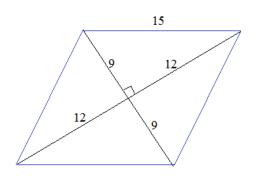
Thanks for visiting the site. (Hope it helped!) If you have questions, suggestions, or requests, just let us know. Best of luck!



Also, at Facebook, Google+, Pinterest, TES, and TeachersPayTeachers

One more question! A rhombus has diagonals that measure 18 and 24. What is the <u>height</u> of the rhombus? (Answer on next page) Challenge Question: A rhombus has diagonals that measure 18 and 24. What is the <u>height</u> of the rhombus?

Step 1: Draw a diagram



Step 3: Solve

area of rhombus: $\frac{1}{2}$ (diagonal 1)(diagonal 2)

area of a parallelogram: (base)(height)

$$\frac{1}{2}(18)(24) = 216$$

Step 2: Recognize useful formulas and quadrilateral properties

the diagonals of a rhombus are perpendicular bisectors

Therefore, the sides of the rhombus are 15

216 = (base)(height)

216 = (15)(height) height = 14.4 units

