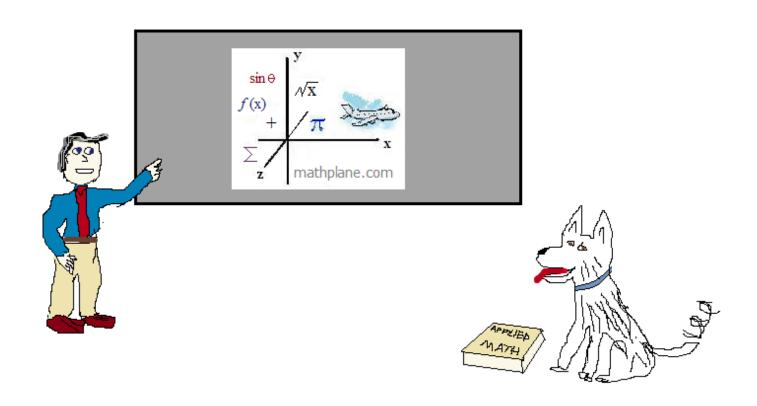
# Additional Derivatives: Trigonometry, Logarithms, and Exponents

Formulas, Examples, and Practice Exercises (with Solutions)



# Natural Logarithms

Definitions:

$$\frac{d}{dx} \left[ \ln x \right] = \frac{1}{x}$$

 $\frac{d}{dx}$   $[\ln x] = \frac{1}{x}$  If *u* is a differentiable function of *x*, then

$$\frac{d}{dx} [\ln u] = \frac{1}{u} \frac{du}{dx}$$

What does it mean? The derivative of a natural logarithm is 'the derivative of the function' 'the function

Examples:  $f(x) = \ln(2x^2 + 4)$ 

$$u = 2x^2 + 4$$

(using the above definition)

$$\frac{du}{dx} = 4x$$

$$f'(x) = \frac{\text{'Derivative of function'}}{\text{'original function'}} = \frac{4x}{(2x^2 + 4)} = \frac{2x}{x^2 + 2}$$

$$\frac{d}{dx} \left[ \ln (2x^2 + 4) \right] = \frac{1}{2x^2 + 4} (4x)$$
$$= \frac{2x}{x^2 + 2}$$

$$g(x) = \ln \sqrt{x+1}$$

"original function" :  $\sqrt{x+1}$ 

"derivative of the function":  $\frac{1}{2} (x+1)^{-1/2} = \frac{1}{2\sqrt{x+1}}$ 

$$g'(x) = \frac{\text{'derivative'}}{\text{'original'}} = \frac{\frac{1}{2\sqrt{x+1}}}{\sqrt{x+1}} = \frac{1}{2(x+1)}$$

#### Trig Functions

Definitions:

$$\frac{d}{dx}\sin u = \cos u \, \frac{du}{dx}$$

$$\frac{d}{dx}\cos u = -\sin u \frac{du}{dx}$$

$$\frac{d}{dx}\sin u = \cos u \frac{du}{dx} \qquad \qquad \frac{d}{dx}\cos u = -\sin u \frac{du}{dx} \qquad \qquad \frac{d}{dx}\tan u = \sec^2 u \frac{du}{dx}$$

$$\frac{d}{dx}\csc u = -\csc u \left(\cot u\right) \frac{du}{dx} \qquad \frac{d}{dx}\sec u = \sec u \left(\tan u\right) \frac{du}{dx} \qquad \frac{d}{dx}\cot u = -\csc^2 u \frac{du}{dx}$$

$$\frac{d}{dx}$$
 sec $u = \sec u (\tan u) \frac{du}{dx}$ 

$$\frac{d}{dx}\cot u = -\csc^2 u \frac{du}{dx}$$

Examples:

$$f(x) = \cos 3x^2$$

"function" = 
$$3x^2$$

$$f'(x) = -\sin(3x^2)(6x) = -6x \sin(3x^2)$$

"derivative of the function" = 6x

Derivatives: Absolute Value and Exponents

## Absolute Value Rule

Definition:

If y = |u|, where u is a differentiable function of x, then

$$\frac{d}{dx}[|u|] = \frac{u}{|u|}\frac{du}{dx}$$

wherever  $u(x) \neq 0$ 

What does it mean?

If you have an equation inside an absolute value, then the derivative is:

equation with out the absolute value equation with the absolute value (derivative of equation)

(and, no zeros in the denominator)

Example:  $f(x) = |4 - x^2|$ 

$$f'(x) = \frac{4-x^2}{|4-x^2|} (-2x)$$

$$f'(x) = (1)(-2x) = -2x$$
 when  $4 - x^2 > 0$ 

$$f'(x) = (-1)(-2x) = 2x$$
 when  $4 - x^2 < 0$ 

And, the derivative does not exist at  $x = \pm 2$ 

#### **Exponential Functions**

Definitions:

$$\frac{d}{dx} [e^{x}] = e^{x}$$

$$\frac{d}{dx} [a^{x}] = a^{x} (\ln a)$$

$$\frac{d}{dx} [e^{u}] = e^{u} \frac{du}{dx}$$

$$\frac{d}{dx} [a^{u}] = a^{u} (\ln a) \frac{du}{dx}$$

What does it mean?

The derivative of 'e to an exponent' is "e to the exponent times the derivative of the exponent."

The derivative of 'number to an exponent' is "number to an exponent times ln(number) times the derivative of the exponent."

Reminder: 
$$e \approx 2.718$$
  
 $\ln(e) = \log_e e = 1$   
 $\ln(4) = \log_e 4 = \text{(approx.) } 1.386$ 

Examples:

$$f(x) = e^{3x-1}$$
  
 $f'(x) = e^{3x-1}(3) = 3e^{3x-1}$ 

$$g(x) = 10^{x^2}$$
  
 $g'(x) = 10^{x^2} \ln(10) (2x)$ 

## Derivatives of Trig Functions

Examples:

$$g(x) = \sin \sqrt{2x}$$

function:  $\sqrt{2x}$ 

derivative of the function:  $\frac{1}{2}(2x)^{\frac{-1}{2}}(2) = \frac{1}{\sqrt{2x}}$ 

$$g'(x) = \cos \sqrt{2x} \left\langle \frac{1}{\sqrt{2x}} \right\rangle = \frac{\cos \sqrt{2x}}{\sqrt{2x}}$$

$$h(x) = \sec^{3}(2x)$$
 Let  $u = 2x$   
 $u' = 2$ 

$$h(x) = \sec(u)^3$$

 $h'(x) = 3\sec(u)^{2} \cdot \sec(\tan u)u'$  $= 3\sec(2x)^{2} \cdot \sec(2x)\tan(2x)(2)$ 

 $= 6\tan(2x)\sec^3(2x)$ 

Note: according to the power rule,  $derivative of [sec(u)]^3$ 

is  $3[sec(u)]^2 \cdot ("derivative of sec(u)")$ 

Find the relative extrema of  $f(x) = \sin 2x + 4$  on the interval [0, 2 T]

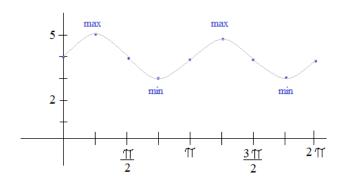
Find f'(x): cos(2x)(2) + 0 = 2cos(2x)

To find the max/min, set f'(x) = 0

$$2\cos(2x) = 0$$

$$cos(2x) = 0$$

$$x = \frac{1}{4} \quad \frac{311}{4} \quad \frac{511}{4} \quad \frac{711}{4}$$



Also, f''(x) = 0 will help identify concavity and points of inflection.

Find derivative of 
$$2\cos(2x)$$
:  $2 \cdot [-\sin(2x)(2)] = -4\sin(2x)$ 

To find points of inflection, set second derivative equal to zero.

$$-4\sin(2x) = 0$$

$$\sin(2x) = 0$$
 points of inflection at  $x = 0$ ,  $\frac{1}{2}$ ,  $\frac{1}{2}$ ,  $\frac{3}{2}$ 

# Derivatives: Natural Logarithms

Example: 
$$y = xe^2 - e^X$$
 Find y'

(product rule)

$$y' = (1)e^2 + (0)e^2(x) - e^X$$

$$\mathbf{v'} = e^2 - e^{\mathbf{X}}$$

derivative of  $e^{u} = \text{"derivative of u"} \cdot e^{u}$ 

# Example: $y = \ln \frac{1}{x}$ Find dy/dx

method 1:

$$\frac{dy}{dx} = \frac{-1(x)^{-2}}{\frac{1}{x}} = \frac{x}{-x^2} = \frac{1}{x}$$

derivative of ln: "derivative of equation" requation"

method 2: (applying log rules)

$$y = \ln(x)^{-1}$$

 $y = -\ln(x)$  (logarithm power rule)

$$\frac{dy}{dx} = \frac{-1}{x}$$

## Example: "The speed of a rumor"

A rumor can be modeled by the function  $p(t) = \frac{340}{1+2^{4-t}}$ 

$$p(t) = \frac{340}{1 + 2^{4-t}}$$

where t is time (hours) and p(t) is the number of people who know about the rumor

a) How many students originally heard the rumor?

$$p(0) = \frac{340}{1+2^{4-0}} = \frac{340}{17} = 20 \text{ students}$$

t	0	1	2	3	4	5	6
p(t)	20	38	68	113	170	227	272

b) How fast is the rumor spreading after 4 hours?

Find p'(t) to find the rate of change.

Using Quotient rule:

$$p'(t) = \frac{0 - 2^{4-t} (\ln 2)(-1)(340)}{(1 + 2^{4-t})^2} \qquad \text{Then, } p'(4) = \frac{0 - 2^0 (\ln 2)(-340)}{(1 + 2^0)^2} = \frac{(\ln 2)(340)}{4} = 58.9$$

Approximately, 59 students/hour

#### Derivatives: More Examples

Example: 
$$\sin(x) = e^y$$
 Find  $\frac{dy}{dx}$ 

Method 1: implicit differentiation

$$cos(x) = e^{y} \frac{dy}{dx}$$

$$\frac{dy}{dx} = \frac{\cos(x)}{e^y}$$

$$sin(x) = e^{y}$$

$$\frac{dy}{dx} = \frac{\cos(x)}{\sin(x)} = \cot(x)$$

Method 2: logarithm properties

Convert exponential into logartihm form

$$y = \ln(\sin(x))$$

$$\frac{dy}{dx} = \frac{\cos(x)}{\sin(x)} = \cot(x)$$

Example:  $y = \log_{6}(3x)$ 

Method 1: implicit differentiation

$$6^y = 3x$$

$$\ln(6) \cdot 6^{9} \frac{dy}{dx} = 3$$

$$\frac{dy}{dx} = \frac{3}{\ln(6) \cdot 6^{y}}$$

$$\frac{dy}{dx} = \frac{3}{\ln(6) \cdot (3x)}$$

ln(6) • 6<sup>5x</sup> • 5

Method 2: Apply the formula

$$y = \log_{6}(3x)$$

$$\frac{dy}{dx} = \frac{\text{"Derivative"}}{\text{"In of the base" "itself"}}$$

$$\frac{dy}{dx} = \frac{3}{\ln(6) \cdot (3x)}$$

Example: 6<sup>5x</sup>

Method 1: Apply formula

Method 2: Use Logrithmic differentiation

$$y = 6^{5x}$$

$$\ln y = \ln 6^{5x}$$

$$\ln y = 5x(\ln 6)$$



derivative of both sides 
$$\frac{1}{y} \frac{dy}{dx} = 5 \ln 6$$

$$\frac{dy}{dx} = \ln 6 \cdot 5 \cdot y$$

Example: 
$$ln\left(\frac{x^2\sqrt{x^2+9}}{\sin 2x}\right)$$

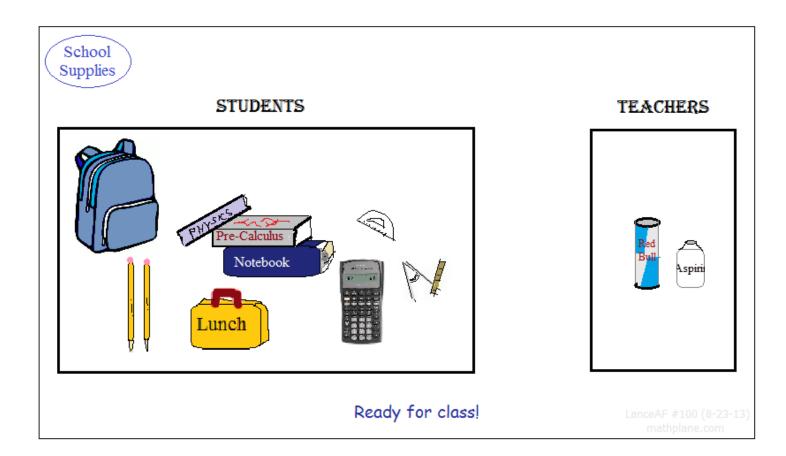
Utilize log properties...

"In of the base" "itself" "derivative"

$$lnx^2 + \frac{1}{2}ln(x^2 + 9) - lnsin2x$$

$$\frac{2x}{x} + \frac{1}{2} \frac{(2x+0)}{(x^2+9)} - \frac{2\cos 2x}{\sin 2x}$$

$$\frac{2}{x} + \frac{x}{(x^2 + 9)} - 2\cot(2x)$$



# Practice Exercises-→

# I. Trigonometry:

a) 
$$f(x) = 2x(\cos x)$$

b) 
$$y = \tan^4 (3 + 4x)$$

c) 
$$g(x) = \frac{1 - \sin x}{1 + \sin x}$$

# II. Logarithms:

a) 
$$y = \ln(x^2)$$

b) 
$$h(x) = \frac{\ln x}{x^2}$$

c) 
$$f(x) = \ln \sqrt{x^2 - 4}$$

# III. Exponents:

a) 
$$y = x^2 e^x$$

b) 
$$y = 3^{x-1}$$

$$c) f(x) = 4e^{2x}$$

## IV: More Questions

a) Find the 1st and 2nd derivatives of the following:

$$sin^2x \hspace{1cm} sin(x^2\,)$$

$$\sin \sqrt{1+x^2}$$

b) 
$$f(x) = 2\cos^3(\frac{3x}{4} + \frac{11}{12})$$
  
 $f'(\frac{1111}{9}) =$ 

c) 
$$y = e^{X}(\sin x + \cos x)$$

$$\frac{dy}{dx} =$$

d) If  $y = (\cos x)(\sin x)$ , what is the slope of the graph at  $\frac{1}{3}$ 

e)  $y = x^n + n^x$ find dy/dx

f) Find the equation of the line tangent to 
$$y = \frac{e^X}{2x+1} \qquad @x = 0$$

$$y = \frac{e^X}{2x+1} \quad @x =$$

g) Find the equation of the line tangent to 
$$f(x) = \cos^2(2x^3)$$
 @  $x = \frac{1}{3}$ 

h) 
$$y = \sin(x^2)\cos(y)$$
  $dy/dx =$ 

i) 
$$y = \sec^2(5x)$$
  $y' =$ 

j) 
$$y = 5^{(2x-3)}$$
  $dy/dx =$ 

k) y = ln(cos2x) find the first derivative.

V. Derivatives of inverses

a) If 
$$f(x) = x^3 + x^2 + x + 3$$
 and  $g(x) = f^{-1}(x)$ 

what is the value of g'(6)?

b) g is differentiable and  $g(x) = f^{-1}(x)$  for all x

$$f(-4) = 12$$
  $f(9) = -4$   $f'(4) = -6$   $f'(9) = 3$ 

$$f'(4) = -$$

$$f'(9) = 3$$

what is g'(-4)?

- a) 1/3
- b) -1/4
- c) 1/9
- d) -1/6
- e) need more information
- c) Find the derivative of  $3\cos^{-1}(\frac{x}{2})$

# I. Trigonometry:

a) 
$$f(x) = 2x(\cos x)$$

(product rule) 
$$u = 2x$$
  
 $u' = 2$   
 $v = \cos x$   
 $v' = -\sin x$ 

$$f'(x) = 2 \cdot (\cos x) + (-\sin x) \cdot 2x$$
$$= 2\cos x - 2x(\sin x)$$
$$= 2(\cos x - x\sin x)$$

## II. Logarithms:

a) 
$$y = \ln(x^2)$$

derivative of natural

log:

"derivative of funtion"
"original function"

$$u = x^2$$
$$u' = 2x$$

$$y' = \frac{2x}{x^2} = \boxed{\frac{2}{x}}$$

# III. Exponents:

a) 
$$y = x^2 e^x$$

(product rule)

$$u = x^{2}$$

$$u' = 2x$$

$$v = e^{x}$$

$$v' = e^{x}$$

b) 
$$y = \tan^4 (3 + 4x)$$
  
 $= [\tan (3 + 4x)]^4$   
(power rule)  $u = \tan (3 + 4x)$   
 $u' = \sec^2 (3 + 4x)(4)$ 

$$\frac{dy}{dx} = 4\tan^3 (3+4x) \cdot [\sec^2 (3+4x)(4)]$$
$$= 16\tan^3 (3+4x) \sec^2 (3+4x)(4)$$

b) 
$$h(x) = \frac{\ln x}{x^2}$$

$$\begin{array}{ll} \text{(quotient rule)} & u = lnx \\ u' = 1/x \\ v = x^2 \\ v' = 2x \end{array}$$

$$h'(x) = \frac{\frac{1}{x} \cdot x^2 - 2x(\ln x)}{(x^2)^2}$$

$$= \frac{x - 2x(\ln x)}{x^4}$$

$$= \frac{1 - 2(\ln x)}{x^3}$$

$$a = 3$$

$$u = x - 1$$

$$u' = 1$$

$$y' = 3^{x-1} (\ln 3)(1)$$
  
=  $\ln 3(3^{x-1})$ 

c) 
$$g(x) = \frac{1 - \sin x}{1 + \sin x}$$

(quotient rule) 
$$u = 1 - \sin x$$
  
 $u' = -\cos x$   
 $v = 1 + \sin x$   
 $v' = \cos x$ 

$$g'(x) = \frac{(-\cos x)(1 + \sin x) - (\cos x)(1 - \sin x)}{(1 + \sin x)^2}$$

$$= \frac{-\cos x - \cos x \sin x - \cos x + \cos x \sin x}{(1 + \sin x)^{2}}$$

$$= \frac{-2\cos x}{(1 + \sin x)^{2}}$$

c) 
$$f(x) = \ln \sqrt{x^2 - 4}$$

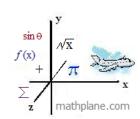
$$u = \sqrt{x^{2} - 4}$$

$$\frac{du}{dx} = \frac{1}{2} (x^{2} - 4)^{2} (2x) = \frac{x}{\sqrt{x^{2} - 4}}$$

$$f'(x) = \frac{\frac{x}{\sqrt{x^2 - 4}}}{\sqrt{x^2 - 4}} = \frac{x}{x^2 - 4}$$

c) 
$$f(x) = 4e^{2x}$$
  
 $f'(x) = 4 [e^{2x}](2)$ 

$$f'(x) = 4 [e^{2x}](2)$$
  
=  $8e^{2x}$ 



a) Find the 1st and 2nd derivatives of the following:

2cos2x

$$\sin^{2} x \qquad \qquad \sin(x^{2})$$

$$(\sin x)^{2} \qquad \qquad y' = \cos(x^{2}) \cdot 2x$$

$$y' = 2(\sin x)^{1} \cdot \cos x \qquad \qquad = 2x \cos(x^{2})$$

$$= \sin 2x \qquad \qquad y'' = 2\cos 2x$$

$$\sin(x^{2})$$

$$y' = \cos(x^{2}) \cdot 2x$$

$$y'' = 2\cos(x^{2}) + -\sin(x^{2}) \cdot 2x \cdot 2x$$

$$= 2\cos(x^{2}) + -\sin(x^{2}) \cdot 2x \cdot 2x$$

$$= 2\cos(x^{2}) - 4x^{2}\sin(x^{2})$$

$$y'' = 2[\cos(x^{2}) - 4x^{2}\sin(x^{2})]$$

$$y'' = 2\cos(x^{2}) - 4x^{2}\sin(x^{2})$$

$$= 2\cos(x^{2}) - 4x^{2}\sin(x^{2})$$

$$= 2\cos(x^{2}) - 4x^{2}\sin(x^{2})$$

b) 
$$f(x) = 2\cos^3\left(\frac{3x}{4} + \frac{17}{12}\right)$$
  
 $f'(\frac{1177}{9}) =$   
 $f(x) = 2\left[\cos\left(\frac{3x}{4} + \frac{17}{12}\right)\right]^3$   
 $f'(x) = 6\cos\left(\frac{3x}{4} + \frac{17}{12}\right)^2 \cdot \left[-\sin\left(\frac{3x}{4} + \frac{17}{12}\right) \cdot \frac{3}{4}\right]$   
 $f'(\frac{1177}{9}) = 6\cos^2\left(\frac{3377}{36} + \frac{17}{12}\right) \cdot \left[-\sin\left(\frac{3377}{36} + \frac{17}{12}\right) \cdot \frac{3}{4}\right]$   
 $6 \cdot (-1)^2 \cdot 0 \cdot \frac{3}{4} = 0$ 

d) If 
$$y = (\cos x)(\sin x)$$
, what is the slope of the graph at  $\frac{1}{3}$ 

$$y' = (-\sin x)(\sin x) + (\cos x)(\cos x)$$
(product rule)
at  $\frac{1}{3}$  slope is  $(-\sin \frac{1}{3})(\sin \frac{1}{3}) + (\cos \frac{1}{3})(\cos \frac{1}{3})$ 

$$-\frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{2} + \frac{1}{2} \cdot \frac{1}{2} = \frac{-1}{2}$$

$$\sin \sqrt{1 + x^{2}}$$

$$y' = \cos(\sqrt{1 + x^{2}}) \cdot \frac{1}{2} (1 + x^{2})^{\frac{-1}{2}} \cdot 2x$$

$$= \frac{x \cos(\sqrt{1 + x^{2}})}{\sqrt{1 + x^{2}}}$$

$$y'' = 1 \cdot \frac{\cos(\sqrt{1 + x^{2}}) - x \cdot \left(-\sin(\sqrt{1 + x^{2}}) \cdot \frac{1}{2} (1 + x^{2})^{\frac{-1}{2}} \cdot 2x\right)}{\left(\sqrt{1 + x^{2}}\right)^{2}}$$

$$= \frac{\cos(\sqrt{1 + x^{2}}) + x^{2} \sin(\sqrt{1 + x^{2}}) \cdot (1 + x^{2})^{\frac{-1}{2}}}{1 + x^{2}}$$

$$\frac{\cos(\sqrt{1 + x^{2}}) + \frac{x^{2} \sin(\sqrt{1 + x^{2}})}{\sqrt{1 + x^{2}}}}{1 + x^{2}}$$

Use the product rule:
$$\frac{dy}{dx} = \begin{cases} y' = e^{X}(\sin x + \cos x) + e^{X}(\cos x + (-\sin x)) \\ u' \quad v \quad u \quad v' \end{cases}$$

$$e^{X}\sin x + e^{X}\cos x + e^{X}\cos x - e^{X}\sin x$$

$$2e^{X}\cos x$$

$$y = \frac{e^{X}}{2x+1} \qquad @x = 0$$

The coordinate of the point is 
$$y = \frac{e^0}{2(0)+1} = \frac{1}{1} = 1$$

The slope at that point is

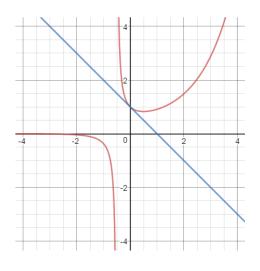
$$y-1 = -1(x+0)$$
  $y = -x+1$ 

product rule

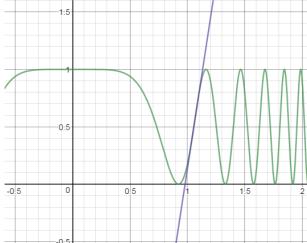
trig derivatives

implicit differentiation

chain rule



# g) Find the equation of the line tangent to $f(x) = \cos^2(2x^3)$ @ $x = \frac{1}{3}$



h)  $y = \sin(x^2)\cos(y)$ 

$$(1)\frac{dy}{dx} = \cos(x^2) \cdot 2x \cdot \cos(y) + (-\sin y \frac{dy}{dx}) \cdot \sin(x^2)$$

dy/dx =

$$\frac{dy}{dx} + \sin(x^2)\sin y \frac{dy}{dx} = \cos(x^2) \cdot 2x \cdot \cos(y)$$

$$\frac{dy}{dx} = \frac{\cos(x^2) \cdot 2x \cdot \cos(y)}{1 + \sin(x^2)\sin y}$$

j) 
$$y = 5^{(2x-3)}$$
  $dy/dx =$ 

$$\frac{dy}{dx} = \ln 5 \cdot 5^{(2x-3)} \cdot 2$$

"In of the base" "itself" "derivative of the exponent"

$$\left[\cos(2x^3)\right]^2$$

$$2 \left[\cos(2x^3)\right]^1 \cdot -\sin(2x^3) \cdot 6x^2$$

at 
$$x = \frac{1}{3}$$
  $f'(x) = 6.533$ 

and, at 
$$\frac{1}{3}$$
  $f(x) = .441$ 

slope is 6.533

the point is 
$$(\frac{1}{3}, .441)$$

$$y - .441 = 6.533(x - \frac{1}{3})$$

i) 
$$y = \sec^2(5x)$$
  $y' =$ 

$$2\sec(5x) \cdot \sec(5x)\tan(5x) \cdot 5$$

power rule chain rule trig derivatives

$$10\sec^2{(5x)}\tan{(5x)}$$

k)  $y = \ln(\cos 2x)$  find the first derivative.

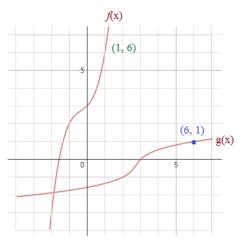
"derivative"

$$y' = \frac{-\sin(2x) \cdot 2}{\cos(2x)} = \boxed{-2\tan(2x)}$$

# V. Derivatives of inverses

a) If 
$$f(x) = x^3 + x^2 + x + 3$$
 and  $g(x) = f^{-1}(x)$ 

what is the value of g'(6)?



Inverses reflect over the line y = x, and the coordinates are reversed...

b) g is differentiable and  $g(x) = f^{-1}(x)$  for all x

$$f(-4) = 12$$
  $f(9) = -4$ 

$$f'(4) = -6$$

$$f'(9) = 3$$

what is g'(-4)?

c) 1/9

d) -1/6

e) need more information

#### SOLUTIONS

$$g'(x) = \frac{1}{f'(y)}$$

Slope at (6, 1) is the reciprocal of the slope at (1, 6)

For y = 6,

$$6 = x^3 + x^2 + x + 3, \qquad x = 1$$

So, the slope at (1, 6) will be the reciprocal of the slope at (6, 1)!

$$f'(x) = 3x^2 + 2x + 1 + 0$$

then, 
$$f'(1) = 3 + 2 + 1 = 6$$

therefore, 
$$g'(6) = \frac{1}{f'(1)} = \frac{1}{6}$$

g(x) and f(x) are inverses...

So, if f(9) = -4, then g(-4) must equal 9.

Then, f'(9) = 3... therefore, the slope of the inverse g'(-4) = 1/3

c) Find the derivative of  $3\cos^{-1}(\frac{x}{2})$ 

since 3 is a constant, we'll ignore that for now...

$$\cos^{-1}\left(\frac{x}{2}\right) = y$$

$$\cos y = \frac{x}{2}$$

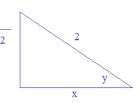
using implicit diff...

-siny 
$$\frac{dy}{dx} = \frac{1}{2}$$

$$\frac{dy}{dx} = \frac{1}{2}$$
 (-cscy)

$$\frac{dy}{dx} = \frac{1}{2} \cdot \frac{-2}{\sqrt{4 - x^2}}$$

simplify and bring in the constant



$$\frac{dy}{dx} = \frac{-3}{\sqrt{4 - x^2}}$$

Thanks for visiting. (Hope it helped!)

If you have questions, suggestions, or requests, let us know.

# Cheers

Also, at Mathplane *Express* for mobile at Mathplane.ORG And, store at TeachersPayTeachers...

