Calculus: Derivatives

Maximum/Minimum Word Problems

Topics include cost function, ellipse, distance, volume, surface area, and more.

Calculus: First Derivative Max/Min Applications

Revenue function: R(x) = 6x1)

Cost function: $C(x) = x^3 - 6x^2 + 15x$

Verify that the best your business can do is 'break even'

Profit = Revenue - Cost

$$P(x) = 6x - (x^3 - 6x^2 + 15x)$$
$$= -x^3 + 6x^2 - 9x$$

To find maximum/minimum profit, set first derivative equal to zero:

P'(x) =
$$-3x^2 + 12x - 9$$
 $x^2 - 4x + 3 = 0$

 $-3x^2 + 12x - 9 = 0$ (divide by -3)

$$x^2 - 4x + 3 = 0$$
 (factor)

$$(x-1)(x-3) = 0$$
 (solve)

$$x = 1$$
 and 3

Test each solution in the original equations!

At 1:

$$R(1) = 6(1) = 6$$

$$C(1) = (1)^3 - 6(1)^2 + 15(1) = 10$$

Cost (10) exceeds Revenue (6)

Business loses money.....

At 3. R(3) = 6(3) = 18

$$C(3) = (3)^3 - 6(3)^2 + 15(3)$$

$$= 27 - 54 + 45 = 18$$

Cost (18) matches Revenue (18)

Business breaks even...

What is the maximum area of a rectangle 2) that is inscribed under $y = -x^2 + 9$ and above the x-axis.

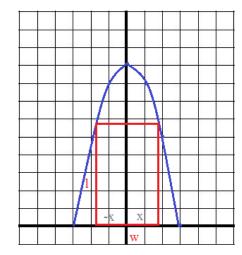
Step 1: Write variables and formulas

Area of rectangle = length
$$x$$
 width

width =
$$x + |-x| = 2x$$

length =
$$-x^2 + 9$$

Step 1a: Draw a picture



Step 2: Find maximum of function (take the derivative, and set = 0)

$$A(x) = (-x^2 + 9)(2x)$$

$$= -2x^3 + 18x$$

$$A'(x) = -6x^2 + 18$$

set equal to zero to find max/min

$$-6x^2 + 18 = 0$$

$$x^2 = 3$$

$$x = \sqrt{3} - \sqrt{3}$$

Step 3: Solve/Answer the question

Since the maximum area occurs at $x = \sqrt{3}$

the length =
$$-(\sqrt{3})^2 + 9 = 6$$

the width =
$$2(\sqrt{3})$$
 = $2\sqrt{3}$

Area = $12\sqrt{3}$ or approximately 20.8 square units

Derivatives: Maximum/Minimum Examples

3) Find the absolute extremes:

$$f(x) = (x-3)^2 + 1$$
 over the domain [2, 6]

Using Derivatives:

Find derivative of the function:

$$f'(x) = 2(x-3)^{1} + 0$$
$$= 2x - 6$$

Then, to find the extremes, set f'(x) = 0

$$2x - 6 = 0$$
$$x = 3$$

Is x = 3 a minimum or a maximum?

Test points:

$$x = 2$$
 $f(2) = 2$
 $x = 3$ $f(3) = 1$ MINIMUM
 $x = 4$ $f(4) = 2$

on the right

Note:

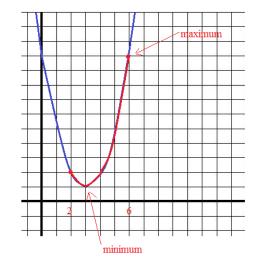
$$f'(2) = -2$$
 Since it is negative, the function decreases on the left $f'(3) = 0$ $f'(4) = 2$ Since it is positive, the function increases

f''(x) = 2 Since it is positive, the function is concave up (this implies the critical value is a minimum!)

Graphing:

$$f(x) = x^2 - 6x + 10$$

Parabola: Axis of symmetry: x = 3 y-intercept: (0, 10) x-intercepts: NONE Vertex: (3, 1)



In the domain [2, 6],

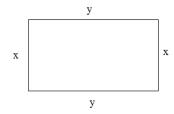
the minimum is x = 3maximum is x = 6

4) Assume you have 60 feet of fencing. What is the maximum area you could enclose? What are the dimensions of the enclosed area?

Step 1: Establish variables and formulas

Area = xy Perimeter = 60
Perimeter =
$$2x + 2y$$
 We want to maximize the area:
 $60 = 2x + 2y$ (with respect to x)
 $30 = x + y$ $A(x) = x(30 - x)$
 $y = 30 - x$ $A(x) = -x^2 + 30x$
 $A'(x) = -2x + 30$

Step 1a: Draw a diagram



Step 3: Find critical values and solve

A'(x) = 0

$$-2x + 30 = 0$$
 $2x + 2y = 60$
 $x = 15$
Since x = 15, y = 15
Area = 225 square feet

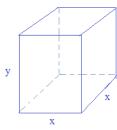
dimensions: 15' x 15'

Step 2: Find derivative of equation you want to maximize

Graph of one fence side and the corresponding area A(x) (15, 225) (0, 0) (30,0) (30,0) (30,0)

- a) What are the dimensions of the container that will minimize the weight?
- b) What is the surface area of the container?

Step 1: Draw a diagram and label



(since it is square-based, the length and width are equal)

Step 3: Find minimum of function!

$$SA = \frac{2400}{x} + x^2$$
$$SA' = \frac{-2400}{x^2} + 2x$$

(set derivative equal to zero)

to find critical values

to find critical values
$$\frac{-2400}{x^2} + 2x = 0 \qquad \text{(multiply by } x^2\text{)}$$

$$2x^3 - 2400 = 0$$

$$x^3 = 1200$$

$$x = 2\sqrt[3]{150} \quad \text{feet}$$

$$x = 10.63 \text{ feet} \quad \text{(approximately)}$$

Volume = (length)(width)(height) Surface Area =
$$4 \cdot (area \text{ of each side}) + (area \text{ of bottom})$$
 $V = x \cdot x \cdot y = x^2 y$

$$600ft^3 = x^2 y$$

**Since we are trying to minimize surface area, we will try to set up SA in terms of one variable (x)

 $y = \frac{600}{x^2}$ therefore, $A = 4x \cdot (area \text{ of each side}) + (area \text{ of bottom})$

$$SA = 4xy + x^2$$

$$SA = 4x \cdot (area \text{ of each side}) + (area \text{ of bottom})$$

Step 4: Answer the questions:

a) What are the dimensions?

Since x = 10.63,
$$y = \frac{600}{(10.63)^2} = 5.31$$
 (approximately)

slightly more than

10.63' x 10.63' x 5.31' \longrightarrow 600 cubic feet

b) What is the surface area of the container?

$$SA = 4xy + x^{2}$$

$$= 4(10.63)(5.31) + (10.63)^{2}$$

$$= 338.78 \text{ square feet}$$

6) Suppose you have a 10' x 20' piece of cardboard.

If you wanted to make an open rectangular box (by cutting out the corners & folding up the sides),

- a) what dimensions would create a box with the largest volume?
- b) what is the maximum volume?

Step 1: Label the diagram and write formulas

(original length)(original width) = 200 sq. ft.

Volume of open box =
$$(length)(width)(height)$$

 $(20 - 2x)(10 - 2x)(x)$

Step 2: Establish function

Since we want to maximize volume,

$$V = (20 - 2x)(10 - 2x)(x)$$

$$V = (20 - 2x)(10x - 2x^{2})$$

$$V = 200x - 40x^{2} - 20x^{2} + 4x^{3}$$

$$V = 4x^{3} - 60x^{2} + 200x$$

$$(To find critical value -- max/min --- set first derivative equal to zero)$$

$$V' = 12x^{2} - 120x + 200 = 0$$

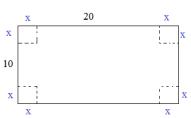
$$(quadratic formula)$$

$$x = \frac{30 \pm \sqrt{900 - 600}}{6}$$

$$= 5 + \frac{5\sqrt{3}}{3} = 7.9$$
extraneous!
$$2 \times 7.9 = 15.8$$

$$15.8 > \text{the width!}$$

 $3x^{2} - 30x + 50 = 0$ $5 - \frac{5\sqrt{3}}{3} = 2.1$



(note: the cut-out corners must be squares; otherwise, the top of the open box will be uneven)

Step 3: Answer the questions

a) What dimension creates the maximum volume?

$$x = 2.1$$
 (cut out 2.1' x 2.1' in each corner)
length = 20 + 2x = 15.8 feet
width = 10 + 2x = 5.9 feet

b) Volume = length x width x height

Your tour company accommodates 60 - 90 people.

If more than 60 people sign up, the rate drops \$2 per person for each additional person after 60...

If less than 60 people sign up, the tour is cancelled.

The cost of each tour is \$6000 plus \$32 per person.

- a) How many people would maximize your profit?
- b) What is your maximum profit?

Step 1: Transform above description into math equations:

The domain is
$$[60, 90]$$
 let $p = \#$ of people

Profit = Revenue - Cost $Cost = \$6000 + \$32p$

Revenue = $p(\$200 - \$2(p - 60))$

Step 3: answer questions

- a) What is the optimal number of people: p = 72
- b) What is your maximum profit?

Revenue:
$$$200 \times 72 = $14,400$$

Discount: 12 people over 60 ---- \$24 discount/person
 $$24 \times 72 = 1728
Total revenue: $$12,672$

Step 2: Maximize equation (profit)

Profit =
$$p(\$200 - \$2(p - 60)) - [\$6000 + \$32p]$$

= $\$200p - \$2p^2 + \$120p - \$6000 - \$32p$
= $\$-2p^2 + \$288p - \$6000$

Take derivative:
$$\frac{dProfit}{dp} = -4p + 288$$

Set equal to zero to find max/min:
$$-4p + 288 = 0$$

 $p = 72$

Step 4: Check your answer

72 tourists: Profit: \$4368

73 tourists: Revenue: \$200 x 73 = \$14,600 Discount: (13 x \$2) x 73 = \$1898 Cost: \$6000 + (\$32 x 73) = \$8336 Profit: \$4366

8) The quantity $Q = 2x^2 + 3y^2$ is subject to the constraint x + y = 5.

What is the minimum quantity of Q?

Since Q is a function of x and y, let's change to 1 variable....

$$x + y = 5$$
 \longrightarrow $y = 5 - x$ then, substitute into the main equation...

$$Q = 2x^{2} + 3(5 - x)^{2}$$

$$Q = 2x^{2} + 75 - 30x + 3x^{2}$$

$$Q = 5x^{2} - 30x + 75$$
 find derivative of Q...
$$Q = 5x^{2} - 30x + 75$$
 find derivative of Q...
$$Q = 10x - 30$$

$$Q = 2(3)^{2} + 3(2)^{2}$$
 then, Q = 35
$$Q = 30$$

$$Q = 35$$

$$Q = 30$$

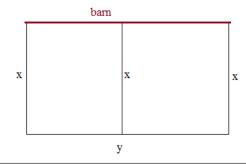
$$Q = 30$$

$$Q = 35$$

Derivative Max/Min Word Problems

9) A farmer is going to build a pen using 240 feet of wood. One side of the pen will border a barn, and there will be a wooden divider to separate the pen into 2 parts.

What is the maximum area of the pen?



Area = xy 'Main Function' that we want to maximize 240 = 3x + y 'Constraint Function'

Using substitution, we make Area as a function of x

Area =
$$x(240 - 3x)$$

 $A = 240x - 3x^2$
 $A' = 240 - 6x$
 $A' = 240 - 6x$
Maximum occurs when $x = 40$ feet and, then when $y = 120$ feet...

Maximum area: 4800 square feet

10) A building's window frame shaped as a rectangle with a semicircle is constructed with 28 feet of wood.

Which dimensions would maximize the light shining inside the building?

To maximize the light, we need to maximize the area of the window.

'Main function to optimize': Area =
$$2xy + \frac{1}{2}\pi x^2$$
rectangle semicircle

'Constraint function'

Perimeter =
$$2x + 2y + \frac{1}{2} \cdot 2 \pi x$$

 $28' = 2x + 2y + \pi x$
 $y = \frac{28' - 2x - \pi x}{2}$

Use substitution and combine the equations

Area =
$$2x(\frac{28 - 2x - \pi x}{2}) + \frac{1}{2}\pi x^2$$

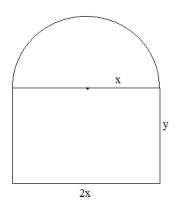
Area = $28x - 2x^2 - \pi x^2 + \frac{1}{2}\pi x^2$
A' = $28 - 4x - 2\pi x + \pi x$

To maximize, set derivative equal to zero....

$$0 = 28 - 4x - \pi x$$

$$28 = 4x + \pi x$$

$$x = \frac{28}{(4 + \pi)} = 3.92 \text{ feet}$$



Bottom: 7.84 feet Left side: 3.92 feet Right side: 3.92 feet

Arch: 3.92 [↑] feet

total: 28 feet

$$y = \frac{28' - 2(3.92') - \Pi(3.92')}{2}$$
$$= \frac{28' - 7.84' - 12.32'}{2} = 3.92 \text{ feet}$$

mathplane.com

Note: since the maximum of A

ignored the radical!

is the same as the maximum of NA, we could have

11) Find the point(s) on the ellipse $x^2 + 4y^2 = 4$ farthest from the point (0, 1).

Step 1: Sketch a diagram

The ellipse in standard form:
$$\frac{x^2}{4} + \frac{y^2}{1} = 1$$

center: (0, 0) major semi-axis: 2 minor semi-axis: 1

horizontal ellipse...

Step 2: Identify main function you wish to maximize

We're looking for the farthest point ---> distance formula

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

since we want the distance from (0, 1):

$$d = \sqrt{(x-0)^2 + (y-1)^2}$$
 where (x, y) is a point from the ellipse..

Step 3: Establish a function of one variable

Rewriting the ellipse: $x^2 = 4 - 4y^2$

then, substitute into distance formula

$$d = \sqrt{(x)^{2} + (y-1)^{2}}$$

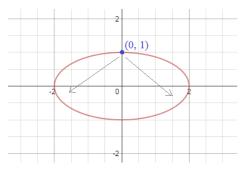
$$d(y) = \sqrt{4 - 4y^{2} + (y-1)^{2}}$$

$$d(y) = \sqrt{5 - 2y - 3y^{2}}$$

Note: we could substitute for y, but substituting for x is much easier...

$$\left(\frac{-4\sqrt{2}}{3} \right)^{\frac{1}{3}}$$

$$\left(\frac{4\sqrt{2}}{3} \right)^{\frac{1}{3}}$$



Step 4: Find the maximum value

$$d'(y) = \frac{1}{2} \left(5 - 2y - 3y^2 \right)^{\frac{-1}{2}} (-2 - 6y)$$

$$d'(y) = \sqrt{\frac{(-1-3y)}{5-2y-3y^2}}$$
 then, set equal to zero

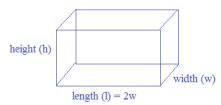
$$y = \frac{-1}{3}$$

Step 5: Answer the question

If
$$y = \frac{-1}{3}$$
 then $x^2 + 4(-1/3)^2 = 4$
 $x^2 = \frac{32}{9}$
 $x = \frac{4\sqrt{12}}{3} = -\frac{4\sqrt{12}}{3}$

12) An open-top rectangular storage container must have volume 10 cubic feet. Also, the length of the base must be twice the width of the base. If the cost of the base is \$10 per square ft. and the cost of each side is \$6 per square ft., what is the minimum cost of a container?

Step 1: Sketch diagram and label variables



Step 2: Identify functions and constraints

$$Volume = lwh = 2w^{2}h = 10$$

$$Cost = \$10(2w^{2}) + 2 x \$6(2wh) + 2 x \$6(wh)$$
 bottom front/back left/right cost cost

Step 3: Establish function (of one variable) that you wish to minimize

Cost =
$$20w^2 + 24wh + 12 wh = 20w^2 + 36wh$$

since (volume) $2w^2 h = 10$ $h = \frac{5}{w^2}$

Substitute into cost function:

$$C(x) = 20w^2 + \frac{180}{w}$$

Step 4: find the minimum

$$C'(x) = 40w - \frac{180}{w^2}$$

set C'(x) = 0,

$$40w = \frac{180}{w^2}$$
 $40w^3 = 180$ $w = 1.65$

so, width = 1.65, length = 3.30 and, 10 = (1.65)(3.30)(h) so height = 1.84 Step 5: Answer the question

Cost of bottom: \$10(1.65)(3.3)= \$54.45

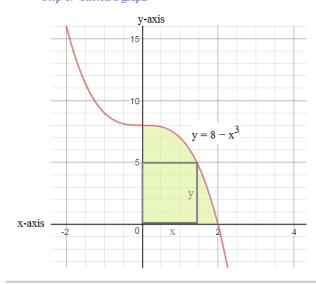
Cost of left/right: 2x \$6(1.65)(1.84)= \$36.43

Cost of front/back: 2x \$6(3.3)(1.84) = \$72.86

Total: \$163.74

the x-axis, y-axis, and $y = 8 - x^3$

Step 1: Sketch a graph



Step 2: Identify the 'optimization' function

We're trying to find the "rectangle with the largest area"

$$Area = xy$$

Since we have 2 variables, we'll substitute for y..

$$A(x) = x(8-x^3)$$
 where $A(x)$ is the area as a function of x

Step 3: Find max/min from derivative

$$A(x) = 8x - x^4$$

$$A'(x) = 8 - 4x^3$$
 $x = \sqrt[3]{2}$

$$x = \sqrt[3]{2}$$

$$0 = 8 - 4x^3$$

Step 4: Answer question

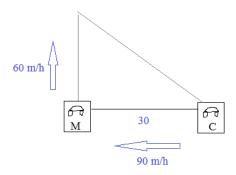
If
$$x = \sqrt[3]{2}$$
 then $y = 6$

so, the dimensions of the rectangle

$$\sqrt[3]{2}$$
 by 6

14) At noon, a corvette is 30 miles due East of a mustang. The corvette goes west at 90 miles per hour. Meanwhile, the mustang goes north at 60 miles per hour. What is the minimum distance between the 2 cars? (When does this occur?)

Step 1: Sketch a diagram and label variables



Step 3: Answer the questions

The minimum distance between cars occurs at 12:14

$$d = \sqrt{(30 - 90t)^2 + (0 + 60t)^2} \quad \text{at } t = .2308$$

$$= \sqrt{(9.228)^2 + (13.84)^2} = 16.6 \text{ miles apart (approx)}$$

Step 2: Identify the optimization function

We're trying to find the minimum distance.

$$d = \sqrt{x^2 + y^2}$$

$$d = \sqrt{(30-90t)^2 + (0+60t)^2}$$
 where t is time in hours

$$d = \sqrt{900 - 5400t + 8100t^2 + 3600t^2} = \sqrt{900 - 5400t + 11700t^2}$$

$$d' = \frac{1}{2} (900 - 5400t + 11700t^2)^{\frac{-1}{2}} (-5400 + 23,400t)$$

$$d' = \frac{(-5400 + 23,400t)}{2 \sqrt{900 - 5400t + 11700t^2}}$$

When is d' = 0? It occurs when the numerator -5400 + 23,400t = 0

t = .2308 hoursor 13.84 minutes Since we're looking for the closest point, we're trying to minimize the distance formula...

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

$$d = \sqrt{(x-4)^2 + (\sin x - 2)^2}$$

$$d(x) = \sqrt{x^2 - 8x + 16 + \sin^2 x - 4\sin x + 4}$$

$$d(x) = \sqrt{x^2 - 8x + 20 + \sin^2 x - 4\sin x}$$

Since the minimum (x) of a function is the same as the minimum (x) of the function squared, we can find the derivative of the function without the radical!

$$d(x) = x^2 - 8x + 20 + \sin^2 x - 4\sin x$$

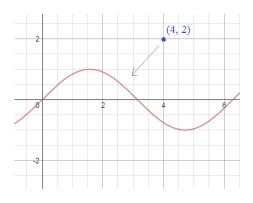
$$d'(x) = 2x - 8 + 2\sin x \cos x - 4\cos x$$

Then, set the derivative equal to zero to find critical values

occurs at
$$x = 2.65$$
 (relative minimum)

and x = 6.18 and x = 5.1 (relative maximum)

Therefore, the closest distance occurs at x = 2.65



16) Find the point on the curve \sqrt{X} that is closest to (5,0).

We want to minimize the distance of (5, 0) to the curve...

$$d = \sqrt{(x-5)^2 + (y-0)^2}$$

First, we'll substitute so that we have one variable...

$$d = \sqrt{(x-5)^2 + (\sqrt{x} - 0)^2}$$

Then, find the derivative....

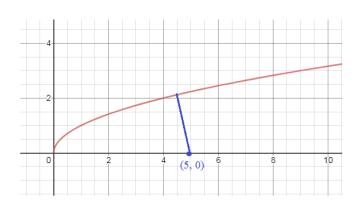
$$d' = \frac{1}{2} (x^2 + 10x + 25 + x) \cdot (2x - 9)$$

And, set equal to zero...

$$\frac{(2x-9)}{2\sqrt{x^2+9x+25}} = 0$$

Therefore, the critical value (minimum) is x = 9/2

$$(\frac{9}{2}, \frac{3}{\sqrt{2}})$$
 approx: (4.5, 2.12)



check: find slope of tangent line.... $y = \sqrt{x}$

$$y' = \frac{1}{2} x^{-1/2}$$

@ x = 4.5, the slope is
$$\frac{1}{2\sqrt{4.5}}$$
 = .236

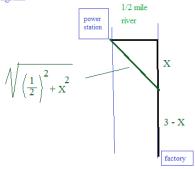
then, find slope of minimum segment...

$$(5, 0)$$
 to $(4.5, 2.12)$ $\implies \frac{-2.12}{.5} = -4.25$ opposite reciprocals

17) A power station is on the side of a river that is 1/2 mile wide. There is a factory located across the river and 3 miles downstream. It costs \$5 per foot to run a cable on land, and it costs \$8 per foot to run a cable underwater.

What is the most economical path for the transmission line?

Step 1: draw a diagram



Step 2: Develop the formulas

Since we're looking for the most economical path, we are trying to *minimize* the cost of the cable.

Cost =
$$8\sqrt{\left(\frac{1}{2}\right)^2 + X} + 5\cdot(3-X)$$
(cable under water) (cable on land)

Step 3: Solve the equation

To find the minimum (or maximum) costs, we'll set the derivative equal to zero.

$$C(x) = 8 / \sqrt{\left(\frac{1}{2}\right)^2 + X^2} + (15 - 5x)$$

$$C'(x) = 8 \cdot \frac{1}{2} \left(x^2 + \frac{1}{4}\right)^{-1/2} (2x) - 5$$

$$= \frac{8x}{\left(x^2 + \frac{1}{4}\right)^{1/2}} - 5$$

Then, set derivative equal to zero...

$$\frac{8x}{\sqrt{x^2 + \frac{1}{4}}} - 5 = 0$$

$$\sqrt[5]{x^2 + \frac{1}{4}} = 8x$$

$$25x^2 + \frac{25}{4} = 64x^2$$

$$25 = 156x^2 \quad \text{x is distance and can't be negative}$$

$$x = \sqrt{\frac{25}{156}} = 40 \text{ miles downstream}$$

Quick check:

$$C(.40) = (.41 \text{ miles})(8) + (2.6 \text{ miles})(5)$$
water land
$$= 3.28 + 13 = 16.28 \quad \text{Minimum cost}$$

$$C(0) = (.5 \text{ miles})(8) + (3 \text{ miles})(5)$$

4 + 15 = 19

$$C(3) = (3.04 \text{ miles})(8) + (0 \text{ miles})(5)$$

24.33 + 0 = 24.33

Entirely under This would be water... This would be the most expensive!

$$C(.5) = (.71 \text{ miles})(8) + (2.5 \text{ miles})(5)$$

 $5.68 + 12.5 = 18.18$

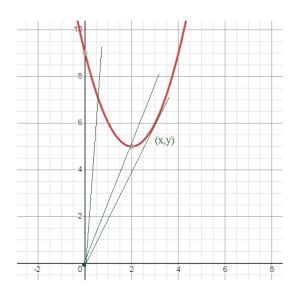
If the cable went a little further downstream it would be more expensive!

$$C(.3) = (.58 \text{ miles})(8) + (2.7)(5)$$

 $4.66 + 13.5 = 18.16$
If the cable was further upstream, it

would also be more expensive!

Step 1: Draw a diagram and outline the question



Step 2: Develop an equation...

We're trying to minimize the slope...

slope
$$m = \frac{y - 0}{x - 0} = \frac{y}{x} \implies \frac{x^2 - 4x + 9}{x}$$

To find the minimum slope, we'll take the derivative and set equal to 0

$$m = x - 4 + \frac{9}{x}$$

$$m' = 1 - 9x^{-2}$$

$$0 = 1 + \frac{9}{x^2}$$
 $x = -6$ or 3

$$x = -3$$
 or 3

(3, 6) would produce a line with minimum slope

(-3, 30) would obviously produce a steeper slope..

Note: derivative is undefine at x = 0..

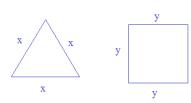
slope of line from (0, 0) to (0, 9) is undefined!!

19) A math decorator wants to make two ornaments with a 12-inch wire.

One ornament will be shaped like a square; the other will be an equilateral triangle.

Where should the decorator split the wire to make the largest ornaments (by area) possible? Or, the smallest ornaments (by area)?

Step 1: Create diagram and label variables



Step 3: Use derivative to find extreme values

$$A(x) = \frac{9^{x^2}}{16} - \frac{9}{2}x + 9 + \frac{x^2 \sqrt{3}}{4}$$

$$A'(x) = \frac{9}{8}x + \frac{9}{2} + \frac{\sqrt{3}x}{2}$$

Set derivative equal to zero

$$\frac{9}{2} = \frac{9}{8}x + \frac{\sqrt{3}x}{2}$$
 $x = 2.26$

The dimensions of the square are 1.3 x 1.3..

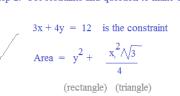
1.69 square inches

And, the lengths of the sides of the equilateral triangle are 2.26...

2.21 square inches

Total area: 3.9 inches.. MINIMUM!!

Step 2: Use restraints and question to make optimization equation.





Then, write function in one variable..

$$y = \frac{12 + 3x}{4}$$

$$A(x) = \left(\frac{12 + 3x}{4}\right)^2 + \frac{x^2 \sqrt{3}}{4}$$

Check and confirm:

Let's look at the extreme possibility....

All wire goes to the square: each side is 3 => area is 9

$$A(0) = 9$$
 MAXIMUM!!

All wire goes to the triangle: each side is 4 \implies area is $4\sqrt{3}$

$$A(4) = 6.92$$

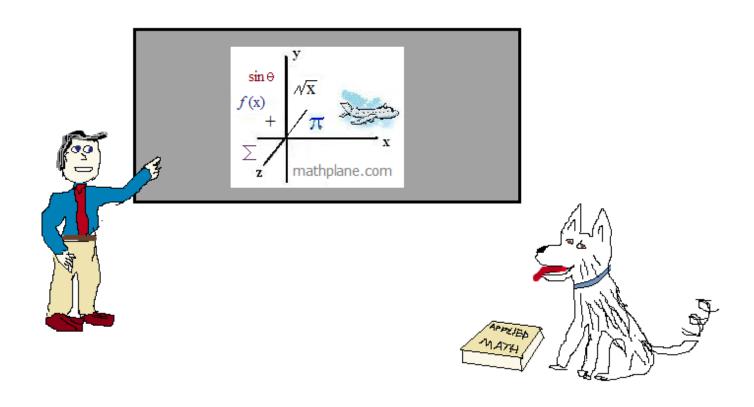
Other tests: x = 2.3 ---> triangle has sides 2.3 (area 2.29) 5.18 square has sides 1.7 (area 2.89)

$$x = 2.2$$
 ---> triangle has sides 2.2 (area 2.09) square has sides 1.35 (area 1.83)

Thanks for visiting. (Hope it helps!)

If you have questions, suggestions, or requests, let us know.

Cheers



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