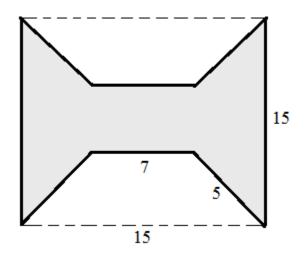
Geometry: Area and Perimeter of Complex Shapes

Notes, Examples, and Practice Quiz (with Solutions)



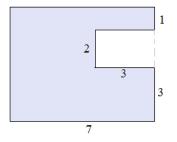
Topics include sector area, segments, special quadrilaterals, ratios, regular polygons, Heron's Formula, and more.

Area and Perimeter of Polygons

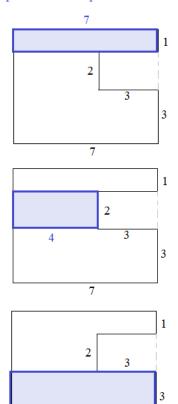
Example: Find the area and perimeter of the (concave) polygon.

Since this is not an ordinary shape, a basic formula will not work. There are 2 approaches to finding the area...

Method 1: "Add the parts"



Step 1: Divide into parts and label



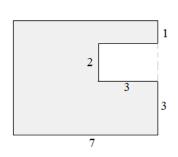
Step 2: Find area of each part area of rectangle: (length)(width)

areas:
$$7 \times 1 = 7$$

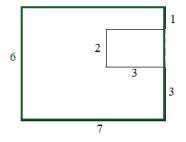
 $4 \times 2 = 8$
 $7 \times 3 = 21$

Step 3: Add the areas

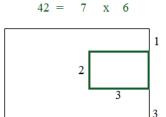
$$7 + 8 + 21 = 36$$
 square units



Method 2: "Cut out piece(s)"



Step 1: find the area of the entire rectangle Area = length x width



Step 2: cut out piece(s)

Area = length x width $6 = 3 \times 2$

Step 3: subtract

42 sq. units - 6 sq. units = 36 square units

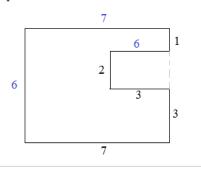
To find the perimeter, carefully add up all the sides:

"outer" sides: 7 + 6 + 7 + 1 + 3 = 24

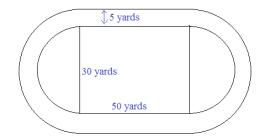
"inner" sides:

6+2+3 = 11

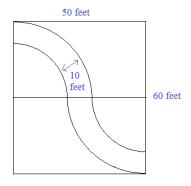
total perimeter: 35 units



Example: Find the distance of the outer track:



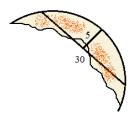
Example: The city wants to pave <u>both</u> sides of this winding road. If the road is 10 feet wide, how long will this stretch of side pavement be?



Example: At a pizzeria, a waiter and customer disagreed about a pizza order.

Unfortunately, the customer had eaten most of the pizza.

However, the math chef came out and measured the remaining portion and determined the size (diameter) of the original pizza.

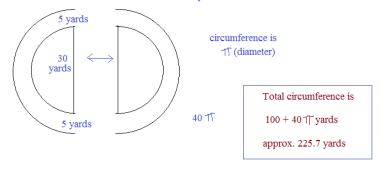


What was the size of the original, full pizza?

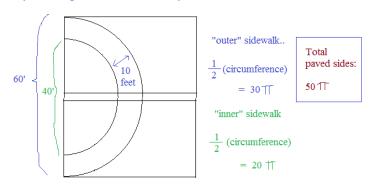
The distance of the OUTER track is the lengths of 2 line segments and the circumference of a circle.

The 2 straight parts of the track: 50 yards each... 100 yards total

The combined turns form a circle with diameter 40 yards

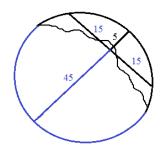


If you rearrange the arcs in the road, they form a semicircle!



Distance of midpoint of arc to the midpoint of the chord is 5 cm.

Chord measures 30 cm.



(15)(15) = (5)(X)chord-chord power theorem

$$X = 45$$

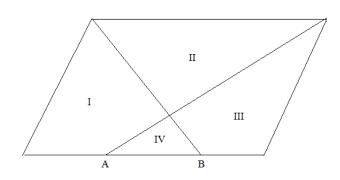
So, the diameter of the pizza is 50 cm..

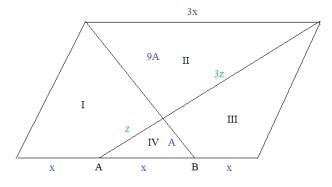
And, the area of the pizza is 625 sq cm..

Example: Given: Parallelogram and

trisection points A and B

Find the ratio of the areas of the sections I:II:III:IV





Since triangles II and IV are similar (angle-angle) and their sides are proportional with a ratio of x:3x, the ratio of the areas is 1:9

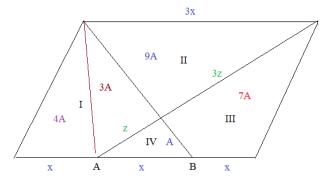
Draw an auxilary line bisecting triangle I/IV

Since triangles II and IV are proportional 3:1, we know the sides z and 3z....

9A II 3Z III III X A X B X

since triangles have same height and bases of ratio z: 3z,

the triangles are 3A: 9A



3A + A = 4A

because the triangles have the same base x and x and the same height...

Section I has an area of 4A (with a base of x)

Sections IV and III has an area of 8A because the base is 2x..

Both triangles have the same height...

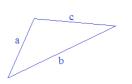
Answer: I 7A
II 9A
III 7A

IV A

The area of a triangle

Area =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

where s is the semiperimeter $s = \frac{a+b+c}{2}$



Example: Find the area of the following triangle.



Since it isn't a right triangle (and we don't know the height), and we don't know any of the angles, we'll apply Heron's Formula...

$$s = \frac{6+7+9}{2} = 12$$

(semiperimeter)

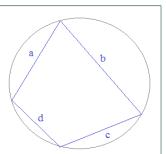
$$s = \frac{6+7+9}{2} = 11 \qquad Area = \sqrt{11(11-6)(11-7)(11-9)}$$
(seminarimeter)

Brahmagupta's Formula

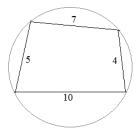
The area of a cyclic quadrilateral

Area =
$$\sqrt{(s-a)(s-b)(s-c)(s-d)}$$

where s is the semiperimeter $s = \frac{a+b+c+d}{2}$



Example: Find the area of the following quadrilateral.



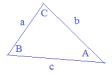
$$s = \frac{5+7+4+10}{2} = 13$$
(semiperimeter) Area = $\sqrt{(13-5)(13-7)(13-4)(13-10)}$

$$= \sqrt{1296} = 36$$

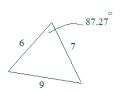
$\frac{1}{2}$ ab(sinC)

The area of a triangle when given an angle and its two adjacent sides is

Area =
$$\frac{1}{2}$$
ab(sinC)



Example: Find the area of the following triangle.



Area =
$$\frac{1}{2}$$
 (6)(7)sin(87.27)

$$= 21\sin(87.27) = 20.98$$

Example: Use Heron's Formula to find the area of the following triangles:

a)
$$s = 18$$

b)
$$s = 10$$
 c) $s = 8$

$$s = 8$$

Area =
$$\sqrt{18(8)(6)(4)}$$
 Area = $\sqrt{10(7)(4)(-1)}$ Area = $\sqrt{8(5)(3)(0)}$

Area =
$$\sqrt{10(7)(4)(-1)}$$

Area =
$$\sqrt{\frac{1}{8(5)(3)(0)}}$$

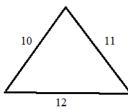
negative!!

= 58.8 (approx.)

Triangle does not exist.

It's a line segment!

Example: What are the lengths of the 3 altitudes in the triangle?

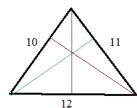


Since the area of a triangle is $\frac{1}{2}$ (base)(height)

if we can find the area, we can determine each altitude (i.e. height)

semiperimeter =
$$\frac{10 + 11 + 12}{2}$$
 = 16.5

area =
$$\sqrt{(16.5)(6.5)(5.5)(4.5)}$$
 = $\sqrt{2654}$ = 51.5



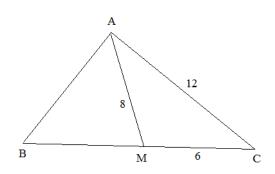
base 12:
$$51.5 = \frac{1}{2}$$
 (base)(height) \longrightarrow 103 = 12(height) 8

base 11:
$$51.5 = \frac{1}{2}$$
(base)(height) $\implies 103 = 11$ (height)

base 10:
$$51.5 = \frac{1}{2}$$
(base)(height) $\implies 103 = 10$ (height)

Triangle median theorem: A median of a triangle divides the triangle into two triangles with the same area....

Example: Find the area of triangle ABC



Using Heron's Formula, we can find the area of \(\triangle AMC \)

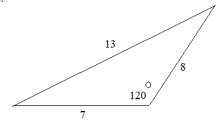
Area =
$$\sqrt{s(s-a)(s-m)(s-c)}$$

semiperimeter (s) =
$$\frac{8+12+6}{2}$$
 = 13 (half the perimeter)

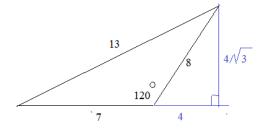
Area of
$$\triangle$$
 AMC = $\sqrt{(13)(7)(1)(5)}$ = 21.33

Therefore, the area of the triangle ABC = 2×21.33

= 42.66

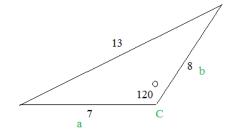


Method 1: Create a right triangle



Area =
$$1/2$$
(base)(height)
 $1/2(7)(4/\sqrt{3}) = 14/\sqrt{3}$

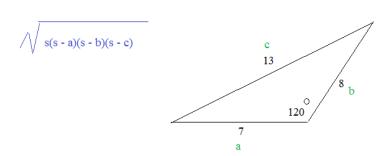
Method 2: Using $\frac{1}{2}$ (a)(b)sin(C)



Area =
$$1/2(7)(8)\sin(120^{\circ})$$

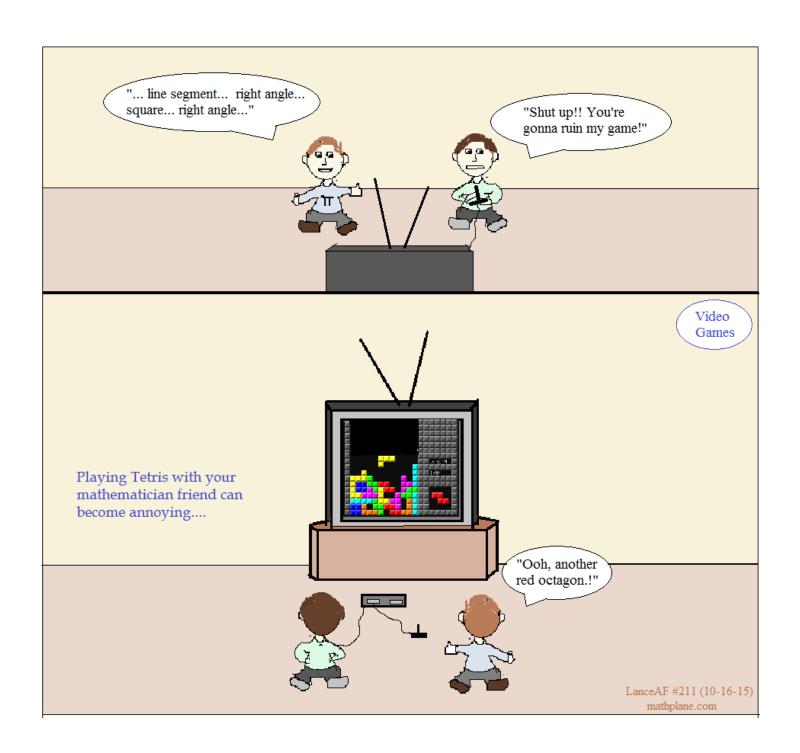
= $28\sin(120^{\circ}) = 14\sqrt{3}$

Method 3: Heron's Theorem



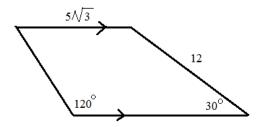
Semiperimeter (s) =
$$\frac{7+8+13}{2}$$
 = 14

Area = $\sqrt{\frac{14(1)(7)(6)}{14\sqrt{3}}}$



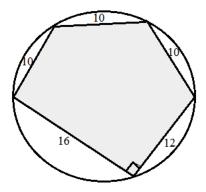
Practice Quiz-→

1) Find the perimeter and area of the quadrilateral:

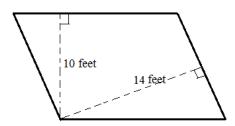


2) The pentagon is inscribed in the circle:

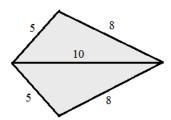
What is the area?



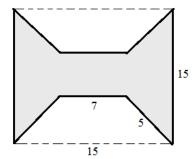
3) If the perimeter of the parallelogram is 120 feet, what is the area?



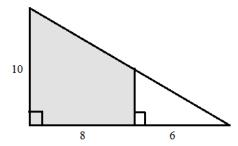
4) Find the area of the kite

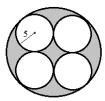


5) The shaded region is a square with 2 congruent isosceles trapezoids removed.
What is the perimeter and area of the shaded figure?



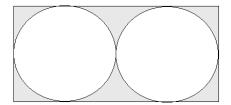
6) Determine the area and perimeter of the shaded region.





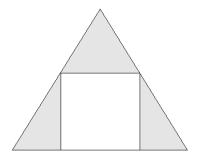
8) The radius of each tangent circle is 8.

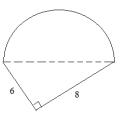
What is the shaded area?



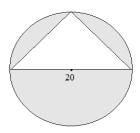
9) The figure is a square 'inscribed' in an equilateral triangle with perimeter 24

Find the shaded area...





11) Find the shaded area:

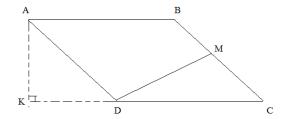


12) Parallelogram ABCD has an area of 60

M is the midpoint of BC

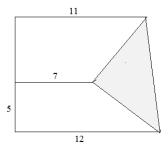
ом ⊥ вс

What is the length of $\overline{AK}\ ?$



13) The 2 trapezoids have the same areas.

What is the area of the triangle?

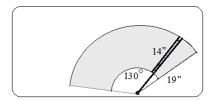


15) The plaque is a rhombus inscribed in a rectangle.

If the diagonals are 12" and 8", how much wood area is available for engraving?



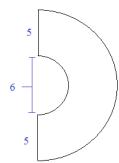
16) A windshield wiper extends 130 degrees. Using the diagram, what area of glass is cleared by the wiper?



17) A trapezoid has diagonals measuring 30 and height 18. What is the area?

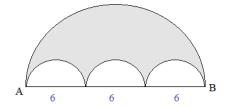
18) Find the perimeter.

Area and Perimeter of Shapes Exercise

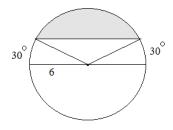


19) Length of \overline{AB} is 18.

The 3 semicircles are congruent. What is the shaded area?

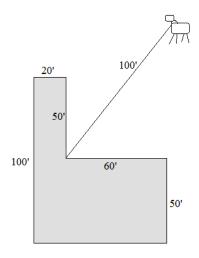


20) Find the measure of the shaded area:



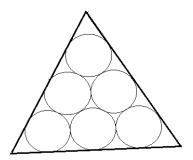
21) A cow is tethered to a 100-foot rope, attached to the inside corner of an L-shaped building (as shown in the diagram).

Find the grazing area of the cow.

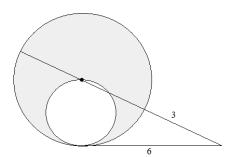


23) Each of these 6 inscribed/tangent circles are congruent with radius 8.

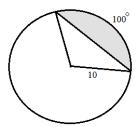
What is the perimeter of the triangle?

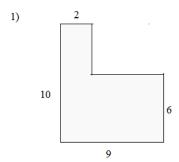


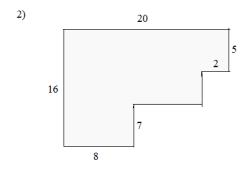
24) Can you find the shaded area?

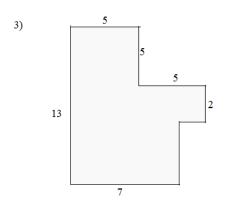


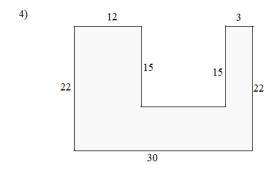
25) What is the area of the shaded segment?

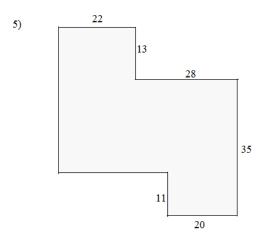


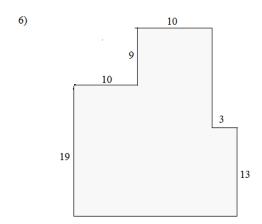


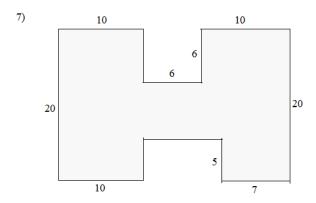


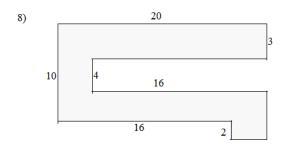


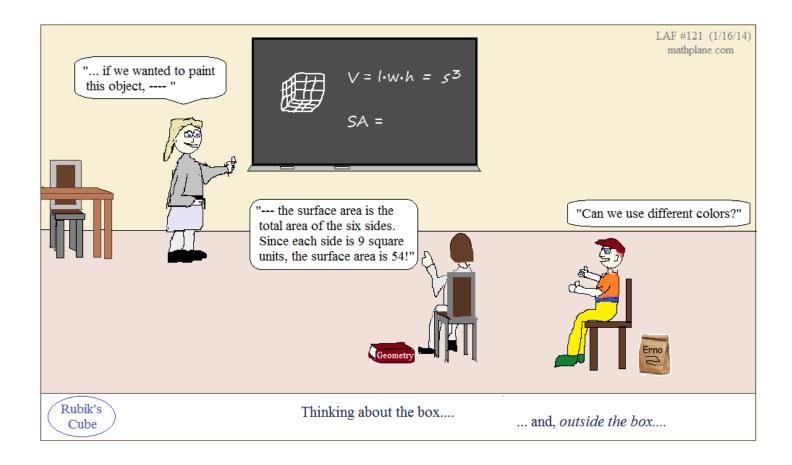








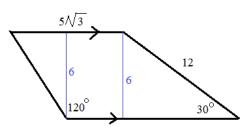




ANSWERS-→

SOLUTIONS

1) Find the perimeter and area of the quadrilateral:

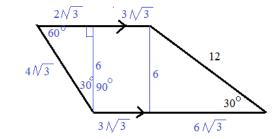


Draw 2 (congruent) altitudes, dividing figure into 3 measurable shapes...

Since the 30-60-90 right triangle has hypotenuse of 12, the opposite side is 6...

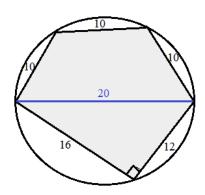
Since upper and lower base are parallel, it's a trapezoid.

Perimeter of trapezoid: $12 + 18\sqrt{3}$ area of trapezoid: $42\sqrt{3}$



2) The pentagon is inscribed in the circle:

What is the area?



Since the bottom of the pentagon is a right angle, we can divide the pentagon into 2 parts!

(triangle inscribed in a semicircle is a right triangle)

Part 2: inscribed quadrilateral --- (Brahmagupta's Formula)

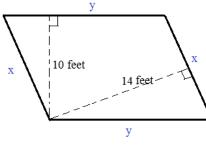
semi-perimeter (s) =
$$\frac{10 + 10 + 10 + 20}{2}$$
 = 25

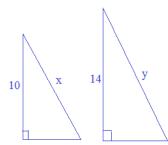
area =
$$\sqrt{(25 - 10)(25 - 10)(25 - 10)(25 - 20)}$$
 = $\sqrt{16875}$

129.9

Total area of pentagon = 225.9 square units (approximately)

3) If the perimeter of the parallelogram is 120 feet, what is the area?





According to Angle-Angle similarity theorem, the 2 right triangles are similar!

$$\frac{10}{14} = \frac{x}{y}$$

$$y = \frac{7x}{5}$$

Parallelogram: opposite angles are congruent opposite sides are congruent

$$2x + 2y = 120$$
 feet -

area = (base)(height)

=
$$(10 \text{ feet})(35 \text{ feet})$$
 = 350 square feet

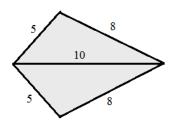
$$2x + 2(\frac{7}{5}x) = 120$$
 feet

$$\frac{10}{5}$$
x + $\frac{14}{5}$ x = 120 feet

$$x = 25$$
 feet and, $y = 35$ feet..

SOLUTIONS

4) Find the area of the kite



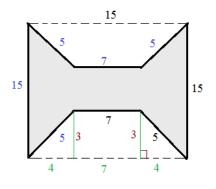
The area of a kite is 1/2(diagonal 1)(diagonal 2) However, we don't know the length of the other diagonal...

So, view this figure as 2 triangles, and use Hero's formula to solve...

semiperimeter (s) =
$$\frac{5+8+10}{2}$$
 = 11.5
area = $\sqrt{(11.5)(11.5-10)(11.5-8)(11.5-5)}$
= $\sqrt{(11.5)(1.5)(3.5)(6.5)}$ = 19.81 (approximately)
So, area of kite is 39.62 square units

The shaded region is a square with 2 congruent isosceles trapezoids removed.

What is the perimeter and area of the shaded figure?



The perimeter is the sum of all the segments:

$$5 + 7 + 5 + 15 + 5 + 7 + 5 + 15 = 64 \text{ units}$$

The area of the shaded figure = area of the square - area of 2 trapezoids

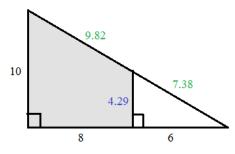
shaded area = 225 + 2(33) = 159 square units

area of square = 225 sq. units

area of trapezoid =
$$\frac{1}{2}$$
 (base1 + base2)(height)
= $\frac{1}{2}$ (15 + 7)(3) = 33

using pythagorean theorem and fact that it's isosceles, we determine the height is 3

6) Determine the area and perimeter of the shaded region.



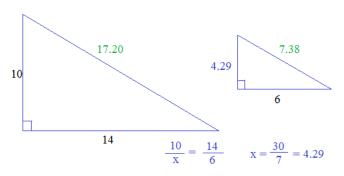
Perimeter = 9.82 + 4.29 + 8 + 10 = 32.11

Area = big triangle area - small triangle area

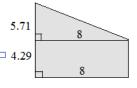
(also, area is lower rectangle + upper triangle...

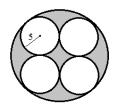
$$(8 \times 4.29) + \frac{1}{2}(8)(5.71) = 34.32 + 22.84 = 57.16$$

First, we need to find the lengths of the remaining segments. (Notice, 2 similar right triangles...)



Then, use Pythagorean Theorem to find hypotenuses..





Finding the area of each small circle is straightforward:

area of circle =
$$\prod$$
 (radius)² = 25 \prod

Therefore, total "area that will be cut out" = 100 T

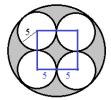
Total shaded area = $(50\sqrt{2} - 25)$

approximately 143.6 square units

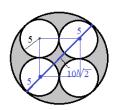
How do we find the area of the large circle? If we connect the 4 centers to each other, we

construct a square with sides 10!

SOLUTIONS







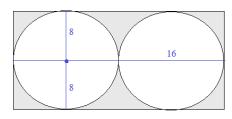
Diameter of large circle is $10 + 10 \sqrt{2}$ then, radius of large circle is $5 + 5\sqrt{2}$

area of circle =
$$\iint$$
 (radius)² = $(5 + 5\sqrt{2})^2$ \iint
area of large circle = $(25 + 50\sqrt{2} + 50)$ \iiint
= $(75 + 50\sqrt{2})$ \iiint

8) The radius of each tangent circle is 8.

What is the shaded area?

The area of the rectangle is length x width = $32 \times 16 = 512$



Then, the area of each circle is

$$\prod$$
 (radius)² =

So, the shaded area is

9) The figure is a square 'inscribed' in an equilateral triangle with perimeter 24

Find the shaded area...

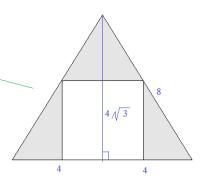
area of triangle is
$$\frac{1}{2}$$
(8)(4 $\sqrt{3}$) = $16\sqrt{3}$

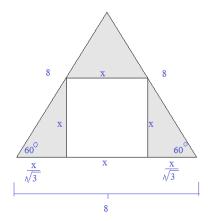
$$x + \frac{x}{\sqrt{3}} + \frac{x}{\sqrt{3}} = 8$$

$$x(1 + \frac{2}{\sqrt{3}}) = 8$$

$$x = \frac{8}{\left(1 + \frac{2}{\sqrt{3}}\right)} = 3.71$$

so, the area of the square is approx. 13.8





shaded area = triangle - square

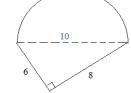
$$16\sqrt{3}$$
 — 13.8 = 13.9

10) Find the perimeter and area of the semicircle and right triangle figure:

diameter is 10 (because of Pythagorean Theorem)

Arc length of semicircle = (1/2)10

Area of semicircle = (1/2)25

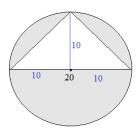


SOLUTIONS

Area and Perimeter of Shapes Exercise

Area of figure =
$$24 + 12.5$$

11) Find the shaded area:



circle area is 100 T

triangle area: 1/2(base)(height)

$$1/2(20)(10) = 100$$

height is 10, because all radii are congruent

Shaded area =
$$100 \text{ T}$$
 - 100

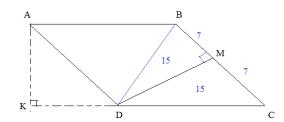
approx. 214 sq units

12) Parallelogram ABCD has an area of 60

M is the midpoint of BC

 $_{\mathrm{DM}}\perp_{\mathrm{BC}}$

What is the length of \overline{AK} ?

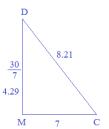


Since M is midpoint, we can divide the segments..

Then, since area of parallelogram is 60, we can draw segments to partition it ...

The area of triangle CMD is 15 and the base is 7

$$\frac{1}{2}$$
 (7)(height) = 15

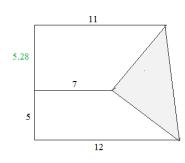


DC = 8.21... This is the base of parallelgram ABCD !!

height = 7.31

13) The 2 trapezoids have the same areas.

What is the area of the triangle?



Area of top trapezoid = $\frac{1}{2}$ h(7 + 11) Since trapezoids have same areas, $\frac{1}{2}$ (5)(7 + 12) = $\frac{1}{2}$ h(7 + 11)

$$\frac{1}{2}(5)(7+12) = \frac{1}{2}h(7+11)$$

Area of bottom trapezoid = $\frac{1}{2}$ (5)(7 + 12)

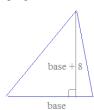
95 = 18hh = 5.28

Area of ENTIRE trapezoid =
$$\frac{1}{2}$$
 (10.28)(12 + 11) = 118.22

Area of each small trapezoid = 47.5

Therefore, area of triangle = 118.22 - 47.5 - 47.5 = 23.22

$$h = b + 8$$



Area =
$$\frac{1}{2}$$
 (base)(height)

$$=\frac{1}{2}$$
 (b)(b+8) = 90

$$= b^2 + 8b = 180$$

$$b^2 + 8b - 180 = 0$$

$$(b+18)(b-10) = 0$$

$$b = 10, -18$$

 $base = 10 inches \quad (cannot be negative!)$

then, height = 18 inches

SOLUTIONS

15) The plaque is a rhombus inscribed in a rectangle. If the diagonals are 12" and 8", how much wood area is available for engraving?



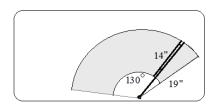
Since the rhombus is inscribed in the rectangle, the diagonals are the same lengths as the sides of the rectangle...

Area of rectangle = $(length)(width) = 12 \times 8 = 96 \text{ sq. inches}$

Area of the rhombus =
$$\frac{1}{2}$$
 d₁d₂ = $\frac{1}{2}$ (12)(8) = 48 sq. inches

The remaining wood area is 96 - 48 = 48 sq. inches...

16) A windshield wiper extends 130 degrees. Using the diagram, what area of glass is cleared by the wiper?



The "outer" sector has a radius of 19 inches.

outer area =
$$\frac{130}{360}$$
 TT $(19)^2$ = 409.5

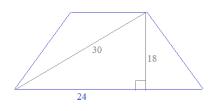
The "inner" sector has a radius of 5 inches.

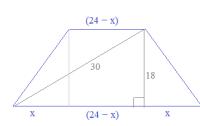
inner area =
$$\frac{130}{360}$$
 $\uparrow \uparrow$ $(5)^2$ = 28.4

shaded area is approximately 381.1 sq inches

17) A trapezoid has diagonals measuring 30 and height 18. What is the area?

Since the diagonals are 30, it must be an isosceles trapezoid... Here is a sketch..





Area =
$$\frac{1}{2}$$
 (base1 + base2)(height)
= $\frac{1}{2}$ ((24 - x) + (x + (24 - x) + x))(18)
= $\frac{1}{2}$ (48)(18) = 432

mathplane.com

SOLUTIONS

Area and Perimeter of Shapes Exercise

30°

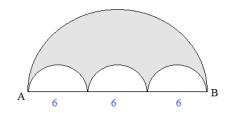
arc length of semicircle: (1/2) ↑ (diameter)

diameter of inner semicircle is 6 diameter of outer semicircle is 16

$$\left(\frac{1}{2}\right)16 \text{ Tr}^2 + \left(\frac{1}{2}\right)6 \text{ Tr}^2 + 5 + 5$$

19) Length of AB is 18.
The 3 semicircles are congruent.
What is the shaded area?

5



Area of semicircle = $(1/2) \text{ Tr (radius)}^2$

Large semicircle:
$$\left| \frac{1}{2} \right| 81 \text{ T}^2 = 40.5 \text{ T}^2$$

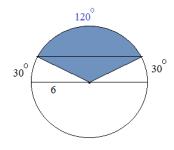
Small semicircle:
$$\left| \frac{1}{2} \right| 9 \text{ m}^2 = 4.5 \text{ m}^2$$

Shaded area:
$$40.5 \text{ T} - 3 \left(4.5 \text{ T} \right) = 27 \text{ T}$$

30°

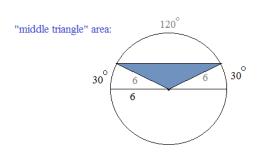
 $12 \uparrow f - 9 \sqrt{3}$

20) Find the measure of the shaded area:

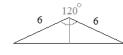


"piece of pie" sector area:

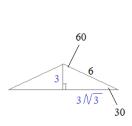
$$\frac{120^{\circ}}{360^{\circ}} \text{ (6)}^2 = 12 \text{ (7)}$$



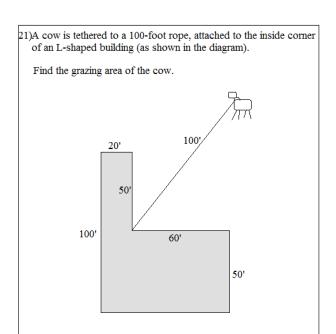
(sides are 6, because all radii are congruent)



obtuse angle is 120, because 30 + 30 + 120 = 180

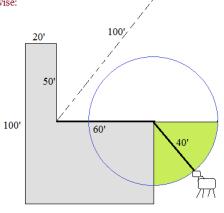


 $\frac{1}{2} (6\sqrt[3]{3})(3) = 9\sqrt[3]{3}$



Sector Area = $\frac{\text{angle measure}}{360 \text{ degrees}} \text{ Tr}^2$

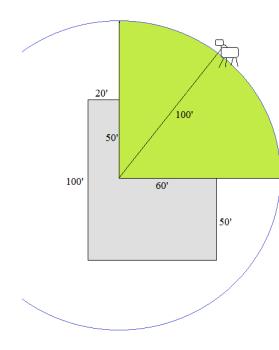
Going clockwise:



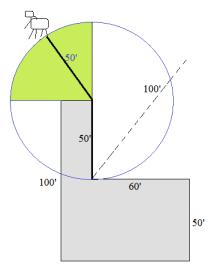
sector area: radius 40' \ominus = 90 degrees

 $\frac{90 \text{ degrees}}{360 \text{ degrees}} \text{ Tr} (40')^2 = 400 \text{ Tr} \text{ square feet}$

Going Counterclockwise:

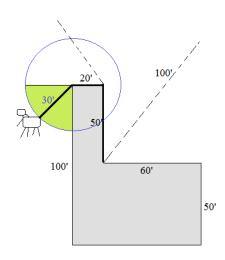


First sector area: radius 100' \bigcirc = 90 degrees



Second sector area: radius 50' \bigcirc = 90 degrees

 $\frac{90 \text{ degrees}}{360 \text{ degrees}} \text{ Tr} (50')^2 = 625 \text{ Tr} \text{ square feet}$



Third sector area: radius 30' \bigcirc = 90 degrees

 $\frac{90 \text{ degrees}}{360 \text{ degrees}} \text{ TT} (30')^2 = 225 \text{ TT} \text{ square feet}$

Total Grazing area: $3750 \, \text{T}'$ square feet (approximately 11,781 sq. feet)

We could use variables to describe the sides... But, for ease, we'll assign easy numbers...

SOLUTIONS

4

Let each side of the large hexagon be 8 units

Since each side is bisected by the inner hexagon, the lengths are 4 and 4



since the ratio of the sides is

$$4\sqrt{3}:8$$

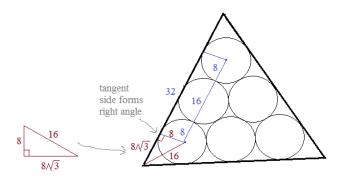
So, each side of outer hexagon is 8 and, each side of inner hexagon is $4\sqrt{3}$

the ratio of the areas is

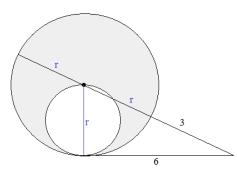
23) Each of these 6 inscribed/tangent circles are congruent with radius 8.

What is the perimeter of the triangle?





24) Can you find the shaded area?



Using power theorem:

$$6 \times 6 = 3 \times (3 + r + r)$$

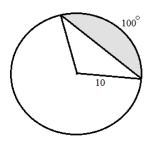
$$12 = 2r + 3$$

$$r = 4.5$$

So, r = 4.5 is the radius of the big circle..

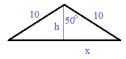
And, 2.25 is the radius of the little circle..

25) What is the area of the shaded segment?



Area of full sector:
$$100 \cdot \frac{100}{360} = 87.27$$
 (approx)

Area of triangle:



Using trigonometry...

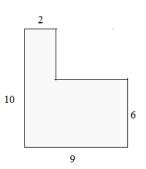
$$cos(50) = \frac{h}{10}$$
 $h = 6.43$
 $sin(50) = \frac{x}{10}$ $x = 7.66$

Area =
$$\frac{1}{2}$$
 (15.32)(6.43) = 49.25

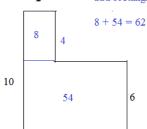
87.27 + 49.25 = 38 (approx)

mathplane.com

1)

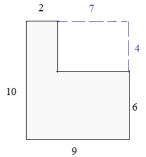


2



9

add rectangles



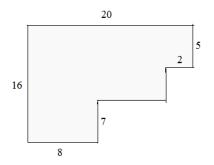
entire rectangle: 90

cut out part: 28

remaining area: 62

62 sq. units

2)



8 10 90 16

128

8

cut into rectangles

label sides

10 5

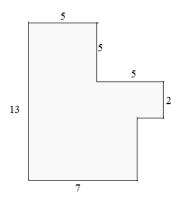
2

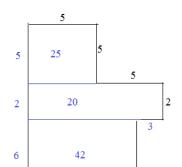
10

calculate rectangle areas

add...
$$128 + 90 + 10 = 228$$
 sq. units

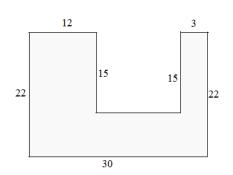
3)

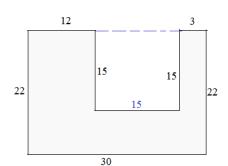




$$25 + 20 + 42 = 87 \text{ sq. units}$$

4)



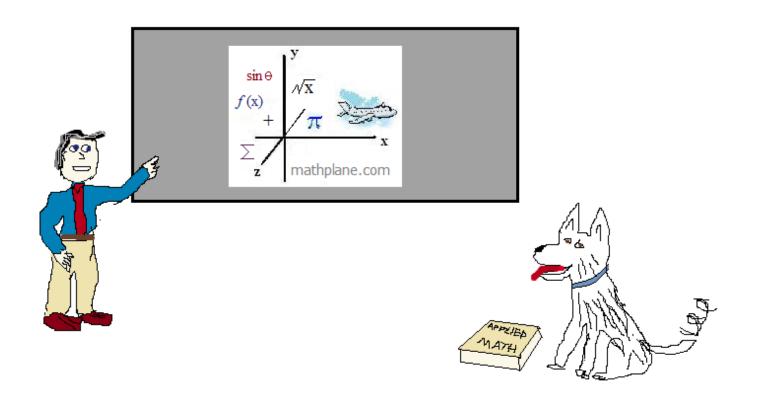


entire rectangle: $22 \times 30 = 660$ cut out square: $15 \times 15 = 225$ area of shape:

$$660 - 225 = 435 \text{ sq units}$$

Thanks for visiting. (Hope it helped!)

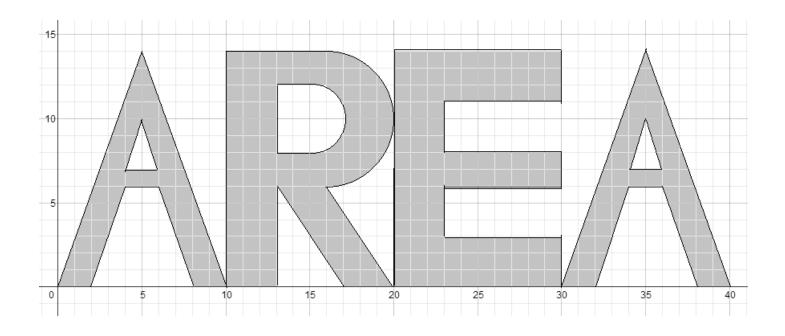
If you have questions, suggestions, or requests, let us know. Cheers.



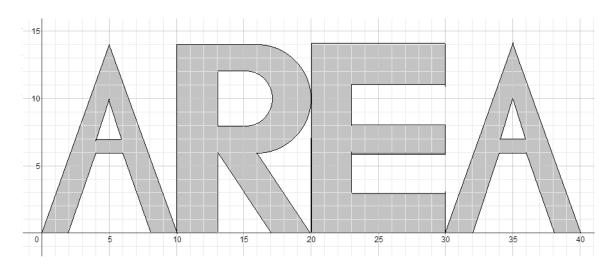
Also, Mathplane Express for mobile at mathplane.ORG

And, we're at TES and TeachersPayTeachers.com

ONE MORE QUESTION:



What is the measure of the shaded AREA?



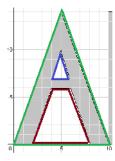
SOLUTION

What is the measure of the shaded AREA?

Area of each "A":

Entire isosceles triangle - little triangle - trapezoid = Area of A

$$\frac{1}{2}$$
 (10 x 14) - $\frac{1}{2}$ (2 x 3) - $\frac{1}{2}$ (6 + 2)(6) = 43

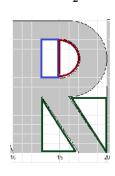


Area of the "R":

Area of bottom part:

Entire rectangle - right triangle - upside down right triangle =

$$(10 \times 6)$$
 $-\frac{1}{2} (4 \times 6)$ $-\frac{1}{2} (6 \times 4) = 36$



Total area of the "R":



Area of top part:

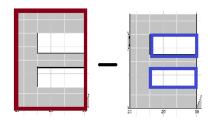
Entire "rectangle/semicircle" - Interior "rectangle/semicircle"

$$(8 \times 6) + \frac{1}{2} \text{Tr} (4)^{2} - \left((2 \times 4) + \frac{1}{2} \text{Tr} (2)^{2} \right) = 48 + 8 \text{Tr} - 8 - 2 \text{Tr} = 40 + 6 \text{Tr}$$

Area of the "E":

Entire rectangle - cut out rectangles = Area of E

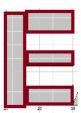
$$(14 \times 10) - 2(3 \times 7) = 98$$



OR, add the parts...

Bottom + Middle + Top + Left = Total

$$(3 \times 7) + (2 \times 7) + (3 \times 7) + (14 \times 3) = 98$$



TOTAL AREA: A R E A 43 + (76 + 6 11) + 98 + 43

260 + 6 ∏ or approximately 278.85