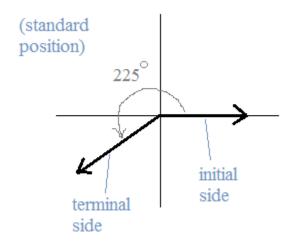
Trigonometry:

Angle Measurement

Notes, Examples, Practice Quiz, and Puzzle (with Solutions)



Includes coterminal and reference angles, Degrees/Minutes/Seconds, angle vs. linear speed, radians, and more.

Degrees/Minutes/Seconds Measurement of Angles

Angle measurements are not always whole numbers.

For example: when you bisect a 45° angle, what is the measure of the resulting angles?

$$\frac{45^{\circ}}{2} = ?$$

The solution contains a 'fractional degree' ..

It can be expressed in 'decimal form'

22° 30' It can be expressed in 'DMS form'

1 degree = 60' (60 minutes)

1 minute = 60" (60 seconds)

Degrees/Minutes/Seconds (DMS) Form

Angle measurements can be expressed using standard divisions of a degree.

1 degree = 60 minutes
$$1^{\circ} = 60'$$

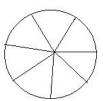
Then, 1 degree = 3600 seconds
$$1^{\circ} = 3600$$
"

Example: Suppose you divide a circle into 7 equal parts. What is the measure of each angle?

$$\frac{360^{\circ}}{7} = \boxed{51.429^{\circ}}$$
 Decimal Form (rounded to 3 decimal places)

$$51.429^{\circ} = 51^{\circ} + .429^{\circ} \times \frac{60'}{1^{\circ}}$$

 $= 51^{\circ} + 25.74'$
 $= 51^{\circ} + 25' + .74' \times \frac{60''}{1'}$
 $= 51^{\circ} + 25' + 44.4''$ DMS Form



Example: Write 72°15' 23" in Decimal Form (rounded to 3 places)

$$72^{\circ}15'23''$$

$$72^{\circ} + \frac{15^{\circ}}{60} + \frac{23^{\circ}}{3600}$$

$$73^{\circ} + 25^{\circ} + 206^{\circ}$$

$$15' \cdot \frac{1}{60'} = .25^{\circ}$$

$$72^{\circ} + .25^{\circ} + .006^{\circ}$$

$$23" \cdot \frac{1}{3600} = .006^{\circ}$$

approximately
$$72.256^{\circ}$$

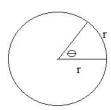
Radian Measurement of Angles

What is a Radian?

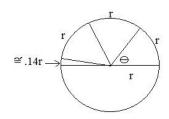
Formal Definition: Measure on an angle with vertex at the center of a circle that subtends an arc equal to the radius of the circle.

What does that mean?

If you take the radius of the circle and lay it on the circle, the angle formed by that arc is ONE RADIAN.



(In other words, if you laid the radius around the circle, it would take approx. 3.14 radii to cover half of the circle..)



It follows that the degree measure of an angle that is 1 radian would be

Converting Radians/Degrees

$$180^{\circ} = \text{Tradians}$$
 $\frac{180^{\circ}}{\text{Tradians}} = 1 = \frac{\text{Tradians}}{180^{\circ}}$

Examples:

Degrees ---> Radians
$$60^{\circ} \cdot \frac{\text{Tradians}}{180^{\circ}} = \frac{\text{Tradians}}{3} \text{ radians (rad)}$$

$$360^{\circ} \cdot \frac{\text{Tradians}}{180^{\circ}} = 2 \text{Tradians}$$

$$147^{\circ} \cdot \frac{\text{Tradians}}{180^{\circ}} \cong 0.817 \text{Tradians}$$

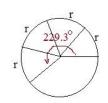
$$\cong 0.817 \cdot (3.14) \text{ radians}$$

approximately 2.56 radians

Radians --- Degrees
$$\frac{1}{2}$$
 radians $\cdot \frac{180^{\circ}}{17}$ radians $= 90^{\circ}$

$$\frac{7}{3}$$
 rad $\cdot \frac{180^{\circ}}{11}$ radians = 420°

4 radians
$$\cdot \frac{180^{\circ}}{\cancel{11}}$$
 radians $= \frac{720^{\circ}}{\cancel{11}} = \frac{720^{\circ}}{3.14}$

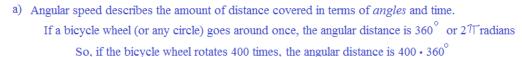


(r = length of radius)

Angular vs. Linear Speed

Example: A bicycle wheel spins at a rate of 400 rotations/minute. If the diameter of the wheel is 26",

- a) what is the angular speed?
- b) what is the linear speed?



= 144,000 degrees/minute

Of

= 800 [↑] radians/minute approx. 2513 radians/minute



b) Linear speed describes the distance covered by a point on the circumference path of the rotating item.

Suppose a little person went around the bicycle wheel one time. He would travel the circumference of the wheel:

circumference =
$$2 \%$$
 radius or $\%$ diameter

Since the wheel's circumference is $7 T \times 26$ inches = 81.68 inches, the linear distance of 400 trips around would be $400(7 T \times 26$ inches) = 32,672 inches

Therefore, the linear speed of the wheel is approximately 32,672 inches/minute or 2723 feet/minute



Now, suppose we measure the angular and linear speed of the bicycle rim.

Again, the wheel spins at a rate of 400 rotations/minute.

If the radius of the rim is 11 inches (diameter is 22 inches), then

- a) what is the angular speed?
- b) what is the linear speed?



$$360 \frac{\text{degrees}}{\text{rotation}} \times 400 \frac{\text{rotations}}{\text{minute}} = 144,000 \frac{\text{degrees}}{\text{minute}}$$



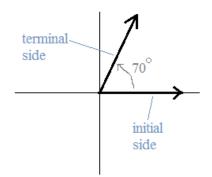
b) linear speed =
$$\frac{\text{distance traveled}}{\text{time}}$$

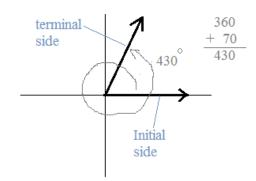


Coterminal vs. Reference Angles

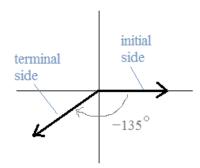
Coterminal Angles: Angles that share the same terminal side (when drawn in standard position)

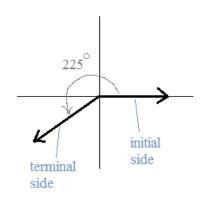
Examples:





70 degree and 430 degree angles are coterminal

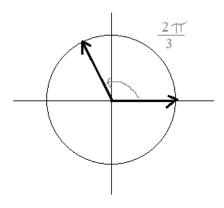


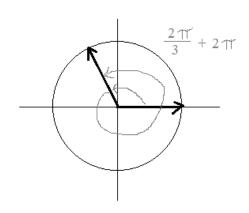


-135 degree and 225 degree angles are coterminal

note:
$$-135^{\circ} + 360^{\circ} = 225^{\circ}$$

If the angle is measured in radians, adding or subtracting 2 T will reveal coterminal angles

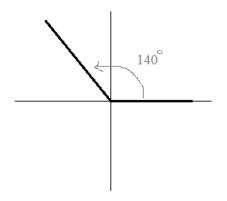




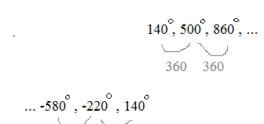
Coterminal vs. Reference Angles

Question: Can you identify one positive and one negative coterminal angle to 140 degrees?

Here is a 140° angle in standard position:

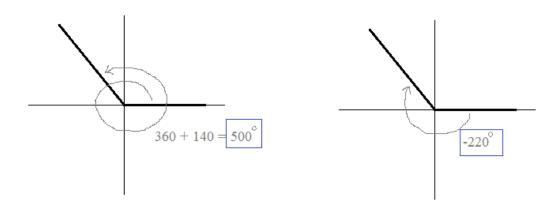


**To find coterminal angles, add/subtract 360°



So, one positive coterminal angle to 140° is 500°

and one negative coterminal angle to 140° is -220°



Question: Are 217° and -143° coterminal angles?

Since -143 + 360 = 217, these are coterminal angles..

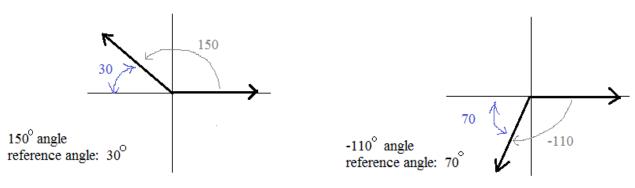
Question: What are all the coterminal angles to -20°?

One way to express the answer: $340^{\circ} + 360^{\circ} n$, where n is any integer...

Coterminal vs. Reference Angles

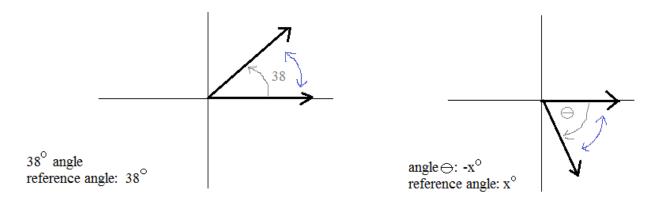
Reference angle: the *acute* angle between the x-axis and the terminal side of an angle (in standard position) ("an acute angle version of an angle")

Examples:

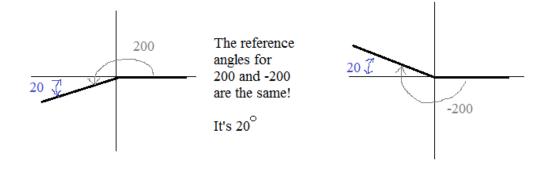


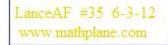
Observations: 1) since reference angles are measures, they have a positive value

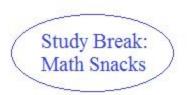
2) any acute angle in quadrant I has an identical reference angle



Questions: Find the reference angles for 200° and -200°









Preferable to ordinary computer cookies ...

Essential part of a well-rounded, academic diet.

Try with (t), or any beverage...

Also, look for Honey Graham Squares in the geometry section of your local store...

PRACTICE TEST (w/SOLUTIONS)-→

- 1) Write 21°18' 49" using decimal degrees.
- 2) Write 88.297° using DMS (Degrees, Minutes, & Seconds)
- 3) ∠A and ∠B are complementary angles.

$$\angle A = 62^{\circ} 15' 23''$$
 What is the measure of $\angle B$?

4) At 2:30pm, what is the angle measure between the hour and minute hands? Express your answer in decimal degree form <u>and</u> DMS form.

5) What is the radian measure of 120° ? 75° ?

6) Convert a) $\frac{\gamma \gamma}{6}$ radians to degrees. b) 3.6 radians to degrees

Coterminal and Reference Angles

I. Coterminal Angles

1) Determine if the following pairs are coterminal:

- 2) Identify one positive and one negative coterminal angle to -30 degrees
- 3) Identify one *positive* and one *negative* coterminal angle to $\frac{1}{3}$ (use radian measures)
- 4) Write an expression that describes all coterminal angles to 100 degrees

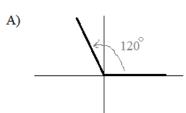
II. Reference Angles

Identify the reference angle for each angle:

B)

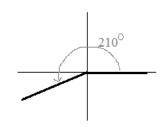
III. Coterminal vs Reference Angles

For each of the following, identify the reference angle and any coterminal angle:



Reference Angle:

Coterminal Angle:



Reference Angle:

Coterminal Angle:

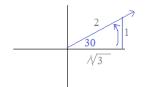
1) 30°

reference angle? 30°

coterminal angle? ex: 390, -330

sine? $\frac{1}{2}$ cosine? $\frac{\sqrt{3}}{2}$

convert to radians: $30 \cdot \frac{1}{180} = \frac{1}{6}$ radians



2) -60[°]

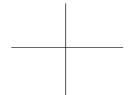
reference angle?

coterminal angle?

sine?

cosine?

convert to radians:



3) -120[°]

reference angle?

2 coterminal angles?

tangent?

cosine?

convert to radians:



4) $\frac{31}{4}$ radians

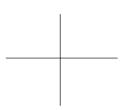
reference angle?

coterminal angle?

sine?

tangent?

convert to degrees:



5) $\frac{-1}{6}$ radians

reference angle?

2 coterminal angles?

sine?

cosine?

convert to degrees:



6) $\frac{9 \, \text{T}}{4}$ radians

reference angle?

coterminal angle?

sine?

tangent?

convert to degrees:



7) 90°

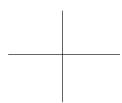
coterminal angle?

tangent?

sine?

cosine?

convert to radians:



8) Tradians

negative coterminal angle?

positive coterminal angle?

sine?

cosine?

convert to degrees:



9) 480°

reference angle?

coterminal angle?

sine?

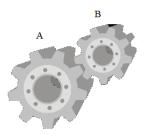
cosine?

convert to radians:

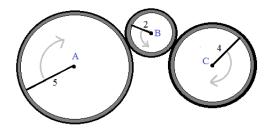


Gear A has a radius of 12 inches. Gear B has a radius of 7 inches.

If A makes 20 revolutions per minute, how many revolutions per minute does B make?



2) If wheel A makes 10 revolutions, how many revolutions will wheel C make?



- 3) A computerized spin balance machine rotates a 25" diameter tire at 480 revolutions per minute.
 - a) find the road speed (in miles per hour) at which the tire is being balanced.
 - b) At what rate should the spin balance machine be set so that the tire is being tested for 70 miles per hour?

SOLUTIONS

1) Write 21°18' 49" using decimal degrees.

$$21^{\circ} + 18' \frac{1^{\circ}}{60'} + 49'' \frac{1^{\circ}}{3600''}$$

 $21^{\circ} + .3^{\circ} + .014^{\circ} = 21.314^{\circ}$

2) Write 88.297° using DMS (Degrees, Minutes, & Seconds)

$$88^{\circ} + .297^{\circ} \frac{60'}{1^{\circ}}$$

$$17.82' \longrightarrow 17' + .82' \frac{60''}{1'}$$

$$49.2''$$

3) ∠A and ∠B are complementary angles.

$$\angle A = 62^{\circ} 15' 23"$$
 What is the measure of $\angle B$?

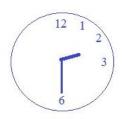
Complementary -- therefore,
 $A + B = 90$ $90^{\circ} - 62^{\circ} 15' 23" = 27^{\circ} 44' 37"$
 $90^{\circ} - 62.26^{\circ} = 27.74^{\circ}$

4) At 2:30pm, what is the angle measure between the hour and minute hands? Express your answer in decimal degree form and DMS form.

3:00 would obviously be 90°

2:30 takes a little bit of thought...

- 1) There are 360 degrees in a circle.. Since there are 12 hours -- 30° between each hour
- 2) At 2:30, the hour hand is HALFWAY between the 2 and the 3..



Degrees from 3 to $6 = 90^{\circ}$

Degrees from 3 to the middle of 2 and $3 = 15^{\circ}$

Angle is $90 + 15 = 105^{\circ}$

5) What is the radian measure of 120° ? 75° ?

$$120^{\circ}$$
 · $\frac{\pi \text{ radians}}{180^{\circ}} = \frac{2}{3} \pi \text{ radians}$ 75° · $\frac{\pi \text{ radians}}{180^{\circ}} = \frac{5}{12} \pi \text{ radians}$ $\cong .417 (3.14) \text{ rad}$ approximately 1.308 rad

6) Convert a) $\frac{\pi}{6}$ radians to degrees. b) 3.6 radians to degrees

$$\frac{\Upsilon}{6} \text{ radians} \cdot \frac{180^{\circ}}{\pi \text{ radians}} = 30^{\circ} \qquad 3.6 \text{ radians} \cdot \frac{180^{\circ}}{\pi \text{ radians}} = \frac{3.6 (180^{\circ})}{\pi}$$

$$\stackrel{\cong}{=} \frac{3.6 (180^{\circ})}{3.14}$$

$$\text{approximately } 206.369^{\circ}$$

Coterminal and Reference Angles

SOLUTIONS

I. Coterminal Angles

1) Determine if the following pairs are coterminal:

a)
$$57^{\circ}$$
 357° NO $357 - 57 = 300$

YES
$$280 - (-80) = 360^{\circ}$$

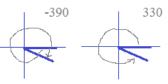
b)
$$-20^{\circ}$$
 160° NO $160 - (-20) = 180$

d)
$$-40^{\circ}30'$$
 $319^{\circ}30'$ YES $-40^{\circ}30'$ - $(319^{\circ}30') = -360^{\circ}$

2) Identify one positive and one negative coterminal angle to -30 degrees

$$-30 + 360 = 330 \text{ degrees}$$
 $-30 - 360 = -390 \text{ degrees}$





3) Identify one *positive* and one *negative* coterminal angle to $\frac{1}{3}$

subtract 2 ↑ ↑

(use radian measures)

add
$$2 \text{ T}$$
 $\boxed{\frac{7 \text{ T}}{3}}$

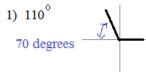
4) Write an expression that describes all coterminal angles to 100 degrees

$$100^{\circ} + 360^{\circ}$$
 n where n is any integer....

II. Reference Angles

Identify the reference angle for each angle:

(reference angle is measured from the terminal side to the x-axis)

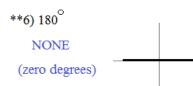






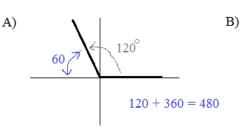


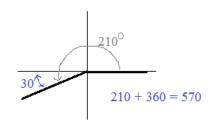
5) -150° 30 degrees



III. Coterminal vs Reference Angles

For each of the following, identify the reference angle and any coterminal angle:





Reference Angle: 60 degrees

Coterminal Angle: 480 degrees

Reference Angle: 30 degrees Coterminal Angle: 570 degrees

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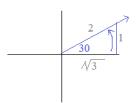
Trigonometry angle measurements and terms

SOLUTIONS

1) 30°

reference angle? 30° coterminal angle? ex: 390, -330 sine? $\frac{1}{2}$ cosine? $\frac{\sqrt{3}}{2}$

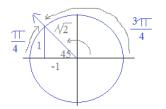
convert to radians: $30 \cdot \frac{1}{180} = \frac{1}{6}$ radians



4) $\frac{37}{4}$ radians

reference angle? $\frac{1}{4}$ or 45 degrees coterminal angle? ex: $\frac{1}{4}$ / $\frac{-5}{4}$ sine? $\frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$

convert to degrees: $\frac{3 + 1}{4}$ 135°



7) 90°

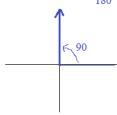
ex: 90 + 360 = 450coterminal angle? 90 - 360 = -270

tangent? undefined

sine? 1

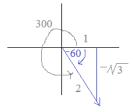
cosine? 0

convert to radians: $90 \cdot \frac{1}{180} = \frac{1}{2}$ radians



2) -60°

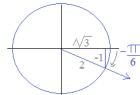
reference angle? coterminal angle? ex: 300, 660 convert to radians: $-60^{\circ} \cdot \frac{71777}{180^{\circ}} = \frac{-7177}{3}$ radians



5) $\frac{-1}{6}$ radians

reference angle? $\frac{11}{6}$ or 30 degrees 2 coterminal angles? $\frac{-1}{6} + 2 = \frac{11}{6}$ sine? $\frac{-1}{2}$ $\frac{-1}{6} - 2 = \frac{13}{6}$ cosine? $\sqrt{3/2}$

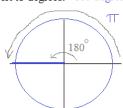
convert to degrees: $-\frac{1}{6} \cdot \frac{180}{1} = -30$ degrees



8) Tradians

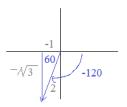
negative coterminal angle? ex: -∏ or -3∏ positive coterminal angle? ex: 3∏ or 5∏ sine? 0 cosine? -1

convert to degrees: 180 degrees



3) -120°

reference angle? 60° 2 coterminal angles? -120 + 360 = 240 $-120 - 360 = -480^{\circ}$ tangent? $\sqrt{3}$ cosine? $-\frac{1}{2}$ convert to radians: $-120 \cdot \frac{117}{180} = \frac{-2117}{3}$ rad



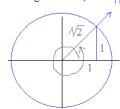
6) $\frac{91}{4}$ radians

reference angle? $\frac{11}{4}$ or 45 degrees

coterminal angle? ex: $\frac{\sqrt{11}}{4}$ sine? $\frac{\sqrt[4]{2}}{2}$

tangent? 1

convert to degrees: $\frac{9}{4} \cdot \frac{180}{1} = 405$



9) 480°

reference angle? 60° coterminal angle? $480 - 360 = 120^{\circ}$

sine?

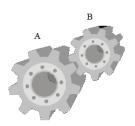
convert to radians: $480 \cdot \frac{1}{180} = \frac{811}{3}$ radians



SOLUTIONS

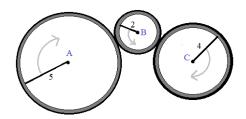
Gear A has a radius of 12 inches.
 Gear B has a radius of 7 inches.

If A makes 20 revolutions per minute, how many revolutions per minute does B make?



Gear B:
$$\frac{480 \text{ TI inches}}{1 \text{ minute}}$$
 $\frac{\cdot}{\cdot}$ $\frac{14 \text{ TI inches}}{1 \text{ revolution}}$ = $34 \frac{2}{7}$ revolutions/minute

2) If wheel A makes 10 revolutions, how many revolutions will wheel C make?



- A 10 revolutions: 100 1 (linear distance)
- B 100 ↑ (25 revolutions)

C 100
$$\uparrow \uparrow$$
 = 12.5 revolutions

- 3) A computerized spin balance machine rotates a 25" diameter tire at 480 revolutions per minute.
 - a) find the road speed (in miles per hour) at which the tire is being balanced.
 - b) At what rate should the spin balance machine be set so that the tire is being tested for 70 miles per hour?
 - a) since we're looking for the "road speed", we need to find 'traveling distance as it relates to time' i.e. miles/hour

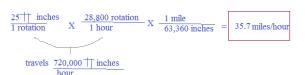
since diameter is 25", every rotation is the circumference: 25

25 inches 1 rotation

since the machine rotates the tire 480 revolutions per minute, it rotates the tire $480 \times 60 = 28,800$ revolutions per hour

28,800 rotation 1 hour

Now, convert to the units miles/hour



NOTE: all the units cancel, leaving miles/hour

b) First, let's find out how many rotations are required to travel 70 miles...

since we're seeking 70 miles/hour.

we know 56,470.7 revolutions/hour are required....

Divide that by 60 minutes:

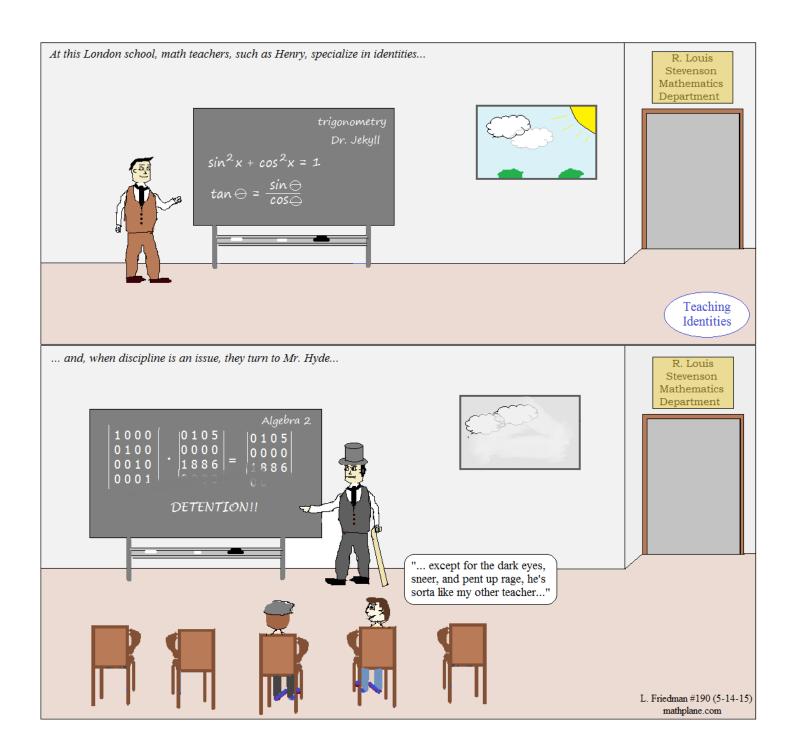
941.18 revolutions/minute

$$\frac{941.18 \text{ rev/minute}}{70 \text{ miles/hour}} = \frac{480 \text{ rev/minute}}{35.7 \text{ miles/hour}} \checkmark$$

Yes, the short-cut from a) to b)

$$\frac{S}{70 \text{ miles/hour}} = \frac{480 \text{ rev/minute}}{35.7 \text{ miles/hour}}$$

$$S = 941.18 \text{ rev/minute}$$



Hidden Message Puzzle-→

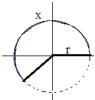


Answer the 12 questions below. Then, convert the numbers into letters to reveal the hidden term!

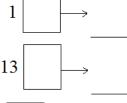
Number Key:

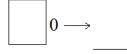
0 1 2 3 4 5 6 7 8 9 A C D E G H K N R T

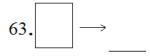
- 1) Seconds between 24° 12' and 24° 11' 41"
- 2) $\frac{3\pi'}{4}$ Radians = x degrees. What is x?
- 3) Minutes in 1/2 degree
- 4) 63°41' 45" : convert to decimal form (round to nearest tenth)
- 5) $71.15^{\circ} = 71^{\circ} x' y''$ What is x?
- 6) $36^{\circ} = \frac{\cancel{1}}{z}$ Radians What is z?
- 7) Angles A and B are complementary. $m\angle A = 43^{\circ} 32' 30'' \quad m\angle B = 46^{\circ} x' 30''$ What is x?
- 8) At 1:00, what is the degree measure between the hour hand and minute hand?
- 9) Approximate arc length of x (measured in radians rounded to nearest integer)



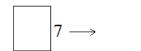
- 10) Degrees in 5 Radians
- 11) Seconds in 1 degree
- 12) Convert to degrees (decimal form): 144°18'

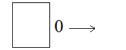


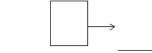


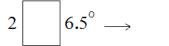


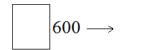


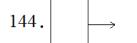














Answer the 12 questions below. Then, convert the numbers into letters to reveal the hidden term!

Number Key:

2 3 1 4 5 6 7 8 ACDEGHKNRT

13

SOLUTIONS

2)
$$\frac{3 \cancel{n}'}{4}$$
 Radians = x degrees. What is x?

$$\frac{3 \text{ pi radians}}{4} \cdot \frac{180 \text{ degrees}}{\text{pi radians}} = 135 \text{ degrees}$$

$$\begin{array}{c|c}
1 & 9 & \longrightarrow & T \\
\hline
\end{array}$$

Η

T

60 minutes = 1 degree... therefore, 30 minutes =
$$1/2$$
 degree

$$\begin{bmatrix} 3 & 0 \longrightarrow & E \end{bmatrix}$$

$$63^{\circ} + 41' \frac{1^{\circ}}{60'} + 45" \frac{1^{\circ}}{3600"} \approx 63 + .6833 + .0125$$

 ≈ 63.6958

63.
$$7 \longrightarrow N$$

9

5)
$$71.15^{\circ} = 71^{\circ} x' y''$$
 What is x?

.15 degrees x
$$\frac{60 \text{ minutes}}{1 \text{ degree}} = 9 \text{ minutes}$$

$$x = 9$$
 $y = 0$

6)
$$36^{\circ} = \frac{\cancel{1}}{2}$$
 Radians What is z?

$$\frac{17}{z} \text{Rad} \left(\frac{180^{\circ}}{\text{T/Rad}} \right) = \frac{180^{\circ}}{z} = 36 \text{ degrees} \qquad z = 5$$

 $43^{\circ} 32' 30'' + 46^{\circ} x' 30'' = 90^{\circ}$

$$5 \longrightarrow H$$

7) Angles A and B are complementary.

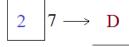
$$m \angle A = 43^{\circ} 32' 30'' \quad m \angle B = 46^{\circ} x' 30'$$

$$89^{\circ} (32 + x)' + 60'' = 90^{\circ}$$

 $x = 27$

$$m\angle A = 43^{\circ} 32' 30'' \qquad m\angle B = 46^{\circ} x' 30''$$

What is x?



Approximate arc length of x (measured in radians - rounded to nearest integer)

clock is 360 degrees 12 hours; 30 degrees between each hour!

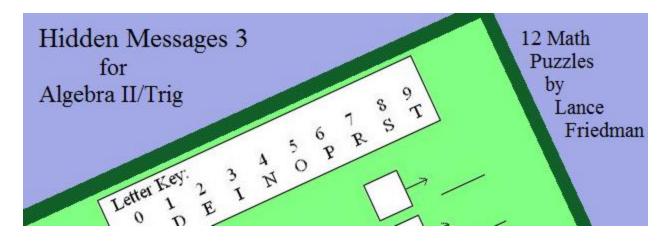
10) Degrees in 5 Radians
$$\frac{180^{\circ}}{\text{Tradians}}$$
 $\frac{1}{900^{\circ}/3.1415} \approx 286.5^{\circ}$

$$4 \longrightarrow G$$

R

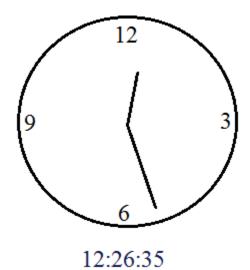
$$\left\langle \frac{60 \text{ seconds}}{1 \text{ minute}} \right\rangle \cdot \left\langle \frac{60 \text{ minutes}}{1 \text{ degree}} \right\rangle = 3600 \text{ secondes/degree}$$

144 degrees + 18 minutes x
$$\frac{1 \text{ degree}}{60 \text{ minutes}}$$
 = 144.3 degrees



More puzzles available in the "travel log collection" at mathplane.com. Proceeds go to site maintenance and improvement. (And, treats for Oscar the Dog!)

Clock Question:



When will the minute hand cross the hour hand?

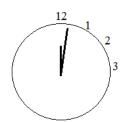
Express the answer to the nearest second.

(Answer and Explanation on the next page)

Question:

A clock sits at exactly 12:02...

What time will the minute hand cross the hour hand? Express the answer to the nearest second...



Measurements to remember:

60 minutes = 1 hour

60 seconds = 1 minute

3600 seconds = 1 hour

Solution:

The hour hand will move from one number to the next every 60 minutes (or 3600 seconds)

The minute hand will move from one number to the next every 5 minutes (or 300 seconds)

The minute hand goes around the clock and returns to the top. (1:00)... The minute hand is on the 12, and the hour hand is on the 1....

Then, the minute hand reaches the 1 five minutes later (1:05)...

***But, during those 5 minutes, the hour hand moved!!

How far?

The hour hand moves from 1 to 2 in 60 minutes...

So, during the 5 minutes, the hour hand moved $\,$ 5/60 or $\,$ 1/12 of the way to $\,$ 2...

So, how long would it take for the minute hand to travel 1/12 of the way to 2?

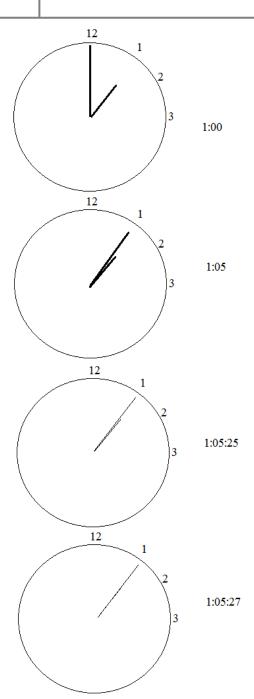
Well, it takes 300 seconds for the minute hand to travel from 1 to 2... Therefore, it takes 25 seconds to travel 1/12 of the way!!

But, wait.... During those 25 seconds, the hour hand is still moving... So, during the 25 seconds, how far did the hour hand move?

Well, it takes 3600 seconds for the hour hand to move from 1 to 2... Therefore, in 25 seconds, the hour hand moved 25/3600 of the distance.. This is approx. .007

Again, it takes 300 seconds for the minute hand to travel from 1 to 2. Therefore, it would take approx. 2 seconds to travel .007 of the way between 1 and 2.

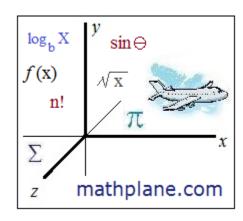
So, the minute hand has moved 63 minutes to get to 1:05...
Then, 25 seconds to close in on the hour hand... 1:05:25...
And, finally, 2 more seconds to reach the hour hand... 1:05:27



Thanks for visiting. (Hope it helped!)

If you have questions, suggestions, or requests, let us know.

Cheers



Also, at TeachersPayTeachers, TES and Pinterest And, mathplane.ORG for mobile and tablets